

IHE 2016

Density dependent groundwater flow

salt water intrusion (and heat transport)

Gualbert Oude Essink

Lecture set-up:

- PowerPoint sheets
- Practicals

<http://freshsalt.deltares.nl>

Deltares
Unit Subsurface and Groundwater Systems
gualbert.oudeessink@deltares.nl



16-17-20-21 June 2016

Groundwater in the Coastal Zone

<http://zoetzout.deltares.nl>
<http://freshsalt.deltares.nl>



Joost Delsman



Pieter Pauw



Sebastian Huzar



Perry de Louw



Esther van Baaren



Jarno Verkaik



Marta Faneca

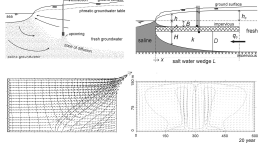


Gualbert Oude Essink

Lecture notes, practicals and ppt on freshsalt.deltares.nl

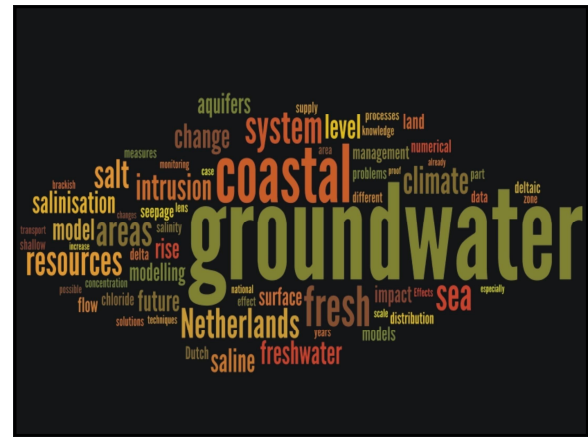
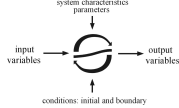
1. Density dependent groundwater flow

<http://publicwiki.deltares.nl/download/attachments/22183944/gwm2.pdf?version=1&modificationDate=126894>



2. Groundwater modelling

<http://publicwiki.deltares.nl/download/attachments/22183944/gwm1.pdf?version=1&modificationDate=126875>



Curriculum Vitae

Introduction

- Delft University of Technology, Civil Engineering: till 1997
Ph.D.-thesis: Impact of sea level rise on groundwater flow regimes
- Utrecht University, Earth Sciences: till 2002
- Free University of Amsterdam, Earth Sciences: till 2004
- Deltares - Geological Survey of the Netherlands
- Utrecht University: from 2014

Qualifications:

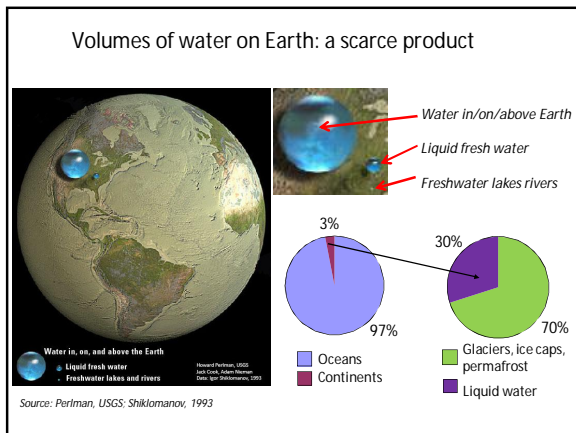
- Groundwater resources management
- Density-dependent groundwater flow and coupled solute transport
- Salt water intrusion in coastal aquifers
- Assessment of climate change on groundwater resources
- Numerical Modeling
- Teaching and training

<http://freshsalt.deltares.nl>

Deltares: gualbert.oudeessink@deltares.nl

Research on groundwater in the coastal zone

- 18 years experience in variable-density dependent groundwater flow and coupled solute transport in the coastal zone
- Incorporating monitoring campaigns results in numerical modeling tools
- Research on new fresh-saline phenomena: salty seepage boils and shallow freshwater lenses in saline environments
- Knowledge on creating 3D initial chloride distribution, based on geostatistics and geophysical data (analyses, VES, borehole measures, AEM)
- Quantifying effects of climate change and sea level rise on fresh groundwater resources
- Developing adaptive and mitigative measures to stop salinization in the coastal groundwater system (e.g. ASR, MAR: fresh keeper, coastal collectors, freshwater storage underground)

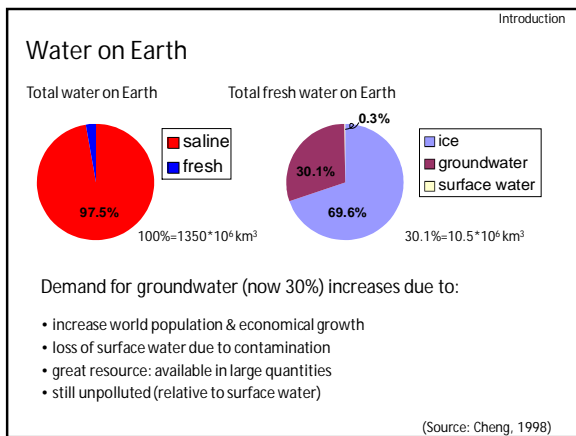


Salt Water Intrusion Meeting, since 1968

<http://www.swim-site.org/>

Themes

- Water system analysis
- Monitoring
- Modelling
- Effects
- Solutions



Salt Water Intrusion Meeting (SWIM)

Home History Next meeting Proceedings Links About this site

Welcome to the homepage of the Salt Water Intrusion Meeting

The Salt Water Intrusion Meeting (SWIM) has been held in different European countries on a biennial basis since 1968 with an increasing number and diversity of participants. In spite of its name, SWIM is not solely restricted to seawater intrusion problems. The meetings are very successful in bringing together people who are interested in saline groundwater issues: well-known specialists, water managers and students.

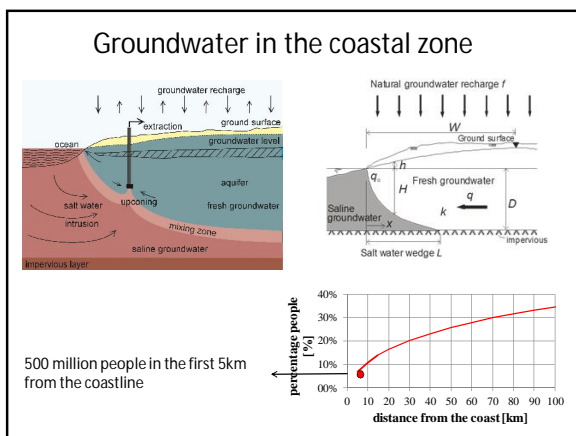
The growing interest among scientists and water managers reflects the increasing relevance of managing saline groundwaters all around the world, especially in densely populated coastal areas. Problems include:

- over-exploitation of water resources, especially in arid and semi-arid areas
- increased demand due to economic development and population growth
- quality deterioration of the available surface water resources
- insufficient knowledge of the aquifer architecture and processes to design sound management programmes
- climate change and sea level rise

Philosophy of SWIM

The SWIM aims to bring together specialists, exchange ideas and discuss results on saline groundwater problems in a friendly and relaxed atmosphere. The meetings have always maintained their informal character with contributions from well-known scientists mixed with young people giving their first presentation. The ambience during the meetings of the last 34 years can be characterized as based on personal contacts and good discussions. There is no SWIM association or so, with memberships and fees; SWIM is carried by persons and institutions in various countries, which have confidence in it and see the usefulness of these meetings.

www.swim-site.org



Salt Water Intrusion Meeting (SWIM)

Home History Next meeting Proceedings Links About this site

The proceedings of the Salt Water Intrusion Meeting

The SWIM proceedings span a period of almost 40 years. The proceedings of the first informal meeting consisted of a few pages in German. Successive meetings all had regular proceedings. They provide an excellent overview of the developments in the research of saline groundwater over the past decades.

At the 18th SWIM in Cartagena it was agreed that efforts will be undertaken to make all SWIM proceedings available through the internet. Currently, the proceedings of the 13th, 15th, 16th, 17th, 19th, 20th, and 21st SWIM and the abstracts of the 18th SWIM are available from this web site. The proceedings of other meetings will become available as soon as they have been digitized. Some hardcopies of proceedings can still be ordered from various publishers. Links to these are provided on this page.

Available for download:

- Proceedings of the 21th Salt Water Intrusion Meeting, S. Miguel, Azores, Portugal
- Abstracts of the 20th Salt Water Intrusion Meeting, Naples, Florida, USA
- Proceedings of the 19th Salt Water Intrusion Meeting, Cagliari, Italy
- Abstracts of the 18th Salt Water Intrusion Meeting, Cartagena, Spain
- Proceedings of the 17th Salt Water Intrusion Meeting, Delft, The Netherlands
- Proceedings of the 16th Salt Water Intrusion Meeting, Wolin Island, Poland
- Proceedings of the 15th Salt Water Intrusion Meeting, Ghent, Belgium
- Proceedings of the 13th Salt Water Intrusion Meeting, Cagliari, Italy

For sale (external links)

- Proceedings of the 18th Salt Water Intrusion Meeting, Cartagena, Spain
- Proceedings of the 12th Salt Water Intrusion Meeting, Barcelona, Spain
- Proceedings of the 6th Salt Water Intrusion Meeting, Hannover, Germany

www.swim-site.org

Salt Water Intrusion Meeting (SWIM)

Home History Next meeting Proceedings Links About this site

Back to all proceedings

Proceedings of the 17th Salt Water Intrusion Meeting, Delft, The Netherlands

www.swim-site.org

Cover
Introduction
Preface
Table of contents

Introductory sessions

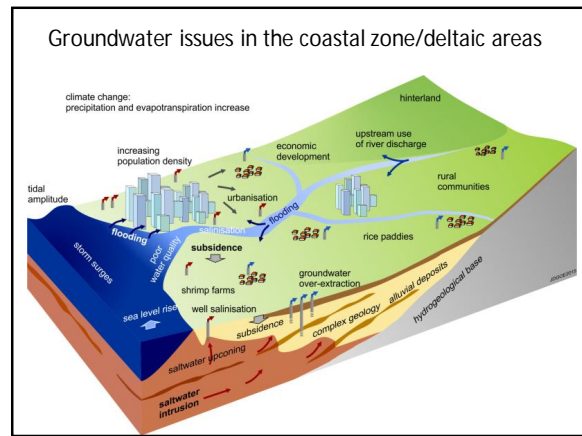
V.C.A. Post - Chemistry for modellers: Aqueous geochemistry in coastal areas
G.H.P. Oude Essink - Modelling for geochemists: Everything you always wanted to know about modelling, but were afraid to ask!

TOPIC 1: BASIC UNDERSTANDING, ANALYTICAL CALCULATION METHODS, MIXING ZONE HYDRODYNAMICS, UNSTEADY STATE SOLUTIONS

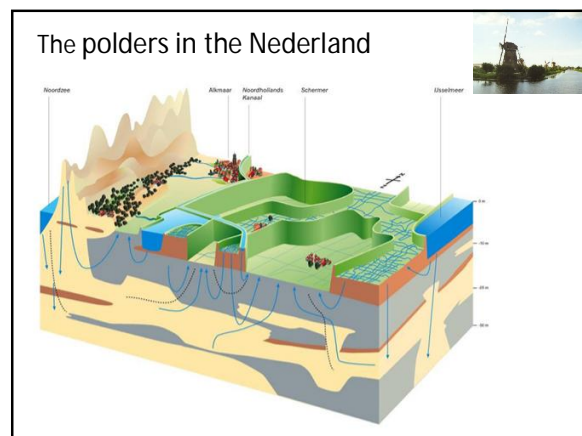
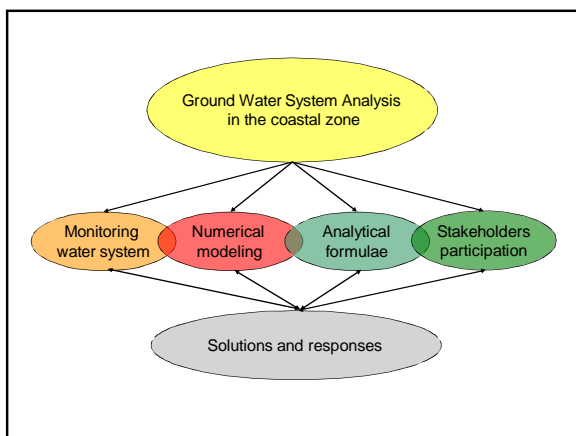
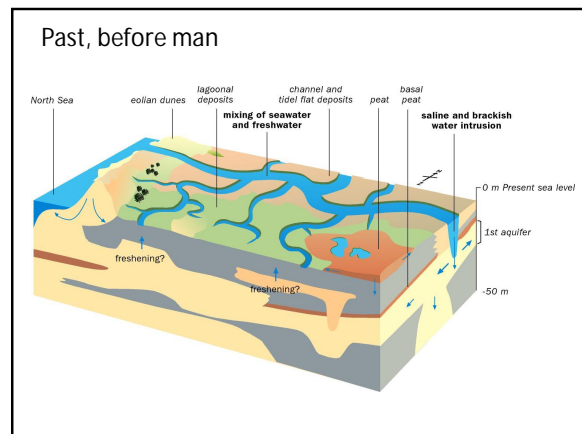
B. Partelleit, W. Kessels and H.D. Schulz - Geochemical processes in the salt-freshwater transition zone - preliminary results of a 2D sand tank experiment
L. Tulpano and M.D. Fidelibus - Mechanisms of groundwater salinization in a coastal karstic aquifer subject to over-exploitation
B. Minema, G. T. Klaver and J. J. P. Verstraalen - Nuland pumping station phased research on the causes of chloride hazards
C. Thoenen - Application of a model adaptive approach to the simulation of density driven flow in an unsaturated laboratory system

TOPIC 2: MODELLING, NEW APPROACHES, SOLUTION OF REAL CASES

N. Van Meir and L. Lebbe - 3D Density-Dependent modelling of sea-level rise scenarios around De Haan (Belgium)
J.M. Van Eick - Adaptive multigrid modeling of density dependent groundwater flow
S.B. Givovich and C.J. Voss - Three-dimensional variable-density flow simulation of a coastal aquifer in southern Oahu



- Introduction
- Topics of density driven groundwater flow
- Introduction
 - water on earth
 - salt water intrusion
 - freshwater head
 - Interface between fresh and saline groundwater
 - analytical formulae (Badon Ghyben-Herzberg)
 - upconing example
 - Numerical modelling
 - mathematical background
 - Benchmark problems: Henry, Elder, Hydrocoin, etc.
 - Case-studies
 - hypothetical cases
 - 2D, 3D cases
 - real cases (Dutch coastal zone)



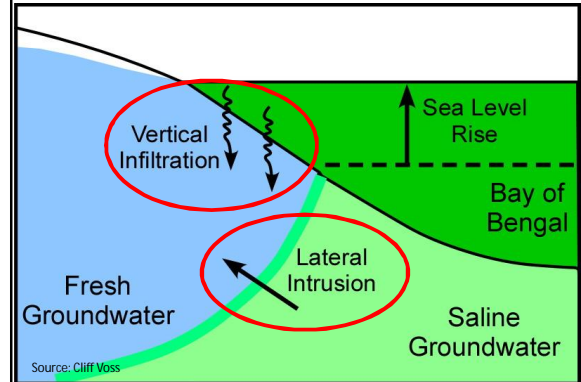
Groundwater in the future

We have to cope with...

- We have to cope with...
- Groundwater extractions
- Development energy use/production (heat-cold)
- Climate change
- Land subsidence
- Development spatial land use
- Politics, Policy & Watermanagement

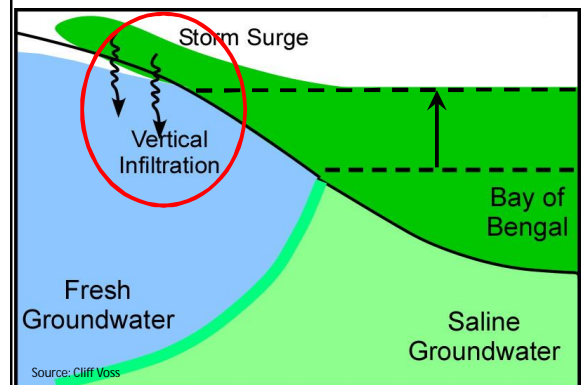
Direct anthropogenic influence on groundwater is more important than climate effect

Modes of Salinization due to Sea-Level Rise



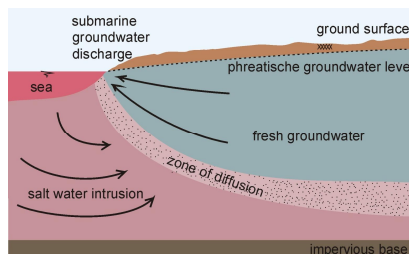
Introduction SWI

Modes of Salinization due to Sea-Level Rise

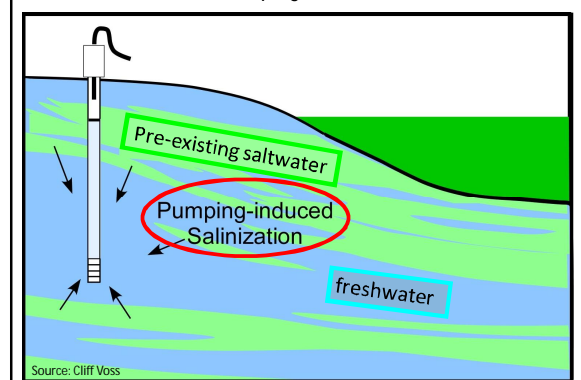


Definition of salt water intrusion

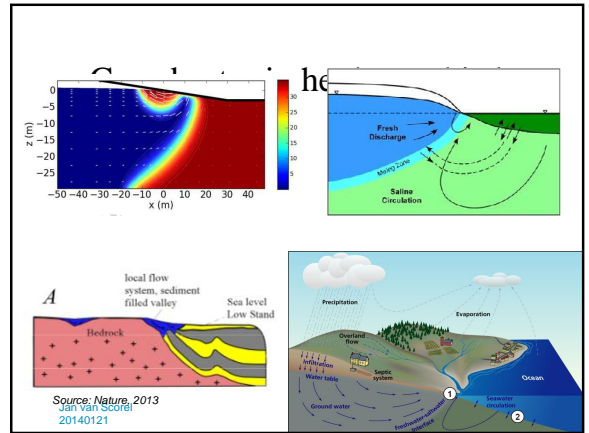
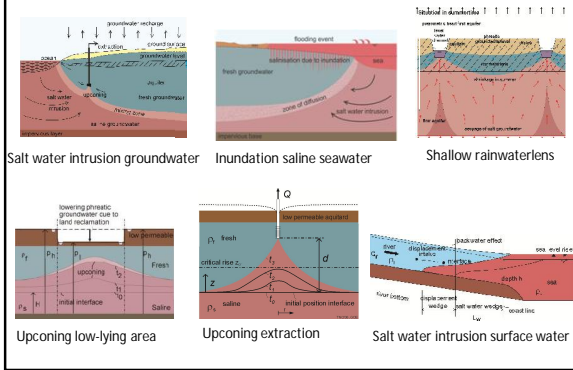
Inflow of saline water into an aquifer which contains fresh water



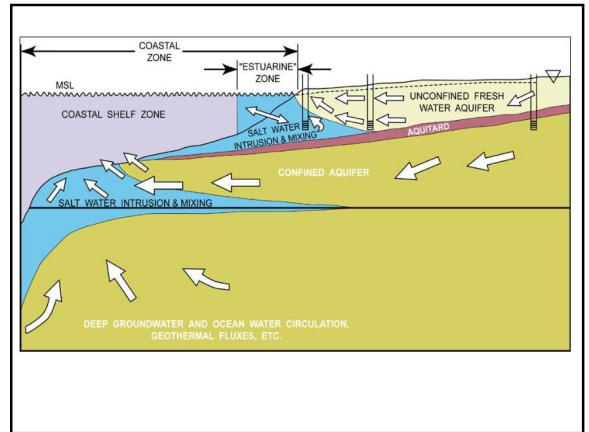
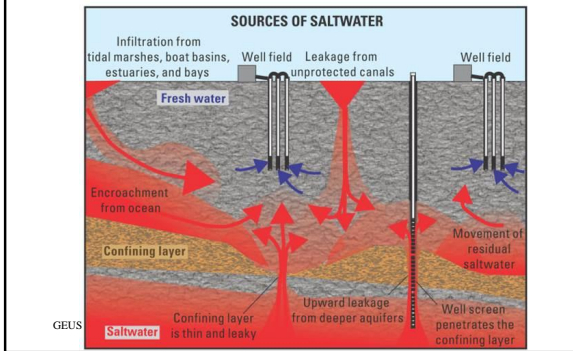
Salinization due to Pumping



