

I HE 2012

# Density dependent groundwater flow

## *salt water intrusion (and heat transport)*

Gualbert Oude Essink

Lecture set-up:

- PowerPoint sheets
- Practicals

<http://freshsalt.deltares.nl>



Deltares - Geological Survey of the Netherlands  
Unit Subsurface and Groundwater Systems  
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14-28-29 June 2012

Introduction

## Curriculum Vitae

- Delft University of Technology, Civil Engineering: till 1997  
Ph.D.-thesis: Impact of sea level rise on groundwater flow regimes
- Utrecht University, Earth Sciences: till 2002  
Lectures in groundwater modelling and transport processes  
Variable-density groundwater flow  
Salt water intrusion and heat transport
- Free University of Amsterdam, Earth Sciences: till 2004  
EC-project CRYSTECHSALIN  
Crystallisation processes in porous media
- Deltares - Geological Survey of the Netherlands  
Salinisation processes in Dutch coastal aquifers  
Effect climate change on freshwater resources  
Water management effect studies

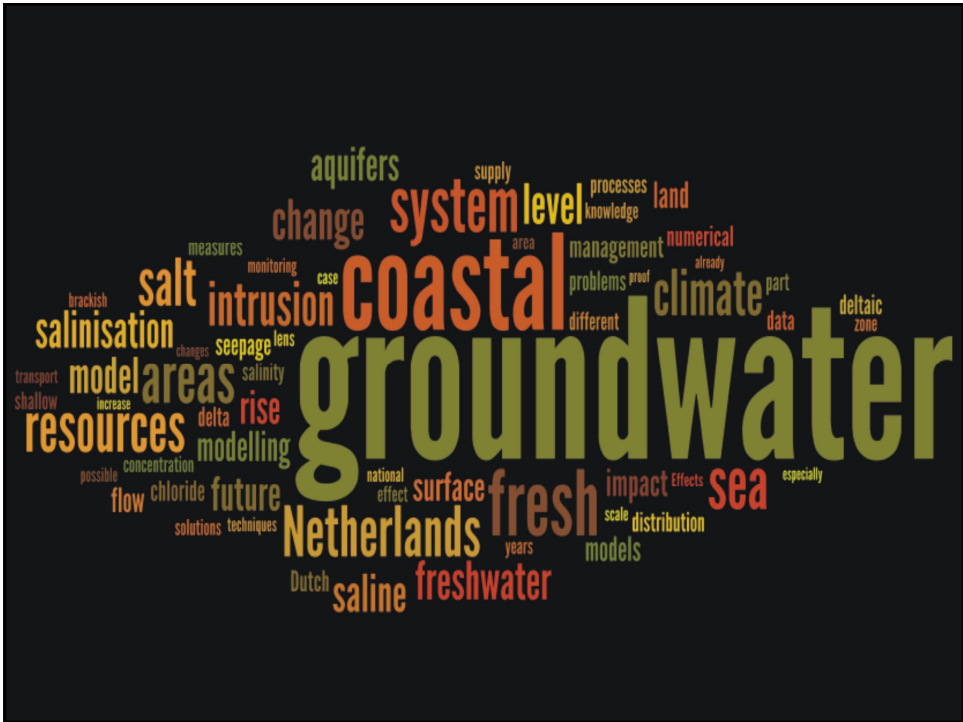
Deltares: [gualbert.oudeessink@deltares.nl](mailto:gualbert.oudeessink@deltares.nl)

## Topics of density driven groundwater flow

1. Introduction
  - water on earth
  - salt water intrusion
  - freshwater head
2. Interface between fresh and saline groundwater
  - analytical formulae
  - upconing example
3. Numerical modelling
  - mathematical background
  - MOCDENS3D, MODFLOW
  - Benchmark problems: Henry, Elder, Hydrocoin, etc.
4. Case-studies
  - hypothetical cases
  - real cases in the Dutch coastal zone

## Topics of density driven groundwater flow

1. Introduction salt water intrusion
  - water on earth
  - concept of salt water intrusion
  - freshwater head
  - compensating measurements
2. **Badon Ghyben-Herzberg**
  - interface between fresh and saline groundwater
  - analytical formulations
  - upconing example
3. **Freshwater head**
  - hydrostatic pressure
4. **Numerical modelling**
  - mathematical background
  - MOCDENS3D, MODFLOW
  - benchmark problems: Henry, Elder, Hydrocoin, etc.
5. **Case studies**
  - hypothetical cases
  - real 3D cases (a.o in the Dutch coastal zone)



# Groundwater in the Coastal Zone

<http://zoetzout.deltares.nl>  
<http://freshsalt.deltares.nl>



Perry de Louw



Joost Delsman



Pieter Pauw



Esther van Baaren



Jarno Verkaik



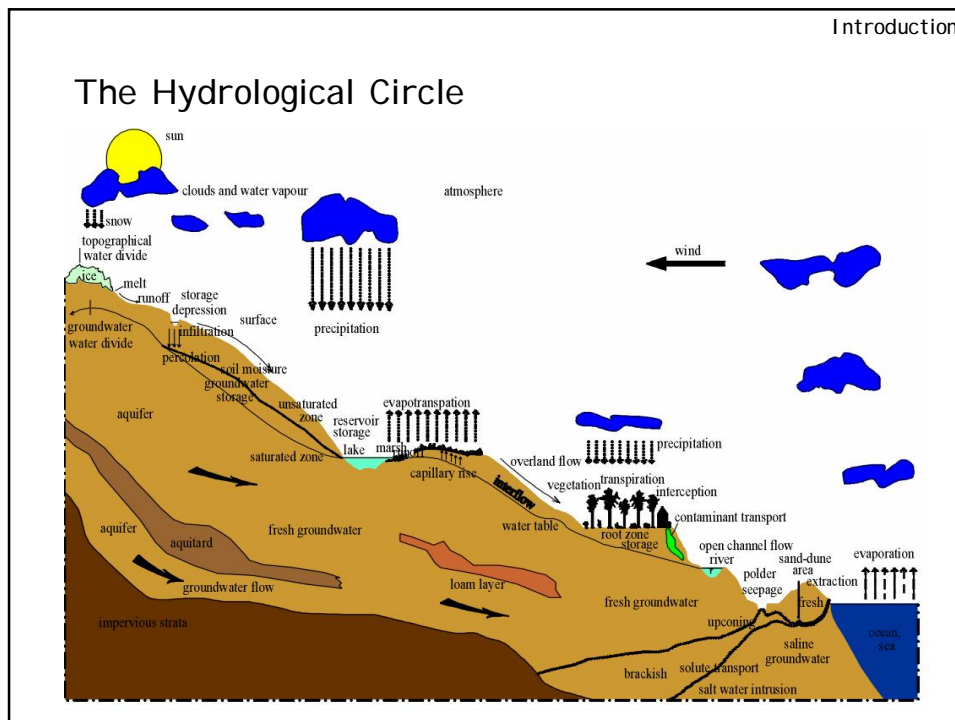
Marta Faneca



Gualbert Oude Essink

## Leading in research on groundwater in the coastal zone

- 15 years experience in variable-density dependent groundwater flow and coupled solute transport in the coastal zone
- Incorporating monitoring campaigns results in numerical modeling tools
- Initiating (inter)national research on new fresh-saline phenomena: salty seepage boils and shallow freshwater lenses in saline environments
- Broad knowledge on creating 3D initial chloride distribution, based on geostatistics and geophysical data (analyses, VES, borehole measurements)
- Quantifying effects of climate change and sea level rise on fresh groundwater resources
- Developing adaptive and mitigative measurements to stop salinization of the coastal groundwater system (e.g. fresh keeper, coastal collectors, freshwater storage underground)

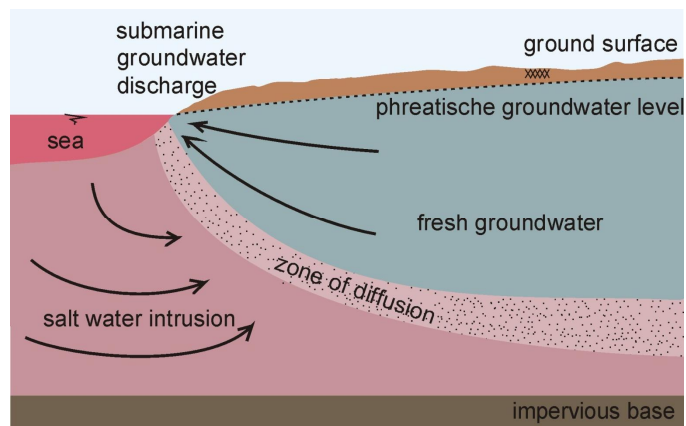


## The Hydrological Cycle

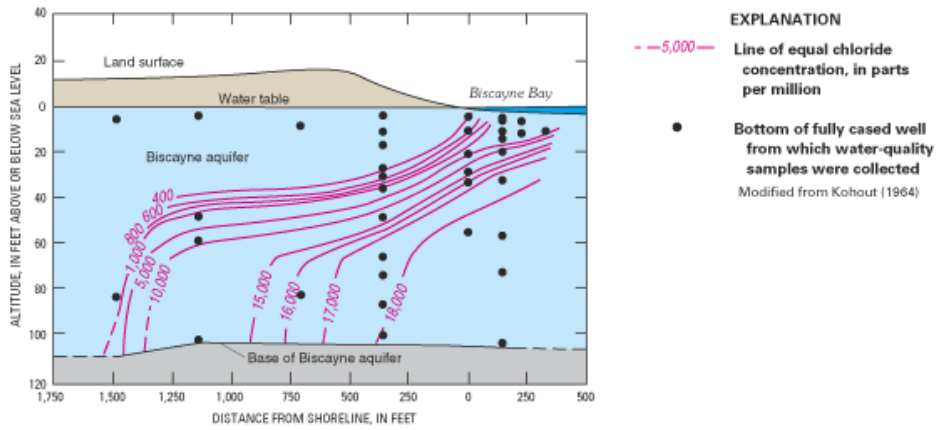


## Definition of salt water intrusion

*Inflow of saline water into an aquifer which contains fresh water*

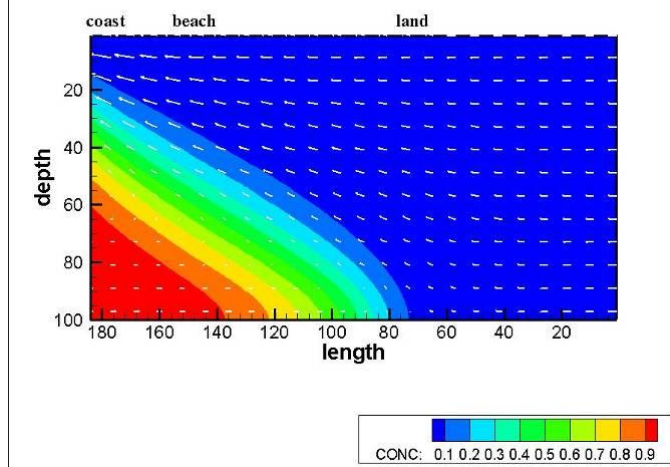


## Biscayne aquifer, Florida USA: Henry's case



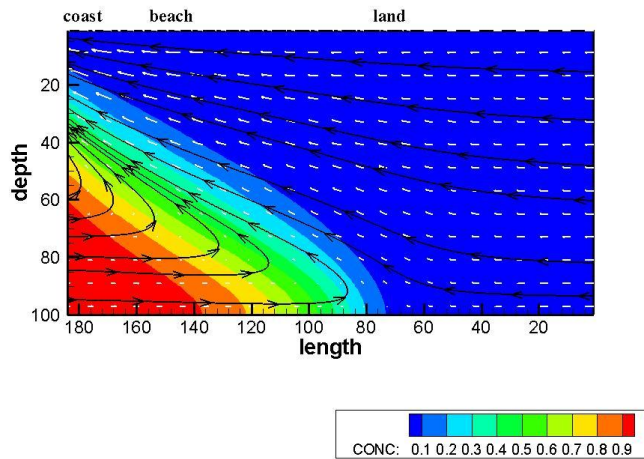
## Definition of salt water intrusion

### Numerical model: Henry's case



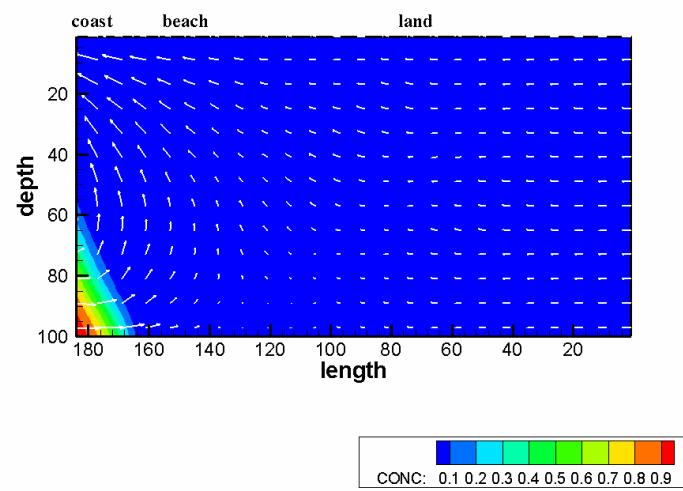
## Definition of salt water intrusion

Numerical model: Henry's case



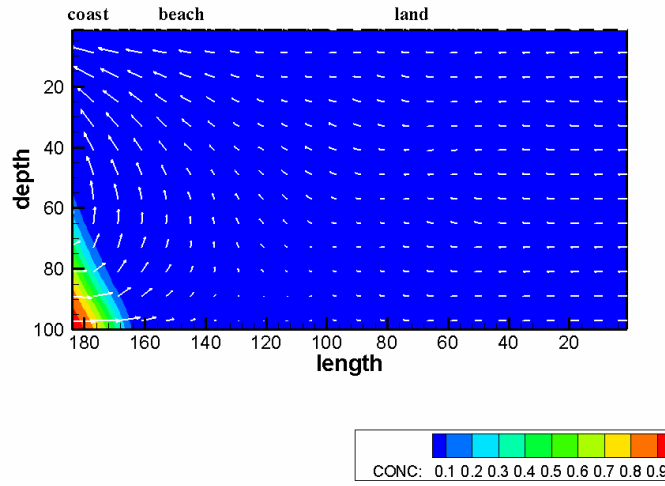
## Sea level rise and salt water intrusion

Effect sea level rise on groundwater system in coastal zone



# Sea level rise and salt water intrusion

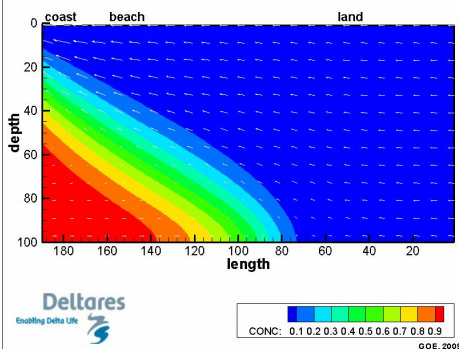
## Effect sea level rise on groundwater system in coastal zone



# Sea level rise and salt water intrusion

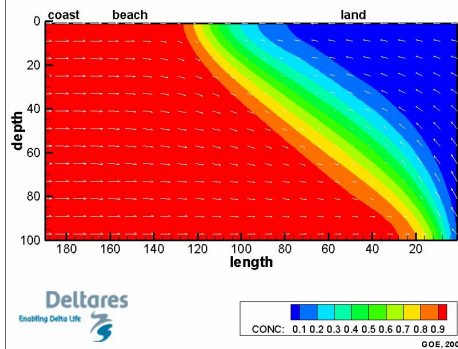
## Impact of sea level rise on a coastal groundwater system:

### a conceptual model of saltwater intrusion



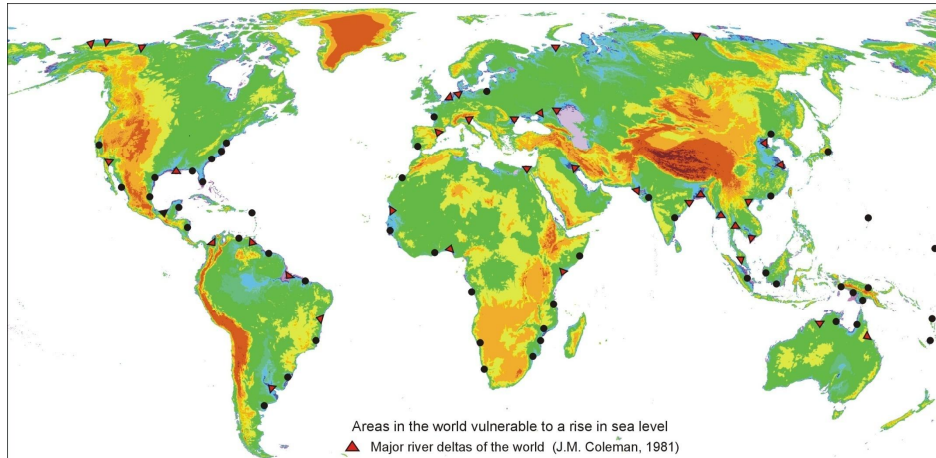
## Impact of sea level rise on a coastal groundwater system:

### a conceptual model of saltwater intrusion





## Areas vulnerable to sea level rise



Introduction

## Water on Earth

Some serious developments:

*"shortage of drinking water will be one of the biggest problems of the 21<sup>st</sup> century"*

*"in 2025, two third of world population will face shortage of water"*

Question:

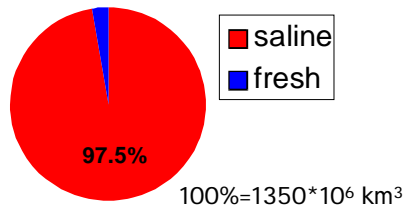
*How much percent of all the water on Earth is fresh?:*

- a. 0.025 %
- b. 0.1 %
- c. 2.5 %
- d. 10 %

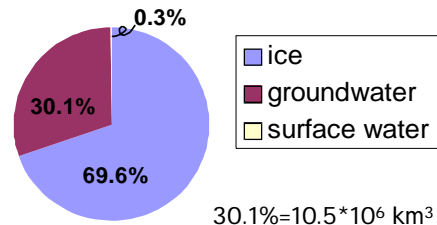
Introduction SWI

## Water on Earth

Total water on Earth



Total fresh water on Earth



Demand for groundwater (now 30%) increases due to:

- increase world population & economical growth
- loss of surface water due to contamination
- great resource: available in large quantities
- still unpolluted (relative to surface water)

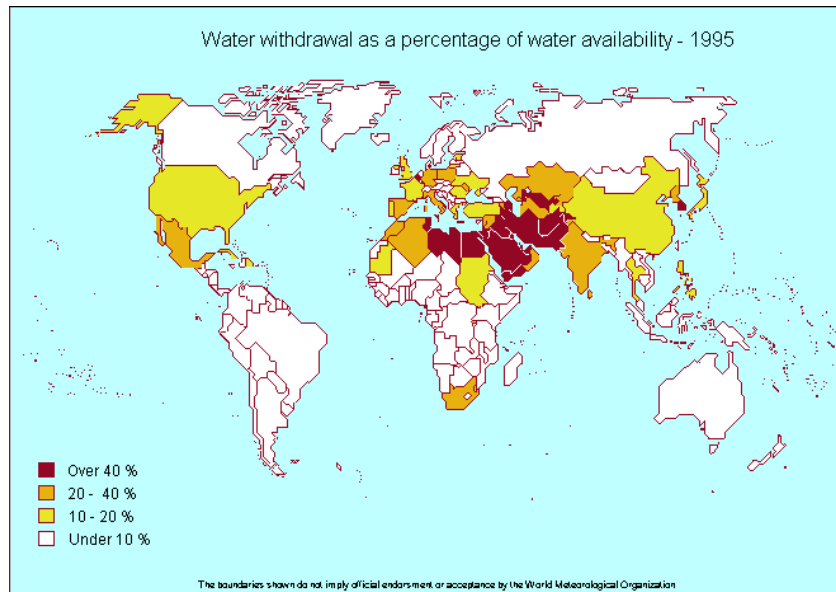
(Source: Cheng, 1998)

### Question:

*Demand fresh water per capita per day in the Netherlands?:*

- 10 litre/day
- 25 litre/day
- 100 litre/day
- 200 litre/day

## Water withdrawal



## Reasons and drawbacks of using groundwater

### Advantage:

- no seasonal effects
- high quality
- low storage costs
- large quantities
- no spatial limitations

### Disadvantage:

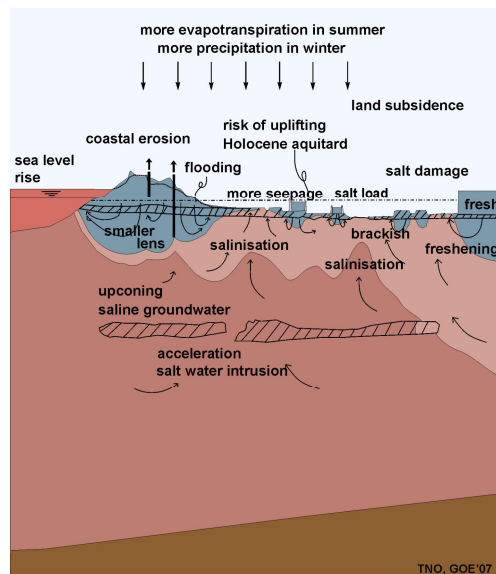
- high extraction costs
- local droughts
- high mineral content
- land subsidence....
- salt water intrusion !

(Source: Cheng, 1998)

### Concept of a coastal area



### Situation in the coastal zone



## Land subsidence

Megacity	Maximum subsidence [m]	Date commenced
Shanghai	2.80	1921
Tokyo	5.00	1930's
Osaka	2.80	1935
Bangkok	1.60	1950's
Tianjin	2.60	1959
Jakarta	0.90	1978
Manila	0.40	1960
Los Angeles	9.00	1930's

Introduction

Salt in water is a problem for different water management sectors:

**-drinking water:**

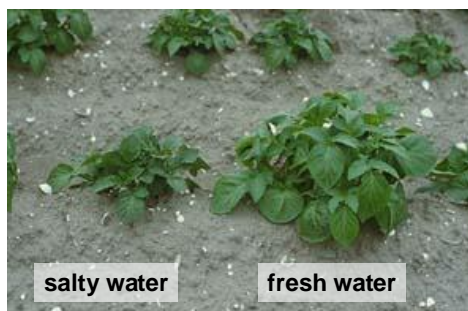
- taste (100-300 mg Cl<sup>-</sup>/l)
- long term health effect
- norm: EC& WHO=150 mg Cl<sup>-</sup>/l (live stock=1500 mg Cl<sup>-</sup>/l)

**-industry:**

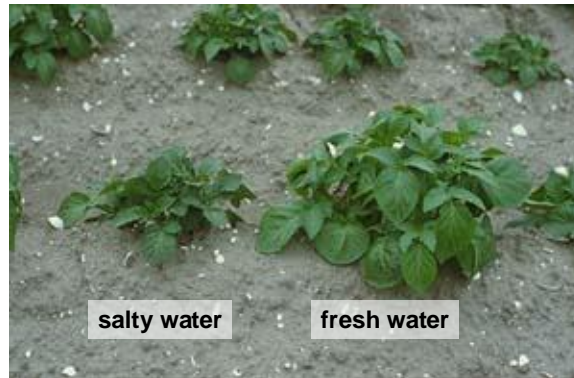
- corrosion pipes
- preparation food

**-irrigation/agriculture:**

- production crops
- salt damage



## Effects salinisation: salt damage



Source: Proefstation voor de Akkerbouw en Groenteteelt, Lelystad

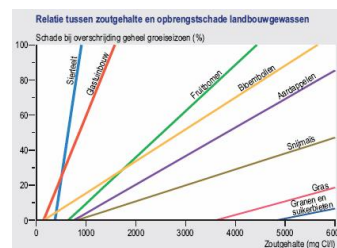
## Salt damage to crops

### Important parameters:

- Chloride concentration in the root zone
- Land use
- Sensitivity crops

Land use	Threshold value root zone (mg Cl <sup>-</sup> /l)	Gradient root zone (-)
Grass	3606	0.0078
Potatoes	756	0.0163
Beet	4831	0.0057
Grains	4831	0.0058
Horticulture	1337	0.0141
Orchard (trees)	642	0.0264
Bulb	153	0.0182

Source: Roest et al., 2003 en Haskoning

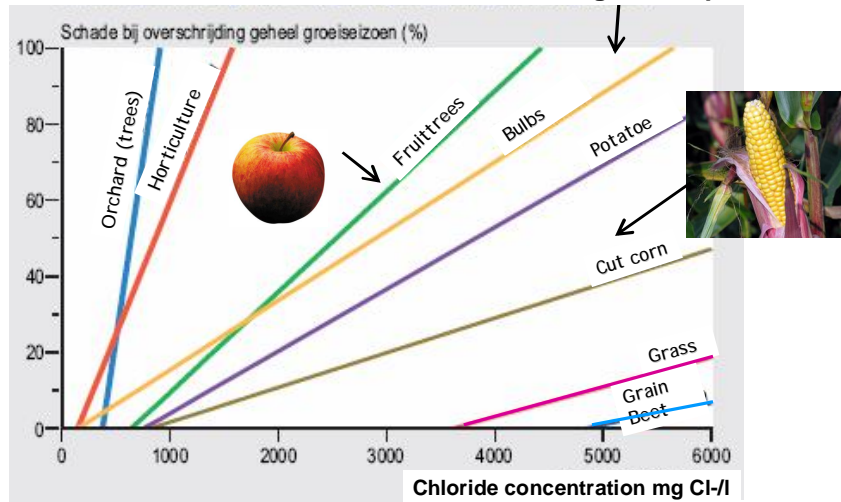


Source: MNP, 2005

# Salt damage to crops



Relation between salt concentration and damage to crops

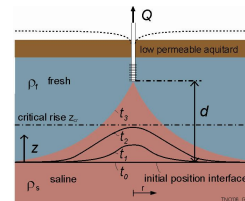
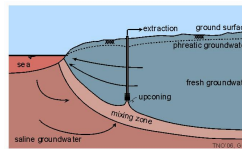
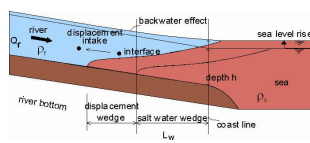


	Soil moisture		Irrigation water	
	Limit	Gradient	Limit	Gradient
<b>Crop</b>	<b>mg/l Cl</b>	<b>%/mg/l Cl</b>	<b>mg/l Cl</b>	<b>%/mg/l Cl</b>
Potatoe	756	0.0163	202	0.0610
Grass	3606	0.0078	962	0.0294
Sugar beat	4831	0.0057	1288	0.0212
Cut Corn	815	0.0091	217	0.0343
Grains	4831	0.0058	1288	0.0218
Fruit trees	642	0.0264	171	0.0991
Orchard (trees)	378	0.1890	101	0.7086
Vegetables	917	0.0158	245	0.0591
Horticulture	1337	0.0141	356	0.0527
Bulbs	153	0.0182	41	0.0683



## Why is salinisation a pressing problem?

- 50% of world population lives <60 km from coastline
- economic and tourist activities increase
- enormous increase in extraction
- irreversible process
- increase saltwater intrusion problem world-wide:
  - upconing
  - salt water wedge
  - decrease outflow  $q_0$
- climate change:
  - sea level rise
  - natural groundwater recharge



## Origin of saline groundwater in the subsoil

### Geological causes:

- marine deposits during geological times
- trans- and regressions in coastal areas (deltas)
- salt/brine dome

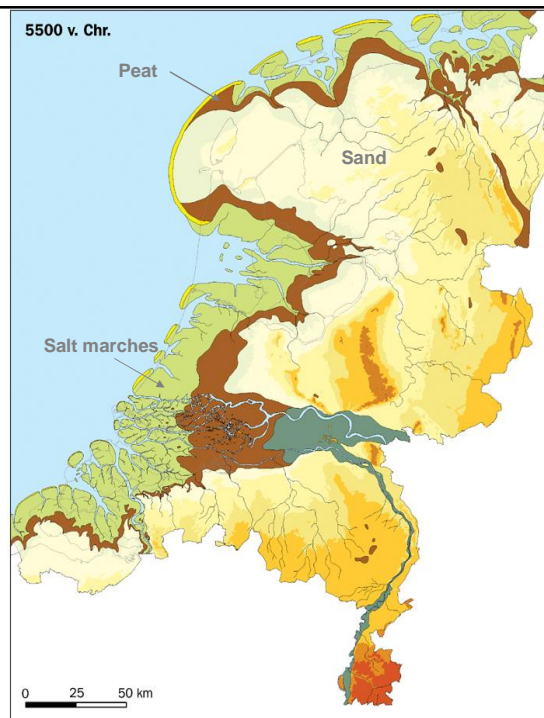
### Anthropogenic causes:

- agriculture/irrigation (salt damage Middle East & Australia)
- upconing under extraction wells throughout the world
- upconing under low-lying areas (e.g. Dutch polders)

## The Holocene transgressions

Major impact on present regional brackish groundwater systems

7500 BP



Introduction

### Processes that accelerate salt water intrusion:

- Sea level rise
- Land subsidence
- Human activities

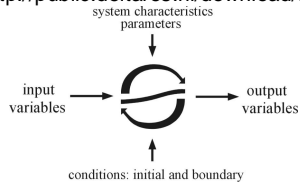
### Threats for:

- drinking water supply in dunes:
  - upconing of saline groundwater
  - decrease of fresh groundwater resources
  - recharge areas reduction
- agriculture:
  - salt damage to crops: salt load and seepage
- water management low-lying areas:
  - flushing water channels
- ecology

# Lecture notes and ppt on freshsalt.deltares.nl

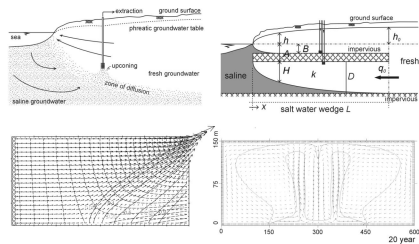
## 1. Density dependent groundwater flow

<http://public.deltares.nl/download/attachments/32113595/gwm1.pdf?version=1>



## 2. Groundwater modelling

<http://public.deltares.nl/download/attachments/32113595/gwm2.pdf?version=1>



<http://public.deltares.nl/display/FRESHSALT/Literature>

### Salt Water Intrusion Meeting (SWIM)

Home History Next meeting Proceedings Links About this site

#### Welcome to the homepage of the Salt Water Intrusion Meeting



The Salt Water Intrusion Meeting (SWIM) has been held in different European countries on a biennial basis since 1968 with an increasing number and diversity of participants. In spite of its name, SWIM is not solely restricted to seawater intrusion problems. The meetings are very successful in bringing together people who are interested in saline groundwater issues: well-known specialists, water managers and students.

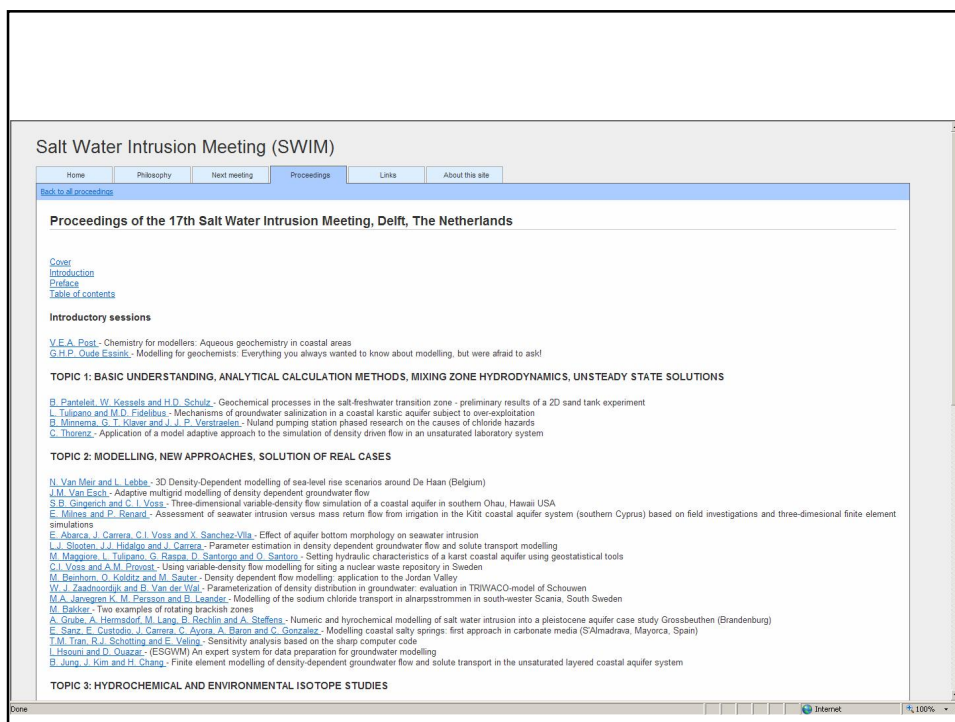
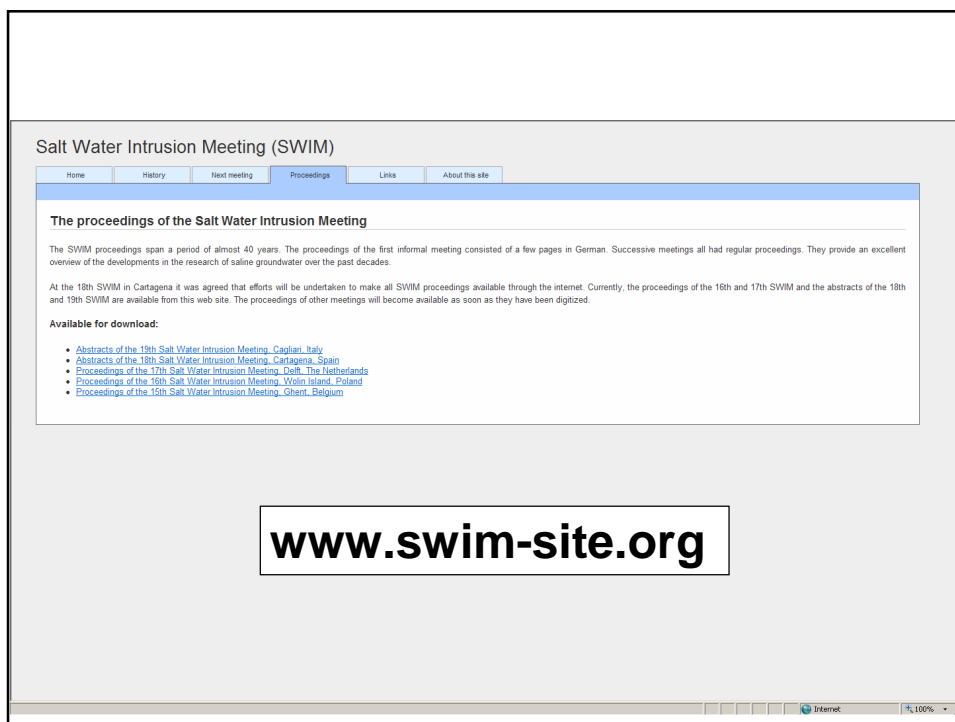
The growing interest among scientists and water managers reflects the increasing relevance of managing saline groundwaters all around the world, especially in densely populated coastal areas. Problems include:

- over-exploitation of water resources, especially in arid and semi-arid areas
- increased demand due to economic development and population growth
- quality deterioration of the available surface water resources
- insufficient knowledge of the aquifer architecture and processes to design sound management
- climate change and sea level rise

#### Philosophy of SWIM

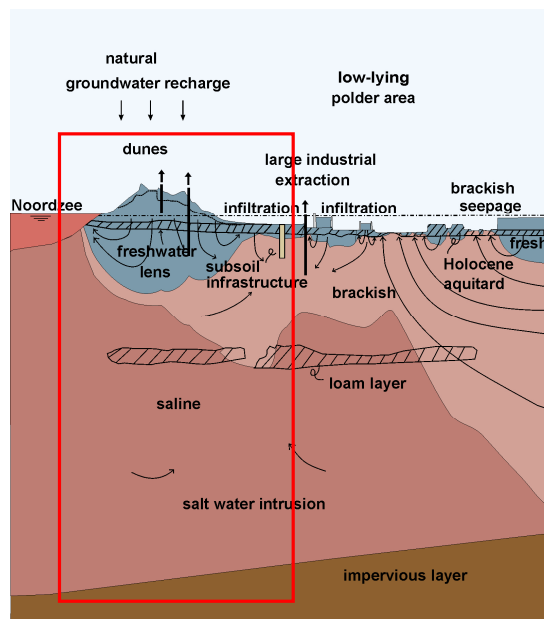
The SWIM aims to bring together specialists, exchange ideas and discuss results on saline groundwater problems in a friendly and relaxed atmosphere. The meetings have always maintained their informal character with contributions from well-known scientists mixed with young people giving their first presentation. The ambience during the meetings of the last 34 years can be characterized as based on personal contacts and good discussions. There is no SWIM association or so, with memberships and fees; SWIM is carried by persons and institutions in various countries, which have confidence in it and see the usefulness of these meetings.

[www.swim-site.org](http://www.swim-site.org)



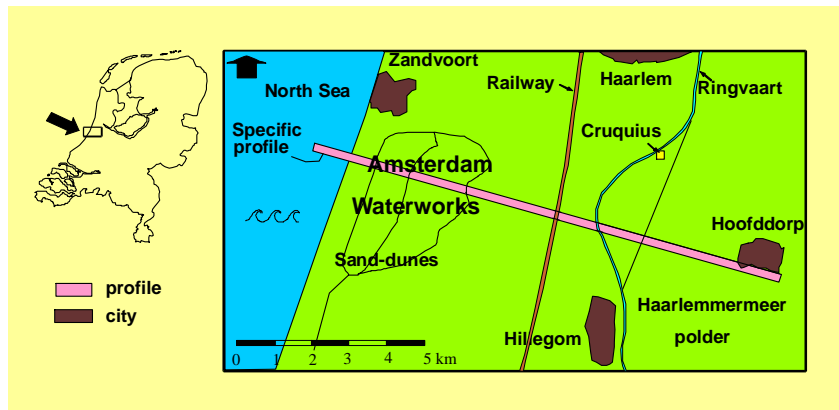
My first density dependent groundwater flow and solute transport model in 1990!

### Saltwater intrusion in the Netherlands



## Saltwater intrusion in the Dutch coastal zone

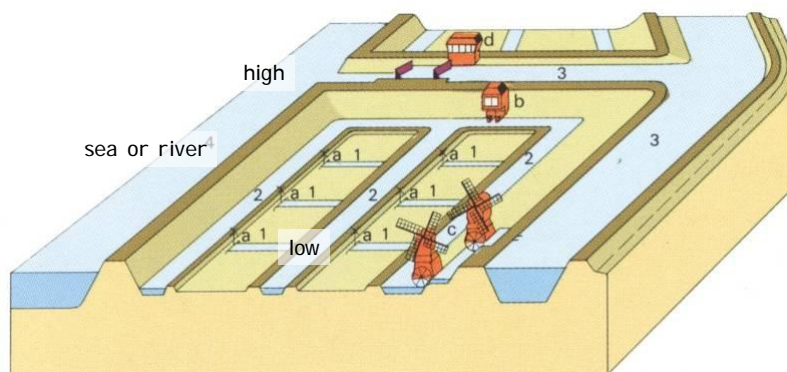
Position profile through Amsterdam Waterworks, Rijnland polders and Haarlemmermeer polder



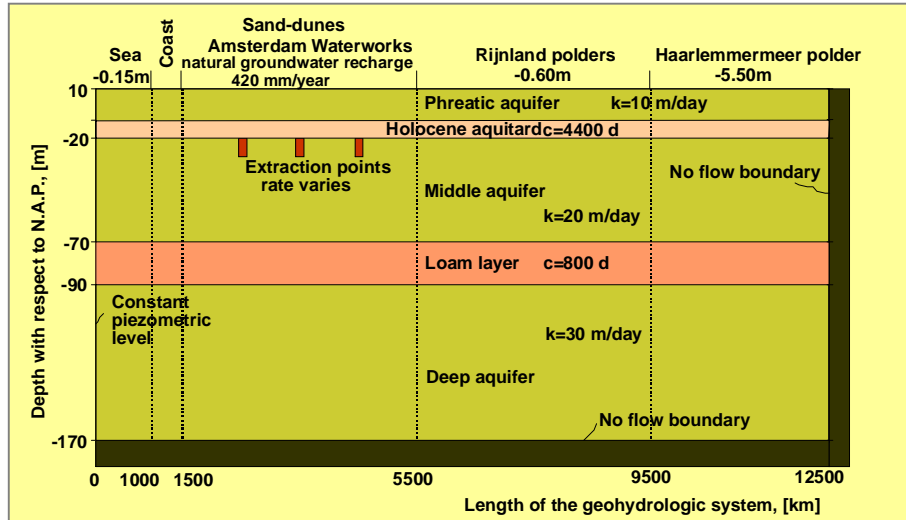
## The polder system

A polder is:

*a sophisticated system to drain the excess of water in a low-lying area*

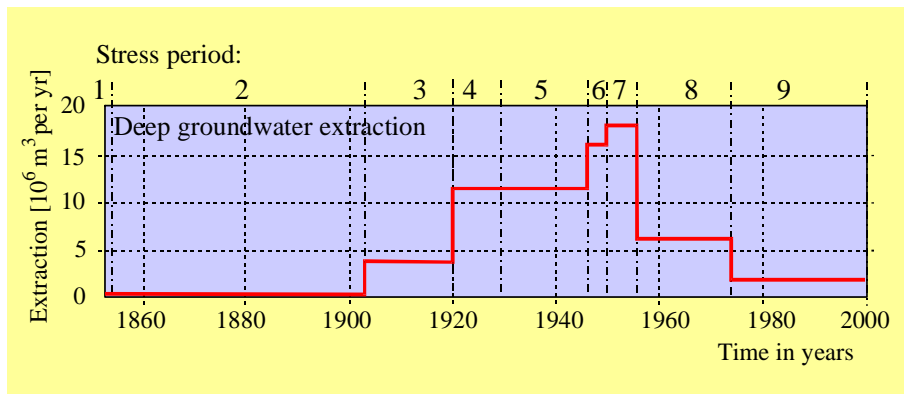


## Geometry, subsoil parameters, boundary conditions

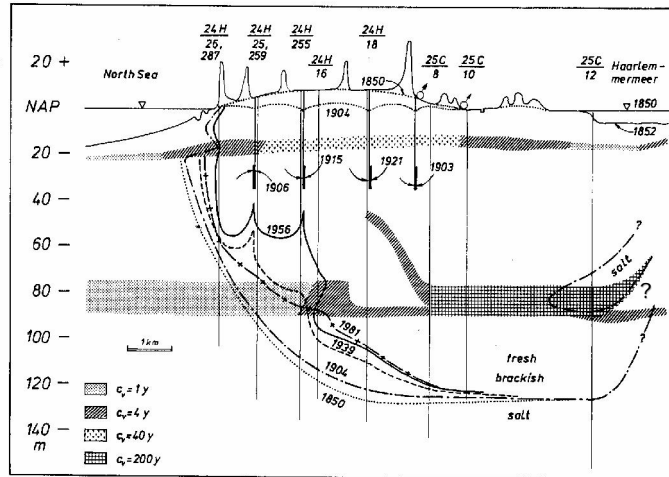
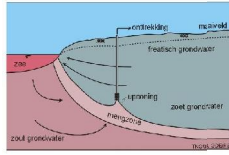


## Saltwater intrusion in the Dutch coastal zone

Groundwater extractions out of the middle aquifer in the sand-dune area of Amsterdam Waterworks

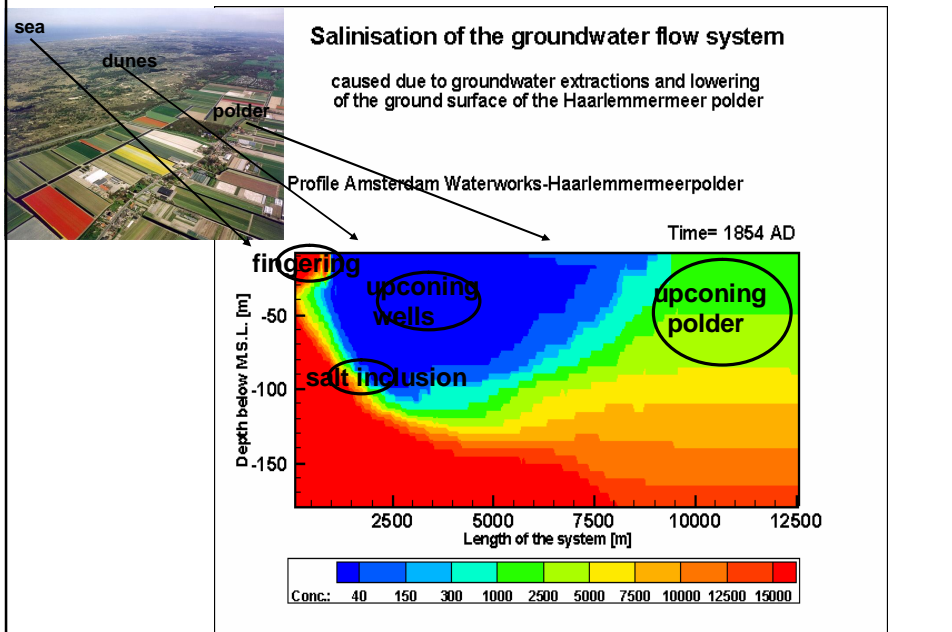


## Upconing of brackish-saline groundwater



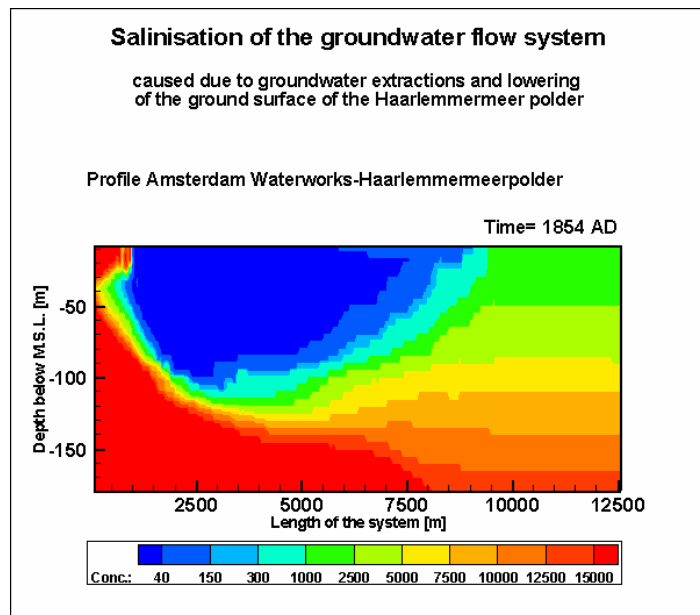
Stuyfzand, 1993

## Saltwater intrusion in the Dutch coastal zone





## Saltwater intrusion in the Dutch coastal zone



## Compensating measures

### Possible solutions to stop salt water intrusion:

- Restriction of groundwater extractions through permits
- Co-operation between authorities and water users
- Desalinisation of saline water
- Technical countermeasures of salt water intrusion
  - six examples

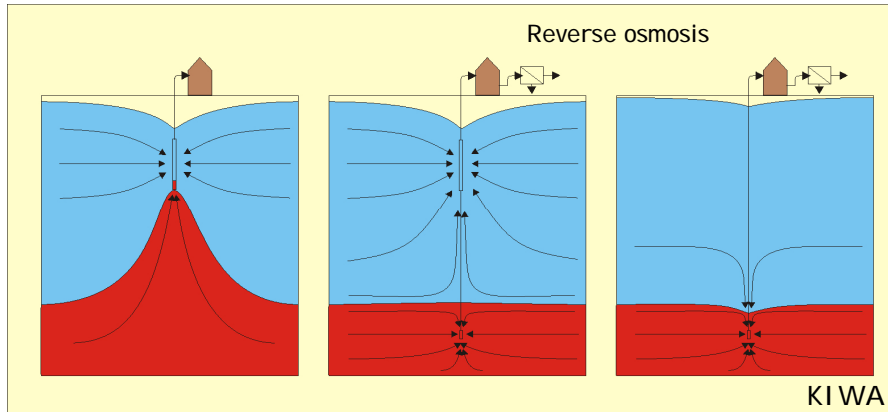
### Tools to understand salt water intrusion:

- Monitoring of salinities and piezometric levels
- Numerical modelling of salt water intrusion

### Measures to compensate salt water intrusion

- 'The Fresh Holder'
- Extraction of saline/brackish groundwater
- Infiltration of fresh surface water
- Modifying pumping rates
- Land reclamation in front of the coast
- Creating physical barriers (crystallisation or biosealing)

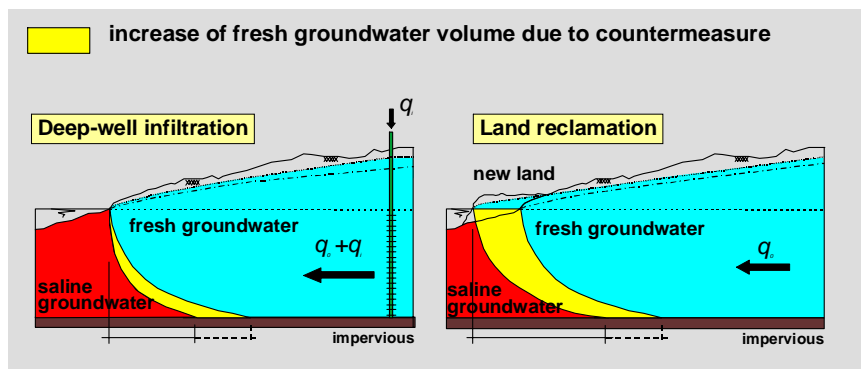
## Solution: The Fresh Holder



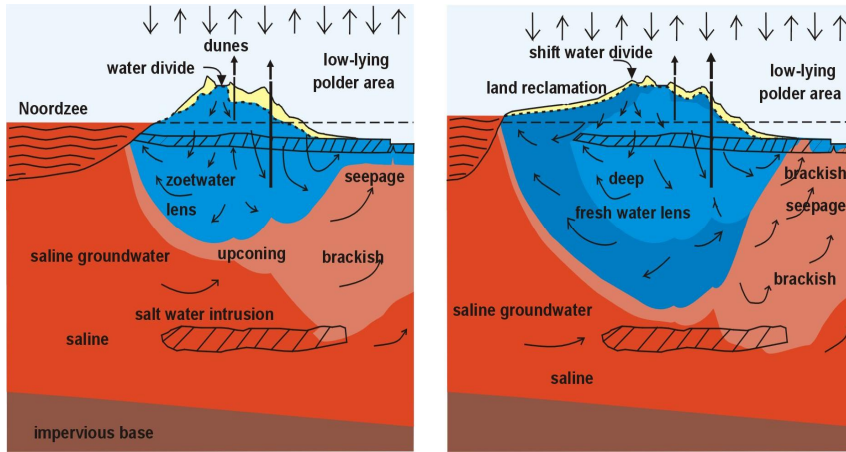
Upconing can be prevented by the extraction of brackish groundwater

This brackish groundwater can be transformed to water of agricultural water quality by using the membrane filtration technique

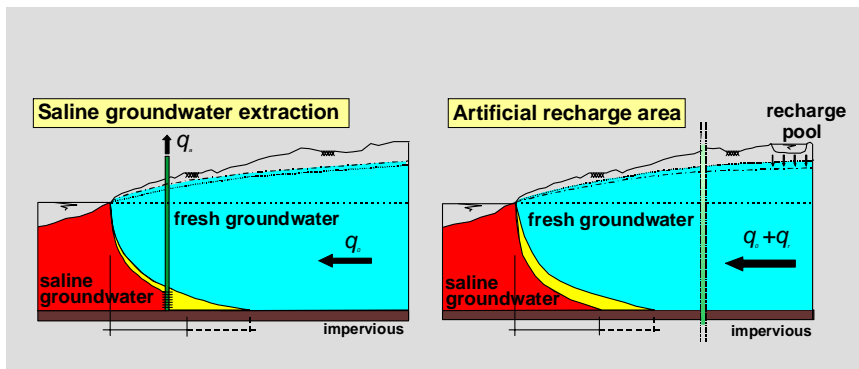
## Countermeasures of salt water intrusion (1)



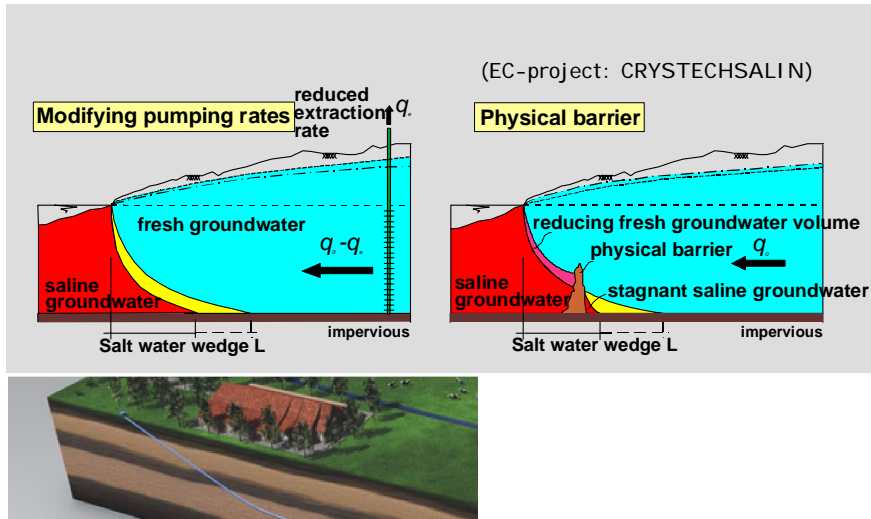
### Countermeasures of salt water intrusion (1)



### Countermeasures of salt water intrusion (2)



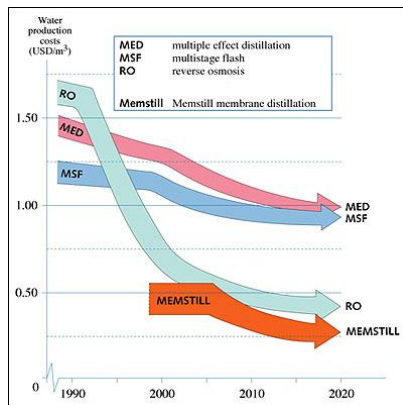
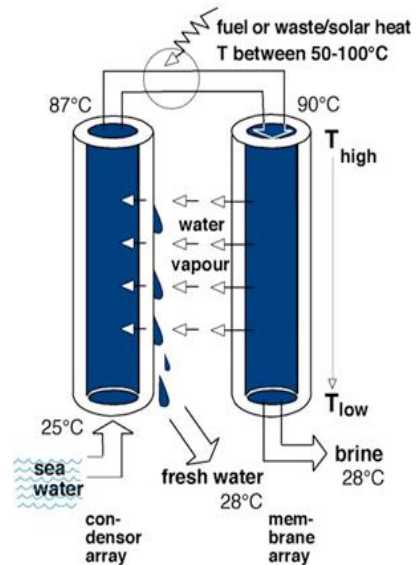
### Countermeasures of salt water intrusion (3)



### Memstill - technology

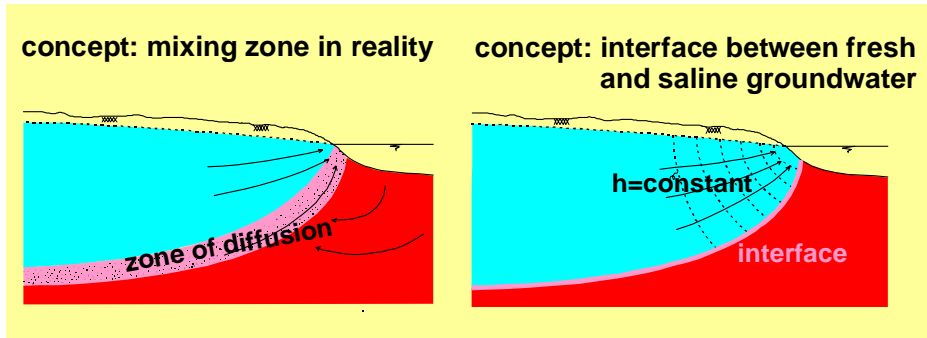
- new, cheap technique
- membrane distillation technique
- no primary energy
- test sites in Rotterdam and Singapore

#### Principle of Memstill-process



## Badon Ghyben-Herzberg principle (I)

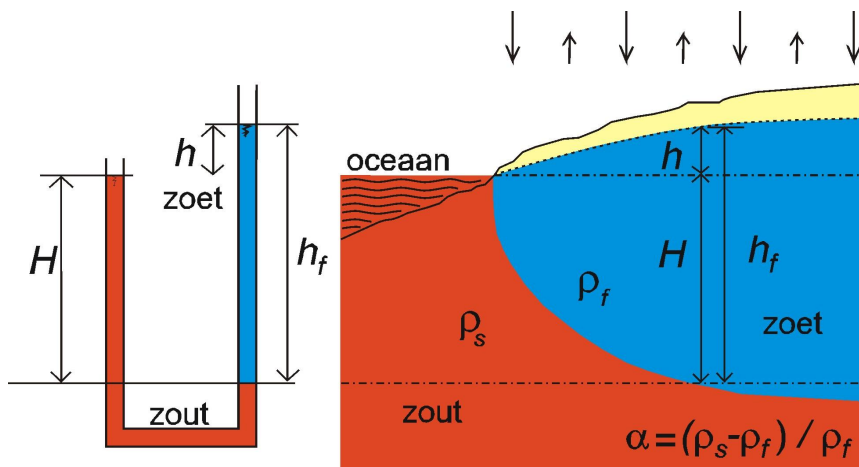
Difference between reality and Badon Ghyben-Herzberg approximation

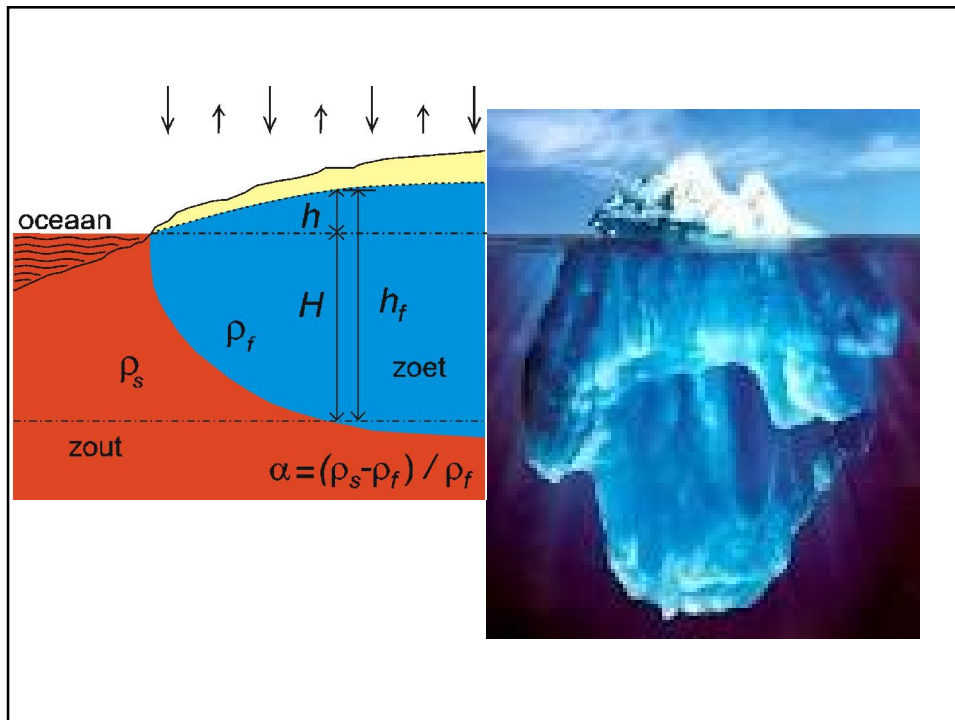


## Badon Ghyben-Herzberg principle

The principle suggests an interface between fresh and saline groundwater

Analogy: iceberg & saline ocean and granite tectonic plate & basalt base



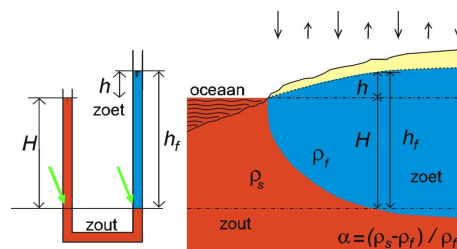


**pressure saline groundwater = pressure fresh groundwater**

$$\rho_s H g = \rho_f (H + h) g$$

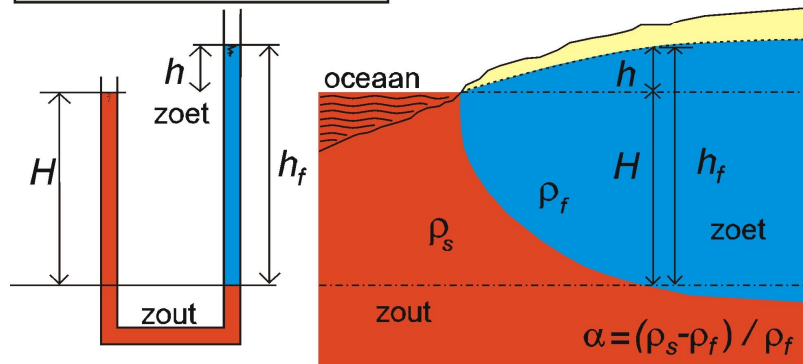
$$h = \frac{\rho_s - \rho_f}{\rho_f} H$$

$$h = \alpha H$$



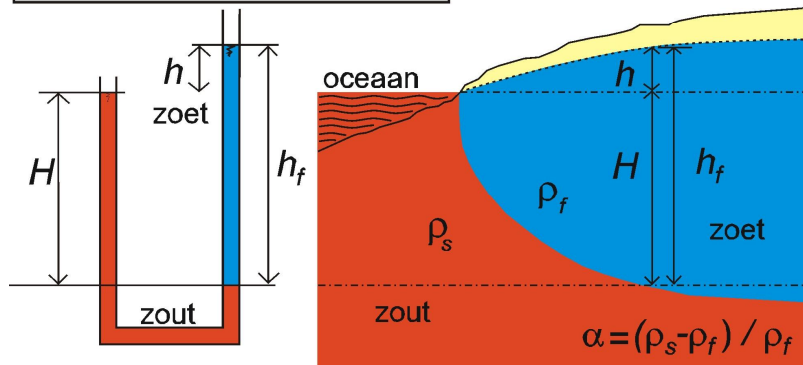
$$h = \alpha H$$

$h = \alpha H$   
 in ocean water  $\alpha = 0.025$   
 $h = 1 \text{ m}$ ,  $H = 40 \text{ m}$



$$h = \alpha H$$

$h = \alpha H$   
 Mediterranean Sea  $\alpha = 0.028$   
 $h = 1 \text{ m}$ ,  $H = 35.7 \text{ m}$





## Badon Ghyben-Herzberg principle

- gives analytical solutions (see later and lectures)
- educational
  
- interface is a simple approximation
- dispersion zone <10m
- relative simple geometries

## Badon Ghyben-Herzberg principle

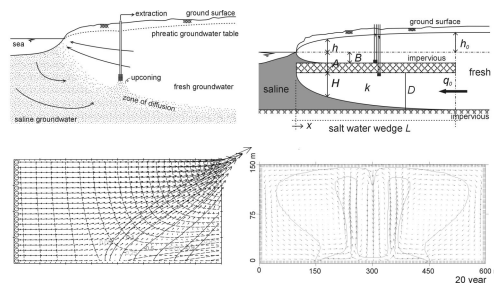
What is the case then  $h \neq \alpha H$ ?

1. still dynamic situation
2. occurrence resistance layer
3. natural groundwater recharge not constant
4. relative density difference  $\alpha$  is not ok
5. occurrence shallow bedrock
6. groundwater extractions

# Analytical solutions

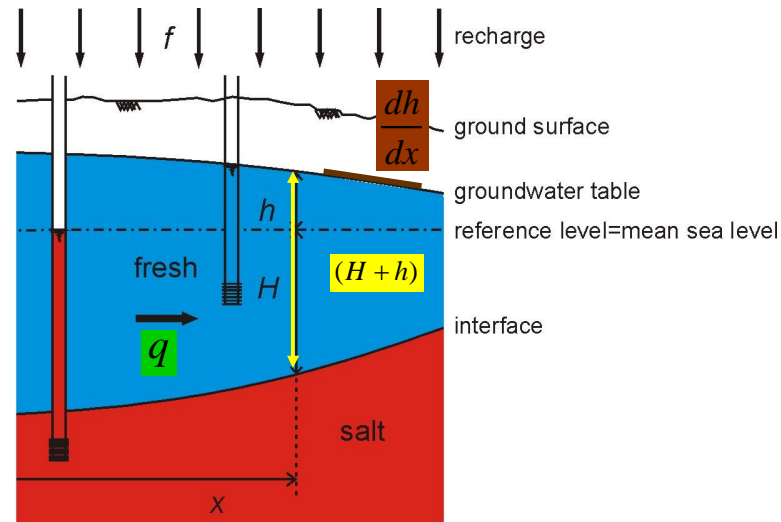
## Analytical solutions

See lecture notes *Density dependent groundwater flow* (p. 29-48)



<http://public.deltares.nl/display/FRESHSALT/Literature>

## Unconfined aquifer (1D situation)



## Unconfined aquifer (1D situation)

(I) Darcy  $q = -k(H + h) \frac{dh}{dx}$

(II) Continuity  $dq = f dx$

(III) BGH  $h = \alpha H$

## Unconfined aquifer (1D situation)

$$dq = f dx \quad \begin{array}{l} \text{integration} \\ \text{gives} \end{array} \quad q = fx + C1$$

$$-k(H+h) \frac{dh}{dx} = fx + C1$$

$$h = \alpha H \rightarrow -k(H + \alpha H) \alpha \frac{dH}{dx} = fx + C1$$

$$H dH = -\frac{fx + C1}{k\alpha(1+\alpha)} dx$$

## Unconfined aquifer (1D situation)

$$H dH = -\frac{fx + C1}{k\alpha(1+\alpha)} dx$$

integration  
gives

$$\frac{1}{2} H^2 = \frac{-\frac{1}{2} fx^2 - C1x + C2}{k\alpha(1+\alpha)}$$

$$H = \sqrt{\frac{-\frac{1}{2} fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}}$$

## Unconfined aquifer (1D situation)

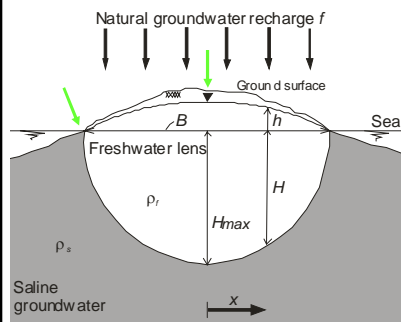
$$H = \sqrt{\frac{-\frac{1}{2}fx^2 - 2C_1x + 2C_2}{k\alpha(1+\alpha)}}$$

$$h = \alpha H$$

$$q = fx + C_1$$

## Example 1: Elongated island

$$H = \sqrt{\frac{-\frac{1}{2}fx^2 - C_1x + C_2}{k\alpha(1+\alpha)}}$$

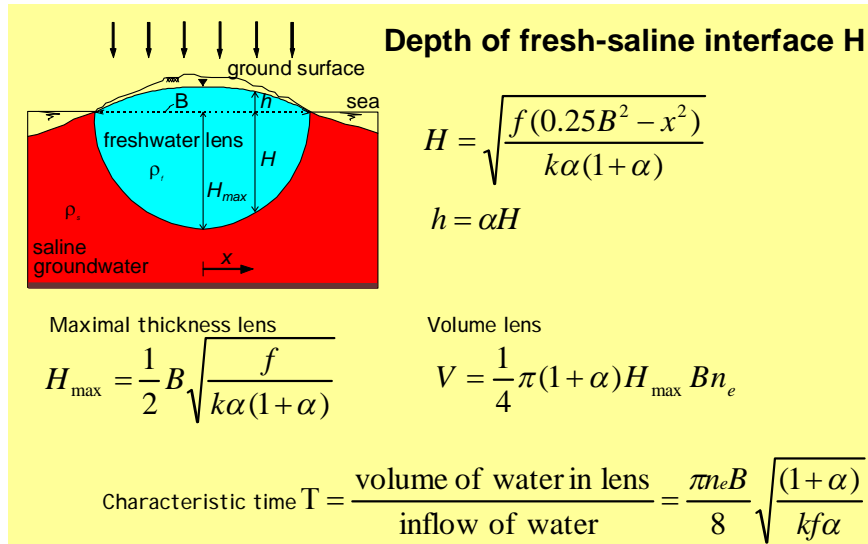


Boundary conditions

$$x = 0 : q = 0 \rightarrow C_1 = 0$$

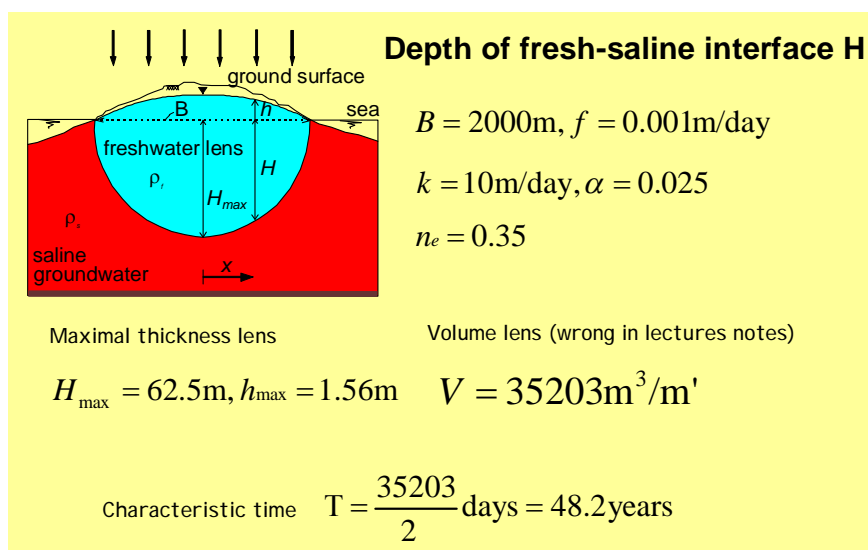
$$x = 0.5B : H = 0 \rightarrow C_2 = fB^2 / 8$$

## Example of analytical solutions (I)



Lecture notes p. 32

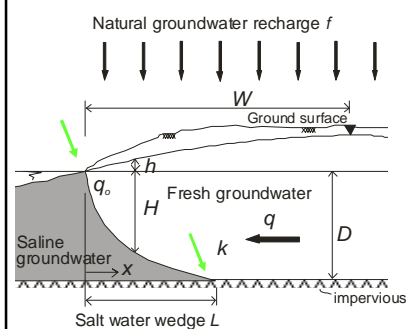
## Example of analytical solutions (I)



Lecture notes p. 32

## Example 2: salt water wedge

$$H = \sqrt{\frac{-\frac{1}{2}fx^2 - C1x + C2}{k\alpha(1+\alpha)}}$$



Boundary conditions

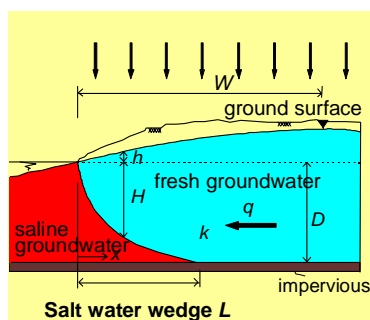
$$x = 0 : q = q_0 \rightarrow q_0 = -fW \rightarrow C1 = q_0$$

$$x = 0 : H = 0 \rightarrow C2 = 0$$

Length of salt water wedge

$$x = L : H = D$$

## Example of analytical solutions (II)



$$L = -\frac{q_0}{f} - \sqrt{-\left(\frac{q_0}{f}\right)^2 - \frac{k}{f}D^2(1+\alpha)\alpha}$$

$$q_0 = -fW$$

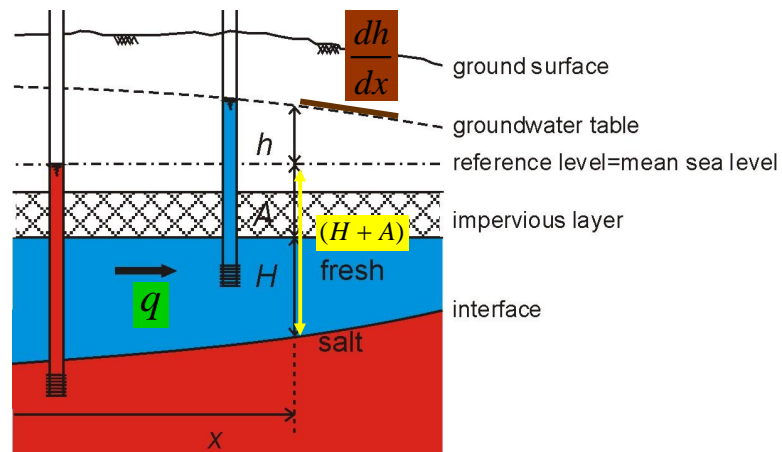
$$h = \alpha H$$

Example:

$$W = 3000\text{m}, f = 0.001\text{m/day}, \alpha = 0.020, k = 20\text{m/day}, D = 50\text{m}$$

$$L = 175.1\text{m}$$

## Confined aquifer (1D situation)



## Confined aquifer (1D situation)

(I) Darcy 
$$q = -kH \frac{dh}{dx}$$

(II) Continuity 
$$q = q_0$$

(III) BGH 
$$h = \alpha(H + A)$$



## Confined aquifer (1D situation)

$$-kH \frac{dh}{dx} = q_0$$

$$HdH = -\frac{q_0}{k\alpha} dx$$

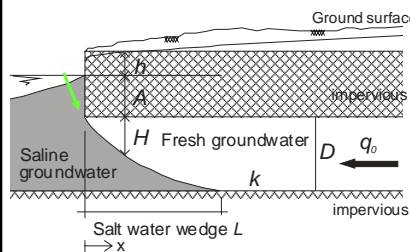
integration  
gives

$$\frac{1}{2}H^2 = \frac{q_0x}{k\alpha} + C$$

$$H = \sqrt{-\frac{2q_0x}{k\alpha} + 2C}$$

## Example 3: salt water wedge confined aquifer

$$H = \sqrt{-\frac{2q_0x}{k\alpha} + 2C}$$



Boundary condition

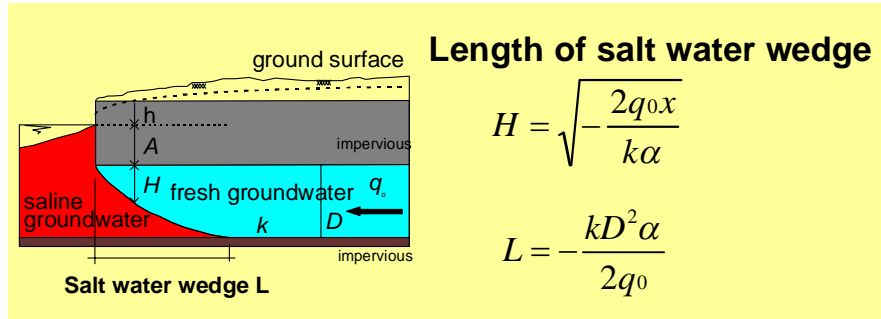
$$x = 0 : H = 0 \rightarrow C = 0$$

$$H = \sqrt{-\frac{2q_0x}{k\alpha}}$$

Length of salt water wedge  $x = L : H = D$

$$L = -\frac{kD^2\alpha}{2q_0}$$

### Example of analytical solutions (III)



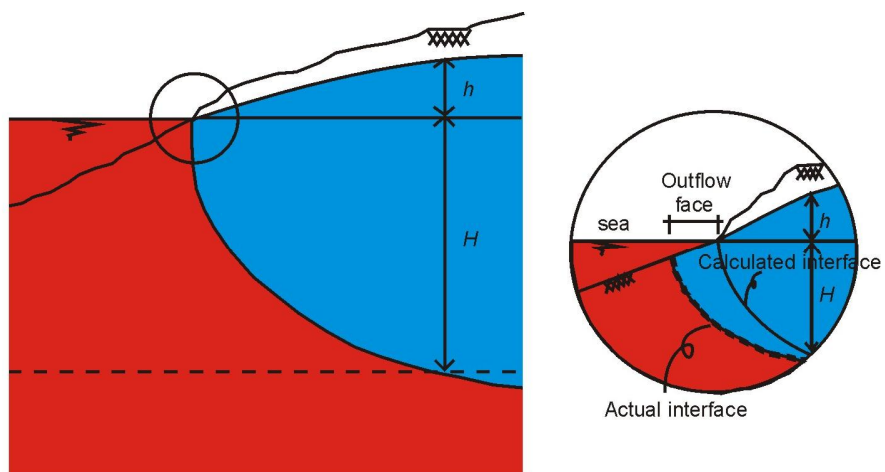
Example:

$W = 2000\text{m}, f = 0.001\text{m/day}, \alpha = 0.025, k = 25\text{m/day}, D = 40\text{m}$

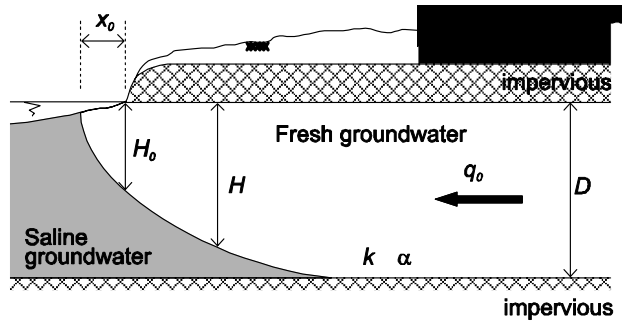
$L = 250\text{m}$

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### Outflow face (Submarine Groundwater Discharge)