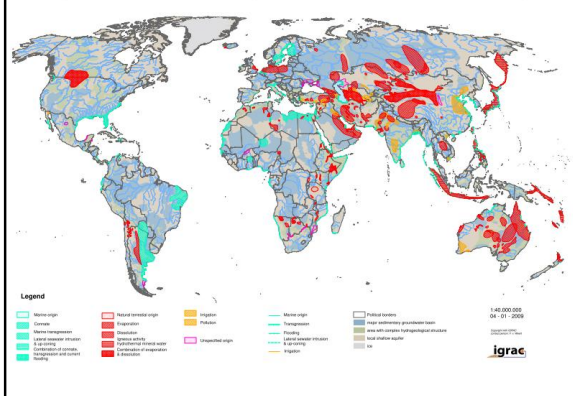
Salinisation processes at local scale



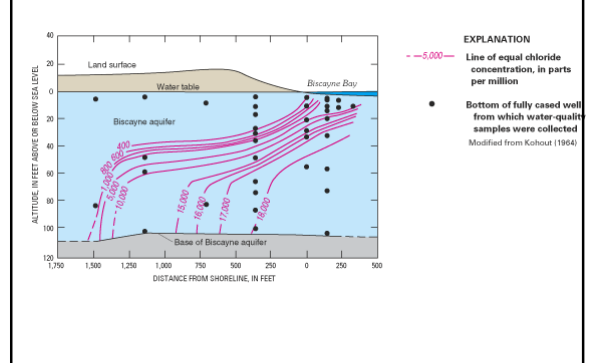
Salinization processes in the coastal zone: combination



Regions with brackish and saline groundwater at shallow and intermediate depths

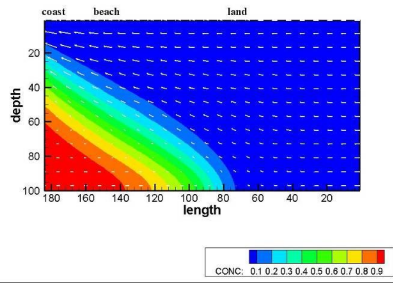


Biscayne aquifer, Florida USA: Henry's case



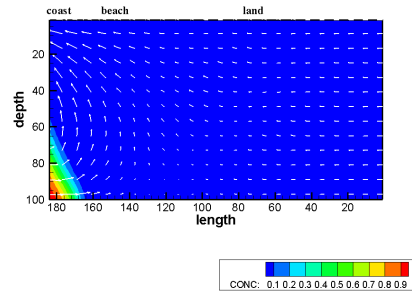
Definition of salt water intrusion

Numerical model: Henry's case



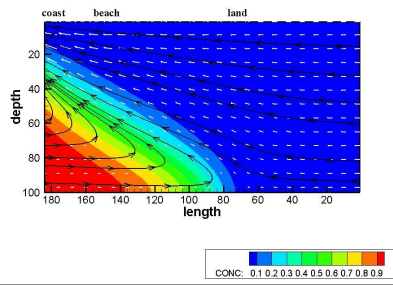
Sea level rise and salt water intrusion

Effect sea level rise on groundwater system in coastal zone



Definition of salt water intrusion

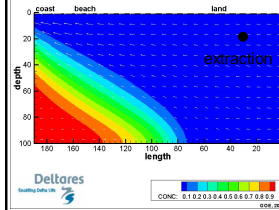
Numerical model: Henry's case



Sea level rise and salt water intrusion

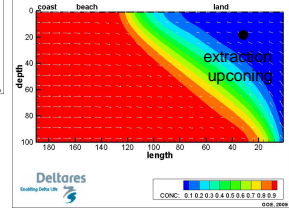
Impact of sea level rise on a coastal groundwater system:

a conceptual model of saltwater intrusion



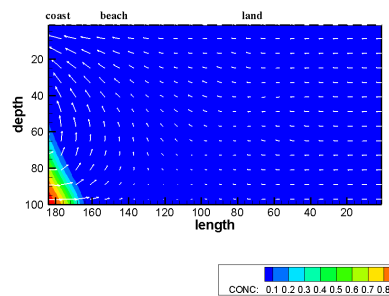
Impact of sea level rise on a coastal groundwater system:

a conceptual model of saltwater intrusion



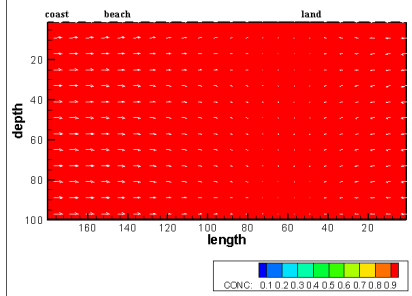
Sea level rise and salt water intrusion

Effect sea level rise on groundwater system in coastal zone

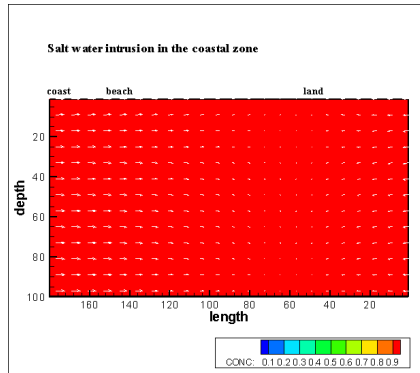


Salt water intrusion

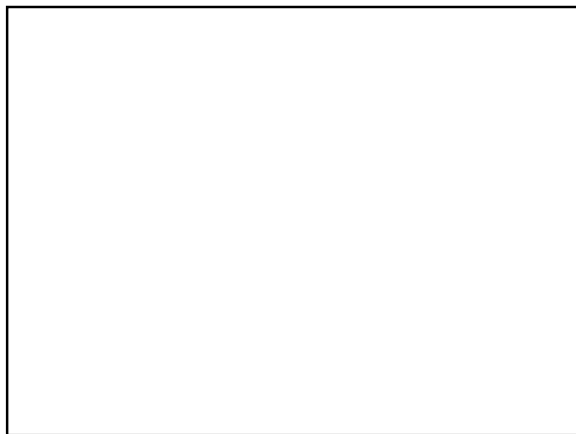
Salt water intrusion in the coastal zone



Salt water intrusion



In 1 liter ocean: about 35 gr salt



In 1 liter ocean: about 35 gr salt



Water on Earth

Introduction

Some serious developments:


"shortage of drinking water will be one of the biggest problems of the 21st century"

"in 2025, two third of world population will face shortage of water"

In 1 liter Dead Sea water (Jordan/Israel) : about 280 gr salt



In 1 liter drinking water: about 0.15 gr salt is allowed



Jan van Scorel
20140121

Salt in water is a problem





Drinking water

Crop damage

Vulnerable nature

Grass can grow well in water with a salt content equal to about 6.5 gr salt in 1 liter water

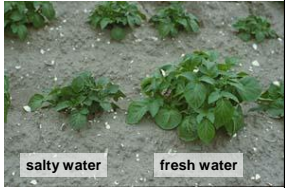


Jan van Scorel
20140121

Introduction

Salt in water is a problem for different water management sectors:

- drinking water:
 - taste (100-300 mg Cl⁻/l)
 - long term health effect
 - norm: EC& WHO=150 mg Cl⁻/l (live stock=1500 mg Cl⁻/l)
- industry:
 - corrosion pipes
 - preparation food
- irrigation/agriculture:
 - production crops
 - salt damage



Definition fresh-brackish-saline

Klasse	Chloride concentratie (mg Cl ⁻ /l)
Zoet	< 1000
Brak	1000 - 3000
Zout	> 3000

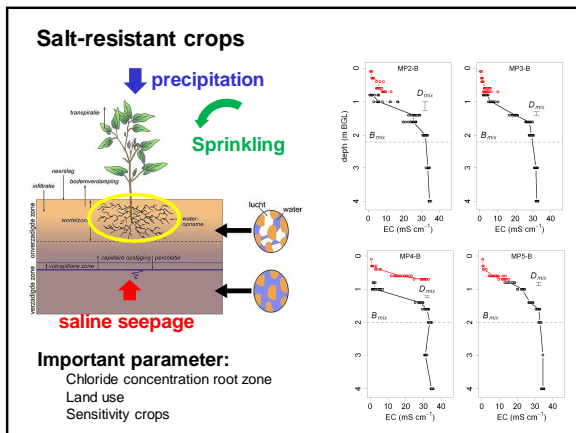
Zieland
Tabel 1: De gebruikte definities voor zoet, brak en zout grondwater in de Zeeuwse Delta. De chloride concentratie, een conservatieve stof die relatief veel bemeeten is i.o.v. andere stoffen, is de dominante representant voor het zoutgehalte.

Type	mS/cm	mg TDS/l	Drinking- or irrigation water
Non-saline or fresh water	<0.8	<600 *	Drinking and irrigation water
Slightly saline	0.8 - 2	600-1.500	Irrigation water
Moderately saline	2-10	1.500-7.000	Primary drainage water and groundwater
Highly saline	10-25	7.000-15.000	Secondary drainage water and groundwater
Very highly saline	25 - 45	15.000-35.000	Seawater is 35000 TDS mg/l
Brine	>45	>45.000	

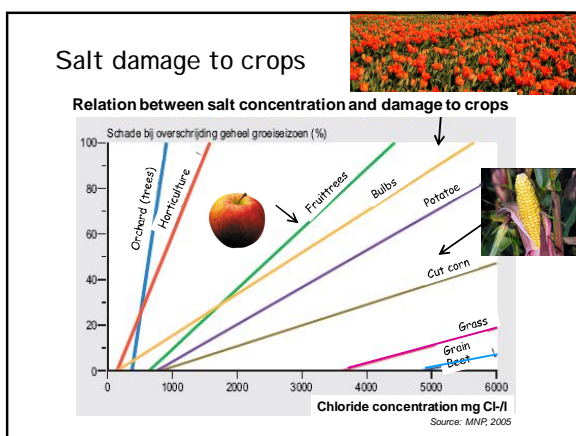
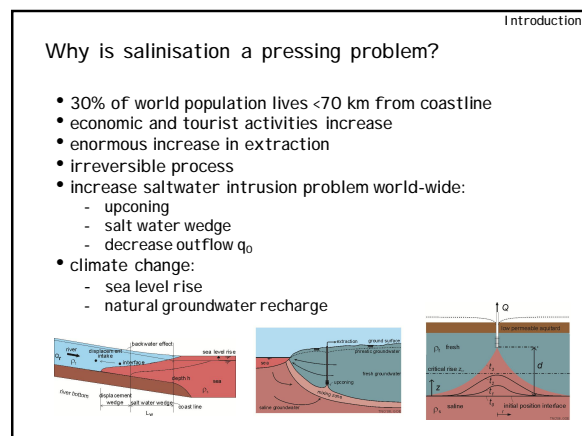
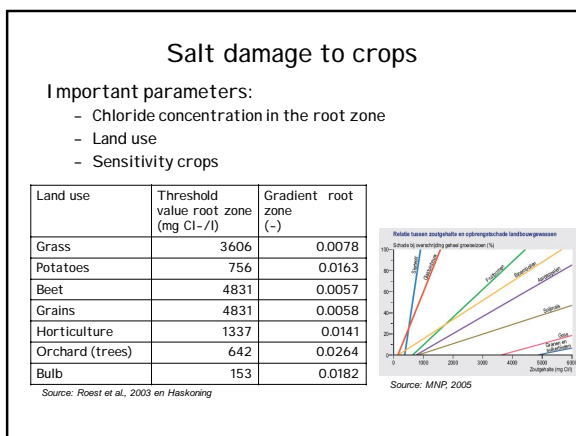
Effects salinisation: salt damage



Source: Proefstation voor de Akkerbouw en Groenteteelt, Lelystad



	Soil moisture		Irrigation water	
	Limit	Gradient	Limit	Gradient
Crop	mg/l Cl	%/mg/l Cl	mg/l Cl	%/mg/l Cl
Potatoe	756	0.0163	202	0.0610
Grass	3606	0.0078	962	0.0294
Sugar beat	4831	0.0057	1288	0.0212
Cut Corn	815	0.0091	217	0.0343
Grains	4831	0.0058	1288	0.0218
Fruit trees	642	0.0264	171	0.0991
Orchard (trees)	378	0.1890	101	0.7086
Vegetables	917	0.0158	245	0.0591
Horticulture	1337	0.0141	356	0.0527
Bulbs	153	0.0182	41	0.0683



Origin of saline groundwater in the subsoil

Geological causes:

- marine deposits during geological times
- trans- and regressions in coastal areas (deltas)
- salt/brine dome

Anthropogenic causes:

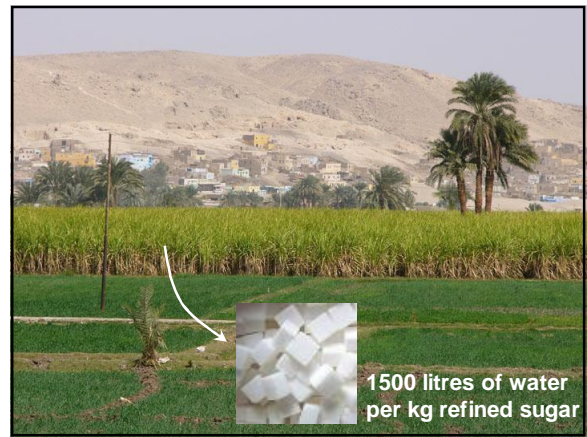
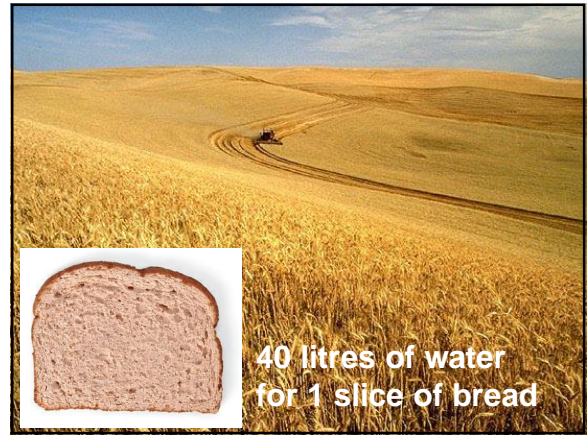
- agriculture/irrigation (salt damage Middle East & Australia)
- upconing under extraction wells throughout the world
- upconing under low-lying areas (e.g. Dutch polders)

Processes that accelerate salt water intrusion:

- Sea level rise
- Land subsidence
- Human activities

Threats for:



- drinking water supply in dunes:
 - upconing of saline groundwater
 - decrease of fresh groundwater resources
 - recharge areas reduction
- agriculture:
 - salt damage to crops: salt load and seepage
- water management low-lying areas:
 - flushing water channels
- ecology

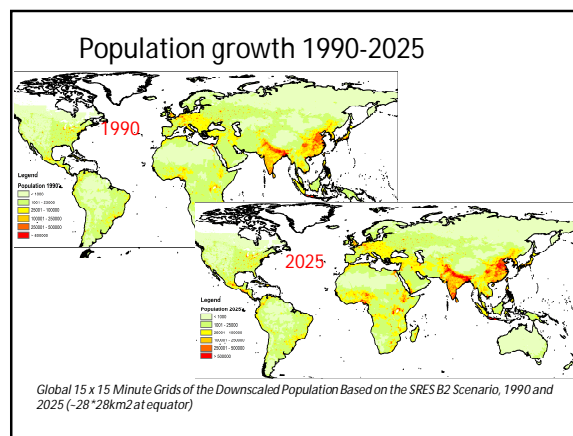
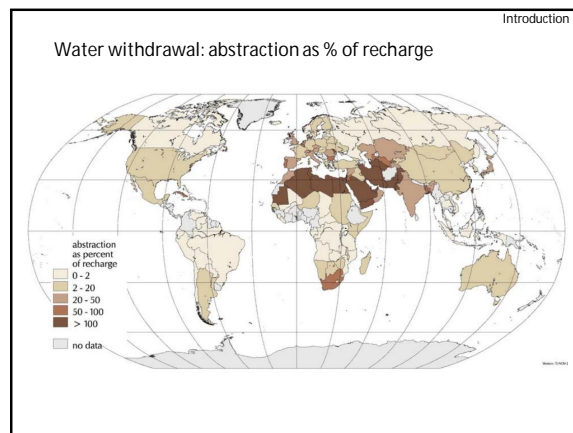
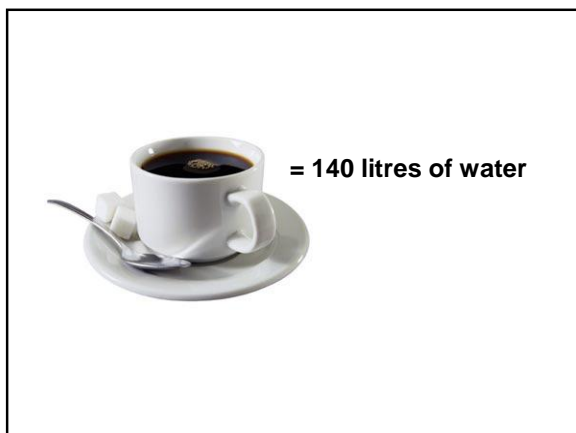


The water footprint of products

global averages

1 kg wheat	1 m ³ water
1 kg rice	3 m ³ water
1 kg milk	1 m ³ water
1 kg cheese	5 m ³ water
1 kg pork	5 m ³ water
1 kg beef	15 m ³ water

Introduction

Question:

Demand fresh water per capita per day in the Netherlands?:

- 10 litre/day
- 25 litre/day
- 100 litre/day
- 200 litre/day

Introduction

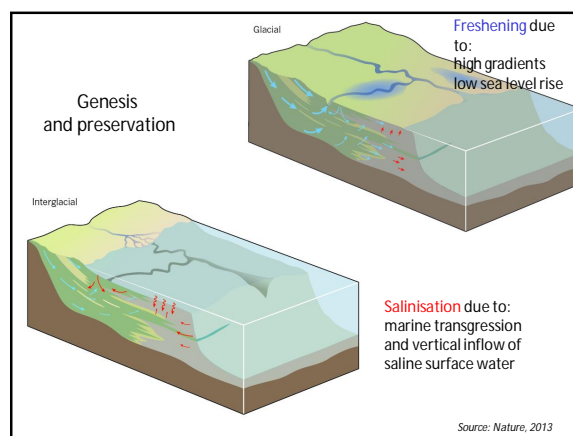
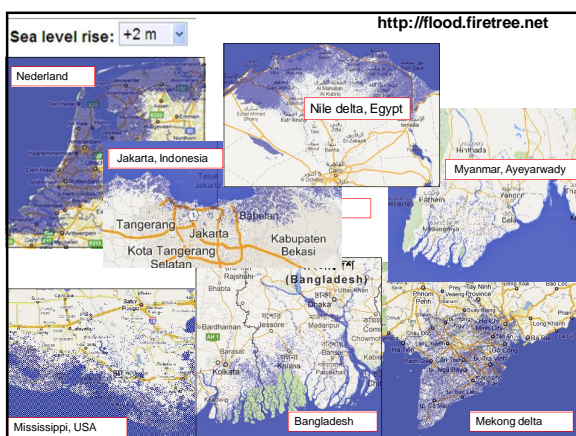
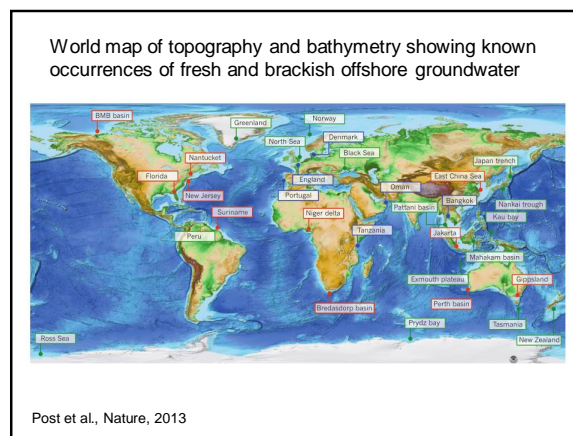
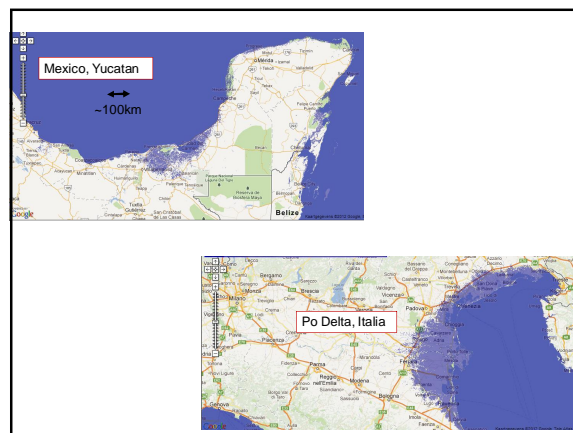
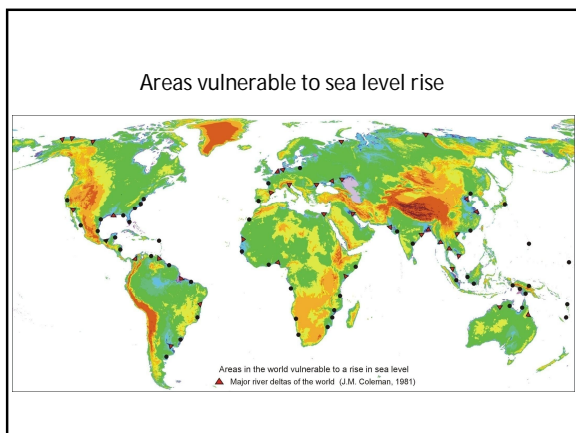
Reasons and drawbacks of using groundwater

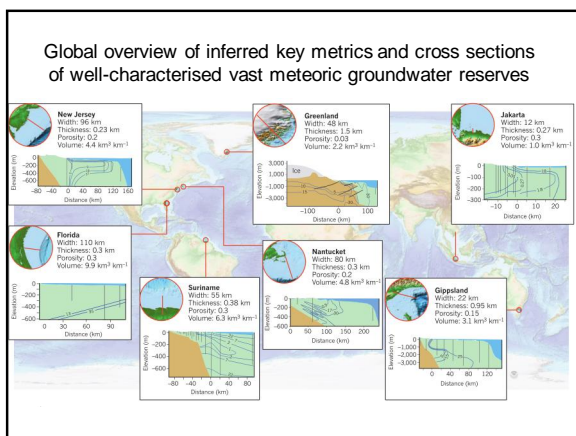
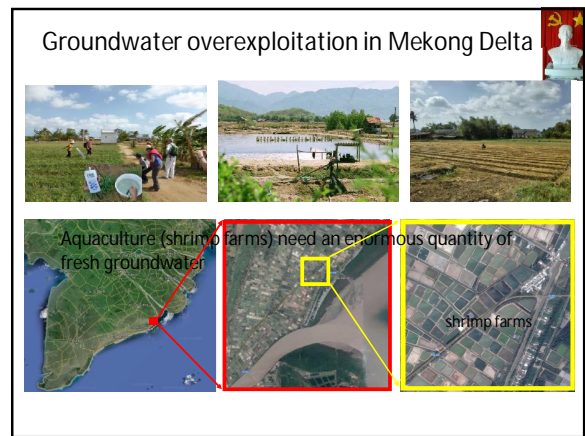
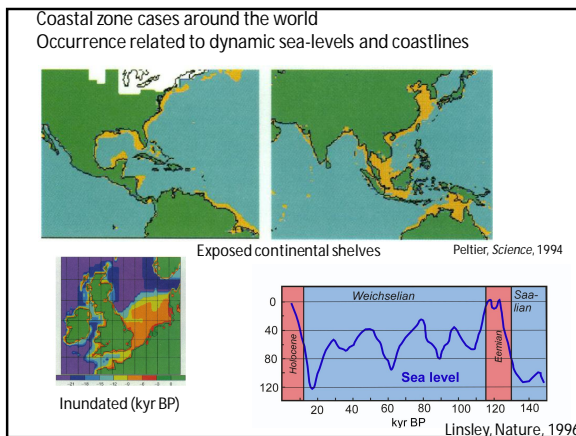
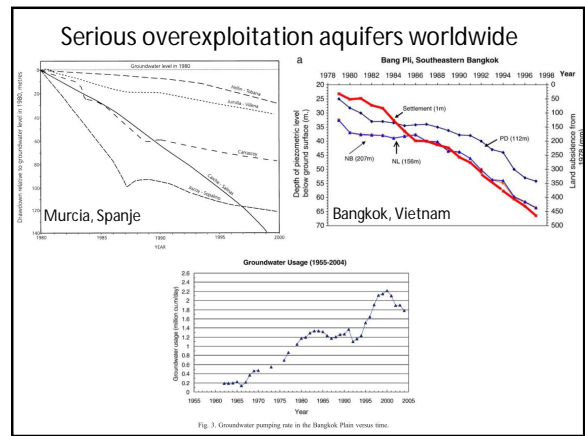
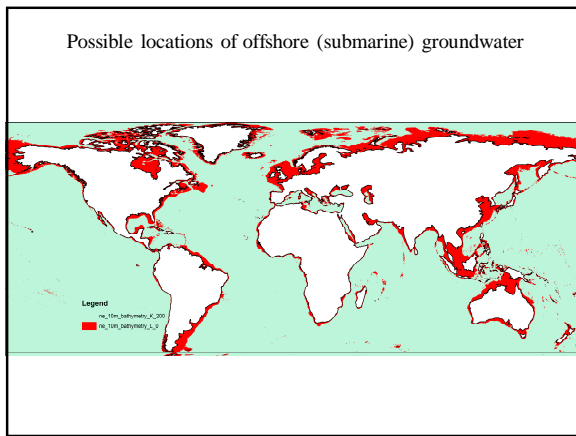
Advantage:

- no seasonal effects
- high quality
- low storage costs
- large quantities
- no spatial limitations

Disadvantage:

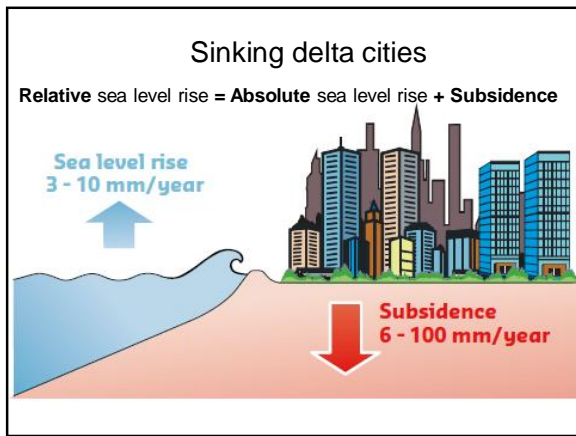
- high extraction costs
- local droughts
- high mineral content
- land subsidence....
- salt water intrusion !





Land subsidence

Megacity	Maximum subsidence [m]	Date commenced
Shanghai	2.80	1921
Tokyo	5.00	1930's
Osaka	2.80	1935
Bangkok	1.60	1950's
Tianjin	2.60	1959
Jakarta	0.90	1978
Manila	0.40	1960
Los Angeles	9.00	1930's

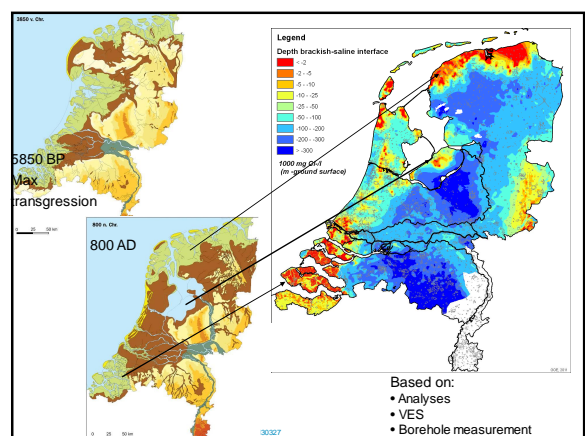
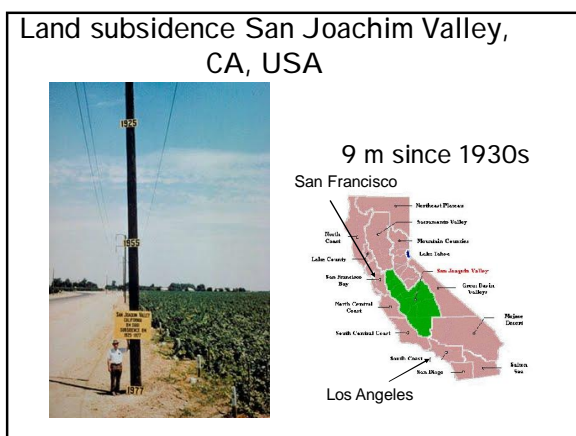
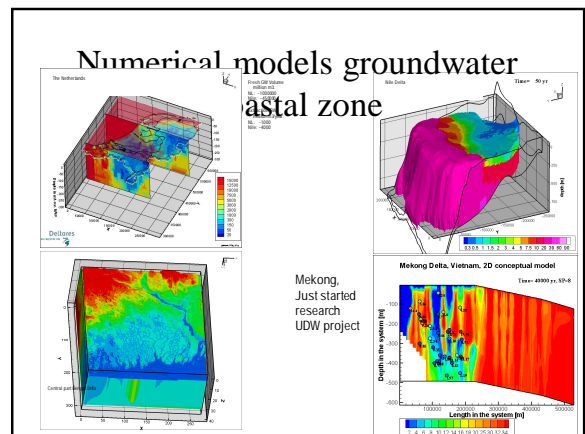
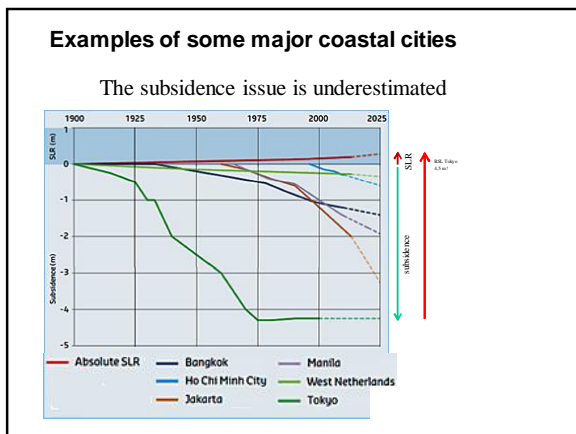


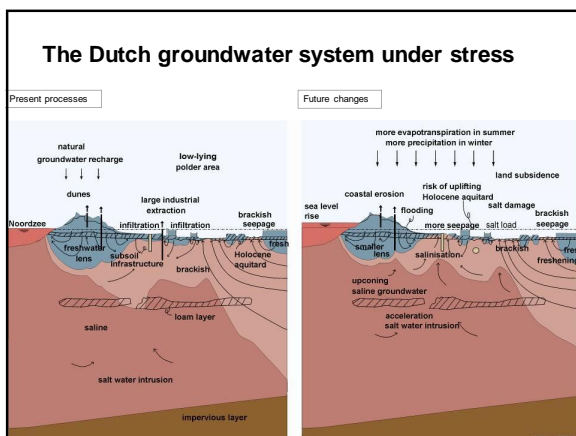
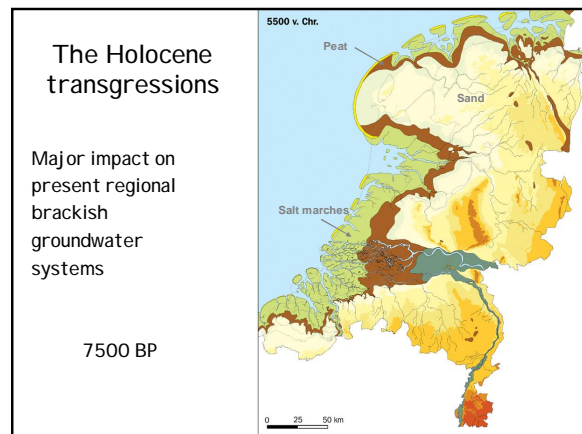
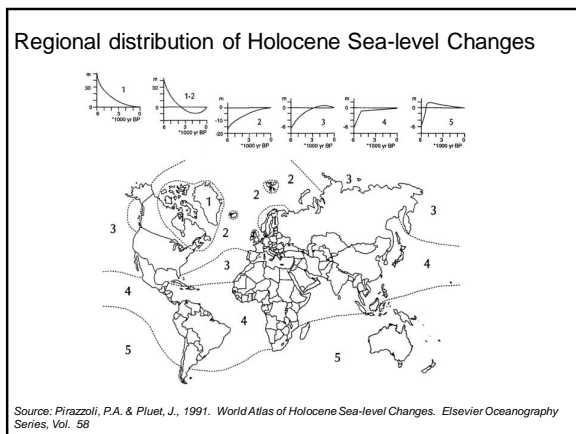
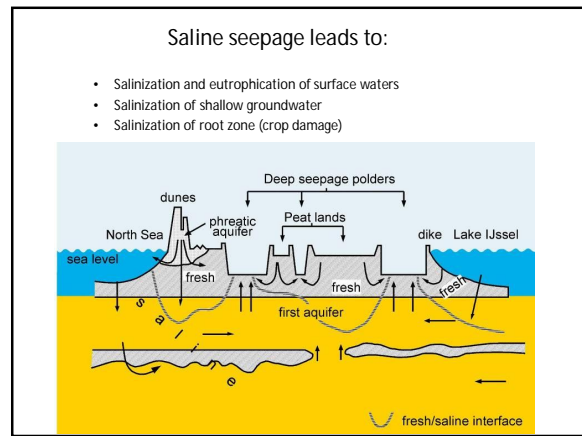
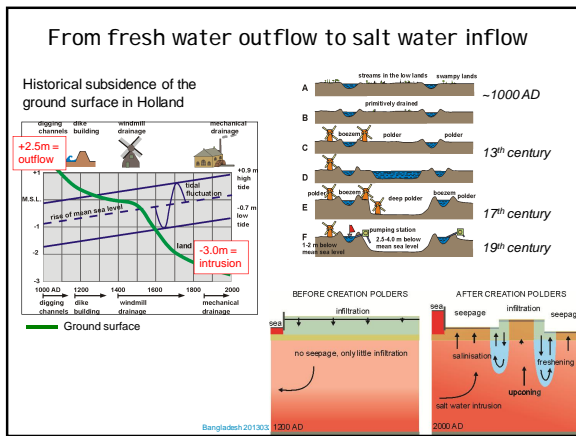
Learn from other areas

Want to get an idea about the effects of climate change in your delta?

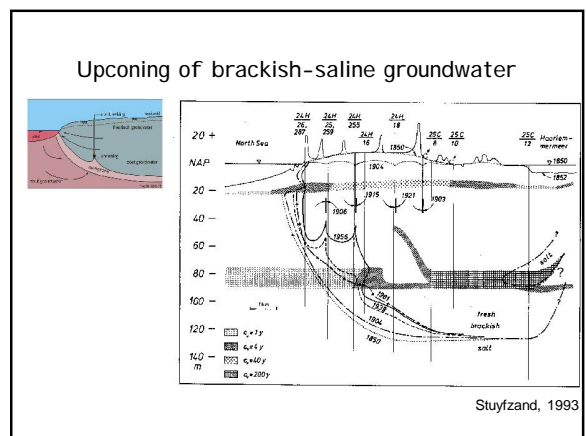
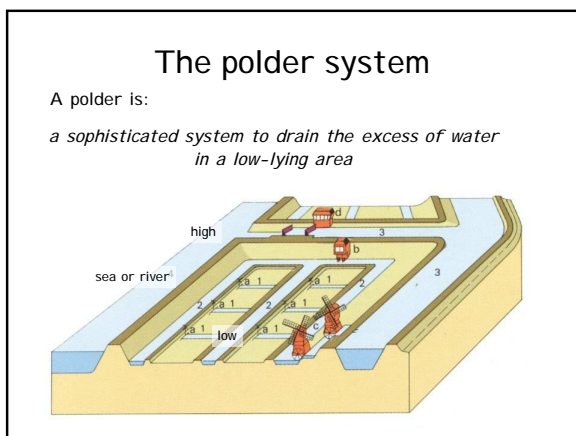
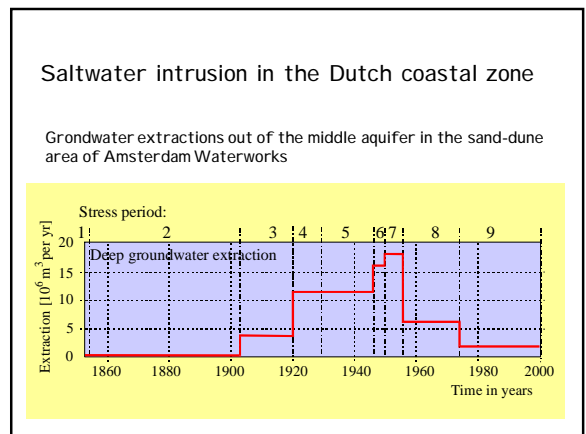
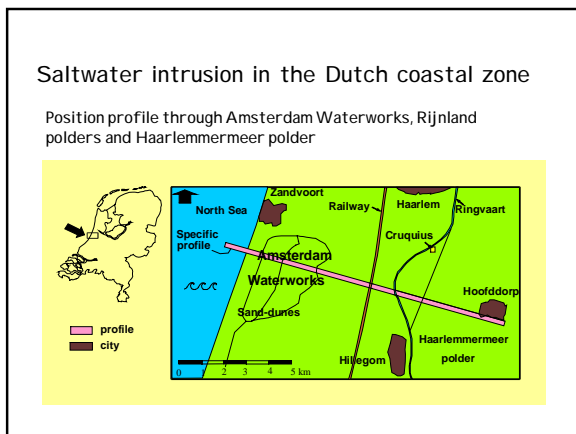
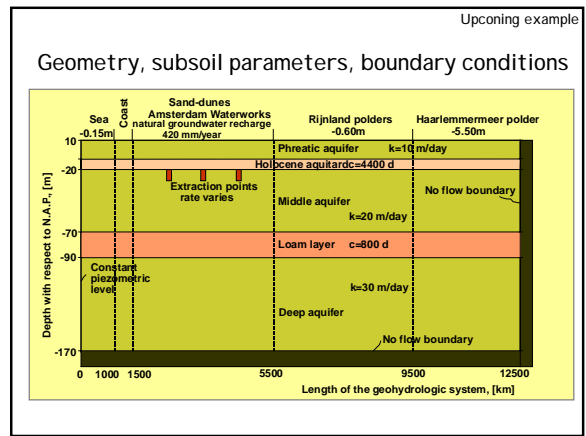
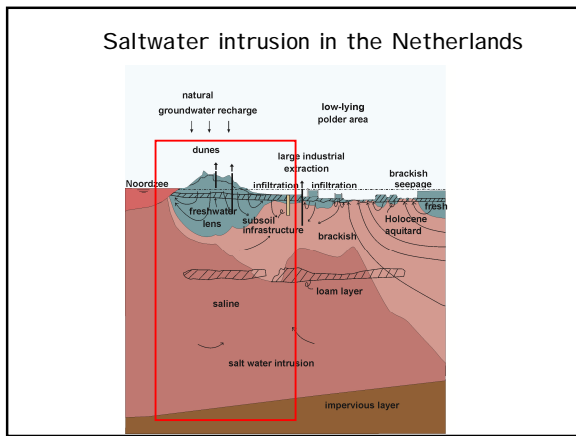
Evaluate past water management in the Dutch delta

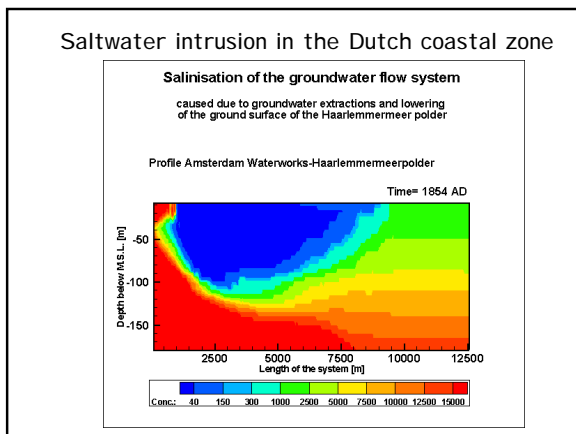
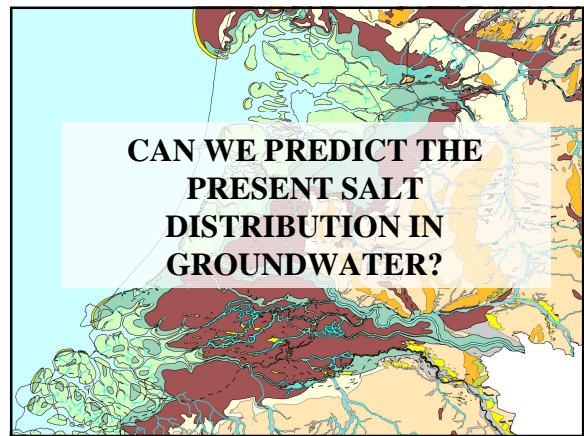
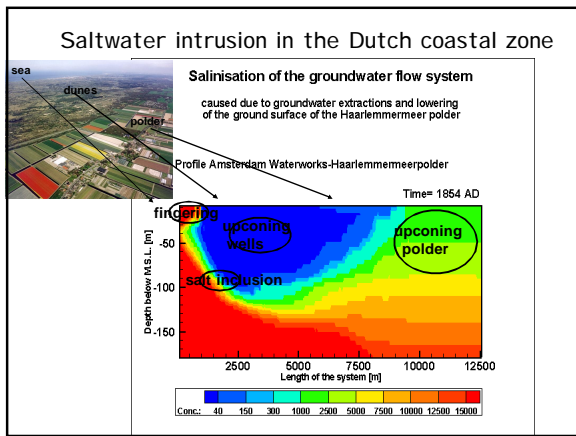
Bangladesh 20130327





My first density dependent groundwater flow and solute transport model in 1990!