### Outflow face (Submarine Groundwater Discharge)



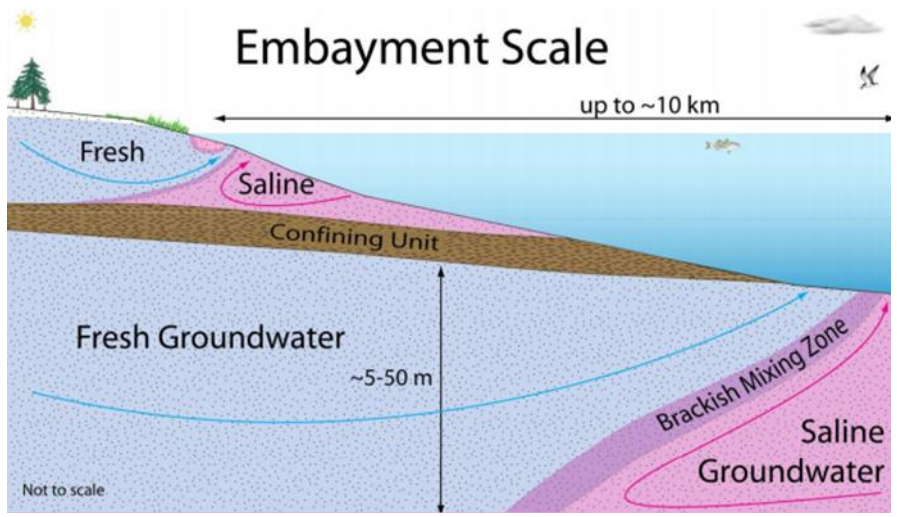
$$x_0 = \frac{q_0}{2k\alpha} \quad H_0 = \frac{q_0}{k\alpha} \quad \text{Glover (1959)}$$

Example:  
 $x_0 = f \cdot L / (2ka) = 0.001 \text{m/d} \cdot 20000 \text{m} / (2 \cdot 20 \cdot 0.025) = 20 \text{m (only!)}$

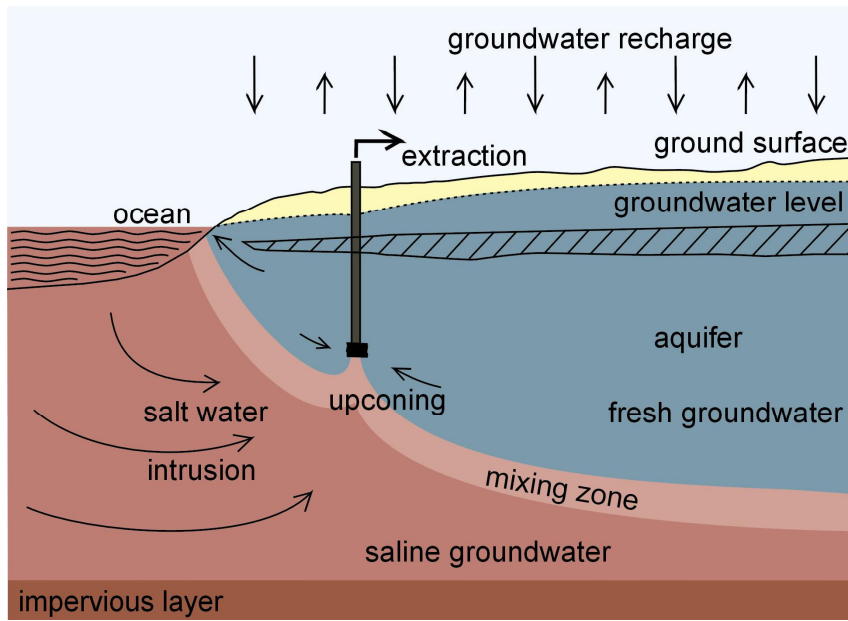
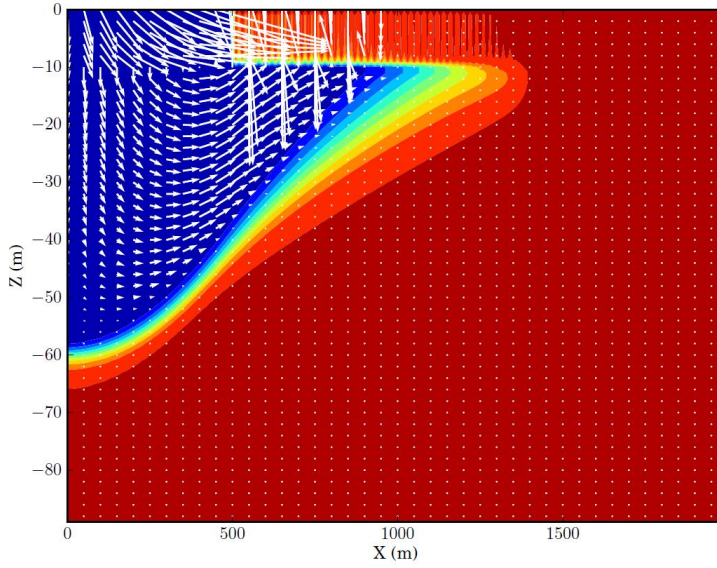
Note: no resistance layer offshore

### Outflow face (Submarine Groundwater Discharge)

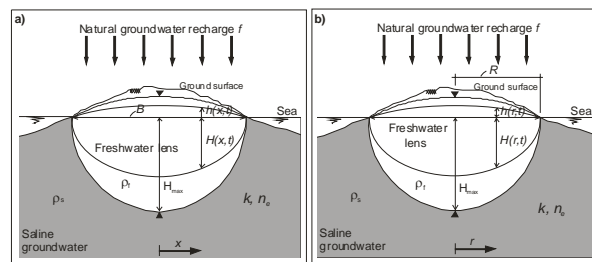
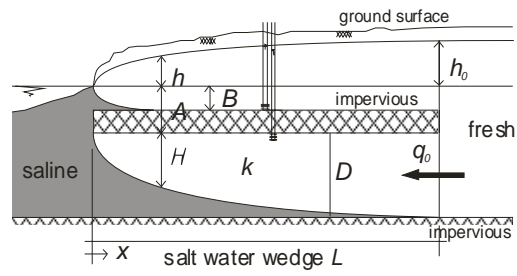
#### Embayment Scale



### Outflow face (Submarine Groundwater Discharge)



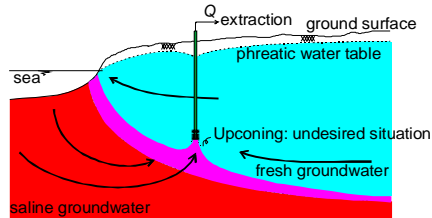
See the lectures for more cases



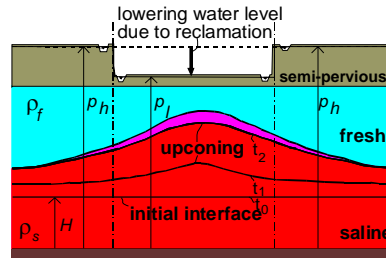
Upconing processes

## Upconing of saline groundwater

Under an extraction well



Under a low-lying polder area

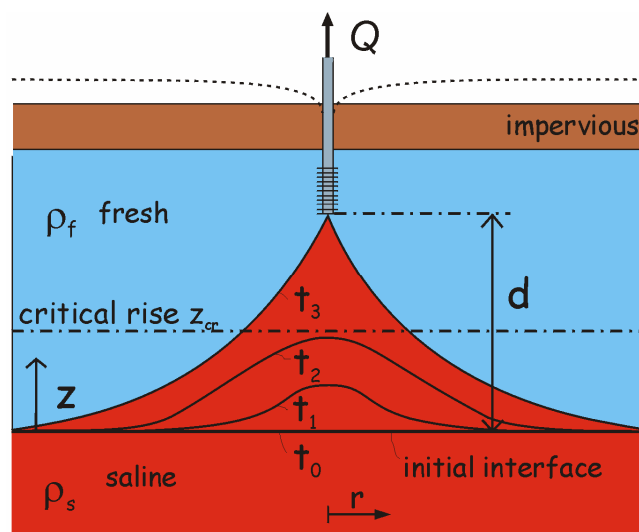


- movement of saline groundwater to extraction wells
- increase in salinity (>150-200 mg Cl-/l)
- lowering of the piezometric head (leads to land subsidence: e.g. Los Angeles: 9 m in the 1930's)

'Solutions': reduce extraction rate, abandon well, inundate polder

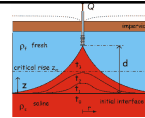
## Examples of analytical solutions (IV)

Upconing of saline groundwater under an extraction well



## Examples of analytical solutions (IV)

Upconing of saline groundwater under an extraction well



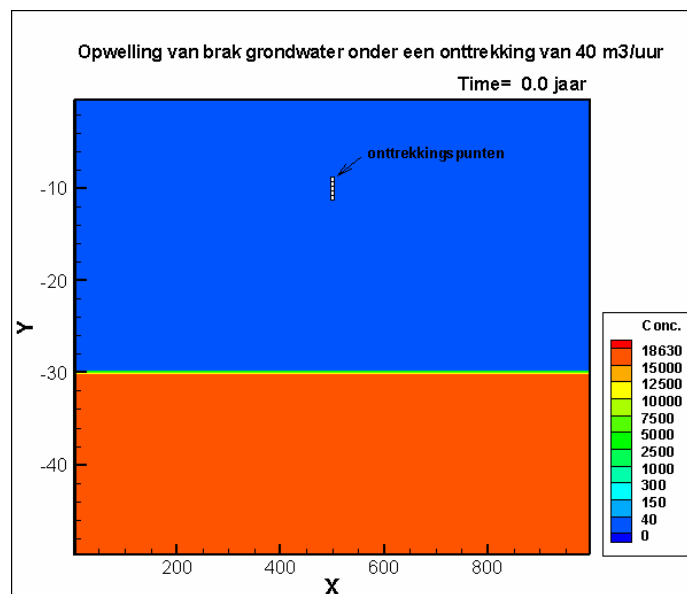
$$z(r, t) = \frac{Q}{2\pi\alpha k_x d} \left[ \frac{1}{(1 + R'^2)^{1/2}} - \frac{1}{[(1 + \gamma')^2 + R'^2]^{1/2}} \right]$$

$$R' = \frac{r k_z}{d k_x} \quad \gamma' = \frac{\alpha k_z}{2n_e d} t$$

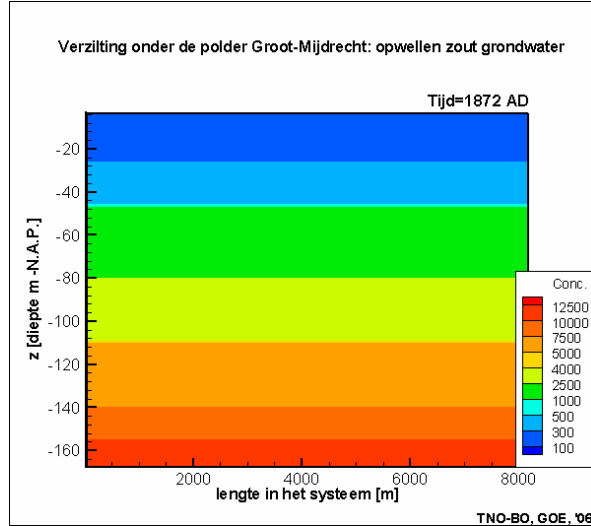
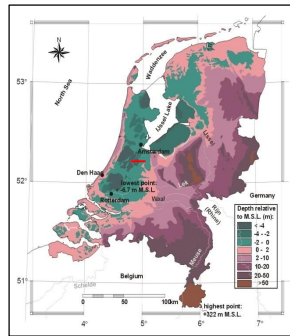
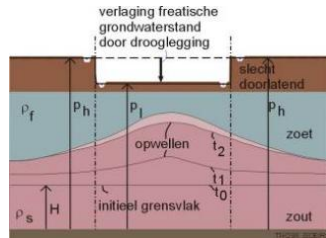
Dagan & Bear, 1968, J. Hydraul. Res 6, 1563-1573

Lecture notes p. 44

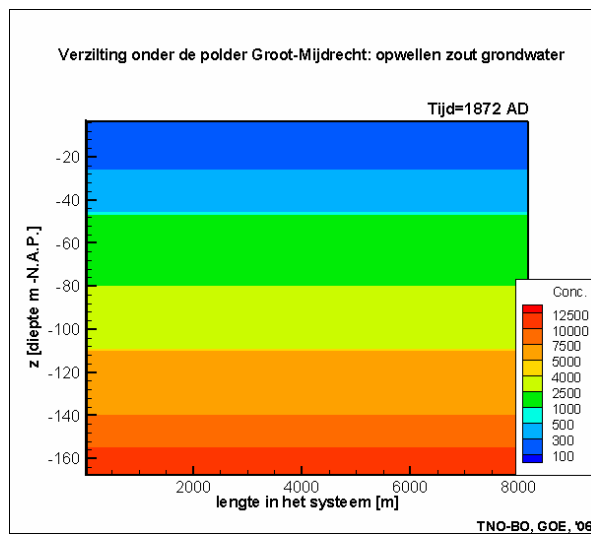
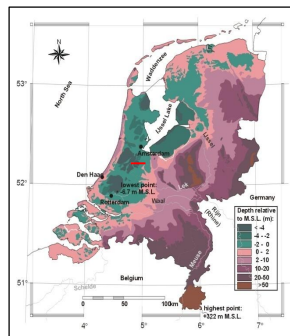
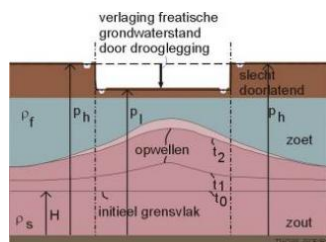
## Upconing of salt under an extraction



## Upconing under a low-lying polder (Groot-Mijdrecht)

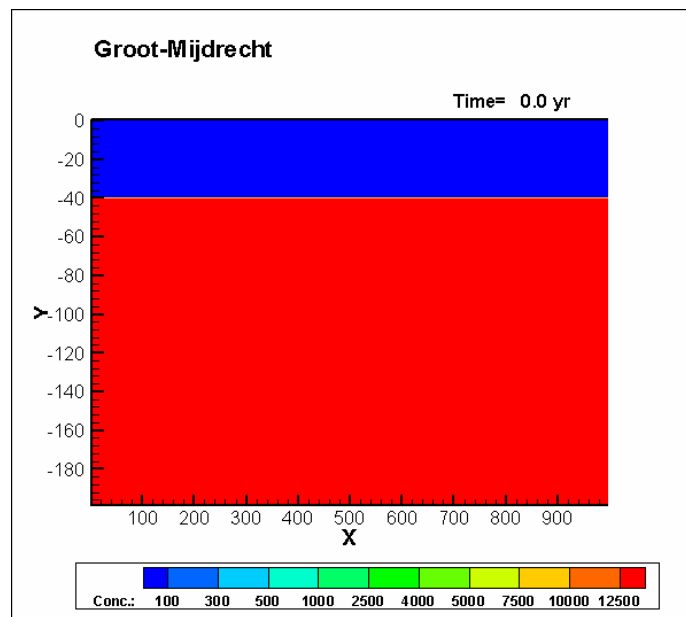


## Upconing under a low-lying polder (Groot-Mijdrecht)

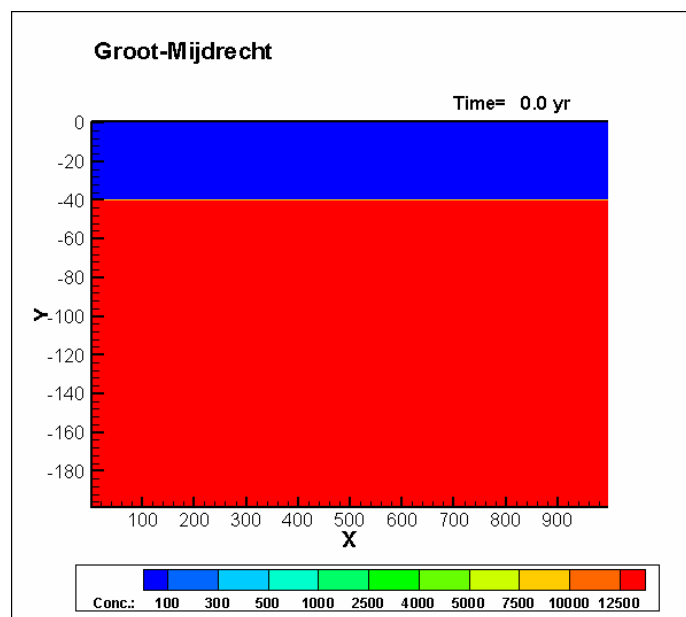




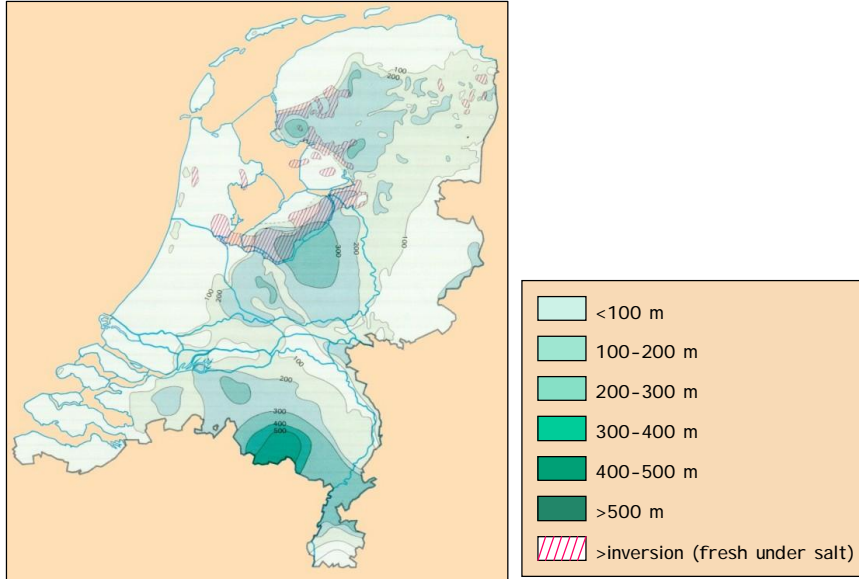
### Upconing under a low-lying polder (Groot-Mijdrecht)



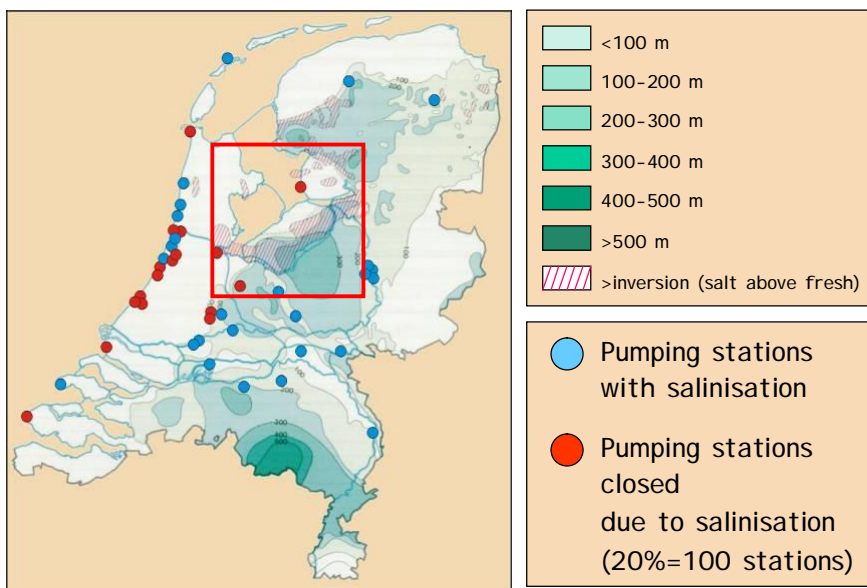
### Upconing under a low-lying polder (Groot-Mijdrecht)



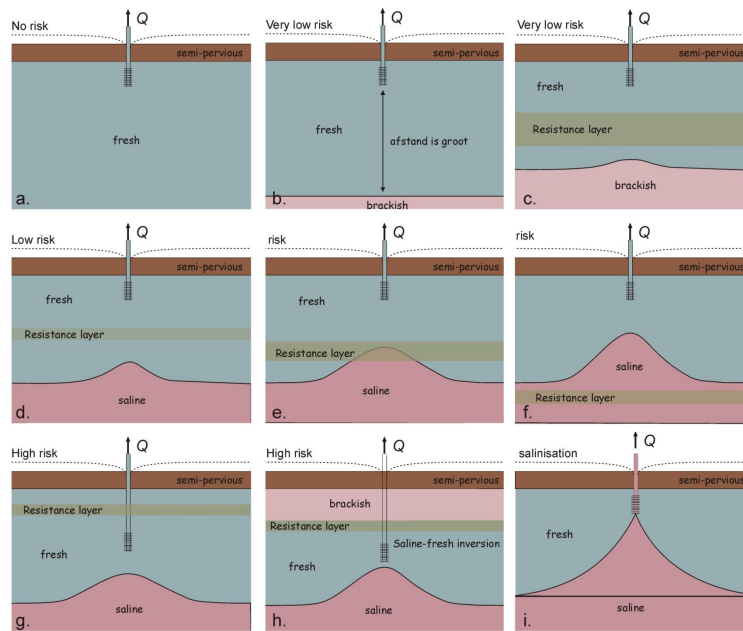
### Fresh-salt interface (150 mg Cl<sup>-</sup>/l)



### Availability of fresh groundwater

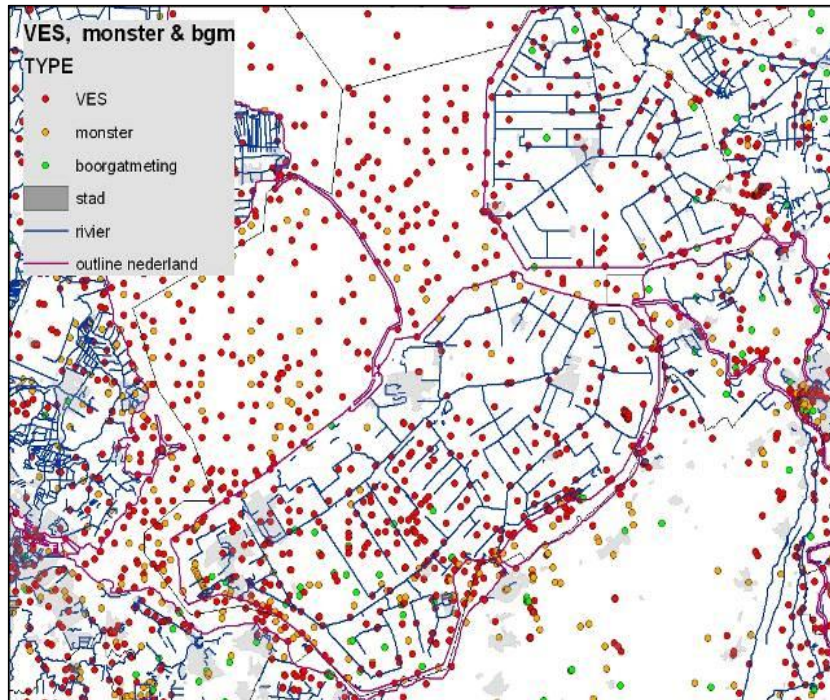


## Different risks of upconing saline groundwater

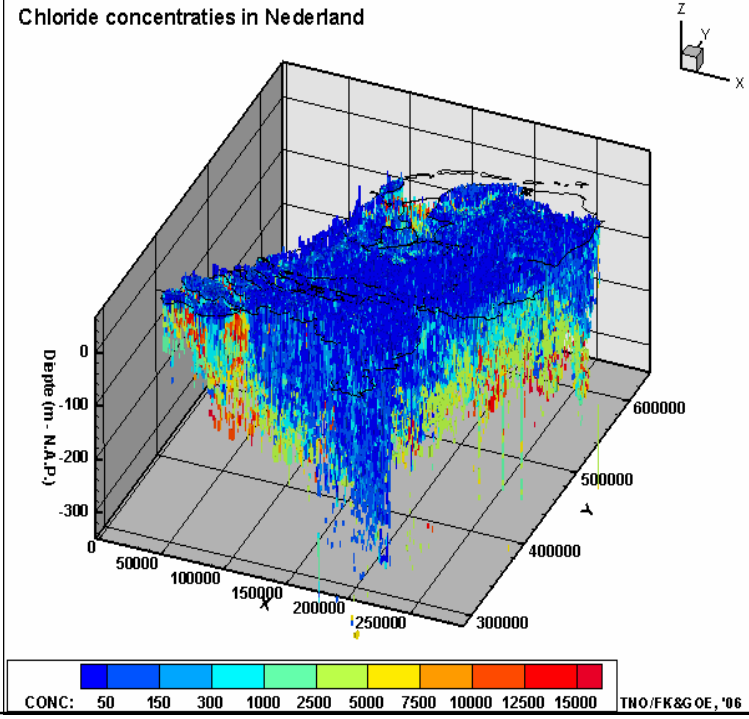


## VES, monster & bgm

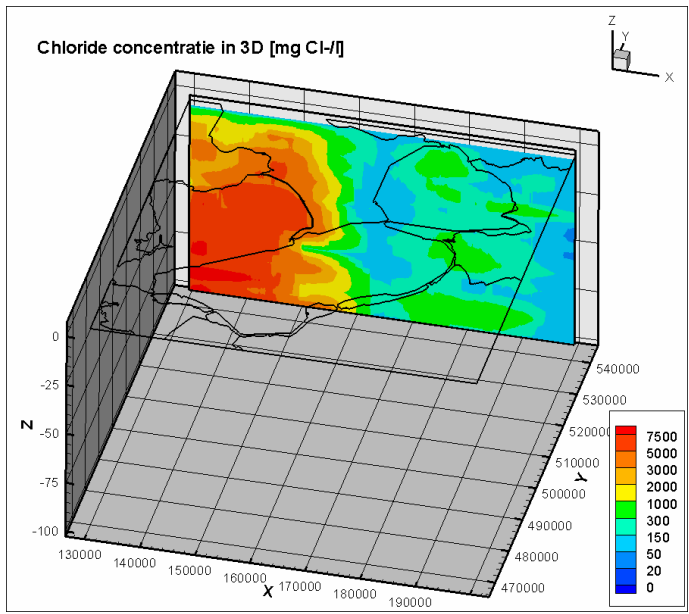
- TYPE
- VES
  - monster
  - boorgatmeting
  - stad
  - rivier
  - outline nederland



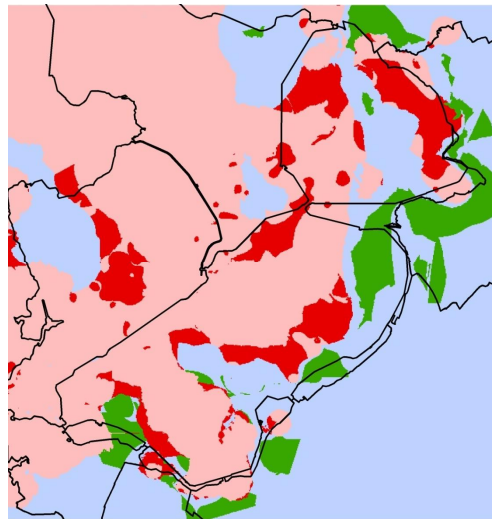
### Chloride concentraties in Nederland



### Animation 3D Chloride concentration

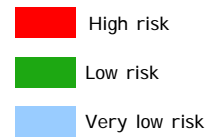


## Upconing in Flevoland

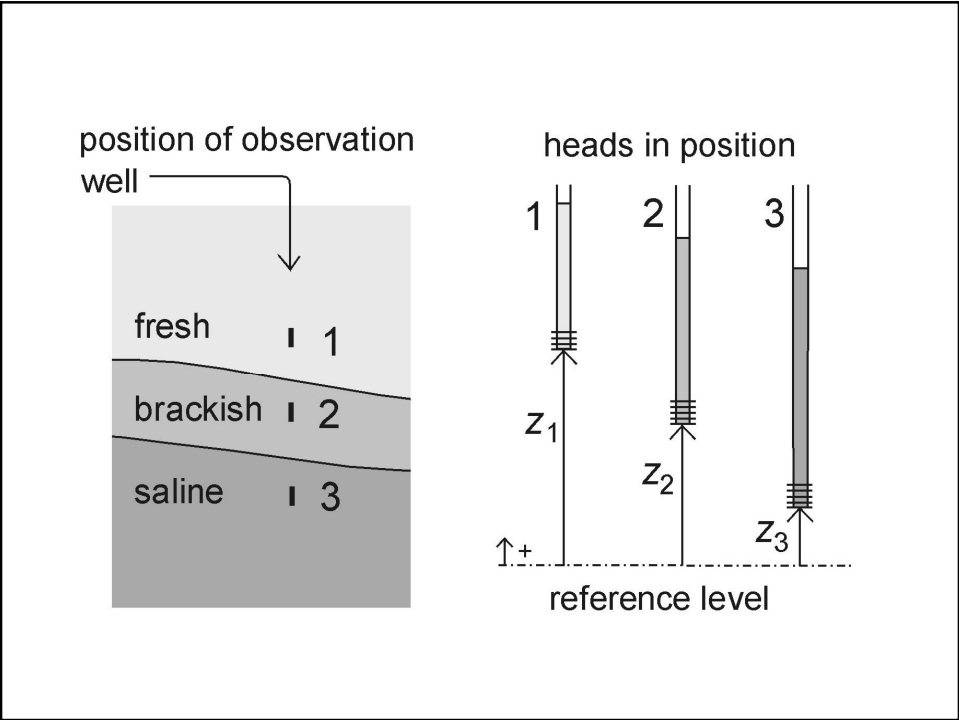
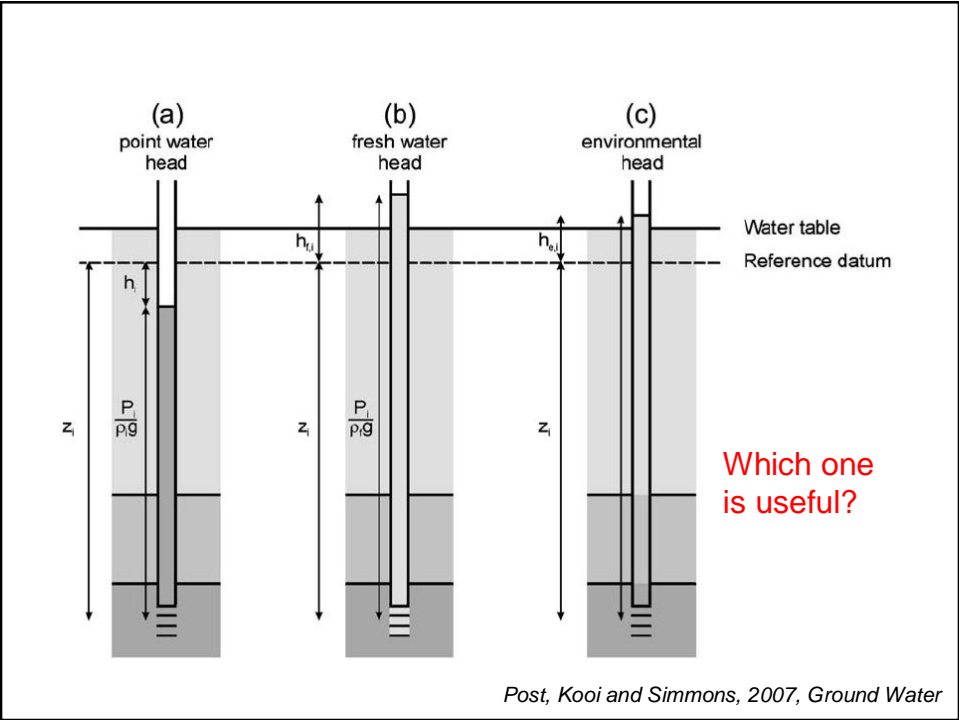


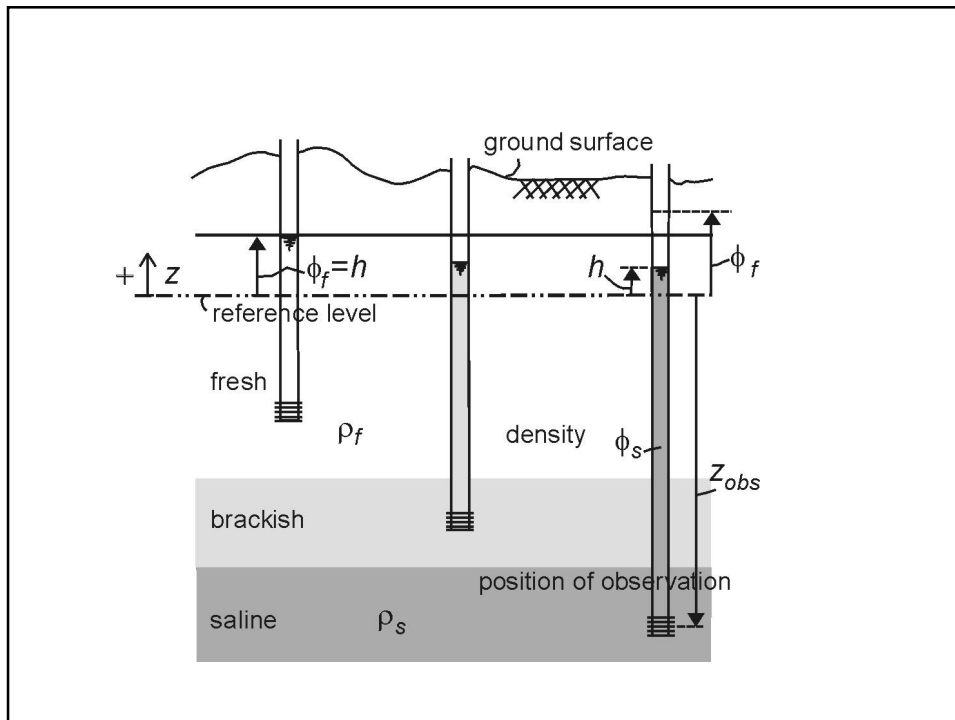
Risk depends on:

- Initial position interface
- Resistance layers
- Existence inversion
- Extraction rate and scheme



Freshwater head  $\phi_f$





$$\phi_f = \frac{p}{\rho_f g} + z$$

1. Groundwater with different densities can be compared
2. Fictive parameter
3. Hydrologists like to use heads instead of pressures
4. Pressure sometimes better
5. Confusing (heads not perpendicular to streamlines)

## Freshwater head $\phi_f$

$$h_f = \frac{\rho}{\rho_f} h$$

$$\phi_f = h_f + z$$

$$\phi_f = \frac{\rho}{\rho_f} h + z$$

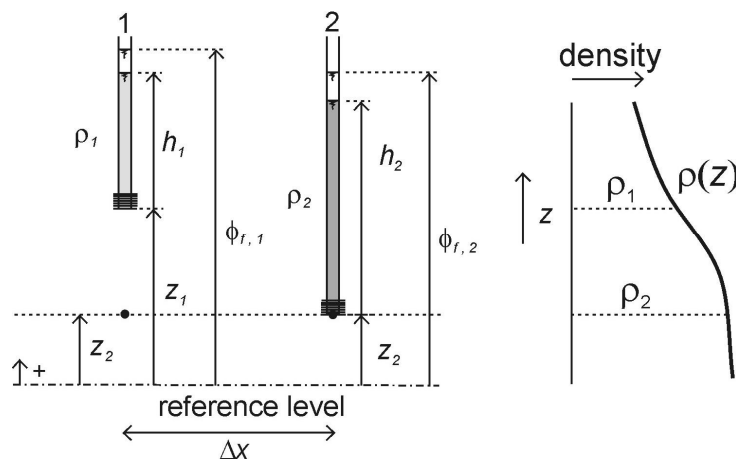
e.g.:

$$\rho_s = 1025 \text{ kg/m}^3$$

$$h = 10 \text{ m}$$

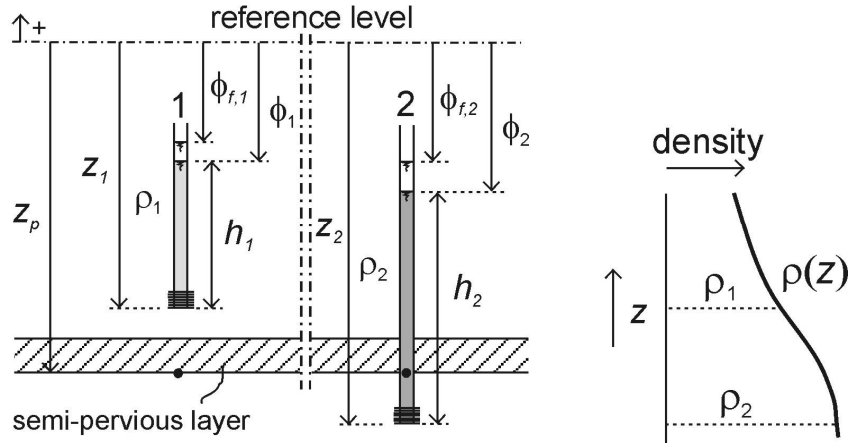
$$\phi_f = 10.25 \text{ m}$$

## Freshwater head $\phi_f$ : horizontal flow?

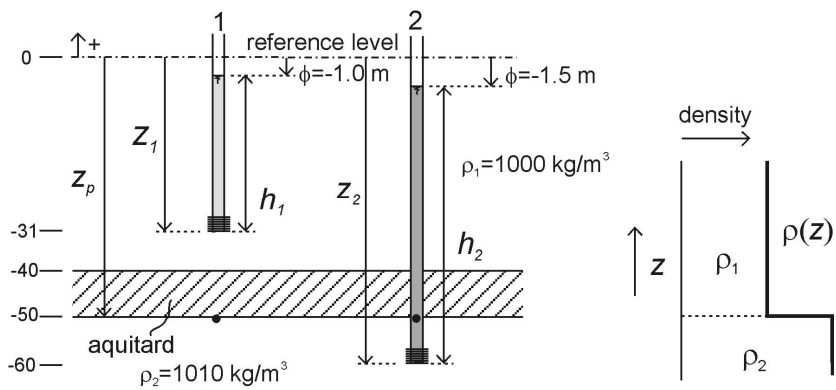




### Freshwater head $\phi_f$ : vertical flow?



### Freshwater head $\phi_f$



Special case: hydrostatic pressure:  $q_z=0$

$$q_z = -\frac{\kappa_z \rho_f g}{\mu} \left( \frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right) \quad \text{no vertical flow}$$

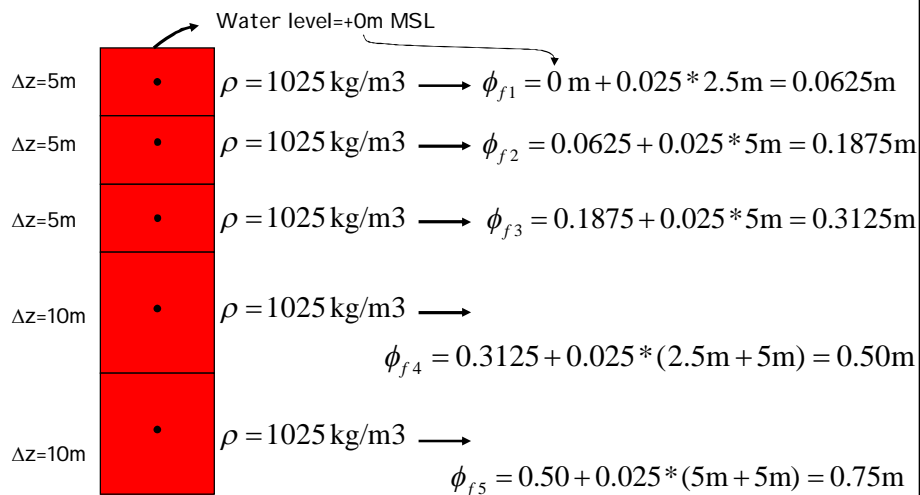
$$0 = \left( \frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$\partial \phi_f = -\frac{\rho - \rho_f}{\rho_f} \partial z$$

$$\phi_{f2} = \phi_{f1} - \frac{\rho - \rho_f}{\rho_f} (z2 - z1)$$

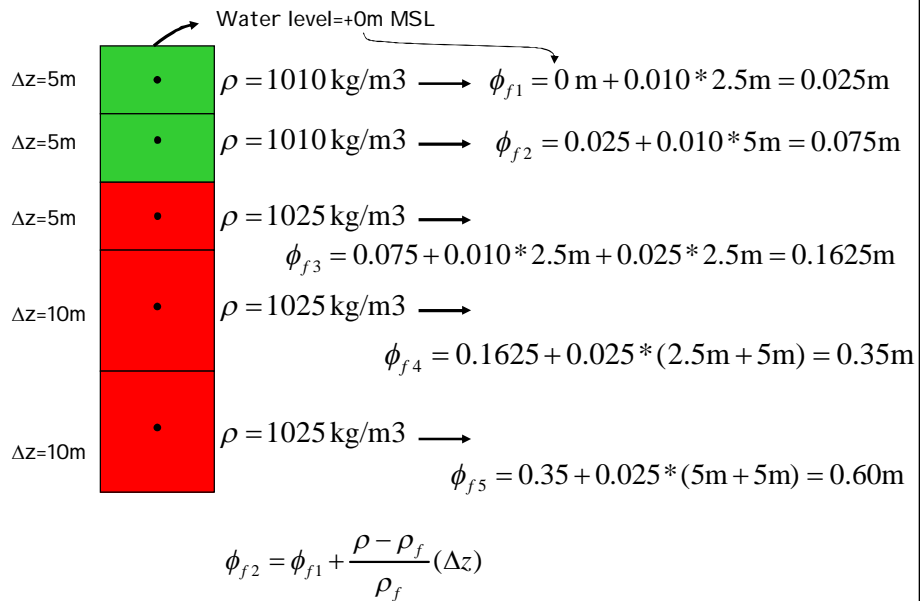
$$\downarrow + \quad \phi_{f2} = \phi_{f1} + \frac{\rho - \rho_f}{\rho_f} (\Delta z)$$

Hydrostatic boundary condition at the sea

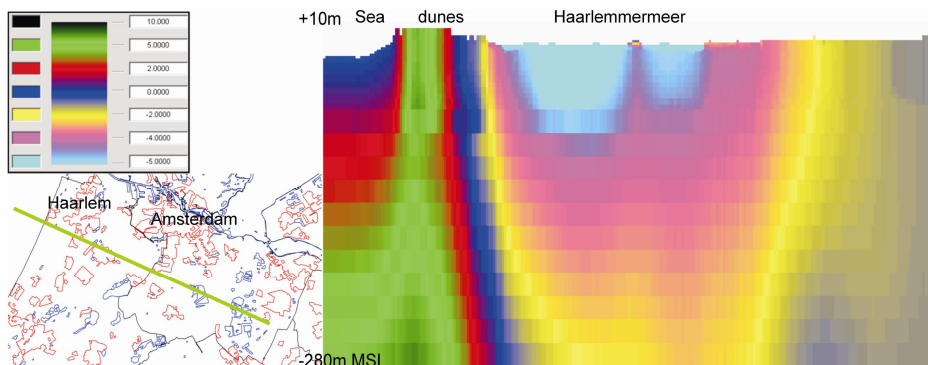


$$\phi_{f2} = \phi_{f1} + \frac{\rho - \rho_f}{\rho_f} (\Delta z)$$

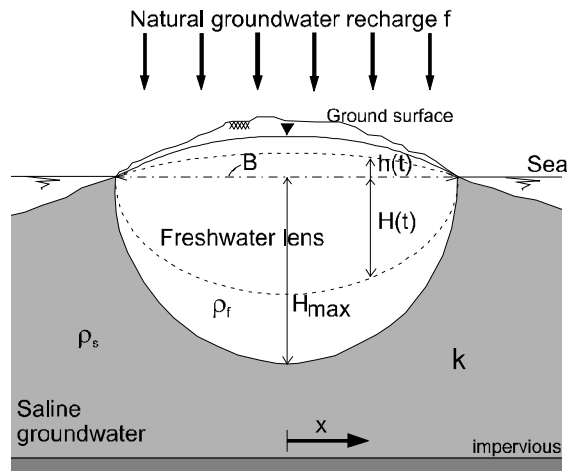
## Hydrostatic boundary condition at the sea



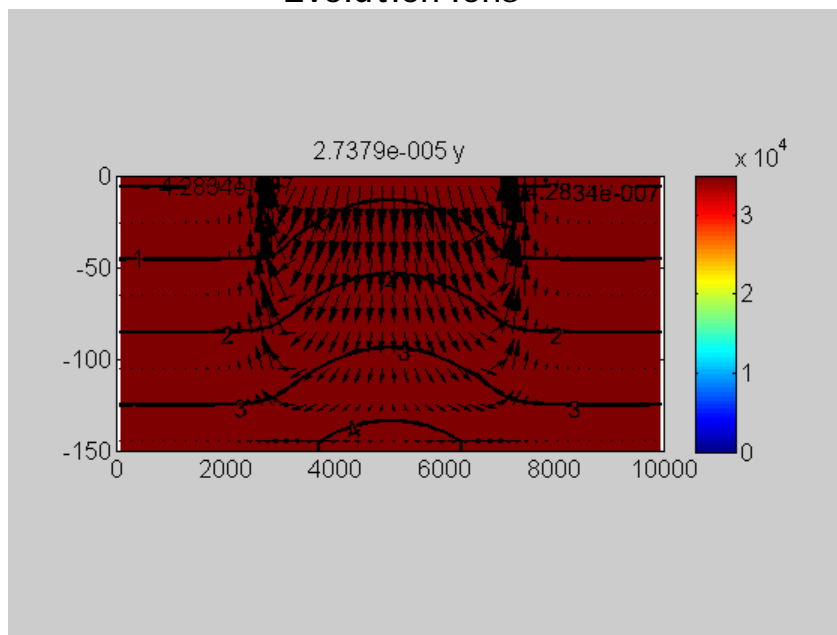
## NHI fresh-salt: 2D profile freshwater head



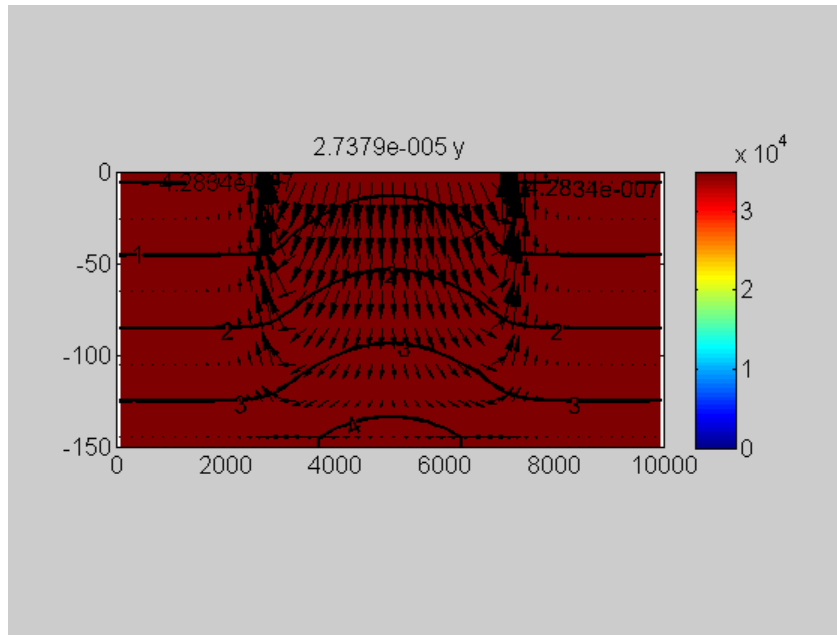
## Case 2: Development of a freshwater lens



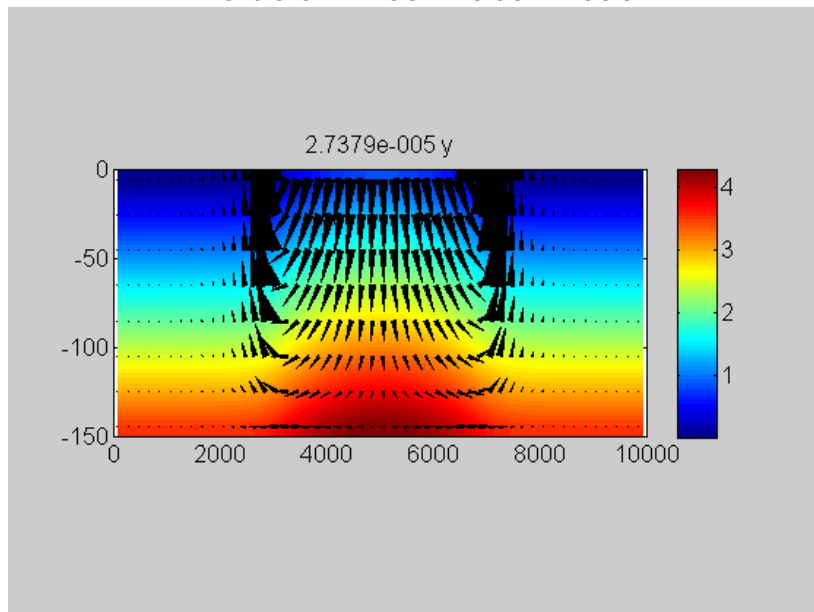
## Evolution lens



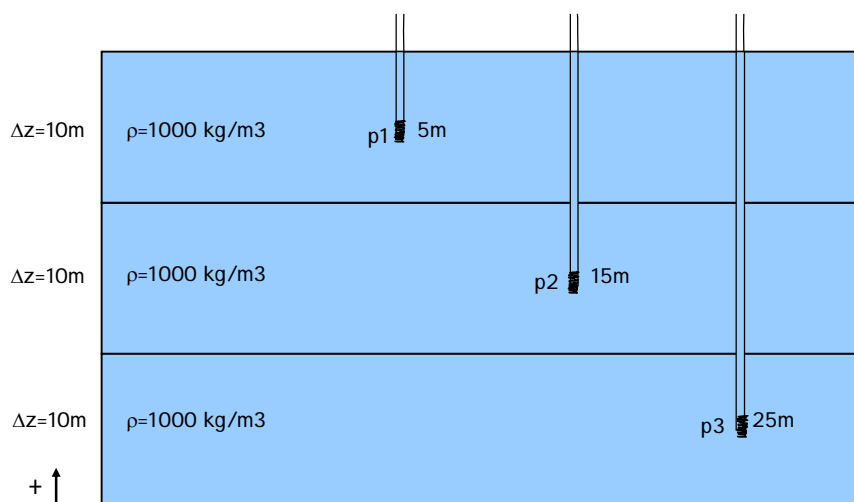
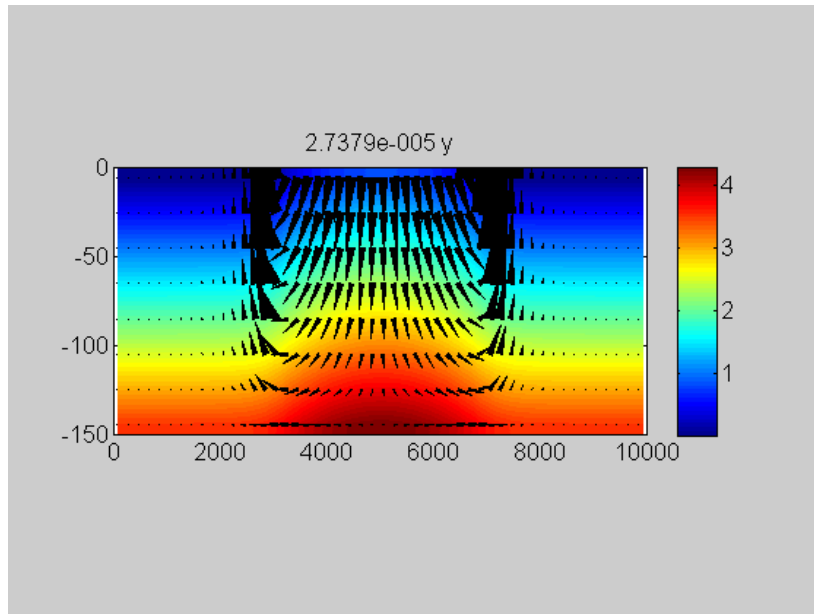
### Evolution lens



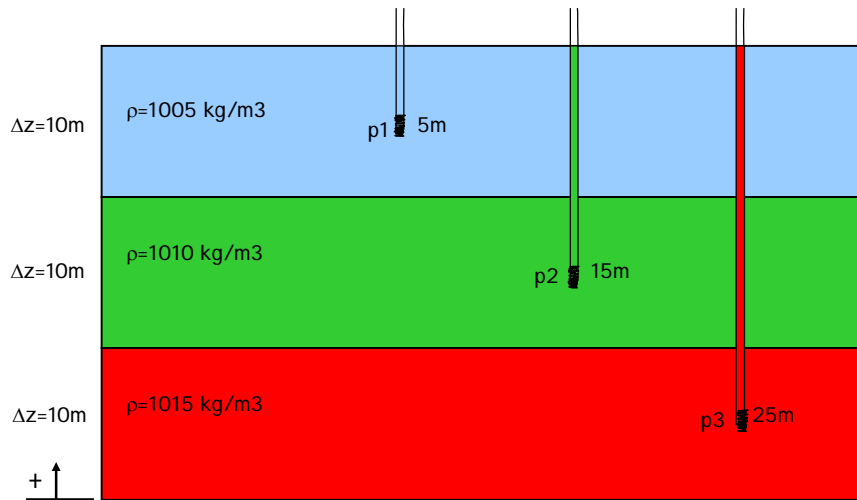
### Evolution freshwater head



### Evolution freshwater head

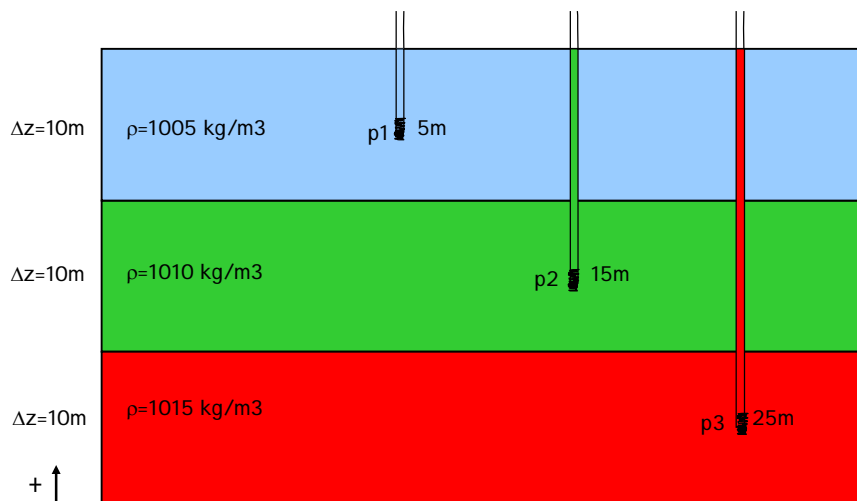


No flow



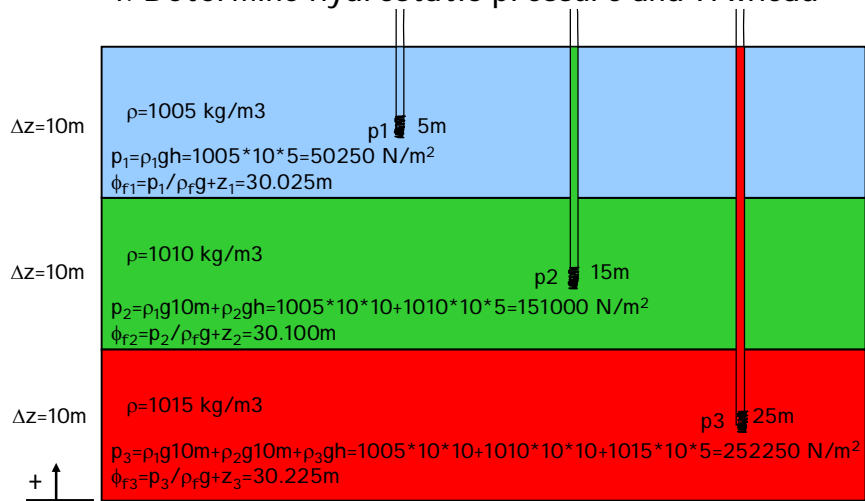
Flow or no flow? (if  $p \neq$  hydrostatic than flow)

Calculate to freshwater head!



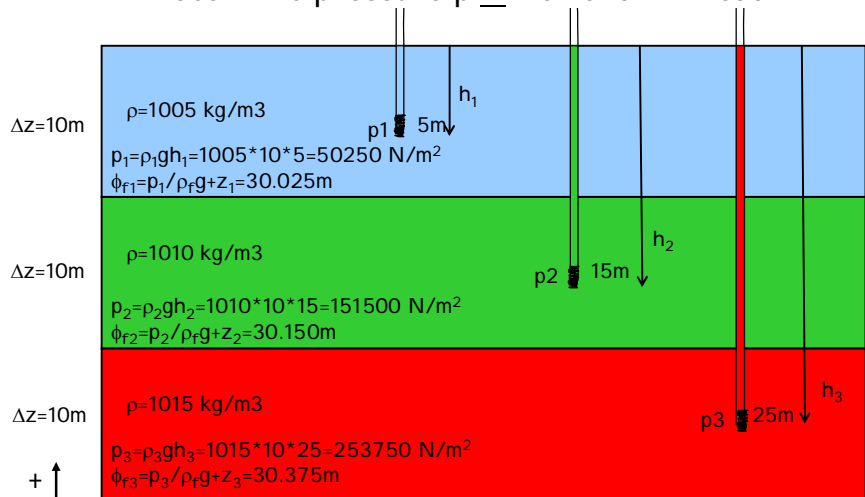
1. Determine hydrostatic pressure (and freshwater head  $\phi_f$ )
2. Determine pressure  $p$  in well! (and freshwater head  $\phi_f$ )

### 1. Determine hydrostatic pressure and frwhead



1. Determine hydrostatic pressure (and freshwater head  $\phi_f$ )
2. Determine pressure  $p$  in well! (and freshwater head  $\phi_f$ )

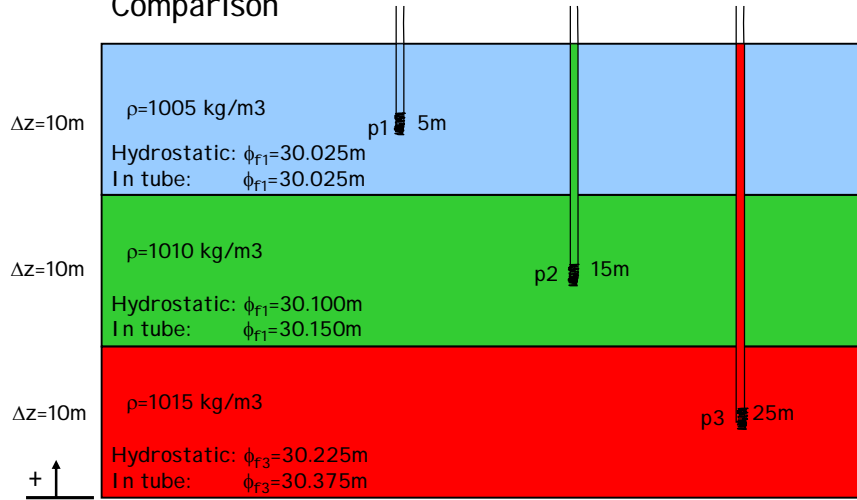
### 2. Determine pressure $p$ in well and frwhead



1. Determine hydrostatic pressure (and freshwater head  $\phi_f$ )
2. Determine pressure  $p$  in well! (and freshwater head  $\phi_f$ )

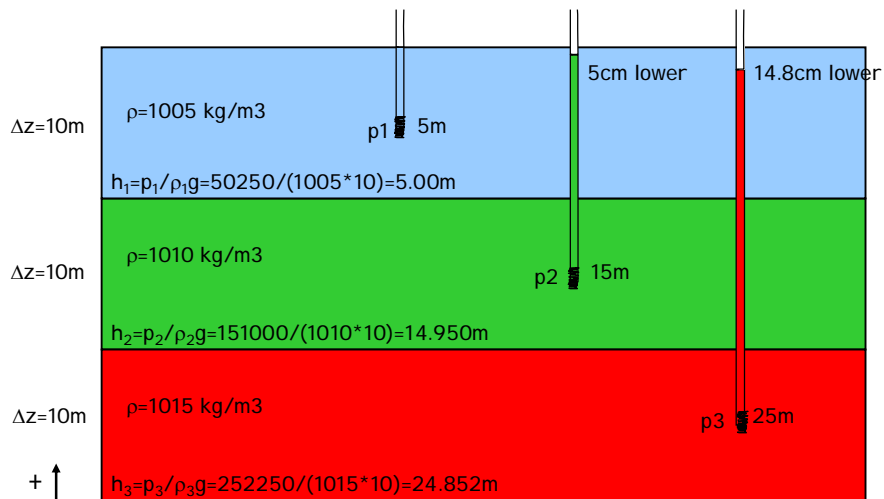


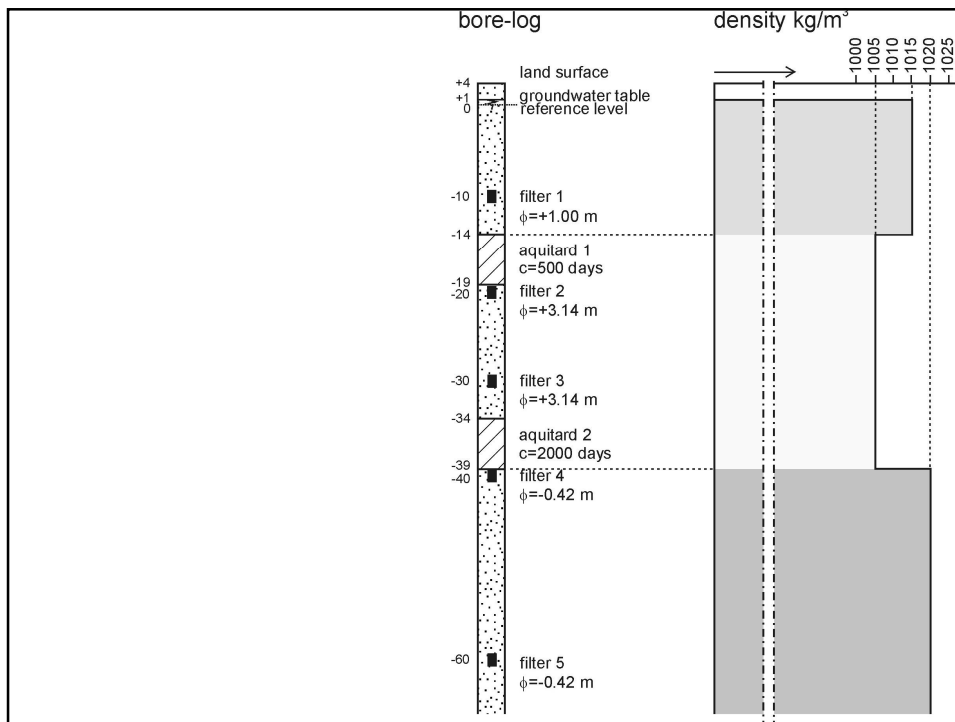
### Comparison



Conclusion: freshwater head not equal, so vertical upward flow!

What would be the water level in the tube if hydrostatic?

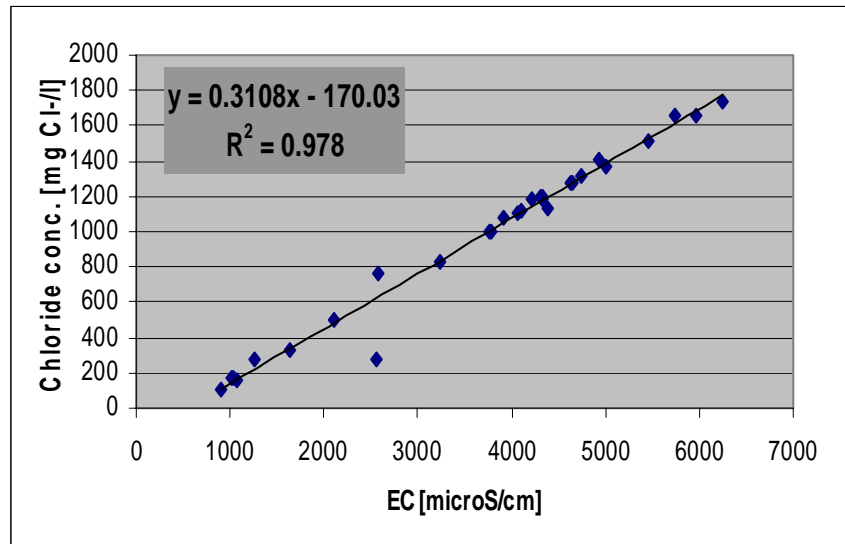




## Take home message

1. In coastal area (with fresh-brackish-saline groundwater), always measure head and Electrical Conductivity (EC)
2. Convert EC to density
3. Determine freshwater head with lecture notes and ppt
4. Determine flow

## Close relation between chloride concentration and Electrical Conductivity



EOS

## Examples of equations of state

Knudsen (1902)

$$\rho_{(S,T)} = 1000 + 0.8054S - 0.0065(T - 4 + 0.2214S)^2$$

T < 15 °C, S < 20 ppt

Linear (concentration)

$$\rho_{(C)} = \rho_f \left[ 1 + \alpha \frac{C_i}{C_s} \right] \quad \text{where } \alpha = \text{relative density difference}$$

Linear (temperature)

$$\rho_{(T)} = \rho_f [1 - \beta(T - T')] ]$$

Exponential (temperature, pressure, salt)

$$\rho_{(T,p,\omega)} = \rho_f e^{-\alpha(T-T_0) + \beta(p-p_0) + \gamma\omega}$$

$$\mu = \mu_0 [1 + (1.85\omega - 4.10\omega^2 + 44.50\omega^3)]$$

# Modelling

salt water intrusion  
density dependent groundwater flow

modelling

Why mathematical modelling anyway?

A model is only a schematisation of the reality!

## Why mathematical modelling anyway?

+:

- cheaper than scale models
- analysis of very complex systems is possible
- a model can be used as a database
- to increase knowledge about a system (water balances)

-:

- simplification of the reality
- only a tool, no purpose on itself
- garbage in=garbage out: (field)data important
- perfect fit measurement and simulation is suspicious

## Numerical modelling variable density flow

Type:

- sharp interface models
- solute transport models

State of the art:

- three-dimensional
- solute transport
- transient

## Solute transport models

Combine  
the groundwater flow equation  
and  
the advection-dispersion equation  
by means of  
an equation of state

## Solute transport equation

Partial differential equation (PDE):

$$R_d \frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left( D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (C V_i) + \frac{(C - C^*) W}{n_e} - R_d \lambda C$$

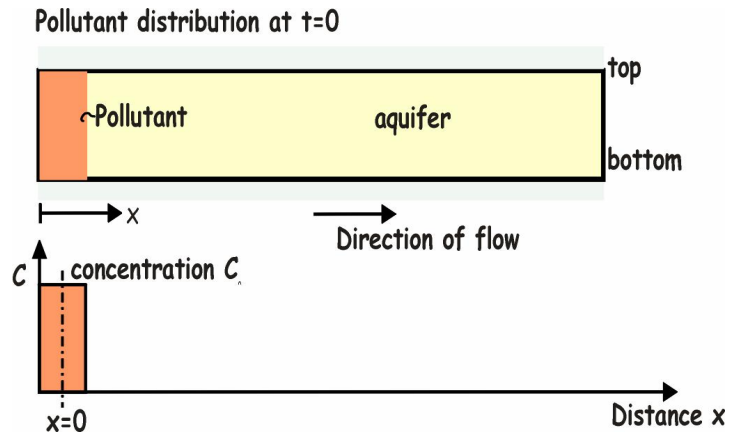
change in concentration    dispersion diffusion    advection    source/sink    decay

$D_{ij}$ =hydrodynamic dispersion [ $L^2 T^{-1}$ ]

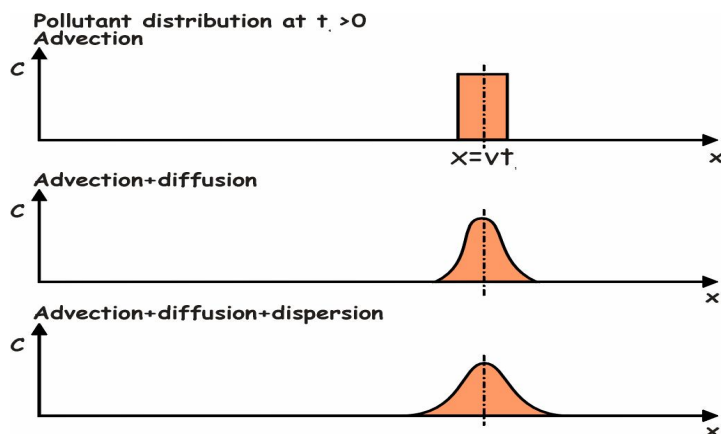
$R_d$ =retardation factor [-]

$\lambda$ =decay-term [ $T^{-1}$ ]

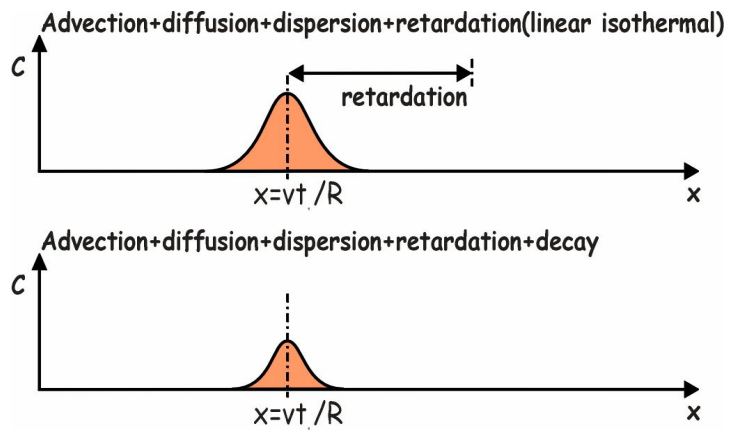
## Solute transport equation: column test (I):



## Solute transport equation: column test (II):



Solute transport equation: column test (III):



## Hydrodynamic dispersion

$$\text{hydrodynamic dispersion} = \text{mechanical dispersion} + \text{diffusion}$$

mechanical dispersion:

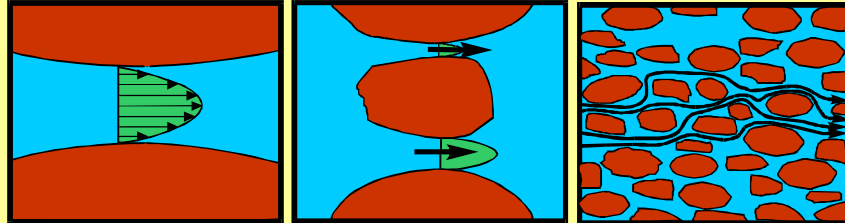
tensor  
velocity dependant

diffusion:

molecular process  
solute spread due to concentration differences



## Mechanical dispersion



Differences in velocity in the pore

Differences in velocity due to variation in pore-dimension

Differences in velocity due to variation in velocity direction

## Solute transport equation: diffusion (I)

diffusion is a slow process: diffusion equation

only 1D-diffusion means:  $R_f=1$ ,  $V_f=0$ ,  $\lambda=0$  and  $W=0$ 

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$$

similarity with non-steady state groundwater flow equation

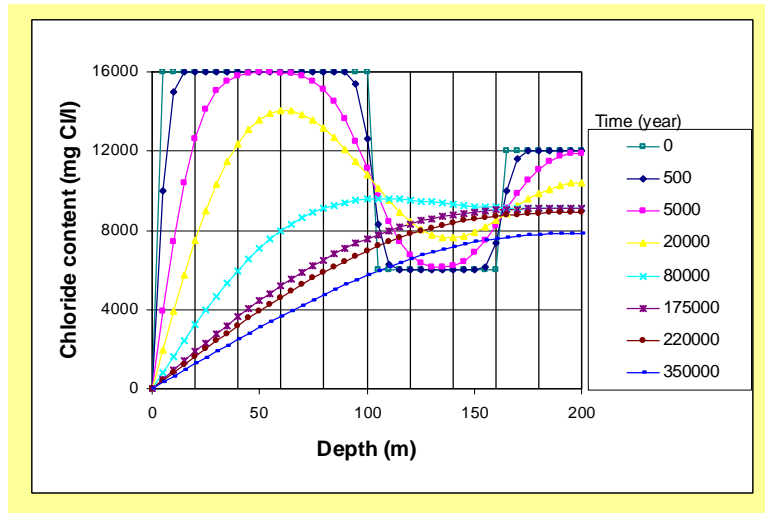
$$S \frac{\partial \phi}{\partial t} = T \frac{\partial^2 \phi}{\partial x^2} + N \quad \frac{T \Delta t}{S \Delta x^2} < 0.5$$

$$\phi_i^{t+\Delta t} = \phi_i^t + \frac{N \Delta t}{S} + \frac{T \Delta t}{S \Delta x^2} (\phi_{i+1}^t - 2\phi_i^t + \phi_{i-1}^t)$$

$$C_i^{t+\Delta t} = C_i^t + \frac{D \Delta t}{\Delta z^2} (C_{i+1}^t - 2C_i^t + C_{i-1}^t) \quad \frac{D \Delta t}{\Delta z^2} < 0.5$$

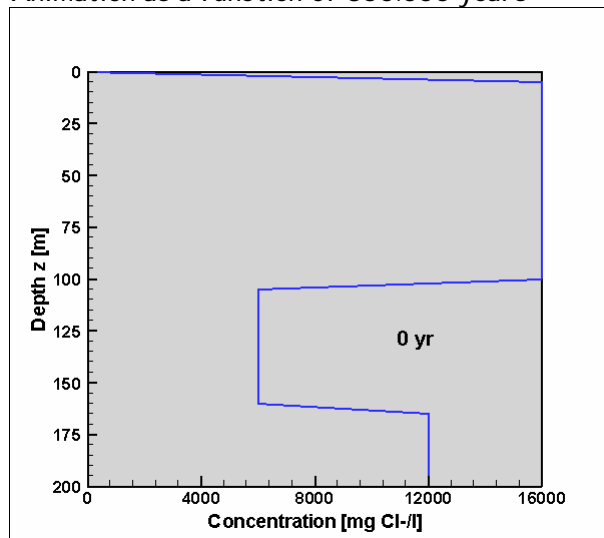
## Solute transport equation: diffusion (II)

diffusion is a slow process: diffusion equation  $\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$



## Solute transport equation: diffusion (III)

Animation as a function of 350.000 years



## Groundwater flow equation (MODFLOW, 1988)

## Darcy

$$q_x = -\frac{\kappa_x \rho_f g}{\mu} \frac{\partial \phi_f}{\partial x}; \quad q_y = -\frac{\kappa_y \rho_f g}{\mu} \frac{\partial \phi_f}{\partial y}; \quad q_z = -\frac{\kappa_z \rho_f g}{\mu} \left( \frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

## Continuity

$$-\left[ \frac{\partial \rho q_x}{\partial x} + \frac{\partial \rho q_y}{\partial y} + \frac{\partial \rho q_z}{\partial z} \right] = \frac{\partial n \rho}{\partial t} + W$$

## Freshwater head

$$\phi_f = \frac{p}{\rho_f g} + z$$

↑  
buoyancy  
term

## Advection-dispersion equation (MOC3D, 1996)

$$\frac{\partial C}{\partial t} = \frac{1}{nR_f} \frac{\partial}{\partial x_i} \left( nD_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{V_i}{R_f} \frac{\partial C}{\partial x_i} + \frac{\Sigma[W(C' - C)]}{nR_f} - \lambda C$$

## Equation of state: relation density &amp; concentration

$$\rho_{i,j,k} = \rho_f (1 + \beta C_{i,j,k})$$

## Examples of equations of state

Knudsen (1902)

$$\rho_{(S,T)} = 1000 + 0.8054S - 0.0065(T - 4 + 0.2214S)^2$$

Linear (concentration)

T &lt; 15 °C, S &lt; 20 ppt

$$\rho_{(C)} = \rho_f \left[ 1 + \alpha \frac{C_i}{C_s} \right] \quad \text{where } \alpha = \text{relative density difference}$$

Linear (temperature)

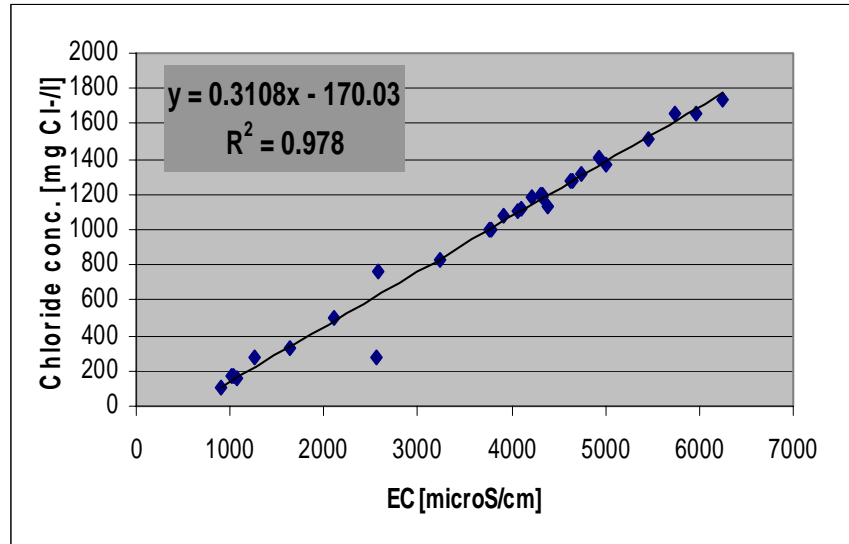
$$\rho_{(T)} = \rho_f [1 - \beta(T - T')] ]$$

Exponential (temperature, pressure, salt)

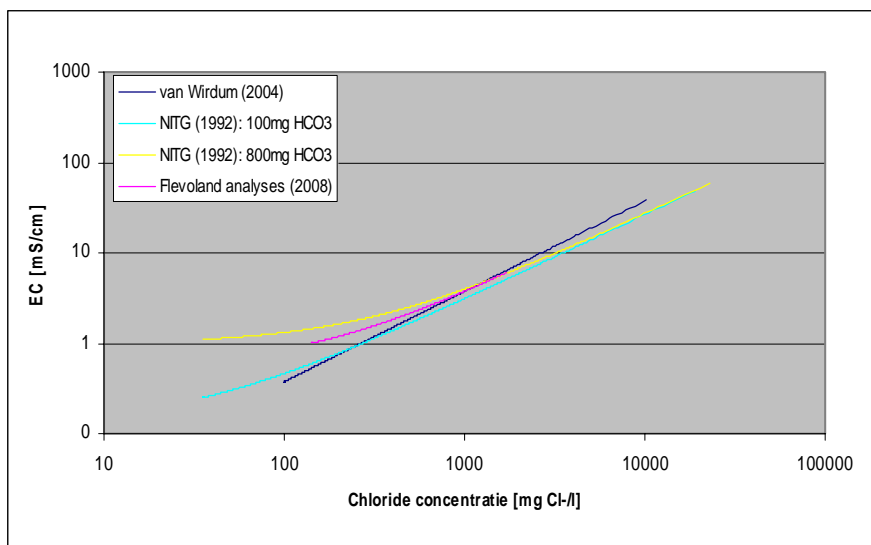
$$\rho_{(T,p,\omega)} = \rho_f e^{-\alpha(T-T_0) + \beta(p-p_0) + \gamma\omega}$$

$$\mu = \mu_0 [1 + (1.85\omega - 4.10\omega^2 + 44.50\omega^3)]$$

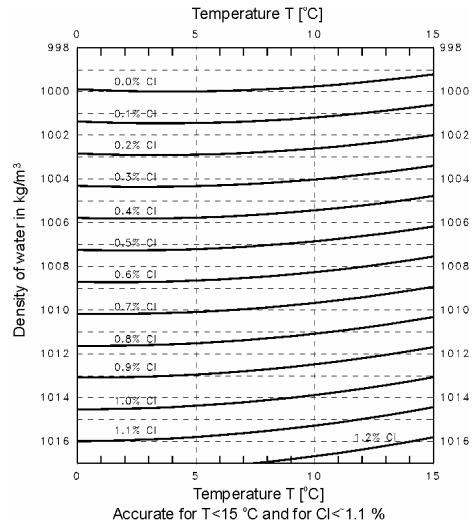
## Close relation between chloride concentration and Electrical Conductivity



## EC-Chloride

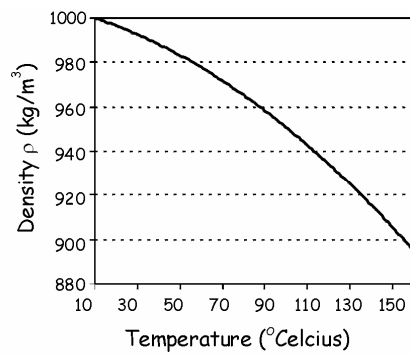
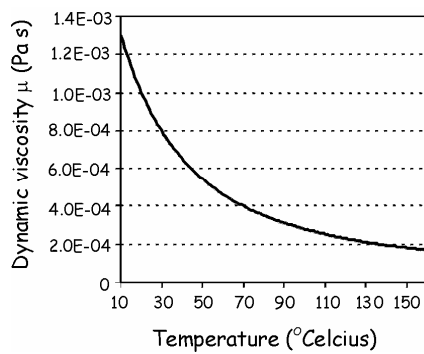


## Density depends on salinity and temperature



$$\rho_{(S,T)} = 1000 + 0.8054S - 0.0065(T - 4 + 0.2214S)^2 \quad \text{Knudsen (1902)}$$

## Density and viscosity depend on temperature (10°C-160 °C)



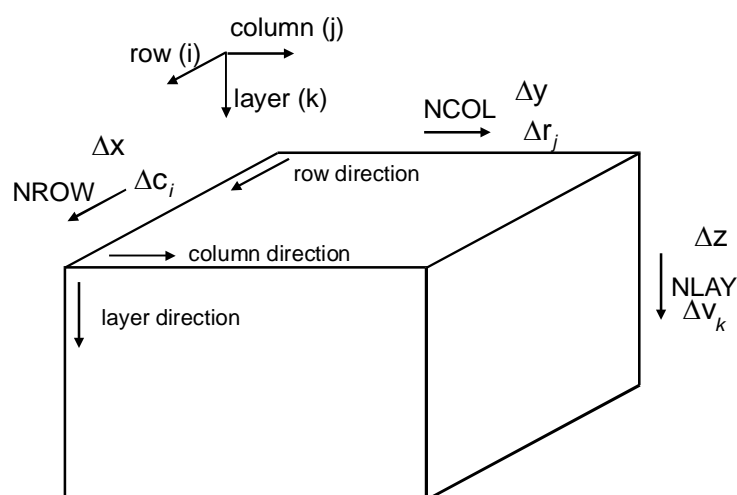
MOCDENS3D is based on MODFLOW

a modular 3D finite-difference ground-water flow model

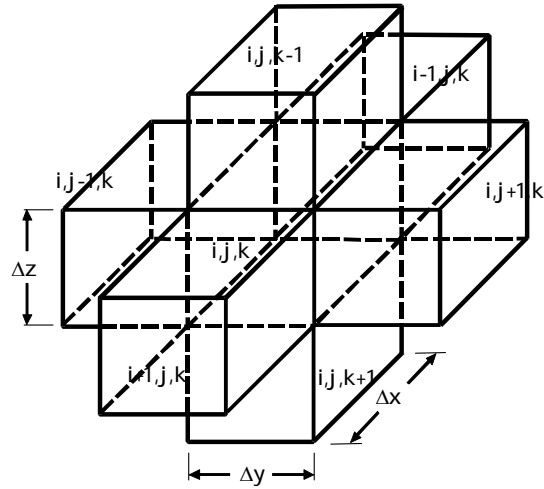
(M.G. McDonald & A.W. Harbaugh, from 1983 on)

- USGS, 'public domain'
- non steady state
- heterogeneous porous medium
- anisotropy
- coupled to reactive solute transport
  - MOC3 (Konikow *et al*, 1996)
  - MT3D, MT3DMS (Zheng, 1990)
  - RT3D
  - PHT3D (Prommer, 2004)
- easy to use due to numerous Graphical User Interfaces (GUI 's)
  - PMWIN, GMS, Visual Modflow, Argus One, Groundwater Vistas, etc.

Nomenclature MODFLOW element  $[i,j,k]$



MODFLOW: start with water balance of one element [i,j,k]



Continuity equation (I)

In - Out = Storage

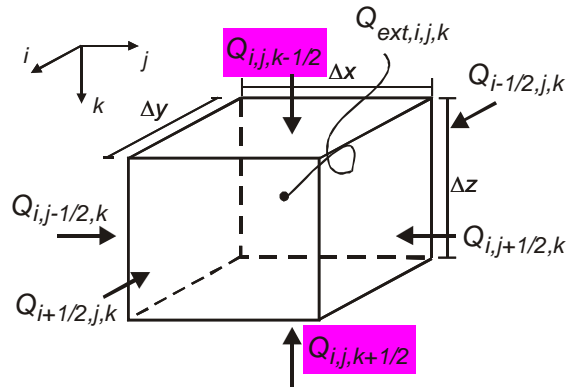
$$\frac{\partial}{\partial x} \left( k_{xx} \frac{\partial \phi}{\partial x} \right) + \frac{\partial}{\partial y} \left( k_{yy} \frac{\partial \phi}{\partial y} \right) + \frac{\partial}{\partial z} \left( k_{zz} \frac{\partial \phi}{\partial z} \right) - W = S_s \frac{\partial \phi}{\partial t}$$

$$\sum Q_i = S_s \frac{\Delta \phi}{\Delta t} \Delta V$$

## Continuity equation (II)

$$\sum Q_i = S_s \frac{\Delta \phi}{\Delta t} \Delta V$$

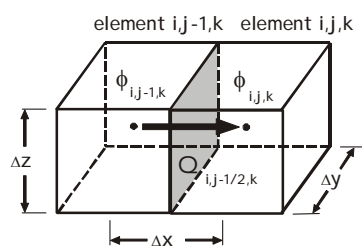
In = positive



$$Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k}$$

$$= S S_{i,j,k} \frac{\phi_{i,j,k}^t - \phi_{i,j,k}^{t+\Delta t}}{\Delta t} \Delta V$$

## Flow equation (Darcy's Law)



$$Q = \text{surface} * q = \text{surface} * k \frac{\partial \phi}{\partial x}$$

$$Q_{i,j-1/2,k} = k_{i,j-1/2,k} \Delta y \Delta z \frac{\phi_{i,j-1,k} - \phi_{i,j,k}}{\Delta x}$$

$$Q_{i,j-1/2,k} = CR_{i,j-1/2,k} (\phi_{i,j-1,k} - \phi_{i,j,k})$$

where  $CR_{i,j-1/2,k} = \frac{k_{i,j-1/2,k} \Delta y \Delta z}{\Delta x}$  is the conductance [ $L^2/T$ ]



## Density dependent vertical flow equation

$$q_z = -\frac{\kappa_z \rho_f g}{\mu} \left( \frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$q_z = -k_z \left( \frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$Q_z = \text{surface} * q_z$$

$$= \text{surface} * k_z \left( \frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$Q_{i,j,k-1/2} = k_{i,j,k-1/2} \Delta x \Delta y \left( \frac{\phi_{f,i,j,k-1} - \phi_{f,i,j,k}}{\Delta z} + BUOY_{i,j,k-1/2} \right)$$

$$Q_{i,j,k-1/2} = CV_{i,j,k-1/2} (\phi_{f,i,j,k-1} - \phi_{f,i,j,k} + BUOY_{i,j,k-1/2} \Delta z)$$

$$\text{where } BUOY_{i,j,k-1/2} = \left( \frac{(\rho_{i,j,k-1/2} + \rho_{i,j,k})/2 - \rho_f}{\rho_f} \right) = \text{buoyancy term [-]}$$

$$\text{where } CV_{i,j,k-1/2} = \frac{k_{i,j,k-1/2} \Delta x \Delta y}{\Delta z} = \text{conductance [L}^2/\text{T]}$$

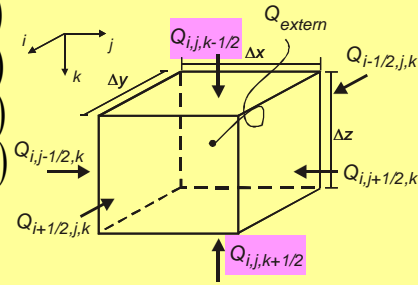
## Density dependent groundwater flow equation

$$Q_{i,j-1/2,k} = CR_{i,j-1/2,k} (\phi_{f,i,j-1,k} - \phi_{f,i,j,k})$$

$$Q_{i,j+1/2,k} = CR_{i,j+1/2,k} (\phi_{f,i,j+1,k} - \phi_{f,i,j,k})$$

$$Q_{i-1/2,j,k} = CC_{i-1/2,j,k} (\phi_{f,i-1,j,k} - \phi_{f,i,j,k})$$

$$Q_{i+1/2,j,k} = CC_{i+1/2,j,k} (\phi_{f,i+1,j,k} - \phi_{f,i,j,k})$$



$$Q_{i,j,k-1/2} = CV_{i,j,k-1/2} \left( \phi_{f,i,j,k-1} - \phi_{f,i,j,k} + BUOY_{i,j,k-1/2} \Delta v_{k-1/2} \right)$$

$$Q_{i,j,k+1/2} = CV_{i,j,k+1/2} \left( \phi_{f,i,j,k+1} - \phi_{f,i,j,k} - BUOY_{i,j,k+1/2} \Delta v_{k+1/2} \right)$$

$$Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k}$$

$$= SS_{i,j,k} \frac{\phi_{f,i,j,k}^t - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t} \Delta V$$

The term  $Q_{ext,i,j,k}$

Takes into account all external sources

Rewriting the term:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

The variable density groundwater flow equation

$$Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k}$$

$$= SS_{i,j,k} \frac{\phi_{f,i,j,k}^t - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t} \Delta V$$

and:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{f,i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

gives:

$$\begin{aligned} & CV_{i,j,k-1/2} \phi_{f,i,j,k-1}^{t+\Delta t} + CC_{i-1/2,j,k} \phi_{f,i-1,j,k}^{t+\Delta t} + CR_{i,j-1/2,k} \phi_{f,i,j-1,k}^{t+\Delta t} \\ & + (-CV_{i,j,k-1/2} - CC_{i-1/2,j,k} - CR_{i,j-1/2,k} - CR_{i,j+1/2,k} - CC_{i+1/2,j,k} - CV_{i,j,k+1/2} + HCOF_{i,j,k}) \phi_{f,i,j,k}^{t+\Delta t} \\ & + CR_{i,j+1/2,k} \phi_{f,i,j+1,k}^{t+\Delta t} + CC_{i+1/2,j,k} \phi_{f,i+1,j,k}^{t+\Delta t} + CV_{i,j,k+1/2} \phi_{f,i,j,k+1}^{t+\Delta t} = RHS_{i,j,k} \end{aligned}$$

with:

$$HCOF_{i,j,k} = P_{i,j,k} - SC1_{i,j,k} / (\Delta t)$$

$$RHS_{i,j,k} = -Q'_{i,j,k} - SC1_{i,j,k} \phi_{f,i,j,k}^t / (\Delta t)$$

$$- CV_{i,j,k-1/2} BUOY_{i,j,k-1/2} \Delta v_{k-1/2} + CV_{i,j,k+1/2} BUOY_{i,j,k+1/2} \Delta v_{k+1/2}$$

$$SC1_{i,j,k} = SS_{i,j,k} \Delta V$$

## Equation of state

$$BUOY_{i,j,k-1/2} = \left( \frac{(\rho_{i,j,k-1/2} + \rho_{i,j,k})/2 - \rho_f}{\rho_f} \right)$$

$$\rho_{i,j,k} = \rho_f \left( 1 + \frac{\rho_s - \rho_f}{\rho_f} \frac{C_{i,j,k}}{C_s} \right)$$

or

$$\rho_{i,j,k} = \rho_f (1 + \beta C_{i,j,k})$$

## Some existing 3D codes which simulate variable density groundwater flow in porous media:

HST3D (*Kipp, '86*)  
 METROPOL (*Sauter, '87*)  
 FEFLOW (*Diersch, '94*)  
 MVAEM (*Strack, '95*)  
 D3F (*Wittum et al., '98*)  
 MOCDENS3D (*Oude Essink, '98*)

SWICHA (*Huyakorn et al., '87*)  
 SWIFT (*Ward, '91*)  
 FAST-C 3D (*Holzbecher, '98*)  
 MODFLOW+MT3D96 (*Gerven, '98*)  
 SEAWAT (*Guo & Bennett, '98*)  
 SUTRA (beta-version, *Voss, '02*)

## Restrictions 3D salt water intrusion modelling in 2011

- the data problem:

- not enough hydrogeological data available
- e.g. the initial density distribution
- especially important issue in data-poor countries

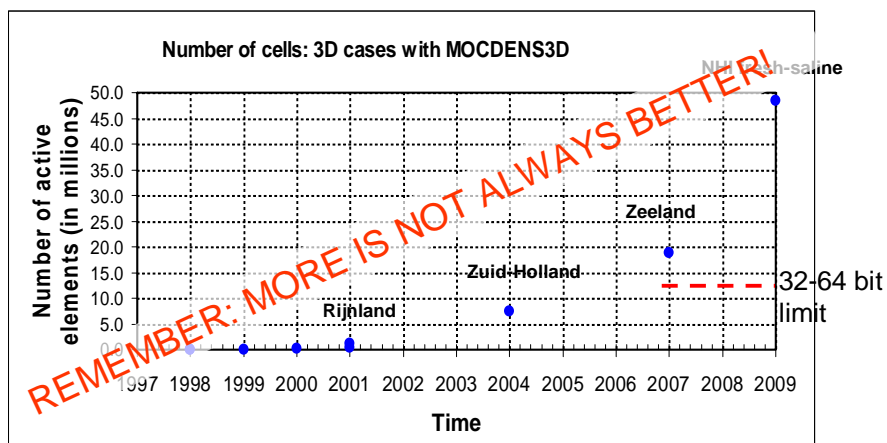
- the computer problem:

- modelling transient 3D systems: computer only good enough at high costs

- the numerical dispersion problem:

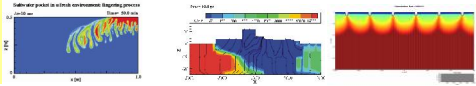
- numerical dispersion is large in case of coarse grid

**DO NOT DO THIS AT HOME (IF YOU HAVE NOT ENOUGH DATA)**

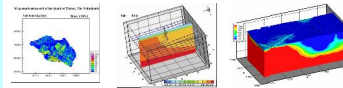


## Different model cell sizes to consider several phenomena

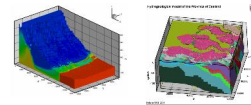
**Sub-local:** fingering, salty sand boils  
Sri Lanka (Tsunami 2004), Zandmotor  
**cell size=1cm-1m**



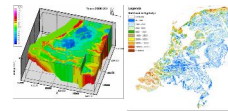
**Local:** rainwaterlenses, heat-cold  
Tholen, Schouwen-Duiveland  
**cell size=5-25m**



**Regional:**  
Zeeland, Gujarat/India, Philippines  
**cell size=100m**



**National:** salt load  
Zuid-Holland, NHI  
**cell size=250m-1km**



### Goal:

To take largest cell size possible to accurately model relevant salinisation processes

## Modelling effect climate change on

### Modelling: fresh-salt groundwater

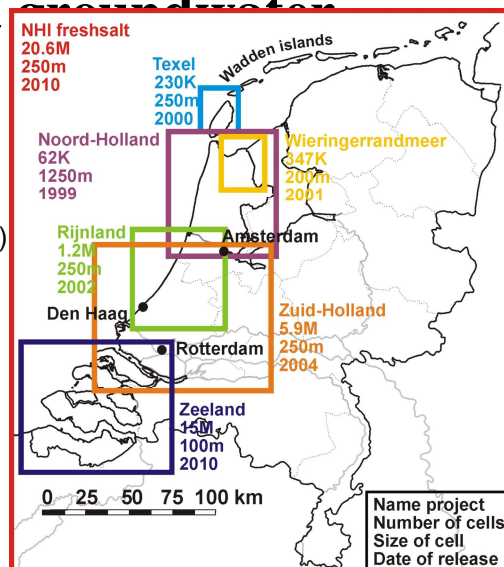
- variable-density
- 3D, non-steady
- groundwater flow
- coupled solute transport

### Code:

MOCDENS3D (MODFLOW family)  
similar to SEAWAT

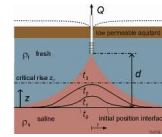
### Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- land subsidence
- changing extraction rates
- adaption measures



## Fields of application of fresh-saline groundwater models

- Water system analysis in brackish-saline environments (salt boils, freshwater lenses)
- Quantifying effects of climate change & sea level rise
- Drinking water issues: upconing saline groundwater under extraction wells
- Developing measurements to stop salinization groundwater systems (e.g. fresh keeper, coastal collectors, freshwater storage underground)
- Impact of the disasters as tsunamis on fresh groundwater resources
- Submarine Groundwater Discharge (marine water pollution, Harmful Algae)



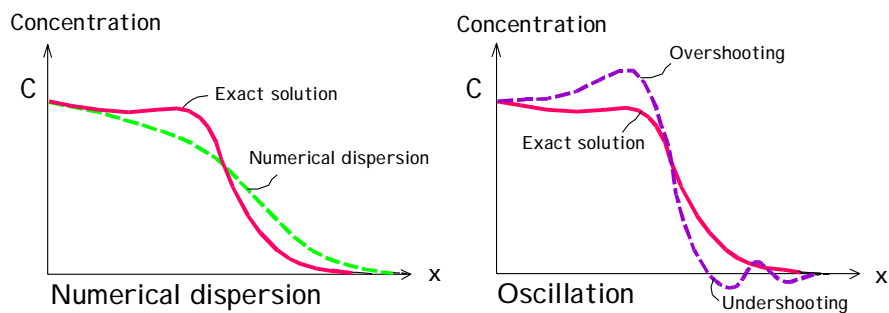
## A good initial density distribution is essential

- Because groundwater and solute transport are coupled, the density influences groundwater velocities
- Numerous density measurements are necessary to get a reliable 3D density matrix

### 'Procedure' to improve initial density distribution

- Implement all chloride data
  - Analyses, Borehole, VES, Airborne techniques (HEM, SkyTem)
  - Better old than nothing
  - Better VES then nothing
- Interpolate and extrapolate
  - Sea = easy (salt)
  - Inland = fresh?
- Start with simulation (10/20/30 years) with mol.diffusion\*1000 to smooth out artificial densities

### Numerical dispersion and oscillation



$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2} \quad C_i^{t+\Delta t} = C_i^t + \frac{D\Delta t}{\Delta z^2} (C_{i+1}^t - 2C_i^t + C_{i-1}^t) \quad \frac{D\Delta t}{\Delta z^2} < 0.5$$

## Numerical dispersion problem (I)

To solve the advection-dispersion equation, standard finite difference and element techniques should consider the following spatial discretisation criterion:

$$\text{Peclet number } Pe \leq 2 \text{ to } 4$$

$$\text{where: } Pe = \left| \frac{V\Delta x}{D_h} \right|$$

- $V$  = effective velocity [L/T]
- $\Delta x$  = dimension grid cell [L]
- $D_h$  = hydrodynamic dispersion [L<sup>2</sup>/T]

## Numerical dispersion problem (II)

For advection dominant groundwater flow, the Peclet number can be rewritten as:

$$\Delta x \leq 2\alpha_L \text{ to } 4\alpha_L$$

where  $\alpha_L$  = longitudinal dispersivity [L]

What does that mean?

If  $\alpha_L$  is small, then  $\Delta x$  should be small too!!

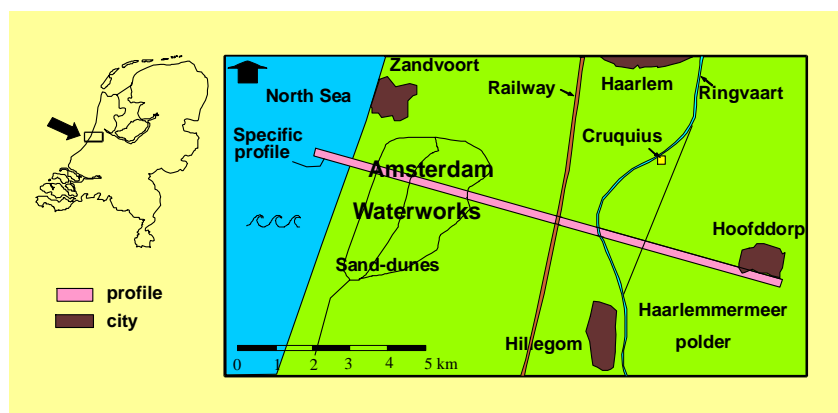


### Numerical dispersion problem (III)

Now follows an transient salt water intrusion case to demonstrate why in many coastal aquifers the longitudinal dispersivity  $\alpha_L$  [L] should be small

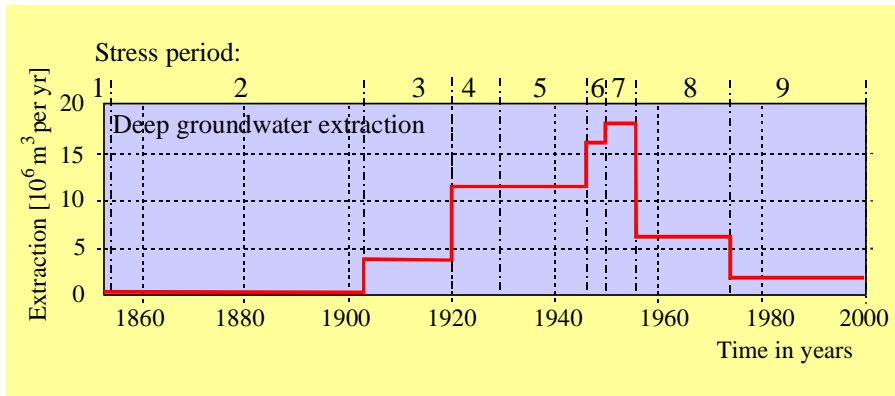
### Effect of $\alpha_L$ on the salinisation of the aquifer (I)

Position profile through Amsterdam Waterworks, Rijnland polders and Haarlemmeer polder



## Effect of $\alpha_L$ on the salinisation of the aquifer (II)

Grondwater extractions out of the middle aquifer in the sand-dune area of Amsterdam Waterworks

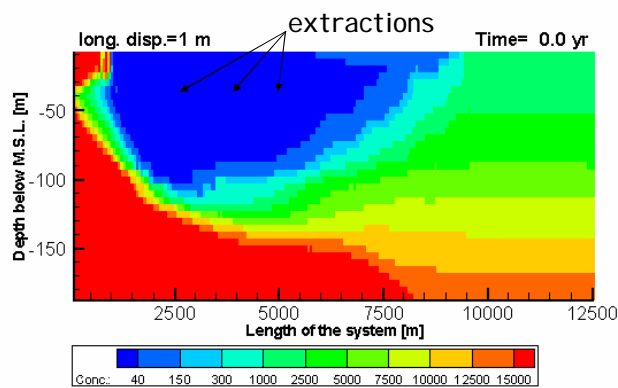


## Effect of $\alpha_L$ on the salinisation of the aquifer (III)

$\alpha_L = 1 \text{ m}$

Initial situation: 154 years ago

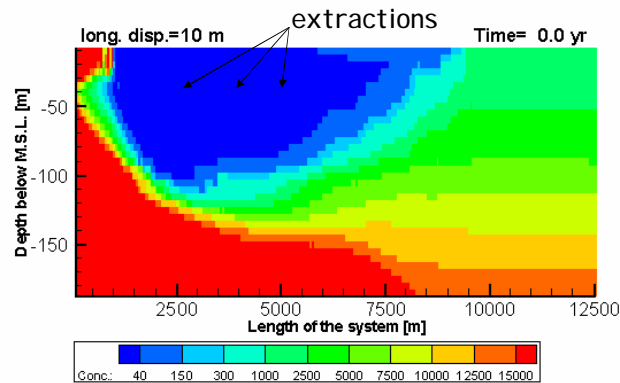
Profile Amsterdam Waterworks-Haarlemmemeerpolder



Effect of  $\alpha_L$  on the salinisation of the aquifer (IV) $\alpha_L = 10$  m

Initial situation: 154 years ago

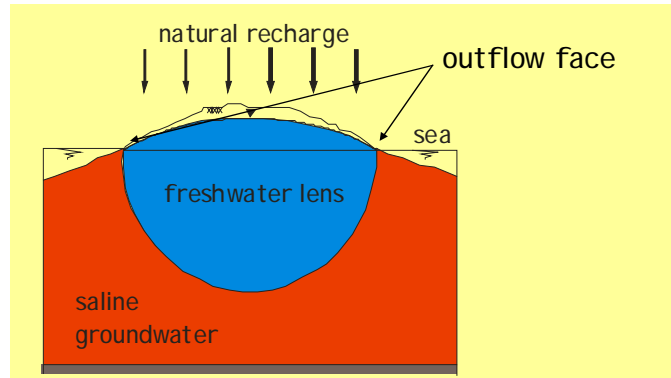
## Profile Amsterdam Waterworks-Haarlemmemeerpolder



## Difficulties with variable density groundwater flow

- Initial density distribution (effects on velocity field) !
- Velocities freshwater lens at the outflow face near the sea
- Boundary conditions (especially concentration boundaries)
- Choice of element size
- Length of flow time step to recalculate groundwater flow

## Outflow face at the coast is difficult to model



Flow converges and thus velocities are very high at the outflow face

This is numerically difficult to handle

## A good initial density distribution is essential

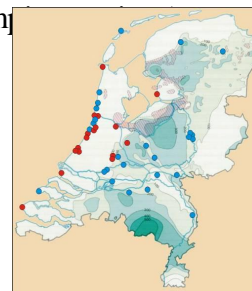
- Because groundwater and solute transport are coupled, the density influences groundwater velocities
- Numerous density measurements are necessary to get a reliable 3D density matrix

## 'Procedure' to improve initial density distribution

- Implement all chloride data
  - Analyses, Borehole, VES
  - Better old than nothing
  - Better VES than nothing
- Interpolate and extrapolate
  - Sea = easy (salt)
  - Inland = fresh?
- Start with simulation (10/20/30 years) with  $\text{mol.diffusion} * 1000$  to smooth out artificial densities

## Monitoring salt in groundwater

- Why monitoring?
  - Mapping salt concentrations in the groundwater
  - Detection of trends (upconing near pumps)
  - System and process knowledge
  - Input for a groundwater model



- Methods:
  1. Direct: water sample available
  2. Indirect: conductance of the subsoil

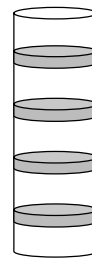
- Pumping stations with salinisation
- Pumping stations closed due to salinisation

## Monitoring salt in groundwater: Direct methods

Method	Advantage	Disadvantage
1. Observation well	<ul style="list-style-type: none"> <li>•High accuracy</li> <li>•Detection trends</li> </ul>	<ul style="list-style-type: none"> <li>•Costly</li> <li>•Point measurement</li> </ul>
2. Well screens in observation well	<ul style="list-style-type: none"> <li>•High accuracy</li> <li>•Detection trends</li> <li>•High vertical resolution</li> </ul>	<ul style="list-style-type: none"> <li>•Costly</li> </ul>
3. Sediment sample (extraction milliliters of water)	<ul style="list-style-type: none"> <li>•High accuracy</li> <li>•High vertical resolution</li> </ul>	<ul style="list-style-type: none"> <li>•Very costly and time consuming</li> </ul>



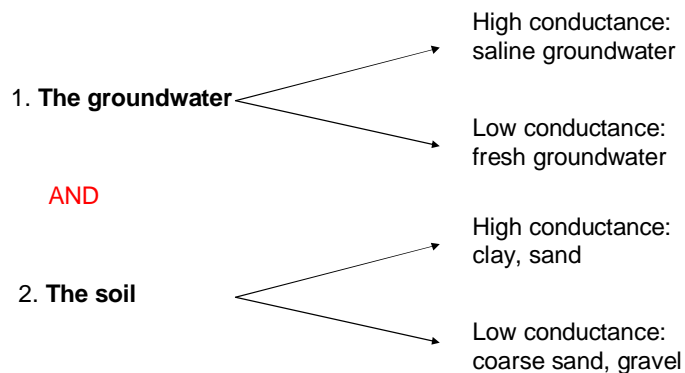
Direct methods 1 and 2



Source: V. Post, 2007

## Monitoring salt in groundwater: Indirect methods

Indirect methods measure the **conductance** of:



Hence information about the lithology (sand, clay etc) is needed!

Source: V. Post, 2007

## Monitoring salt in groundwater: Indirect methods

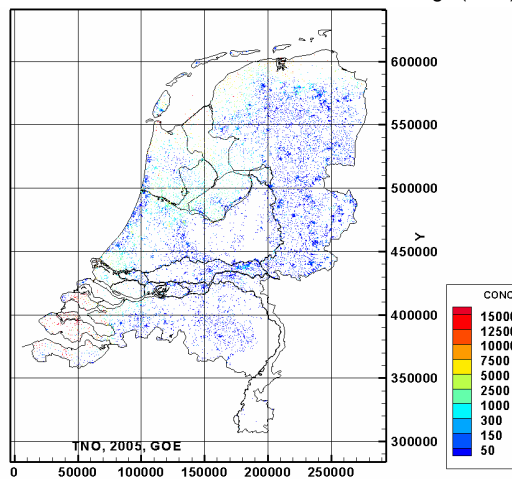
Method	Advantages	Disadvantages
1. Electrical conductance measurements	<ul style="list-style-type: none"> <li>•High resolution (3D)</li> <li>•Depth ~200 m</li> </ul>	<ul style="list-style-type: none"> <li>•Time consuming</li> </ul>
2. Electromagnetic measurements	<ul style="list-style-type: none"> <li>•Fast</li> </ul>	<ul style="list-style-type: none"> <li>•Limited vertical resolution</li> <li>•Sensitive for underground conductors (pipes)</li> </ul>
3. Satellites	<ul style="list-style-type: none"> <li>•Suitable for large areas</li> </ul>	<ul style="list-style-type: none"> <li>•Small vertical resolution</li> <li>•Low accuracy</li> </ul>

Source: V. Post, 2007

## Method used at Deltares

Number of measurements bottom Holocene top layer :  
direct methods and Vertical Electric Soundings (VES)

- Combination of:
- Direct measurements
  - Electrical conductance measurements
    - Surface (VES)
    - Borehole



Source: Oude Essink et al (2005)

## Electrical conductance measurements

### 1. Measuring:

- **Inside a borehole**
- From surface level
- From the air



Source: TNO

Source: V. Post, 2007

## Electrical conductance measurements

### 1. Measuring:

- Inside a borehole
- **From surface level (depth ~ 200 m)**
- From the air



Source: V. Post, 2007



Source: Vitens



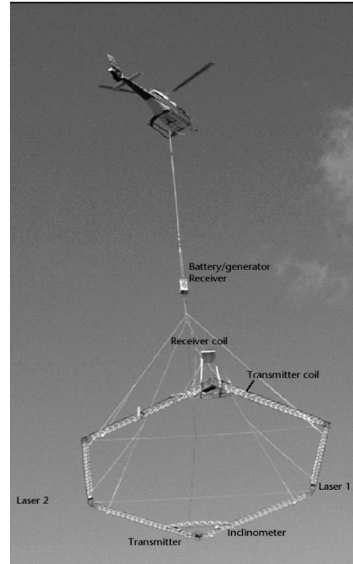
# Electrical conductance measurements

## 1. Measuring:

- Inside a borehole
- From surface level
- **From the air**



Source: V. Post, 2007



# Monitoring salt in groundwater: Indirect methods

- **Electrical conductance measurements**

$$\rho_s = F * \rho_w$$

$\rho_s$  = resistance subsoil & groundwater  
 $\rho_w$  = resistance groundwater  
 F = formation factor

Lithology	F
Gravel with sand	7
Coarse sand	5
Sand with silt	2 - 3
Clay	1-3*
peat	1*

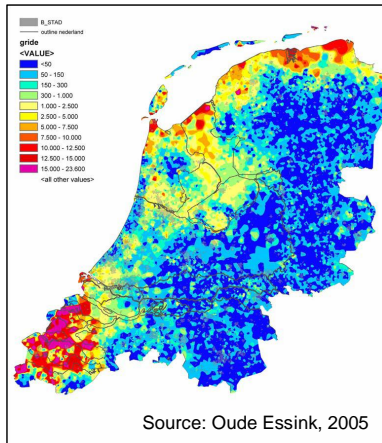
} → *F varies with the resistance of the groundwater*

If the lithology is known AND the measurement is in an aquifer  
 →  $\rho_w$  can be calculated

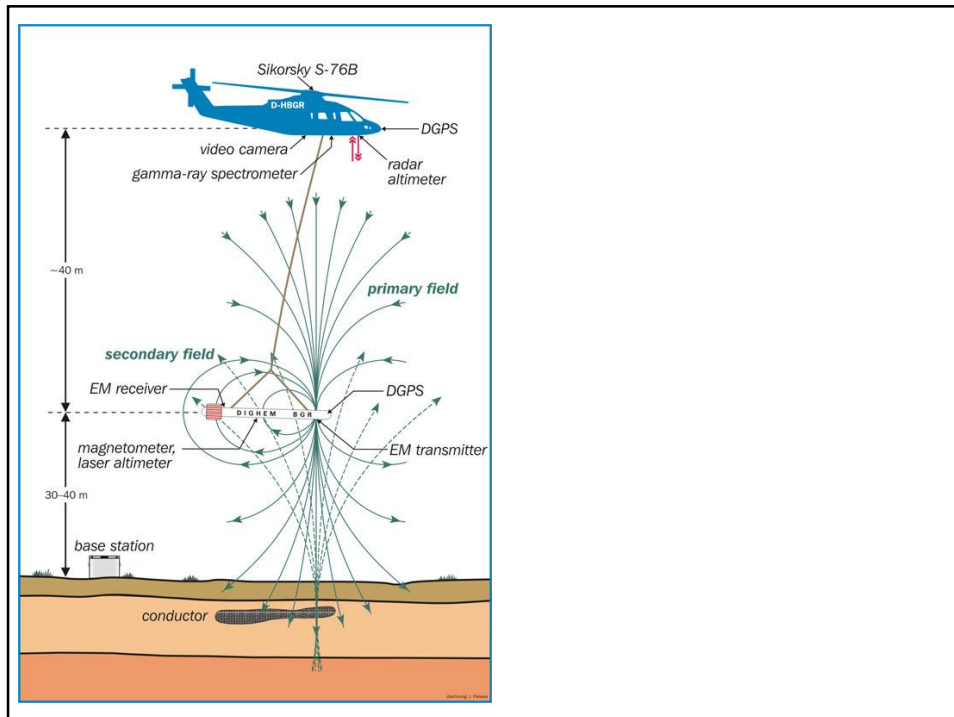
VES measurements are used in combination with borehole logging

Source: Oude Essink, 2005

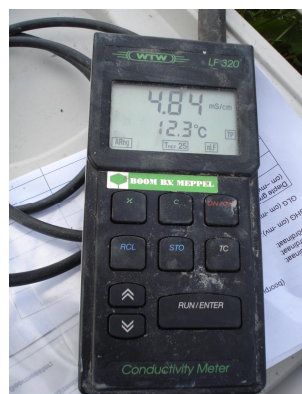
## Result: chloride concentration bottom Holocene top layer



- Software Geological Survey of the Netherlands (TNO) is used to determine the salt concentration of the groundwater in the measurements
- Inter- and extrapolation is used to make a continuous field
- 2D Result is a combination of:
  1. Direct measurements (3500)
  2. Electrical conductance in boreholes (2000)
  3. Vertical Electric Sounding (VES) measurements (10.000)



# T-EC probe

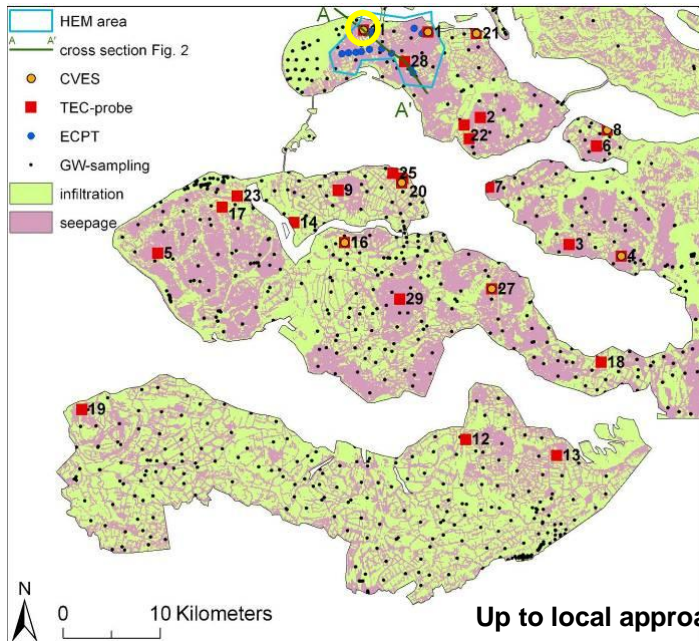


# TEC fieldwork

## Altitude measurements



# Monitoring network in our Pilot Area Zeeland



Up to local approach

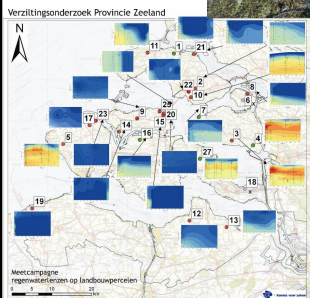
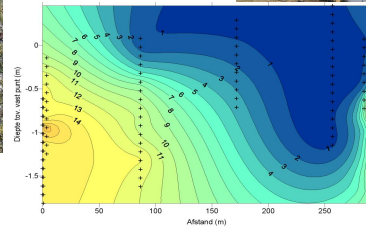
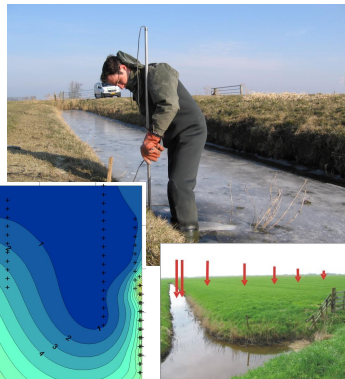
## Example: Assessing effect of climate change on salt water intrusion

### Monitoring:

- piezometric head and solute concentration
- TEC probes, CVES
- online

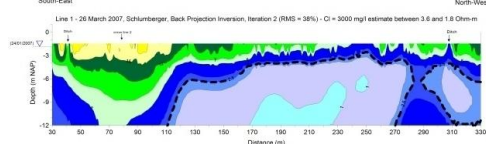
Source: Oude Essink, 2009

TEC probe

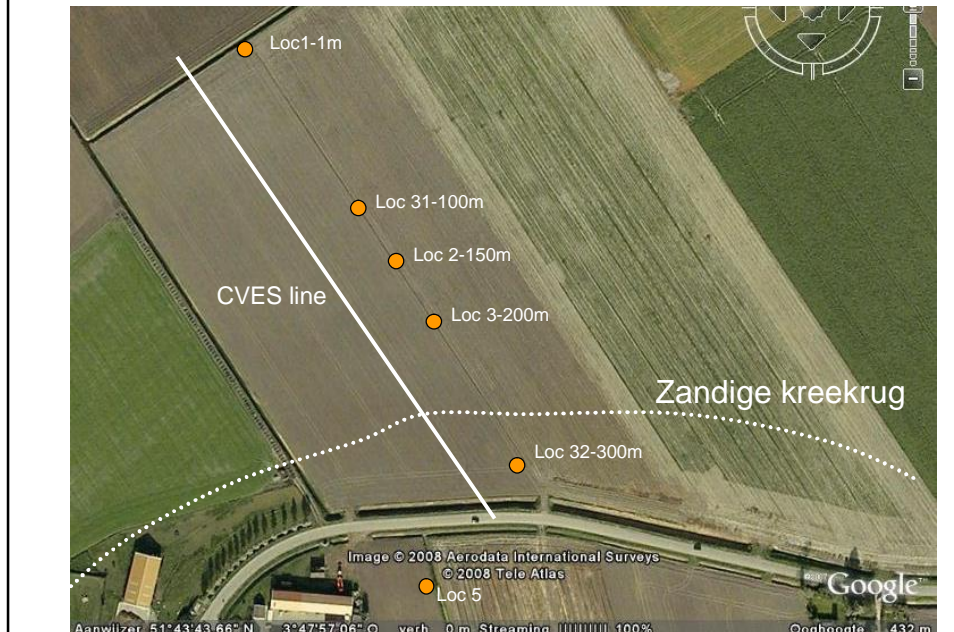


Site 11 - Renesse

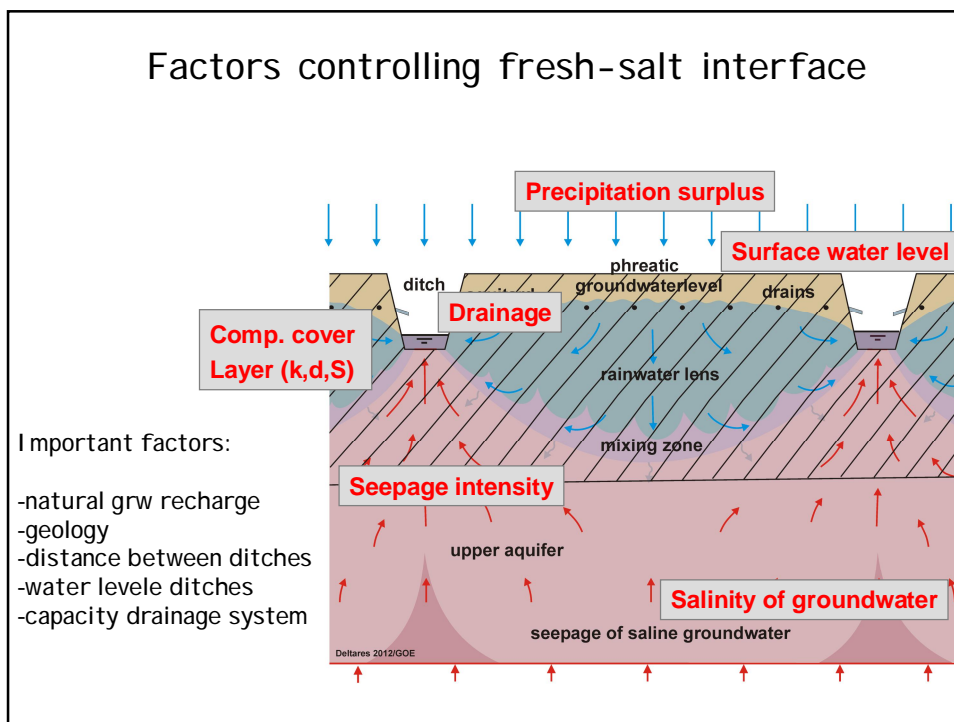
CVES



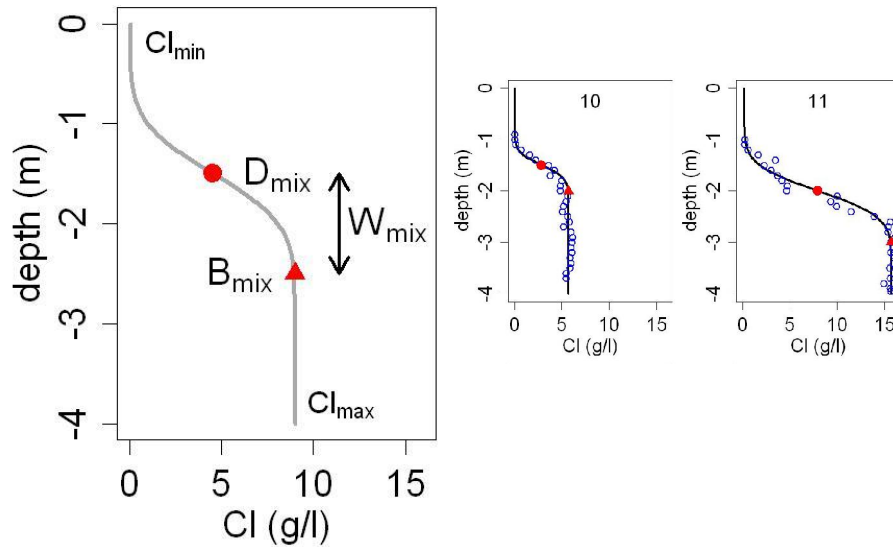
## Site 11: from infiltration to seepage



## Factors controlling fresh-salt interface

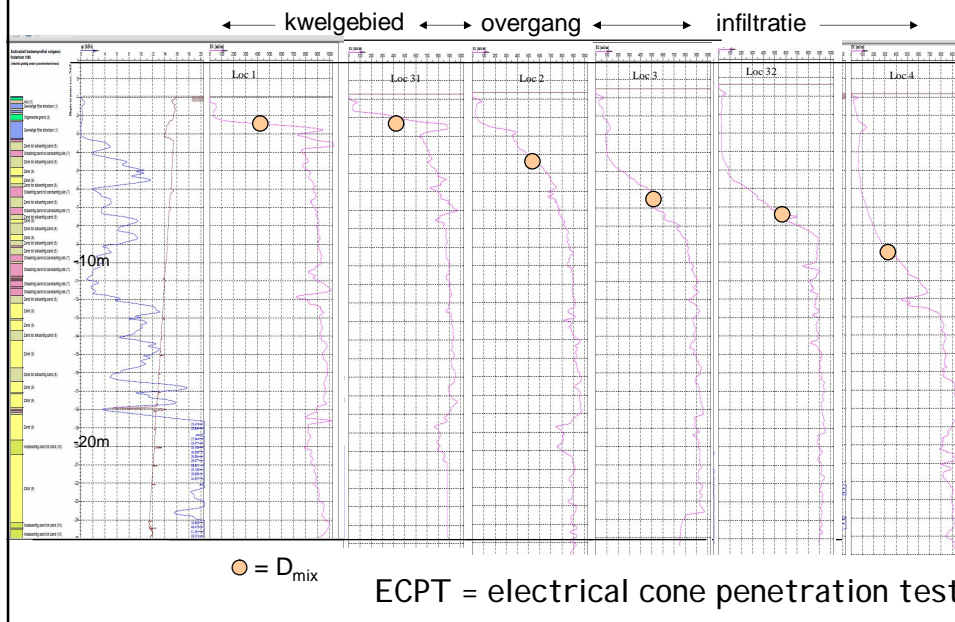


## Lens characteristics



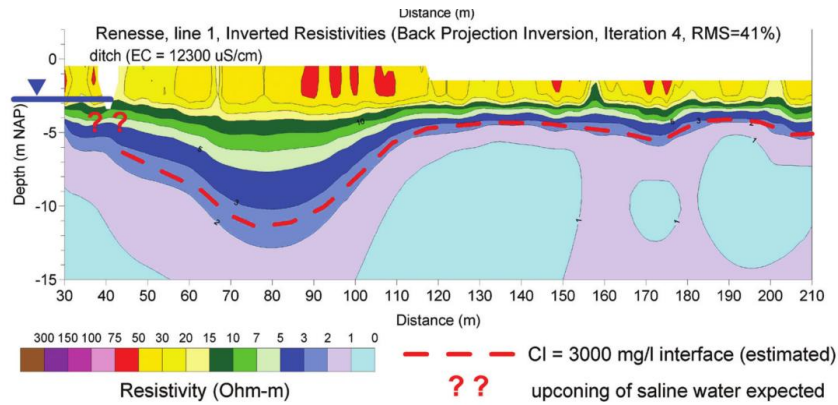
Louw, P.G.B., de Eeman, S., Siemon, B., Voortman, B.R., Gunnink, J., Baaren, E.S., van and G.H.P. Oude Essink, Shallow rainwater lenses in deltaic areas with saline seepage, *Hydrol. Earth Syst. Sci. Discuss.*, 8, 7657-7707, 2011.

## Results from ECPT's (soundings)

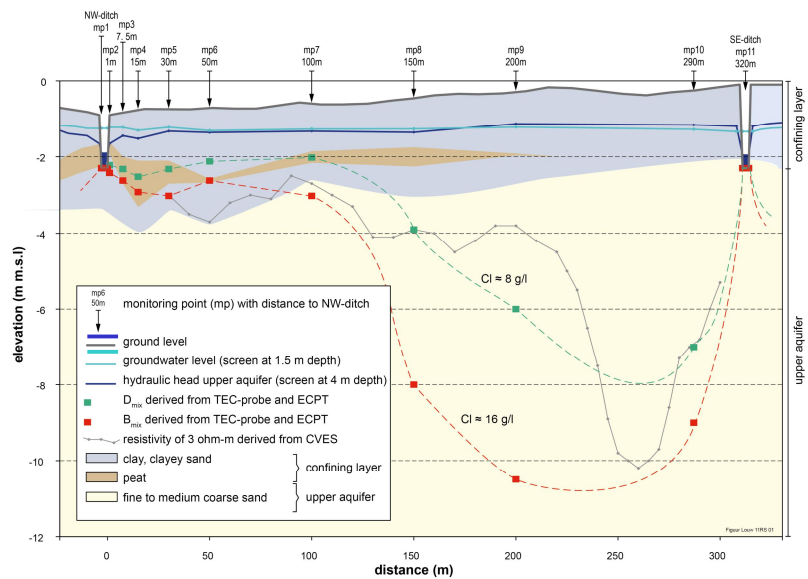


# CVES

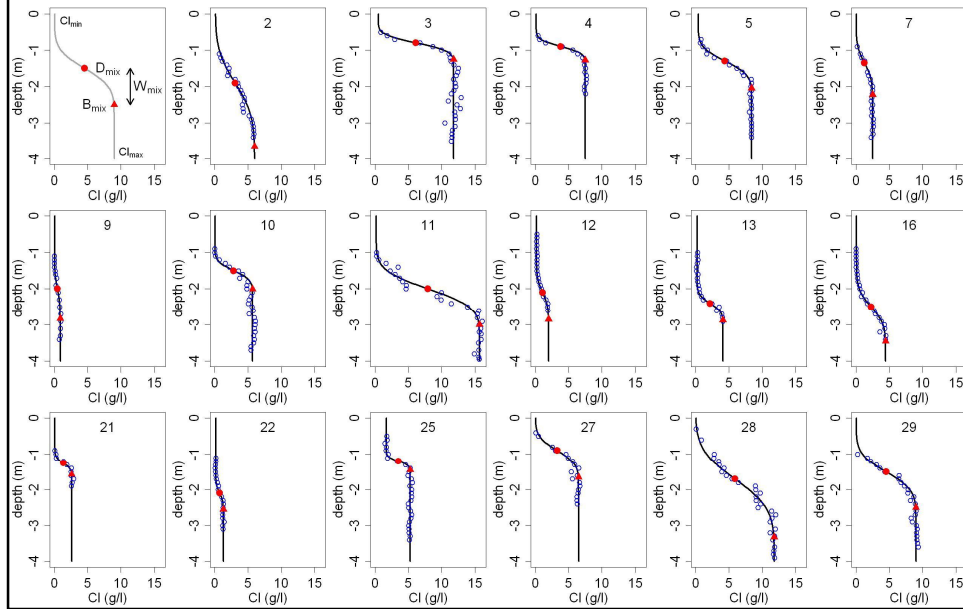
## CVES: continuous vertical electrical sounding



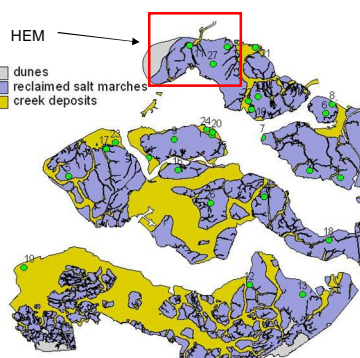
## Seepage / infiltration determines thickness rainwater lens



## TEC-probe results

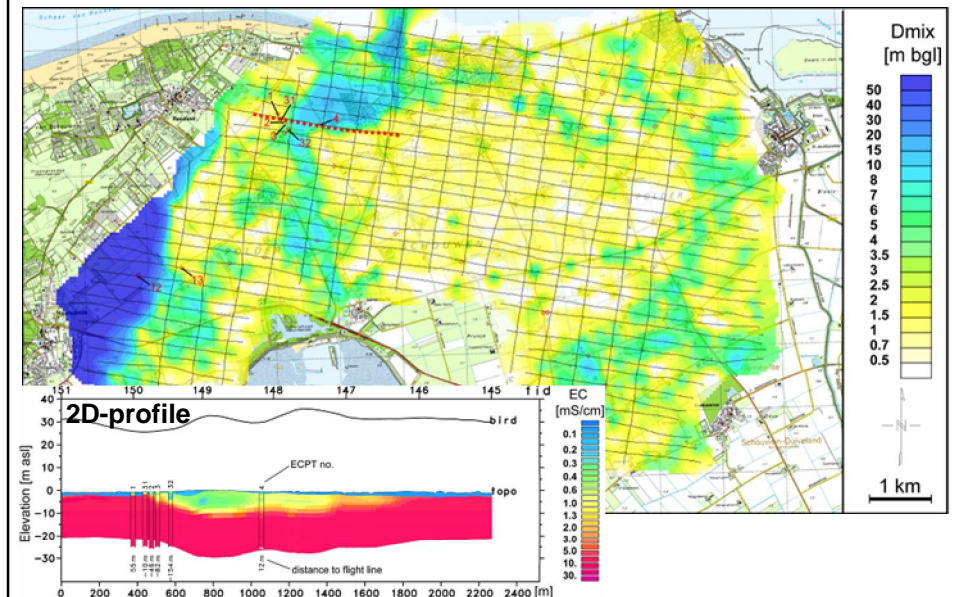


## Helicopter-EM data for mapping fresh-saline groundwater

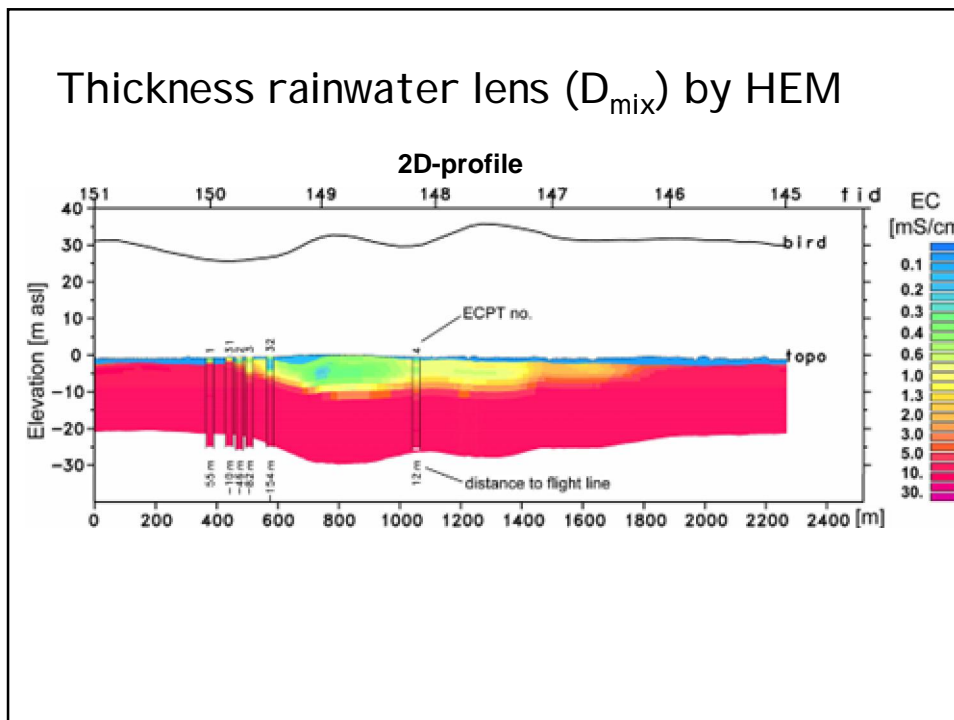




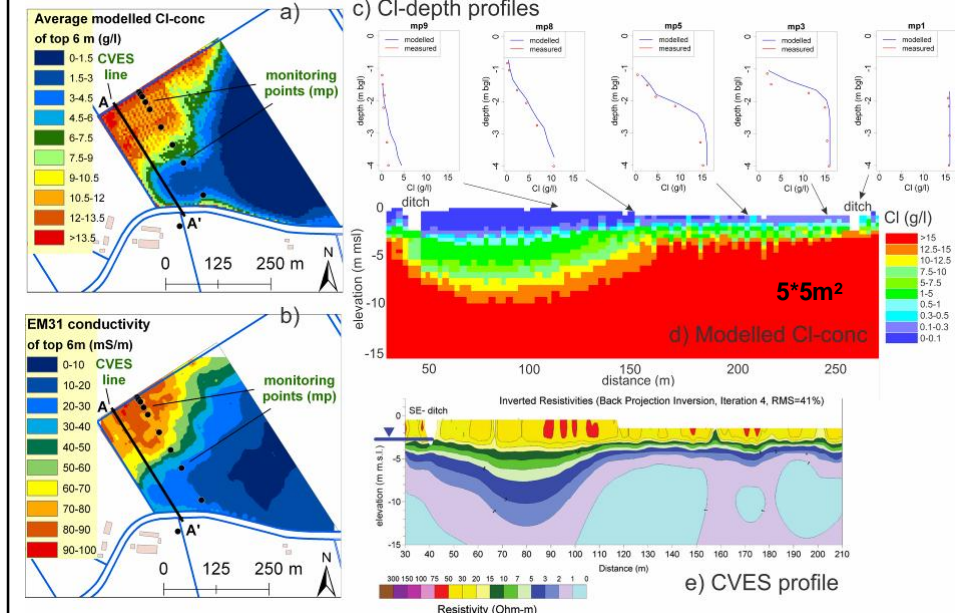
## Thickness rainwater lens ( $D_{mix}$ ) by HEM



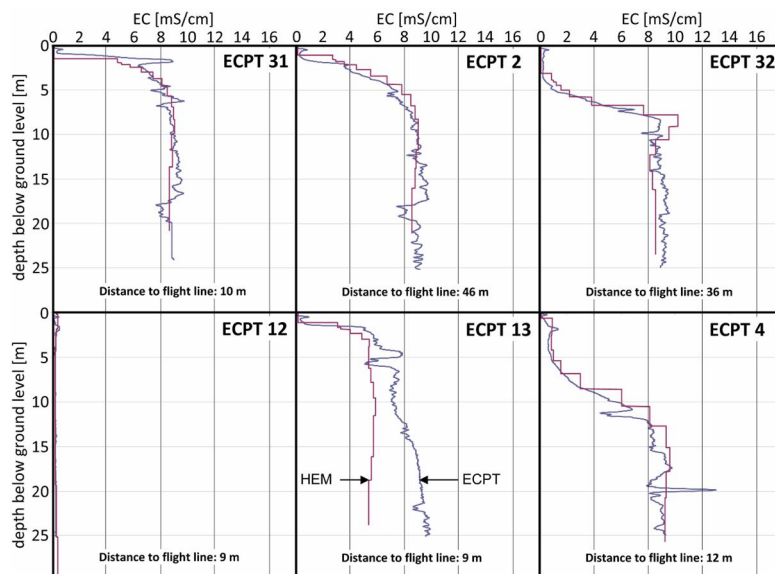
## Thickness rainwater lens ( $D_{mix}$ ) by HEM



# Comparison monitoring data with model results

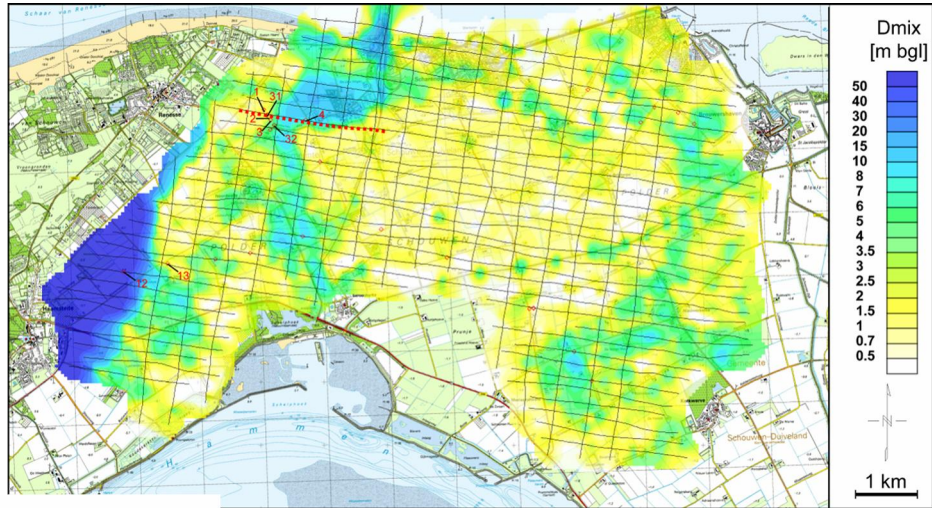


# Comparison HEM – ECPT



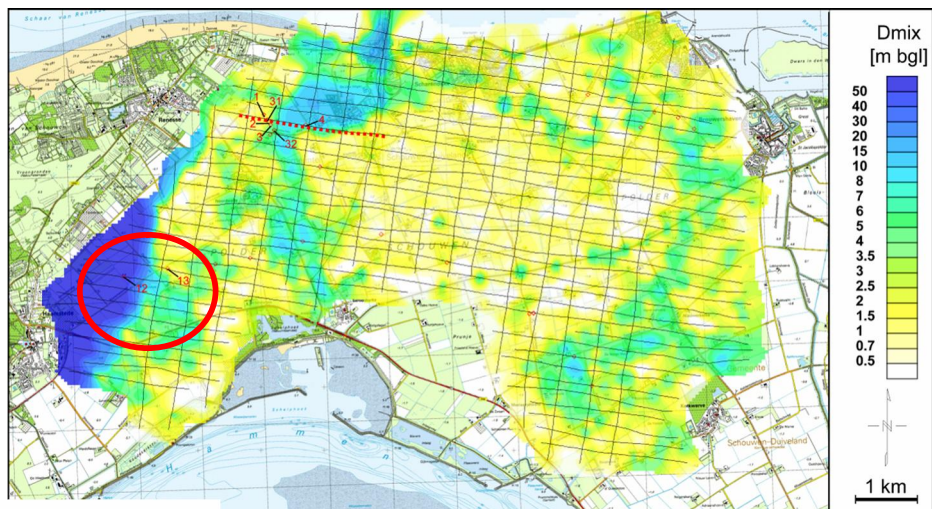
Rainwater lens thickness ( $D_{mix}$  = average position mixing zone)

mapped with HEM



Rainwater lens thickness ( $D_{mix}$  = average position mixing zone)

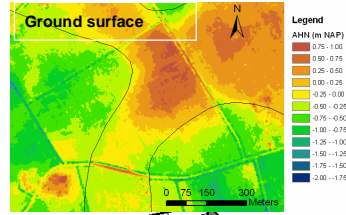
mapped with HEM



# Local 3D model of the agricultural plot

## Modelling:

- variable-density
- 3D, non-steady
- groundwater flow & coupled solute transport
- model cell size: 5\*5m<sup>2</sup>

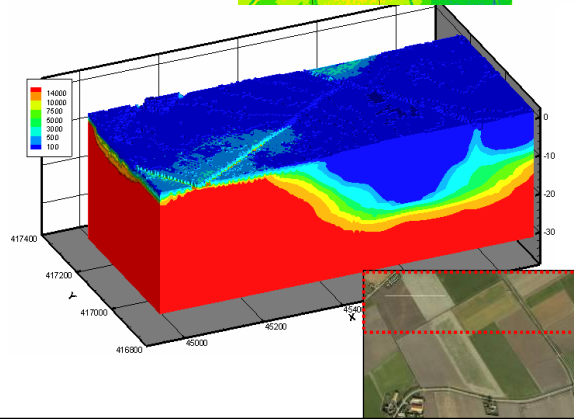


## Code:

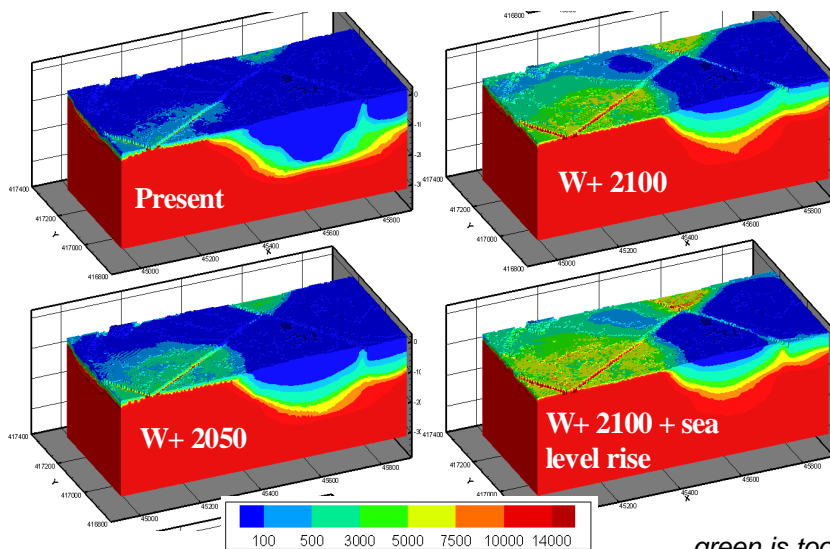
MOCDENS3D

## Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- (adaption measures)



## Local approach: simulated Cl-conc. with different CC-scenarios

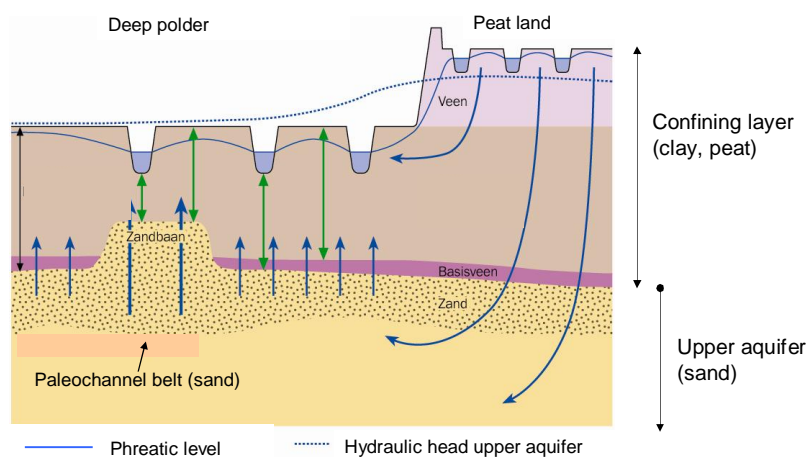


*green is too salty to grow fresh crops*

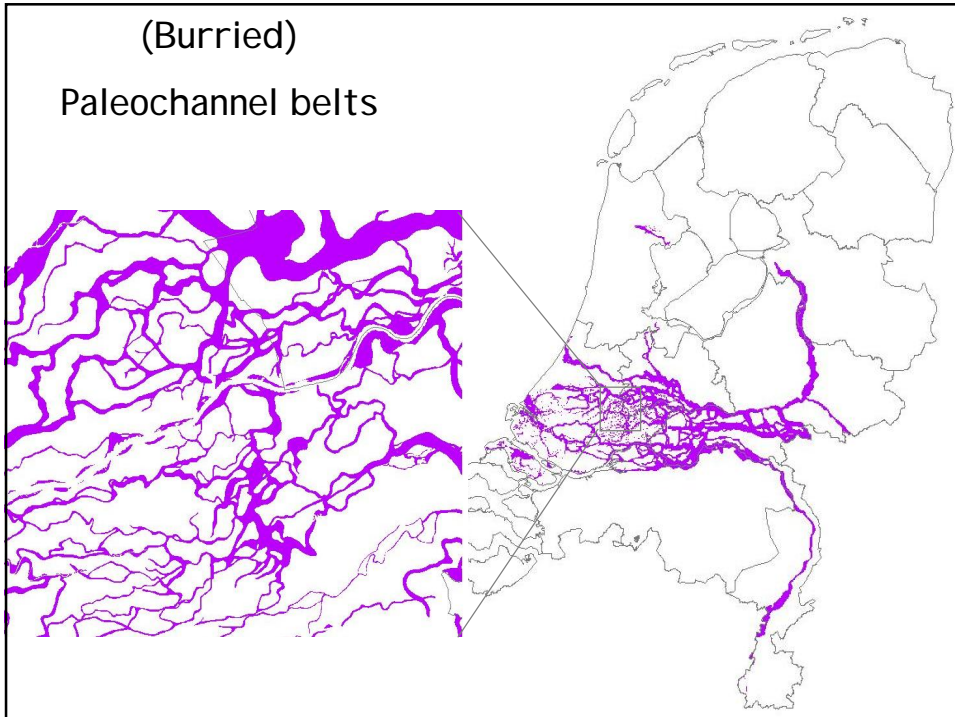
# Salty boils

Louw, P.G.B., de, Oude Essink, G.H.P., Stuyfzand, P.J., Zee, van der, S.E.A.T.M., 2010, Upward groundwater flow in boils as the dominant mechanism of salinization in deep polders, The Netherlands, *J. Hydrol.* 394, 494-506.