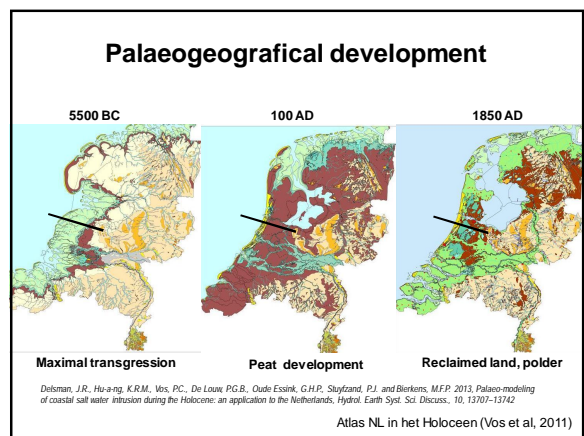




Palaeo hydrogeological modelling

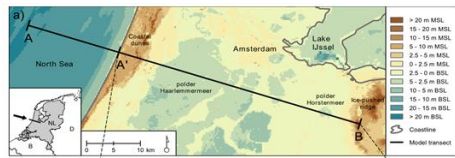
Palaeo-modeling salt water intrusion during the Holocene: an application to the Netherlands

J.R. Delsman, K. Hu-a-ng, P.C. Vos, P.G.B. de Louw, G.H.P. Oude Essink and M.F.P. Bierkens

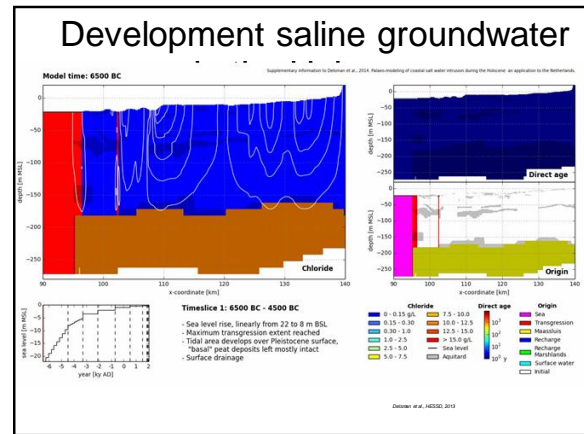
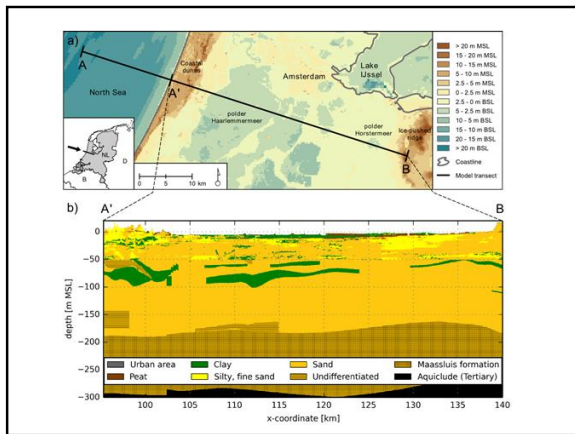
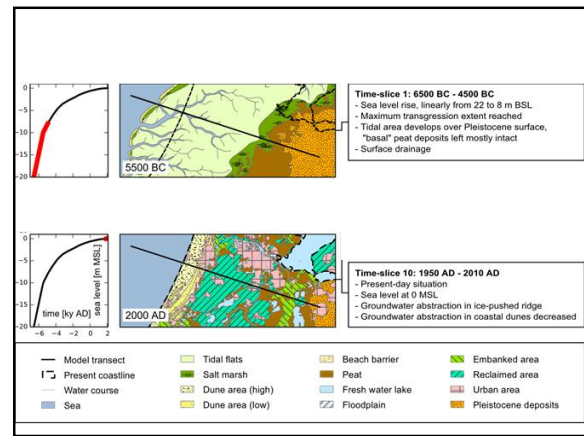


Occurrence of salt under the polder Haarlemmermeer

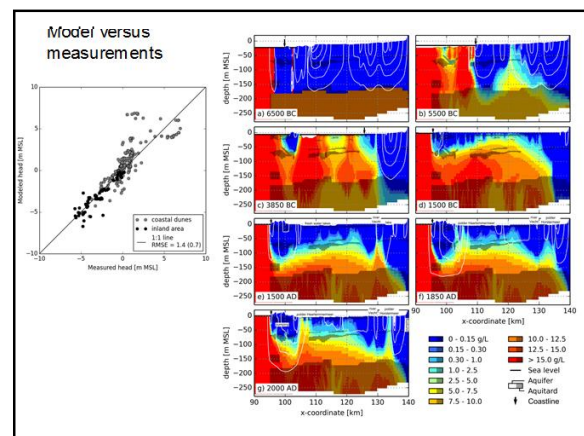
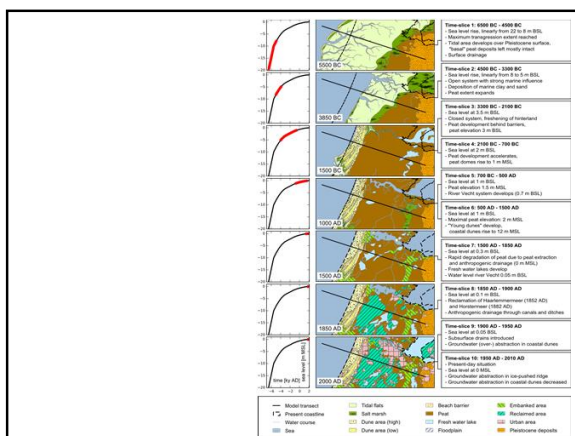
- Model profile Zandvoort - Hoofddorp - Hilversum
- Palaeogeographical development (Vos et al, 2011)
- 6500 BC - 2010 AD
- marine transgression
- Peat development, peat degradation, drainage, reclamation

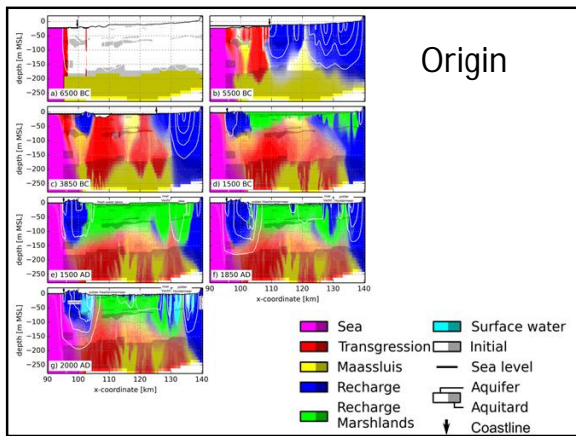


Delsman et al., HESS, 2013



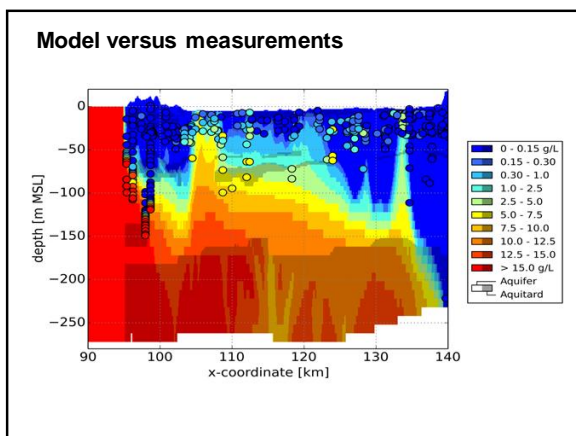
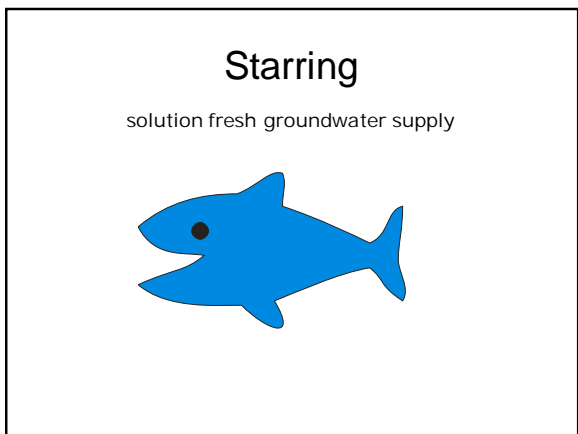
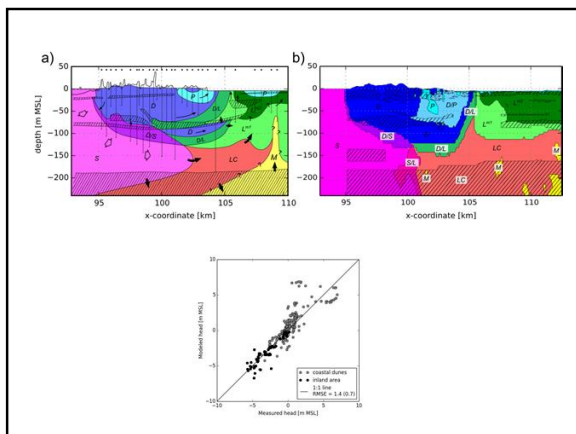
Delsman et al., HESS, 2013





Base idea

Many local solutions for fresh groundwater supply can have regional impact



Starring

Local solution fresh groundwater supply

Starring

climate and global change



What should be the response?

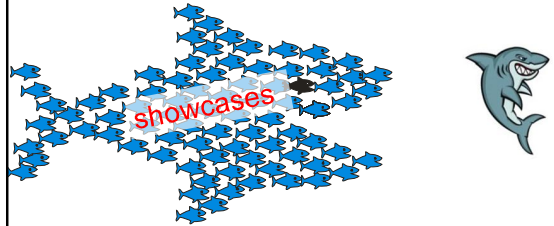
Starring

climate and global change



Many local solutions fresh groundwater supply

climate and global change



Many local solutions for fresh groundwater supply can have regional impact!

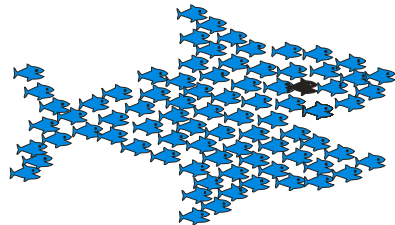
Solutions and responses

Local solution fresh groundwater supply

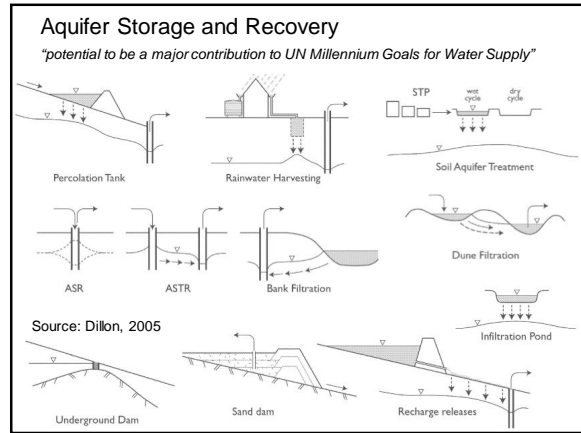
climate and global change



- upscaling local cases to regional strategy
- assess economical feasibility
- increase impact: communicate our showcases
- working together



Compensating measures

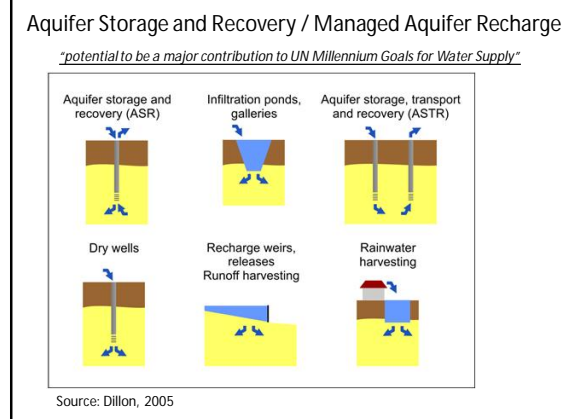


Possible solutions to stop salt water intrusion:

- Restriction of groundwater extractions through permits
- Co-operation between authorities and water users
- Desalination of saline water
- Technical countermeasures of salt water intrusion
 - six examples

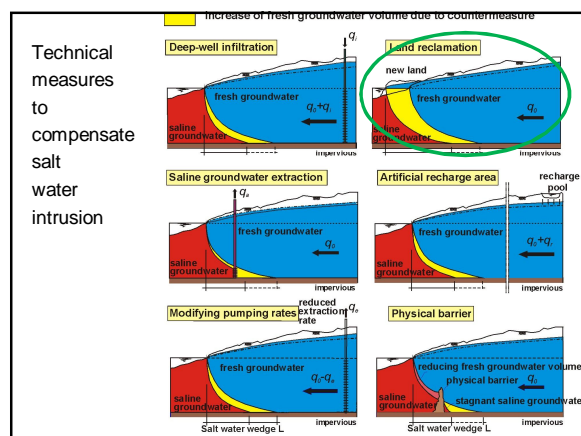
Tools to understand salt water intrusion:

- Monitoring of salinities and piezometric levels
- Numerical modelling of salt water intrusion



Measures to compensate salt water intrusion

- 'The Fresh Holder'
- Extraction of saline/brackish groundwater
- Infiltration of fresh surface water
- Modifying pumping rates
- Land reclamation in front of the coast
- Creating physical barriers (chrySTALLISATION or biosealing)

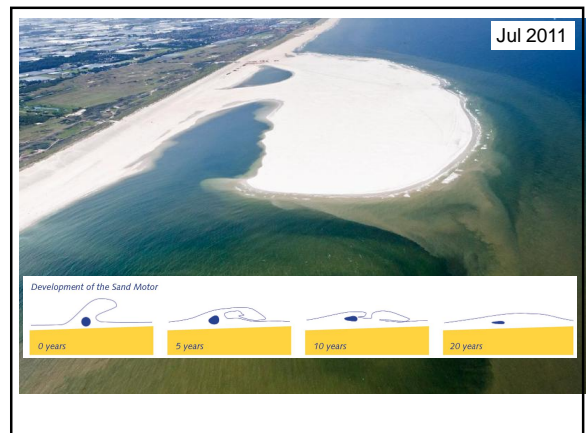
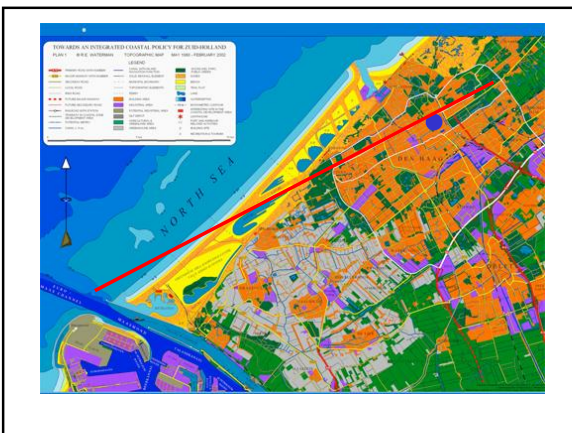
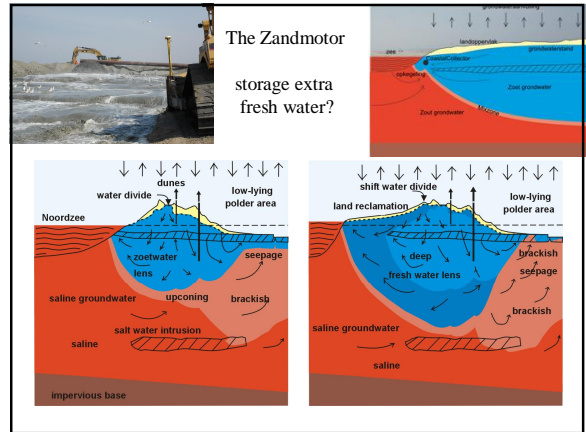
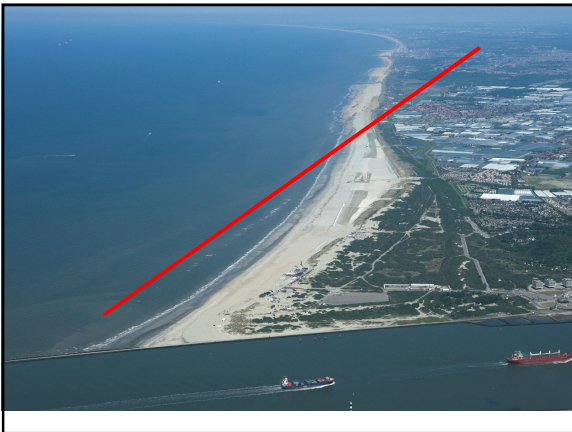


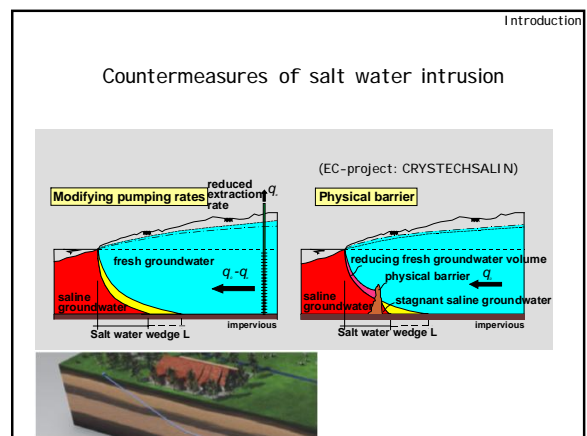
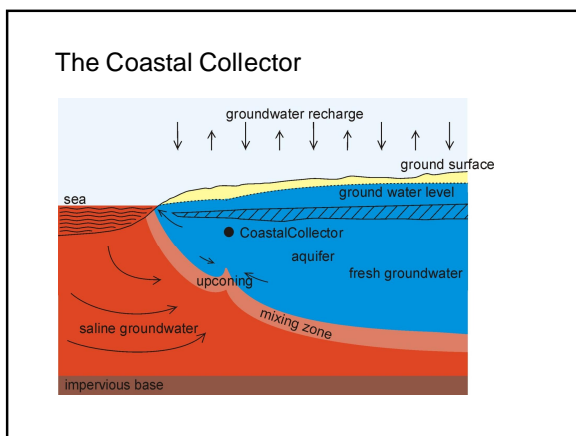
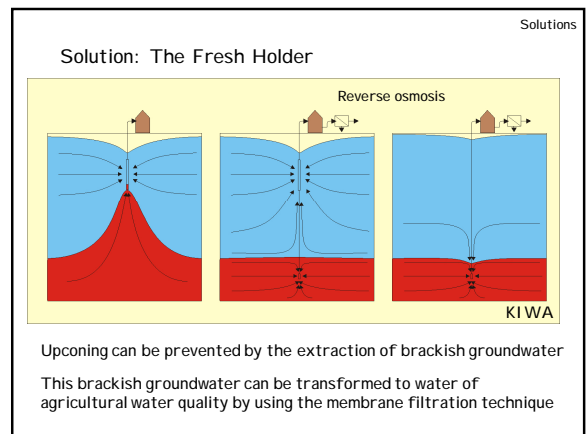
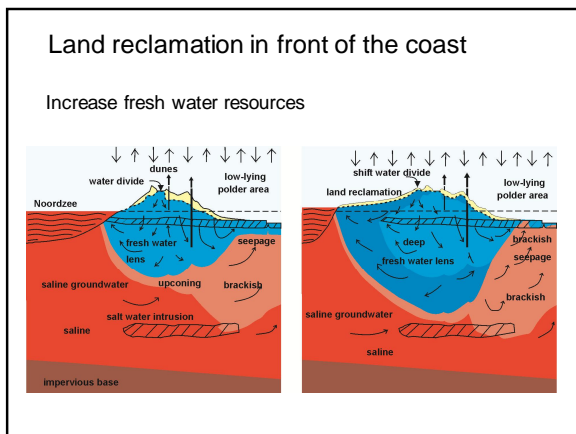
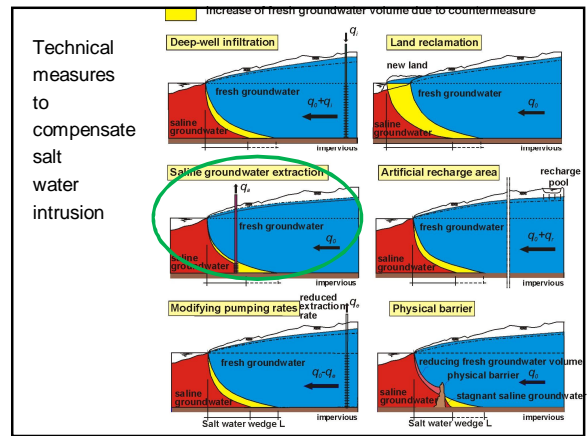
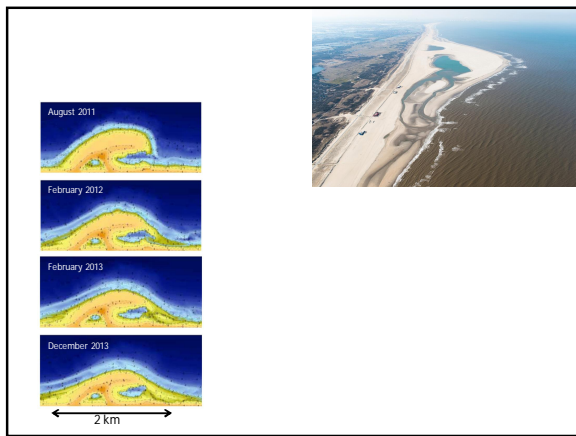
Land reclamation

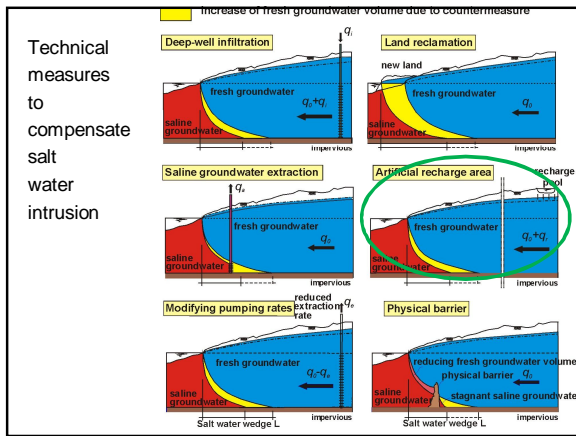
The Zandmotor: effects at the hinterland?