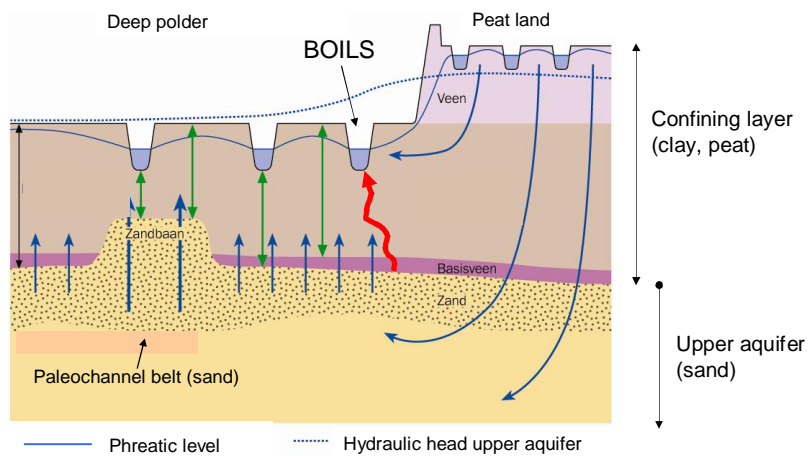
## Upward groundwater seepage in a deep polder and paleochannel belts as preferential flow paths



(Buried)  
Paleochannel belts



## Preferential seepage via boils



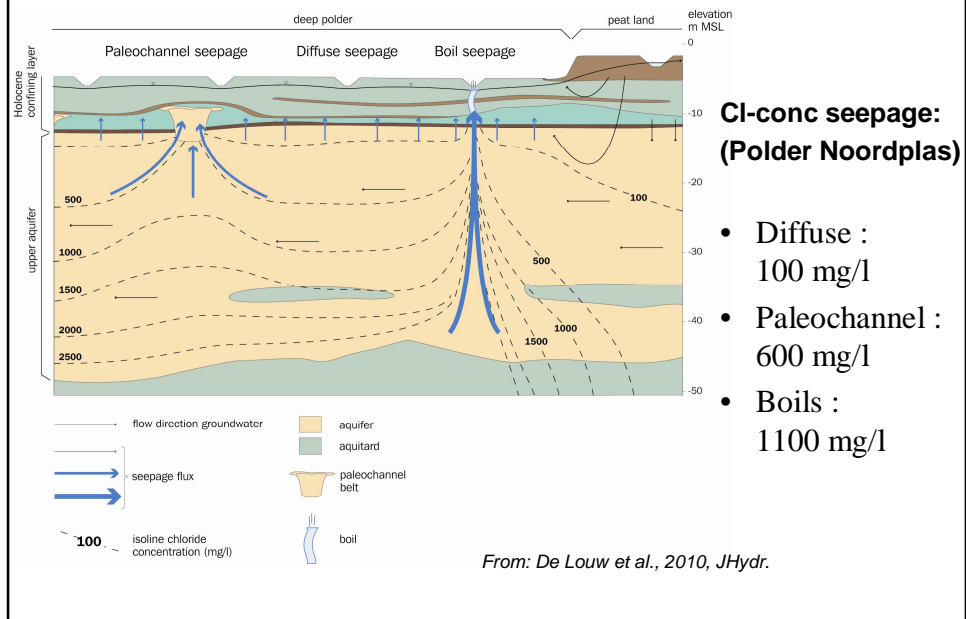
## Preferential saline seepage via boils



## Preferential saline seepage via boils



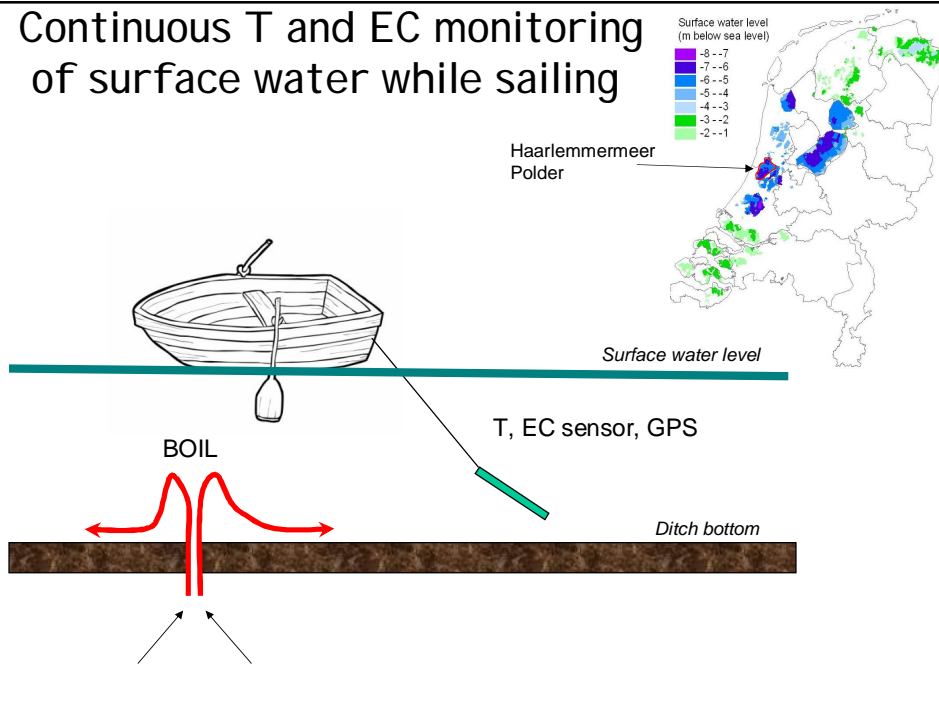
## Three types of upward groundwater seepage



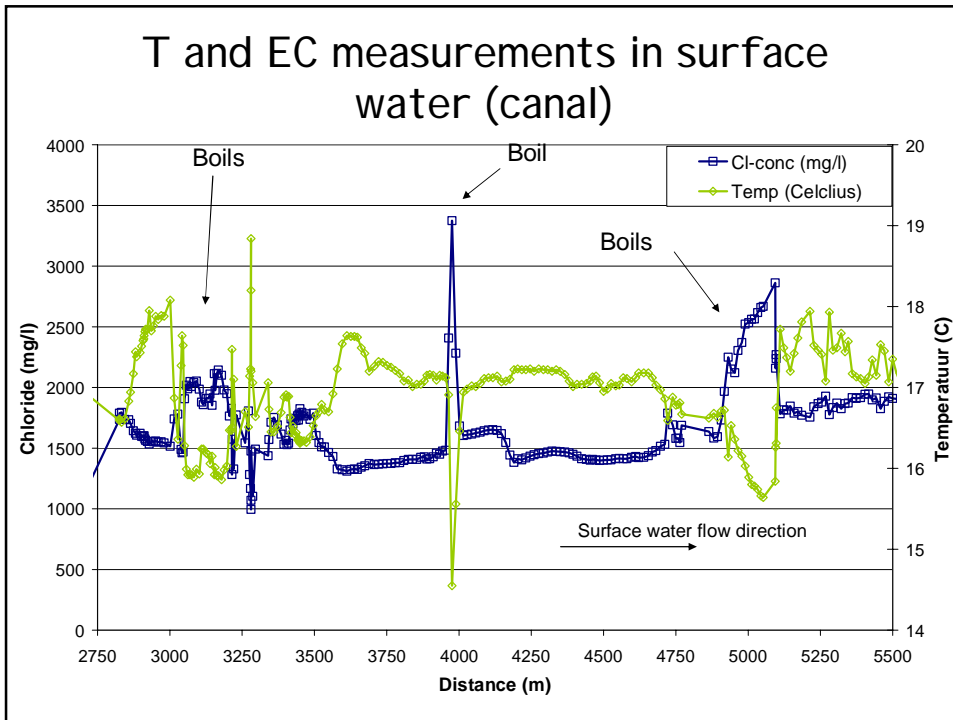


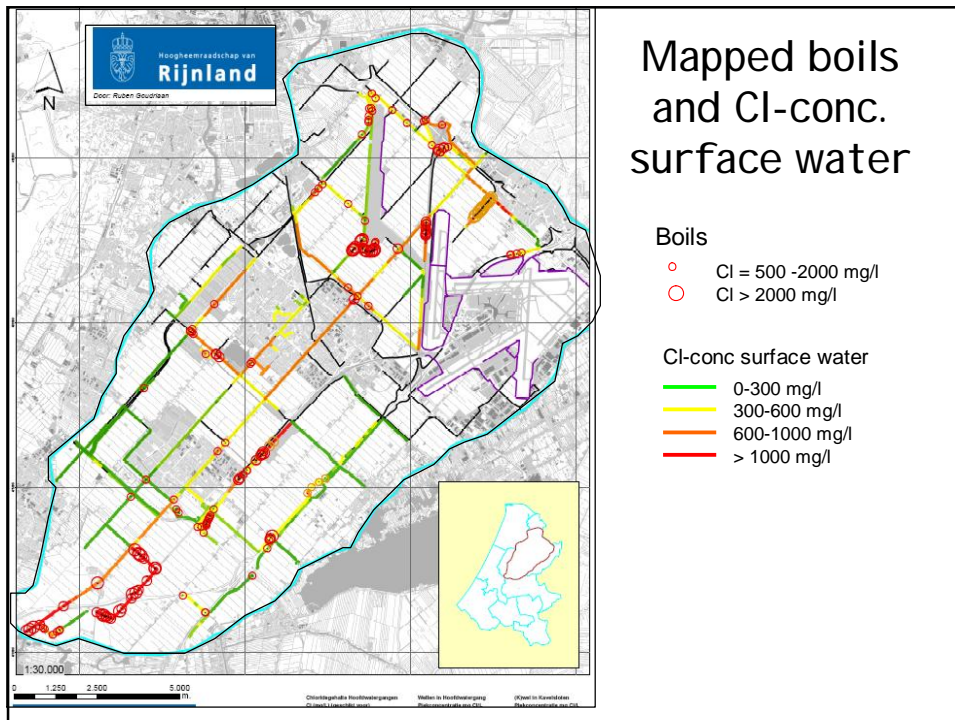


# Continuous T and EC monitoring of surface water while sailing



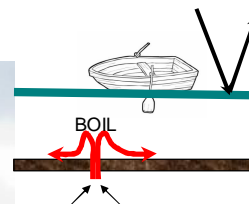
## T and EC measurements in surface water (canal)





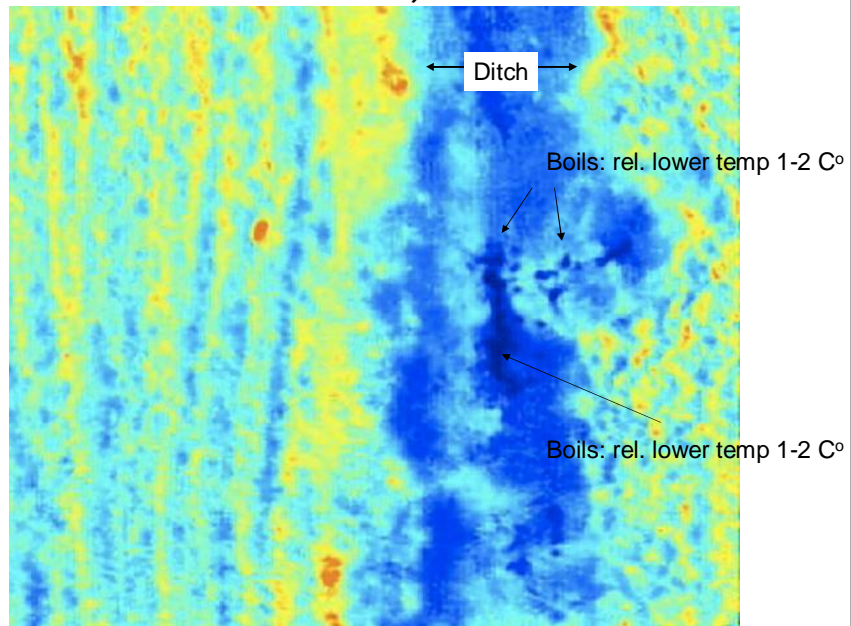
## LARS technology (TNO Industry): Thermal Infra-red

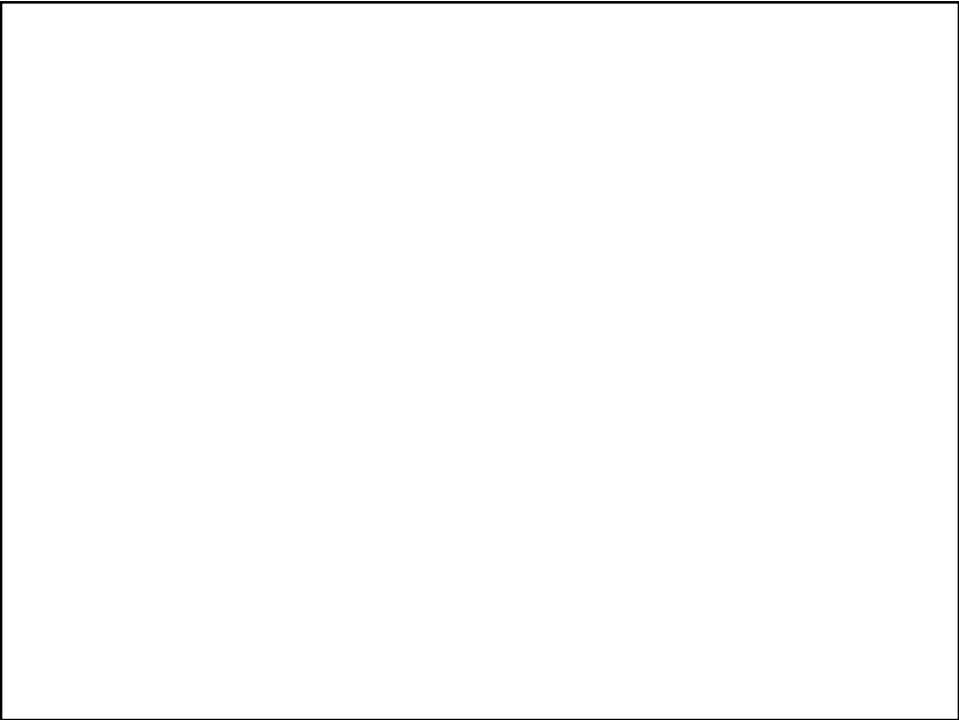
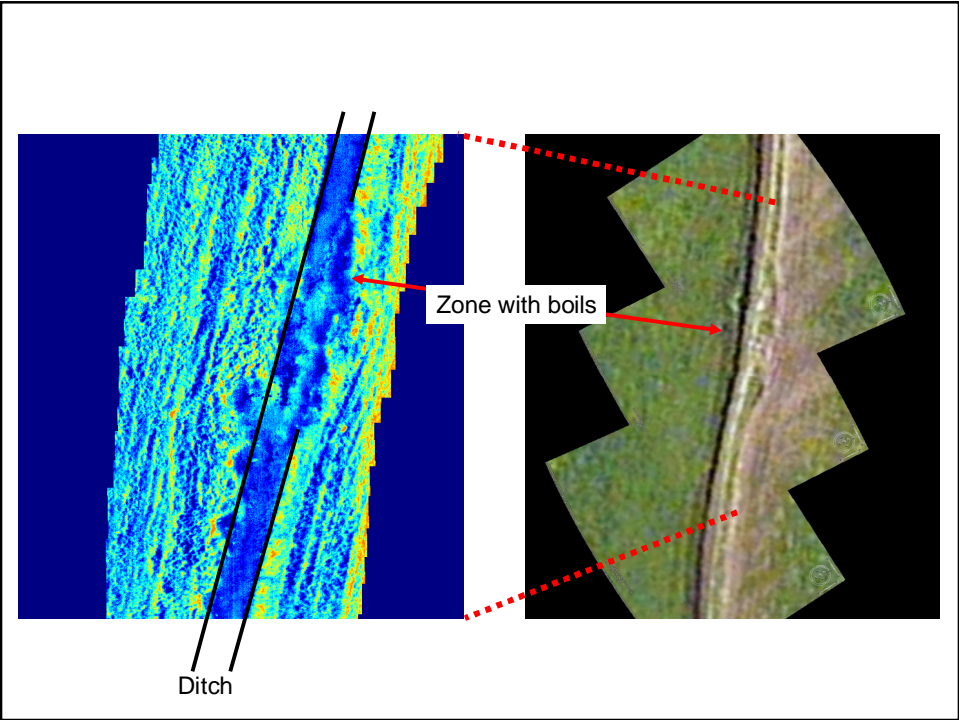
- Altitude: 0-150 m
- Temp-detection using Thermal Infra Red sensors (only surface !)





Thermal infra-red results (blue is cold, red is warm)





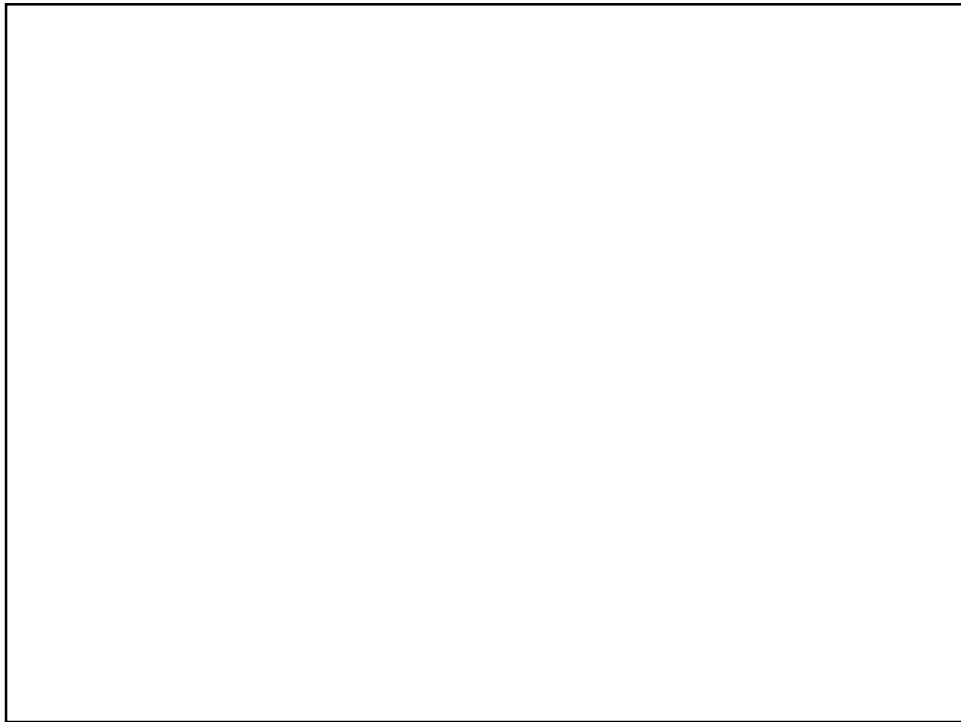
## Examples of variable-density groundwater flow

- Rotating immiscible interface
- Henry's problem
- Evolution freshwater lens
- Hydrocoin
- Salt water pocket
- Broad 14 Basin, North Sea
- Heat transport: Elder and Rayleigh=4000
- 5 Dutch 3D cases
- Freshwater lenses
- Effect of Tsunami on groundwater resources

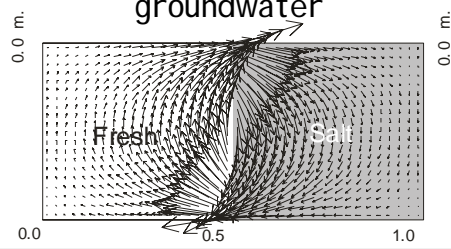
## Rotating immiscible interfaces

### Conclusion:

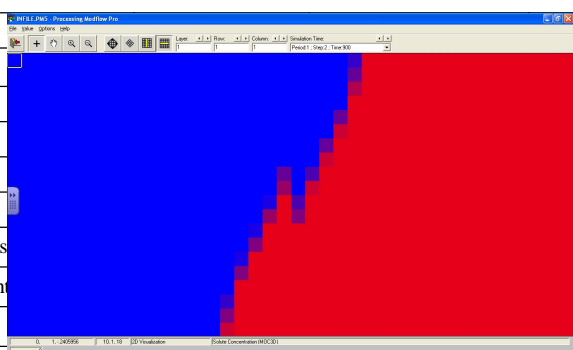
To check the variable-density component of your code, this immiscible interface benchmark can be used.



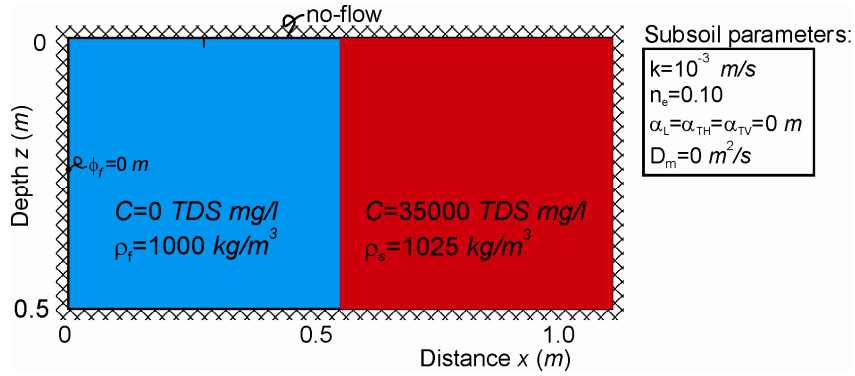
Case 1: Vertical interface between fresh and saline groundwater



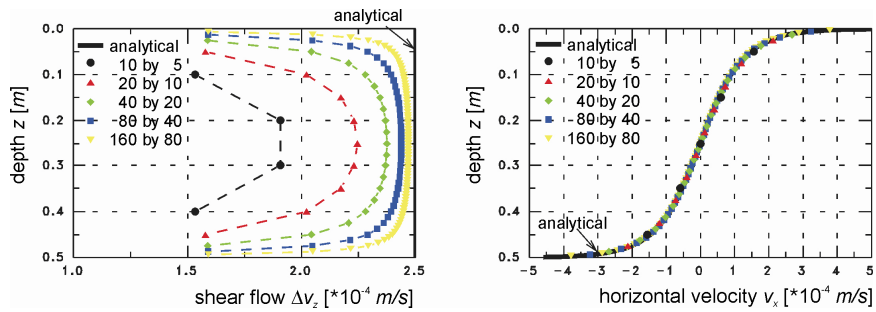
Parameters	
Layers	1
Rows	10 <sup>-3</sup> m/s
Columns	10 <sup>-5</sup> m/s
$\Delta x$	
$\Delta y$	
$\Delta z$	
Stress periods	
Initial concentration	
buoyancy	



## Vertical interface



## Effect of the number of cells on the shear flow at the interface at t=0

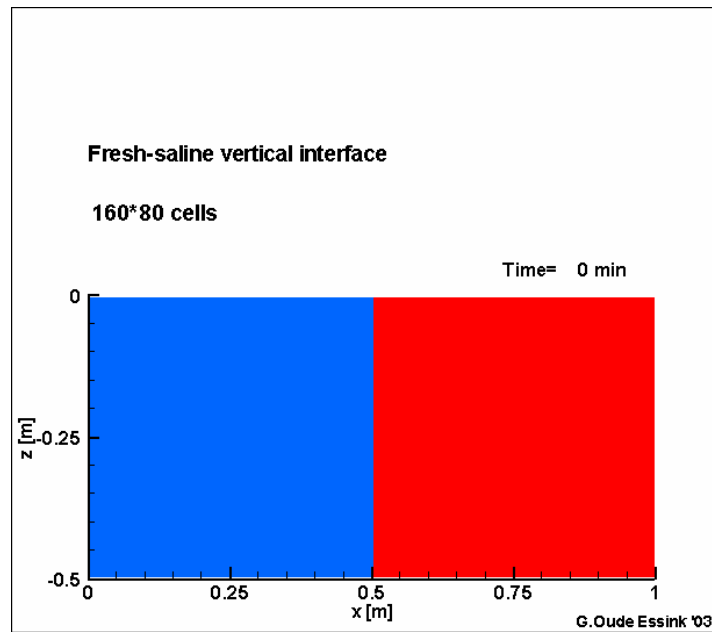


$$\Delta v_z = \frac{k}{n_e} \left( \frac{\rho_s - \rho_f}{\rho_f} \right)$$

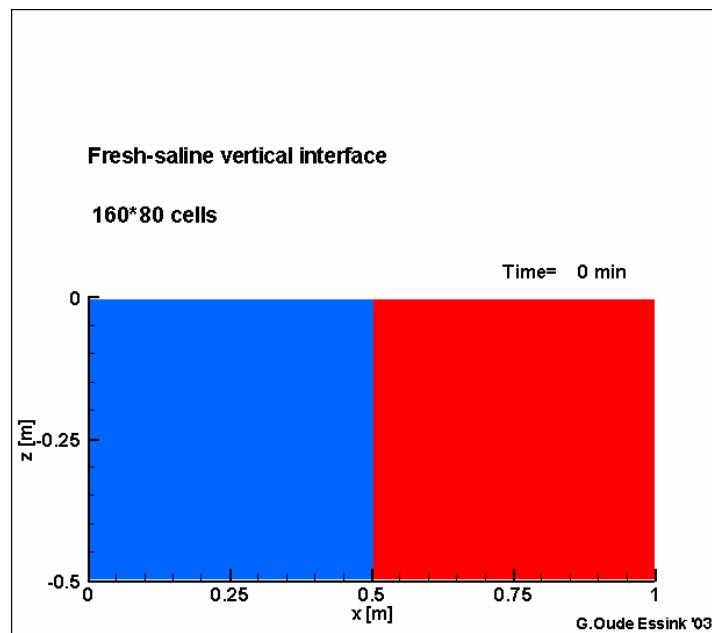
$$v_x = \frac{k}{n_e} \left( \frac{\rho_s - \rho_f}{\rho_f} \right) \frac{1}{\pi} \ln \tan \left( \frac{\pi z}{2D} \right)$$



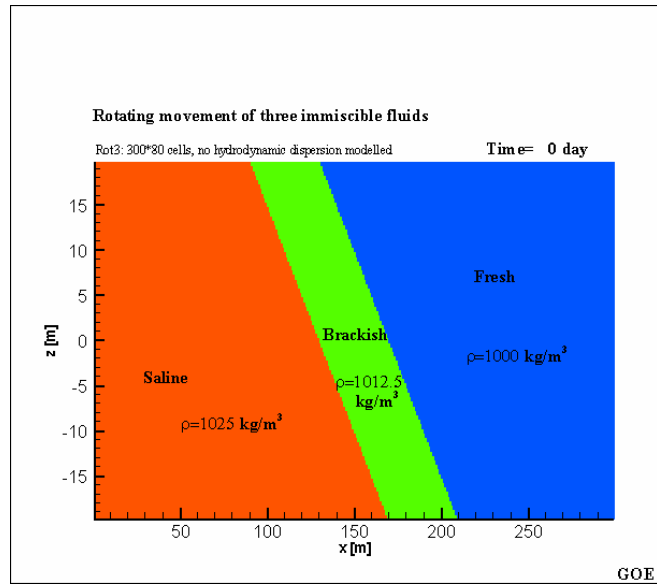
## Vertical interface



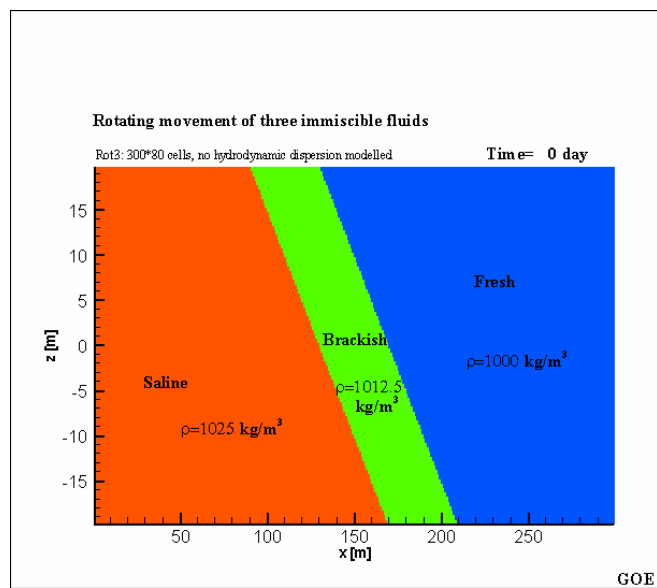
## Vertical interface



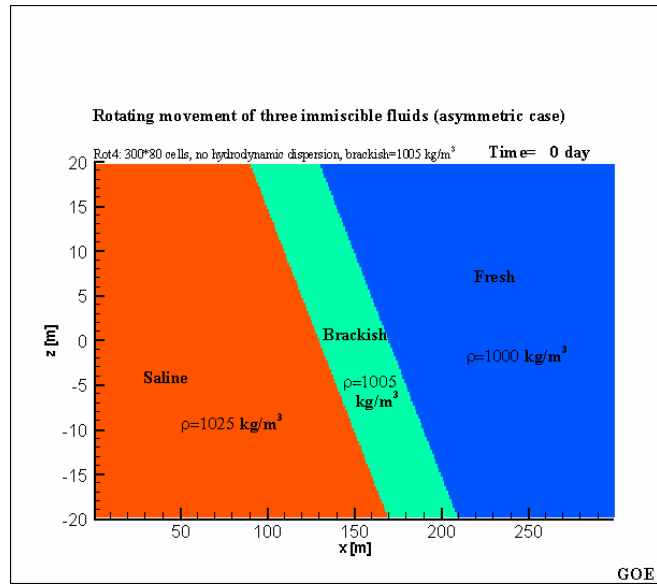
## Rotating immiscible interfaces



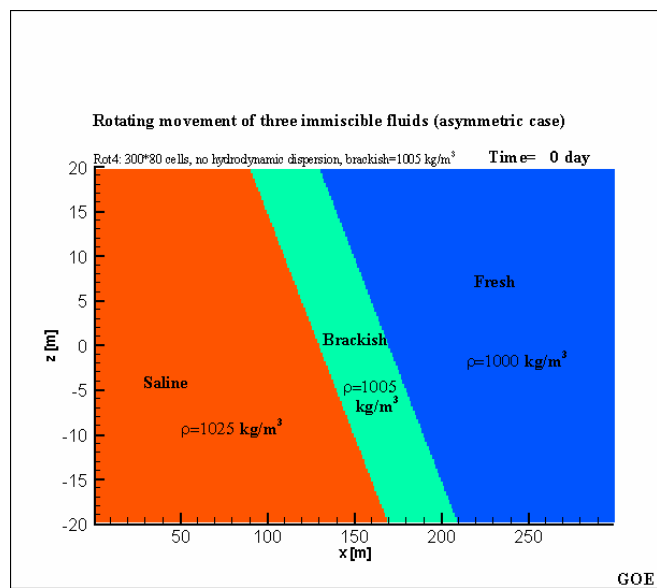
## Rotating immiscible interfaces

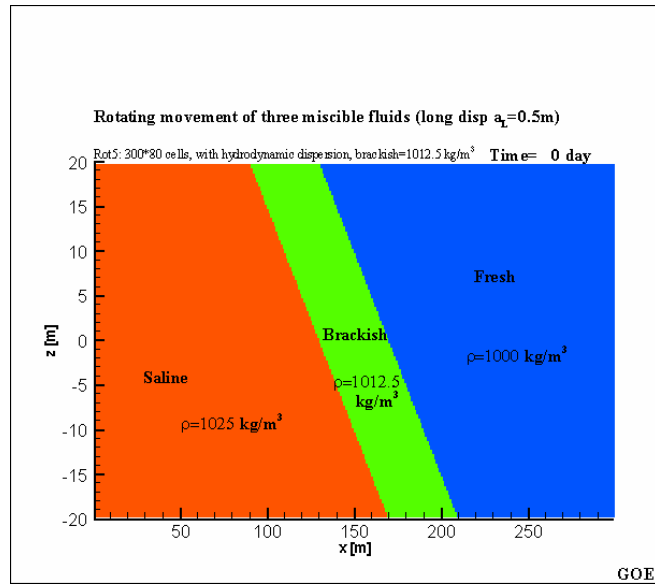
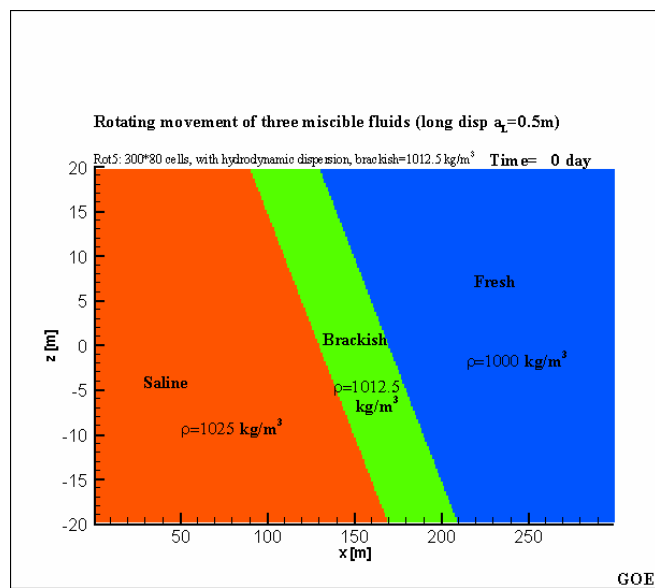


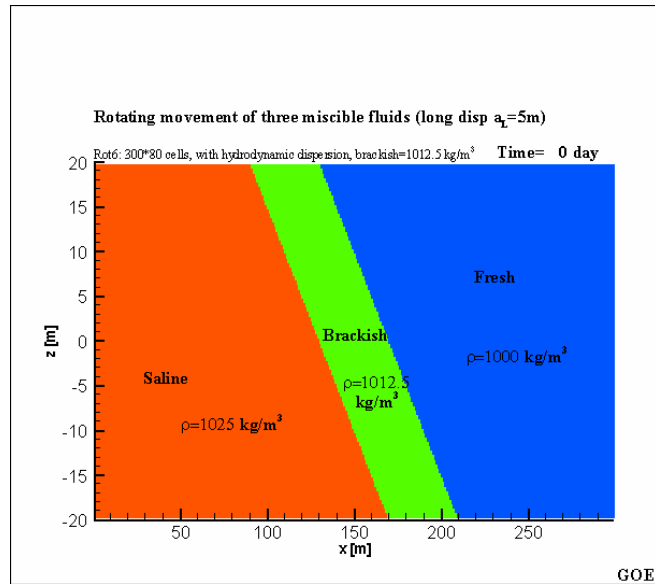
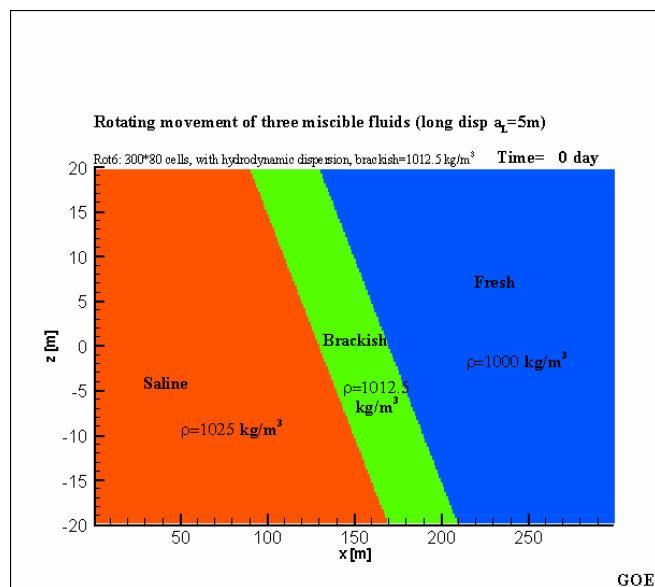
## Rotating immiscible interfaces (asymmetric)



## Rotating immiscible interfaces (asymmetric)



Rotating interfaces with dispersion  $\alpha_L=0.5m$ Rotating interfaces with dispersion  $\alpha_L=0.5m$ 

Rotating interfaces with dispersion  $\alpha_L=5m$ Rotating interfaces with dispersion  $\alpha_L=5m$ 

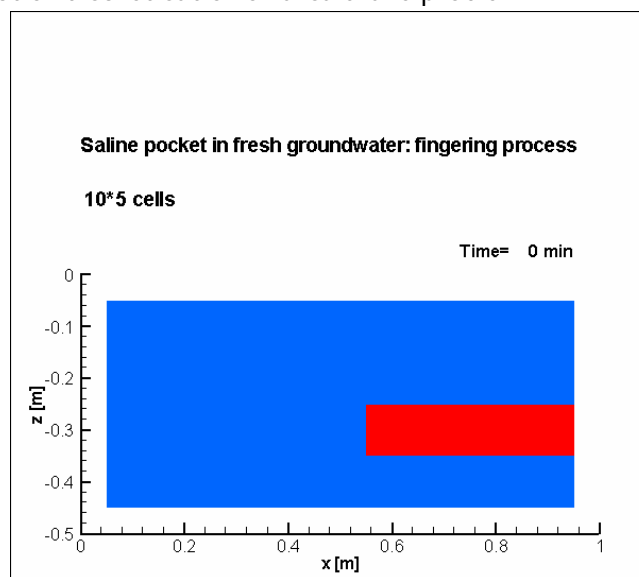
## Salt water pocket in a fresh environment

Grid convergence  
Time step

## Salt water pocket in a fresh environment (I)

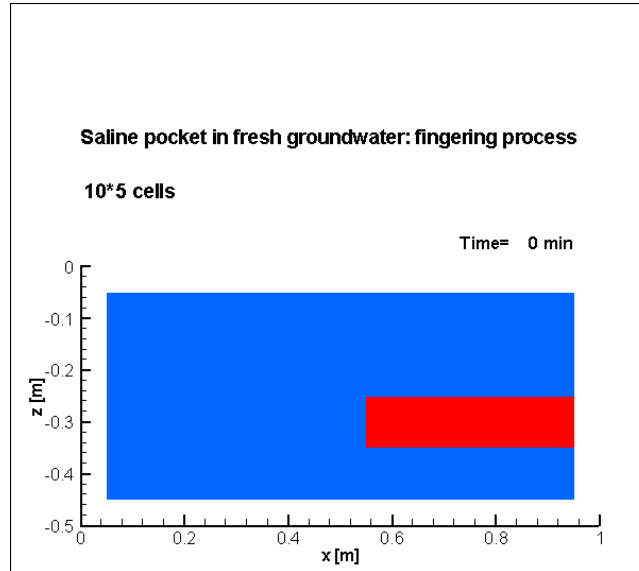
cases

Effect of discretisation on a 'salt lake problem'



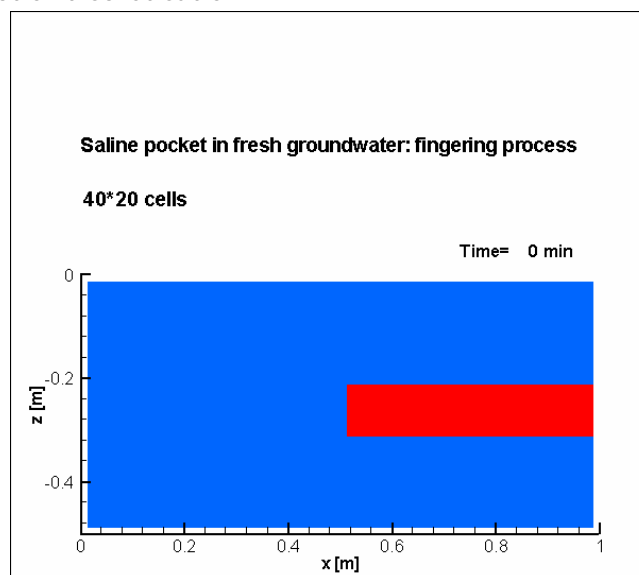
## Salt water pocket in a fresh environment (I)

Effect of discretisation on a 'salt lake problem'



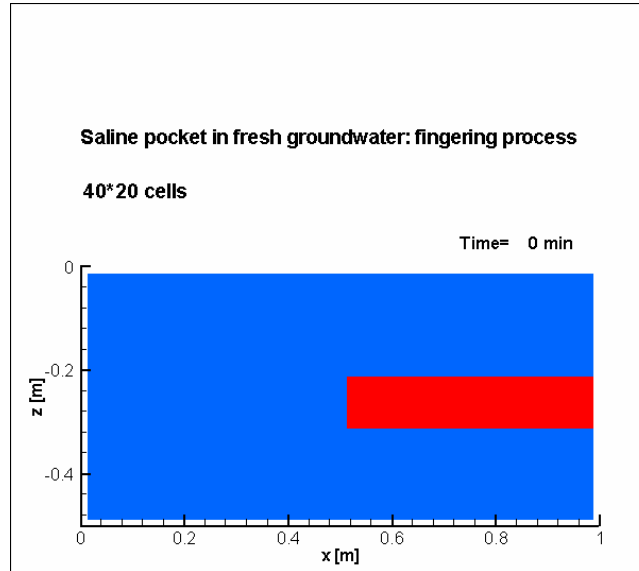
## Salt water pocket in a fresh environment (II)

Effect of discretisation



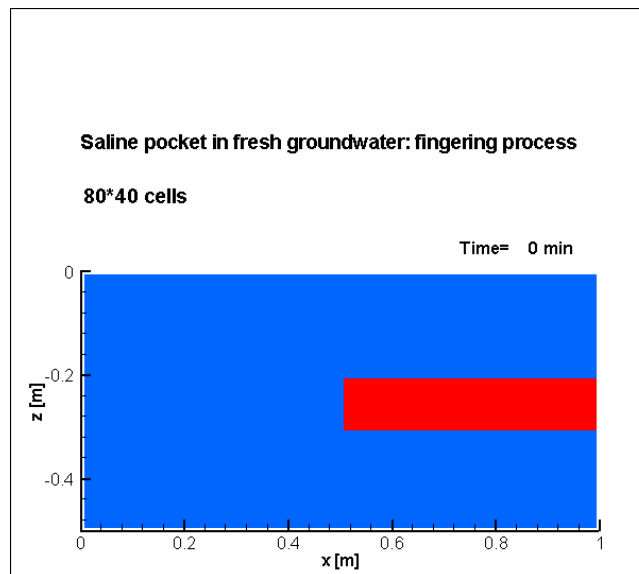
## Salt water pocket in a fresh environment (II)

Effect of discretisation



## Salt water pocket in a fresh environment (III)

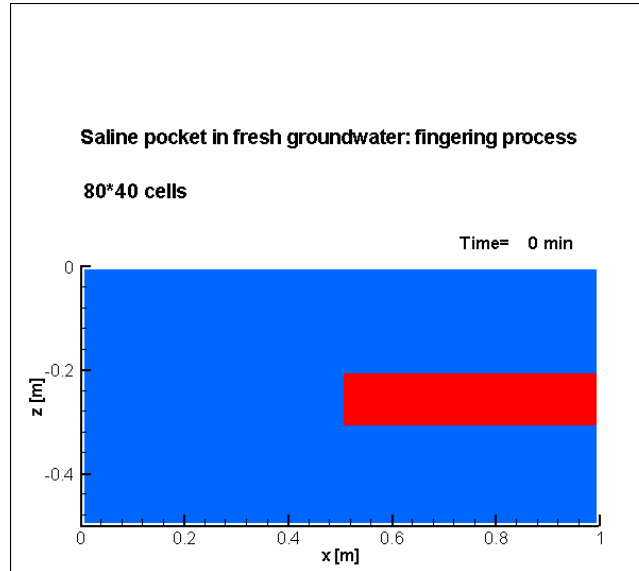
Effect of discretisation





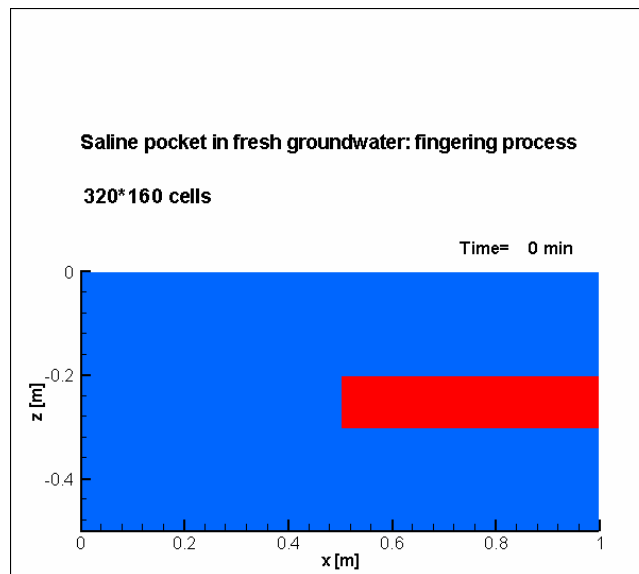
### Salt water pocket in a fresh environment (III)

Effect of discretisation



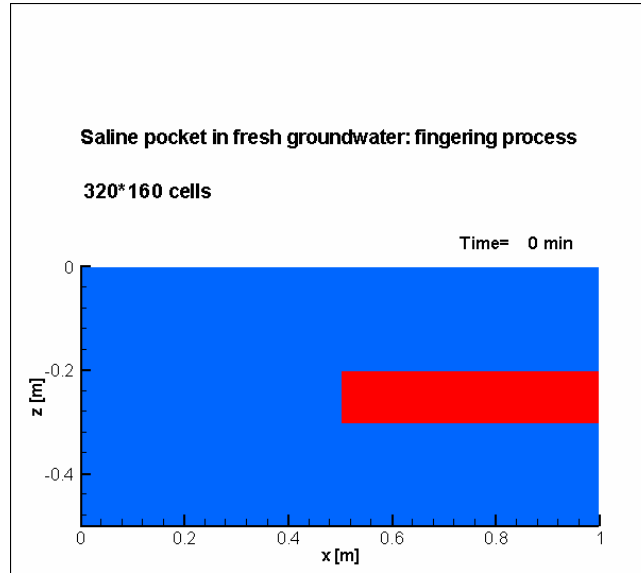
### Salt water pocket in a fresh environment (IV)

Effect of discretisation



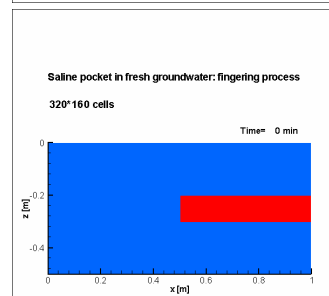
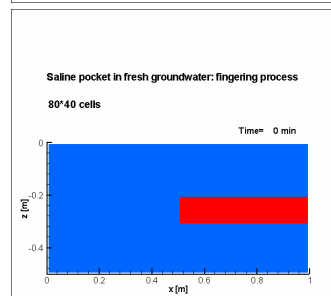
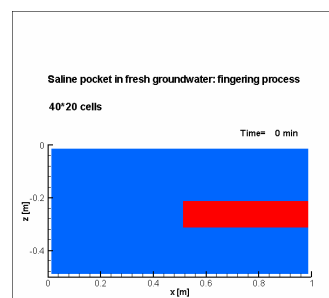
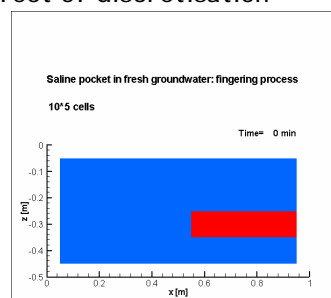
## Salt water pocket in a fresh environment (IV)

Effect of discretisation



## Salt water pocket in a fresh environment (V)

Effect of discretisation

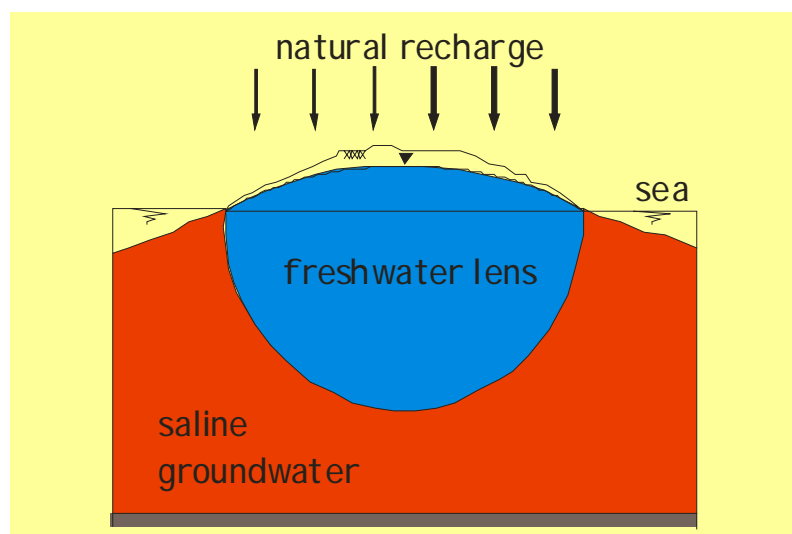


## Salt water pocket in a fresh environment (VI)

### Conclusion:

- For some physical processes, a large number of cells is necessary
- Check always grid convergence!

## Evolution of a freshwater lens



## Question:

*How long does it take before the volume of a freshwater lens is filled?:*

- a. 5 years
- b. 25 years
- c. 100 years
- d. 500 years

**T = specific time scale**

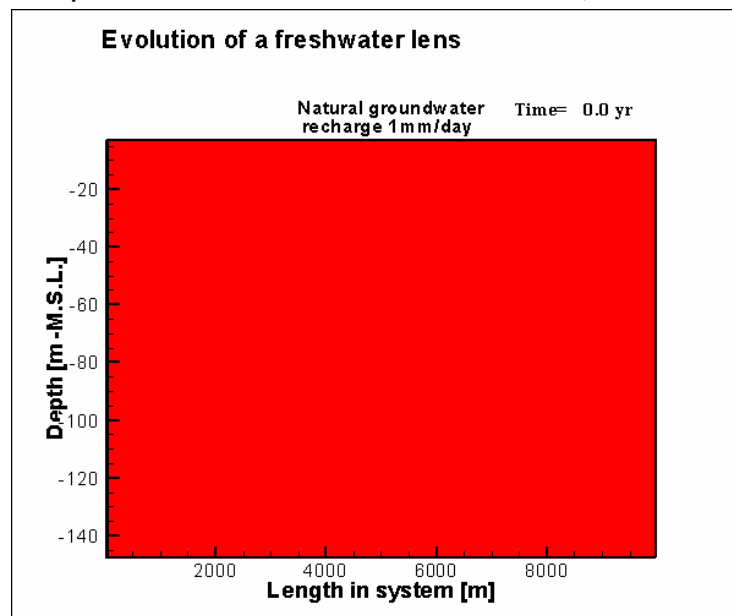
**T = time period before the lens has reached 95% of its final form**

In the Netherlands: T = 75-200 jaar,

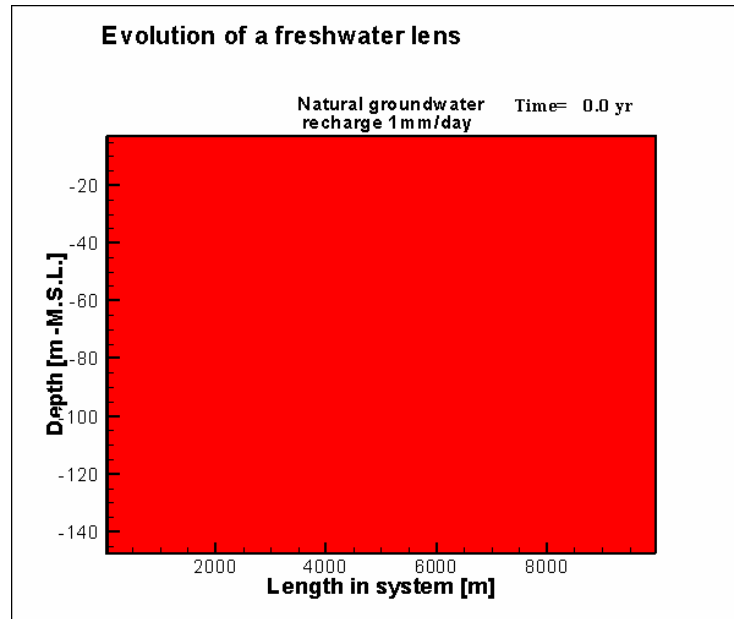
depends on:

- width dune area
- natural groundwater recharge
- hydraulic conductivity soil

Concept: evolution freshwater lens (not Griend!)



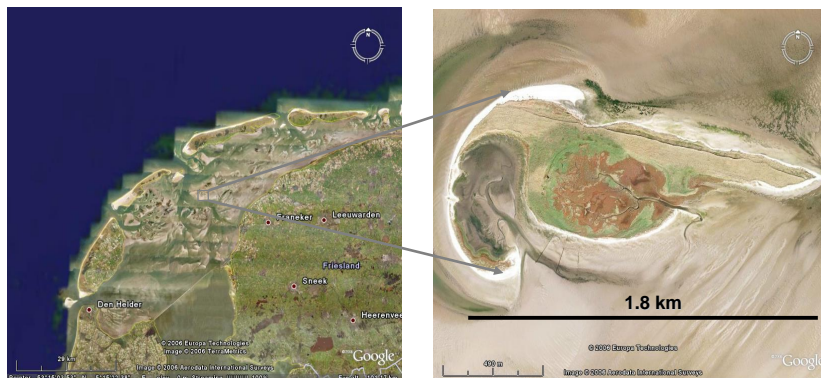
## Concept: evolution freshwater lens (not Griend!)



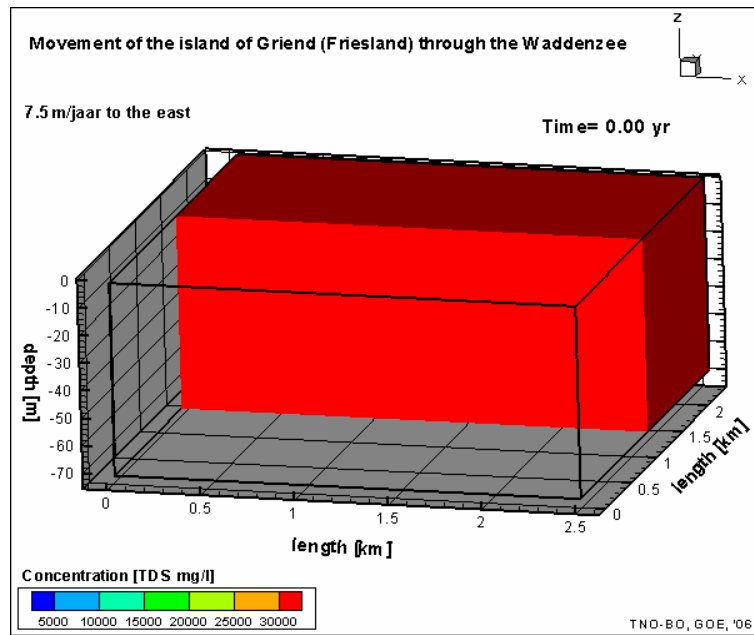
## The island of Griend

Issues:

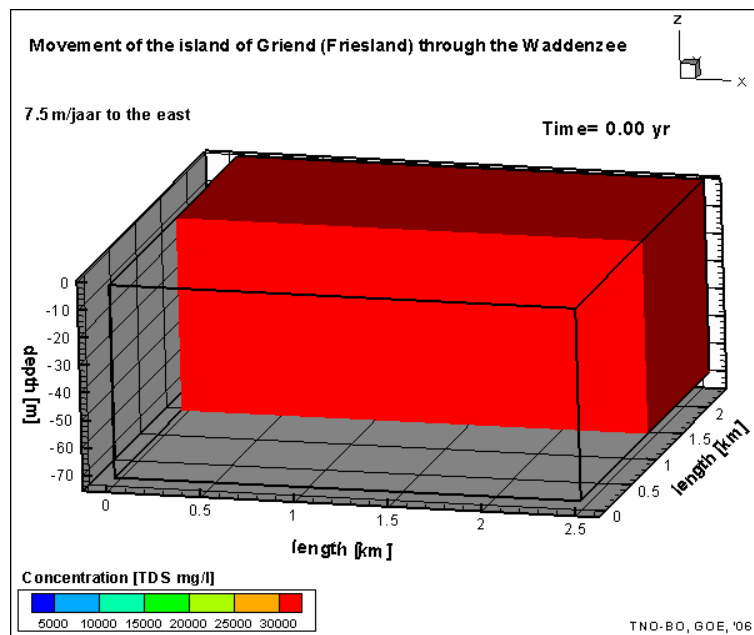
1. Small island moves ~7.5m per year to the east
2. Effect on the volume of the freshwater lens:
  - Can a lens be developed?
  - What is the thickness of the lens?



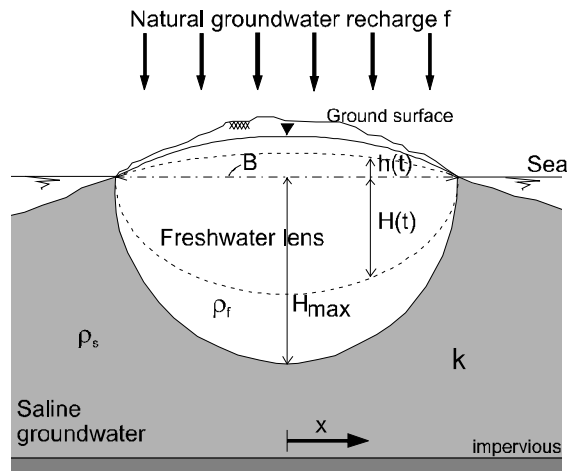
## Movement of De Griend and creation of the lens



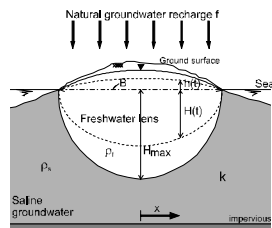
## Movement of De Griend and creation of the lens



## Case 2: Development of a freshwater lens

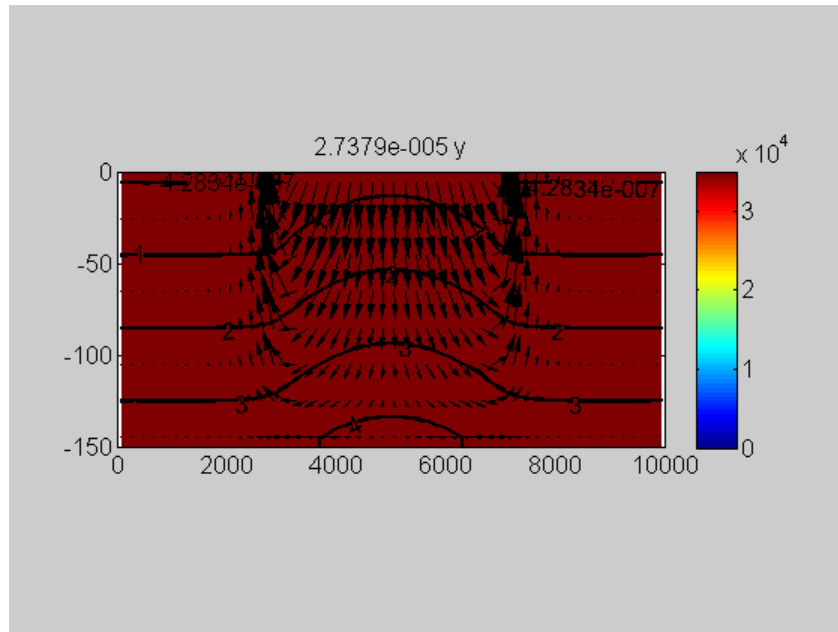


## Case 2: Development of a freshwater lens

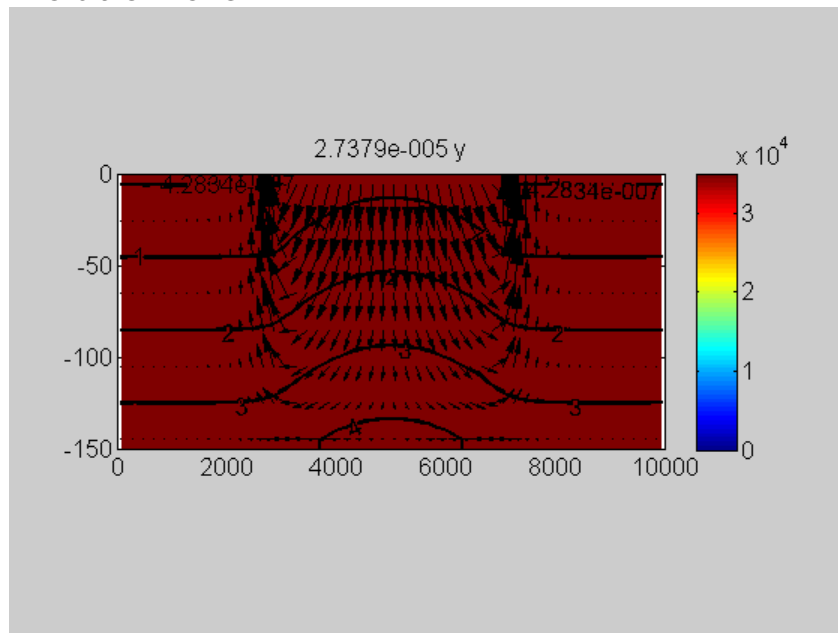


Parameters			
Layers	15	$K_{hor}$	20 m/d
Rows	1	T	200 m/d
Columns	100	Anisotropy $K_{hor}/K_{ver}$	10
$\Delta x$	100 m	ne	0.35
$\Delta y$	10 m	$\alpha L$	0 m
$\Delta z$	10 m	$\alpha T$	0 m
Stress periods	10	recharge	360 mm/y
Initial concentration	35000 mg/l	Recharge concentration	0 mg/l
bouyancy	0.025		

## Evolution lens

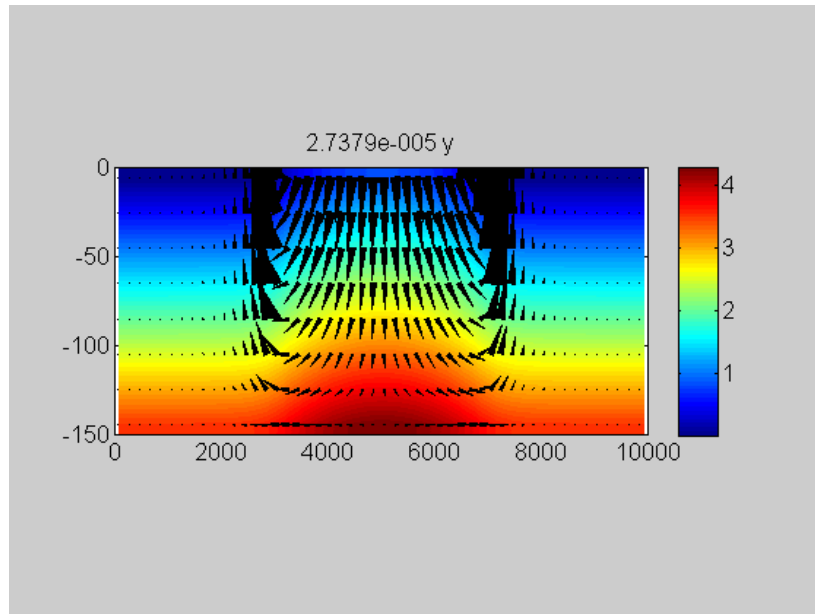


## Evolution lens

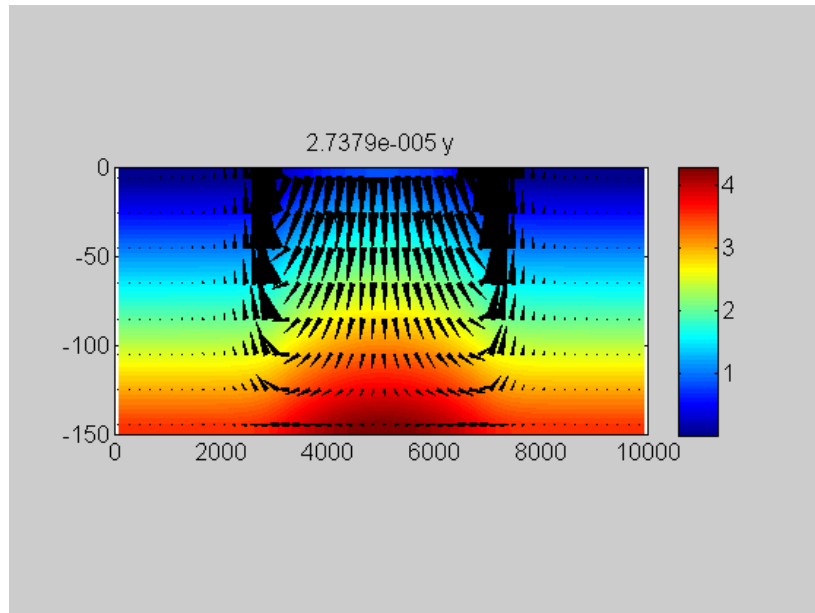




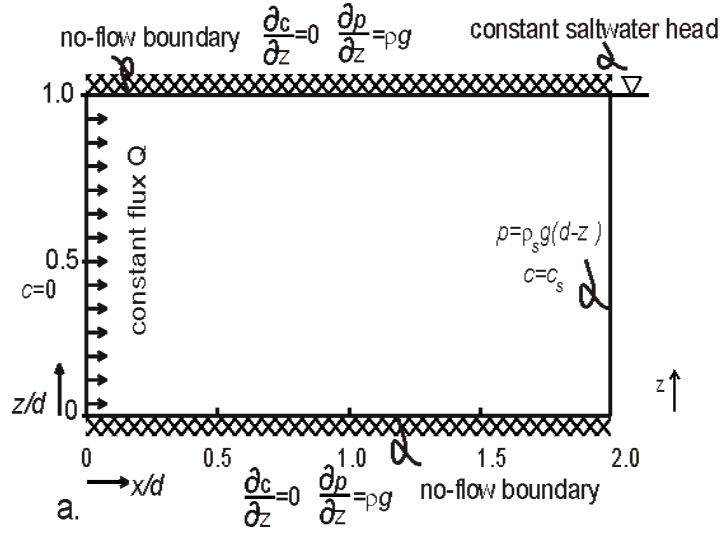
### Evolution freshwater head



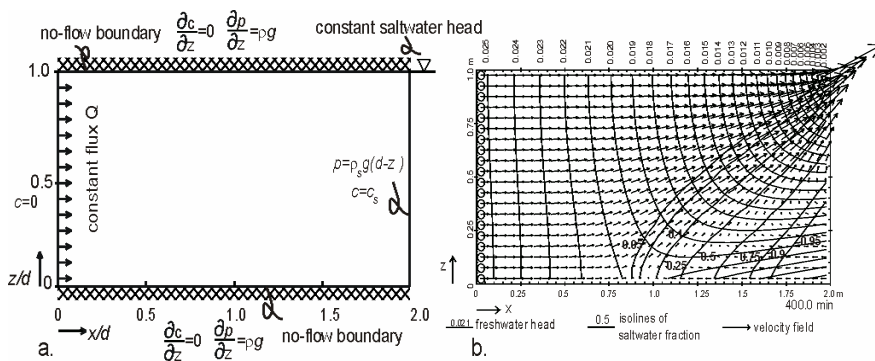
### Evolution freshwater head



### Henry's problem (1964)

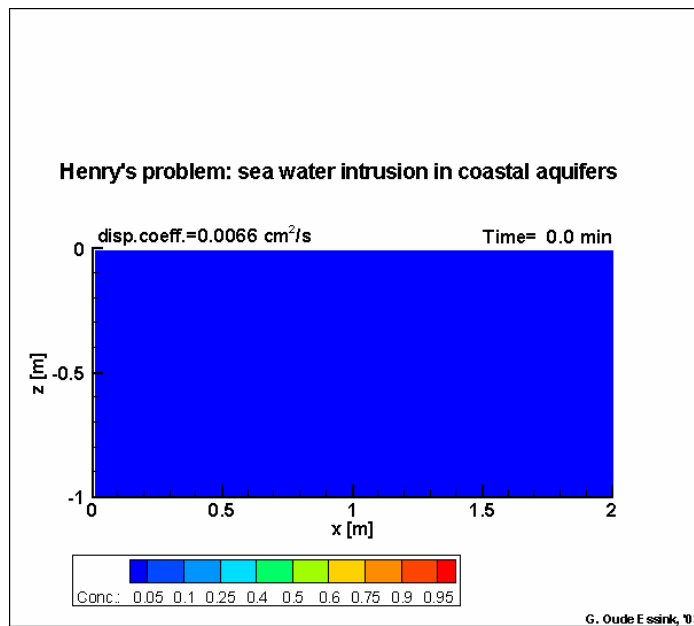


### Henry's problem



## Henry's problem

cases



## Henry's problem

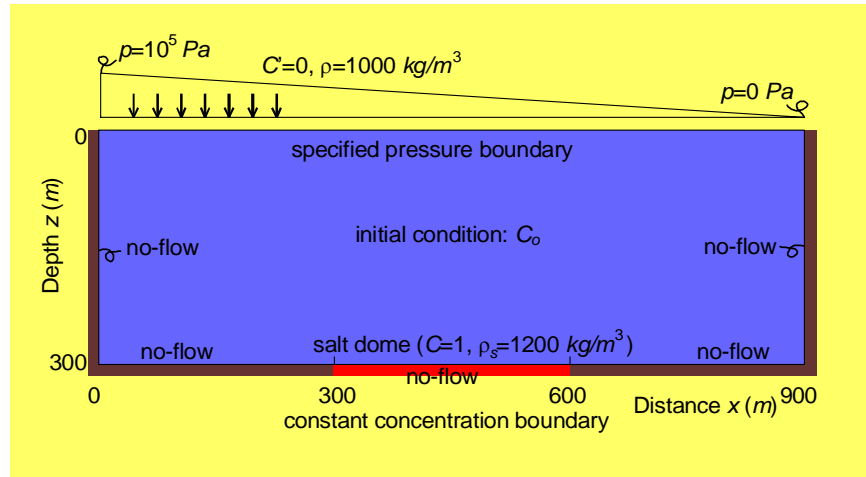
cases

Don't use the Henry problem as a variable-density benchmark, because even with a constant density model, the results are more or less the same!

## Hydrocoin:

cases

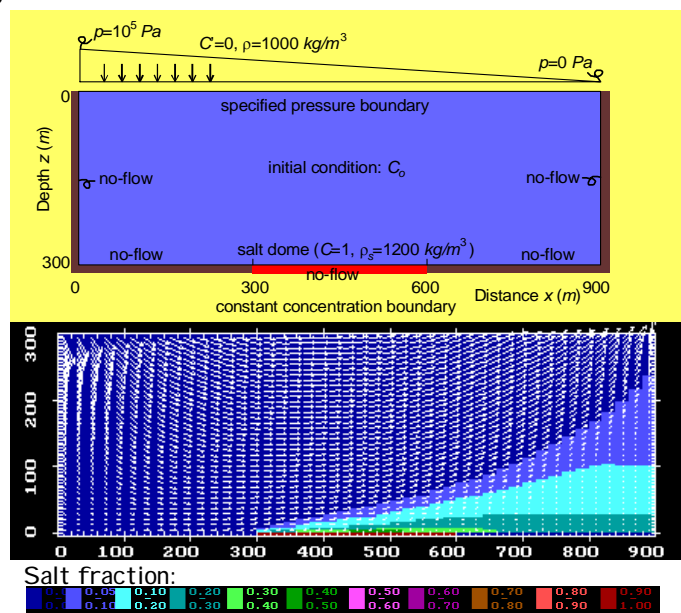
disposal of high-level nuclear waste  
groundwater movement near salt domes  
Gorleben salt dome, Germany



## Hydrocoin:

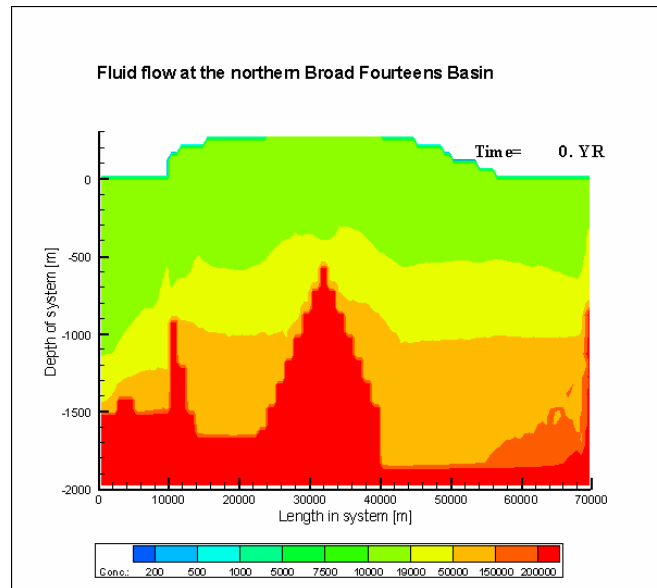
cases

groundwater movement near salt domes



## Broad 14 Basin, North Sea

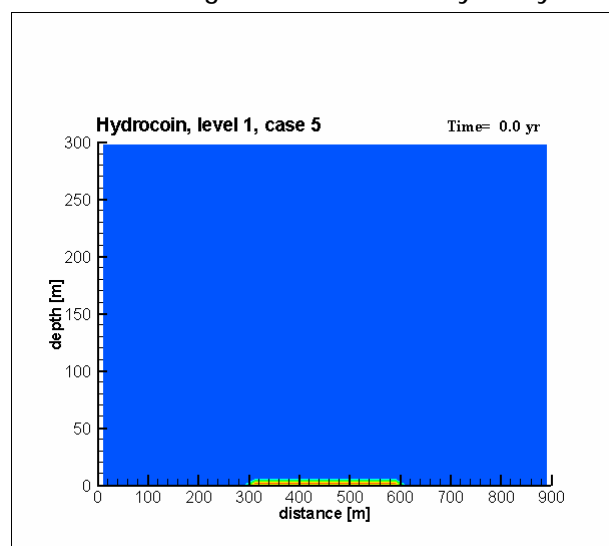
Geofluids'03, with L. Bouw



Bouw, L. & Oude Essink, G.H.P. 2003. Development of a freshwater lens in the inverted Broad Fourteens Basin, Netherlands offshore, J. of Geochemical Exploration (78-79), 321-325.

### Hydrocoin: effect of boundary condition (I)

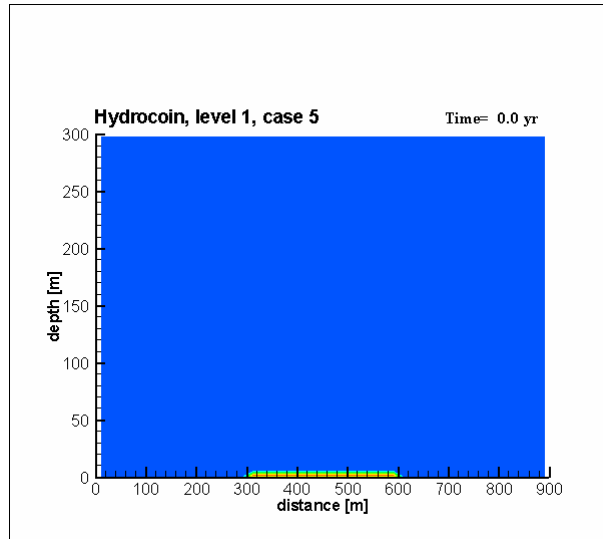
supply of brine through advection and hydrodynamic dispersion



*recirculation type*

Hydrocoin: effect of boundary condition (I)  
supply of brine through advection and hydrodynamic dispersion

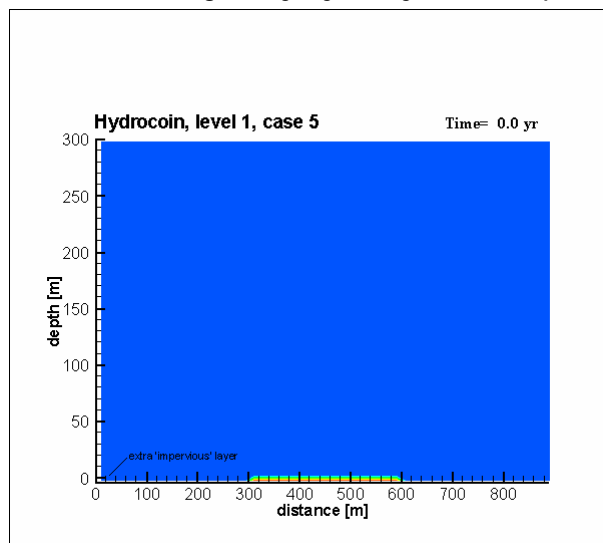
cases



*recirculation type*

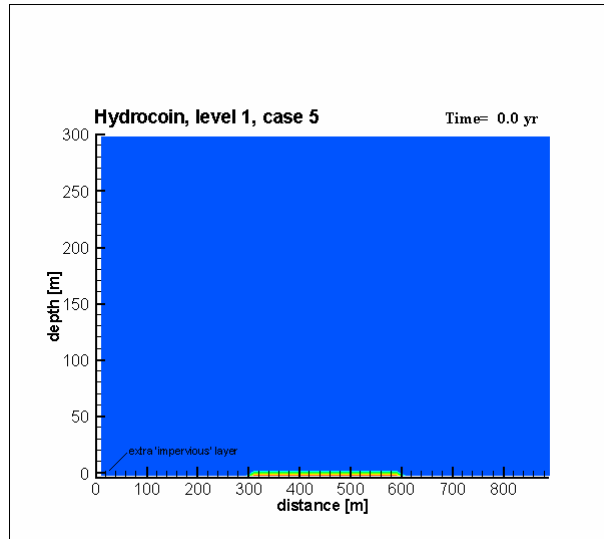
Hydrocoin: effect of boundary condition (II)  
supply of brine through only hydrodynamic dispersion

cases



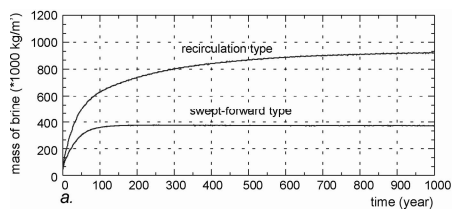
*swept-forward type*

## Hydrocoin: effect of boundary condition (II) supply of brine through only hydrodynamic dispersion

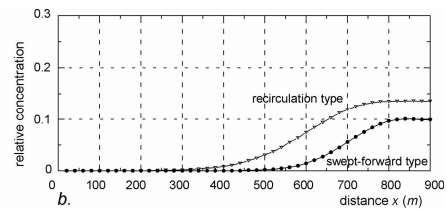


*swept-forward type*

## Hydrocoin: difference recirculation vs swept forward

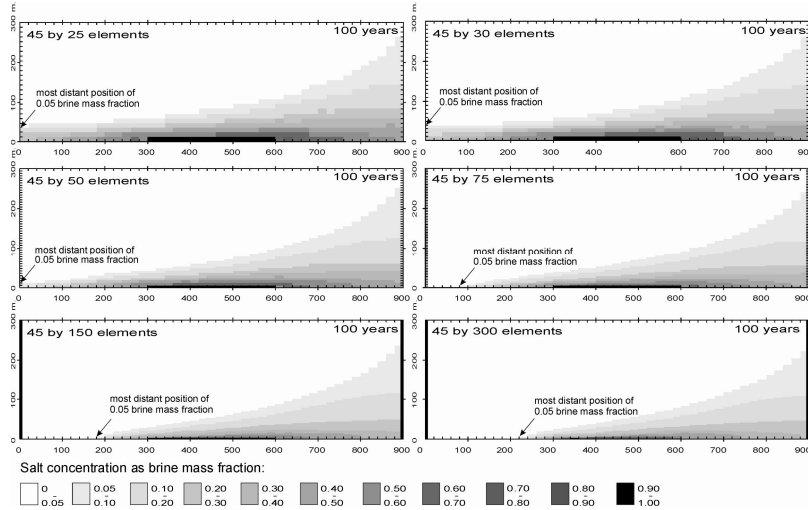


total mass of brine



brine conc at depth=200m

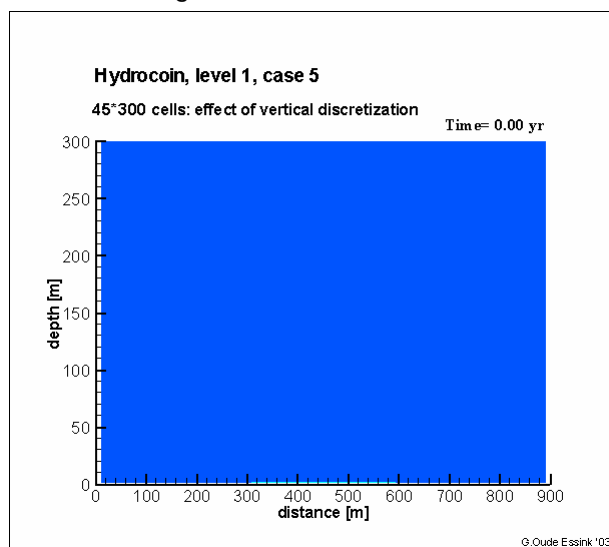
## Hydrocoin: effect of vertical grid size



## Recirculation type

## Hydrocoin: effect of vertical discretization (III) <sup>cases</sup>

more vertical cells give better solution

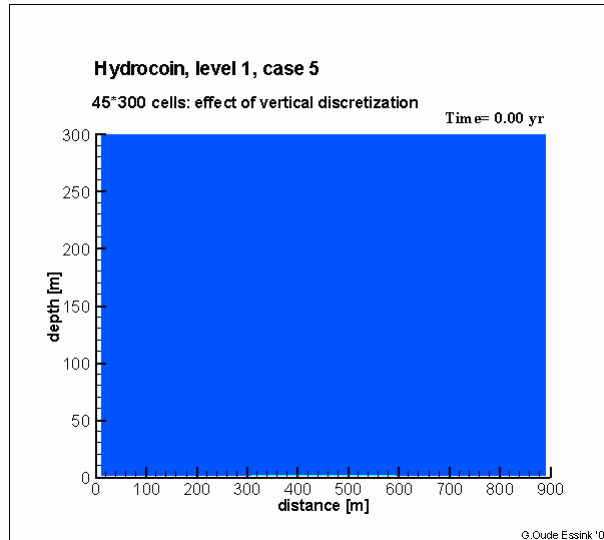


*like the swept-forward type*



## Hydrocoin: effect of vertical discretization (III)

more vertical cells give better solution

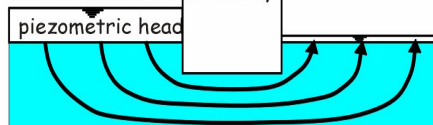


*like the swept-forward type*

## Analogy physical processes

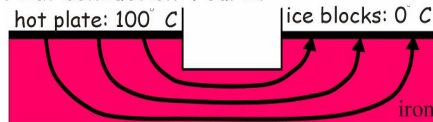
Heat transport (analogy with solute transport)

Groundwater flow: Darcy



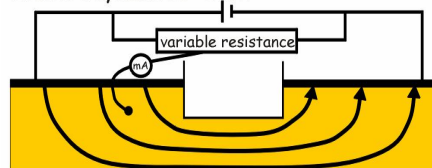
$$q = -k \frac{\partial \phi}{\partial x}$$

Heat conduction: Fourier



$$h = -\lambda \frac{\partial T}{\partial x}$$

Electrodynamics: Ohm



$$i = -\sigma \frac{\partial V}{\partial x}$$

## Conduction and convection of heat

$$h = -\lambda_e \frac{\partial T}{\partial x} + n_e \rho c_f VT$$

thermal conductivity [Joule/(ms<sup>0</sup> C)]  
 $\lambda_e = n_e \lambda_{fluid} + (1 - n_e) \lambda_{solid}$

heat flux    conduction (Fourier)    convection (fluid flow)

continuity equation

$$-\frac{\partial h}{\partial x} = \rho' c' \frac{\partial T}{\partial t}$$

specific heat capacity [Joule/(kg<sup>0</sup> C)]  
 $\rho' c' = n_e \rho c_{fluid} + (1 - n_e) \rho_{solid} c_{solid}$

## Analogy solute and heat transport

Solute: advection-dispersion equation

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left( D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (C V_i) + \frac{(C - C)W}{n_e}$$

Heat: convection-conduction equation

$$\rho' c' \frac{\partial T}{\partial t} = \frac{\partial}{\partial x_i} \left( \Lambda_{ij} \frac{\partial T}{\partial x_j} \right) - \rho c_f \frac{\partial T q_i}{\partial x_i} + \Gamma$$

## Analogy heat and solute transport

Heat transport

Convection-conduction equation

$$\rho'c \frac{\partial T}{\partial t} = \frac{\partial}{\partial x_i} \left( \Lambda_{ij} \frac{\partial T}{\partial x_j} \right) - \rho c_f \frac{\partial T q_i}{\partial x_i} + \Gamma$$

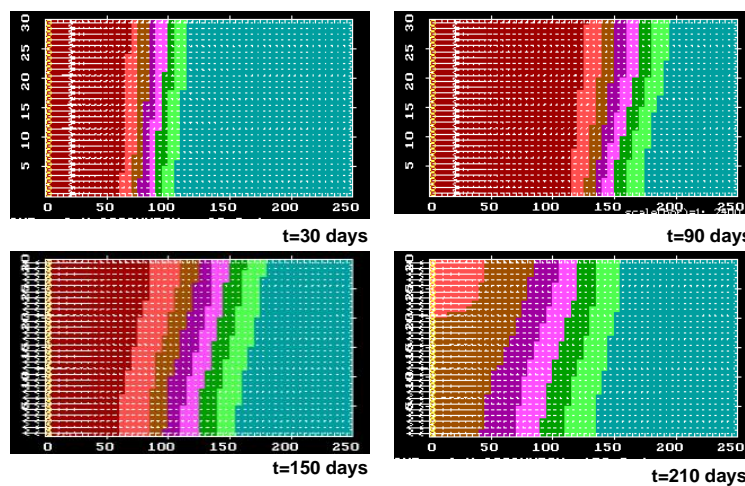
Equation of state: relation density & temperature

$$\rho_{i,j,k} = \rho_f (1 - \alpha_f T_{i,j,k})$$

Analogy between solute and heat transport

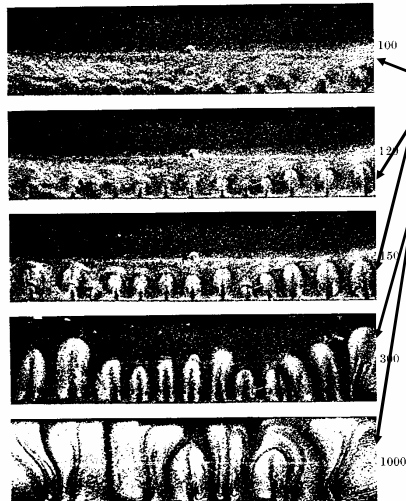
Solute	Heat
$C$	$T$
$R_d$	$1 + \frac{(1-n_e)\rho_s c_s}{n_e \rho c_f}$
$D_m$	$\frac{n_e \lambda_e + (1-n_e)\lambda_s}{n_e \rho c_f}$
$\lambda$	0