The Zandmotor: effects at the hinterland?







Case study: Water Farm

- 3 km² area
- 8 farms
 - 4 arable farming
 - 2 horticulture
 - 2 fruit
- start case study 2010

Aquifer Storage and Recovery in the coastal zone

www.go-fresh.info

Goal: Increase fresh groundwater resources in saline seepage areas in the southwestern part of the Dutch Delta

Methods: 3 pilot studies: infiltration of fresh water in times of water excess and extraction in times of droughts

Many small local solutions together can be enough for a regional fresh water supply

Creekridge Infiltration Test: Increase fresh water in creek ridge by injection of fresh surface water and extraction of saline groundwater

The Freshmaker: Increase fresh water volume in creek ridge by passive infiltration via drainage

Drains2Buffer: Maintain fresh water volume in shallow rainwater lenses by smart deep controlled drainage

- codesign measures
- communication to outside world

farmers

Researchers: scenario analysis

Lowering of fresh-salt interface due to the raised ditch level scenario

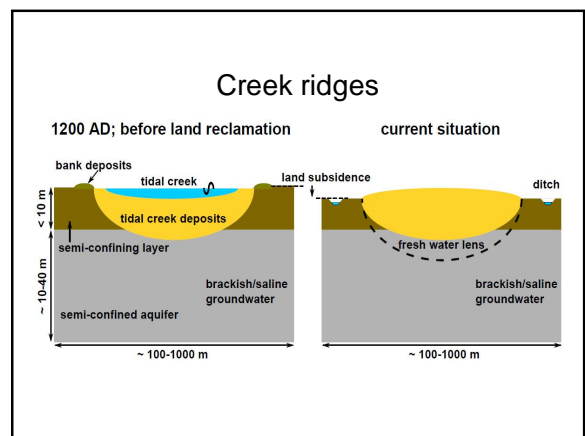
Legend: Lowering of interface (m)

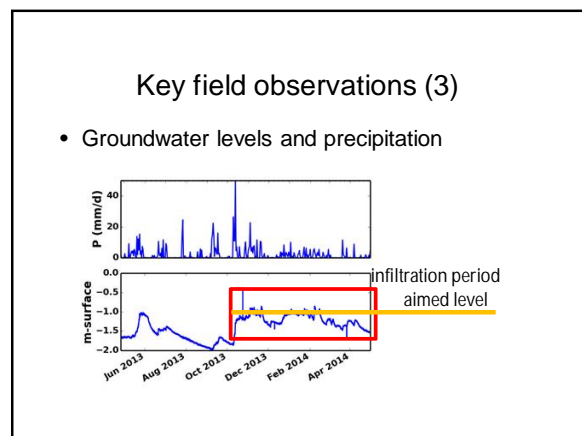
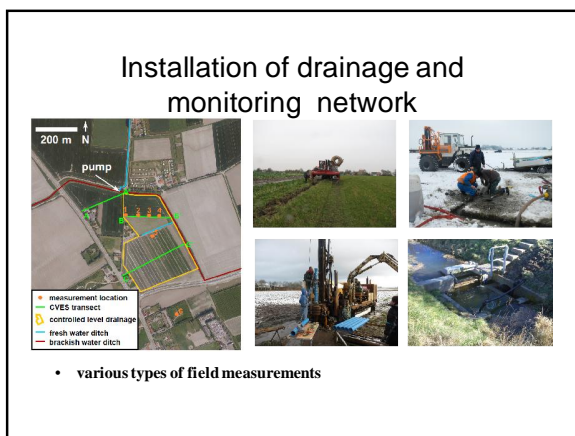
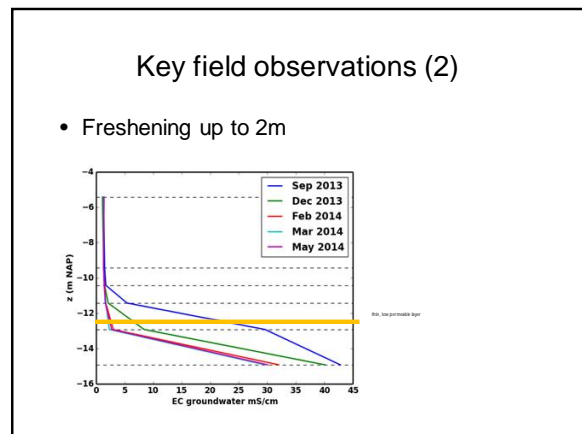
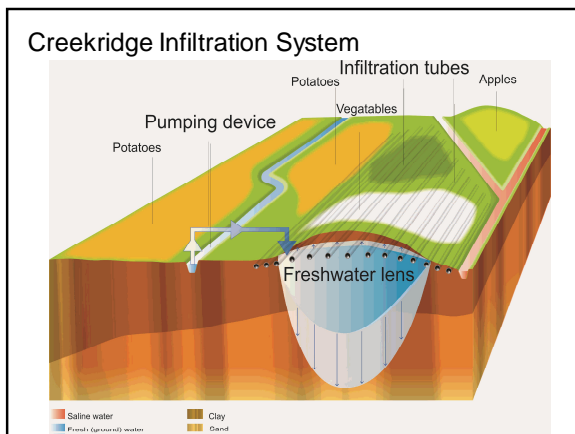
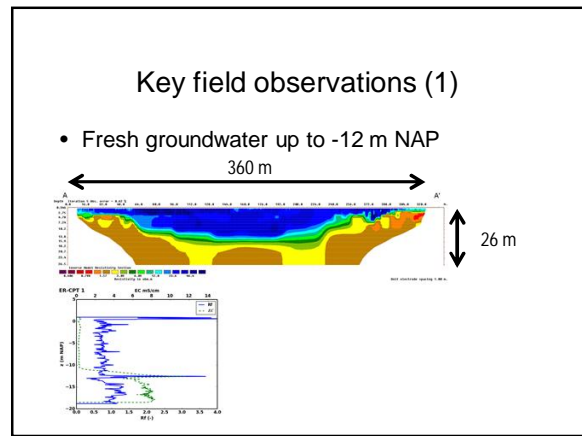
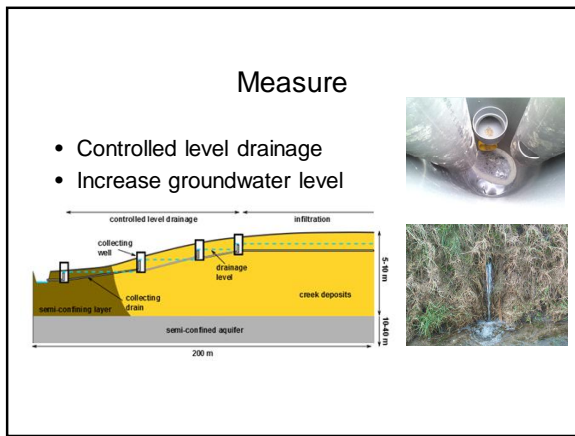
- 0-0.5
- 0.5-1
- 1-2
- 2-3
- 3-4
- 4-6
- 6-9
- 9-15.67

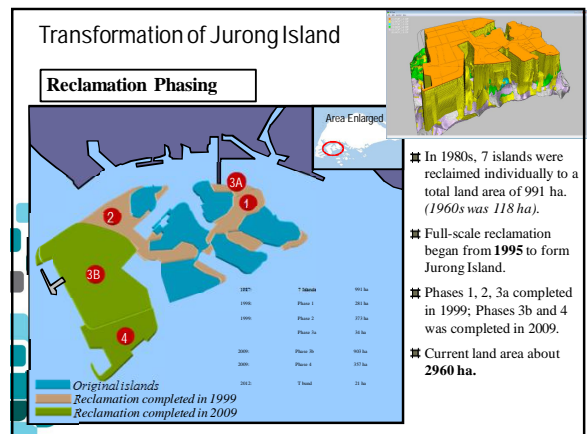
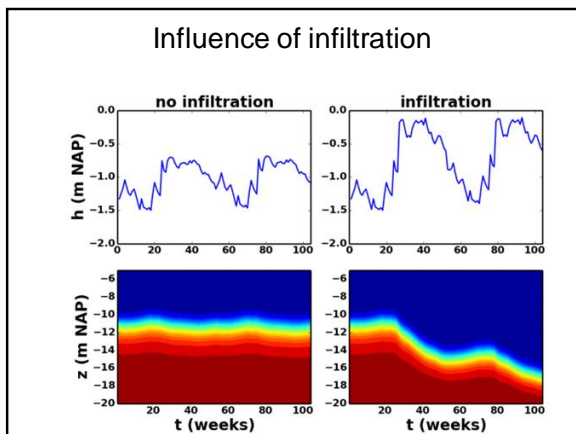
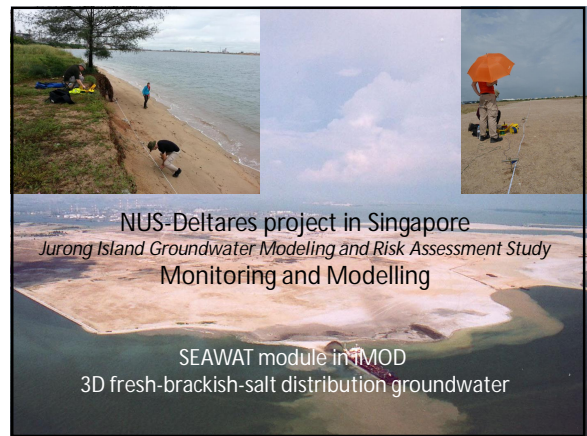
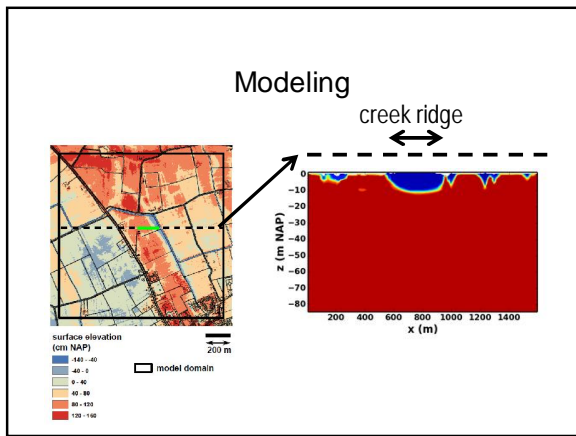
drainage company

Problem statement

- Crop damage southwestern part of the Netherlands
- Fresh groundwater below creek ridges

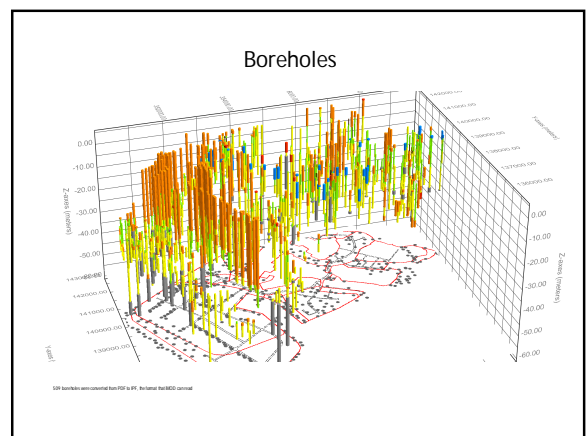


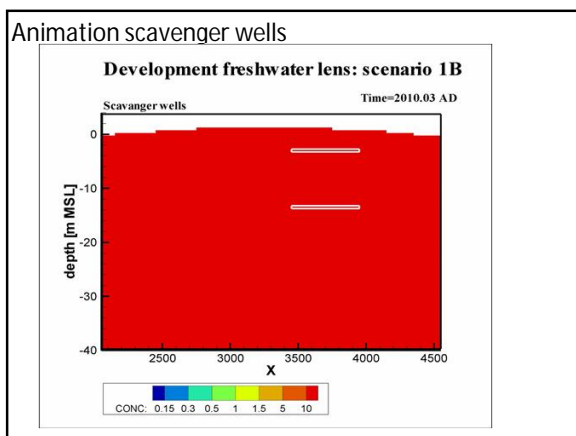
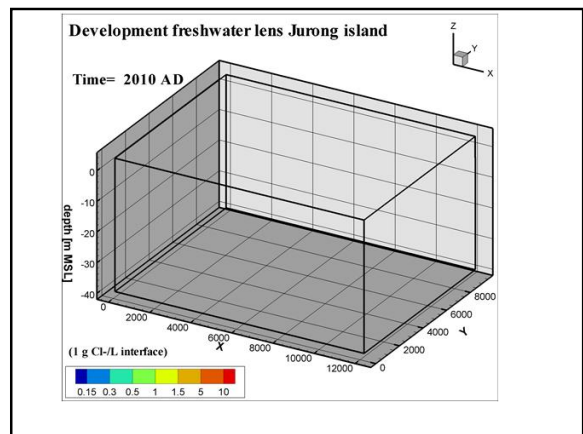
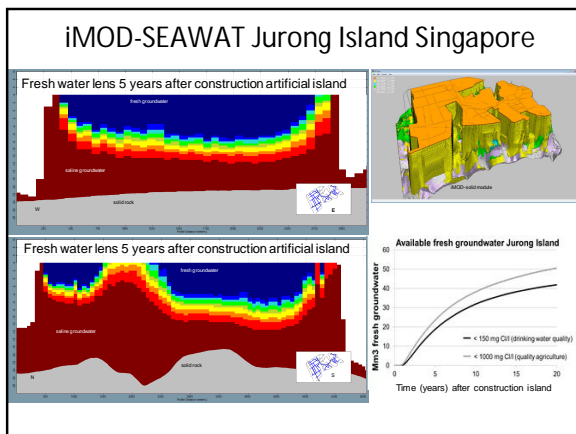
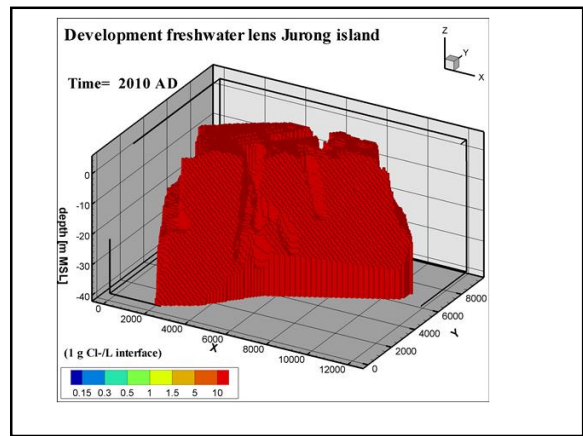
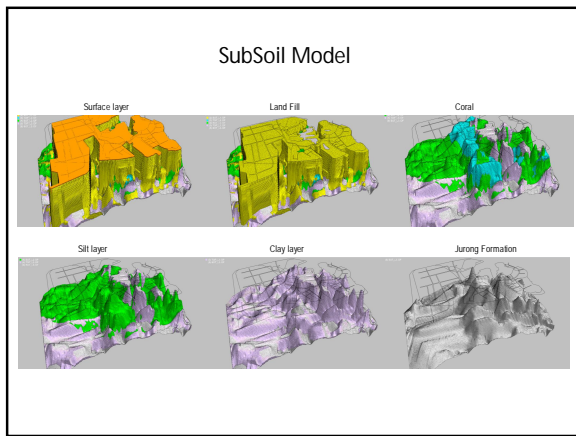




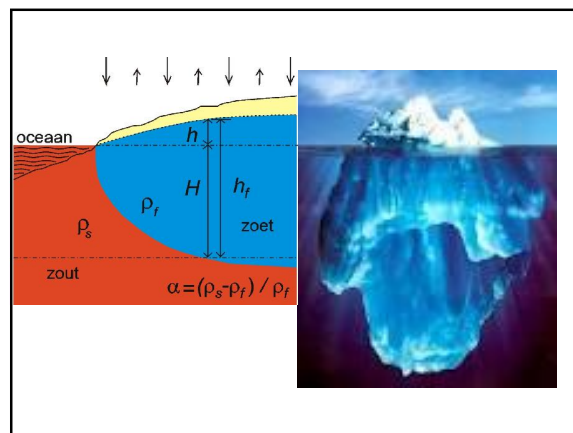
Singapore Jurong Island

Aquifer Storage and Recovery





Sharp interface between fresh and saline groundwater



Introduction

Badon Ghyben-Herzberg principle

Difference between reality and Badon Ghyben-Herzberg approximation

concept: mixing zone in reality

concept: interface between fresh and saline groundwater

pressure saline groundwater = pressure fresh groundwater

$$\rho_s H g = \rho_f (H + h) g$$

$$h = \frac{\rho_s - \rho_f}{\rho_f} H$$

$$h = \alpha H$$

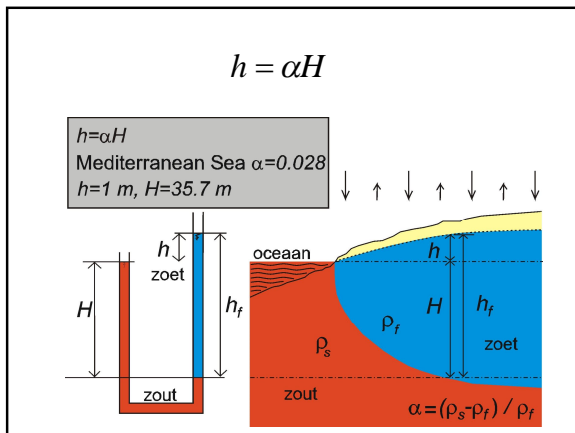
Badon Ghyben-Herzberg principle

The principle suggests an interface between fresh and saline groundwater

Analogy: iceberg & saline ocean and granite tectonic plate & basalt base

$$h = \alpha H$$

$h = \alpha H$
in ocean water $\alpha = 0.025$
 $h = 1 \text{ m}, H = 40 \text{ m}$



Analytical solutions

- ### Badon Ghyben-Herzberg principle
- gives analytical solutions (see later and lectures)
 - educational

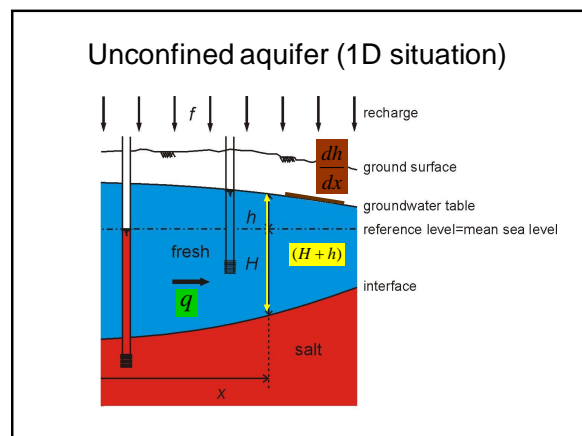
 - interface is a simple approximation
 - dispersion zone < 10m
 - relative simple geometries

Analytical solutions

See lecture notes *Density dependent groundwater flow* (p. 29-48)

<http://public.deltares.nl/display/FRESHSALT/Download>

- ### Badon Ghyben-Herzberg principle
- What is the case then $h \neq \alpha H$?
1. still dynamic situation
 2. occurrence resistance layer
 3. natural groundwater recharge not constant
 4. relative density difference α is not ok
 5. occurrence shallow bedrock
 6. groundwater extractions



Unconfined aquifer (1D situation)

(I) Darcy $q = -k(H+h) \frac{dh}{dx}$

(II) Continuity $dq = f dx$

(III) BGH $h = \alpha H$

Unconfined aquifer (1D situation)

$$H = \sqrt{\frac{-fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}}$$

$$h = \alpha H$$

$$q = fx + C1$$

Unconfined aquifer (1D situation)

$dq = f dx$ integration gives $q = fx + C1$

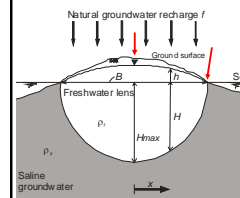
$$-k(H+h) \frac{dh}{dx} = fx + C1$$

$h = \alpha H \rightarrow -k(H+\alpha H)\alpha \frac{dH}{dx} = fx + C1$

$$H dH = -\frac{fx + C1}{k\alpha(1+\alpha)} dx$$

Example 1: Elongated island

$$H = \sqrt{\frac{-fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}} \quad q = fx + C1$$



Boundary conditions

$x = 0 : q = 0 \rightarrow C1 = 0$

$x = 0.5B : H = 0 \rightarrow C2 = fB^2 / 8$

Unconfined aquifer (1D situation)

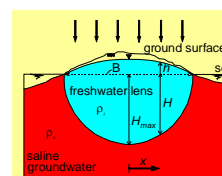
$$H dH = -\frac{fx + C1}{k\alpha(1+\alpha)} dx$$

integration gives

$$\frac{1}{2} H^2 = \frac{-\frac{1}{2} fx^2 - C1x + C2}{k\alpha(1+\alpha)}$$

$$H = \sqrt{\frac{-fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}}$$

Example of analytical solutions (I)