## Energy storage in geothermal reservoirs



## Elder problem (I)

It is originally a heat transport problem



Phases:

1. Stable growth diffusive boundary layer
2. Development flow cells embedded in boundary layer
3. Emergence of disturbances that grow into fingers

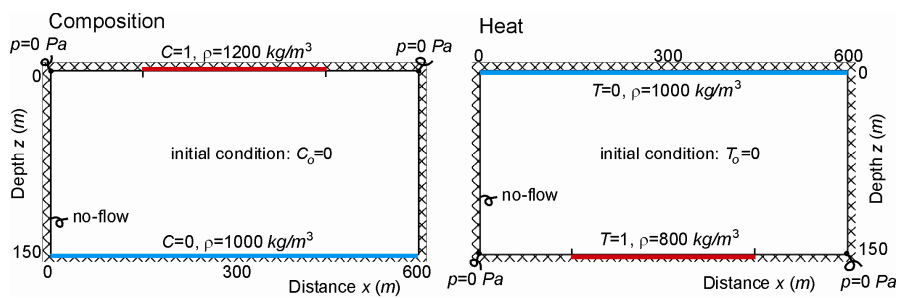
Convection of heat occurs when:

$$\text{Rayleigh number} > 4\pi^2$$

Elder, J. Fluid Mech. 32, 69-96, 1968

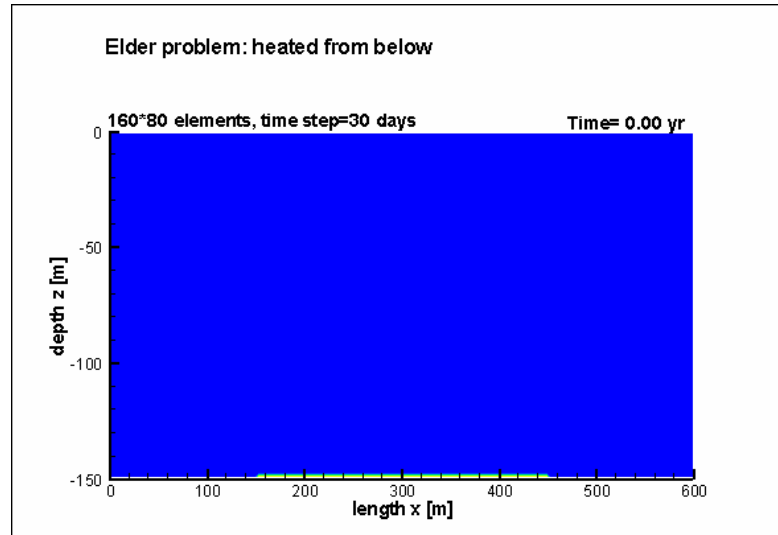
## Elder problem (II)

### Analogy composition and heat



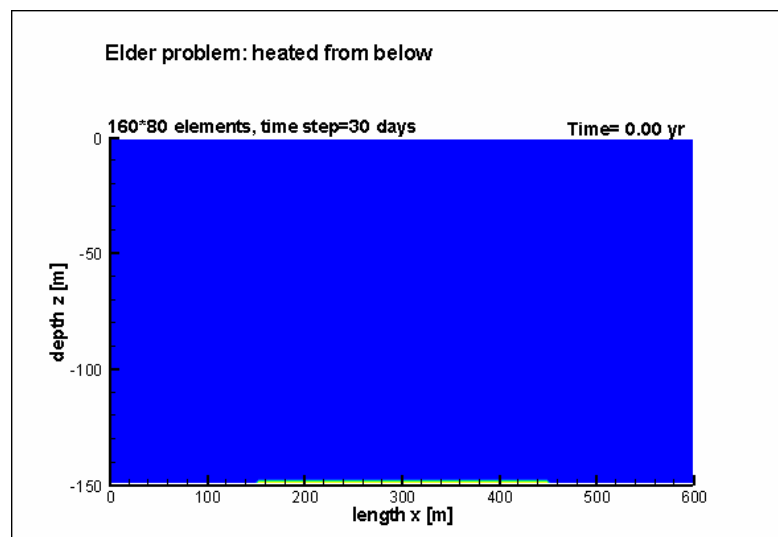
### Elder problem (III)

Development of convection cells (Rayleigh number=400)

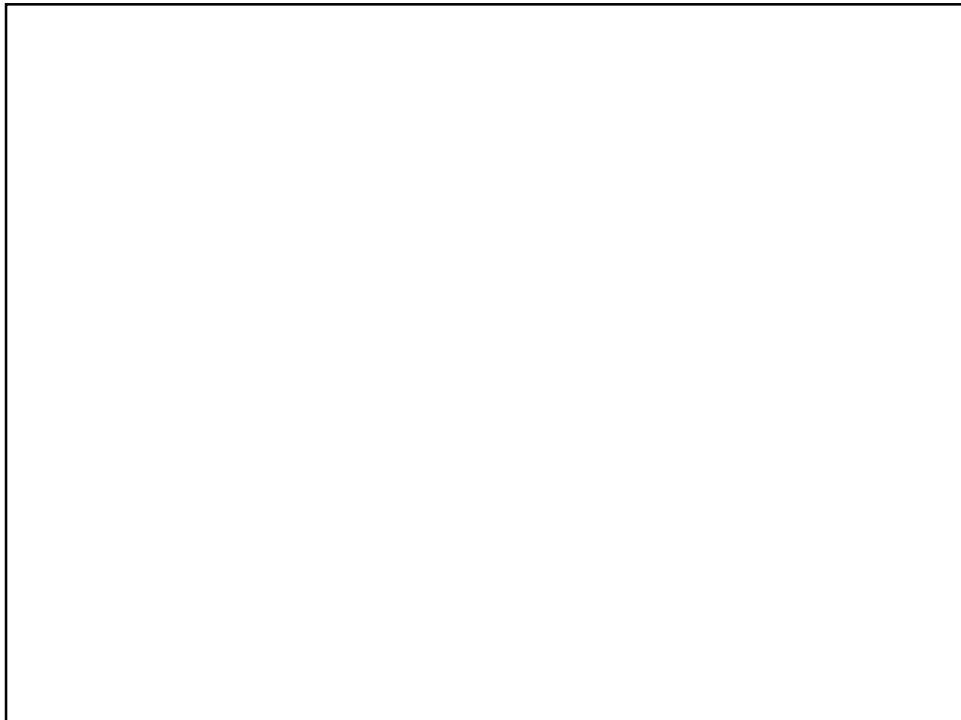
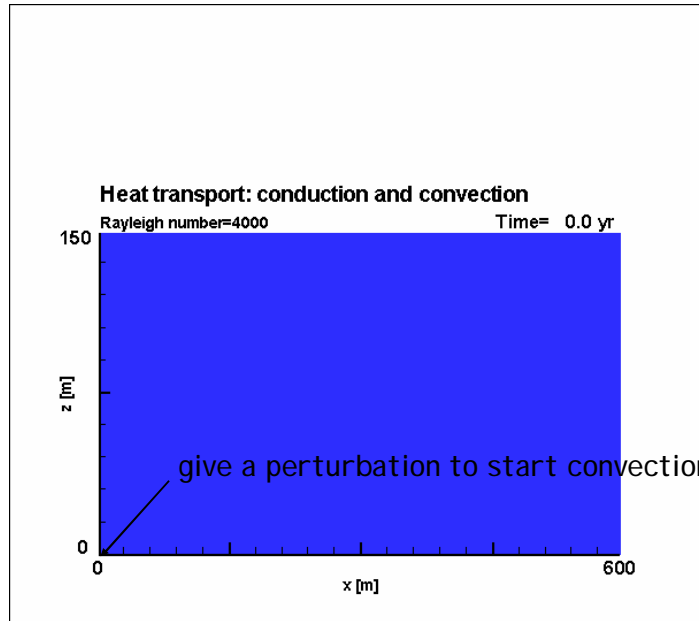


### Elder problem (III)

Development of convection cells (Rayleigh number=400)



# Heat transport (Rayleigh number=4000)



## Impact of the 26-12-04 Tsunami on groundwater systems



Sri Lanka  
Some days after December 26<sup>th</sup>, 2004



## Impact of the 26-12-04 Tsunami on groundwater systems

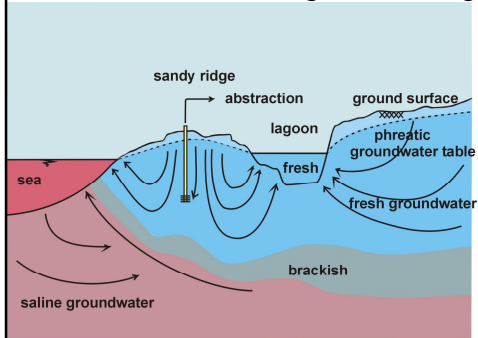
Impression of relevant salinisation processes by conceptual models of salt water intrusion in coastal aquifers:

1. Fingering processes in the subsoil
2. Evolution of a freshwater lens after flooding by sea water
3. Freshwater lens in a coastal aquifer with a brackish lagoon

Next step:  
quantifying processes in real situations, using topographic and hydrogeological data, and ending up with vulnerability maps

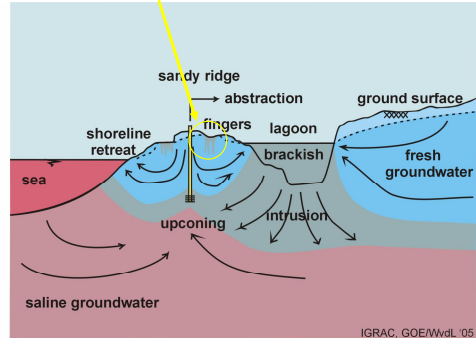
# Concept 1: Fingering processes in the subsoil

## Case Sri Lanka: lagoon setting



Before the Tsunami

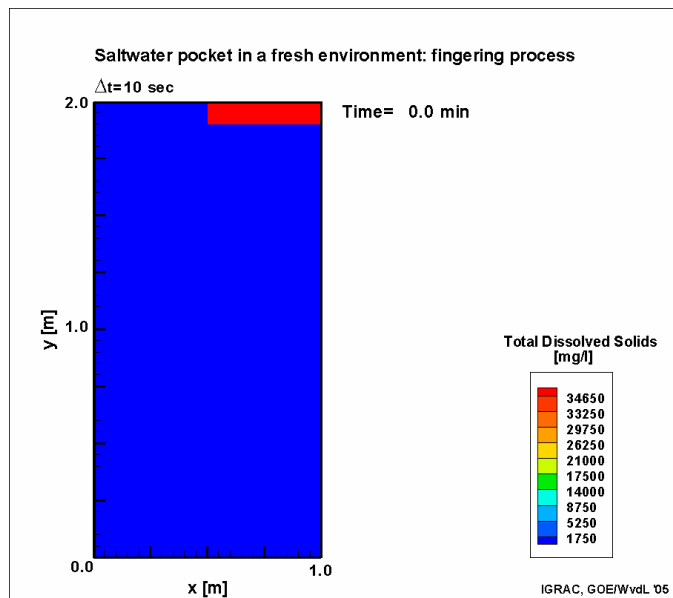
## fingering processes



After the Tsunami

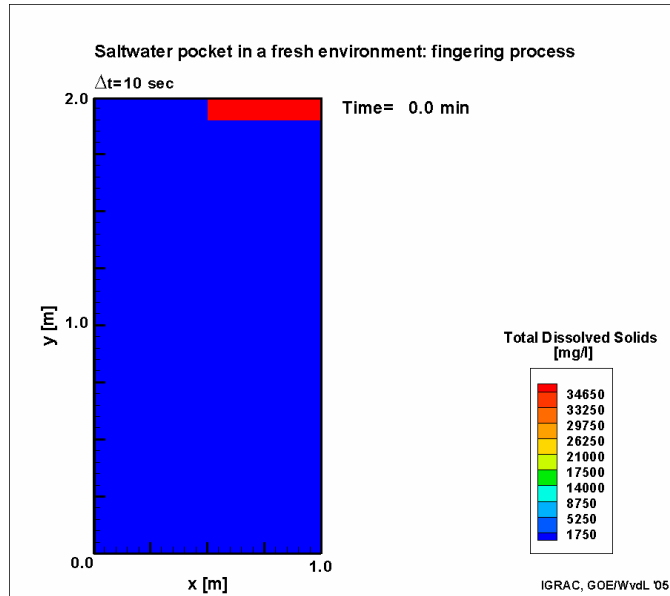
IGRAC, GOE/WvdL 05

# Concept 1: Fingering processes in the subsoil

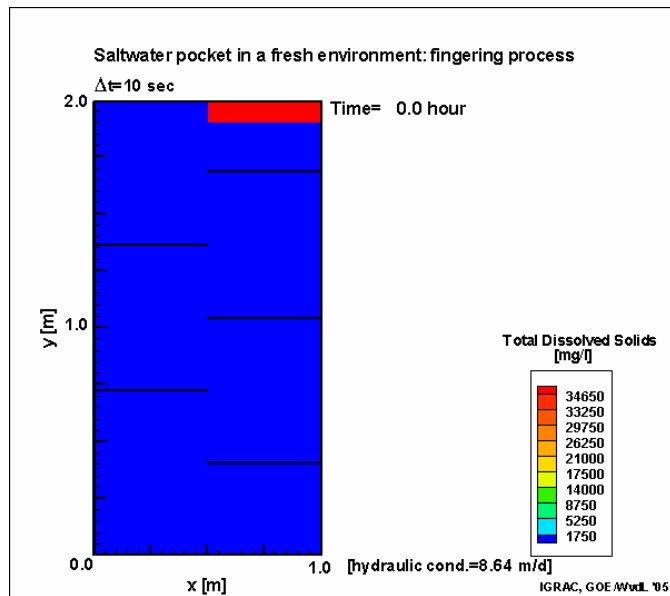




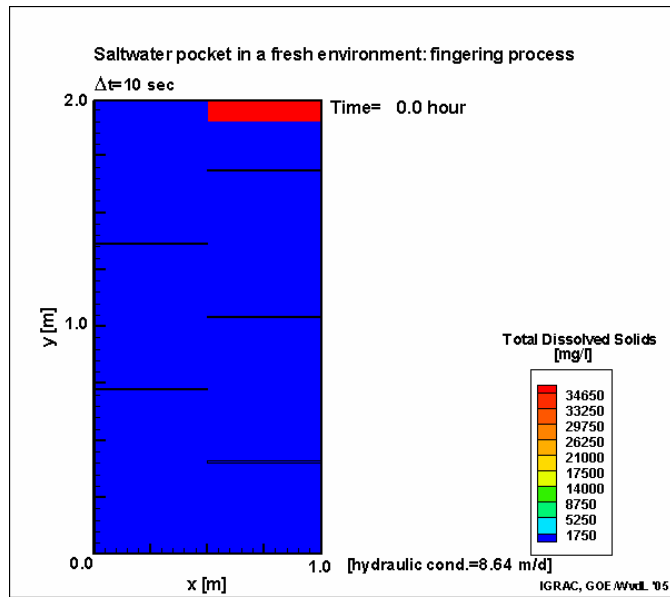
## Concept 1: Fingering processes in the subsoil



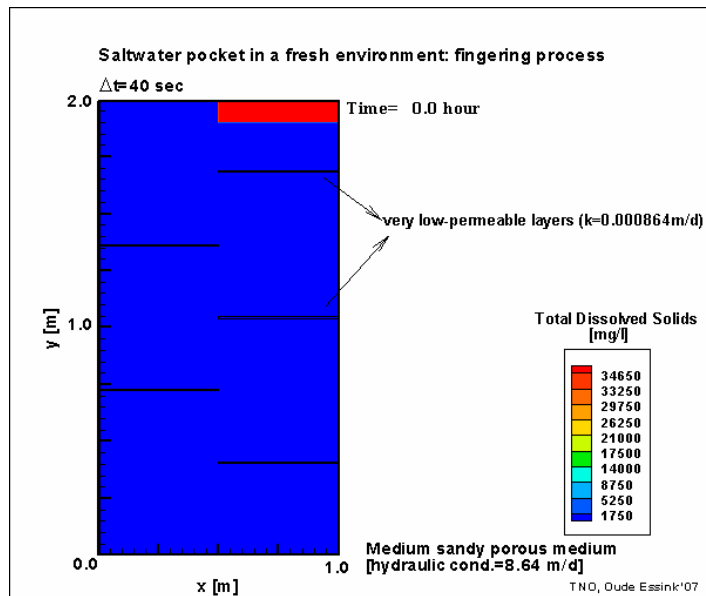
## Concept 1: Fingering processes in the subsoil



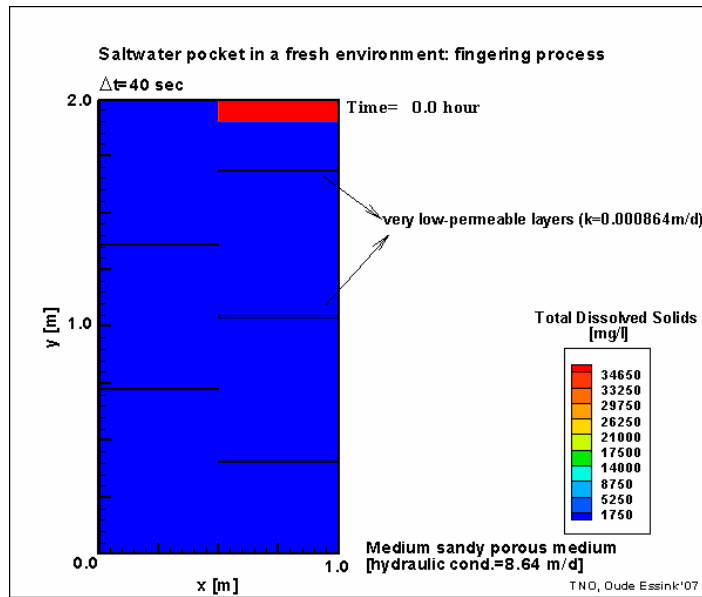
## Concept 1: Fingering processes in the subsoil



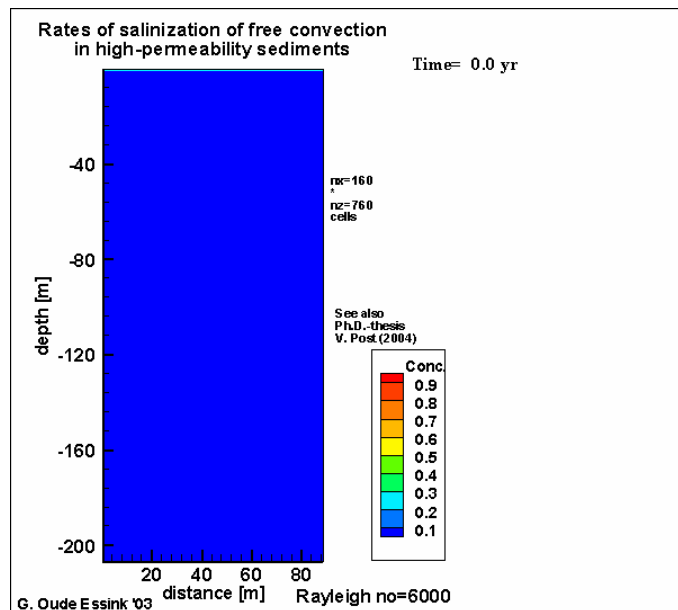
## Concept 1: Fingering processes in the subsoil



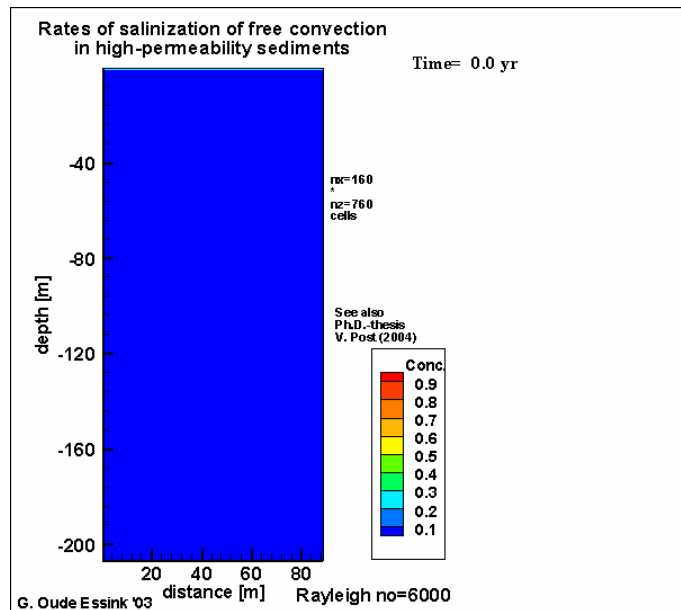
## Concept 1: Fingering processes in the subsoil



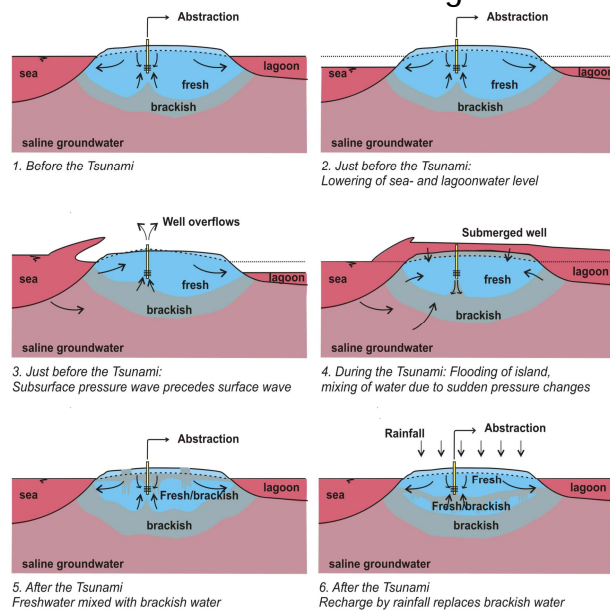
## Concept 1: Fingering processes in the subsoil



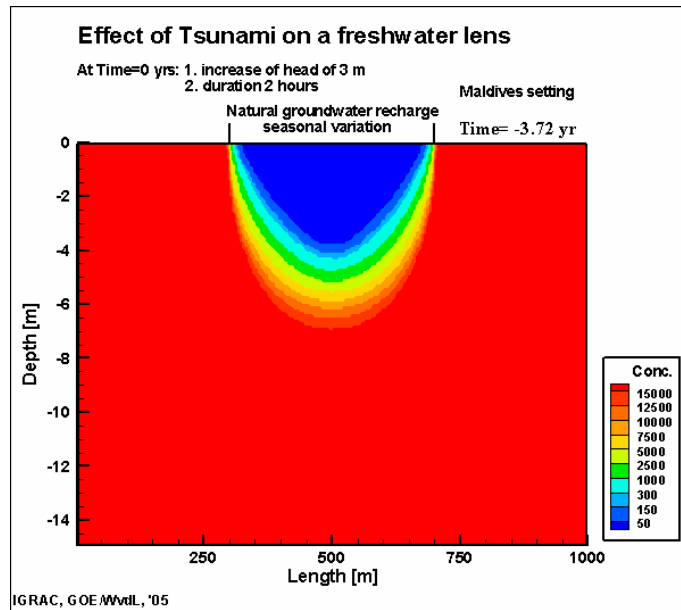
## Concept 1: Fingering processes in the subsoil



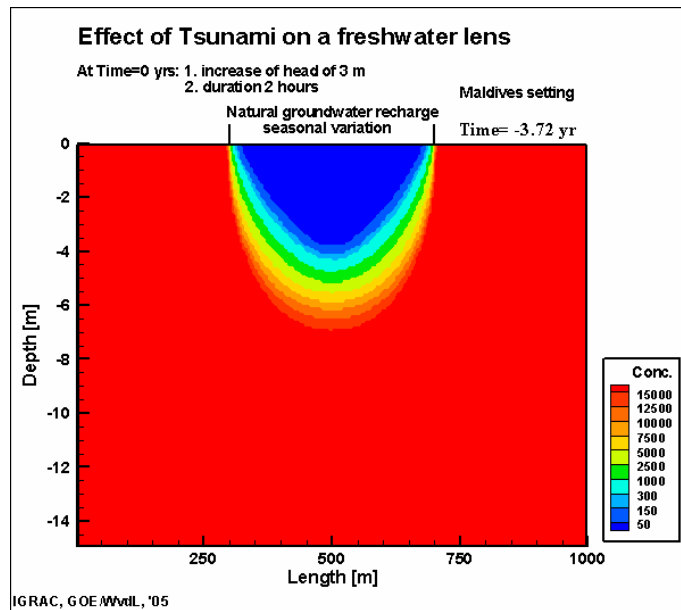
## Concept 2: Evolution of a freshwater lens after flooding



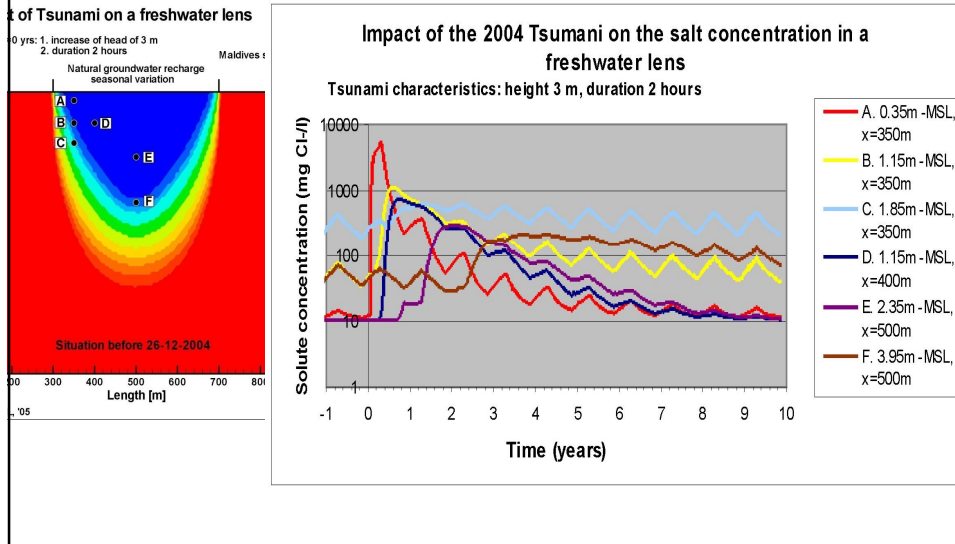
## Concept 2: Evolution of a freshwater lens after flooding



## Concept 2: Evolution of a freshwater lens after flooding

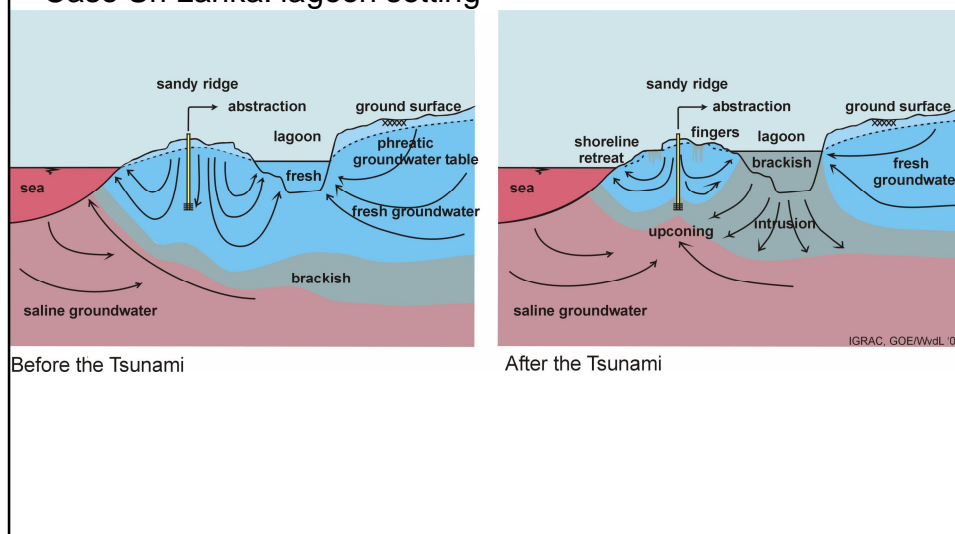


## Concept 2: Evolution of a freshwater lens after flooding

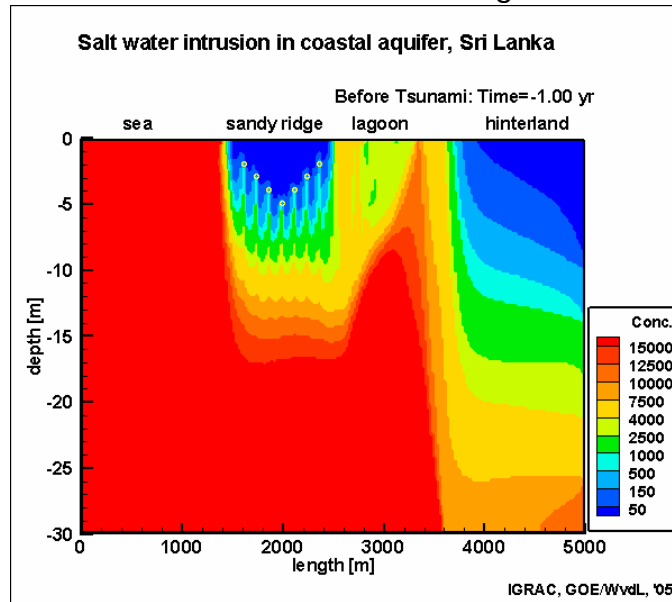


## Concept 3: Freshwater lens in a coastal aquifer with a brackish lagoon

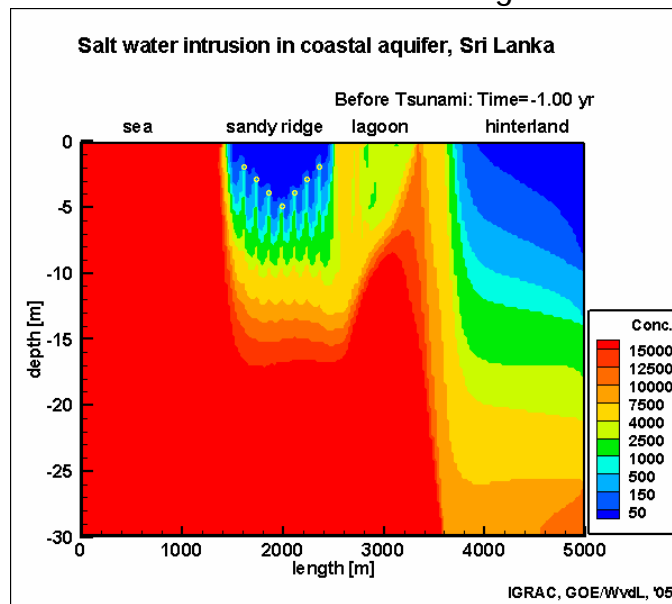
### Case Sri Lanka: lagoon setting



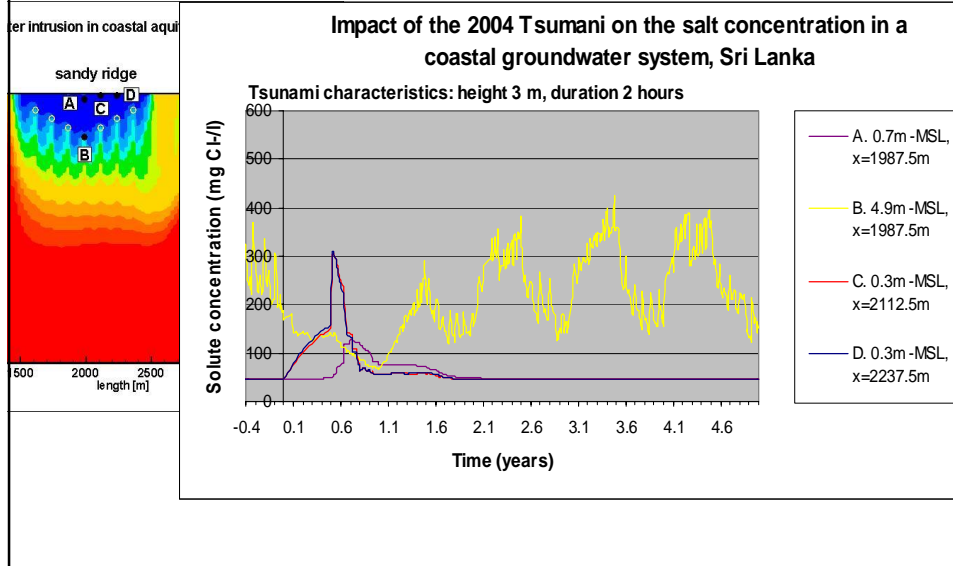
### Concept 3: Freshwater lens in a coastal aquifer with a brackish lagoon



### Concept 3: Freshwater lens in a coastal aquifer with a brackish lagoon



### Concept 3: Freshwater lens in a coastal aquifer with a brackish lagoon



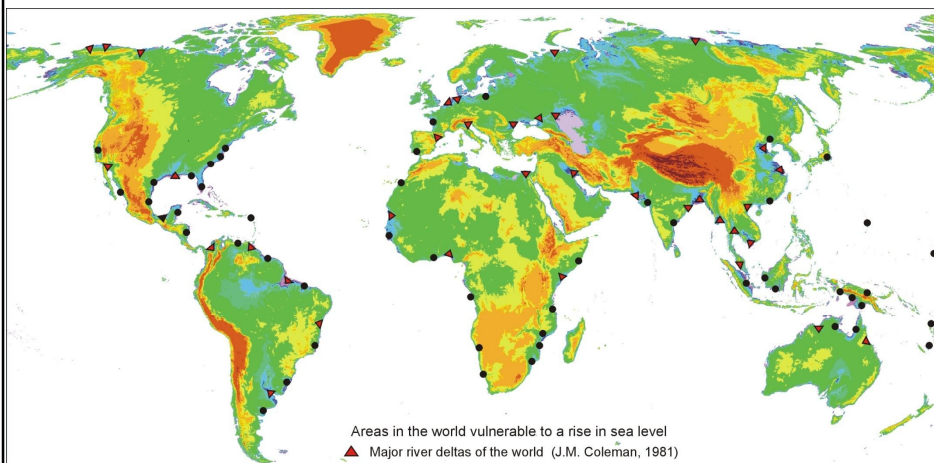
Effect sea level rise



## Effects of sea level rise on groundwater resources in deltaic areas

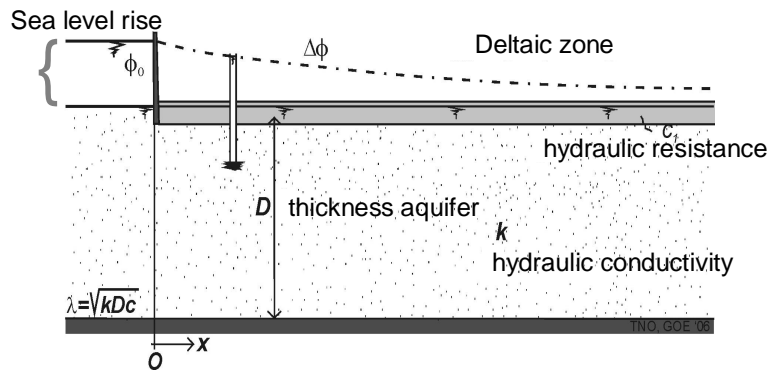
1. Increase of salt water intrusion
2. Increase of upconing under groundwater extraction wells
3. Increase of piezometric head
4. Increase of seepage and salt load to the surface water system
5. Risk of instable Holocene aquitards
6. [Decrease of fresh groundwater reservoirs due to decrease in natural groundwater recharge]

## Effects of sea level rise on groundwater resources in deltaic areas



Digital Elevation Model (DEM)

Effect of sea level rise:  
Analytical approach for zone of influence in deltaic areas



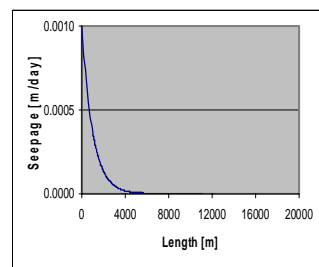
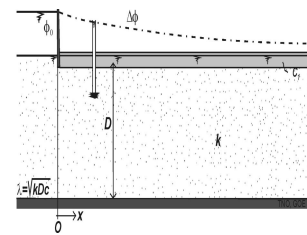
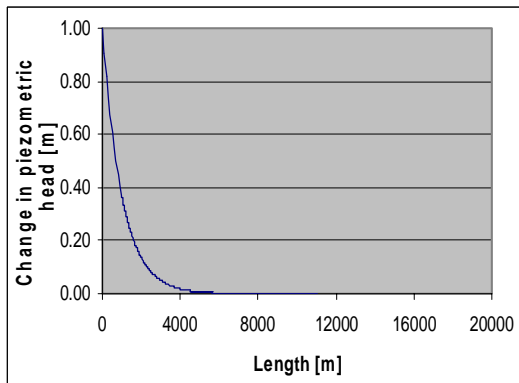
$$\Delta\phi(x) = \phi_0 e^{-x/\lambda}$$

$$\lambda = \sqrt{kDc}$$

- Zone of influence is equal to sqrt( $kDc$ )
- At  $x=3\lambda$ , only 5% of sea level rise is detectable

Effect of sea level rise:  
Case 1 with Dutch subsoil parameters

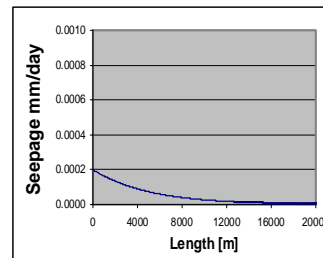
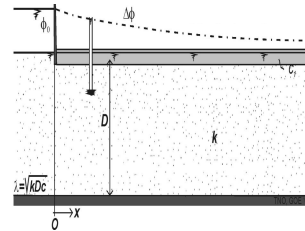
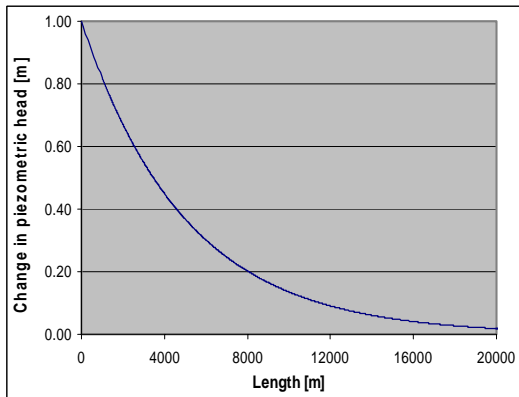
$kD = 1000 \text{ m}^2/\text{day}$   
 $c = 1000 \text{ day}$   
 $\lambda = 1000 \text{ m}$



## Effect of sea level rise:

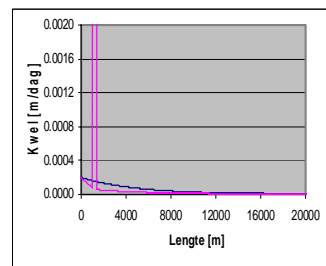
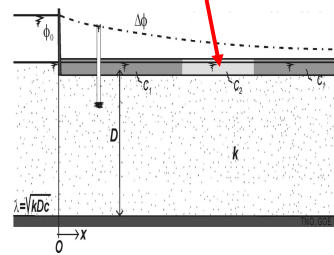
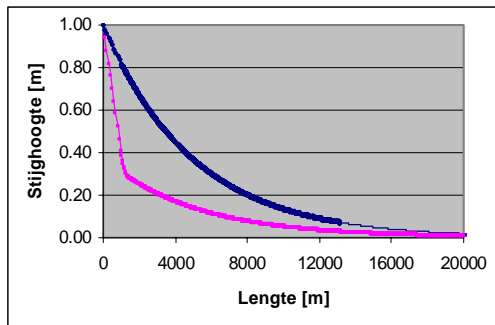
### Case 2 with Dutch subsoil parameters

$kD = 5000 \text{ m}^2/\text{day}$   
 $c = 5000 \text{ day}$   
 $\lambda = 5000 \text{ m}$



### Case 3 with Dutch subsoil parameters

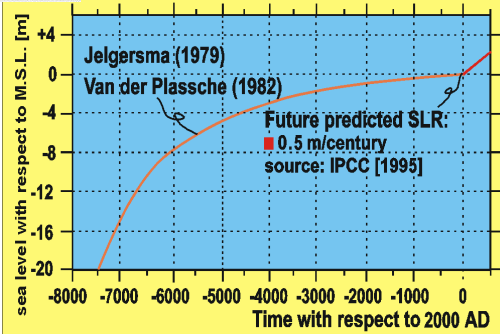
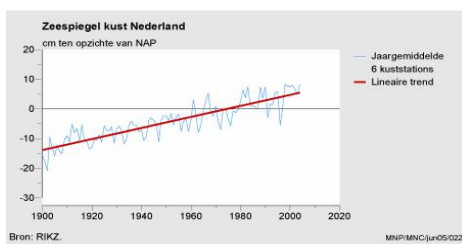
$kD = 5000 \text{ m}^2/\text{dag}$   
 $c_1 = 5000 \text{ dag}, \quad c_2 = 50 \text{ dag}$



# Climate change is HOT!



## Past and future sea level rise in the Netherlands

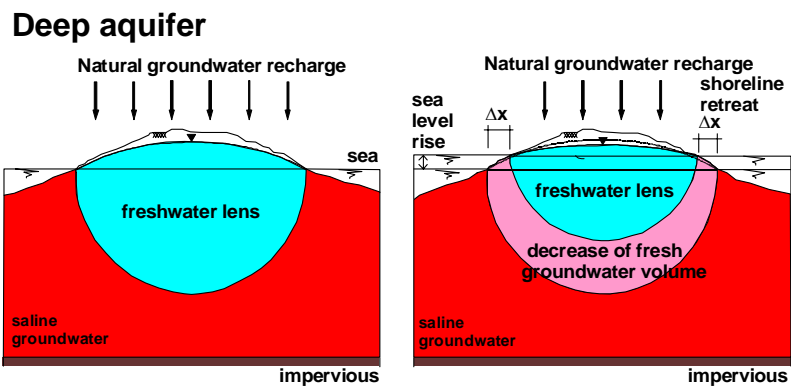


## Implementing new KNMI 06 climate scenarios

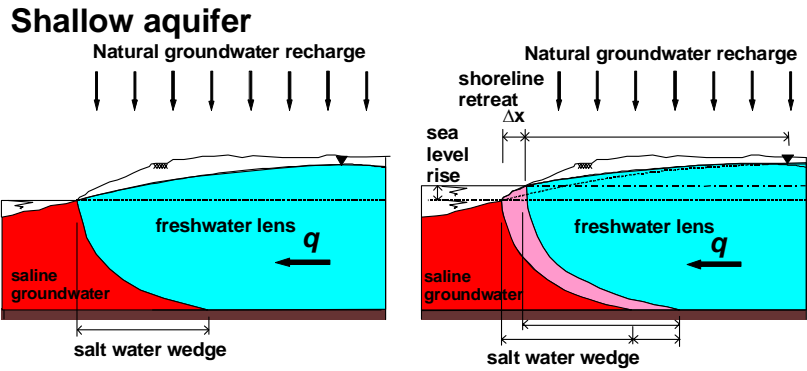
2100		G	G+	W	W+	C	C+
Worldwide temperature rise in 2050		+1°C	+1°C	+2°C	+2°C	+3°C	+3°C
Worldwide temperature rise in 2100		+2°C	+2°C	+4°C	+4°C	+6°C	+6°C
Change in airstream pattern Western Europa		no	yes	no	yes	no	yes
Winter	Average temperature	+1,8°C	+2,3°C	+3,6°C	+4,6°C	+5,4°C	+6,9°C
	Coldest winter day each year	+2,1°C	+2,9°C	+4,2°C	+5,8°C	+6,3°C	+7,8°C
	Average precipitation	7%	14%	14%	28%	21%	42%
Summer	Average temperature	+1,7°C	+2,8°C	+3,4°C	+5,6°C	+5,1°C	+8,4°C
	Hottest summer day each year	+2,1°C	+3,8°C	+4,2°C	+7,6°C	+6,3°C	+11,4°C
	Average precipitation	6%	-19%	12%	-38%	18%	-57%
Sea level rise	Absolute rise (cm)	35-60	35-60	40-85	40-85	45-110	45-110

Introduction

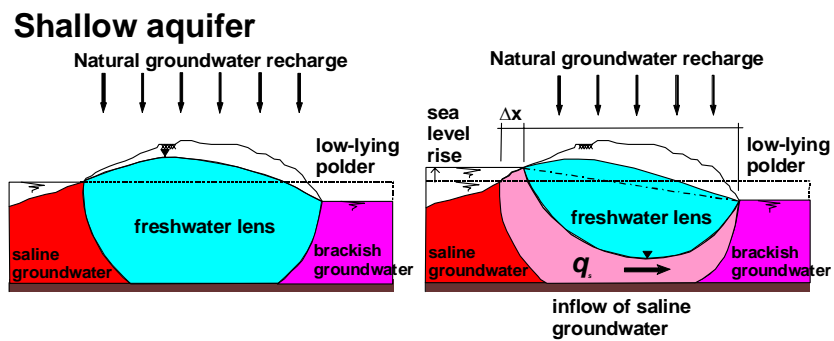
Effect of a relative sea level rise (1):



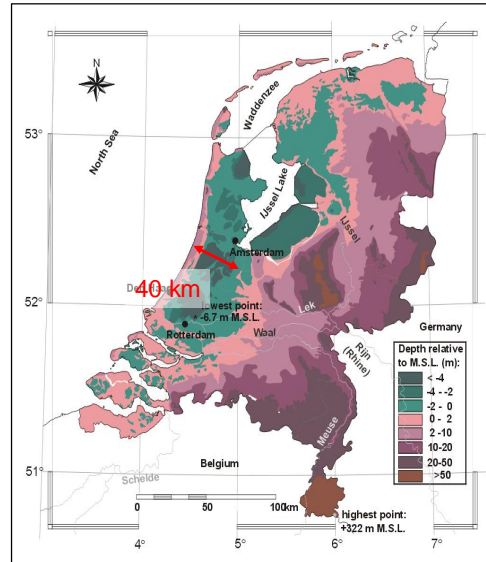
### Effect of a relative sea level rise (2):



### Effect of a relative sea level rise (3):

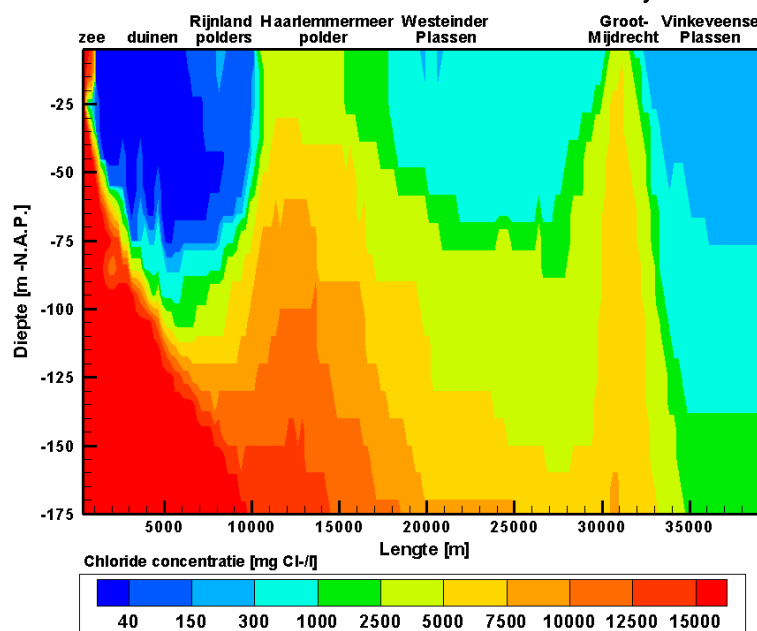


## 2D Profile and effect sea level rise



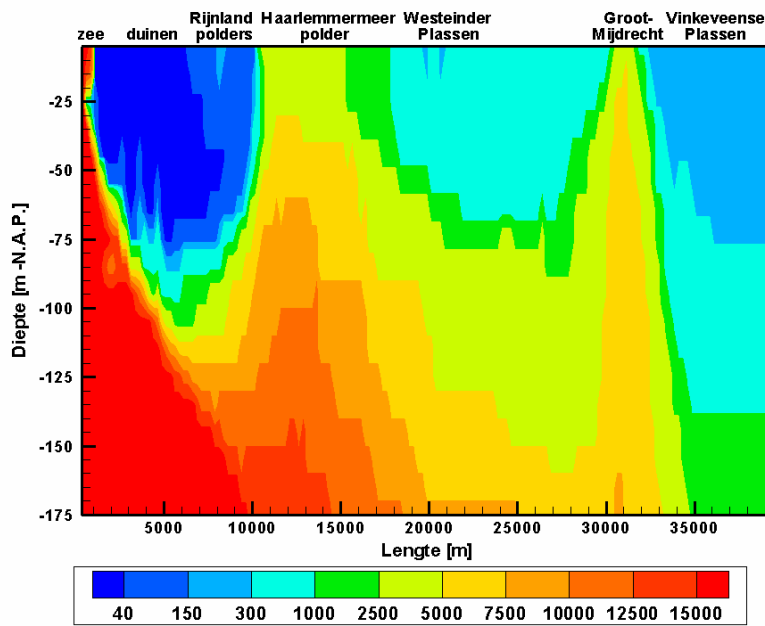
### Verzilting van het regionale grondwater systeem door autonome processen (geen zeespiegelstijging)

Tijd= 1990 AD



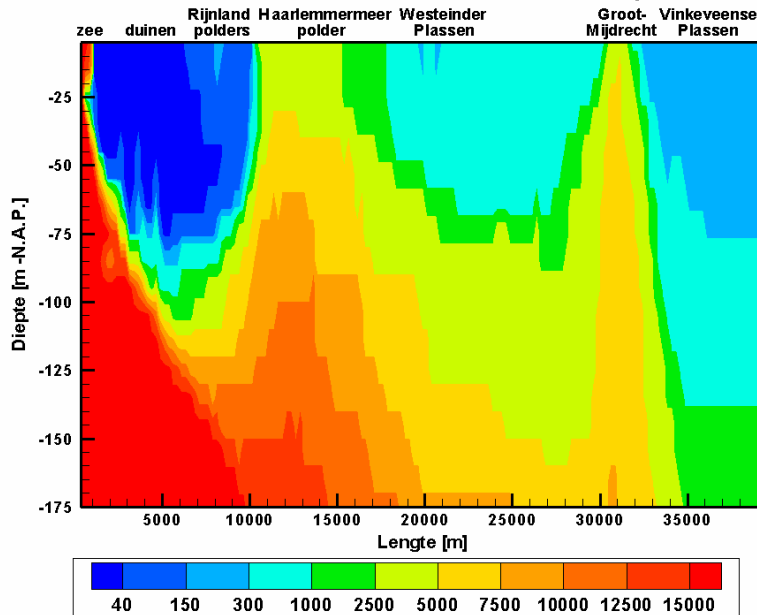
Verziltion van het regionale grondwater systeem door autonome processen  
(geen zeespiegelstijging)

Tijd= 1990 AD



Verziltion van het regionale grondwater systeem door autonome processen  
(zeespiegel daling = -60 cm per eeuw)

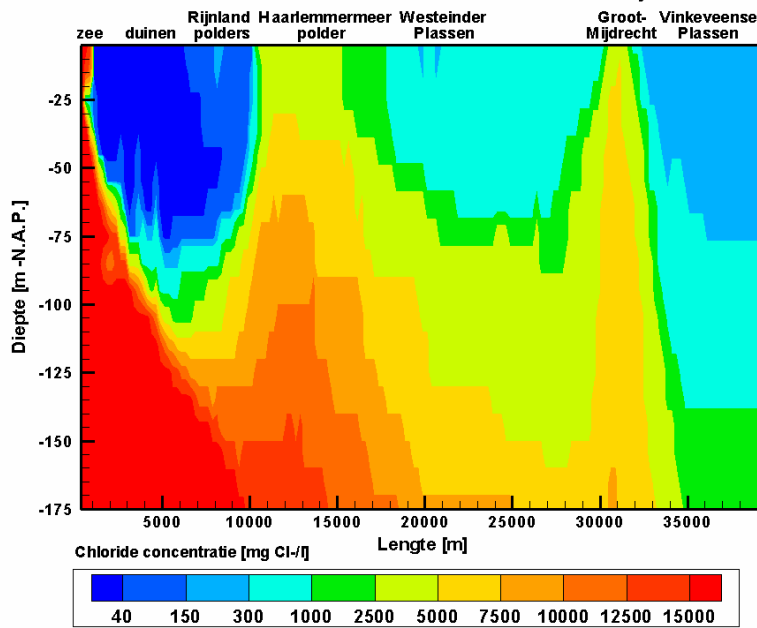
Tijd= 1990 AD





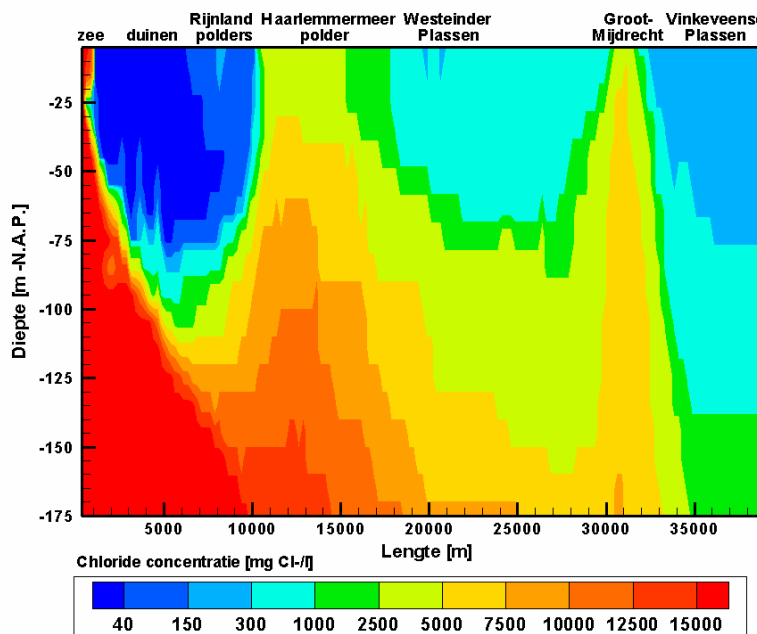
Verziltig van het regionale grondwater systeem door autonome processen  
(zeespiegelstijging=60cm per eeuw)

Tijd= 1990 AD



Verziltig van het regionale grondwater systeem door autonome processen  
(zeespiegelstijging=150cm per eeuw)

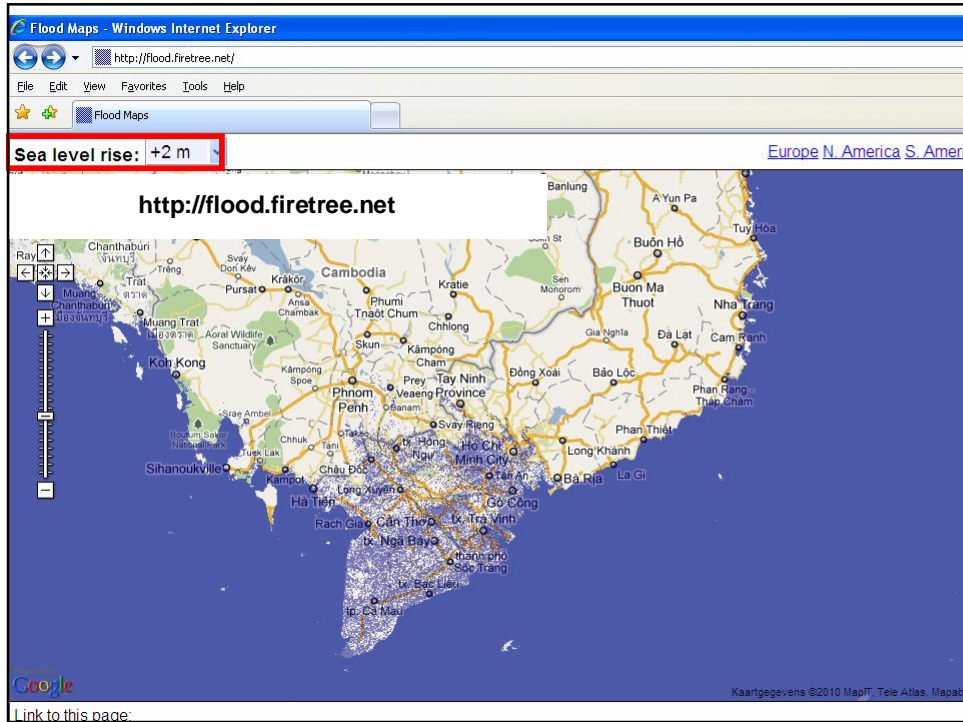
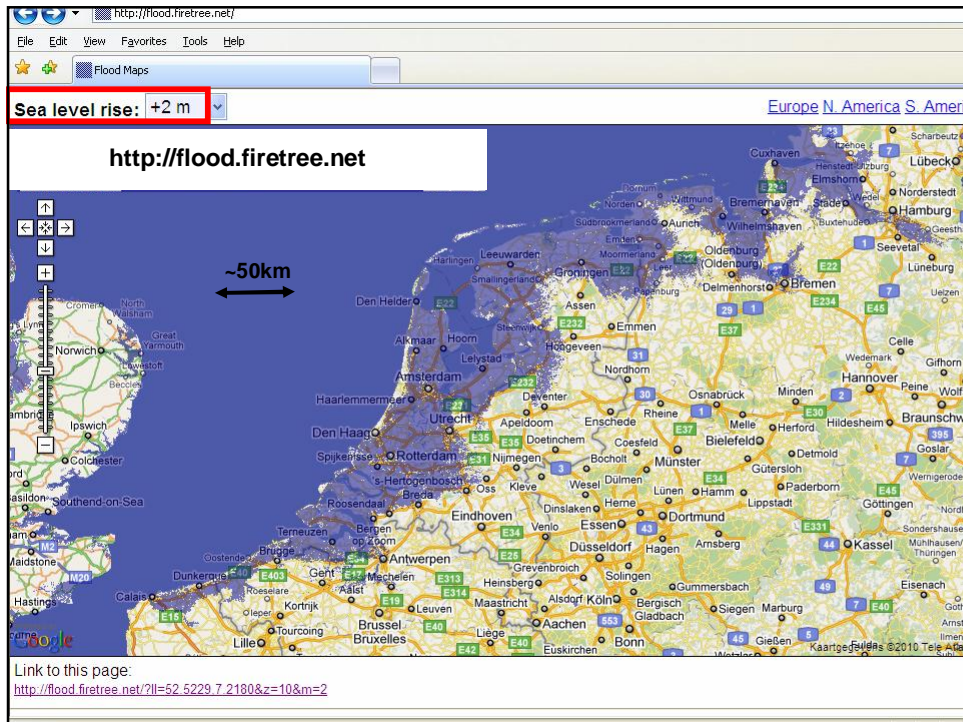
Tijd= 1990 AD



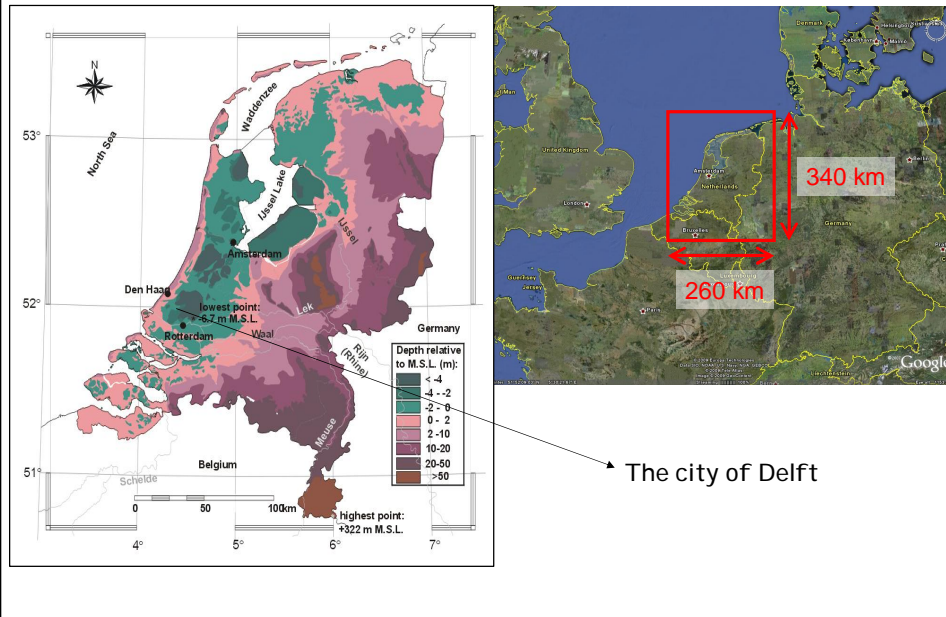
To get an idea about the possible future effects of sea level  
rise and climate change in your delta ...

*evaluate of the past water management in the Dutch delta*

Salt water intrusion in the Netherlands



## The 'low-lying' lands: Netherlands



## Case study: The Netherlands

The Dutch coastal zone is already theathened by sea level rise and land subsidence for many centuries

Intensive water management system

Coping with salt water intrusion problems since 1950's



## The 'low-lying' lands: Netherlands

The facts:

- a deltaic area with 3 rivers: Meuse, Scheldt & Rhine
- 25% of land surface is lying below mean sea level
- 65 % would be flooded regularly if there were no dunes and dikes
- 8 million people would be endangered



## The Great Flooding in february 1953

Combination of high tide and heavy storm:

- 1853 casualties
- 2000 km<sup>2</sup> flooded



## Infrastructure to protect our low-lying land from flooding



## River flooding in 1995

Combination of heavy rains upstream the catchment & short retention time



## Dike collapse 2003

Combination of peat dike instability and very dry summer

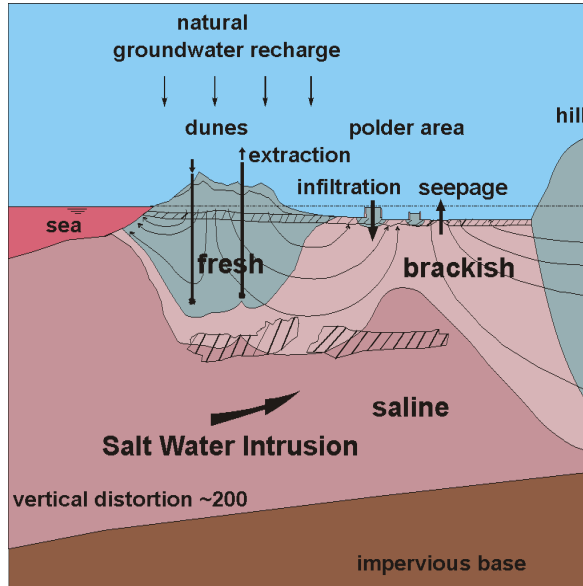


## Estimated water management costs 'to keep our feet dry'

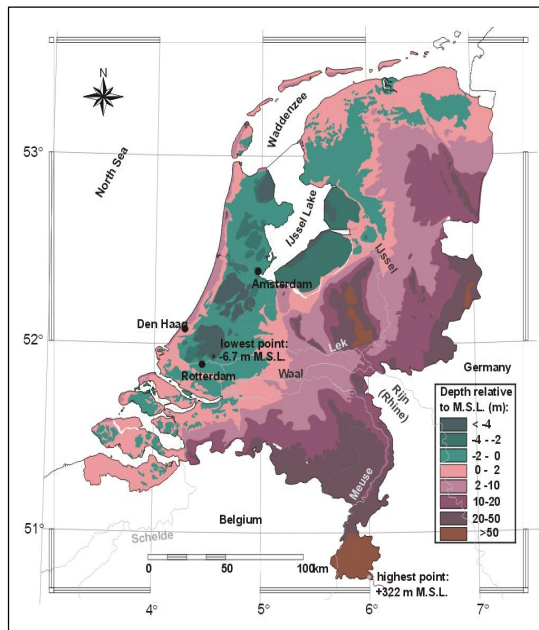
Costs up till 2050 in billion euros:

ivers: upper part	5.7
ivers: lower part	5.6
low-lands	1.7
coastal zone	8.0
infrastructure	3.5
purchase of ground	2.0
	-----+
	26.5 billion euros

### Salt water intrusion in the Netherlands



### Present ground surface in the Netherlands

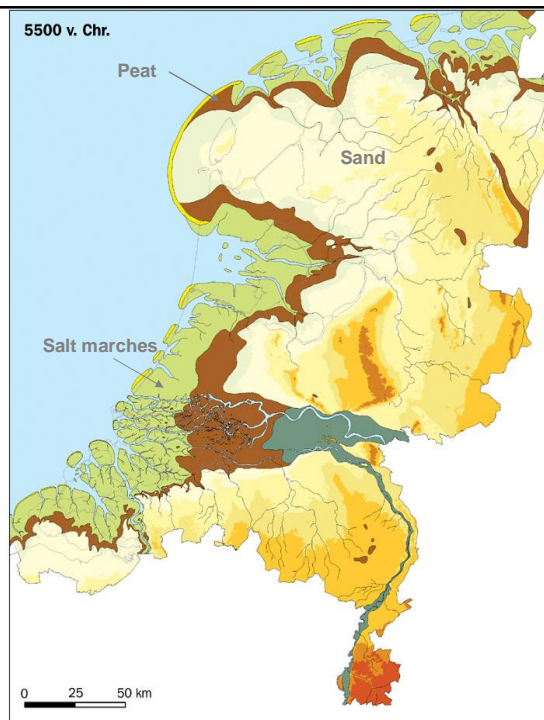




## The Holocene transgressions

Major impact on present regional brackish groundwater systems

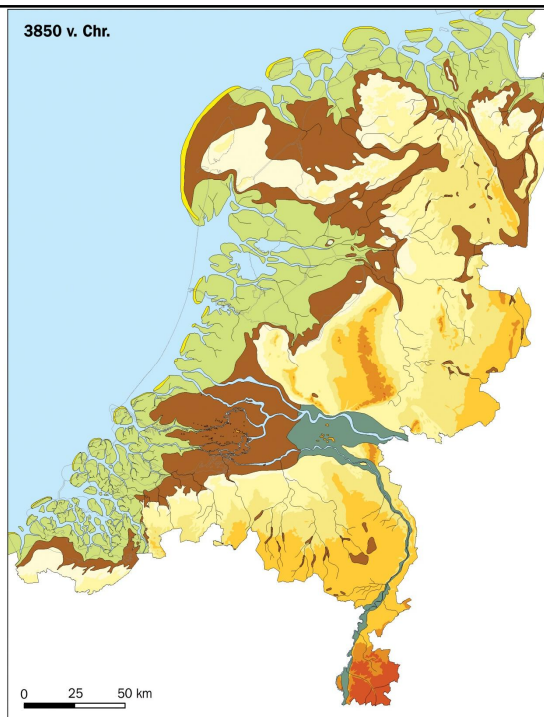
7500 BP



## The Holocene transgressions

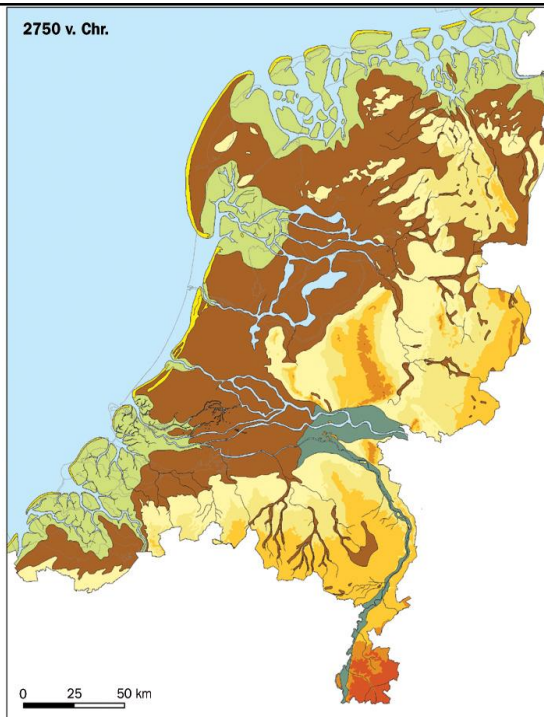
Maximum transgression

5850 BP



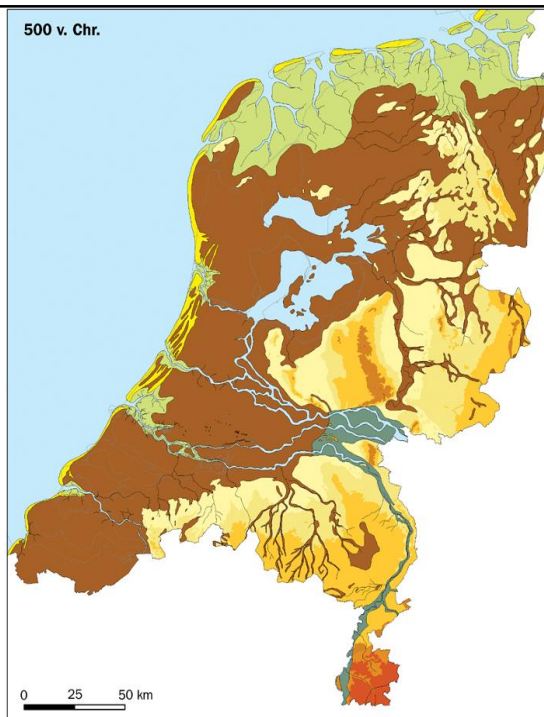
# The Holocene transgressions

4750 BP



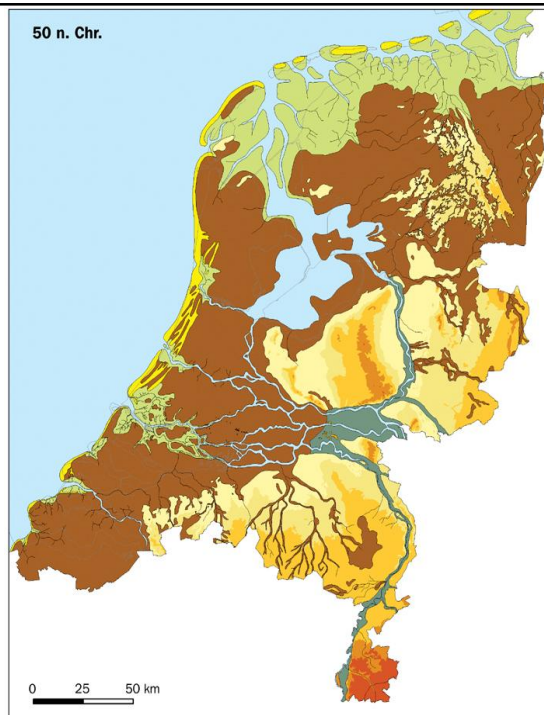
# The Holocene transgressions

2500 BP



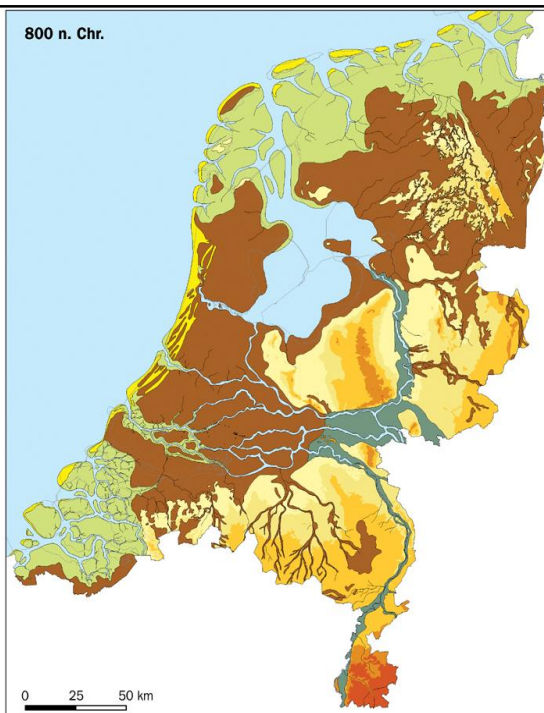
# The Holocene transgressions

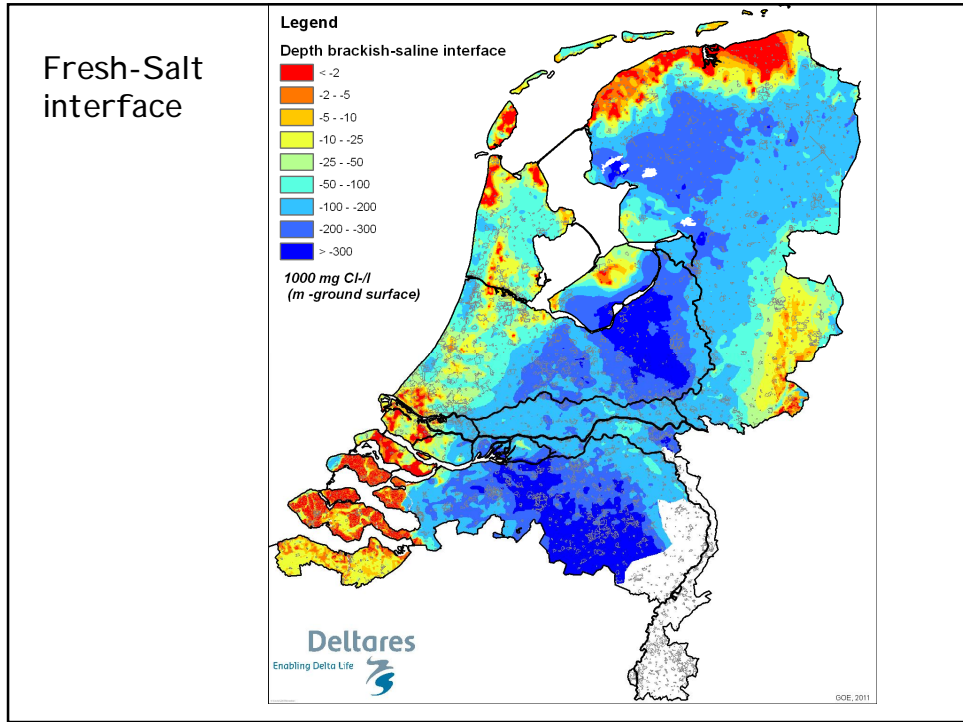
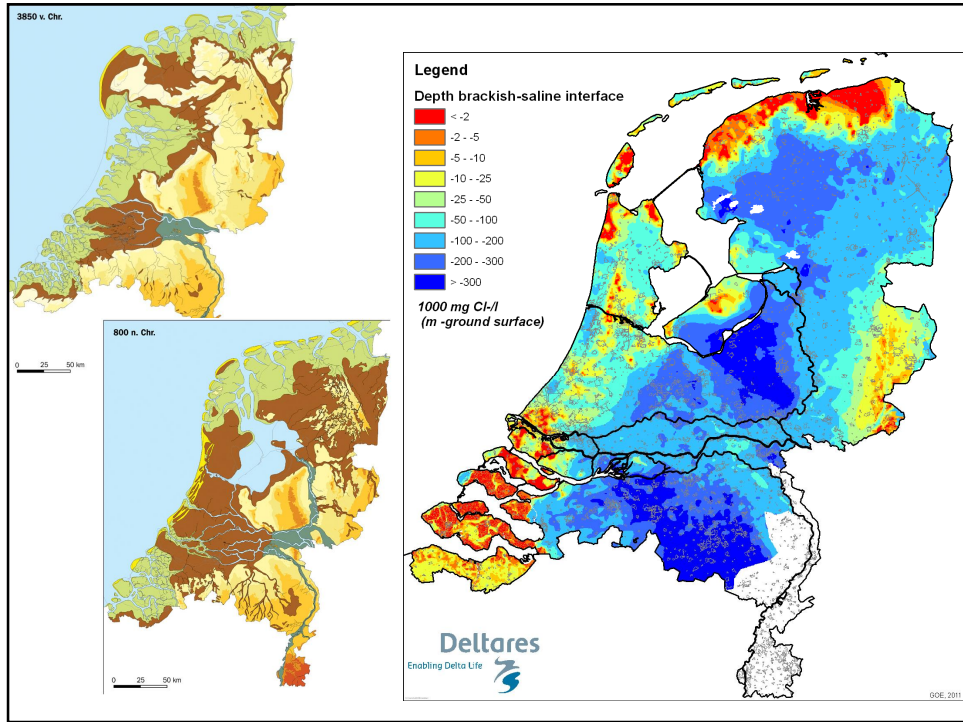
50 AD (Roman time)



# The Holocene transgressions

800 AD





## Salinisation of the Dutch subsurface

### Physical transport processes:

- advective: e.g. trans- and regressions
- dispersive: mixing with marine deposits
- diffusive: e.g. IJsselmeer lake
- chemical: solution, precipitation, ion-exchange

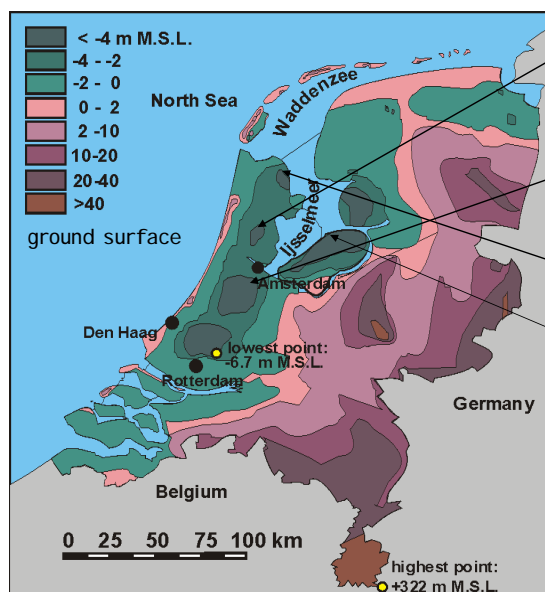
### Anthropogenic causes:

- land subsidence
- polder level lowering
- groundwater extractions

### Future developments (climate change):

- sea level rise
- changes in recharge

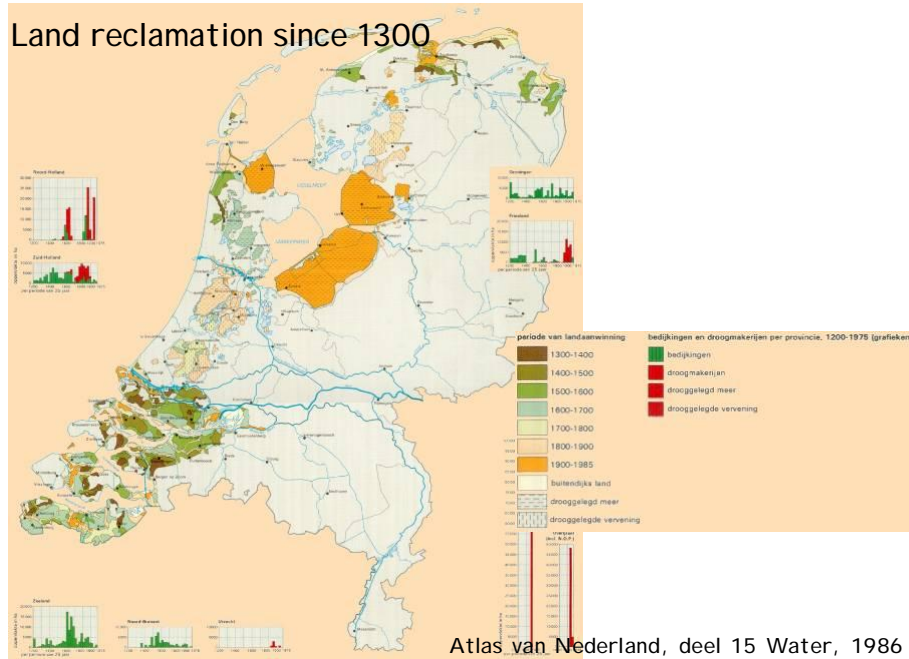
## Abrupt land subsidence



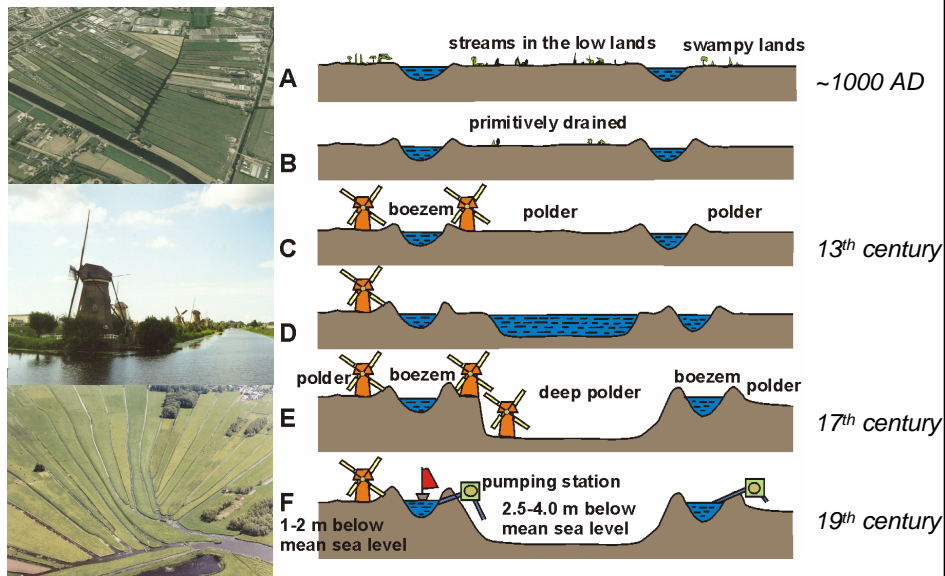
### position polders:

- Beemster 1608-1612
- Wormer 1625-1626
- Schermer 1633-1635
- Purmer 1618-1622
- Haarlemmermeer polder 1850-1852
- Wieringermeer polder ~1930
- Flevo polders 1950-60s

## Land reclamation since 1300



## Development of the Dutch 'Polder' Landscape

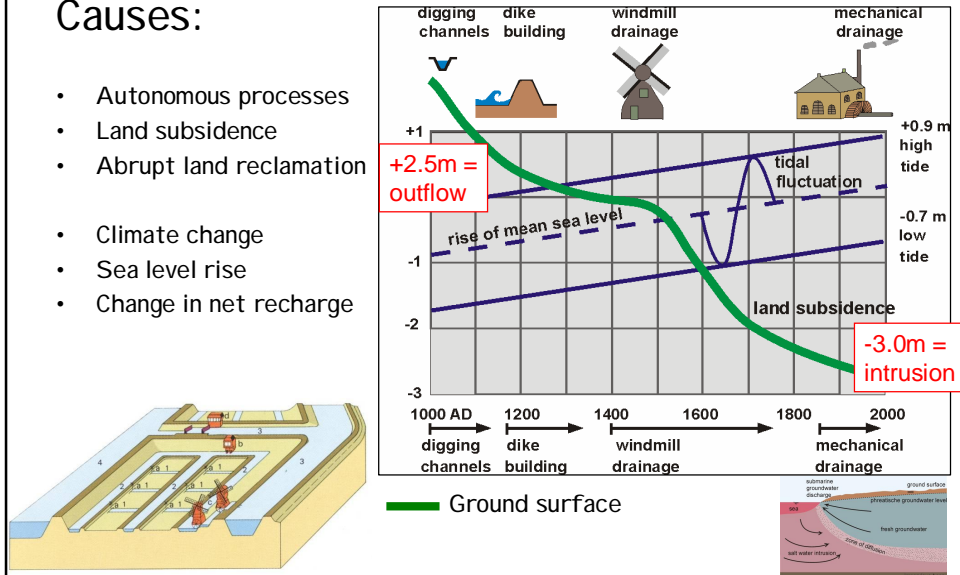


# From fresh water outflow to salt water inflow

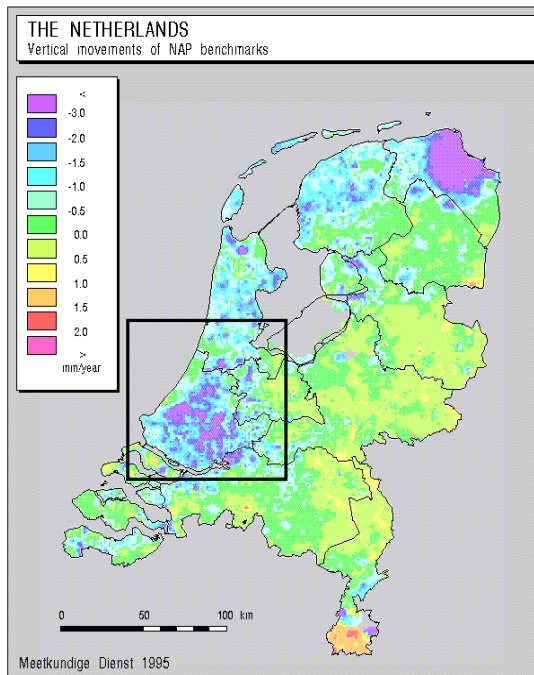
## Causes:

- Autonomous processes
- Land subsidence
- Abrupt land reclamation
- Climate change
- Sea level rise
- Change in net recharge

## Historical subsidence of the ground surface in Holland



## Land subsidence related to M.S.L.



## Land subsidence



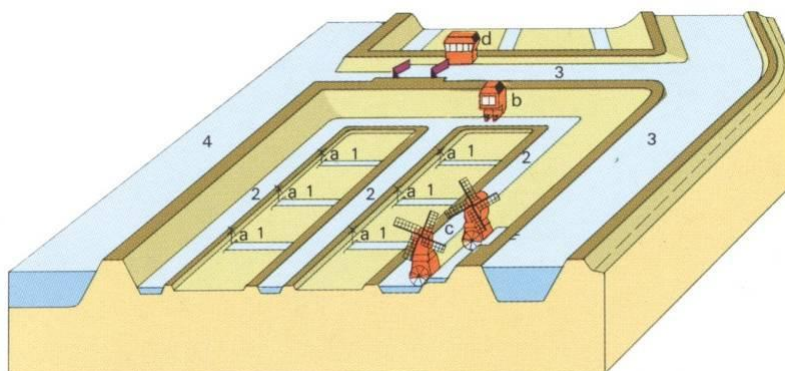
up to 1 m per century



## The polder system

A land below the sea with an excess of water needs..

*a sophisticated drainage system*





The polder system

*Many agricultural plots with different water levels throughout the season*



The polder system



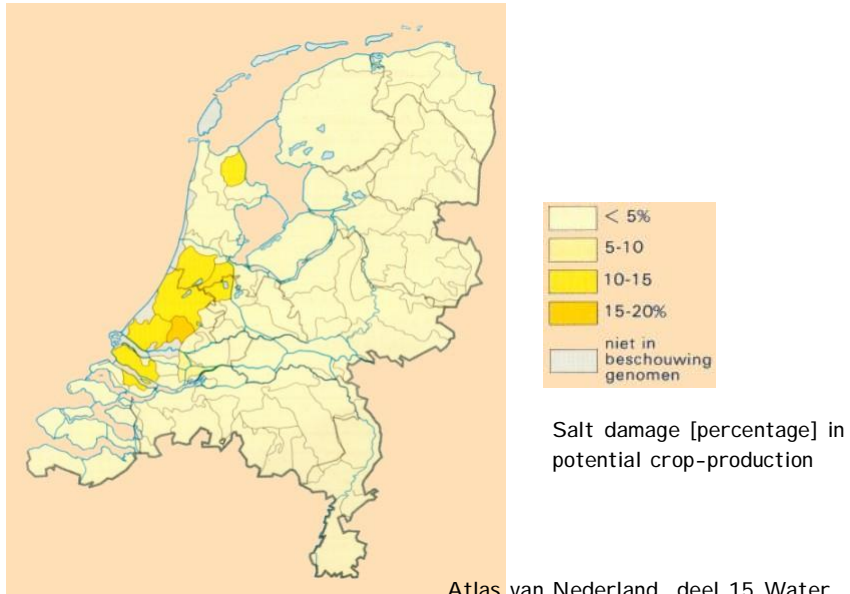
## The polder system



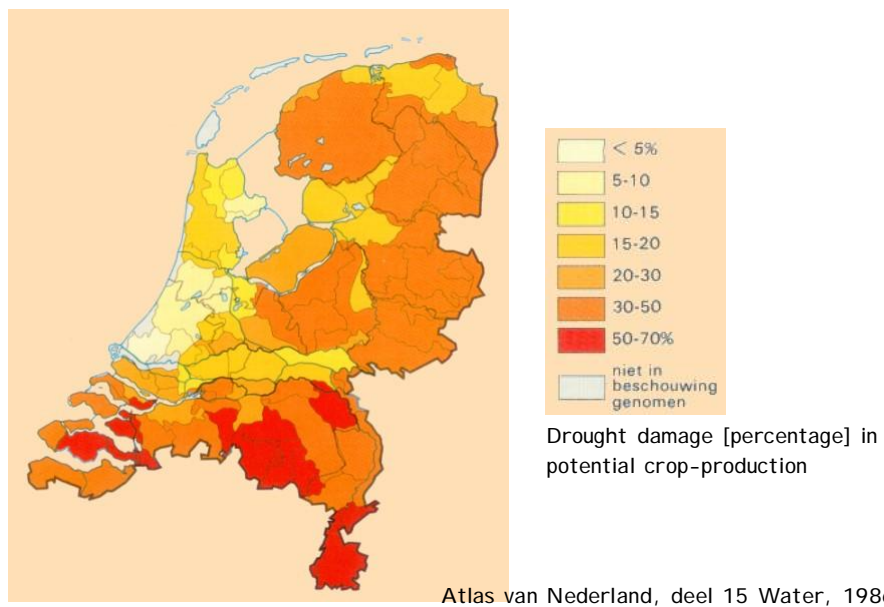
## Bulb farms at the landside of the sand dunes



### Salt damage in 1976 (very dry year)



### Drought damage in 1976 (very dry year)



### 'Wetting' damage

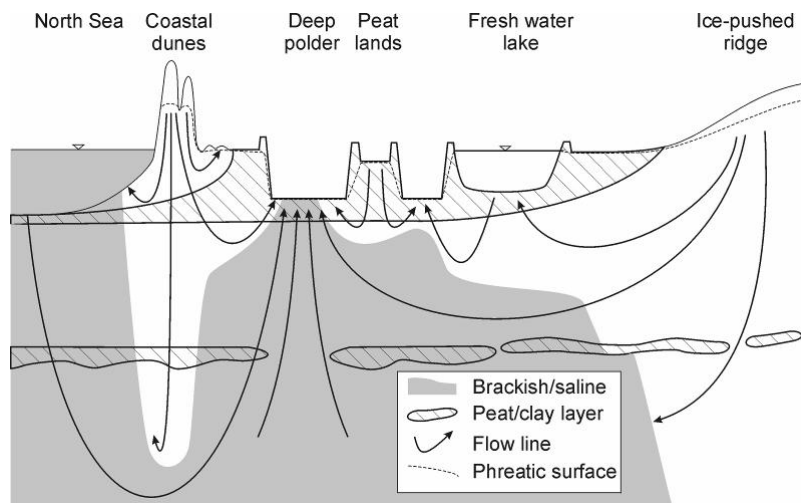


Normal situation

*Crop damage due to a reduction in groundwater extraction in the dune area*

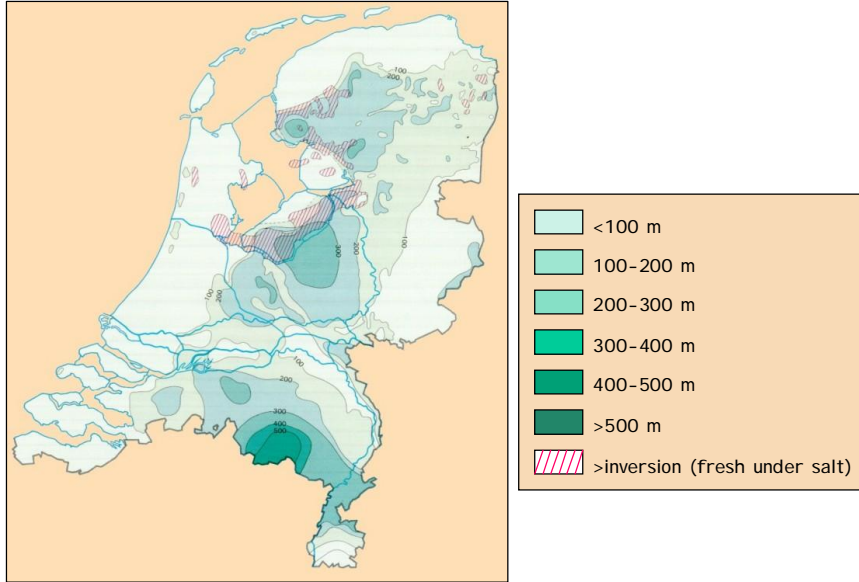


### Now focus on groundwater...



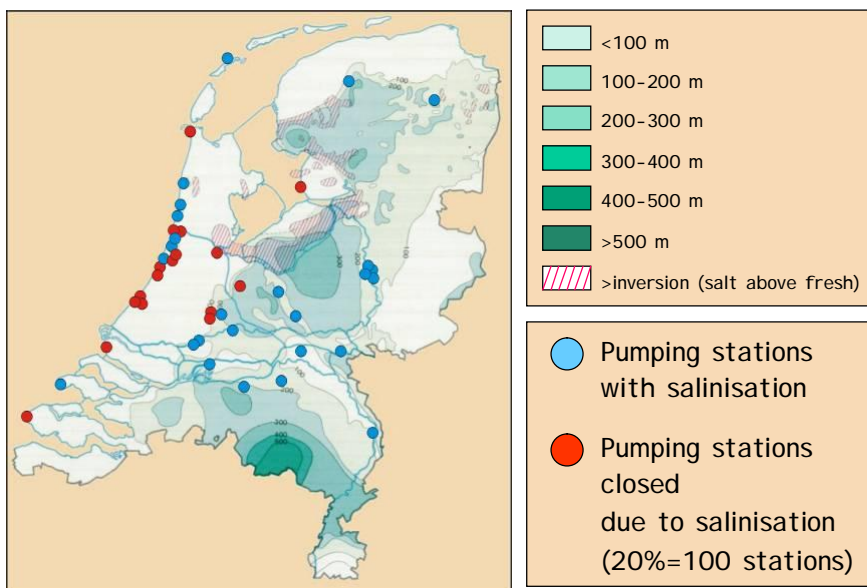
Present situation

### Fresh-salt interface (150 mg Cl<sup>-</sup>/l)

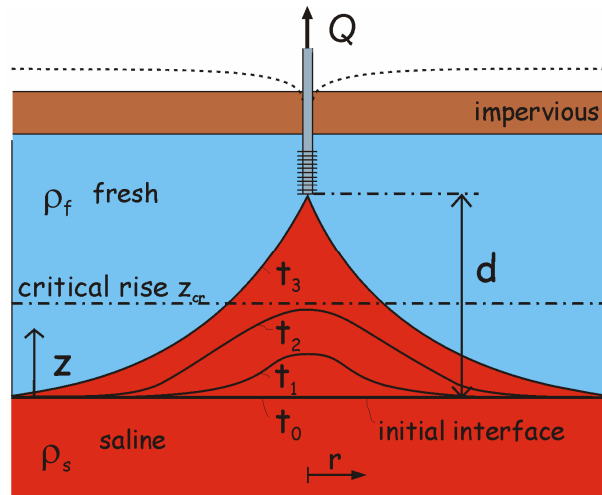


Impacts

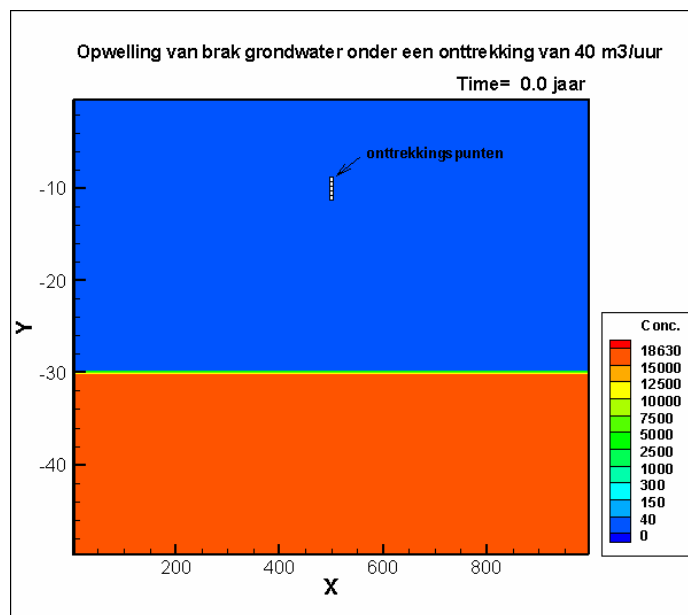
### Availability of fresh groundwater



### Upconing of saline groundwater under extraction well



### Upconing of salt under an extraction



## Threats to water management due to climate change:

Short term threats:

- flooding
- dike collapse
- drought

*asks for operational water management*

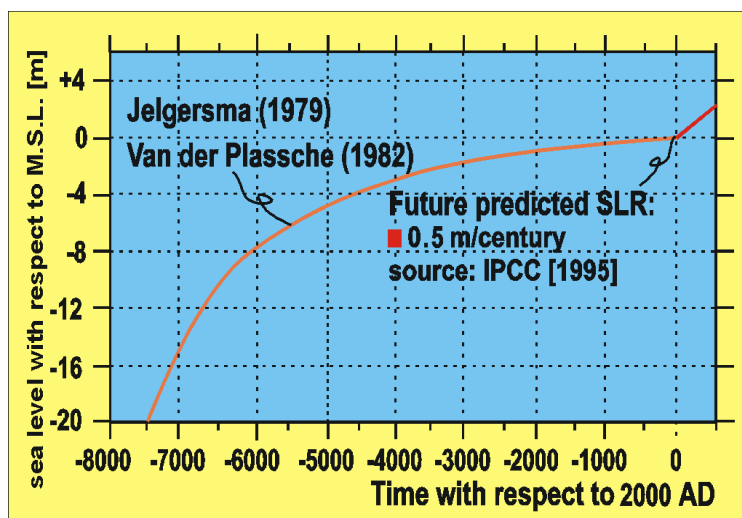
Long term threats:

- salt water intrusion
- land subsidence
- smaller fresh groundwater resources

*asks for strategic water management*

Dutch setting

### Past and future sea level rise in the Netherlands



## Numerical variable density models at Deltares

### Characteristics:

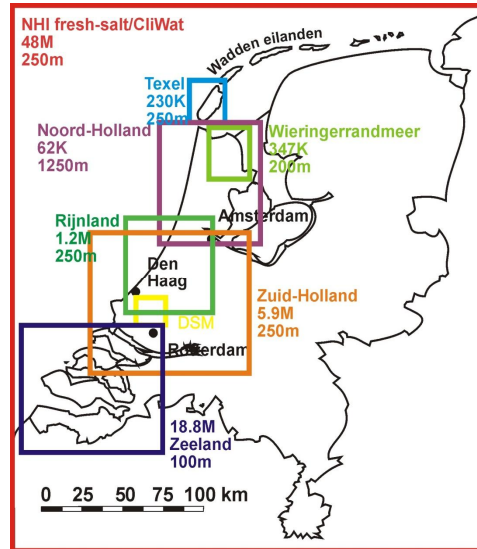
- variable-density groundwater
- fresh, brackish and saline
- 3D, non-steady
- coupled solute transport

### Code (MODFLOW family):

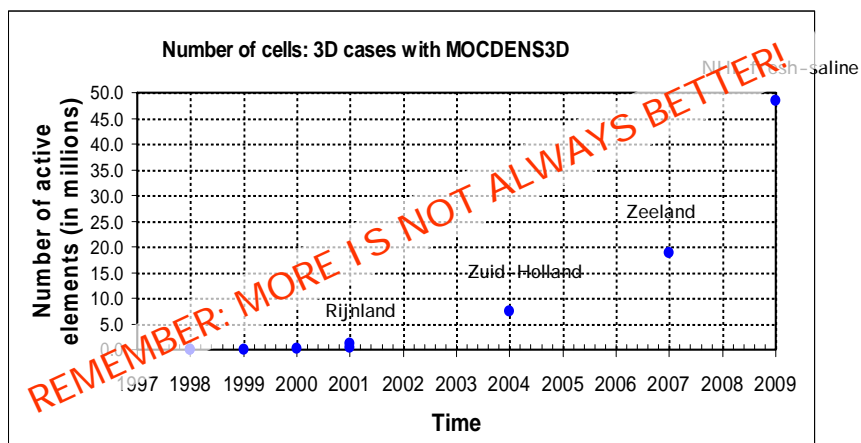
MOCDENS3D  
SEAWAT

### Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- land subsidence
- changing extraction rates
- adaption measures



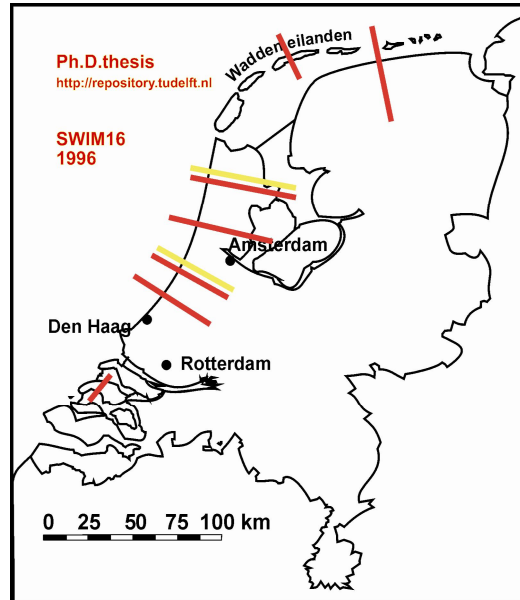
**'DO NOT DO THIS AT HOME!' (DATA PROBLEM)**





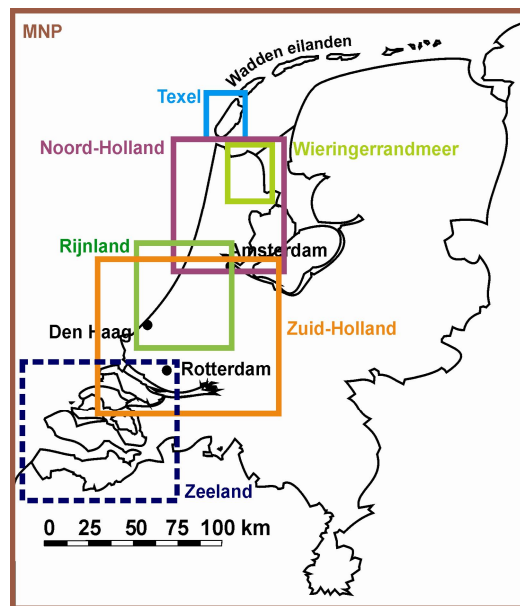
## Modelling effect sea level rise on salt water intrusion

### 2D models



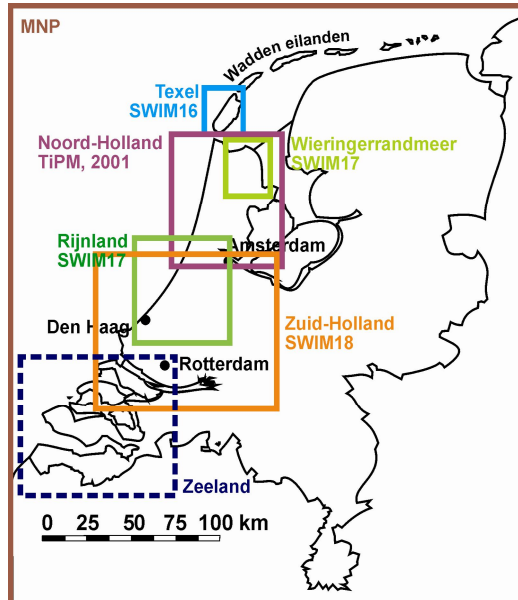
## Modelling effect sea level rise on salt water intrusion

### 3D models



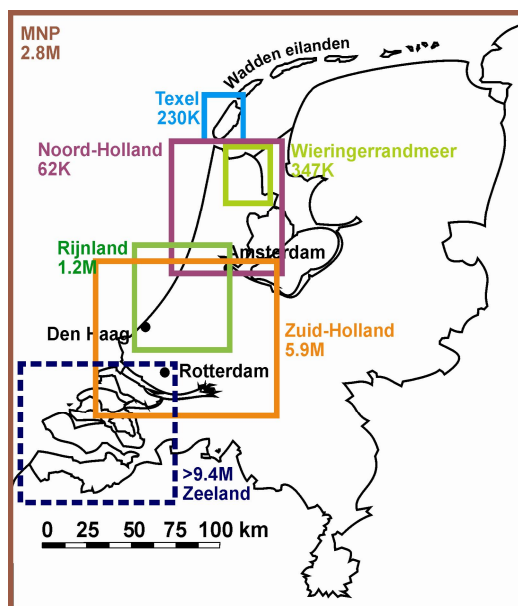
## Modelling effect sea level rise on salt water intrusion

3D models  
SWIM



## Modelling effect sea level rise on salt water intrusion

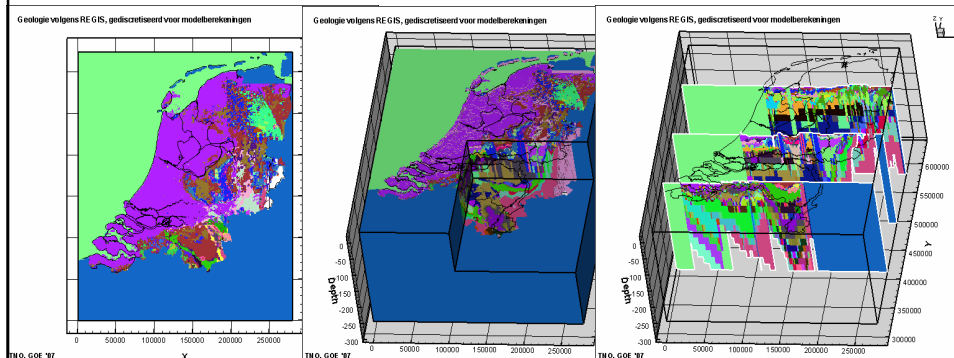
3D models  
number cells



## Recent model study for the whole Netherlands on the effect of sea level rise of water management (1)

Using the national subsoil parametrisation

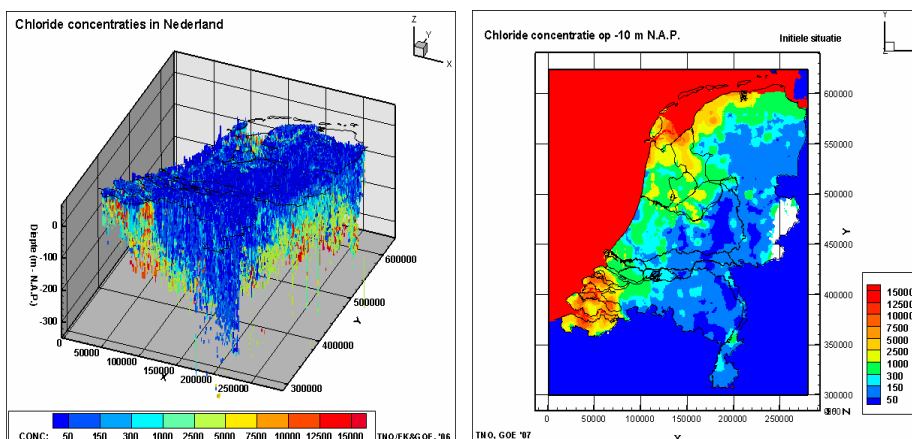
- REGIS V2
- Top geological system from +10m up to -280m M.S.L.
- 31 modellayers with thicknesses: 2\*5m; 10\*2m; 8\*5m en 11\*20m
- cellsize 1000x1000m (coarse)



## Recent model study for the whole Netherlands on the effect of sea level rise of water management (2)

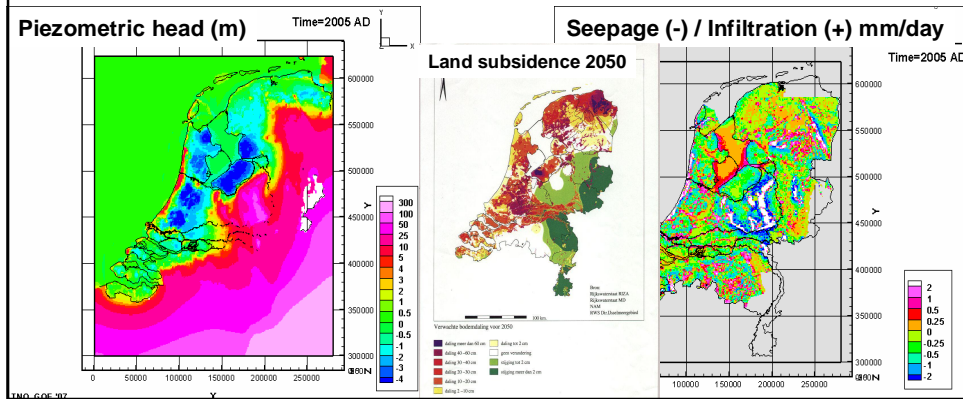
Using the national 3D salt concentration in groundwater

Zoet-Zout REGIS: ~65000 measuring points (analyses, VES, Borehole)

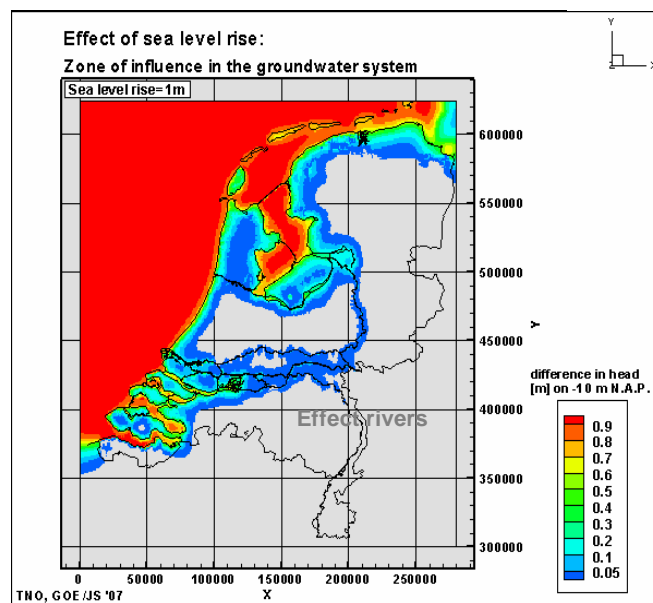


## Recent model study for the whole Netherlands on the effect of sea level rise of water management (3)

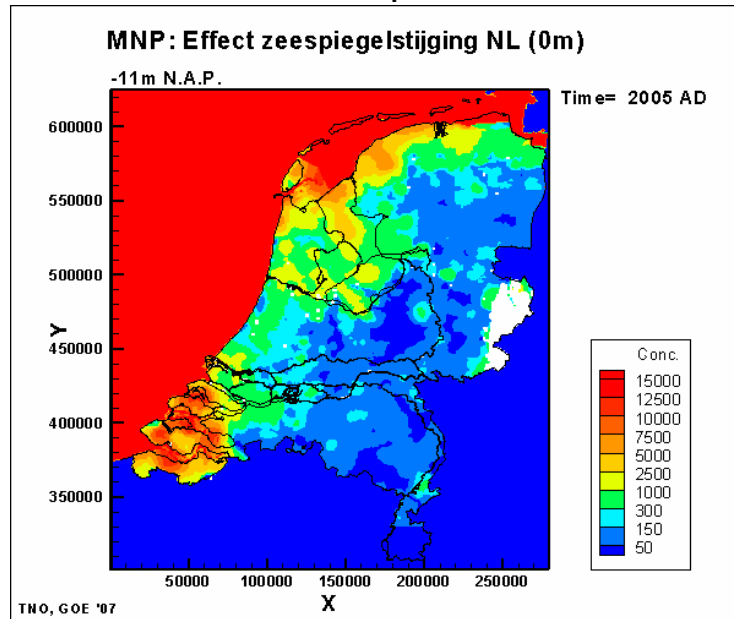
- Variable-density 3D groundwater flow model and coupled solute transport
  - 10 scenario's, including extreme sea level rise
  - including land subsidence estimates



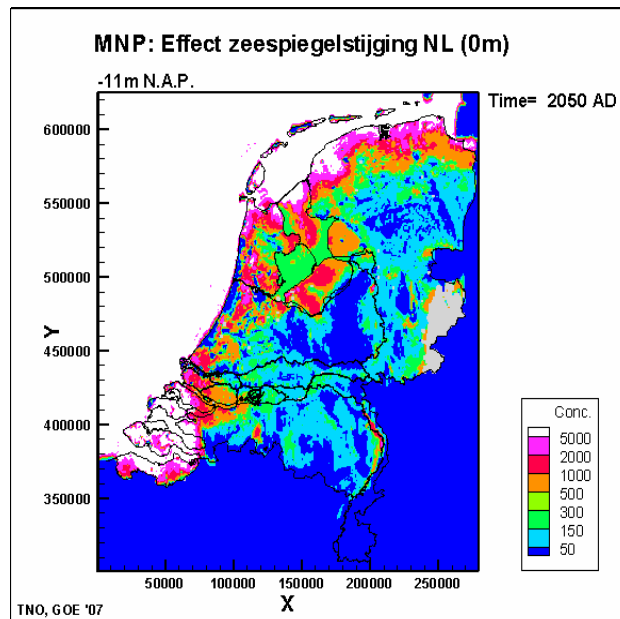
## Results: zone of influence 1m sea level rise



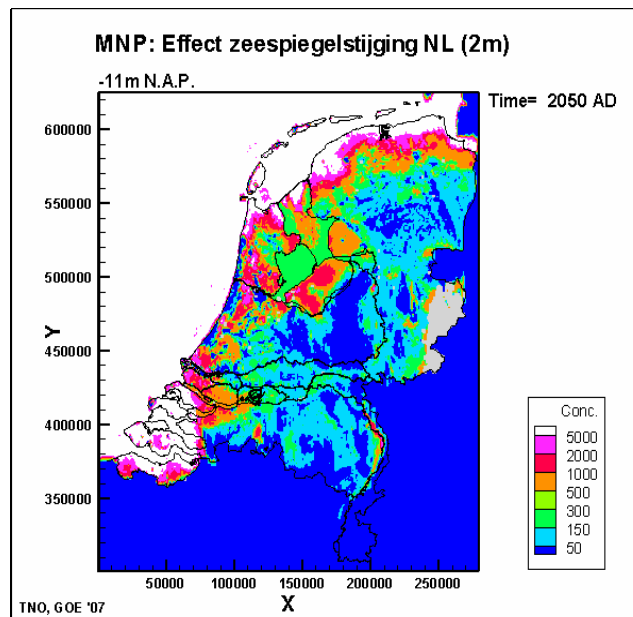
## Salinisation over the period 2000-2050



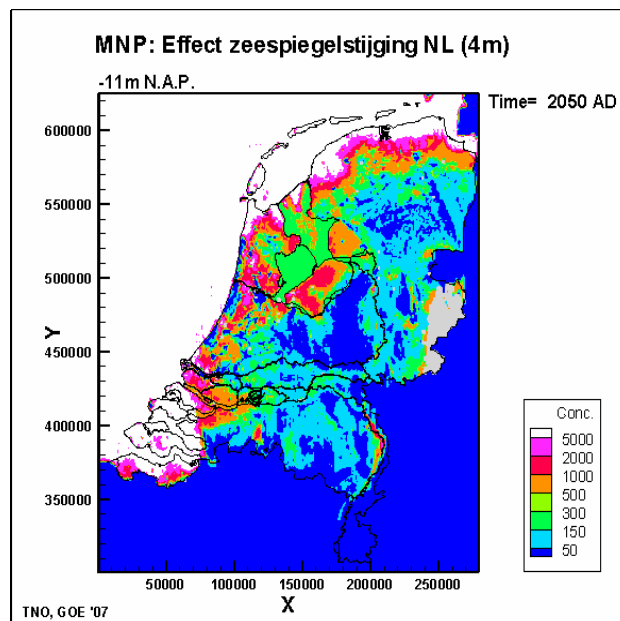
## Salinisation subsoil at 0m sea level rise in 2050



## Salinisation subsoil at 2m sea level rise in 2050

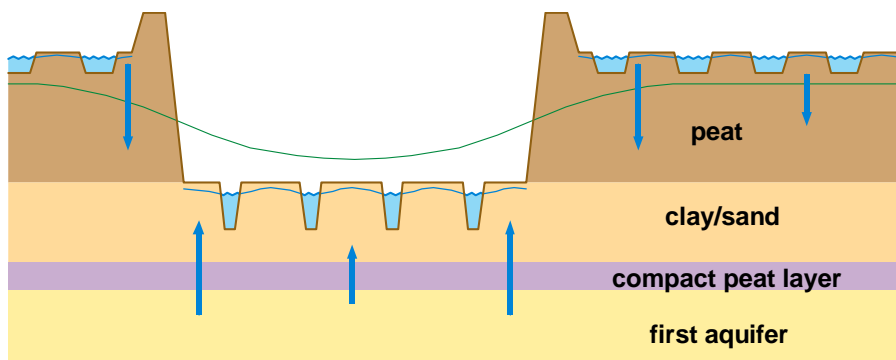


## Salinisation subsoil at 4m sea level rise in 2050

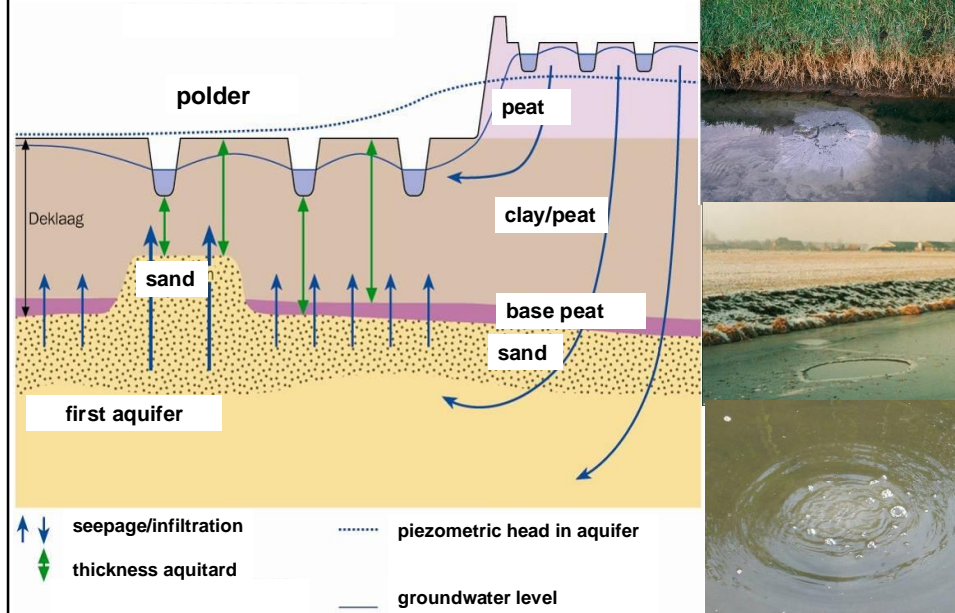


# Salty wells

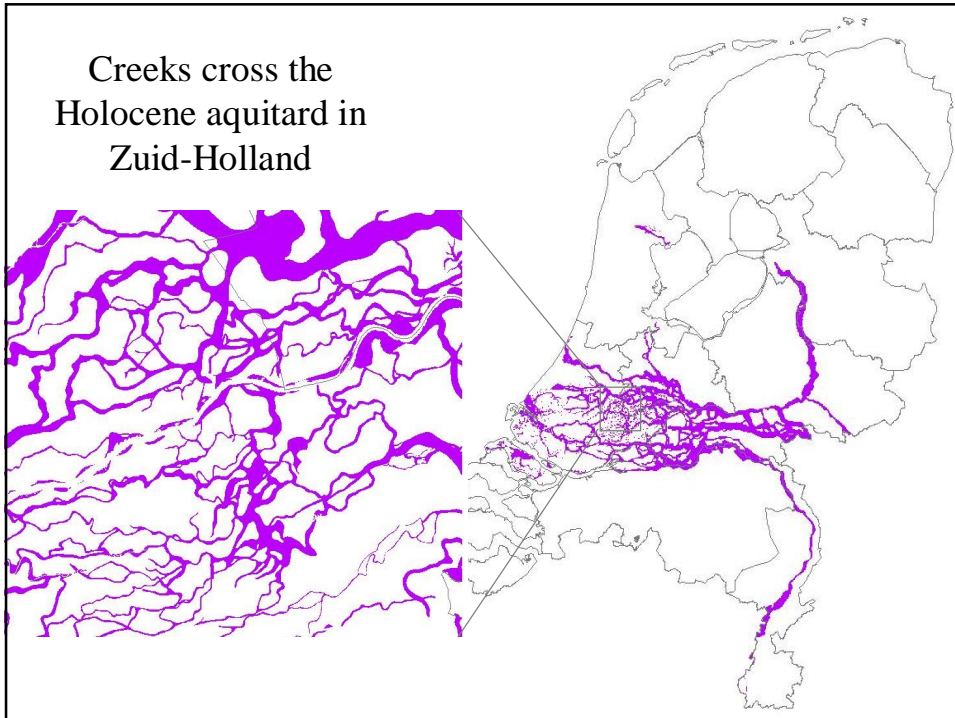
Seepage and infiltration situation around deep polders



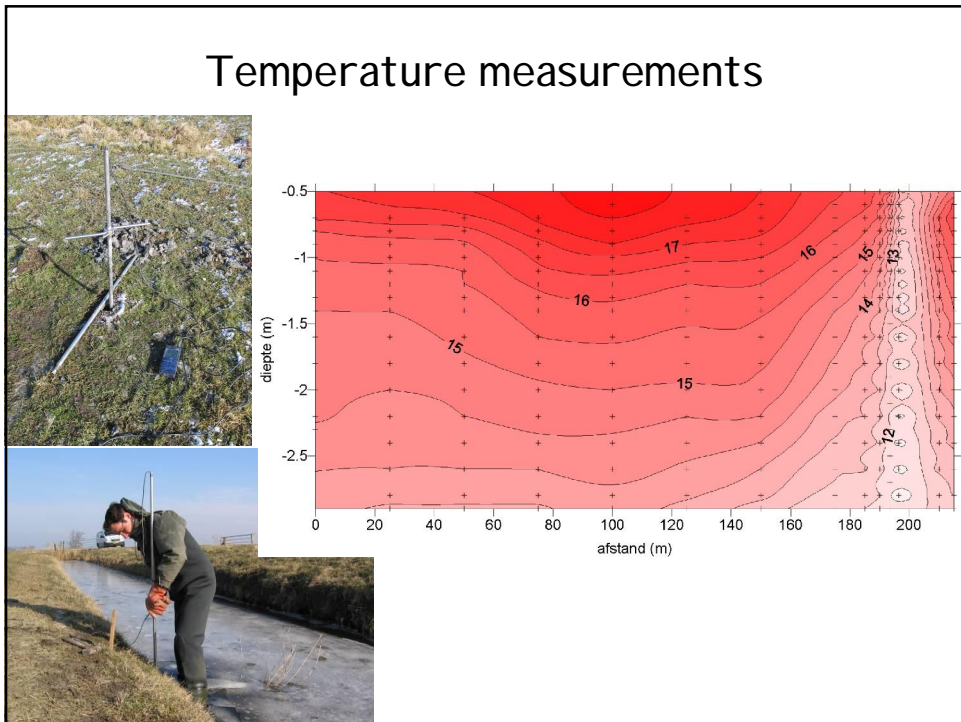
## Risk of instable Holocene aquitards (1)



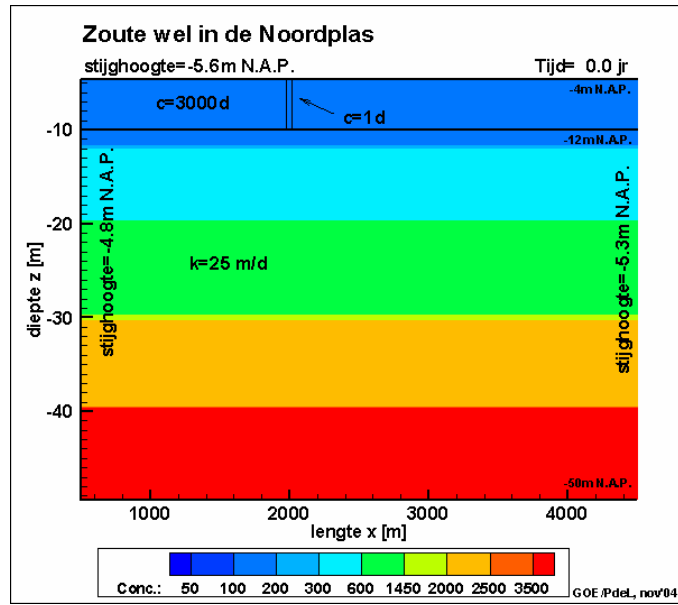
## Creeks cross the Holocene aquitard in Zuid-Holland





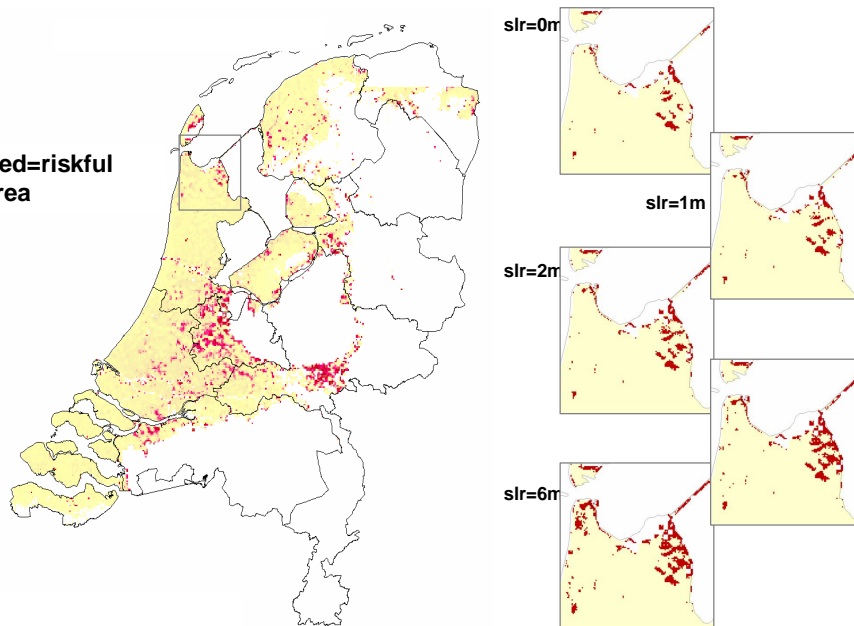


## Simulation of salt groundwater towards wells

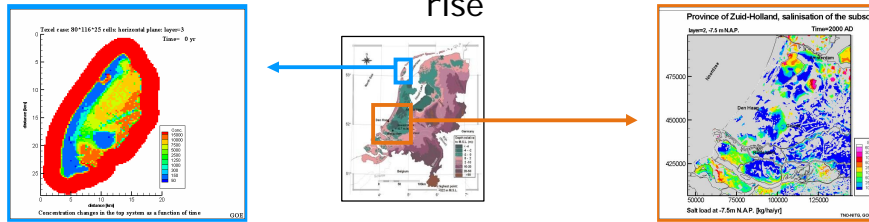


## Risk of instable Holocene aquitards (2)

Red=riskful area



## Quantification hydrogeological impacts of sea level rise

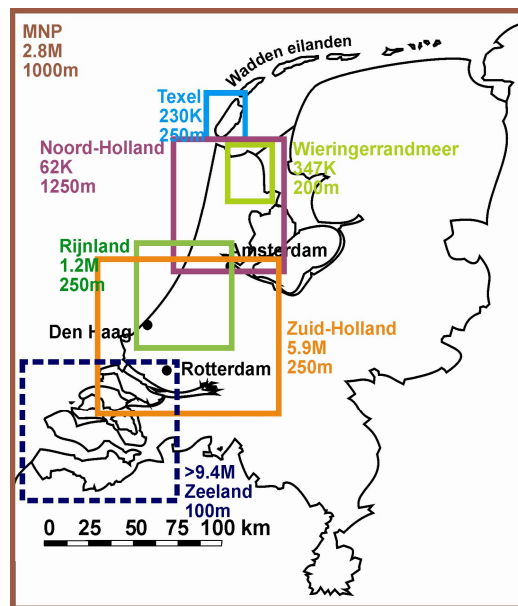


Situation at 2100 AD with sea level rise of 0.5m/century,  
Including land subsidence at Zuid-Holland (max 1.0m/century)

	<u>Texel</u>	<u>Zuid-Holland</u>
Increase seepage (%)	+22	+4
Increase salt load (%)	+46	+34
Hinge area: from infiltration to seepage (% land surface)	+3	+5

## Modelling effect sea level rise on salt water intrusion

3D models  
number cells  
grid size



### Characteristics 3D Cases (I): geometry & subsoil

Case	Kop van Noord-Holland	Texel	Wieringer-meerpolder	Rijnland
total land surface [km <sup>2</sup> ]	2150	130	200	1100
L <sub>x</sub> *L <sub>y</sub> modelled area [km]	65*51	20*29	23*27	52*60
depth system [m -N.A.P]	290	302	385	190
aquifer hydr.cond. [m/d]	5-70	5-30	15-40	12-70
aquitard hydr.cond. [m/d]	0.12-0.001	0.01-1	0.012-0.056	2.5E-4-0.8
porosity	0.35	0.3	0.25	0.25
anisotropy [k <sub>z</sub> /k <sub>x</sub> ]	0.4	0.4	0.25	0.1
long. dispersivity α <sub>L</sub> [m]**	2	2	2	1
# head&conc. observations	not applicable*	111	95	1632
characteristics head calibration	not applicable*	Δφ =0.24 m σ=0.77 m	Δφ =0.34 m σ=0.21 m	Δφ =0.60 m σ=0.77 m

\* calibration with seepage & salt load in polders

\*\*molecular diffusion=10<sup>-9</sup> m<sup>2</sup>/s; trans. disp.=1/10 long. disp.

### Characteristics 3D Cases (II): model parameters

Case	Kop van Noord-Holland	Texel	Wieringer-meerpolder	Rijnland (=391 EM RAM)
horizontal cell size [m]	1250*1250	250*250	200*200	250*250
vertical cell size [m]	10	1.5 to 20	2 to 70	5 to 10
total # active cells	~40.000	~126.000	~312.000	~1.200.000
# cells	41*52*29	80*116*23	116*136*22	209*241*24
# particles per cell	27	8	8	8
total time [yr]	1000	500	50	500

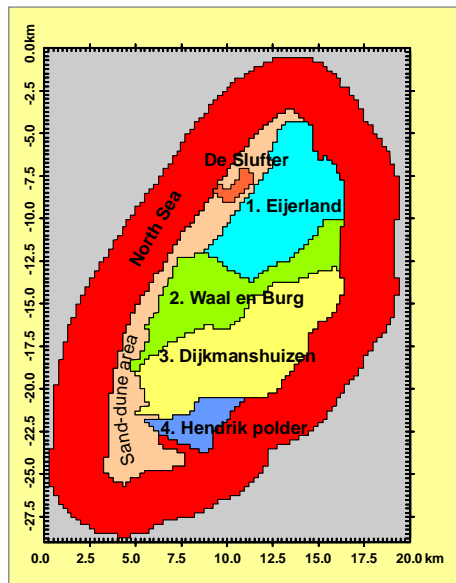
convergence head criterion= 10<sup>-5</sup>/10<sup>-4</sup> m

flow time step Δt=1 year

## Model of the island of Texel

### Characteristics of the island of Texel (I)

Texel



•Tourist island in summer time

•Land surface: 130 km<sup>2</sup>

•Polder areas:

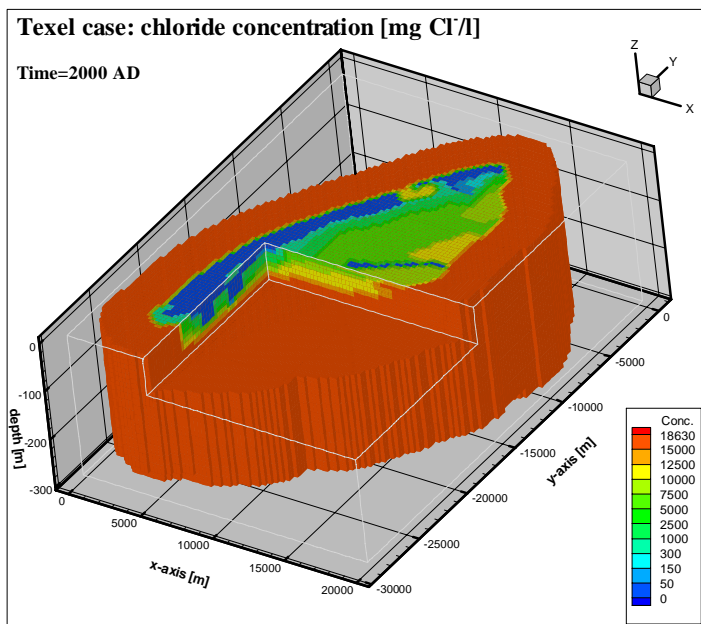
- 1. Eijerland
- 2. Waal en Burg
- 3. Dijkmanshuizen
- 4. Hendrik polder

• Sand-dune area at western side

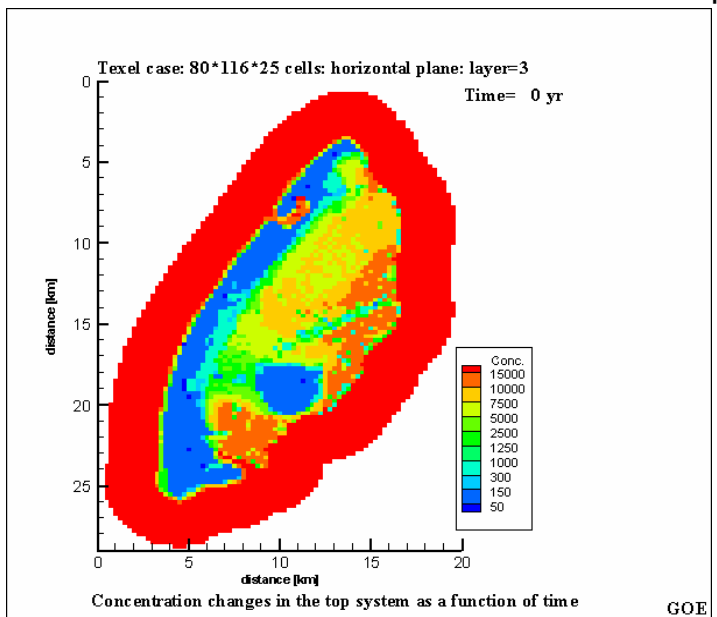
• 'De Slufter' is a tidal salt-marsh

• North Sea surrounds the island

### Texel: present 3D chloride distribution

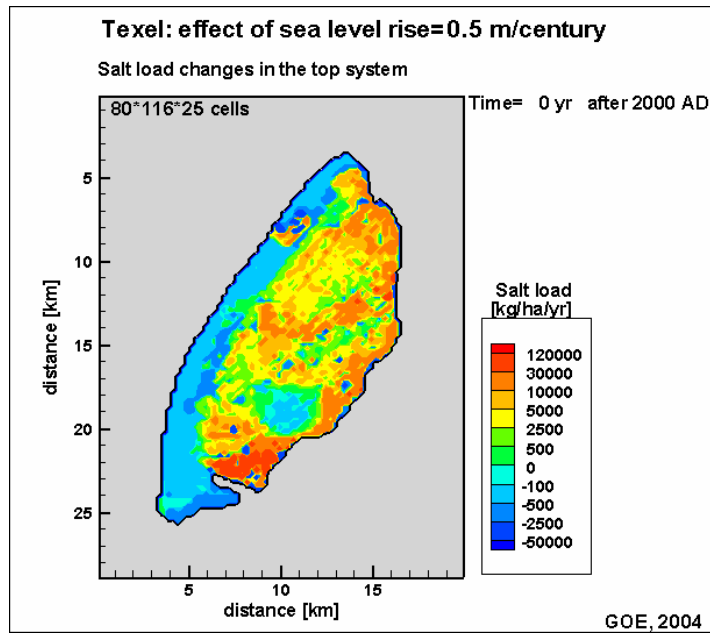


### Texel: reference case=autonomous development



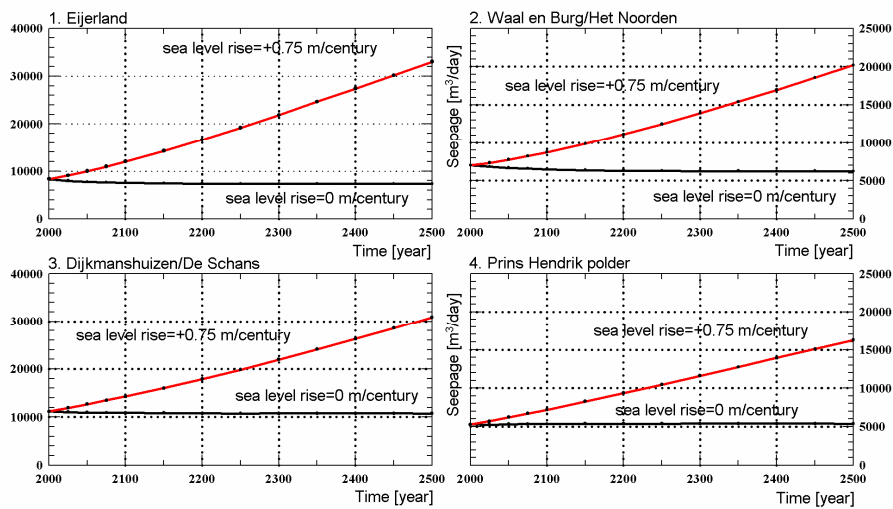
# Texel: effect of sea level rise on salt load

Texel

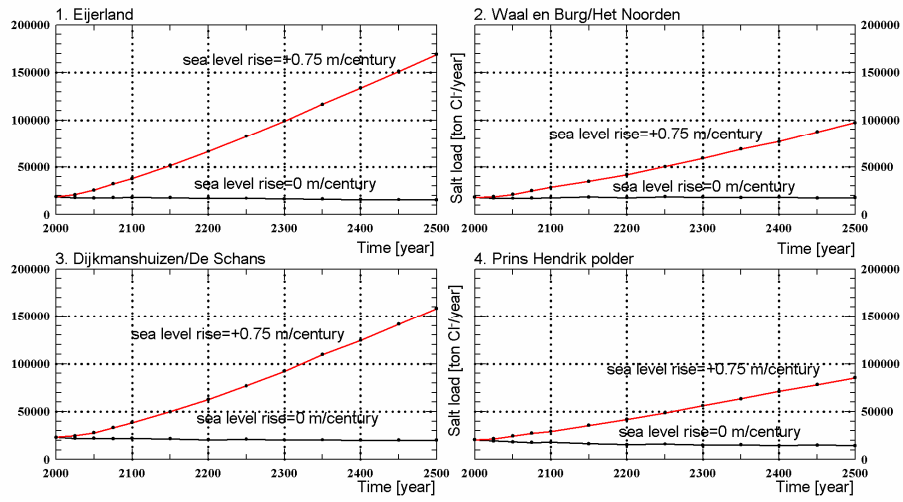


# Texel: change in seepage of the four polders

Texel



## Texel: change in salt load of the four polders



Model of the Province of Zuid-Holland



## Case study: Province of Zuid-Holland

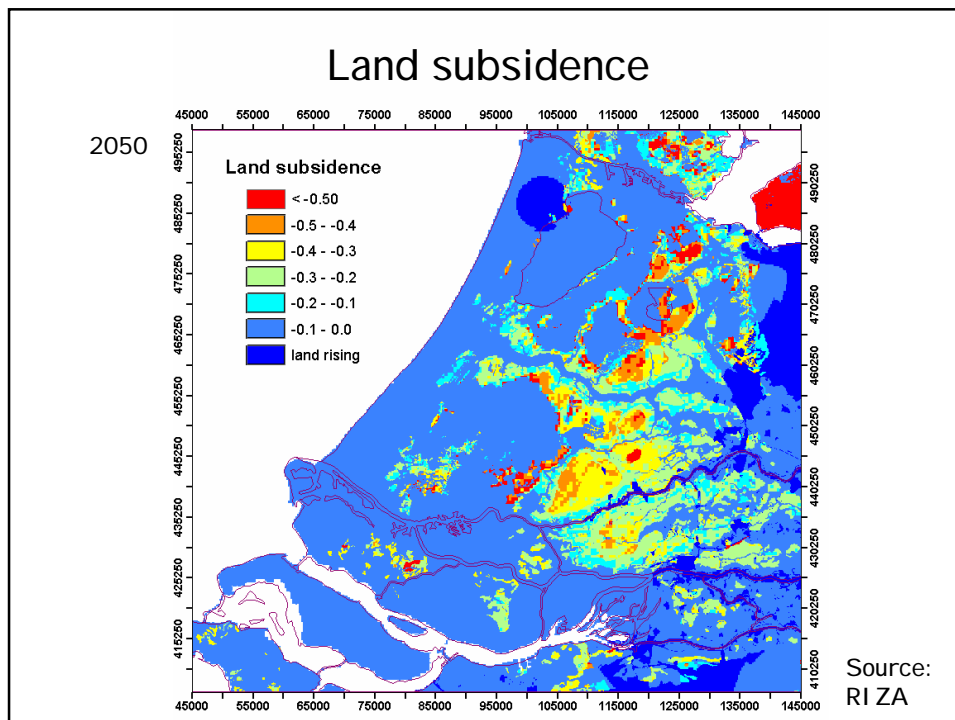
European water framework directive

*“in 2015, state of all groundwaters and surface waters must be good“*

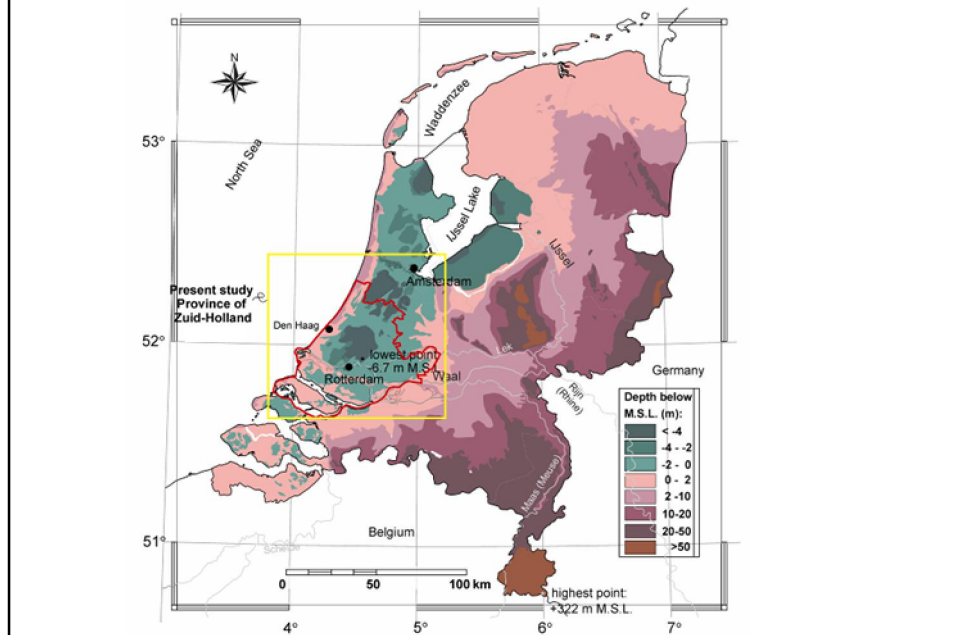
Identification of all fresh groundwater bodies in the province

How fast is the salinisation process?

More seepage, more salt load?



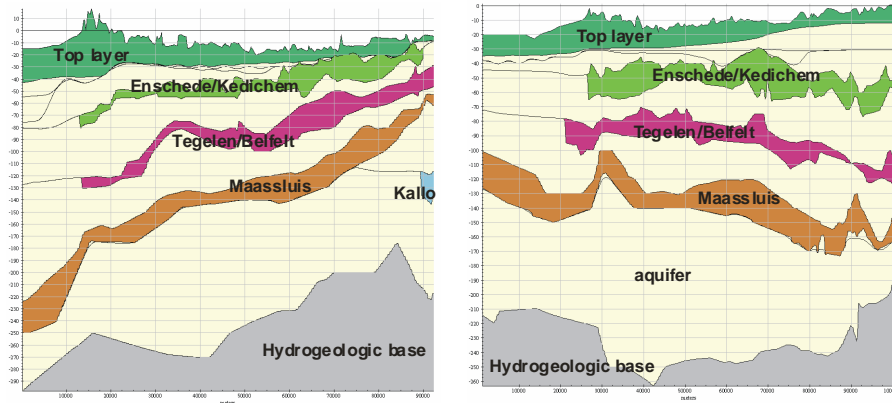
## Location of the Province of Zuid-Holland



## Numerical model description

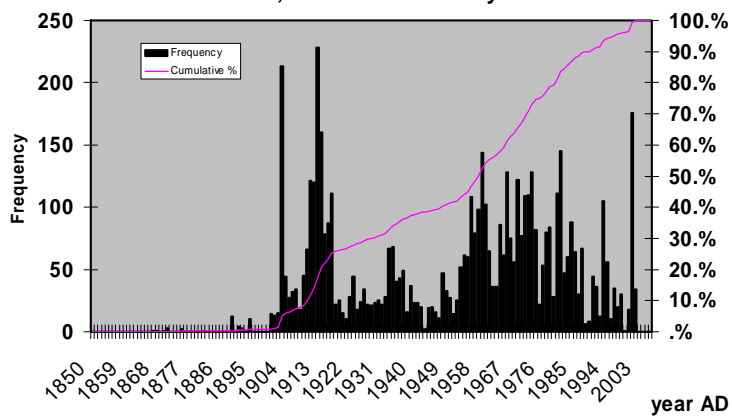
- variable-density groundwater flow
- coupled solute transport
- MOCDENS3D
- area: 100km \* 92.5km \* 300m depth
- 400 \* 370 cells, 40 layers
- ~4 million active cells
- uses most accurate Dutch 3D subsurface schematization available
- 9 aquifers and aquitards
- uses 5772 chloride concentration measurements

## Position and name of aquitards



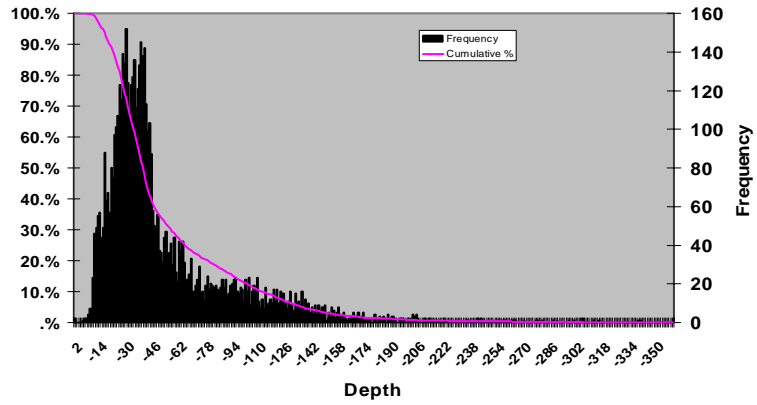
## 3D interpolation of chloride-concentration

### Chloride concentration measurements in Province Zuid-Holland, used in 3D-density matrix

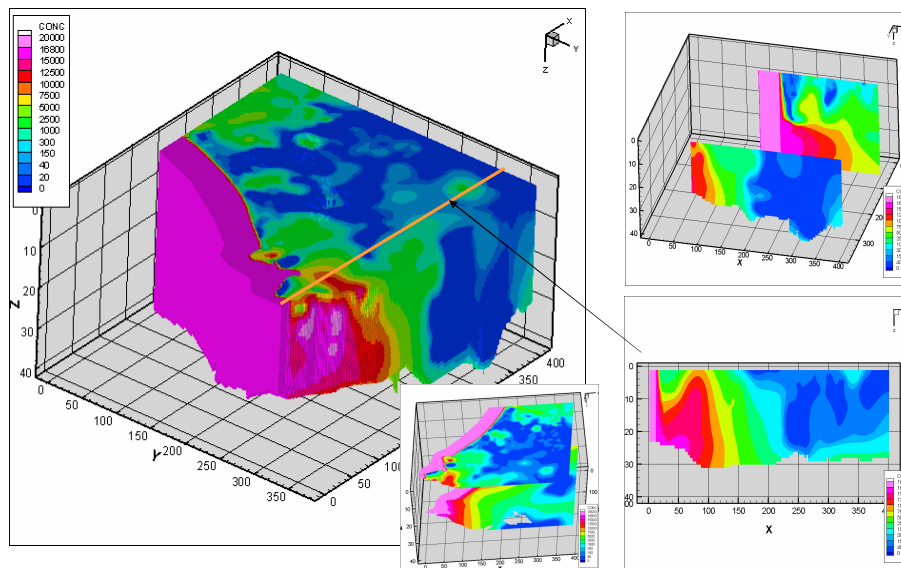


## 3D interpolation of chloride-concentration

Histogram: depth Chloride measurements



## Initial chloride distribution



## Present freshwater volume

27 billion m<sup>3</sup>

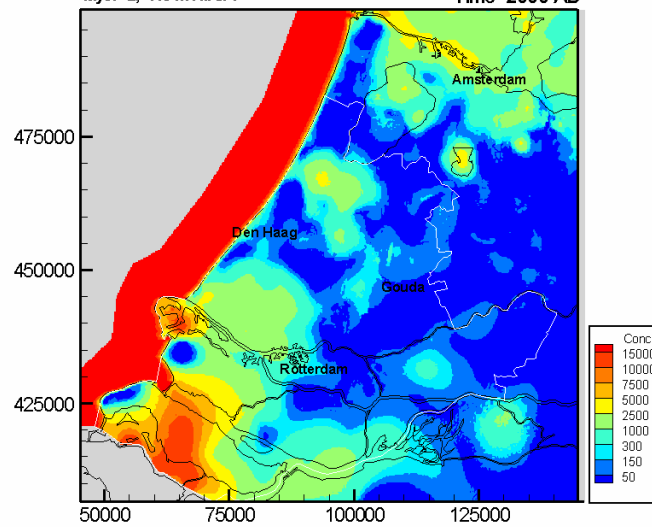
36% fresh, 14% brackish, 50% saline

## Results: Chloride conc. in 200 yrs

Province of Zuid-Holland, salinisation of the subsoil

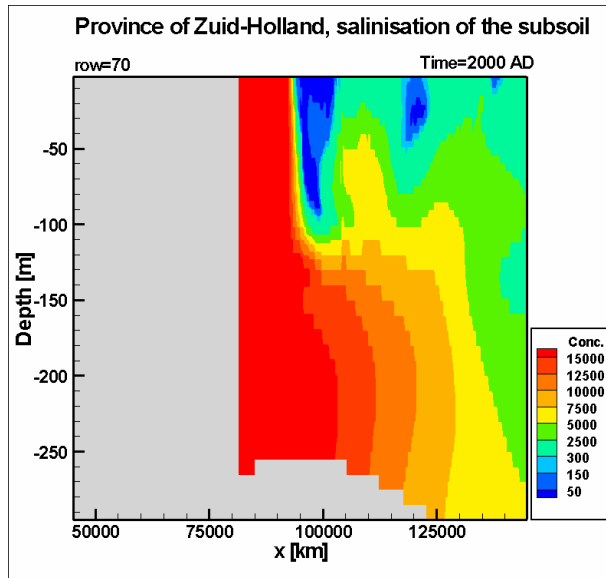
layer=2, -7.5 m N.A.P.