Depth of fresh-saline interface H

$$H = \sqrt{\frac{f(0.25B^2 - x^2)}{k\alpha(1+\alpha)}}$$

$$h = \alpha H$$

Maximal thickness lens

$$H_{\max} = \frac{1}{2} B \sqrt{\frac{f}{k\alpha(1+\alpha)}}$$

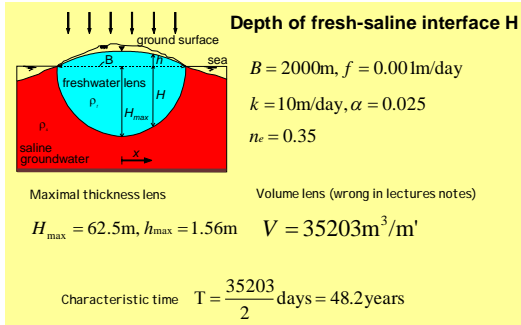
Volume lens

$$V = \frac{1}{4} \pi (1+\alpha) H_{\max} B n_e$$

$$\text{Characteristic time } T = \frac{\text{volume of water in lens}}{\text{inflow of water}} = \frac{\pi n_e B}{8} \sqrt{\frac{(1+\alpha)}{k f \alpha}}$$

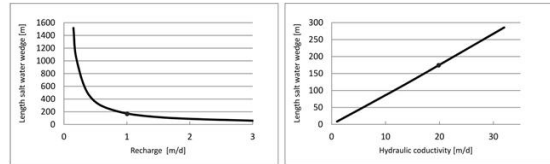
Lecture notes p. 32

Example of analytical solutions (I)



Lecture notes p. 32

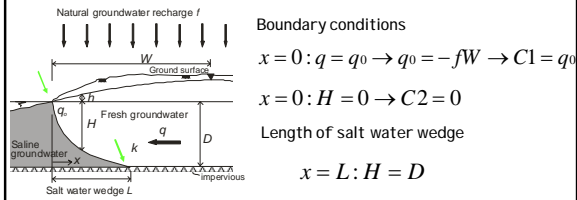
Length of the salt water wedge as a function of a. recharge and b. hydraulic conductivity



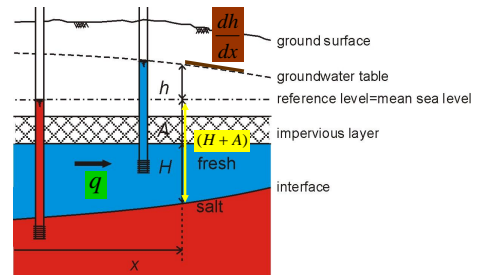
the dots resample with the example mentioned above

Example 2: salt water wedge

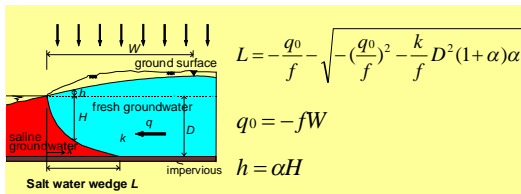
$$H = \sqrt{\frac{-fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}} \quad q = fx + C1$$



Confined aquifer (1D situation)



Example of analytical solutions (II)



Lecture notes p. 33

Confined aquifer (1D situation)

- (I) Darcy $q = -kH \frac{dh}{dx}$
- (II) Continuity $q = q_0$
- (III) BGH $h = \alpha(H + A)$

Confined aquifer (1D situation)

$$-kH \frac{dh}{dx} = q_0$$

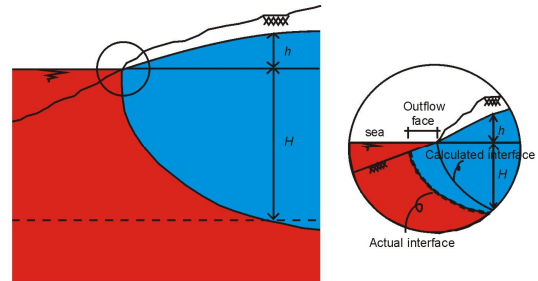
$$HdH = -\frac{q_0}{k\alpha} dx$$

integration gives

$$\frac{1}{2}H^2 = \frac{q_0x}{k\alpha} + C$$

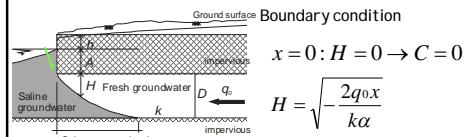
$$H = \sqrt{-\frac{2q_0x}{k\alpha} + 2C}$$

Outflow face (Submarine Groundwater Discharge)



Example 3: salt water wedge confined aquifer

$$H = \sqrt{-\frac{2q_0x}{k\alpha} + 2C}$$



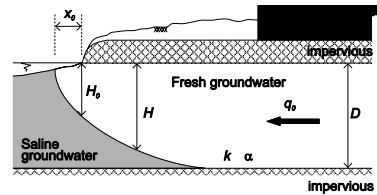
Boundary condition $x=0: H=0 \rightarrow C=0$

$$H = \sqrt{\frac{2q_0x}{k\alpha}}$$

Length of salt water wedge $x=L: H=D$

$$L = -\frac{kD^2\alpha}{2q_0}$$

Outflow face (Submarine Groundwater Discharge)

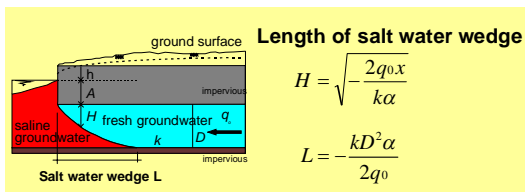


$$x_0 = \frac{q_0}{2k\alpha} \quad H_0 = \frac{q_0}{k\alpha} \quad \text{Glover (1959)}$$

Example: $x_0 = f \cdot L / (2ka) = 0.001\text{m}/\text{d} \cdot 20000\text{m} / (2 \cdot 20 \cdot 0.025) = 20\text{m}$ (only!)

Note: no resistance layer of offshore

Example of analytical solutions (III)



Length of salt water wedge

$$H = \sqrt{\frac{2q_0x}{k\alpha}}$$

$$L = -\frac{kD^2\alpha}{2q_0}$$

Example:

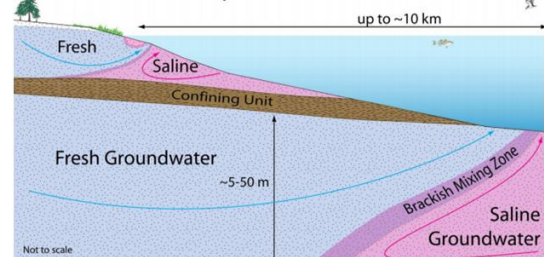
$W = 2000\text{m}, f = 0.001\text{m}/\text{day}, \alpha = 0.025, k = 25\text{m}/\text{day}, D = 40\text{m}$

$L = 250\text{m}$

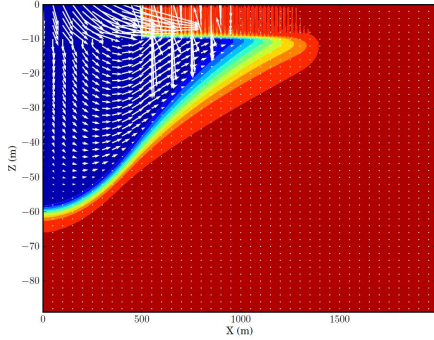
Lecture notes p. 35-36

Outflow face (Submarine Groundwater Discharge)

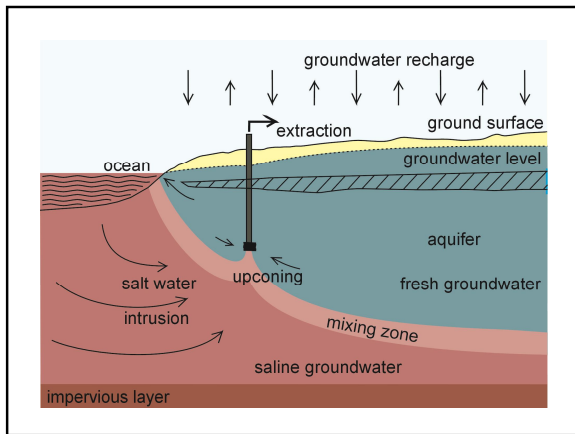
Embayment Scale



Outflow face (Submarine Groundwater Discharge)

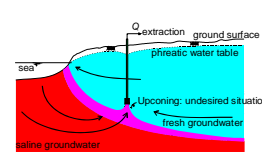


Upconing processes

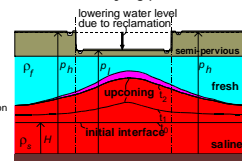


Upconing of saline groundwater

Under an extraction well



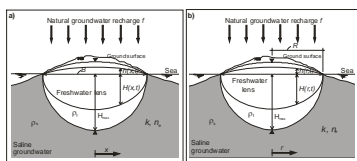
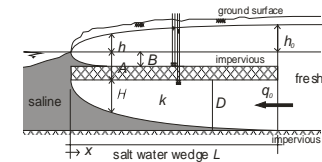
Under a low-lying polder area



- movement of saline groundwater to extraction wells
- increase in salinity (>150-200 mg Cl-/l)
- lowering of the piezometric head (leads to land subsidence: e.g. Los Angeles: 9 m in the 1930's)

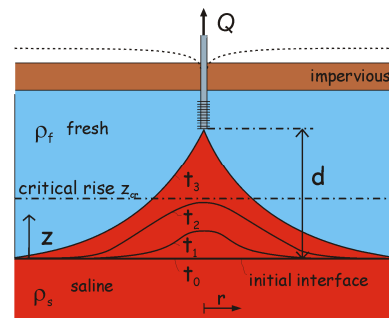
'Solutions': reduce extraction rate, abandon well, inundate polder

See the lectures for more cases



Examples of analytical solutions (IV)

Upconing of saline groundwater under an extraction well



Lecture notes p. 44

Examples of analytical solutions (IV)

Upconing of saline groundwater under an extraction well

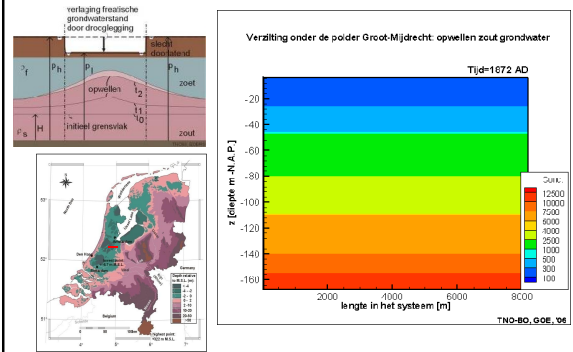
$$z(r, t) = \frac{Q}{2\pi\alpha k_x d} \left[\frac{1}{(1 + R^2)^{1/2}} - \frac{1}{[(1 + \gamma')^2 + R^2]^{1/2}} \right]$$

$$R' = \frac{r k_z}{d k_x} \quad \gamma' = \frac{\alpha k_z}{2n_e d} t$$

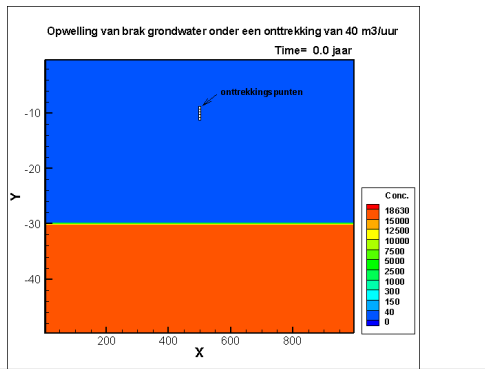
Dagan & Bear, 1968, J. Hydraul. Res 6, 1563-1573

Lecture notes p. 44

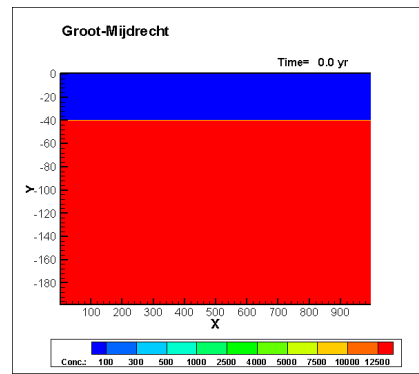
Upconing under a low-lying polder (Groot-Mijdrecht)



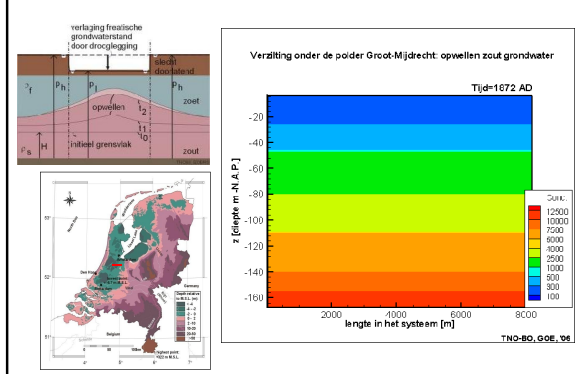
Upconing of salt under an extraction



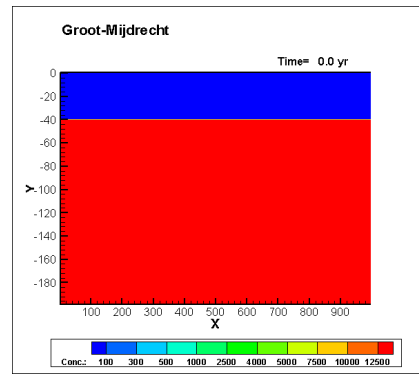
Upconing under a low-lying polder (Groot-Mijdrecht)

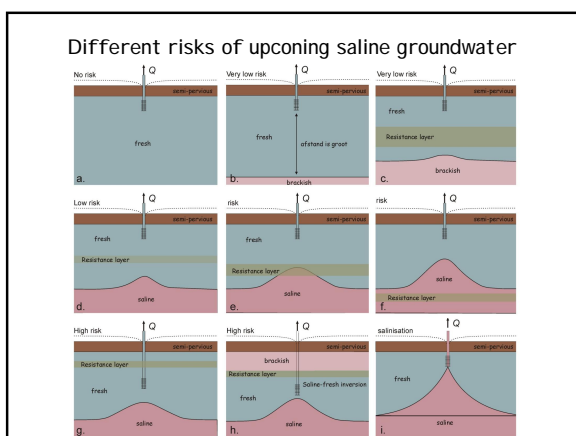
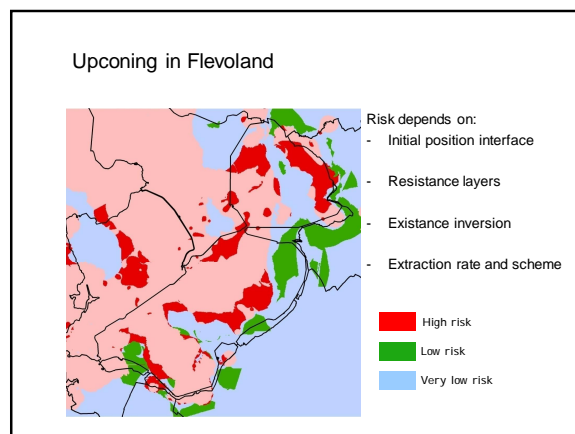
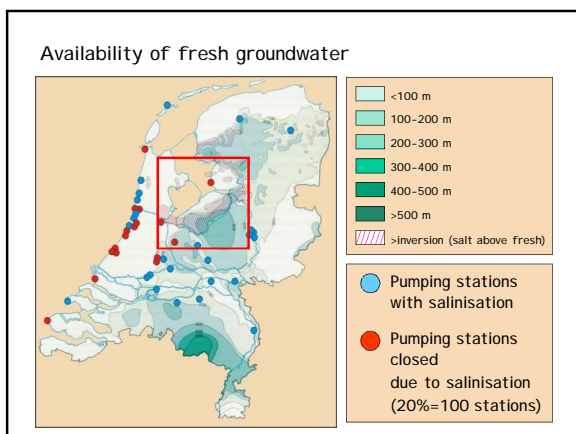
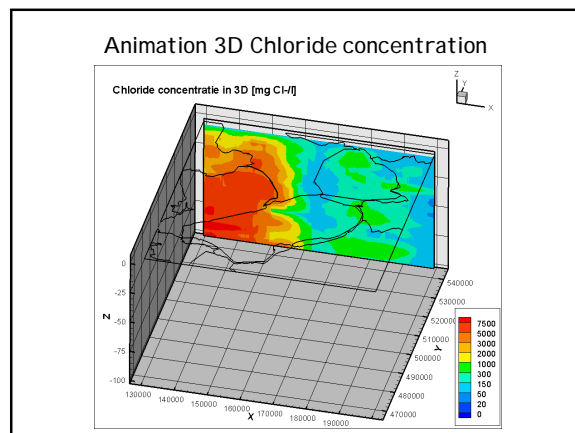
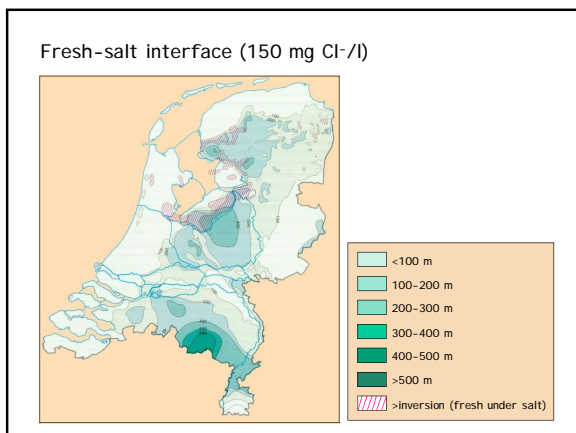


Upconing under a low-lying polder (Groot-Mijdrecht)



Upconing under a low-lying polder (Groot-Mijdrecht)





Modelling

salt water intrusion
density dependent groundwater flow

modelling

Why mathematical modelling anyway?

A model is only a schematisation of the reality!

modelling

Solute transport models

Combine
the groundwater flow equation
and
the advection-dispersion equation
by means of
an equation of state

modelling

Why mathematical modelling anyway?