Time=2000 AD

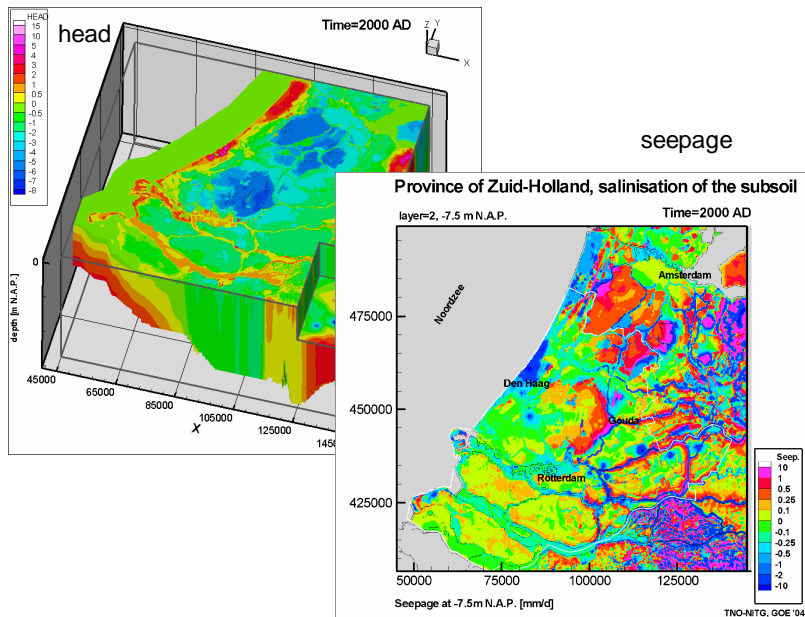


TNO-NITG, GOE '04

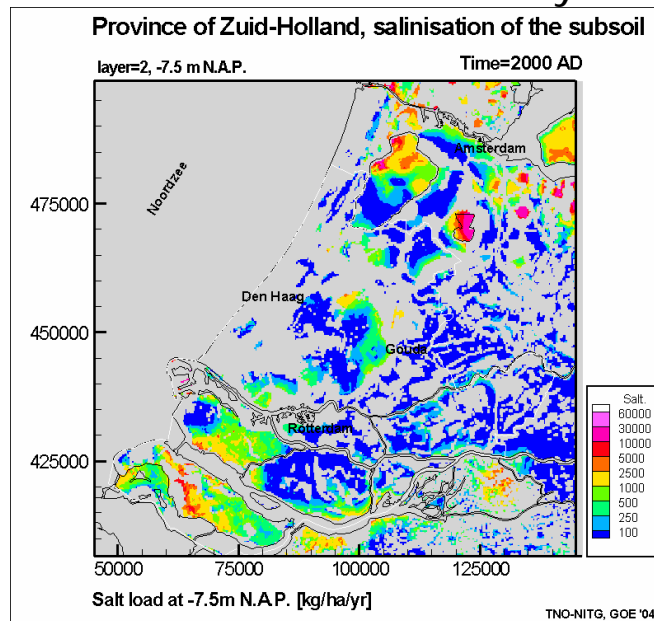
## Results: Chloride conc. in 200 yrs



## Results: freshwater head and seepage at 2000 AD



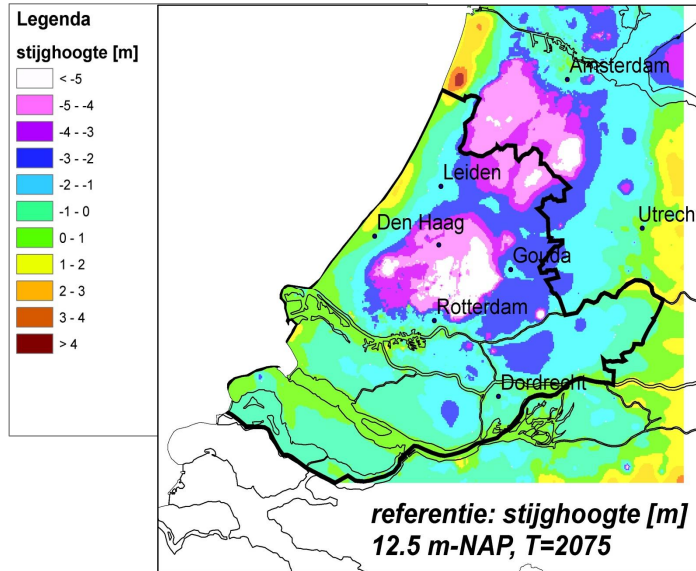
## Results: Salt load in 200 yrs



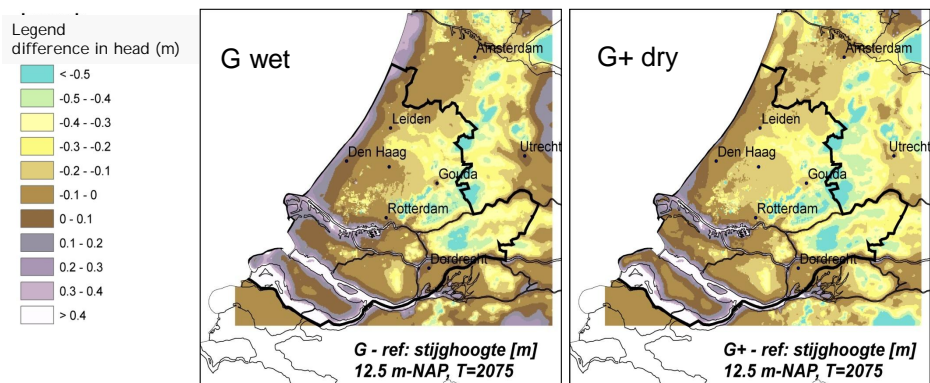
Effect sea level rise, change in natural groundwater recharge and land subsidence on freshwater head in aquifer

Some regional modelling results

### Freshwater head at -12.5 M.S.L.



### Difference in freshwater head on op -12.5 N.A.P.: G scenarios

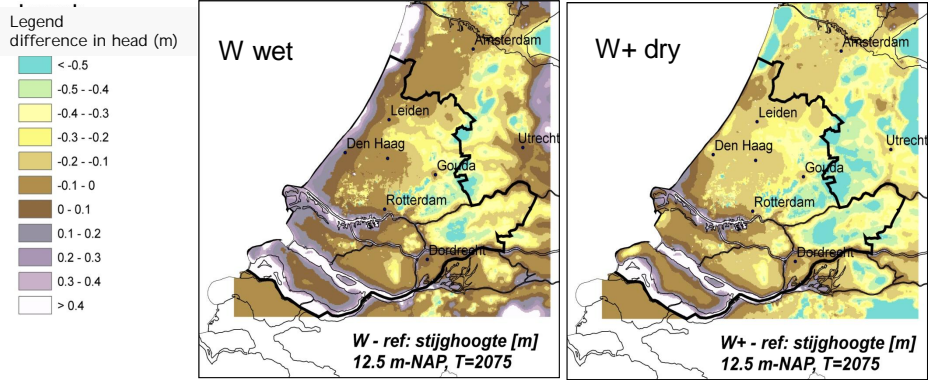


Sea level rise is 60 cm

Including change in natural groundwater recharge

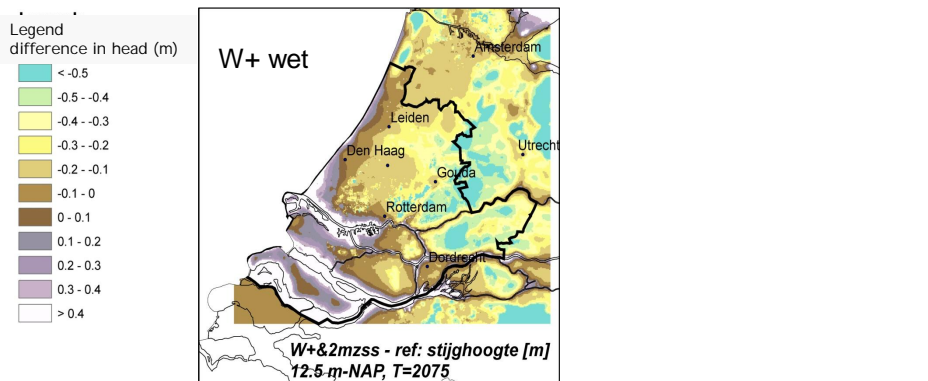


Difference in freshwater head on -12.5 N.A.P.: W scenarios



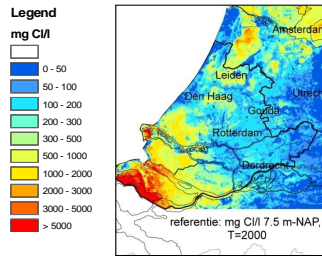
Sea level rise is 85 cm

Difference in freshwater head on -12.5 N.A.P.: W scenarios



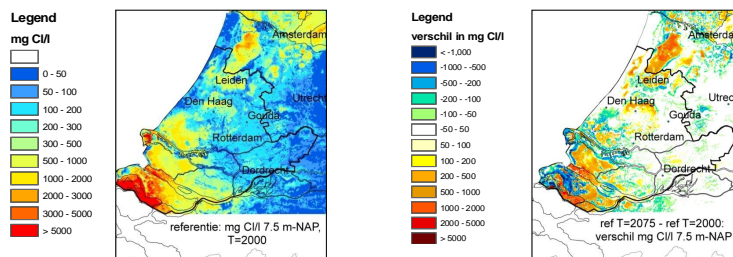
Sea level rise is 200 cm

## Salinisation/freshening Netherlands?: Present situation



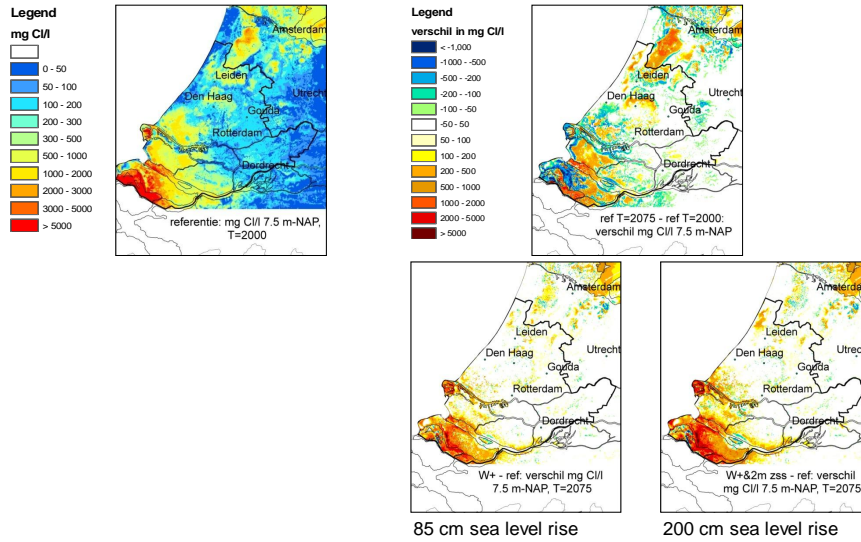
modelstudy

## Salinisation/freshening Netherlands?: Autonomous processes



modelstudy

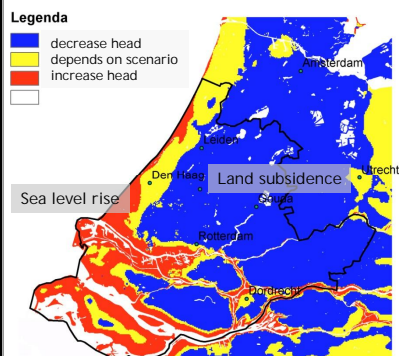
## Salinisation/freshening Netherlands?: climate change



modelstudy

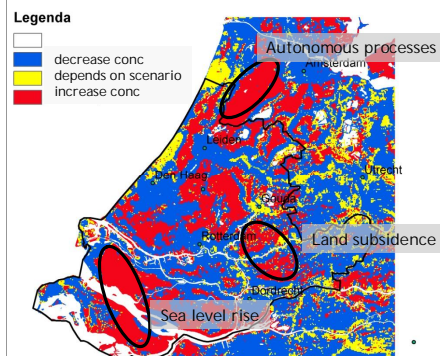
## Effect climate scenarios in 2075 on

### freshwater head



Increase or decrease head for all climate scenarios G, G+, W, W+

### salinisation



Increase or decrease concentration for all climate scenarios G, G+, W, W+

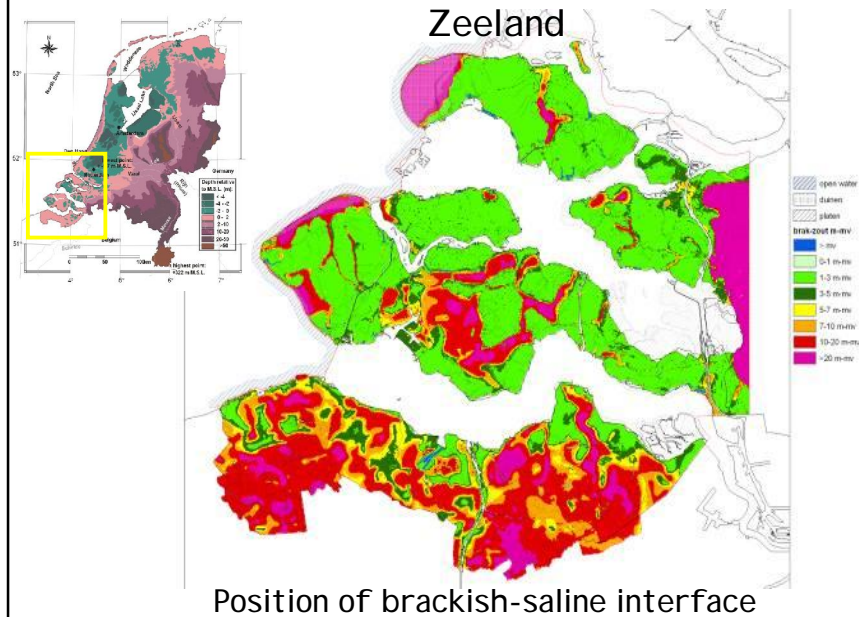
Modelstudie PZH

## Rainwater lenses in an agricultural setting

Shallow dynamic freshwater bodies flowing upon brackish-saline groundwater

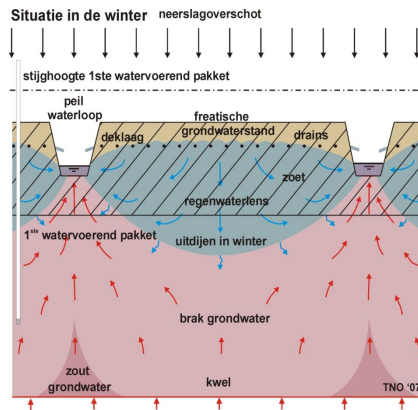
- density dependent
- dynamics: seasonal & long-year

## Salinisation of the phreatic groundwater in Zeeland

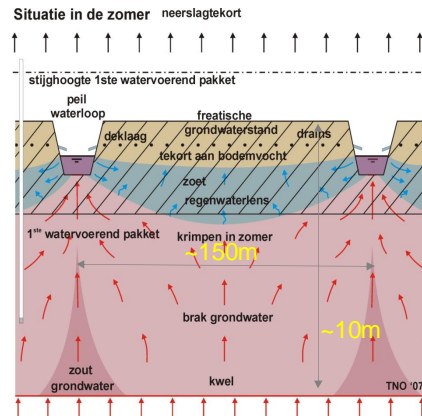


# Salinisation of the phreatic groundwater in Zeeland

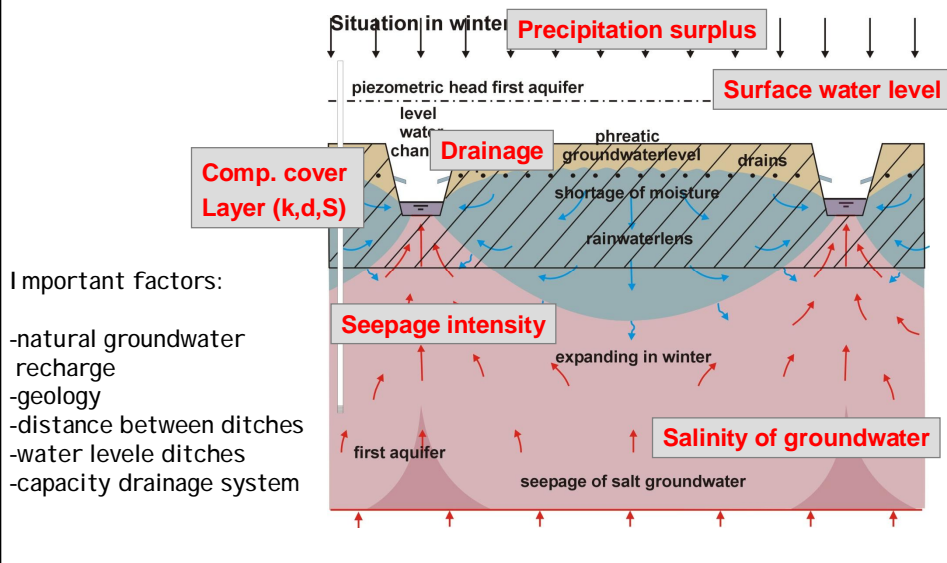
Dynamic rainwater lenses floating on saline groundwater



thickness rainwater lens varies due to the dynamics in seasonal and long-year natural groundwater recharge

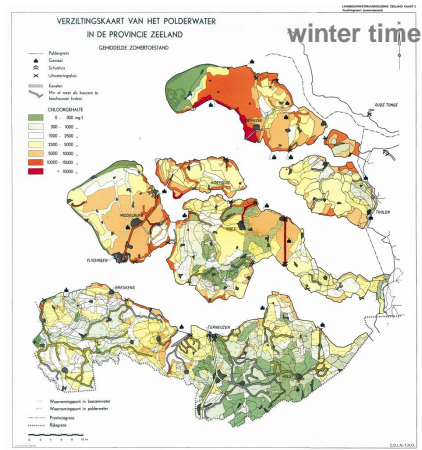
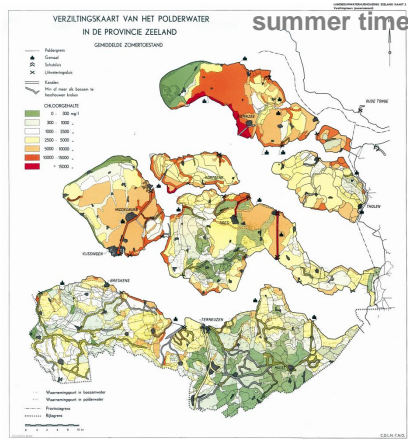


# Factors controlling fresh-salt interface

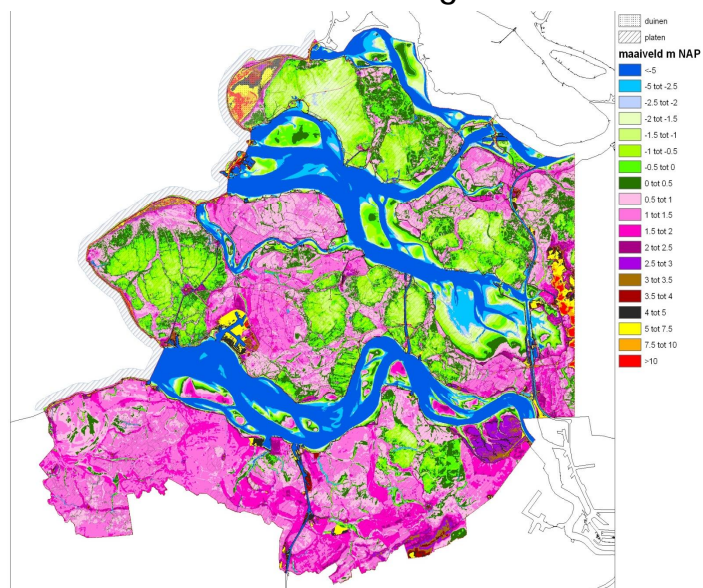


- Important factors:
- natural groundwater recharge
  - geology
  - distance between ditches
  - water level ditches
  - capacity drainage system

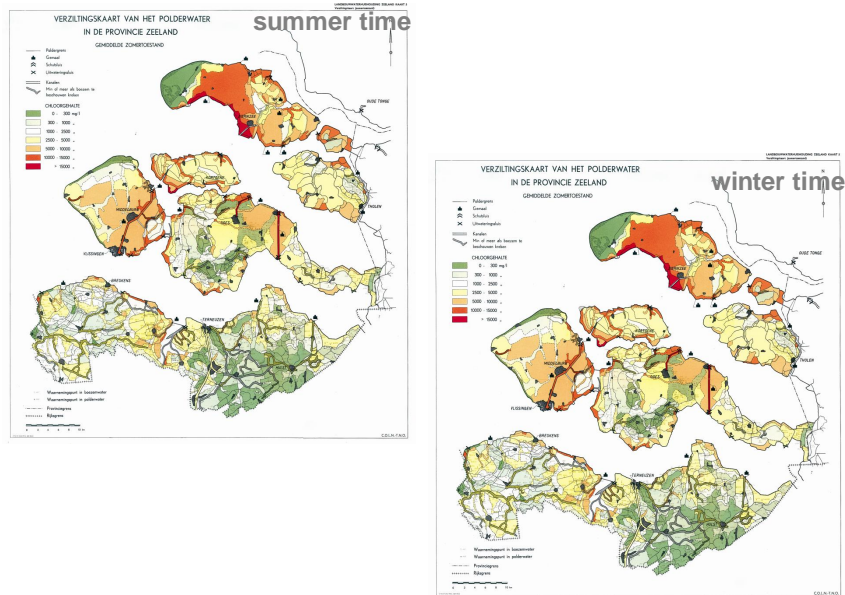
# Salinisation surface water



# Position of the ground surface



## Salinisation surface water



## Problem definition dynamic freshwater lenses



Salt in the agricultural plots originates from:

- surface water system (irrigation water)
- groundwater system (salt load to the root zone)

The salinisation will increase due to:

- sea level rise
- climate change
- water level management



## How to tackle the problem?

### Field measurements at parcels

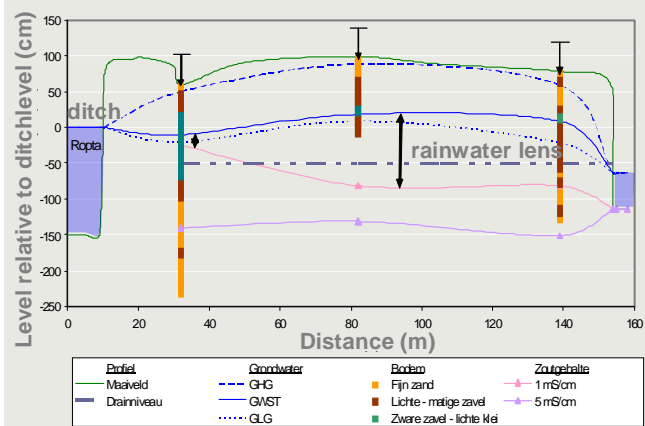
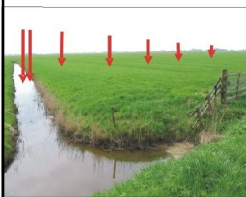
- fresh-brackish-salt interface at local scale using T-EC-probe and later CVES and ERT
- groundwater level and quality
- surface water level and quality

### Modelling

- density dependent groundwater flow
- two different scales:
  - regional scale: transect perpendicular at coast
  - local scale: parcel between two ditches

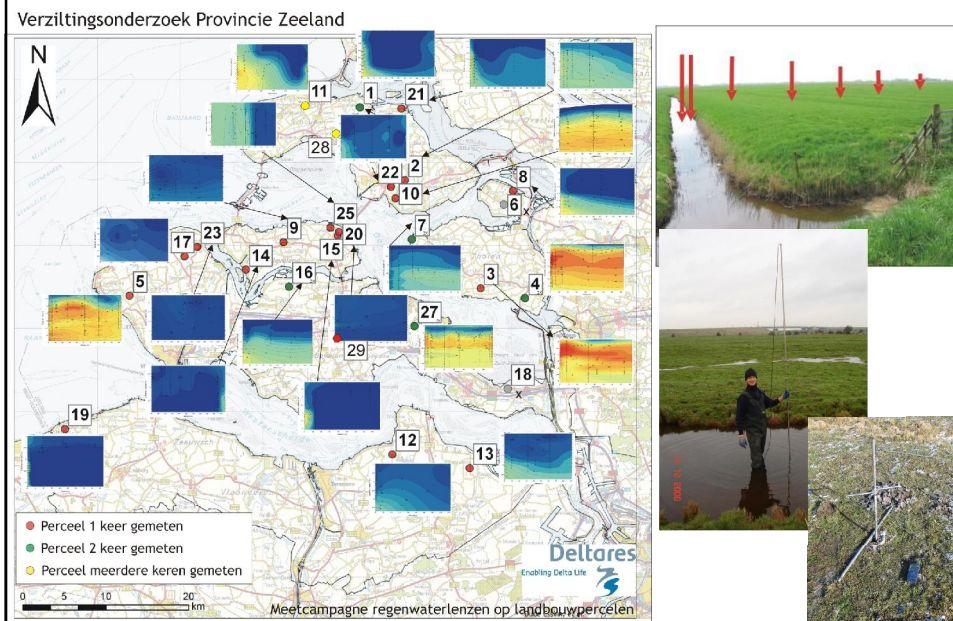


## Use field measurements to understand the process

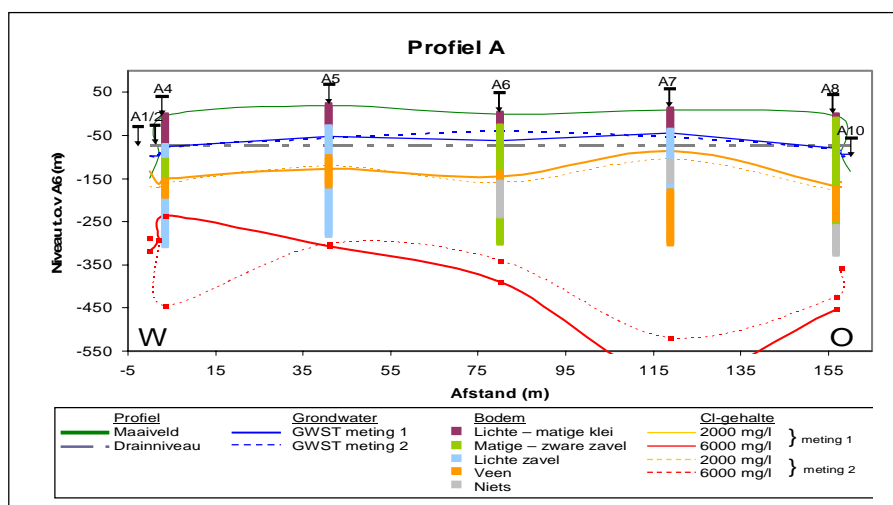




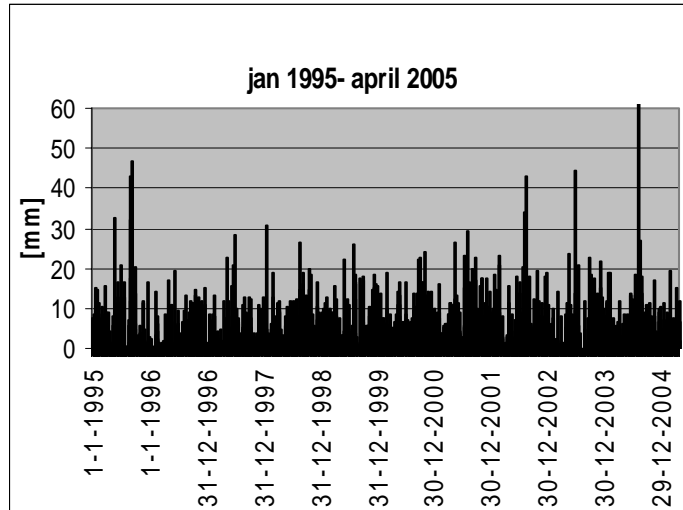
# TEC-probe Monitoring campaign 2005-2009



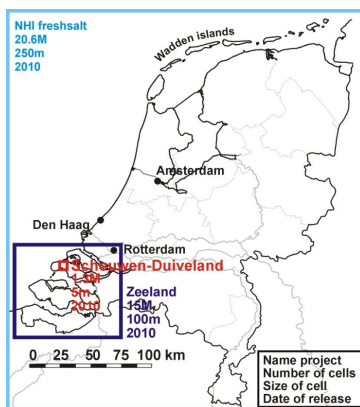
## Measuring and monitoring thickness freshwater lens with a T-EC probe

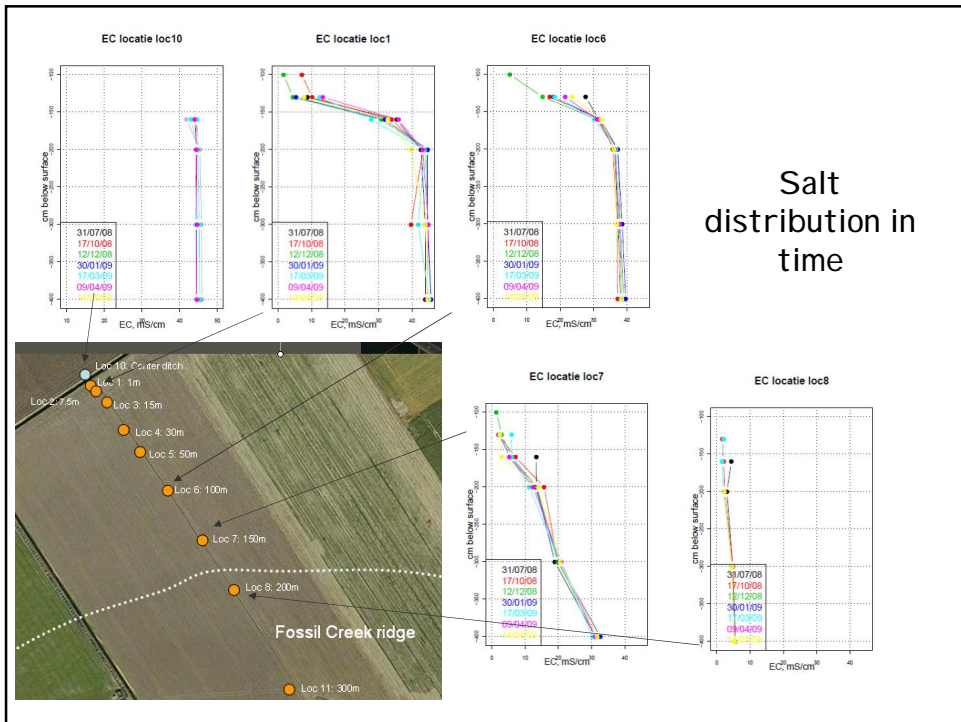


## Real recharge data used

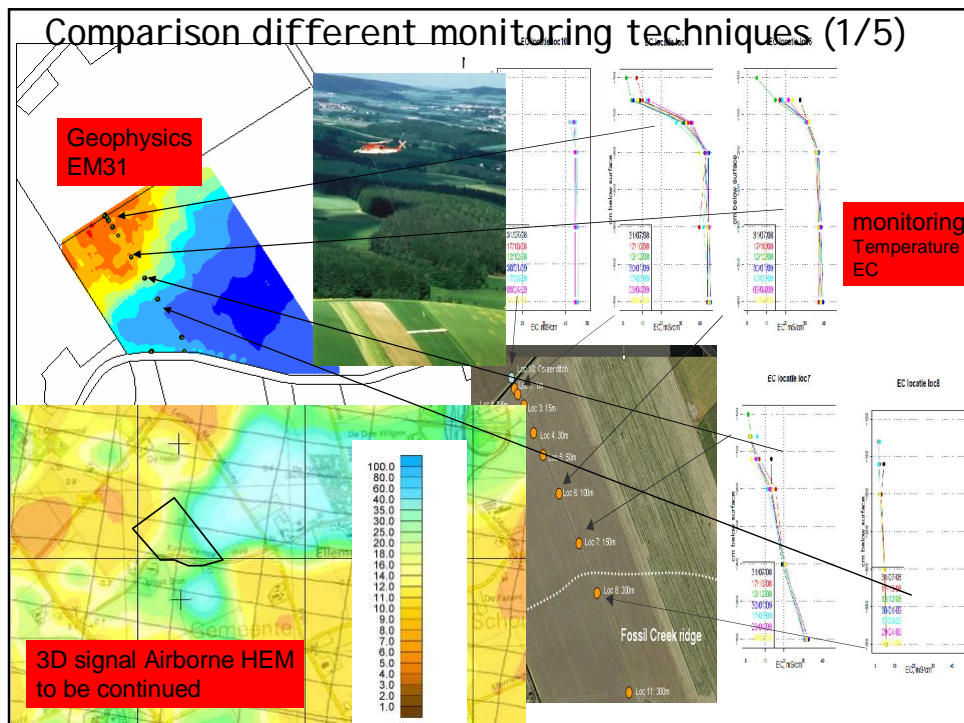


## Description local area





- TEC
- sampling
- EM31
- CVES
- HEM
- ECPT
- Numerical models (2D and 3D)



## Local 3D model of the agricultural plot

### Modelling:

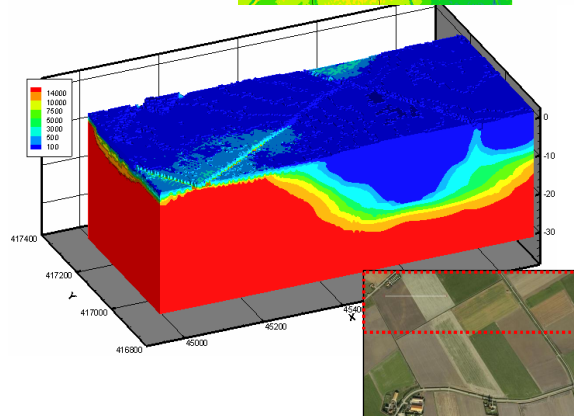
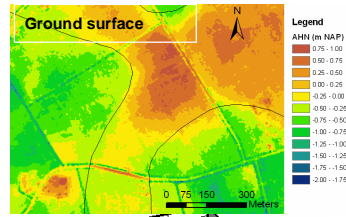
- variable-density
- 3D, non-steady
- groundwater flow & coupled solute transport
- model cell size: 5\*5m<sup>2</sup>

### Code:

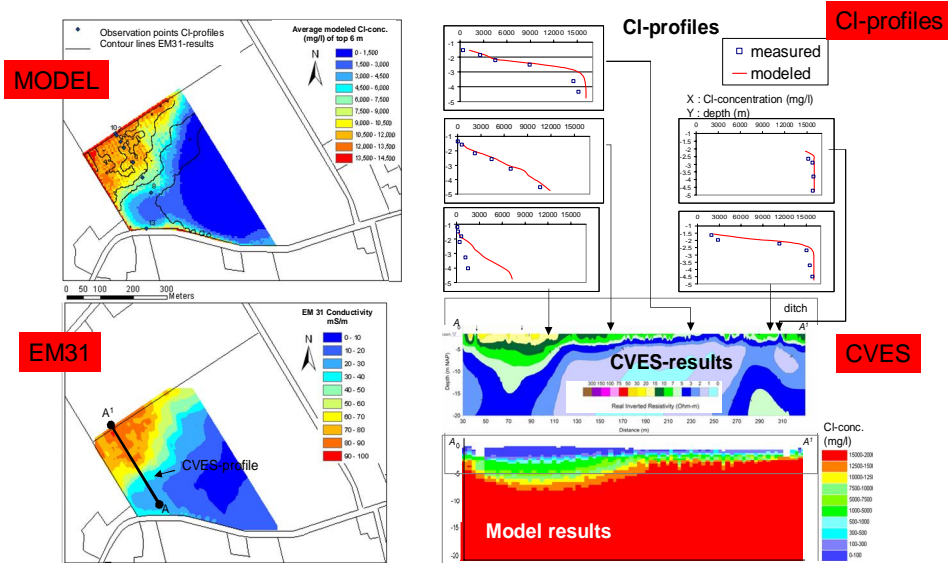
MOCDENS3D

### Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- (adaption measures)



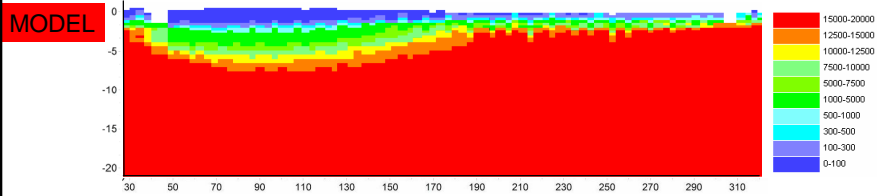
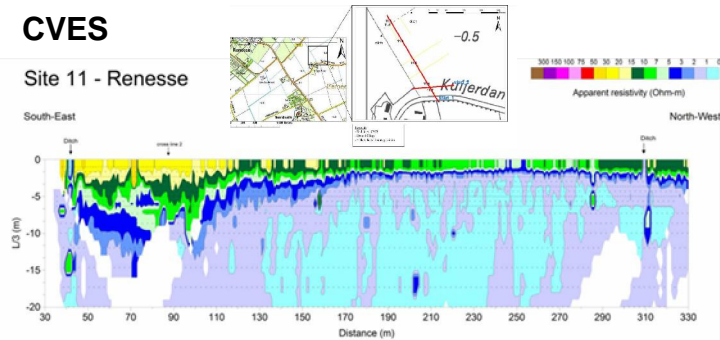
## Comparison model with EM31, CVES, profiles



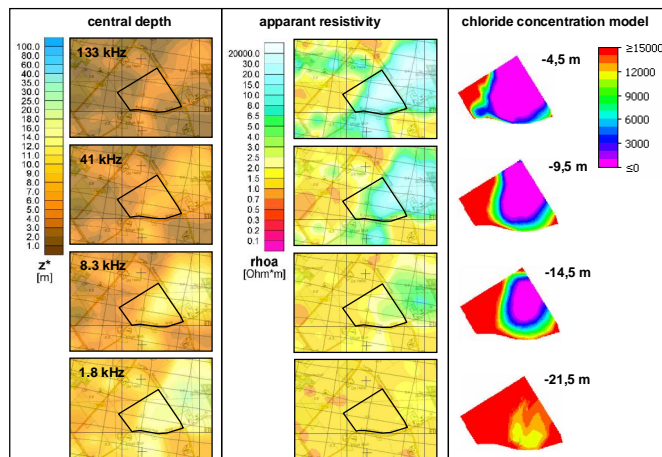
# Comparison 3D model and CVES

## CVES

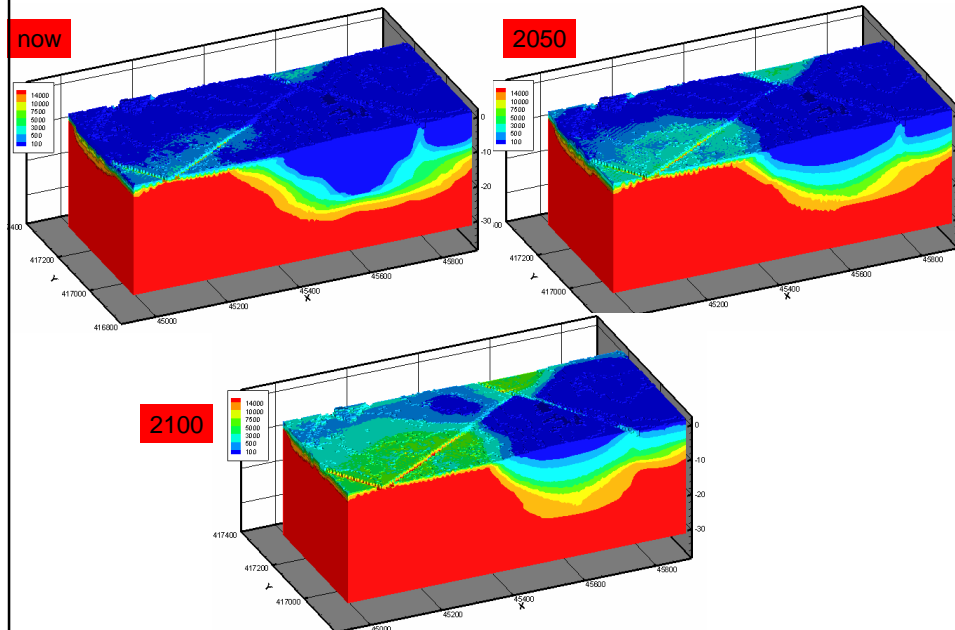
Site 11 - Renesse



# HEM data



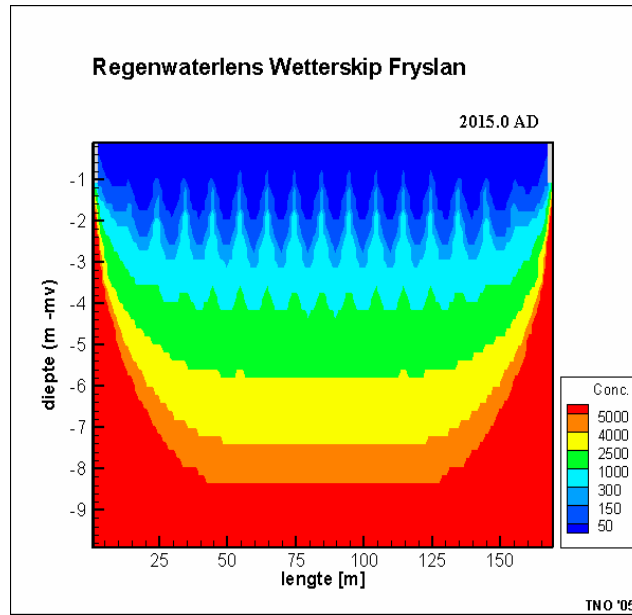
## Climate change scenario (dry): model result



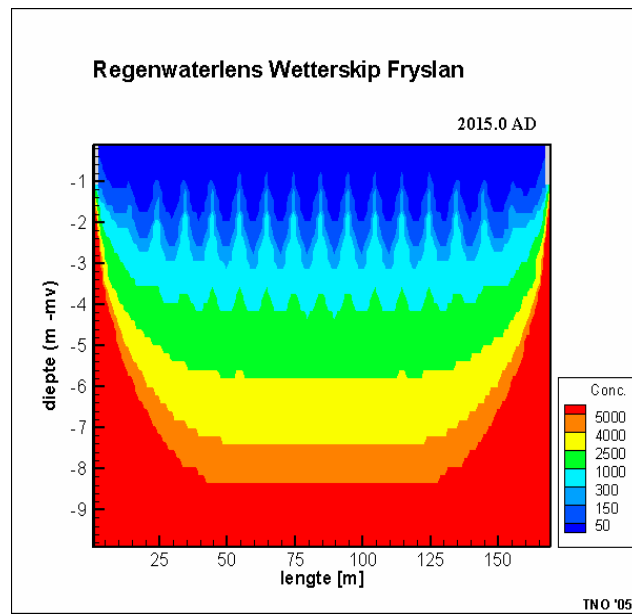
## To be continued...

- Implementing more realisations of 3D geology and initial 3D fresh-saline
  - Analyse the differences
- Running climate change scenarios (on national and regional level)
  - Effect on surface water (salt load)
  - Effect on root zone (rainwater lenses)
  - Effect on freshwater volumes (drinking water)
- Compare model results of different scales and give recommendations

## Model the dynamics of fresh-brackish-salt interface

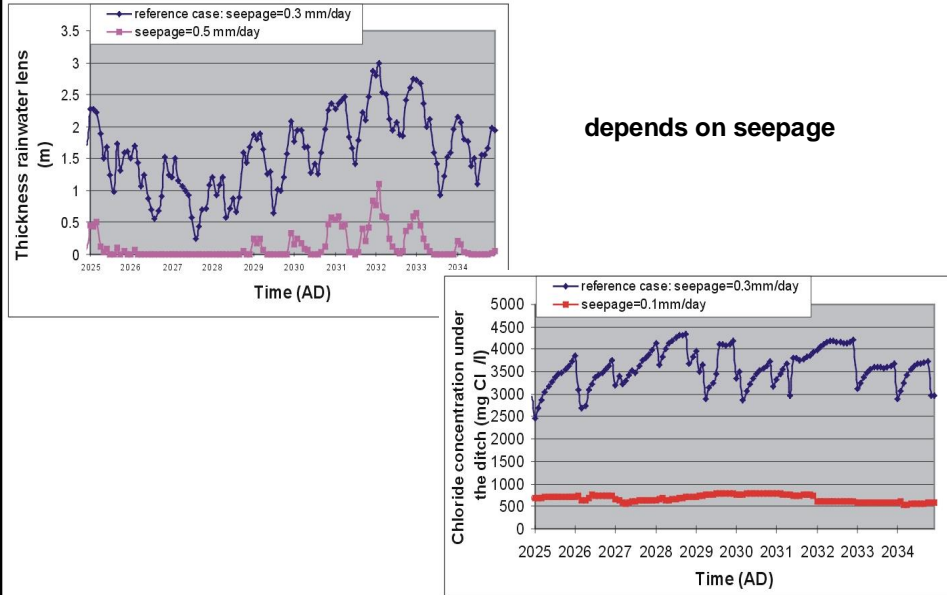


## Model the dynamics of fresh-brackish-salt interface





## Thickness of the lens and salt load to surface water varies



### Conclusions (salinisation Dutch aquifers):

- Salinisation in the Netherlands is a non-stationary process
- Three physical processes threaten the Dutch aquifers:
  - autonomous development
  - land subsidence
  - sea level rise
- Increase in seepage and salt load can be severe during the coming 50/100 years
- Modelling techniques are available to assess possible effects

### Recommendations (salinisation Dutch aquifers):

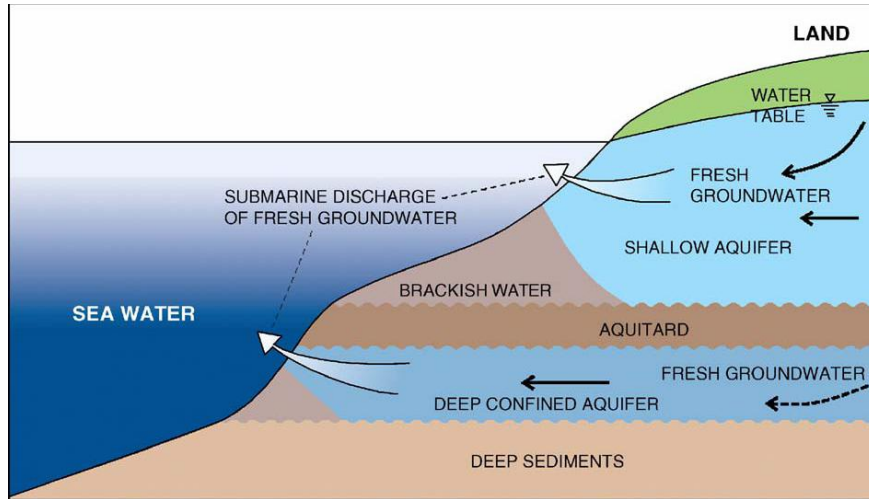
- Number of quality measurements should be increased
- Feasibility study is necessary to implement potential technical measures to compensate salt water intrusion

## International

- Philippines (submarine groundwater discharge)
- Gujarat, India (evaluation anti-swi measures)
- Maldives (effect dec 2004 Tsunami)

# What is Submarine Groundwater Discharge (SGD)?

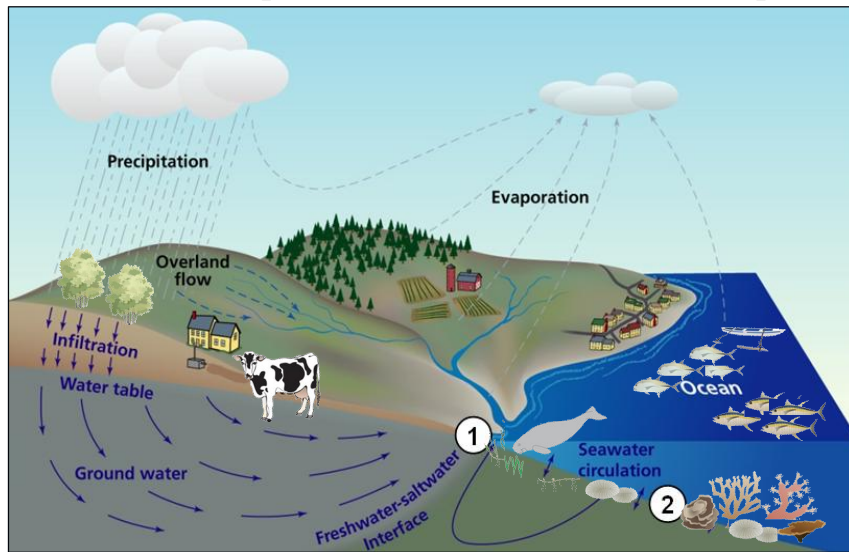
*any flow of water out across the sea floor*



Burnett et al,

# Why study SGD?

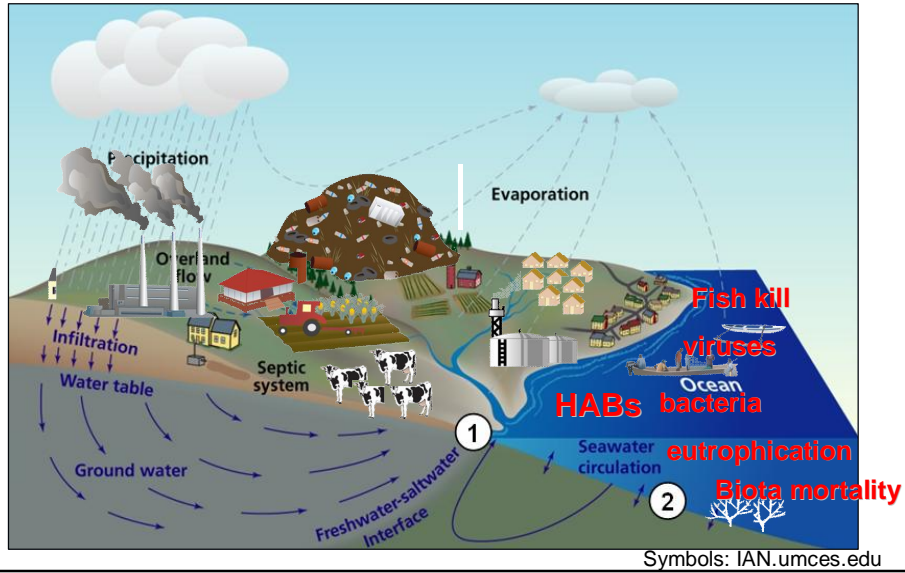
Nutrients are transported from land to sea via SGD pathway



Symbols: IAN.umces.edu

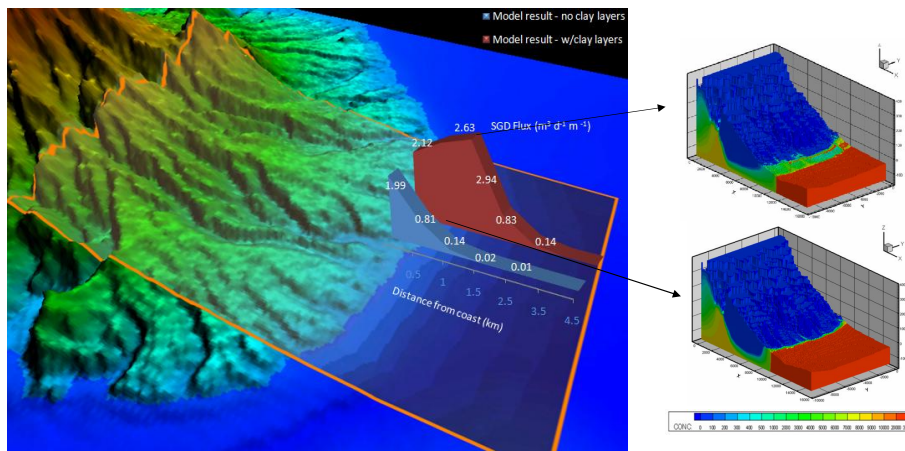
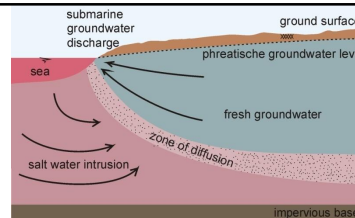
# Why study SGD?

Nutrients are transported from land to sea via SGD pathway



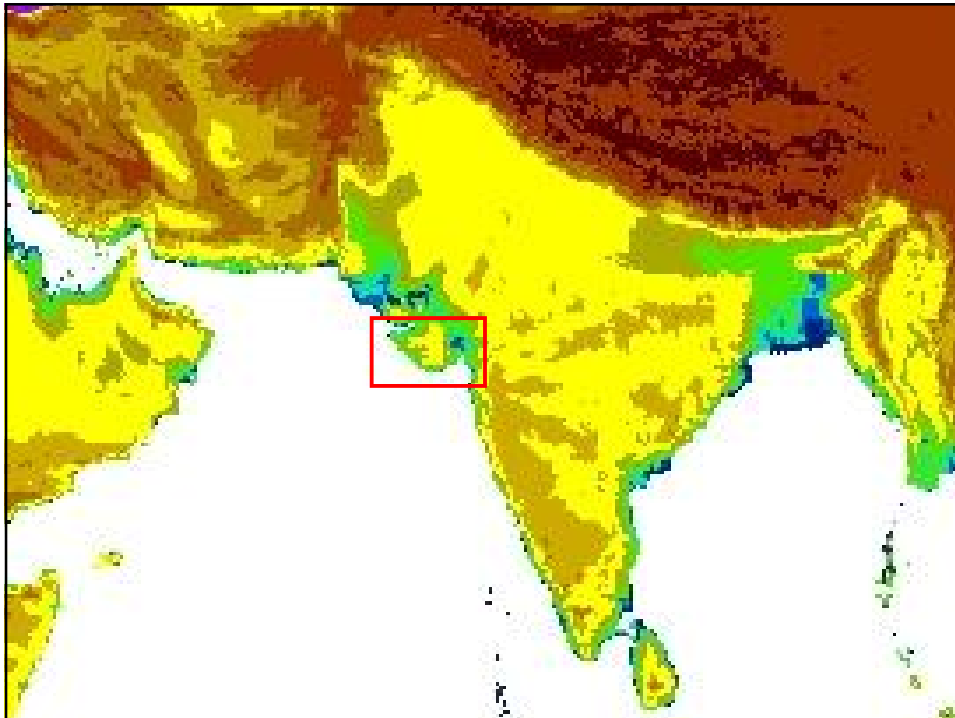
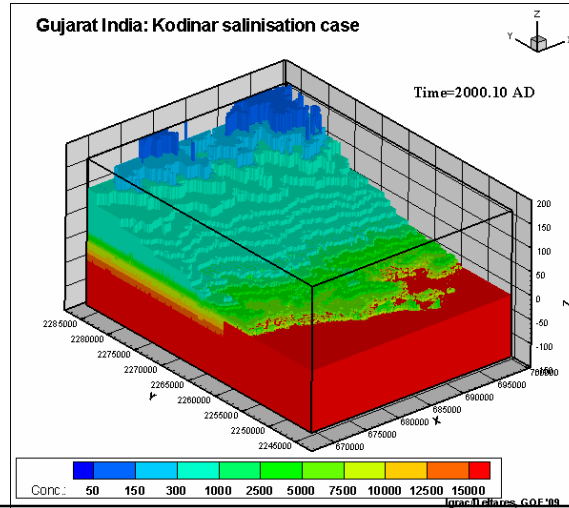
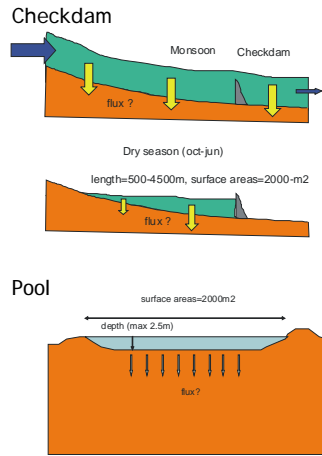
## Philippines

Submarine Groundwater Discharge

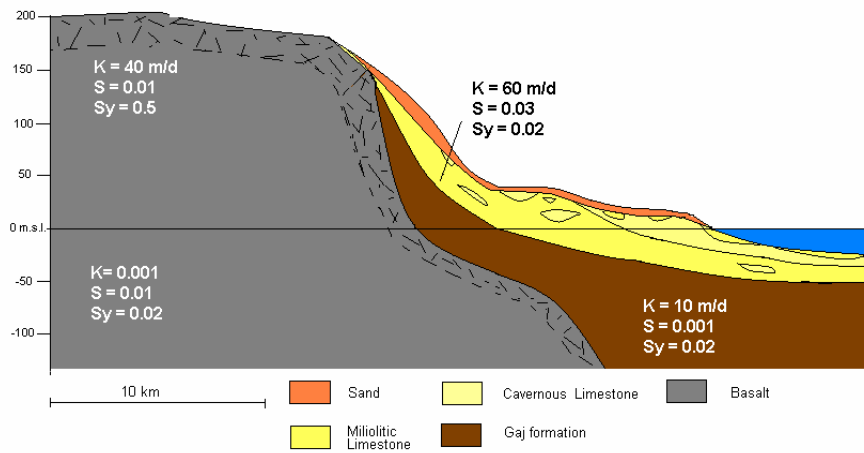


# Gujarat, India

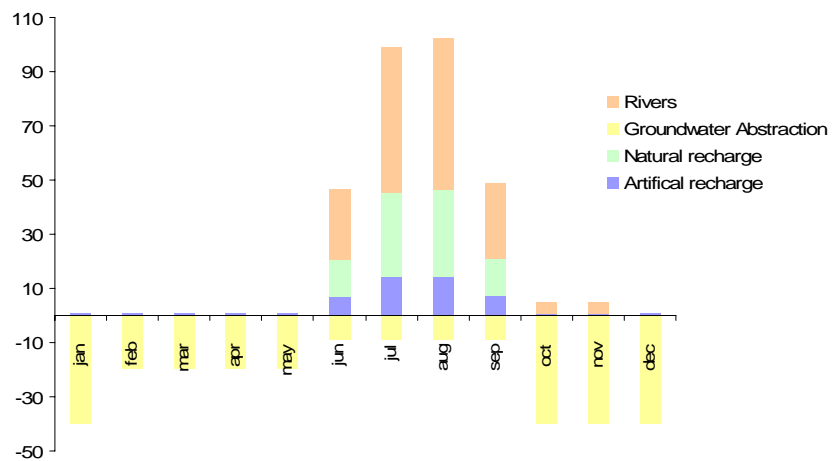
## Learning from the Salinity Ingress Prevention Measures in the Coastal Area of Gujarat



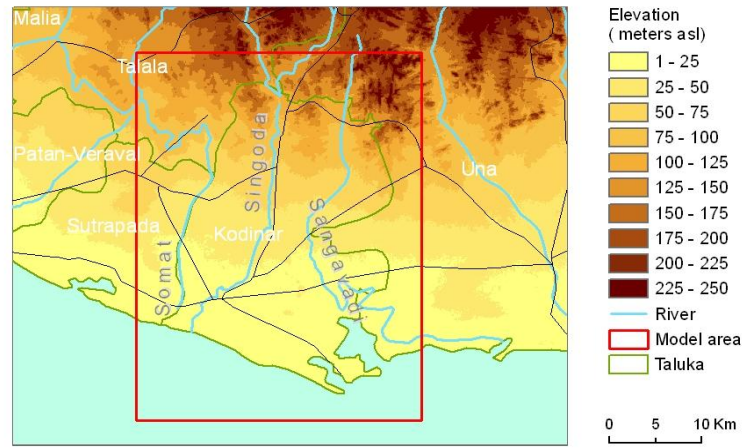
## Hydrogeology, 2D profile



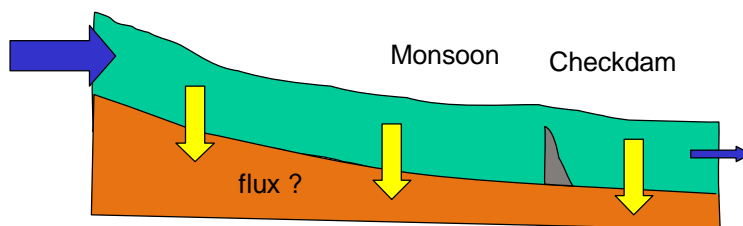
## Waterbalance



## Topography, elevation

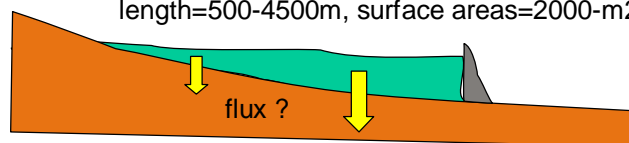


## Concept Checkdam

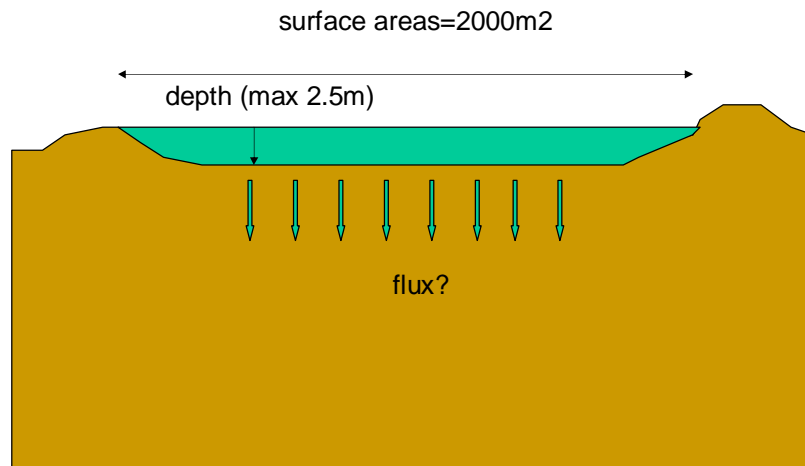


Dry season (oct-jun)

length=500-4500m, surface areas=2000-m<sup>2</sup>

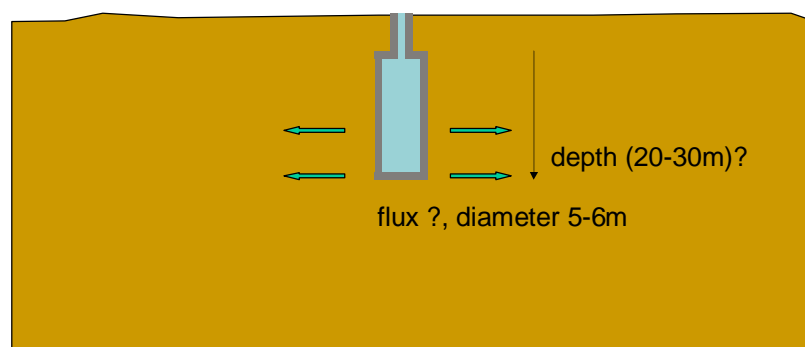


## Concept Pond



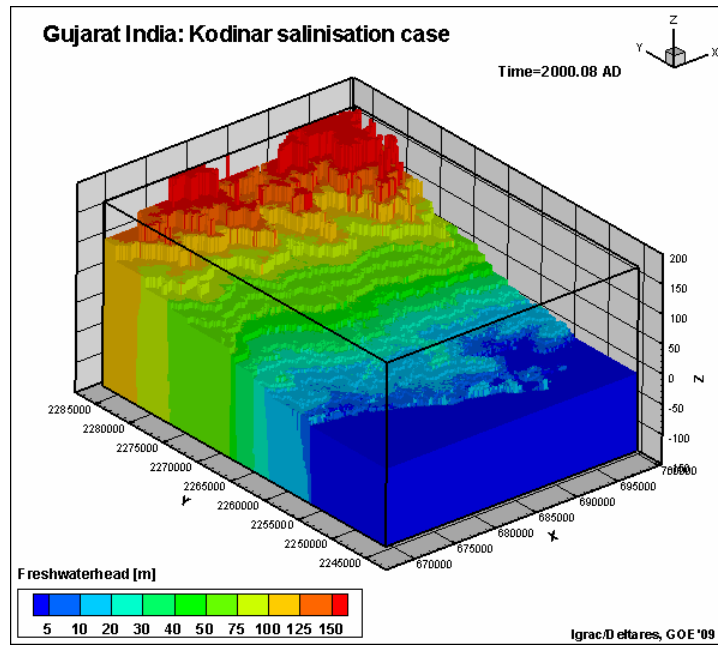
## Concept Percolation tank

number of wells per village: ?

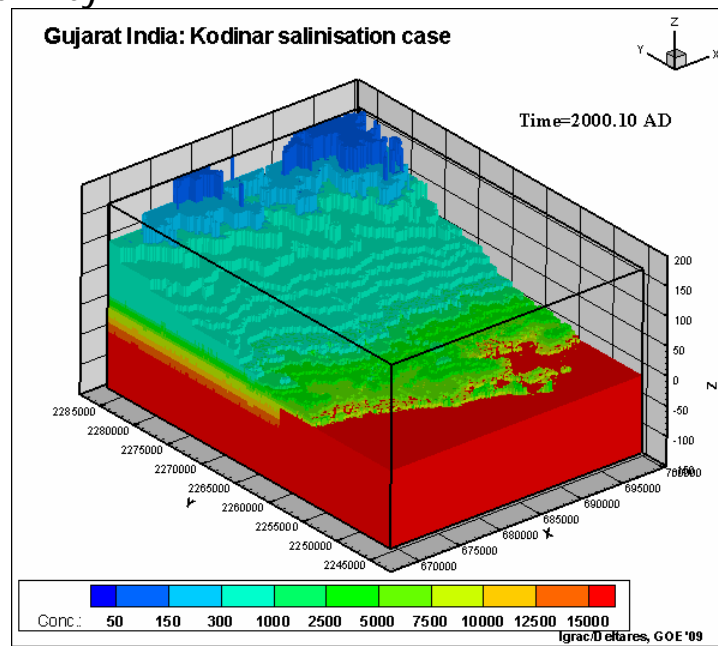




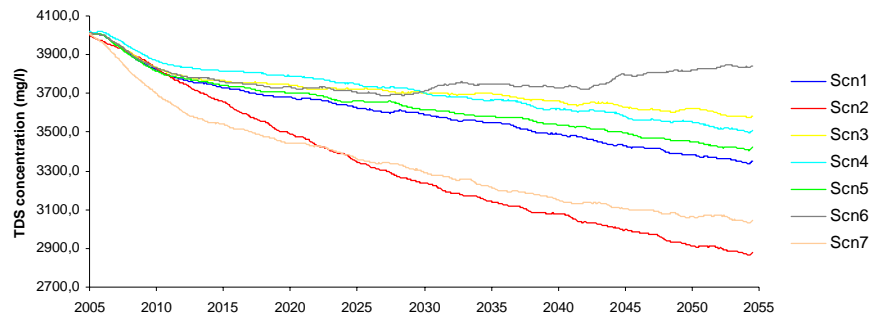
# Freshwater head



# Salinity



## Average TDS concentration



- Scn1. Reference case
- Scn2. Reference case without artificial recharge
- Scn3. Business as usual - increase in population, increase in abstraction
- Scn4. Business to the max (agricultural production and increase abstraction in summer)
- Scn5. Reference case plus industrial zone development (increase of industr. abstraction)
- Scn6. Drought scenario - climate change, sea level rise
- Scn7. Reference case plus water saving measures

## Conclusions (modelling of variable-density flow)

- Don't use the Henry problem to test your variable-density code
- Use enough cells to model the Hydrocoin and Elder problem

### For modelling 3D systems:

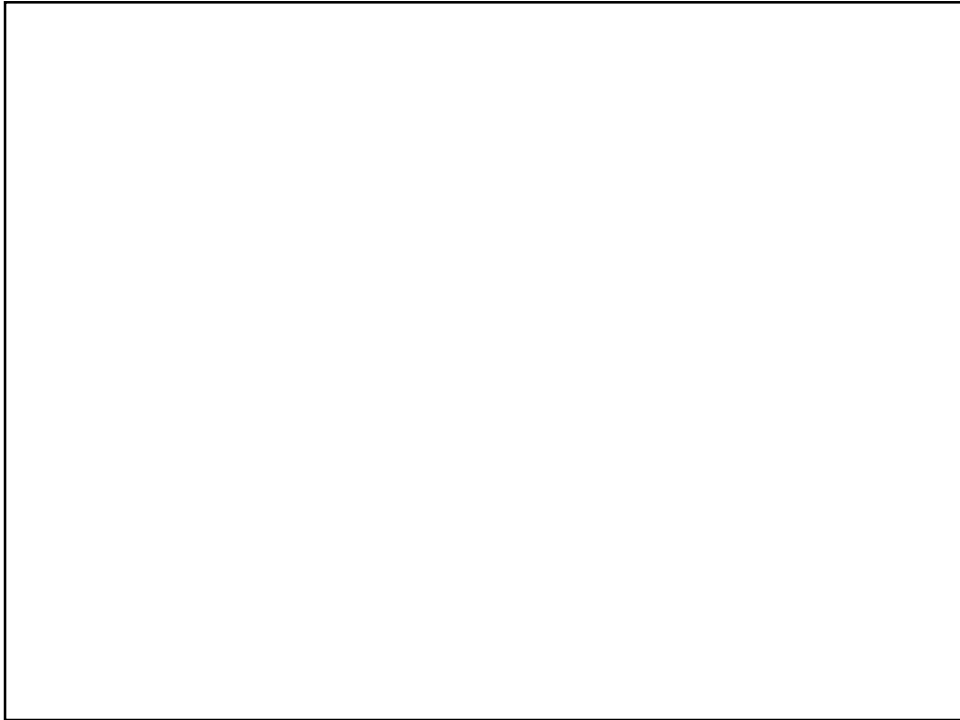
- Remember the Peclet discretisation limitation for cell sizes (unless you're using the method of characteristics!)
- Longitudinal dispersivity should not be too large (e.g. <10m)
- It's important to derive a very accurate density distribution (as that significantly effects the velocity field!)
- Watch out for numerical problems at the outflow face to the sea

## Challenges for the future

- Improve the 3D density matrix, e.g. by more types of measurements
- Implement effect of climate change and sea level rise on coastal aquifers
- Optimisation of (ground)water management in coastal aquifers by using 3D variable-density flow models
- Improve calibration of 3D models by using transient data of solute concentrations
- Incorporate reactive multicomponent solute transport

## Leading in research on groundwater in the coastal zone

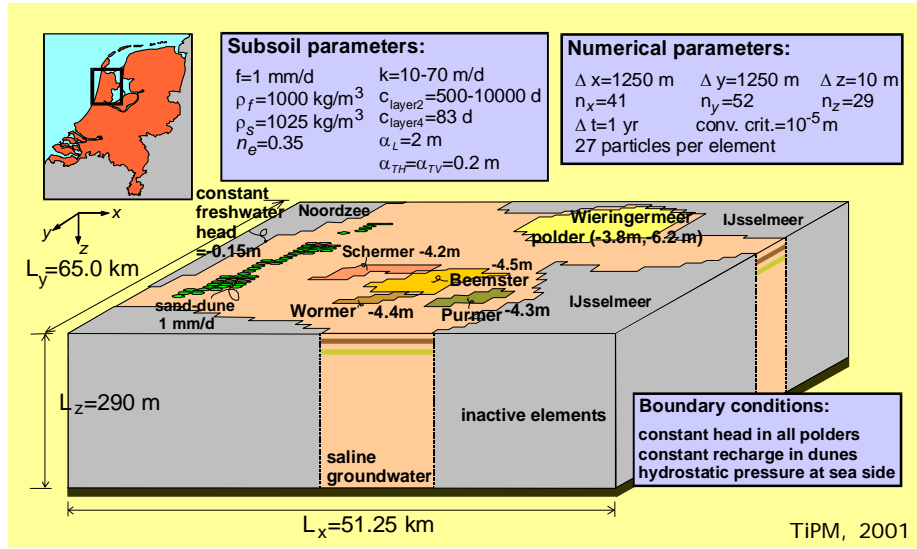
- 15 years experience in variable-density dependent groundwater flow and coupled solute transport in the coastal zone
- Incorporating monitoring campaigns results in numerical modeling tools
- Initiating (inter)national research on new fresh-saline phenomena: salty seepage boils and thin freshwater lenses in saline environments
- Broad knowledge on creating 3D initial chloride distribution, based on geostatistics and geophysical data (analyses, VES, borehole measurements)
- Quantifying effects of climate change and sea level rise on fresh groundwater resources
- Developing adaptive and mitigative measurements to stop salinization of the coastal groundwater system (e.g. fresh keeper, coastal collectors, freshwater storage underground)



Model of the Kop van Noord-Holland,  
The Netherlands

*Oude Essink, G. H. P. 2001. Saltwater intrusion in 3D large-scale aquifers: a Dutch case. Phys. & Chem. of the Earth 26(4): 337-344.*

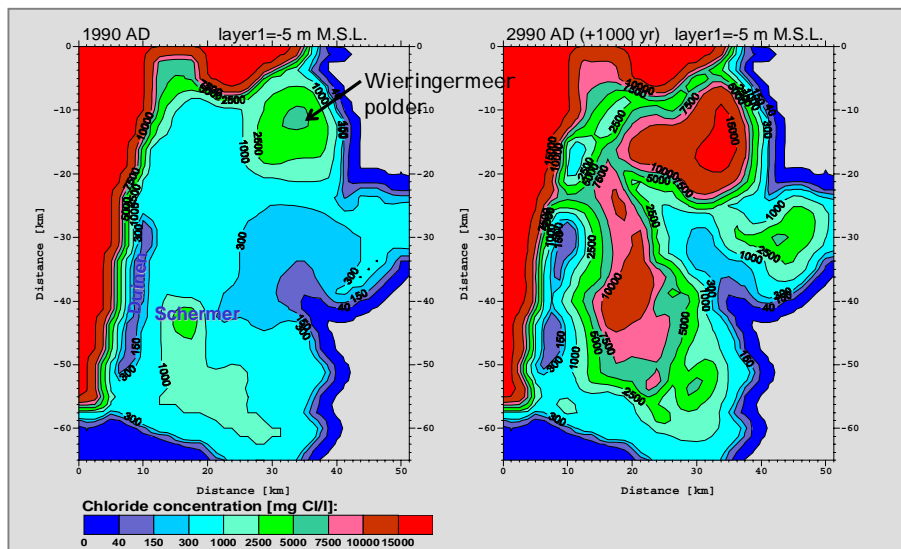
## Characteristics of the Kop van Noord-Holland (I)



## Kop van Noord-Holland (II)

Reference case=autonomous development

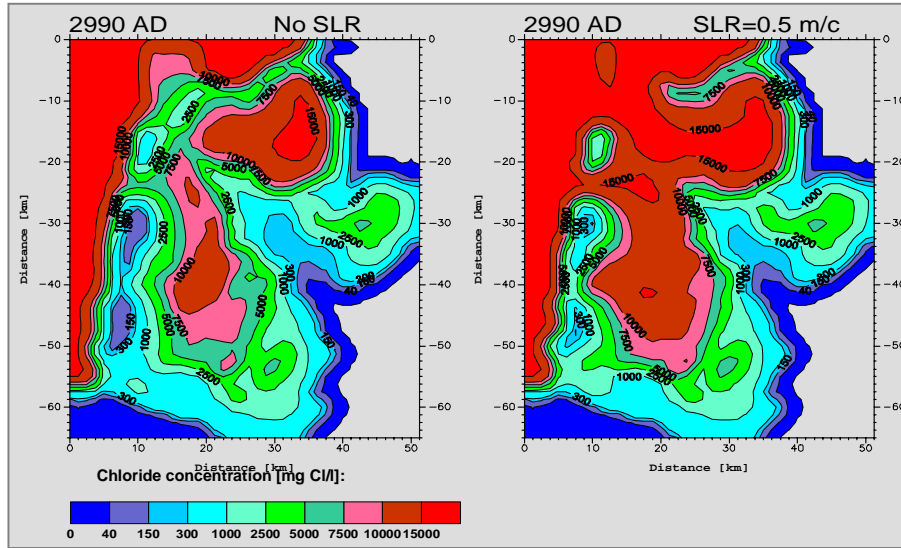
Change in concentration in the top system during 1000 years



### Kop van Noord-Holland (III)

Sea level rise case=0.50 m/century

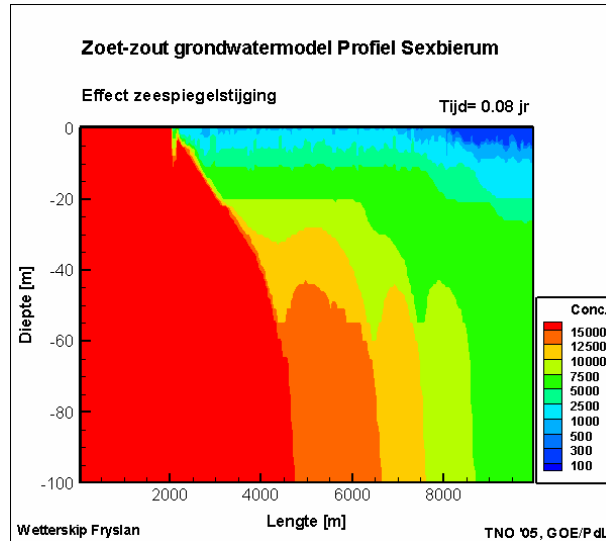
Change in concentration in the top system during 1000 years



Model of the Wetterskip of Fryslan

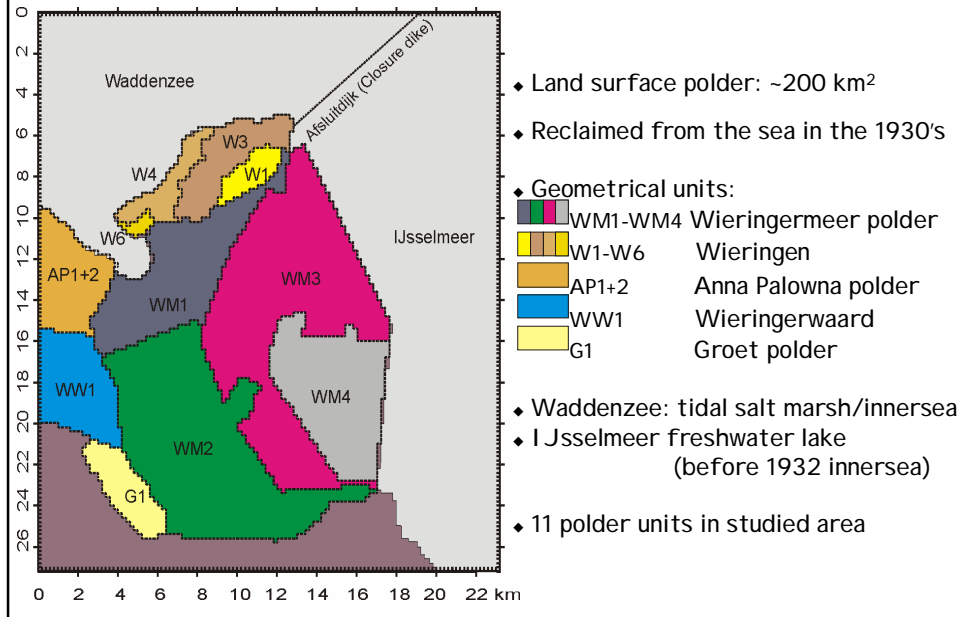
# Wetterskip Fryslan

- Zoutverdeling - Huidige en toekomstige situatie (+30jaar)
- Effect zeespiegelstijging en bodemdaling door zoutwinning

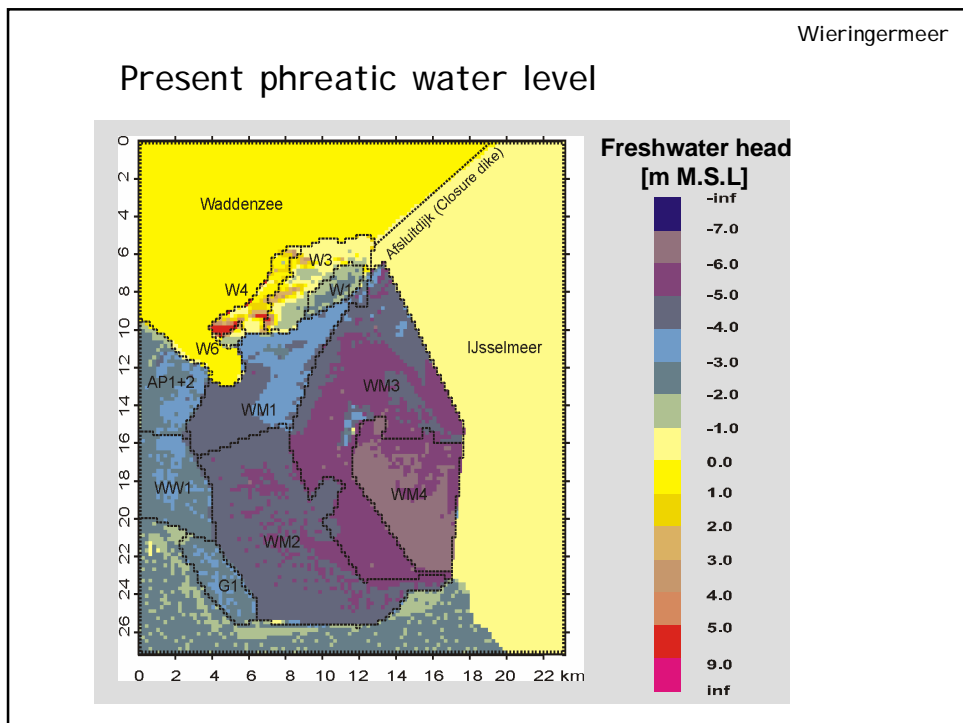


Model of the Wieringermeer polder

### Characteristics of the Wieringermeer polder

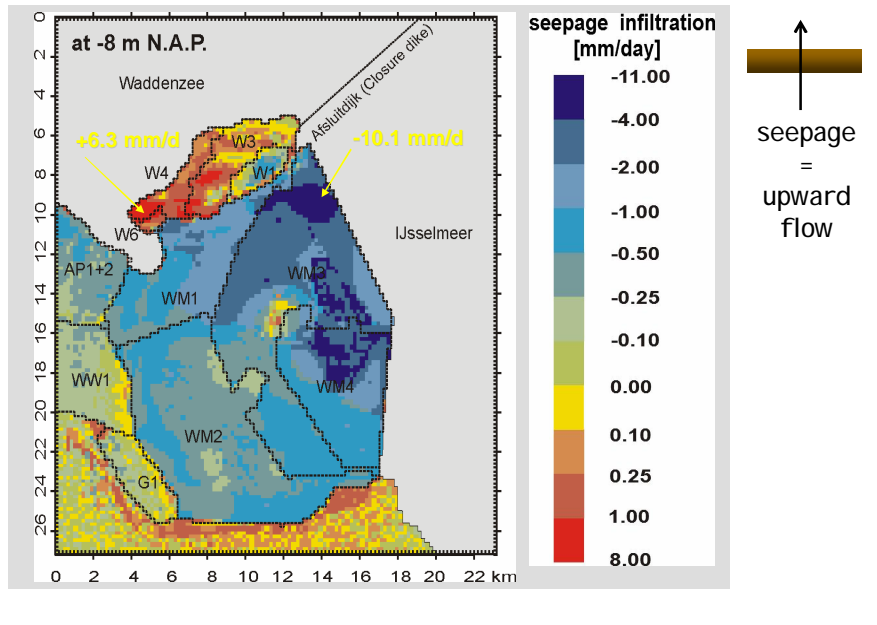


### Present phreatic water level

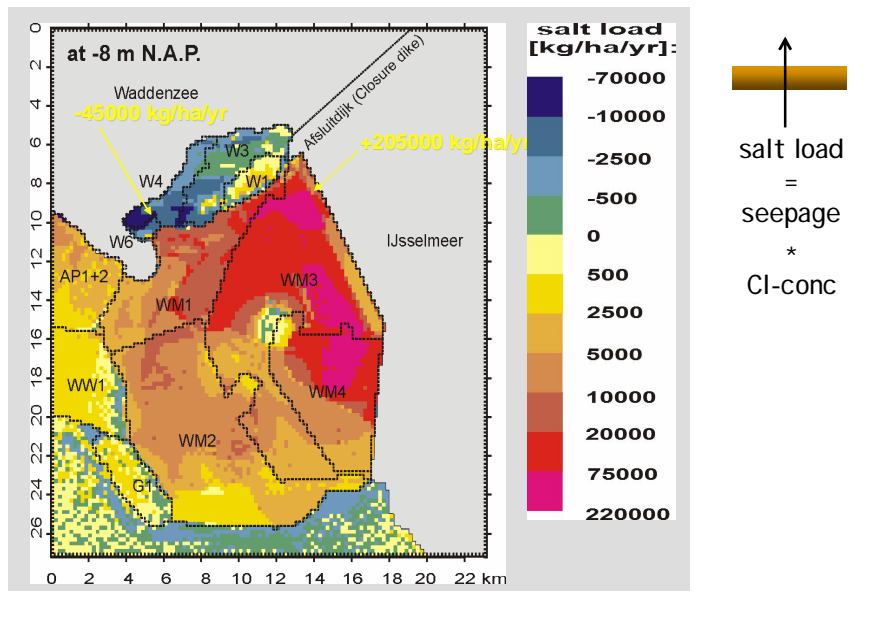




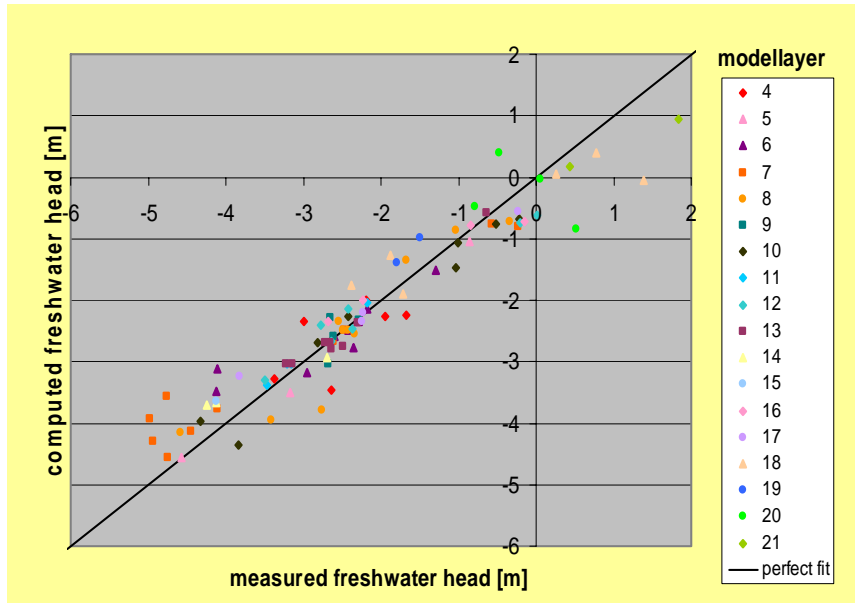
### Calculated present seepage and infiltration



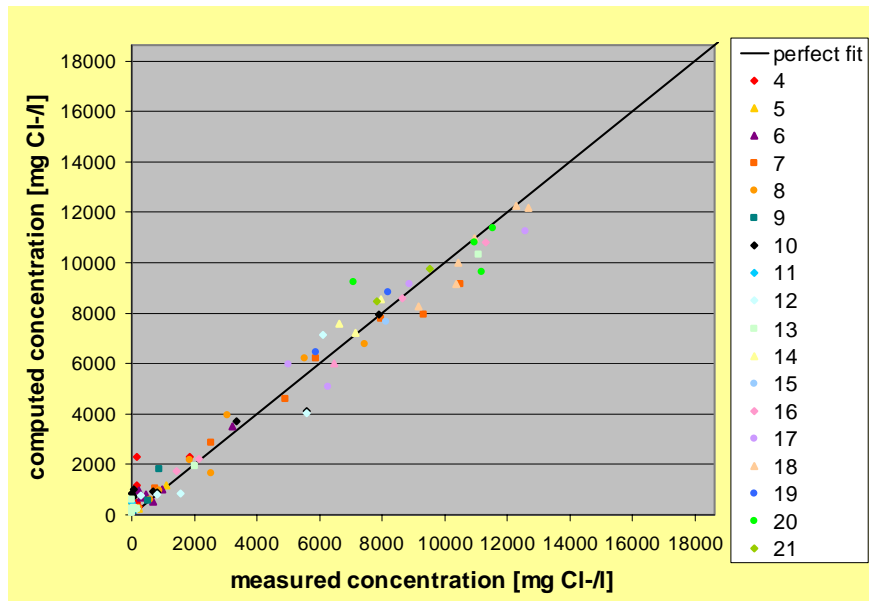
### Calculated present salt load



### Calibration characteristics (I): freshwater head



### Calibration characteristics (II): concentration



## Two future scenarios (during 50 years):

### I Reference case

- present mean sea level
- autonomous development

### II Sea level rise case

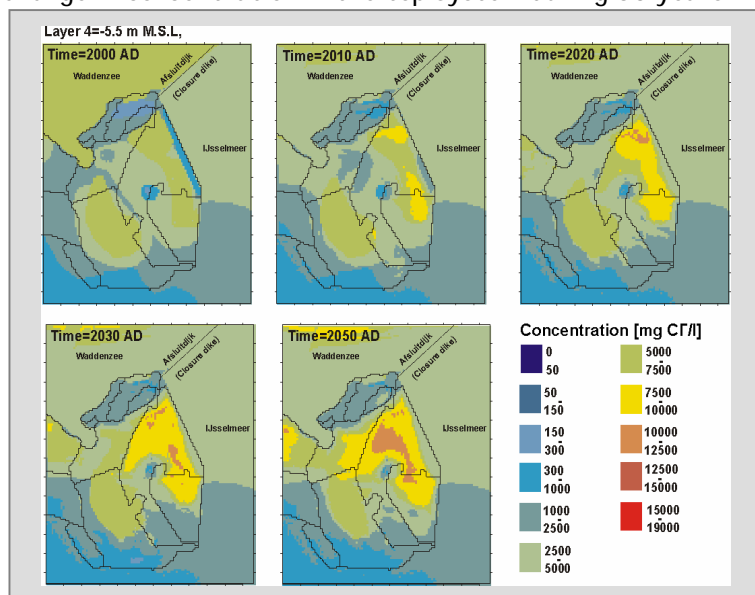
- relative sea level rise of 0.75 m/century

Interest is focused on:

- A. Change in concentration in top layer
- B. Change in seepage in the polder
- C. Change in salt load in the polder

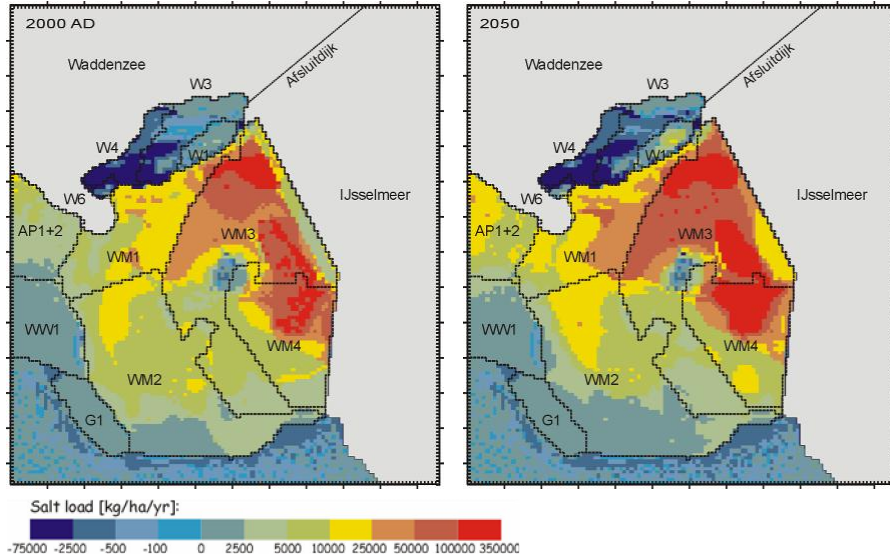
## Wieringermeer: reference case

Change in concentration in the top system during 50 years



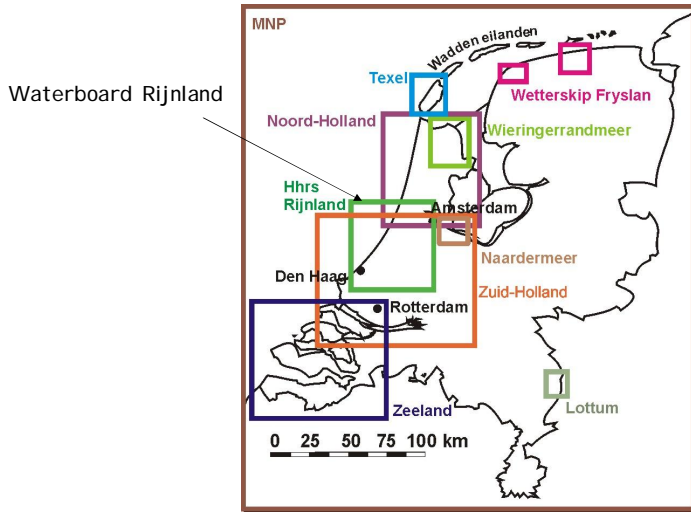
### Wieringermeer: reference case

Change in salt load in the top system during 50 years



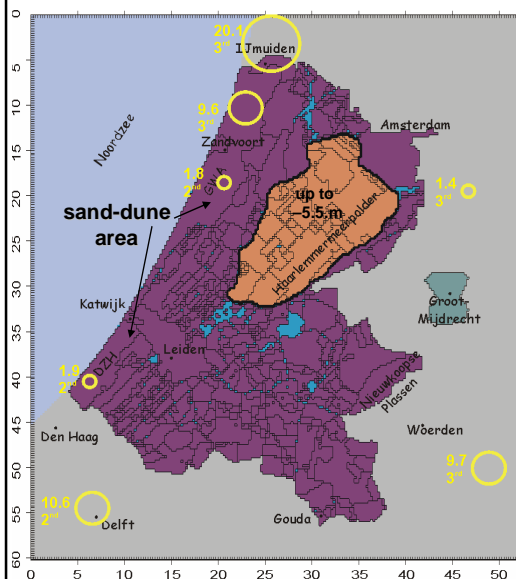
Model of the Waterboard Rijnland

### 3D Case: effect measurements Waterboard Rijnland



### Characteristics of the Waterboard Rijnland

Rijnland



- Land surface: ~1100 km<sup>2</sup>

- Geometrical units:

- 1. Waterboard of Rijnland
- 2. Haarlemmermeerpolder
- 3. Open Water
- 4. Sea
- 5. Remaining land
- 6. Polder Groot-Mijdrecht

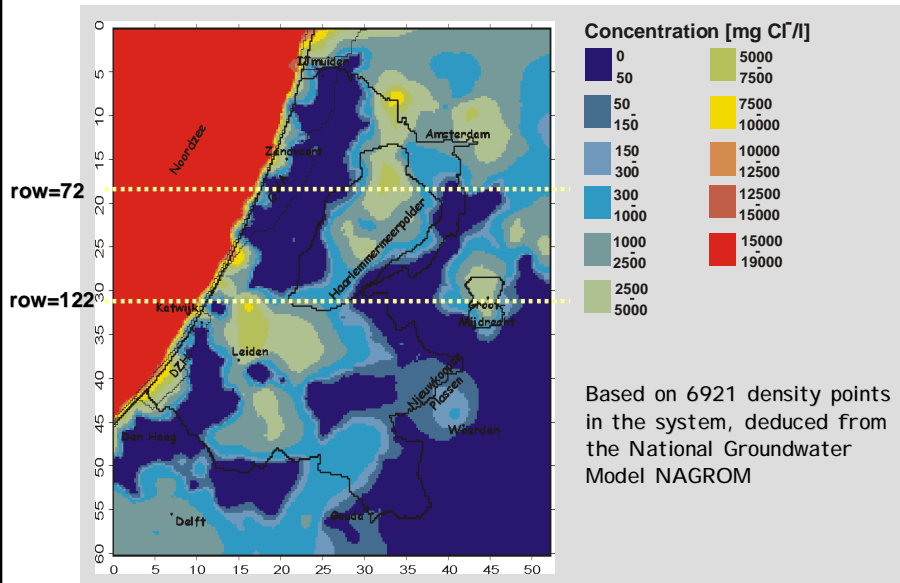
- 550 polder units in Water Board

=position of extraction

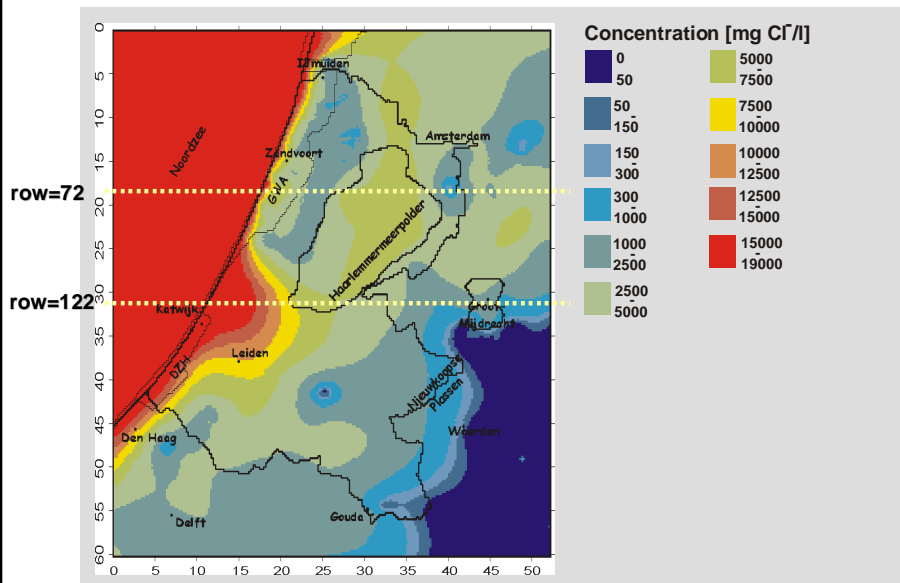
**9.6** =rate of extraction [ $10^6$  m<sup>3</sup>/yr]

**3<sup>rd</sup>** =aquifer from which water is extracted

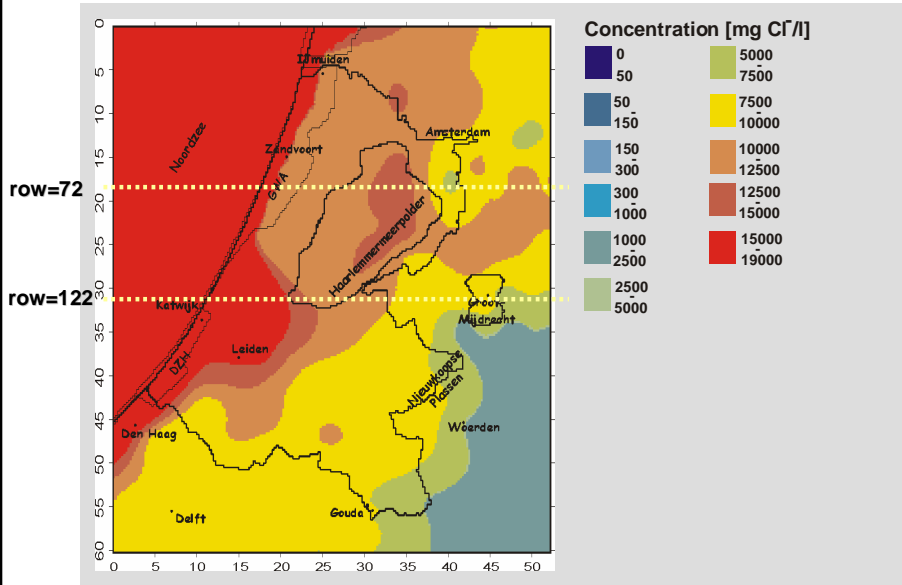
### Present chloride concentration in the top layer



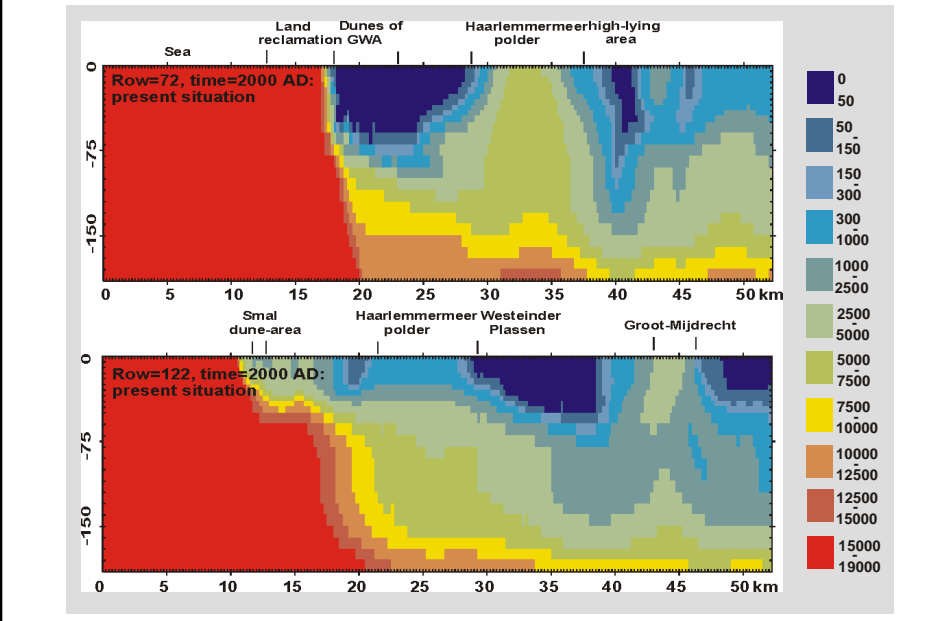
### Present chloride concentration at -95 m N.A.P.



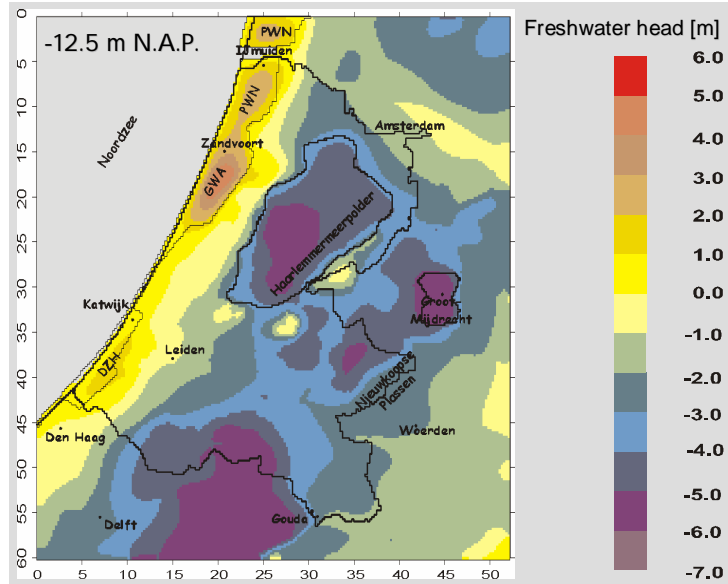
Present chloride concentration at -175 m N.A.P.



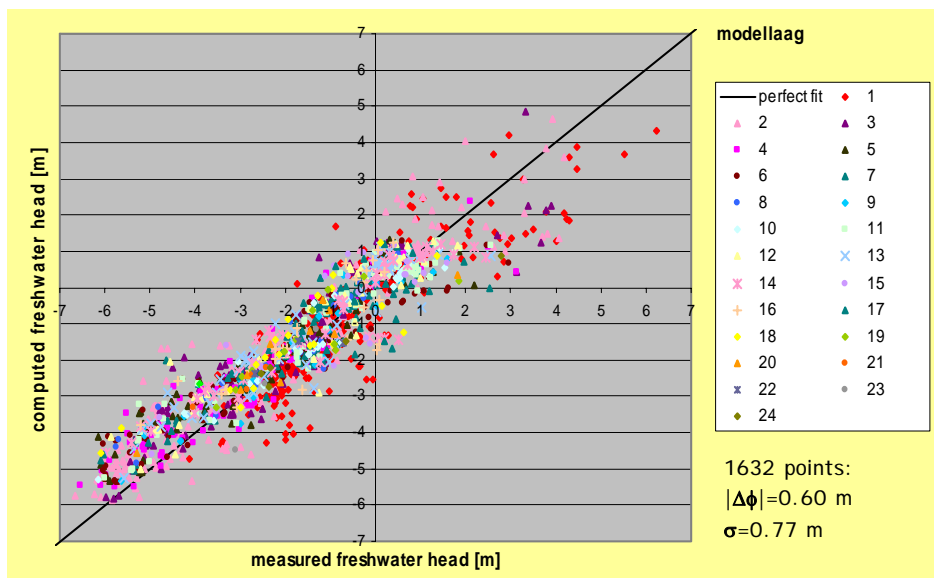
Present chloride concentration in row 72 and 122



### Computed present phreatic water level

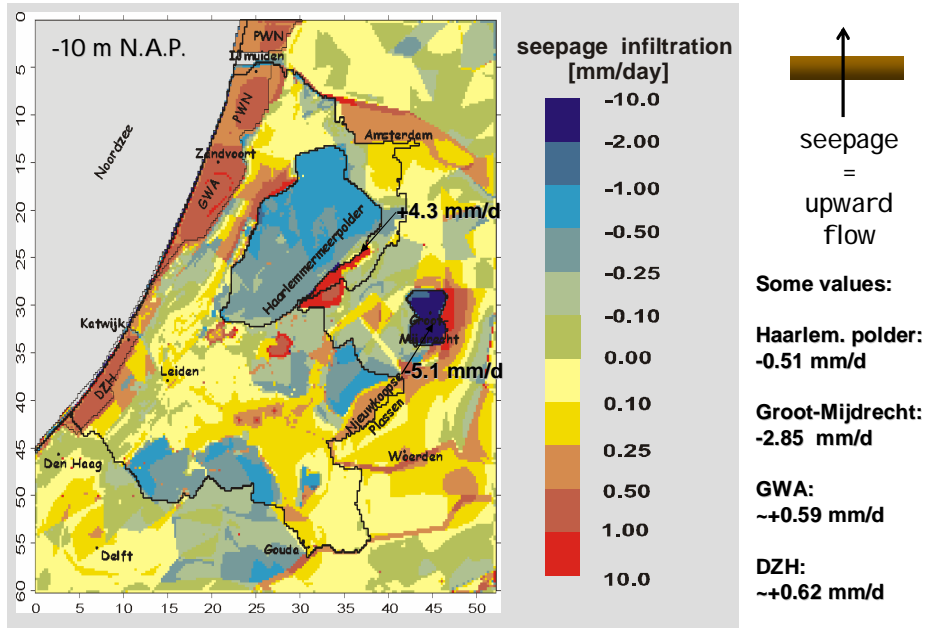


### Calibration characteristics: head

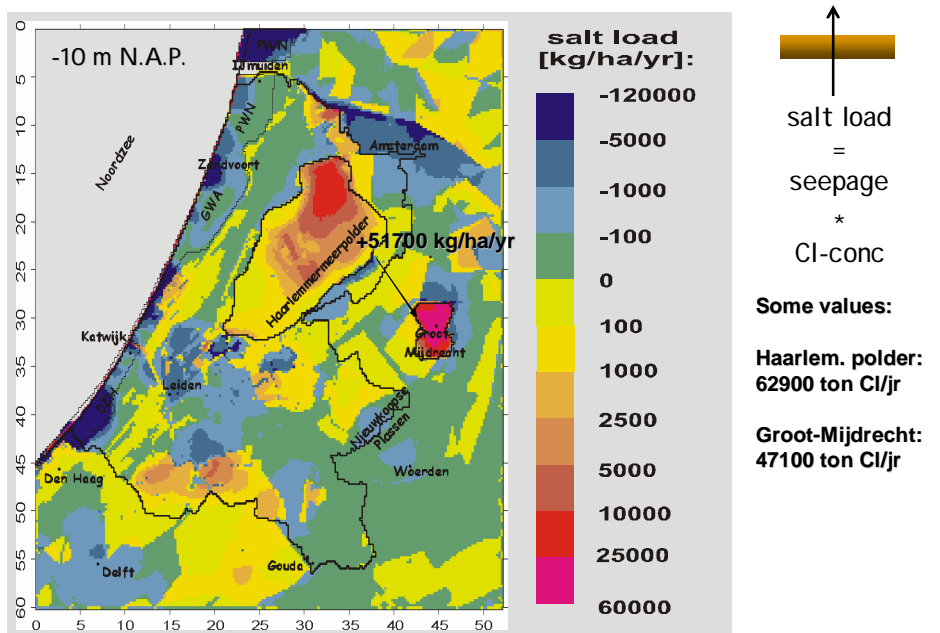




### Calculated present seepage and infiltration



### Calculated present salt load



## Four future scenarios (during 500 years):

### I. Reference case

-to determine autonomous salt water intrusion

### II. Climate change case:

-sea level rise of 0.9 m/century

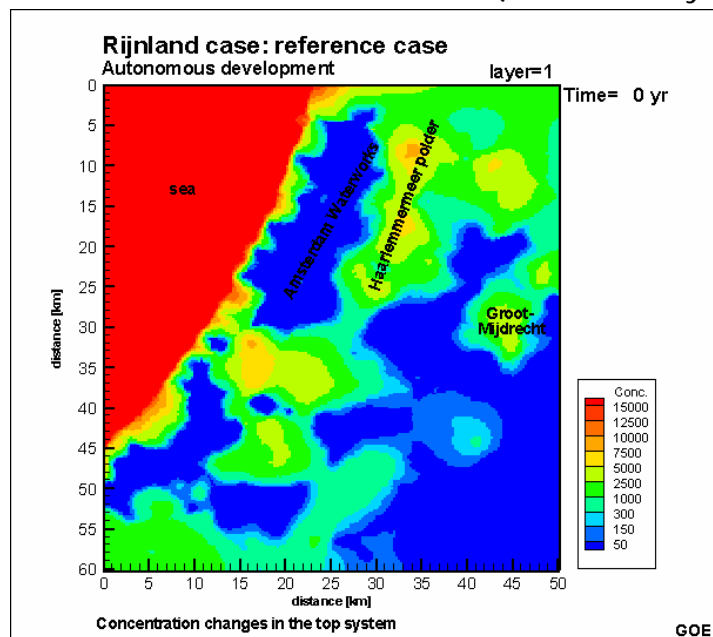
-increase of natural recharge in dunes with 6%

-decrease of groundwater extraction in some sand-dunes

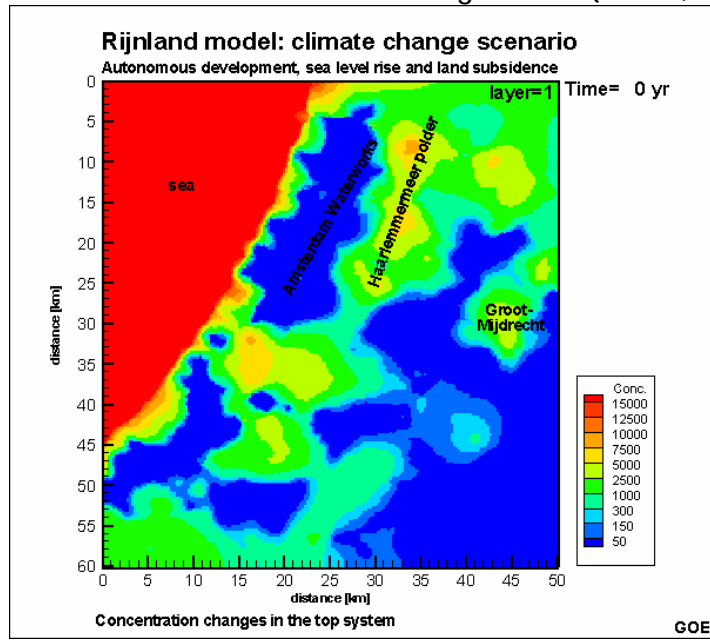
-land subsidence in polder area: 0.3 and 1.0 m/century

### III. Compensating measures

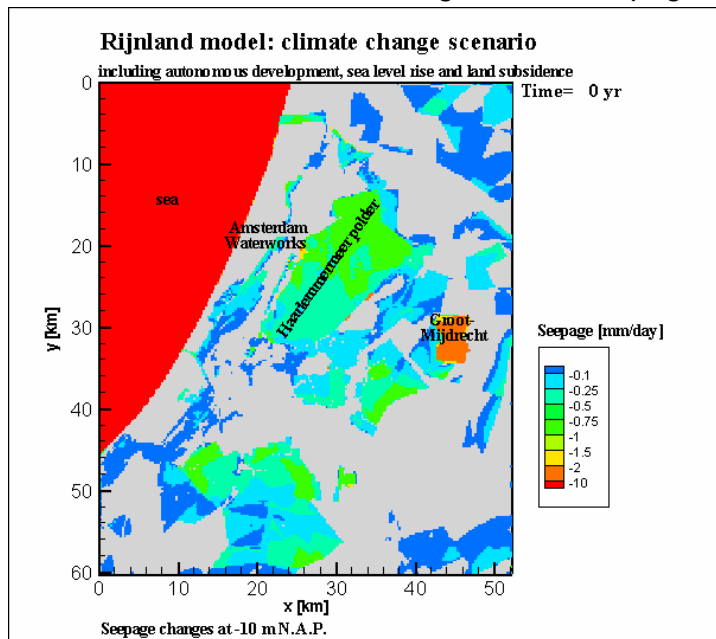
## Rijnland model: I. reference case (conc., 500 yr)



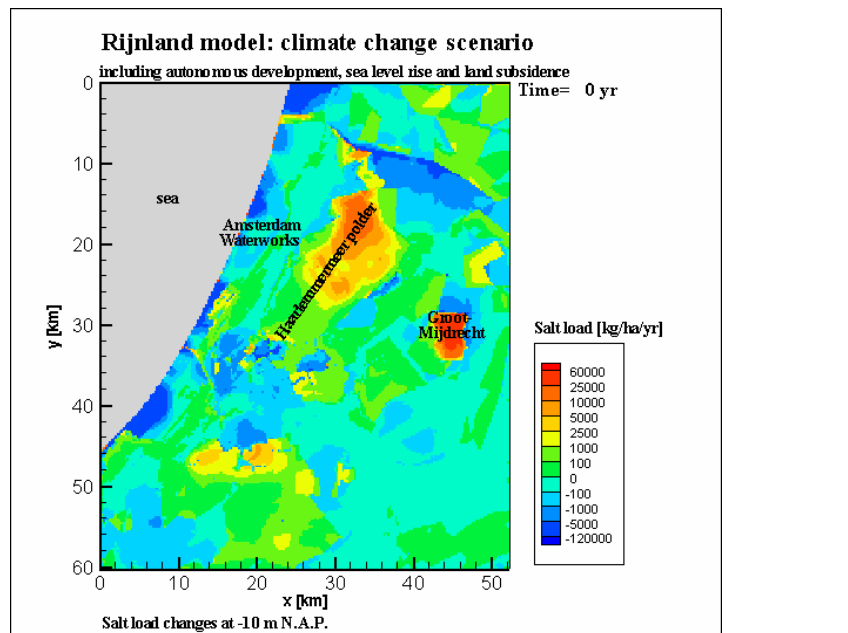
### Rijnland model: II. climate change case (conc., 500 yr)



### Rijnland model : II. climate change case (seepage, 500 yr)



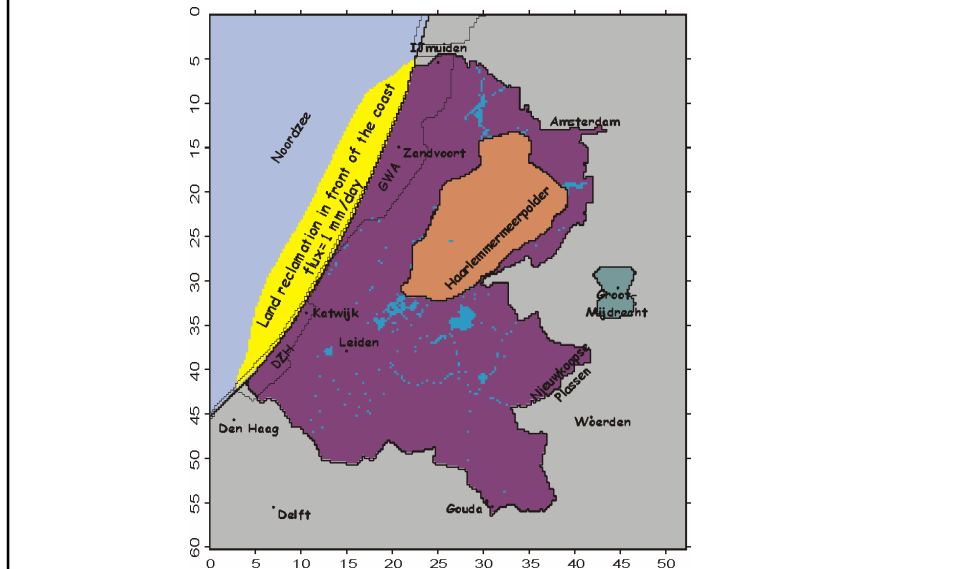
## Rijnland model: II. climate change case (salt load, 500 yr)



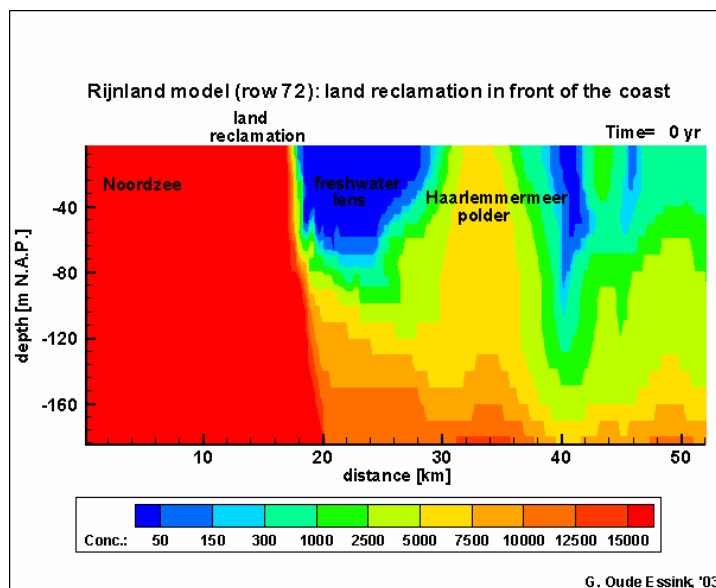
## Possible measures to compensate salt water intrusion

1. Land reclamation in front of the coast
2. Inundation of low-lying polders
3. Extraction of saline/brackish groundwater
4. Infiltration of fresh surface water
5. Creating physical barriers

### 1. Rijnland model: land reclamation case

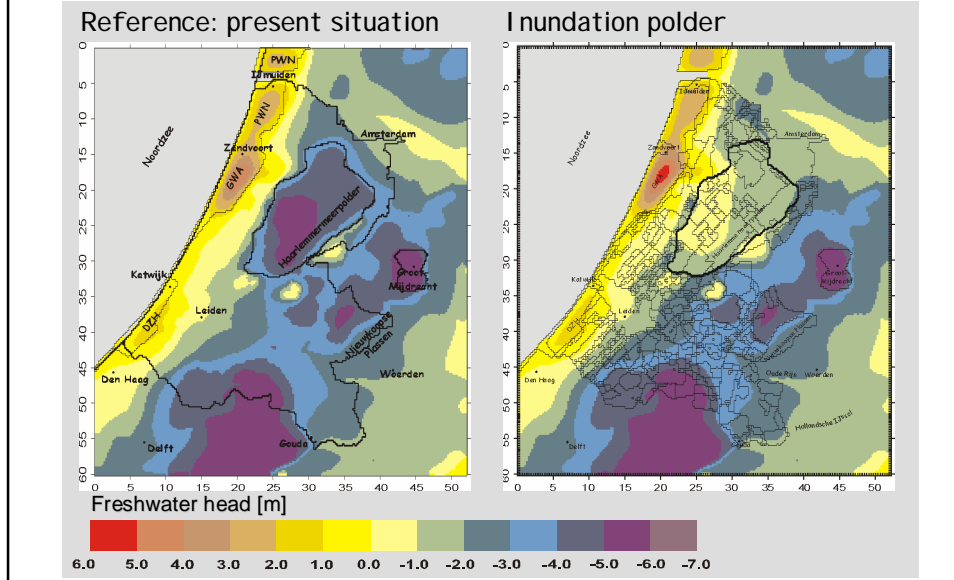


### 1. Land reclamation in front of the coast



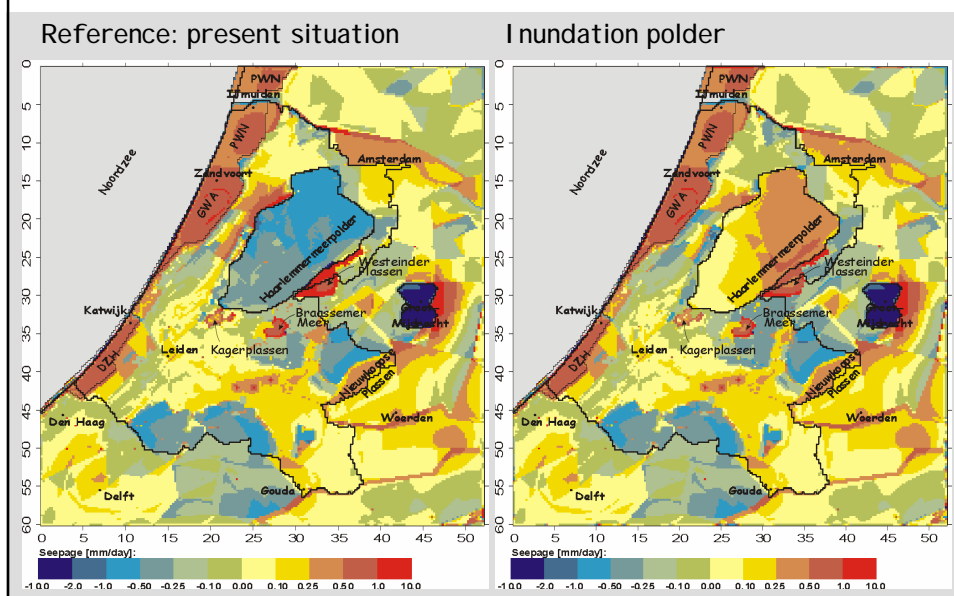
## 2. Rijnland model: I nundation Haarlemmermeerpolder

### Calculated present phreatic water head

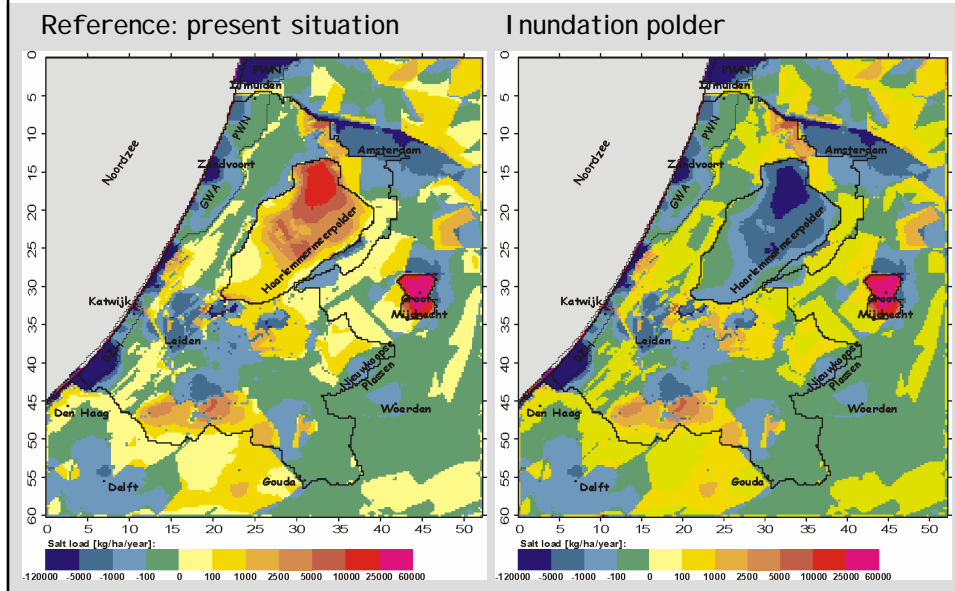


## 2. Rijnland model : I nundation Haarlemmermeerpolder

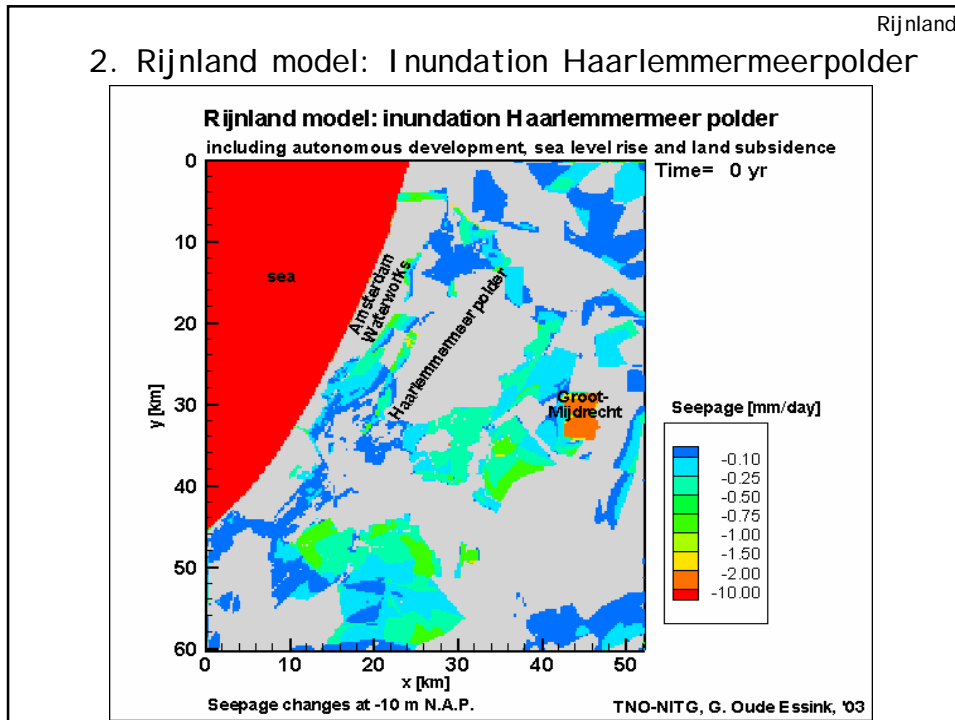
### Calculated seepage and infiltration on -10 m M.S.L.



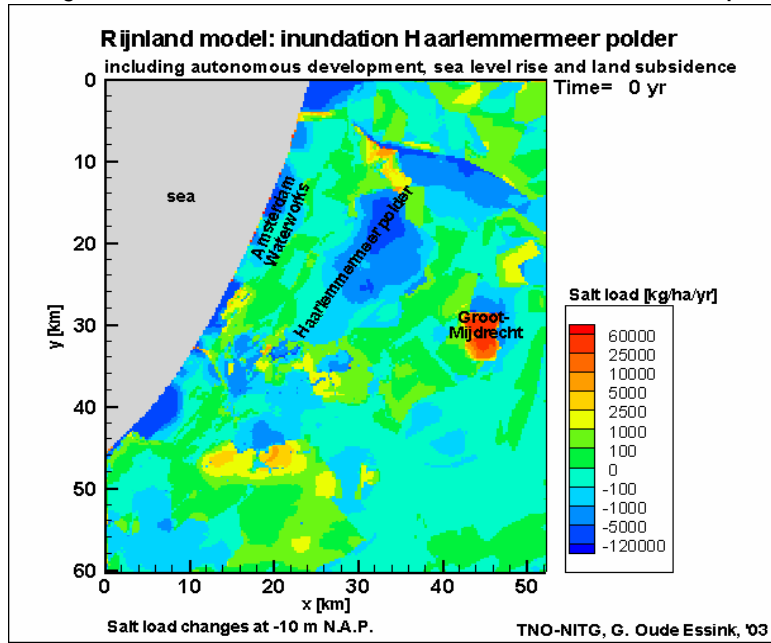
## 2. Rijnland model: Inundation Haarlemmermeerpolder Calculated salt load on -10 m M.S.L.



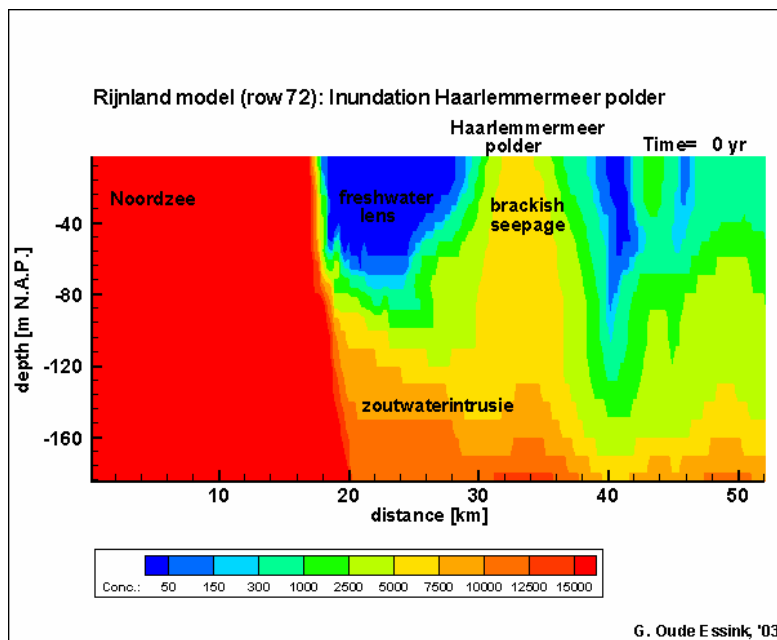
## 2. Rijnland model: Inundation Haarlemmermeerpolder



## 2. Rijnland model: Inundation Haarlemmermeerpolder



## 2. Rijnland model: Inundation Haarl.polder (conc, 500 jr)

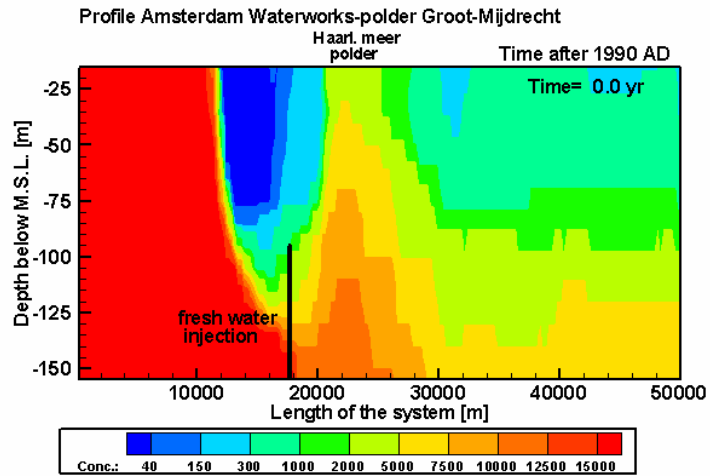




#### 4. Injection of fresh water (conc, 1000 yr)

##### Salinisation of the groundwater flow system

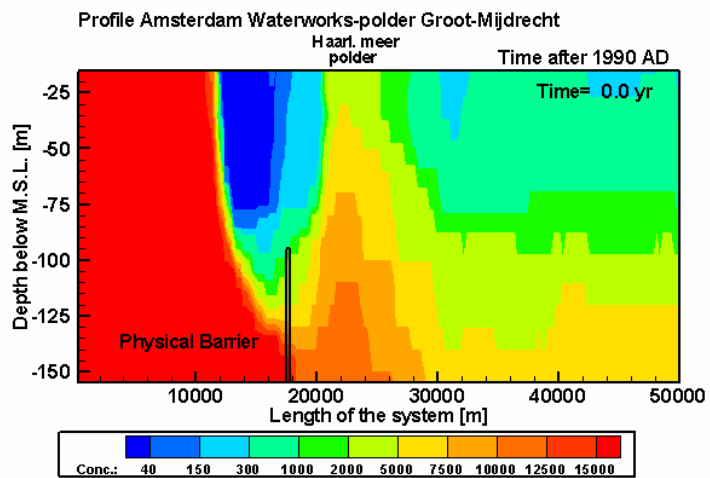
The change in salt content in the subsurface due to fresh water injection and a sea level rise of 0.6 m per century



#### 5. Physical barrier (conc, 1000 yr)

##### Salinisation of a groundwater flow system

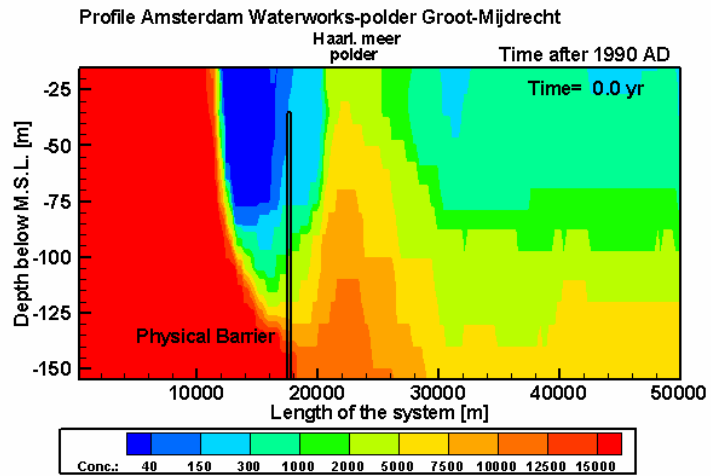
The change in salt content in the subsurface due to a physical barrier in the deep coastal aquifer and a sea level rise of 0.6 m per century



## 5. Physical barrier (conc, 1000 yr)

### Salinisation of the groundwater flow system

The change in salt content in the subsurface due to a physical barrier in the deep coastal aquifer and a sea level rise of 0.6 m per century



MOCDENS3D

*MOCDENS3D is similar to SEAWAT*

## MOCDENS3D

non-steady 3D variable-density groundwater flow

- Genesis present salt-fresh distribution
- Upconing of saline groundwater under extraction wells
- Effects of land subsidence and climate change on groundwater systems

## MOCDENS3D

MOCDENS3D = MOC3D (*Konikow et al., 1996*)  
but adapted for density differences

- density dependent groundwater flow
  - motion: Darcy
  - continuity: mass balance
- solute transport
  - advection
  - hydrodynamic dispersion: mixing of solutes
- fresh, brackish and saline groundwater
- relation between density & concentration

Solving the solute transport equation

MOC particle tracking

MOCDENS3D

Characteristics MOCDENS3D:

- integration of MODFLOW and MOC3D
- finite difference method for groundwater flow
- method of characteristics (particle tracking) for solute transport
- transient flow of groundwater

Advantage MOCDENS3D:

- no numerical problems if grid Peclet numbers are high
- large-scale geometries with limited number of elements are no problem

## Method of Characteristics (MOC)

Solve the advection-dispersion equation (ADE)  
with the Method of Characteristics

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left( D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (C V_i) + \frac{(C - C)W}{n_e}$$

Lagrangian approach:

Splitting up the advection part and the dispersion/source part:

- advection by means of a particle tracking technique
- dispersion/source by means of the finite difference method

## Length flow time step

**NOT EQUAL TO SOLUTE TIME STEP !**

Stability criteria for solute transport equation (I)

1. Neumann criterion:

$$\frac{D_{xx} \Delta t_s}{\Delta x^2} + \frac{D_{yy} \Delta t_s}{\Delta y^2} + \frac{D_{zz} \Delta t_s}{\Delta z^2} \leq 0.5$$

$$\Delta t_s \leq \frac{0.5}{\frac{D_{xx}}{\Delta x^2} + \frac{D_{yy}}{\Delta y^2} + \frac{D_{zz}}{\Delta z^2}}$$

## Stability criteria for solute transport equation (II)

2. Mixing criterion:

$$\Delta t_s \leq \frac{n_e b_{i,j,k}^k}{Q'_{i,j,k}}$$

Change in concentration in element is not allowed to be larger than the difference between the present concentration in the element and the concentration in the source

## Stability criteria for solute transport equation (III)

3. Courant criterion:

$$0 < \xi \leq 1$$

$$\Delta t_s \leq \frac{\xi \Delta x}{V_{x,\max}} \quad \Delta t_s \leq \frac{\xi \Delta y}{V_{y,\max}} \quad \Delta t_s \leq \frac{\xi \Delta z}{V_{z,\max}}$$

### Advantage of the MOC approach by splitting up the advection-dispersion equation

It is difficult to solve the whole advection-dispersion equation in one step, because the so-called Peclet-number is high in most groundwater flow/solute transport problems.

The Peclet number stands for the ratio between advection and dispersion

### Procedure of MOC: advective transport by particle tracking

- Place a number of particles in each element
- Determine the effective velocity of each particle by (bi)linear interpolation of the velocity field which is derived from MODFLOW
- Move particles during one solute time step  $\Delta t_{\text{solute}}$
- Average values of all particles in an element to one node value
- Calculate the change in concentration in all nodes due to advective transport
- Add this result to dispersive/source changes of solute transport

## Steps in MOC-procedure

1. Determine concentration gradients at old timestep  $k-1$
2. Move particles to model advective transport
3. Concentration of particles to concentration in element node
4. Determine concentration gradients on new timestep  $k^*$
5. Determine concentration in element node after advective, dispersive/source transport on timestep  $k$

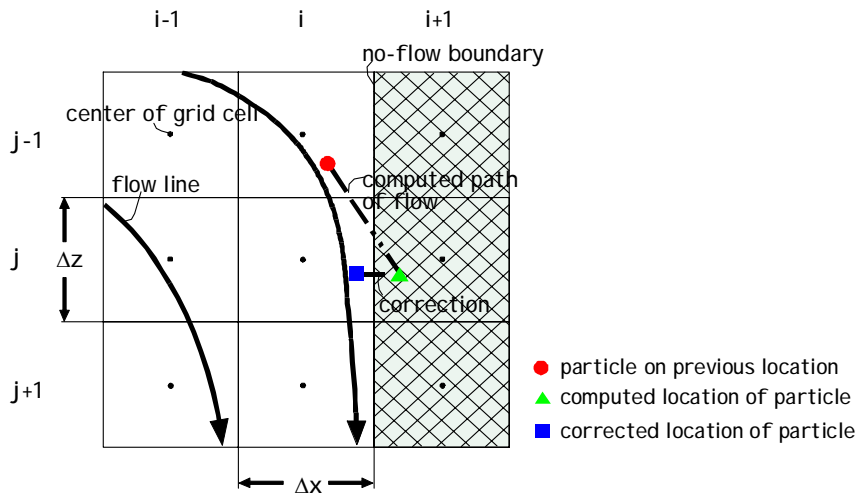
*Konikow and Bredehoeft, 1978*

## Causes of errors in MOC-procedure

1. Concentration gradients
2. Average from particles to node element, and visa versa
3. Concentration of sources/sinks to entire element
4. Empty elements
5. No-flow boundary: reflection in boundary



### Reflection in boundary



### Stability criteria (III)

#### 3. Courant criterium

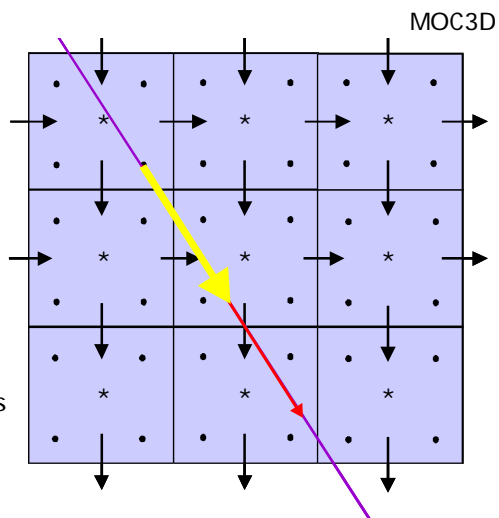
- \* Node element
- Particle
- Velocity direction
- ↘ Movement particles

$$0 < \xi \leq 1$$

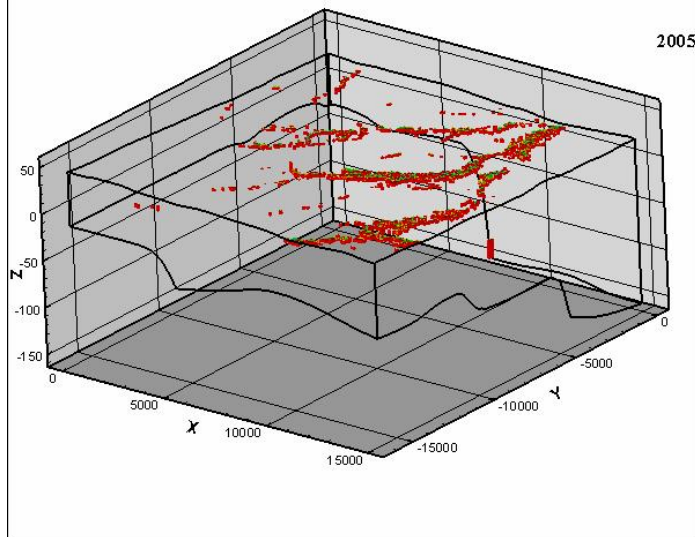
$$\Delta t_s \leq \frac{\xi \Delta x}{V_{x,\max}}$$

$$\Delta t_s \leq \frac{\xi \Delta y}{V_{y,\max}}$$

$$\Delta t_s \leq \frac{\xi \Delta z}{V_{z,\max}}$$



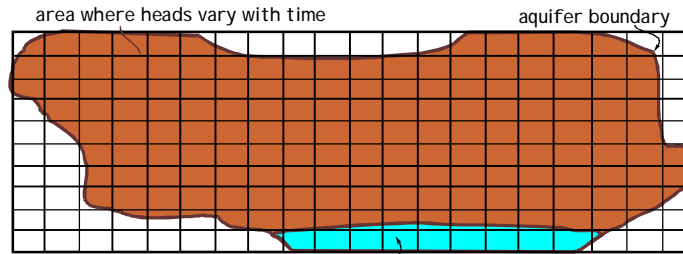
Courant criterion: places where timestep is smaller than 40 days



MODFLOW

### Boundary conditions in MODFLOW (I)

Example of a system with three types of boundary conditions



Numeric model

0	1	1	1	1	1	0	0	0	0	0	0	0	1	1	1	1	1	0	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	0	0	0	0	0	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	0	0

### Boundary conditions in MODFLOW (II)

- For a constant head condition: IBOUND<0
- For a no flow condition: IBOUND=0
- For a variable head: IBOUND>0

### Packages in MODFLOW

1. Well package
2. River package
3. Recharge package
4. Drain package
5. Evaporation package
6. General head package

### 1. Well package

$$Q_{well} = Q_{i,j,k}$$

Example: an extraction of 10 m<sup>3</sup> per day should be inserted in an element as:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

$$Q_{ext,i,j,k} = -10 \quad (\text{in} = \text{positive})$$

$$Q'_{i,j,k} = -10$$

## WEL

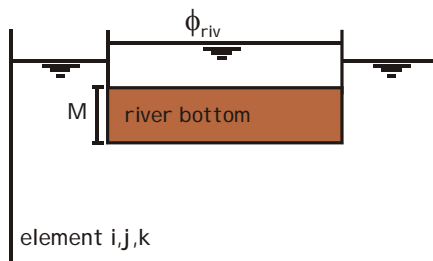
```
2503          0  AUXILIARY CON  CBCALLOCATE  MXWELL, IWELBD
2503          ITMP (NWELLS)
1            1      1      1.360      0.0
1            1      2      1.360      0.0
1            1      3      1.360      0.0
1            1      4      1.360      0.0
1            1      5      1.360      0.0
1            1      6      1.360      0.0
1            1      7      1.360      0.0
.
.
.
Number of Wells for this stress period
-1
-1
-1
```

## GHB

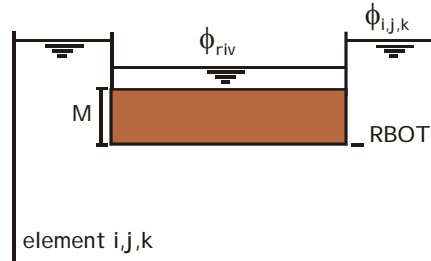
```
5            0  AUXILIARY CONC  CBCALLOCATE  MXGHB, IGHBB
5            ITMP (NGHB)
1            3      1      5.000     10.0     100.0
1            3      2      5.000     10.0     100.0
1            3      3      5.000     10.0     100.0
1            3      4      5.000     10.0     100.0
1            3      5      5.000     10.0     100.0
.
.
.
number of ghb cells
-1
5            ITMP (NGHB)
1            3      1      2.500     10.0     100.0
1            3      2      2.500     10.0     100.0
1            3      3      2.500     10.0     100.0
1            3      4      2.500     10.0     100.0
.
.
.
number of ghb cells
1            3      5      2.500     10.0     100.0
-1
```

## 2. River package (I)

river loses water



river gains water



$$Q_{riv} = KLW \left( \frac{\phi_{riv} - \phi_{i,j,k}}{M} \right)$$

$$Q_{riv} = \frac{KLW}{M} (\phi_{riv} - \phi_{i,j,k}) \Leftrightarrow Q_{riv} = C_{riv} (\phi_{riv} - \phi_{i,j,k})$$

## 2. River package (II)

$$Q_{riv} = C_{riv} (\phi_{riv} - \phi_{i,j,k})$$

Example: the river conductance  $C_{riv}$  is 20 m<sup>2</sup>/day and the river level=3 m, then this package should be inserted in an element as:

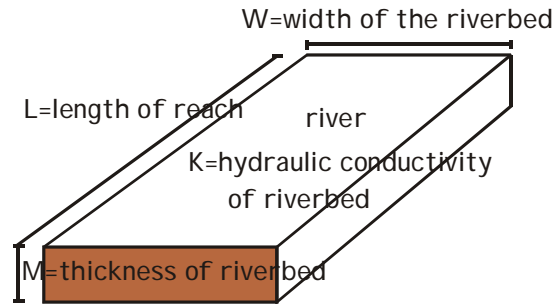
$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

$$Q_{ext,i,j,k} = 20(3 - \phi_{i,j,k})$$

$$Q'_{i,j,k} = 60 \quad \text{and} \quad P_{i,j,k} = -20$$

## 2. River package (III)

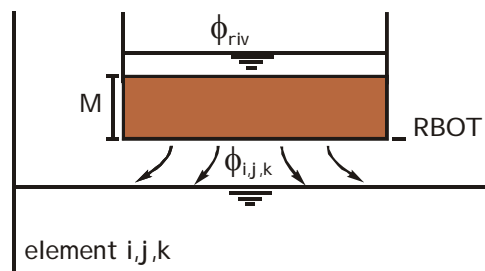
Determine the conductance of the river in one element:



where  $C_{riv} = \frac{KLW}{M}$  is the  
 conductance [ $L^2/T$ ] of the river

## 2. River package (IV)

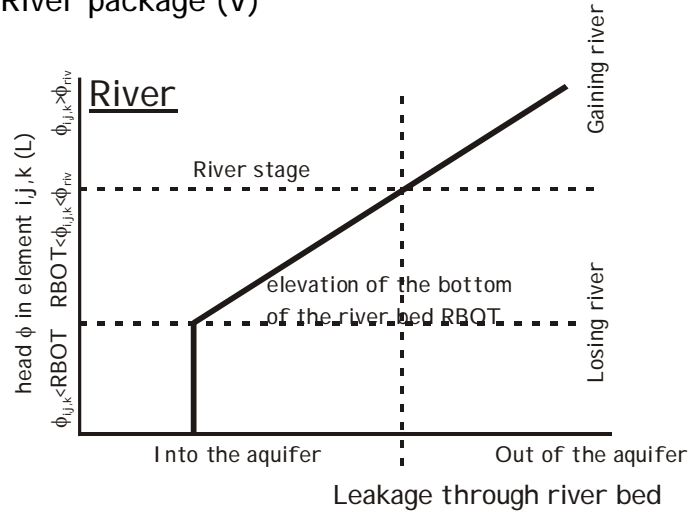
Leakage to the groundwater system



Special case:

if  $\phi_{i,j,k} < RBOT$ , then  $Q_{riv} = C_{riv} (\phi_{riv} - RBOT)$

## 2. River package (V)



## RIV

```

5          0      AUXILIARY CONC CBCALLOCATE MXRIV,IWELBD
5          ITMP (NRIVERS)
1          3      1          2.00      10.00      -2.00      100.00
1          3      2          2.00      10.00      -2.00      100.00
1          3      3          2.00      10.00      -2.00      100.00
1          3      4          2.00      10.00      -2.00      100.00
1          3      5          2.00      10.00      -2.00      100.00
.
.
number of river cells
-1
5          ITMP (NRIVERS)
1          3      1          2.00      10.00      -2.00      100.00
1          3      2          2.00      10.00      -2.00      100.00
1          3      3          2.00      10.00      -2.00      100.00
1          3      4          2.00      10.00      -2.00      100.00
1          3      5          2.00      10.00      -2.00      100.00
.
.
number of river cells
-1

```



3. Recharge package

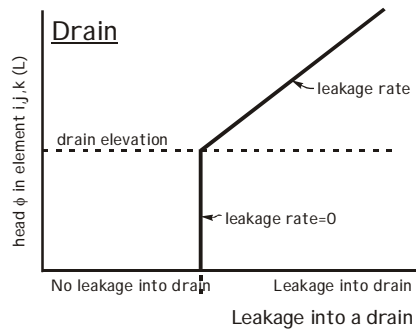
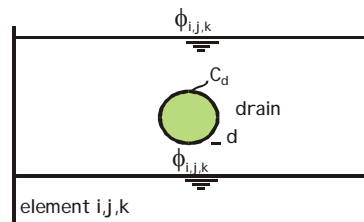
$$Q_{rec} = I\Delta x\Delta y$$

4. Drain package

$$Q_{dm} = C_{dm}(\phi_{i,j,k} - d)$$

Special case:

if  $\phi_{i,j,k} < d$  then  $Q_{dm} = 0$



## DRN

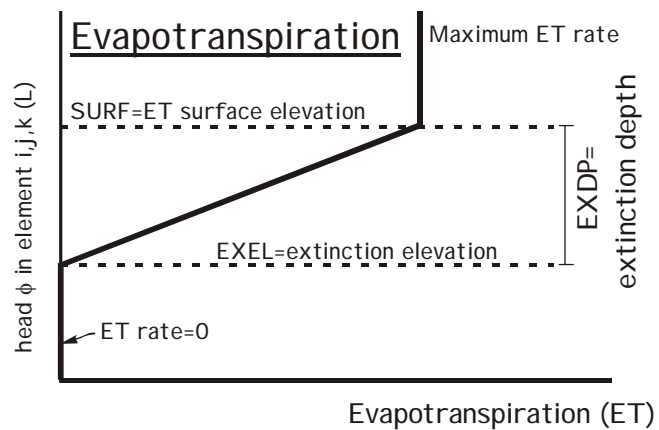
```

5          0  AUXILIARY CONC CBCALLOCATE MXDRAIN, IDRNB
5          ITMP (NDRAIN)
1          3    1 -1.000   10.0   100.0
1          3    2 -1.000   10.0   100.0
1          3    3 -1.000   10.0   100.0
1          3    4 -1.000   10.0   100.0
1          3    5 -1.000   10.0   100.0
.
.
.
number of drainage cells
-1
5          ITMP (NDRAIN)
1          3    1 -1.000   10.0   100.0
1          3    2 -1.000   10.0   100.0
1          3    3 -1.000   10.0   100.0
1          3    4 -1.000   10.0   100.0
1          3    5 -1.000   10.0   100.0
.
.
.
number of drainage cells
-1

```

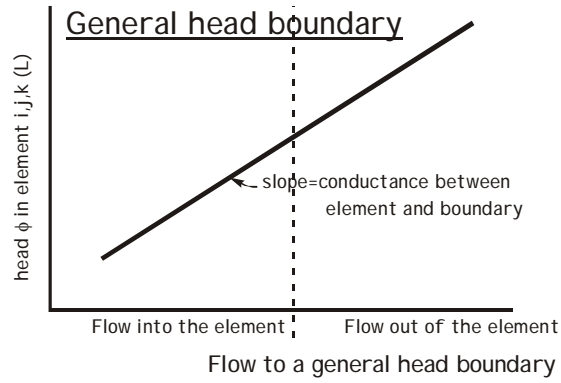
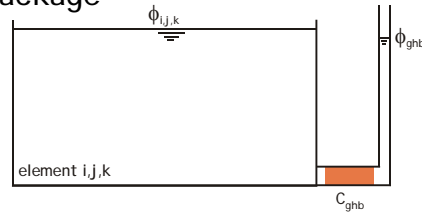
MODFLOW

## 5. Evapotranspiration package



### 6. General head boundary package

$$Q_{ghb} = C_{ghb} (\phi_{ghb} - \phi_{i,j,k})$$



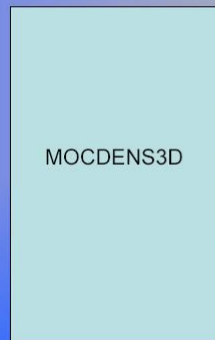
### MOCDENS3D

necessary files

- (name).bas
- (name).bcf
- (name).moc
- (name).sip
- densin.dat
- 2 name- files

optional files

- (name).wel
- (name).riv
- (name).drn
- (name).ghb



- fresh water heads
- concentrations
- velocities

- 1 (name).bas-file
- 2 (name).bcf-file
- 3 (name).moc-file
- 4 (name).wel-file
- 5 (name).riv-file
- 6 (name).drn-file
- 7 (name).ghb-file
- 8 (name).sip-file
- 9 densin.dat-file
- 10 (name).nam-files

## INFILE.NAM

```
List 16 flow.out  
BAS 95 test.bas  
BCF 11 test.bcf  
SIP 19 test.sip  
WEL 66 test.wel  
CONC 33 test_moc.nam
```

## TEST\_MOC.NAM

```
clst 94 test.out  
moc 96 test.moc  
oba 45 test.oba  
data 44 test.obs
```

## BAS

basic grid example

```
          NLAY      NROW      NCOL      NPER      ITMUNI  
          4          50          50          4          4  
FREE  
          0          1          ; IAPART,ISTR  
          95          1(50I2)          3          ; IBOUND 1  
-1-1-1-1-1-1-1-1-1-1-1-1-1-1 ... NCOL  
.  
.  
.  
NROW  
Repeated for every layer  
  9999.00          ; HNOFLO  
    95          1(50F7.2)          1          ; HEAD 1  
4.50  4.50  4.50  4.50 ... NCOL  
.  
.  
.  
NROW  
Repeated for every layer  
  100.00          10          1          PERLEN, NSTP, TSMULTI  
  100.00          10          1          PERLEN, NSTP, TSMULTI  
  100.00          10          1          PERLEN, NSTP, TSMULTI  
  100.00          10          1          PERLEN, NSTP, TSMULTI
```

## BCF

```
          1          0 0.0 0 0.0 0 0          ISS, IBCFBD          BCF Input  
0 0 0 0 LAYCON  
0          1 TRPY  
0          20.0 DELR  
0          20.0 DELC  
0          10.000 TRAN 1  
0          0.0020 VERT/THCK 1  
0          0.500 TRAN 2  
0          0.0020 VERT/THCK 2  
0          15.000 TRAN 3  
0          0.0300 VERT/THCK 3  
0          25.000 TRAN 4
```

## BCF

```
          1          0 0 0 0 0 0 0 0  ISS,IBCFBD      BCF Input
0 0 0 0  LAYCON
          0          1 TRPY
          0          20.0 DELR
          0          20.0 DELC
          11         1.0 (50F6.2)          1      ; TRAN 1
10.00 10.00 10.00 10.00 10.00 10.00 10.00 10.00 ... NCOL
.
.
.
NROW
          11         1.0 (50F7.4)          1      ; VERT/THCK 1
0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 ... NCOL
.
.
.
NROW
Repeated for every layer
```

## BCF

```
          0          0 0 0 0 0 0 0 0  ISS,IBCFBD      BCF Input
0 0 0 0  LAYCON
          0          1 TRPY
          0          20.0 DELR
          0          20.0 DELC
          0 0.002000 SF 1
          0 10.0000 TRAN 1
          0 0.0020 VERT/THCK 1
          0 0.005000 SF 2
          0 0.5000 TRAN 2
          0 0.0020 VERT/THCK 2
          0 0.000100 SF 3
          0 15.0000 TRAN 3
          0 0.0300 VERT/THCK 3
          0 0.000100 SF 4
          0 25.0000 TRAN 4
```

## BCF

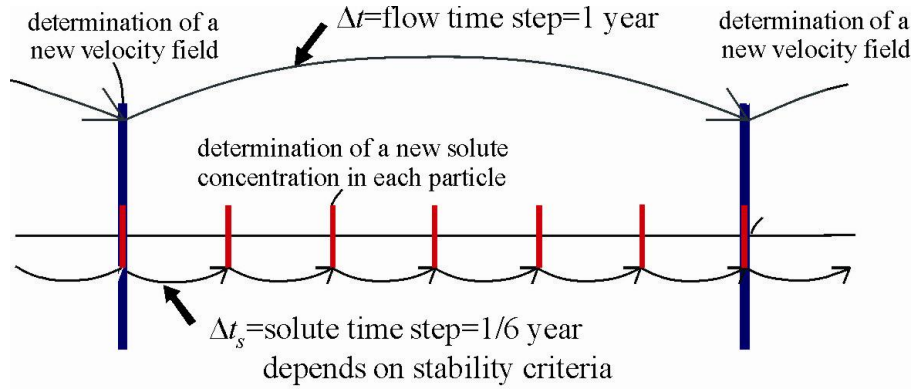
```
0 0 0 0 LAYCON          0          0 0.0 0 0.0 0 0 ISS,IBCFBD      BCF Input
0          0          1 TRPY
0          20.0 DELR
0          20.0 DELC
11 1.000000 (50F9.6)          1      ; SF 1
0.002000 0.002000 0.002000 0.002000 0.002000 0.002000 0.002000 0.002000 ... NCOL
.
.
.
NROW
11          1.0 (50F6.2)          1      ; TRAN 1
10.00 10.00 10.00 10.00 10.00 10.00 10.00 10.00 10.00 10.00 10.00 10.00 ... NCOL
.
.
.
NROW
11          1.0 (50F7.4)          1      ; VERT/THCK 1
0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 0.0020 ... NCOL
.
.
.
NROW
Repeated for every layer
```

MODFLOW

## Time indication MODFLOW

```
I TMUNI =1: seconde
I TMUNI =2: minute
I TMUNI =3: hour
I TMUNI =4: day
I TMUNI =5: year
```

## Flow time step and solute time step



- \* velocity field remains constant during 1 year
- \* solute concentration changes during each solute time step

## MOC (1/2)

moc basic grid example

```

1      4      1      50      1      50 ISLAY1 ISLAY2 ISROW1 ISROW2
0      0      0 NODISP DECAY  DIFFUSION
0      8 NPMAX  NPTPND
0.6    0.05    2 CELDIS FZERO  INTRPL
0      3      0      8      0      8      -1 NPNTCL ICONFM ... IVELFM
-9999 CNOFLOW
96      1.0(50F9.2)
0.00    0.00    0.00    0.00    0.00    0.00    0.00 ... NCOL
.
.
.
NROW
Repeated for every layer
1 NZONES
-1      0.0
0      1
0      1 ; IGENPT 1
0      1 ; IGENPT 2
0      1 ; IGENPT 3
0      1 ; IGENPT 4
0      0.50 ; ALONG
0      0.050 ; ATRANH
0      0.005 ; ATRANV
0      1.000 RF1
0      5.0 THICK 1
0      0.38 POR 1
0      5.0 THICK 2

```



## MOC (2/2)

Repeated for every layer

```
1 NZONES
-1      0.0
0       1      ; IGENPT 1
0       1      ; IGENPT 2
0       1      ; IGENPT 3
0       1      ; IGENPT 4
0       0.50   ; ALONG
0       0.050  ; ATRANH
0       0.005  ; ATRANV
0       1.000  RF1
0       5.0    THICK 1
0       0.38   POR 1
0       5.0    THICK 2
0       0.38   POR 2
0       5.0    THICK 3
0       0.38   POR 3
0       5.0    THICK 4
0       0.38   POR 4
```

## DENSIN.DAT

```
30000.0  0.020  CONCD  DVCONC
0.0      32.5   175    500    1000   2700   CONC.COLORS FOR FILM-OPTION
5000     7500  10000  15000  20000  27000  CONC.COLORS FOR FILM-OPTION
```