+:

- cheaper than scale models
- analysis of very complex systems is possible
- a model can be used as a database
- to increase knowledge about a system (water balances)

-:

- simplification of the reality
- only a tool, no purpose on itself
- garbage in=garbage out: (field)data important
- perfect fit measurement and simulation is suspicious

modelling

Solute transport equation

Partial differential equation (PDE):

$$R_d \frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (C V_i) + \frac{(C - C^*) W}{n_e} - R_d \lambda C$$

change in concentration dispersion diffusion advection source/sink decay

D_{ij} =hydrodynamic dispersion [$L^2 T^{-1}$]
 R_d =retardation factor [-]
 λ =decay-term [T^{-1}]

modelling

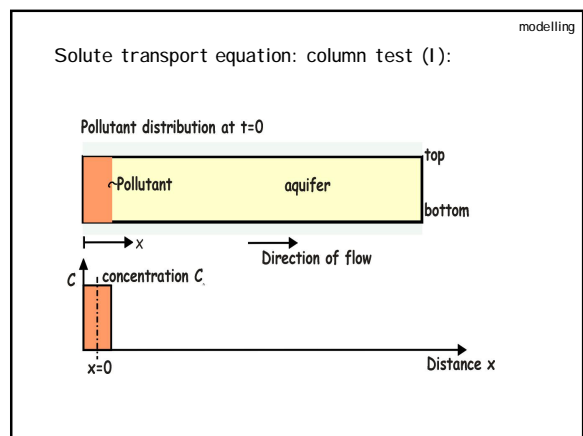
Numerical modelling variable density flow

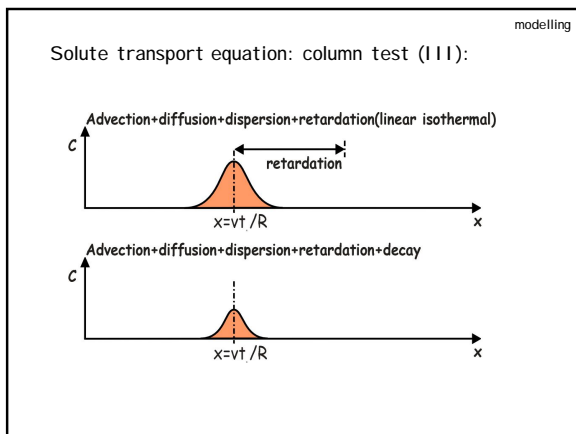
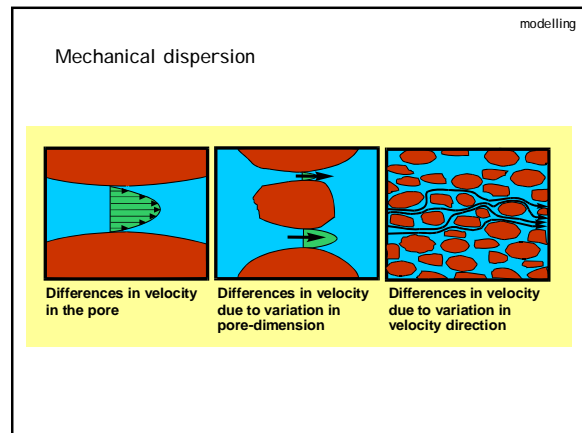
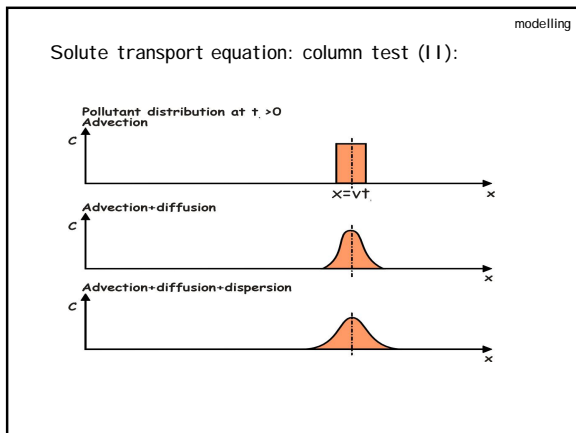
Type:

- sharp interface models
- solute transport models

State of the art:

- three-dimensional
- solute transport
- transient





modelling

Solute transport equation: diffusion (I)

diffusion is a slow process: diffusion equation

only 1D-diffusion means: $R_r=1, V_r=0, \lambda=0$ and $W=0$

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$$

similarity with non-steady state groundwater flow equation

$$S \frac{\partial \phi}{\partial t} = T \frac{\partial^2 \phi}{\partial x^2} + N \quad \frac{T \Delta t}{S \Delta x^2} < 0.5$$

$$\phi_i^{t+\Delta t} = \phi_i^t + \frac{N \Delta t}{S} + \frac{T \Delta t}{S \Delta x^2} (\phi_{i+1}^t - 2\phi_i^t + \phi_{i-1}^t)$$

$$C_i^{t+\Delta t} = C_i^t + \frac{D \Delta t}{\Delta z^2} (C_{i+1}^t - 2C_i^t + C_{i-1}^t) \quad \frac{D \Delta t}{\Delta z^2} < 0.5$$

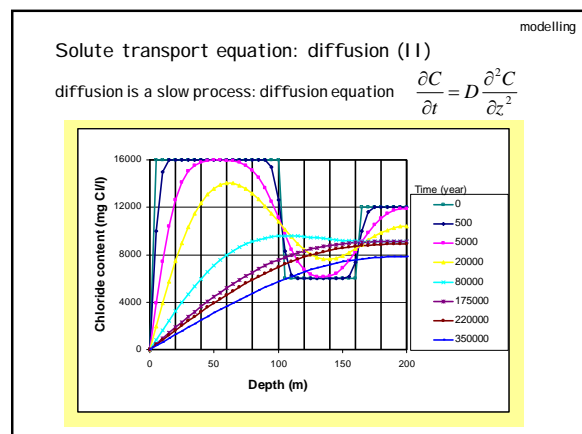
modelling

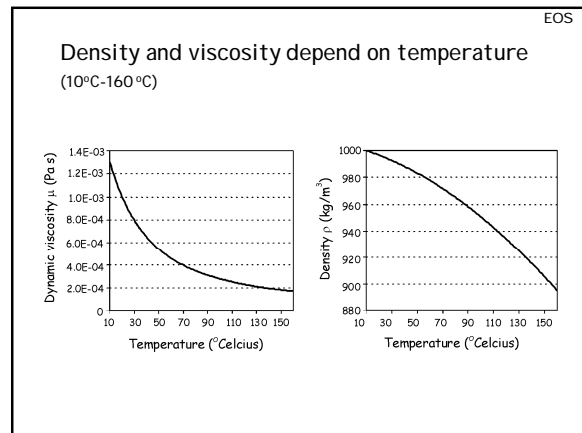
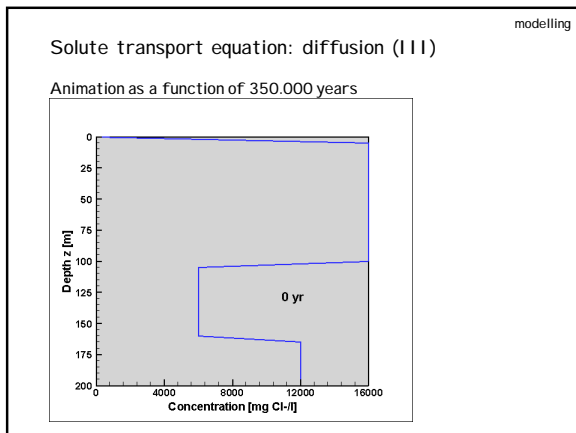
Hydrodynamic dispersion

hydrodynamic dispersion
=
mechanical dispersion+ diffusion

mechanical dispersion:
tensor
velocity dependant

diffusion:
molecular process
solutes spread due to concentration differences





MOCDENS3D

Groundwater flow equation (MODFLOW, 1988)

Darcy
 $q_x = -\frac{\kappa_x \rho_f g}{\mu} \frac{\partial \phi_f}{\partial x}; q_y = -\frac{\kappa_y \rho_f g}{\mu} \frac{\partial \phi_f}{\partial y}; q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$

Continuity
 $-\left[\frac{\partial \rho q_x}{\partial x} + \frac{\partial \rho q_y}{\partial y} + \frac{\partial \rho q_z}{\partial z} \right] - \frac{\partial n p}{\partial t} + W$

Freshwater head
 $\phi_f = \frac{p}{\rho_f g} + z$

↑
buoyancy term

Advection-dispersion equation (MOC3D, 1996)

$$\frac{\partial C}{\partial t} = \frac{1}{nK_f} \frac{\partial}{\partial x_i} \left(nD_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{V_i}{K_f} \frac{\partial C}{\partial x_i} + \frac{\sum [W(C'-C)]}{nK_f} - \lambda C$$

Equation of state: relation density & concentration

$$\rho_{i,j,k} = \rho_f (1 + \beta C_{i,j,k})$$

EOS

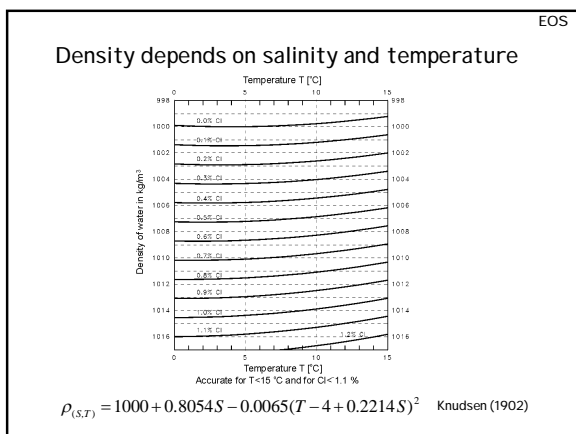
Examples of equations of state

Knudsen (1902)
 $\rho_{(S,T)} = 1000 + 0.8054S - 0.0065(T - 4 + 0.2214S)^2$
T < 15 °C, S < 20 ppt

Linear (concentration)
 $\rho_{(C)} = \rho_f \left[1 + \alpha \frac{C_i}{C_s} \right]$ where α = relative density difference

Linear (temperature)
 $\rho_{(T)} = \rho_f [1 - \beta(T - T^*)]$

Exponential (temperature, pressure, salt)
 $\rho_{(T,p,w)} = \rho_f e^{-\alpha(T-T_0) + \beta(p-p_0) + \gamma w}$

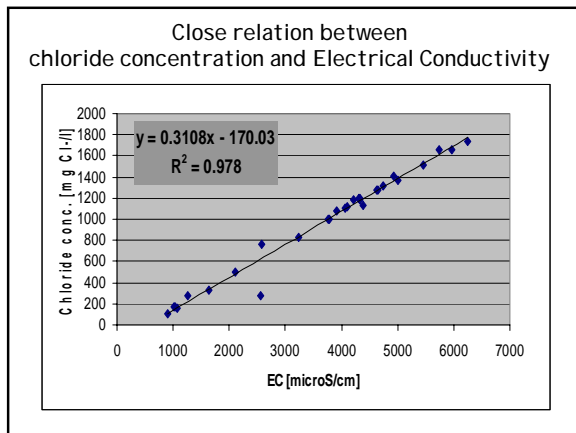


Equation of state (SEAWAT)

$$\rho_{i,j,k} = \rho_f + \frac{\partial \rho}{\partial C} C_{i,j,k}$$

e.g.:

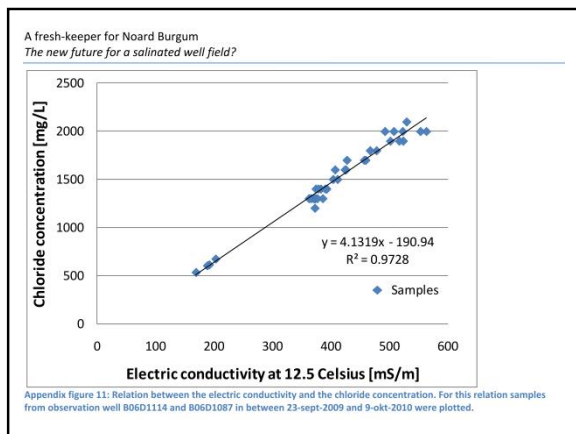
- conc = 35 TDS g/l: DRHODC = 0.7143
- conc = 19000 mg Cl-/l: DRHODC = 0.001316 (as 1025 = 1000 + 0.001316 * 19000)



modelling

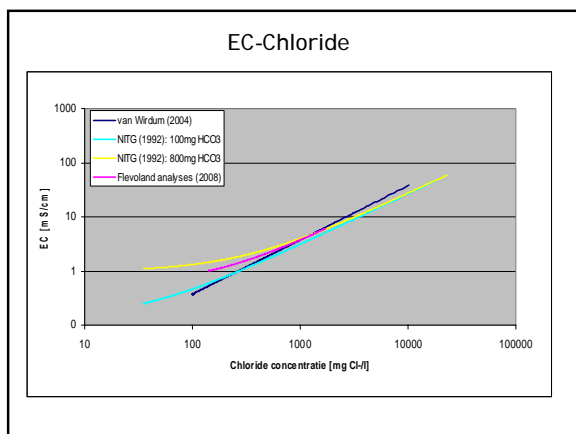
Some existing 3D codes which simulate variable density groundwater flow in porous media:

SEAWAT (Guo & Bennett, '98)	SWICHA (Huyakorn et al., '87)
METROPOL (Sauter, '87)	SWIFT (Ward, '91)
FEFLOW (Diersch, '94)	FAST-C 3D (Holzbecher, '98)
MVAEM (Strack, '95)	MODFLOW+MT3D96 (Gervin, '98)
D3F (Wittum et al., '98)	HST3D (Kipp, '86)
MOCDENS3D (Oude Essink, '98)	SUTRA (beta-version, Voss, '02)



Restrictions 3D salt water intrusion modelling in 2015

- the data problem:
 - not enough hydrogeological data available
 - e.g. the initial density distribution
 - especially important issue in data-poor countries
- the computer problem:
 - modelling transient 3D systems: computer only good enough at high costs
- the numerical dispersion problem:
 - numerical dispersion is large in case of coarse grid



Restrictions 3D salt water intrusion modelling in 2015

- the data problem:
 - not enough hydrogeological data available
 - e.g. the initial density distribution
 - especially important issue in data-poor countries
- the computer problem:
 - modelling transient 3D systems: computer only good enough at high costs
- the numerical dispersion problem:
 - numerical dispersion is large in case of coarse grid

solution is better software
 solution is 64 bits computer

MOCDENS3D

MOCDENS3D is based on MODFLOW

a modular 3D finite-difference ground-water flow model

(M.G. McDonald & A.W. Harbaugh, from 1983 on)

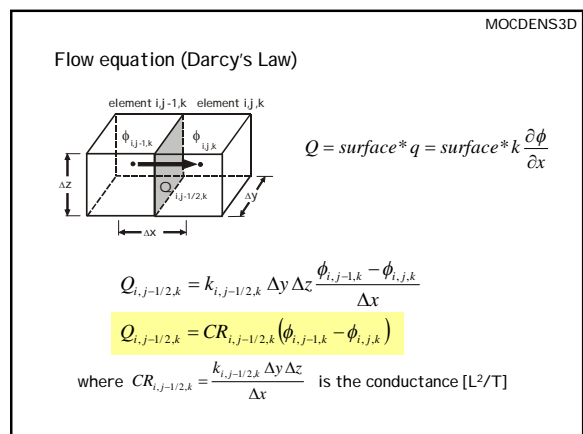
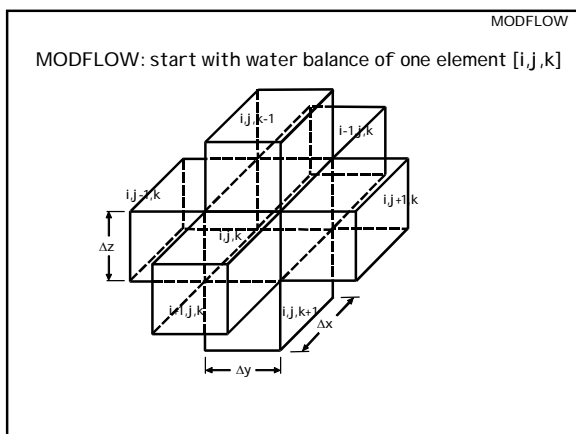
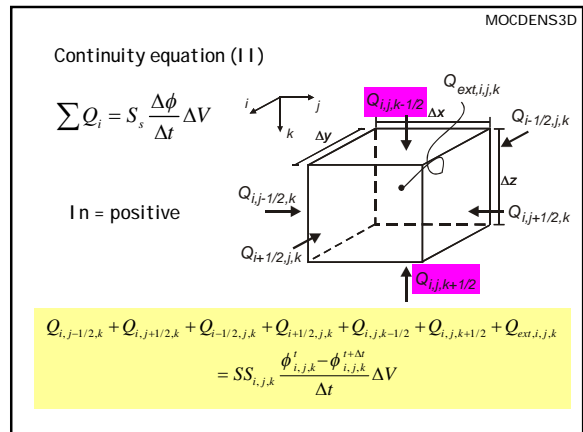
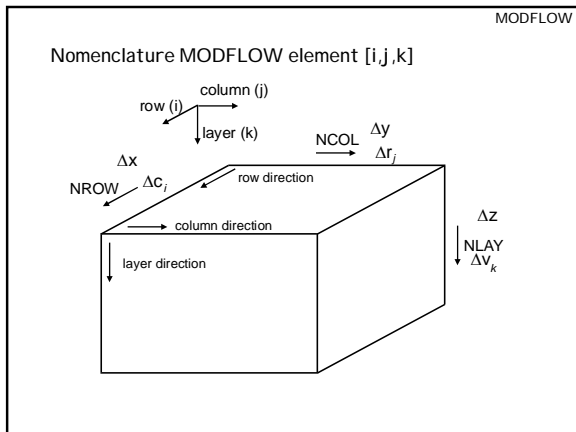
- USGS, 'public domain'
- non steady state
- heterogeneous porous medium
- anisotropy
- coupled to reactive solute transport
 - MOC3 (Konikow *et al.*, 1996)
 - MT3D, MT3DMS (Zheng, 1990)
 - RT3D
 - PHT3D (Prommer, 2004)
- easy to use due to numerous Graphical User Interfaces (GUI's)
 - PMWIN, GMS, Visual Modflow, Argus One, Groundwater Vistas, etc.

MODFLOW

Continuity equation (I)

In - Out = Storage

$$\frac{\partial}{\partial x} \left(k_{xx} \frac{\partial \phi}{\partial x} \right) + \frac{\partial}{\partial y} \left(k_{yy} \frac{\partial \phi}{\partial y} \right) + \frac{\partial}{\partial z} \left(k_{zz} \frac{\partial \phi}{\partial z} \right) - W = S_s \frac{\partial \phi}{\partial t}$$

$$\sum Q_i = S_s \frac{\Delta \phi}{\Delta t} \Delta V$$


MOCDENS3D

Density dependent vertical flow equation

$$q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$q_z = -k_z \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$Q_z = \text{surface} * q_z = \text{surface} * k_z \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$Q_{i,j,k-1/2} = k_{i,j,k-1/2} \Delta x \Delta y \left(\frac{\phi_{f,i,j,k-1} - \phi_{f,i,j,k}}{\Delta z} + BUOY_{i,j,k-1/2} \right)$$

$$Q_{i,j,k-1/2} = CV_{i,j,k-1/2} (\phi_{f,i,j,k-1} - \phi_{f,i,j,k} + BUOY_{i,j,k-1/2} \Delta z)$$

where $BUOY_{i,j,k-1/2} = \left(\frac{\rho_{i,j,k-1/2} + \rho_{i,j,k}}{2} - \rho_f \right)$ =buoyancy term [-]

where $CV_{i,j,k-1/2} = \frac{k_{i,j,k-1/2} \Delta x \Delta y}{\Delta z}$ =conductance [L²/T]

MOCDENS3D

The variable density groundwater flow equation

$$Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k}$$

$$= SS_{i,j,k} \frac{\phi'_{f,i,j,k} - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t} \Delta V$$

and:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{f,i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

gives:

$$CV_{i,j,k-1/2} \phi_{f,i,j,k-1}^{t+\Delta t} + CC_{i-1/2,j,k} \phi_{f,i-1,j,k}^{t+\Delta t} + CR_{i,j-1/2,k} \phi_{f,i,j-1/2,k}^{t+\Delta t} + CR_{i,j+1/2,k} \phi_{f,i,j+1/2,k}^{t+\Delta t}$$

$$+ (-CV_{i,j,k+1/2} - CC_{i+1/2,j,k} - CR_{i,j-1/2,k} - CR_{i,j+1/2,k} - CC_{i+1/2,j,k} - CV_{i,j,k+1/2} + HCOF_{i,j,k}) \phi_{f,i,j,k}^{t+\Delta t}$$

$$+ CR_{i,j-1/2,k} \phi_{f,i,j-1/2,k}^{t+\Delta t} + CC_{i+1/2,j,k} \phi_{f,i+1/2,j,k}^{t+\Delta t} + CV_{i,j,k+1/2} \phi_{f,i,j,k+1/2}^{t+\Delta t} = RHS_{i,j,k}$$

with:

$$HCOF_{i,j,k} = P_{i,j,k} - SC1_{i,j,k} (\Delta t)$$

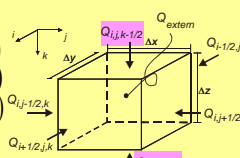
$$RHS_{i,j,k} = -Q'_{i,j,k} - SC1_{i,j,k} \phi_{f,i,j,k}^t / (\Delta t)$$

$$- CV_{i,j,k-1/2} BUOY_{i,j,k-1/2} \Delta v_{k-1/2} + CV_{i,j,k+1/2} BUOY_{i,j,k+1/2} \Delta v_{k+1/2}$$

$$SC1_{i,j,k} = SS_{i,j,k} \Delta V$$

MOCDENS3D

Density dependent groundwater flow equation



$$Q_{i,j-1/2,k} = CR_{i,j-1/2,k} (\phi_{f,i,j-1,k} - \phi_{f,i,j,k})$$

$$Q_{i,j+1/2,k} = CR_{i,j+1/2,k} (\phi_{f,i,j+1,k} - \phi_{f,i,j,k})$$

$$Q_{i-1/2,j,k} = CC_{i-1/2,j,k} (\phi_{f,i-1,j,k} - \phi_{f,i,j,k})$$

$$Q_{i+1/2,j,k} = CC_{i+1/2,j,k} (\phi_{f,i+1,j,k} - \phi_{f,i,j,k})$$

$$Q_{i,j,k-1/2} = CV_{i,j,k-1/2} (\phi_{f,i,j,k-1} - \phi_{f,i,j,k} + BUOY_{i,j,k-1/2} \Delta v_{k-1/2})$$

$$Q_{i,j,k+1/2} = CV_{i,j,k+1/2} (\phi_{f,i,j,k+1} - \phi_{f,i,j,k} - BUOY_{i,j,k+1/2} \Delta v_{k+1/2})$$

$$Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k}$$

$$= SS_{i,j,k} \frac{\phi'_{f,i,j,k} - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t} \Delta V$$

MOCDENS3D

Equation of state

$$BUOY_{i,j,k-1/2} = \left(\frac{(\rho_{i,j,k-1/2} + \rho_{i,j,k}) / 2 - \rho_f}{\rho_f} \right)$$

$$\rho_{i,j,k} = \rho_f \left(1 + \frac{\rho_s - \rho_f}{\rho_f} \frac{C_{i,j,k}}{C_s} \right)$$

or

$$\rho_{i,j,k} = \rho_f (1 + \beta C_{i,j,k})$$

MOCDENS3D

The term $Q_{ext,i,j,k}$

Takes into account all external sources

Rewriting the term:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

MODFLOW

Method of Characteristics (MOC)

Solve the advection-dispersion equation (ADE) with the Method of Characteristics

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_j} \left(D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (CV_i) + \frac{(C-C)W}{n_e}$$

Lagrangian approach:

Splitting up the advection part and the dispersion/source part:

- advection by means of a particle tracking technique
- dispersion/source by means of the finite difference method

Length flow time step

NOT EQUAL TO SOLUTE TIME STEP !

Stability criteria for solute transport equation (I)

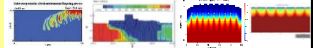
1. Neumann criterion:

$$\frac{D_{xx} \Delta t_s}{\Delta x^2} + \frac{D_{yy} \Delta t_s}{\Delta y^2} + \frac{D_{zz} \Delta t_s}{\Delta z^2} \leq 0.5$$

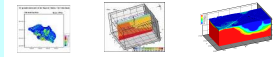
$$\Delta t_s \leq \frac{0.5}{\frac{D_{xx}}{\Delta x^2} + \frac{D_{yy}}{\Delta y^2} + \frac{D_{zz}}{\Delta z^2}}$$

Modelling fresh-salt groundwater on different scales

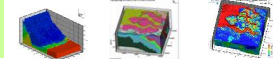
Sub-local: fingering, salty sand boils
Sri Lanka (Tsunami 2004),
Zandmotor
cell size=1cm-1m



Local: rainwaterlenses, heat-cold
Tholen, Schouwen-Duiveland
cell size=5-25m



Regional:
Zeeland, Gujarat/India, Philippines
cell size=100m



National: salt load
Bangladesh, Zuid-Holland, NHI
cell size=250m-2km

**Goal:**

To take largest cell size possible to accurately model relevant salinisation processes

Stability criteria for solute transport equation (II)

2. Mixing criterion:

$$\Delta t_s \leq \frac{n_e b_{i,j,k}^k}{Q_{i,j,k}}$$

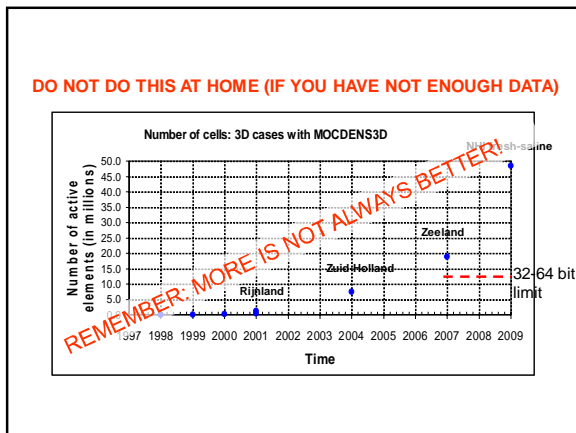
Change in concentration in element is not allowed to be larger than the difference between the present concentration in the element and the concentration in the source

Stability criteria for solute transport equation (III)

3. Courant criterion:

$$0 < \xi \leq 1$$

$$\Delta t_s \leq \frac{\xi \Delta x}{V_{x,\max}} \quad \Delta t_s \leq \frac{\xi \Delta y}{V_{y,\max}} \quad \Delta t_s \leq \frac{\xi \Delta z}{V_{z,\max}}$$



- variable density
- Difficulties with variable density groundwater flow
- Initial density distribution (effects on velocity field) !
 - Velocities freshwater lens at the outflow face near the sea
 - Boundary conditions (especially concentration boundaries)
 - Choice of element size
 - Length of flow time step to recalculate groundwater flow

Modelling effect climate change on fresh-salt groundwater

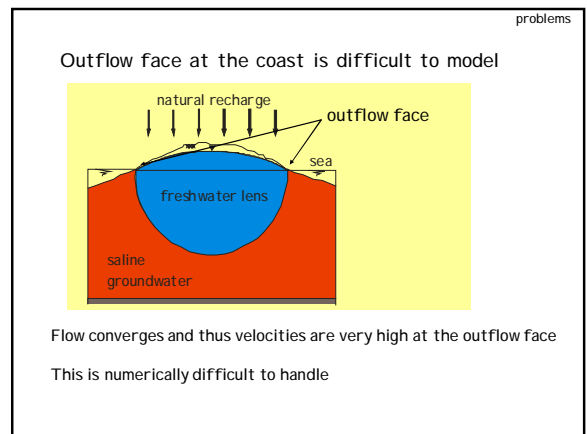
Modelling:

- variable-density
- 3D, non-steady
- groundwater flow
- coupled solute transport

Code:
MOCDENS3D (MODFLOW family)
similar to SEAWAT

Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- land subsidence
- changing extraction rates
- adaption measures



- Fields of application of fresh-saline groundwater models**
- Water system analysis in brackish-saline environments (salt loads, salt boils, freshwater lenses)
 - Quantifying effects of climate change & sea level rise
 - Drinking water issues: upconing saline groundwater under extraction wells
 - Developing measurements to stop salinization groundwater systems (e.g. fresh keeper, coastal collectors, freshwater storage underground)
 - Impact of the disasters as tsunamis on fresh groundwater resources
 - Submarine Groundwater Discharge (marine water pollution, Harmful Algae)
-

- A good initial density distribution is essential**
- Because groundwater and solute transport are coupled, the density influences groundwater velocities
 - Numerous density measurements are necessary to get a reliable 3D density matrix

'Procedure' to improve initial density distribution

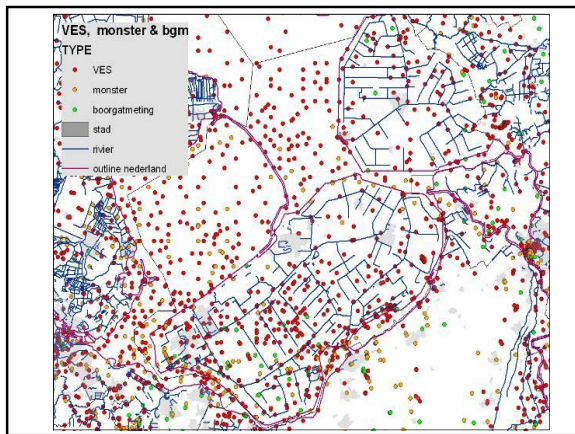
- Implement all chloride data
 - Analyses, Borehole, VES, Airborne techniques (HEM, SkyTem)
 - Better old then nothing
 - Better VES then nothing
- Interpolate and extrapolate
 - Sea = easy (salt)
 - Inland = fresh?
- Start with simulation (10/20/30 years) with mol.diffusion*1000 to smooth out artificial densities

Mapping brackish-saline interface Zeeland

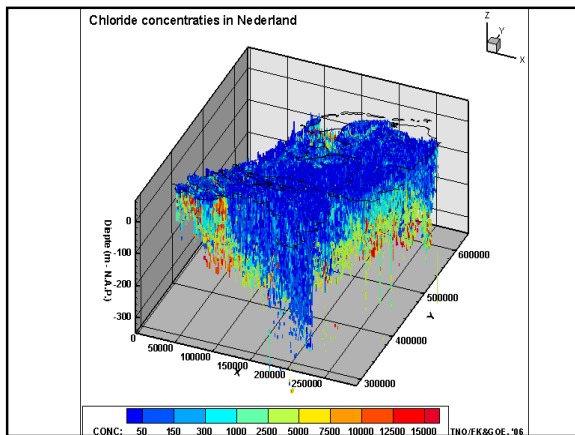
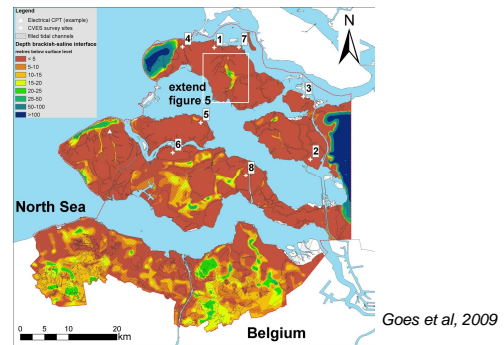
*Combining different types of data sources:

Data type	Characteristics of measurement	# Data	Determined	Accuracy depth of interfaces
Groundwater Samples	OD in situ	721	Chloride concentration	Depends on positions of screens
Geo-electrical borehole logs	1D in situ	149	1D chloride profile, Depth fresh-brackish and brackish-saline interface, Inversions.	±1 m
Electrical CPT	1D in situ (max. depth 50 m)	71	Borehole log	±1 m
VES	1D from surface	1113	Depth brackish-saline interface, Major inversions, (1D chloride profile).	±20% of depth
EM34	1D from surface	3251	Depth brackish-saline interface	ranges of 7.5, 15 or 30 m (accuracy decreases with depth)
Groundwater Abstractions	OD in situ	716	Depth brackish-saline interface	a range depending on screen depth
Unique locations		6021		

20130322 DGG

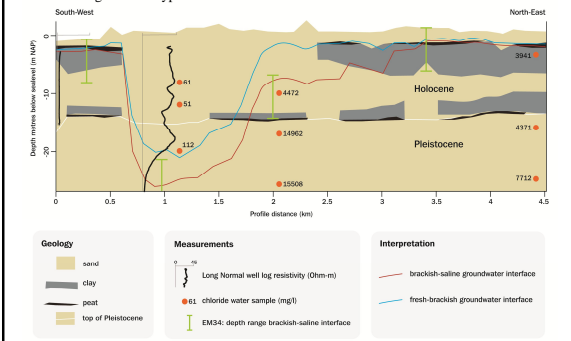


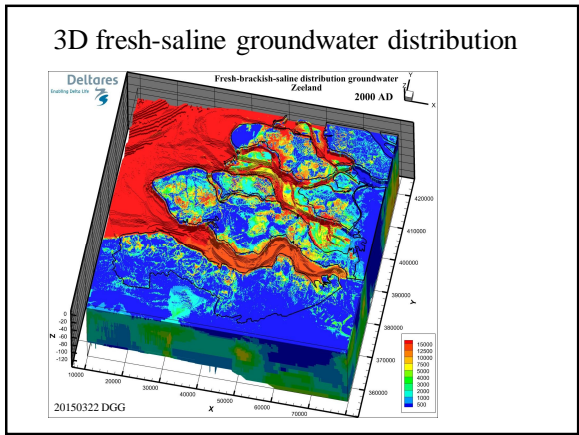
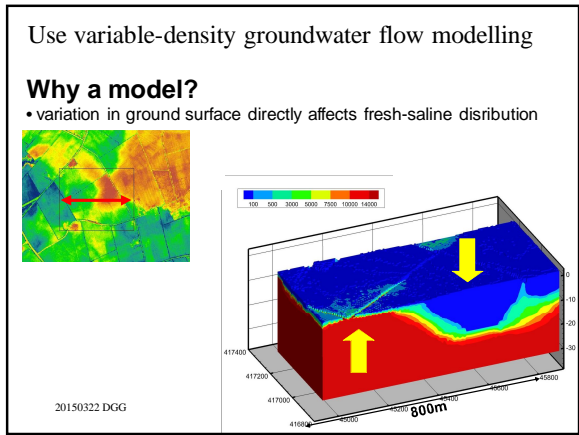
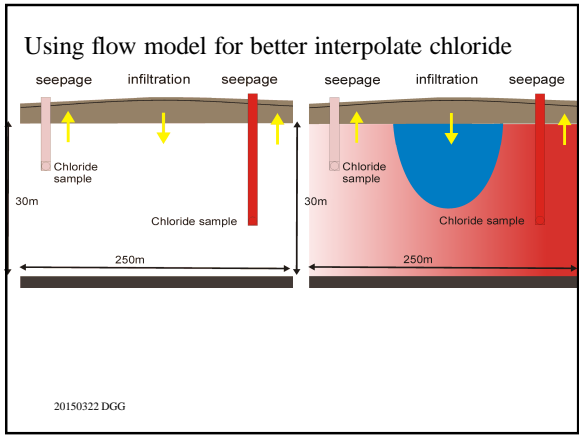
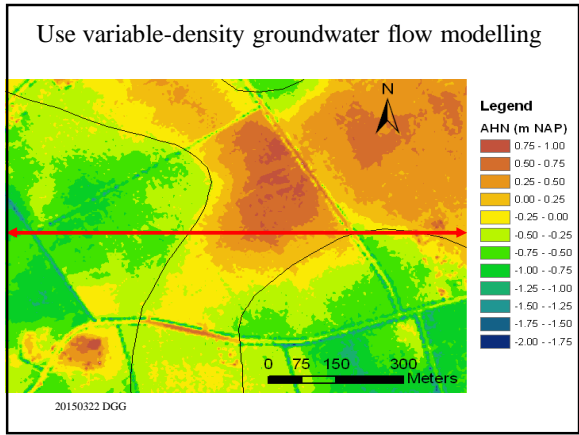
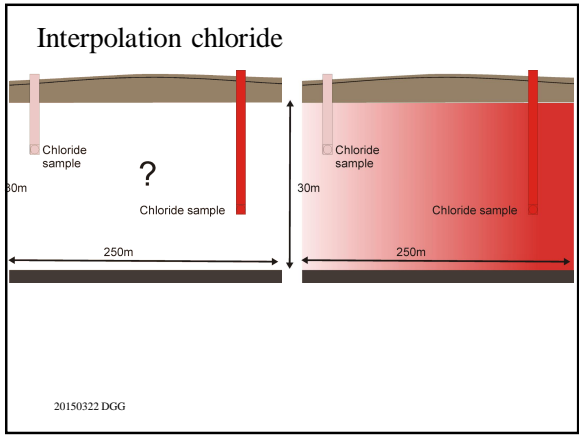
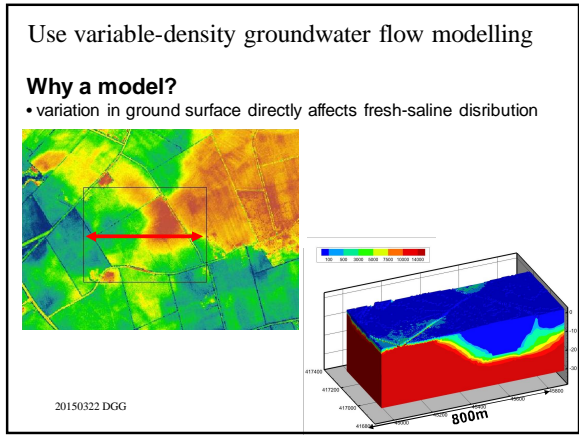
Mapping brackish-saline interface

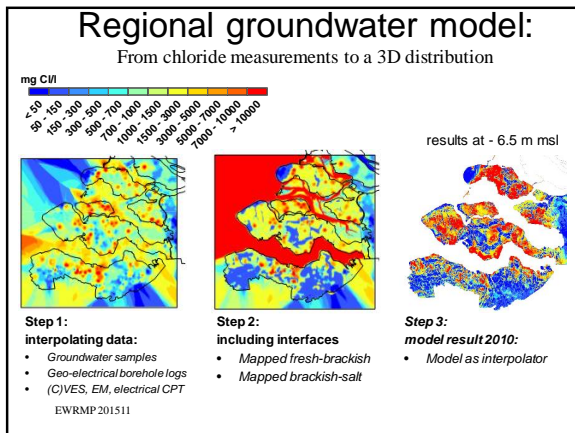


Mapping brackish-saline interface

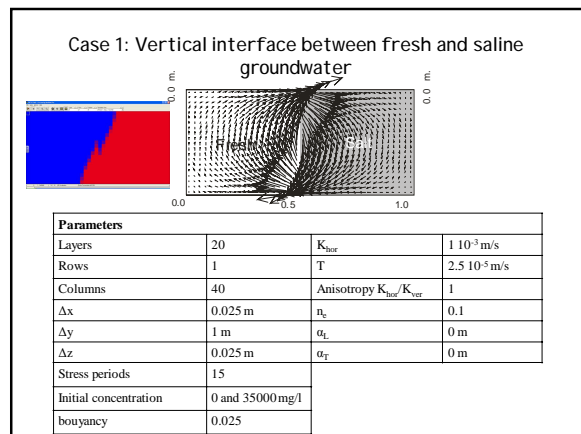
*Combining different types of data sources







- modelling
- ### Examples of variable-density groundwater flow
- Rotating immiscible interface
 - Henry's problem
 - Evolution freshwater lens
 - Hydrocoin
 - Salt water pocket
 - Broad 14 Basin, North Sea
 - Heat transport: Elder and Rayleigh=4000
 - 5 Dutch 3D cases
 - Freshwater lenses
 - Effect of Tsunami on groundwater resources

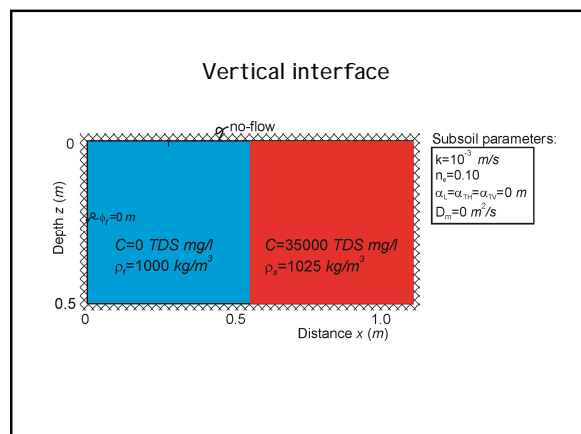


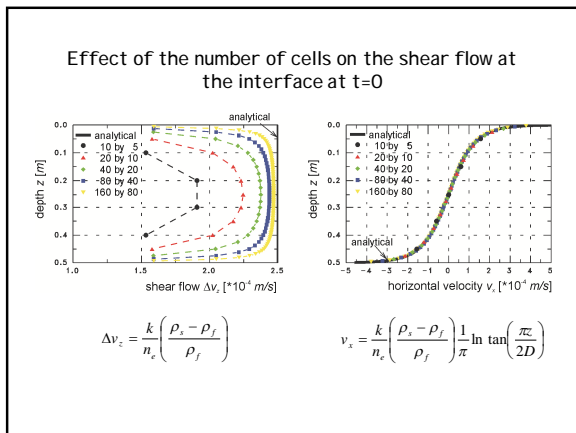
cases

Rotating immiscible interfaces

Conclusion:

To check the variable-density component of your code, this immiscible interface benchmark can be used.

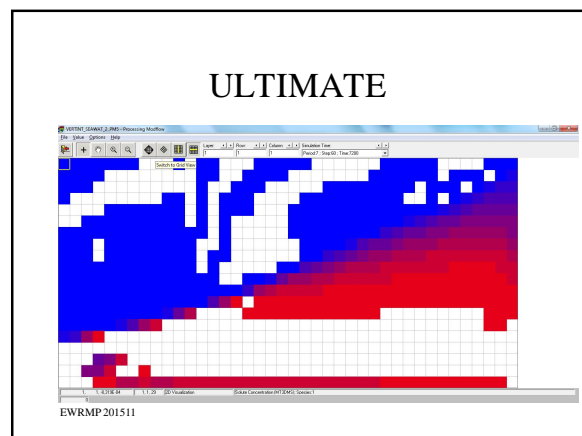
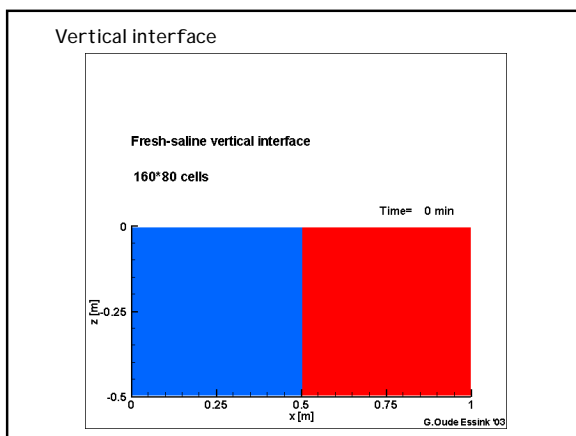
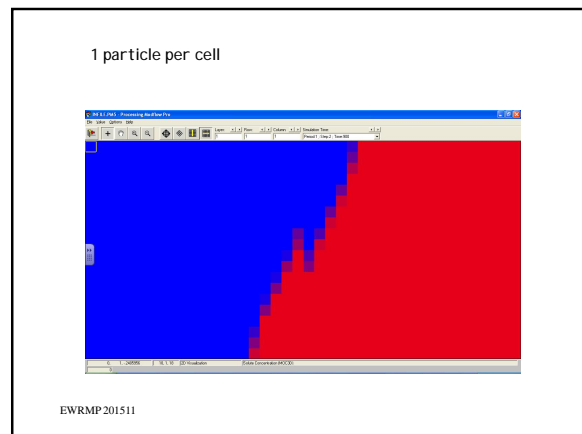
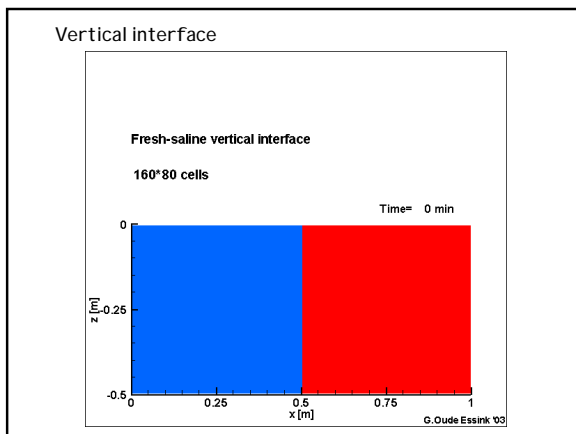




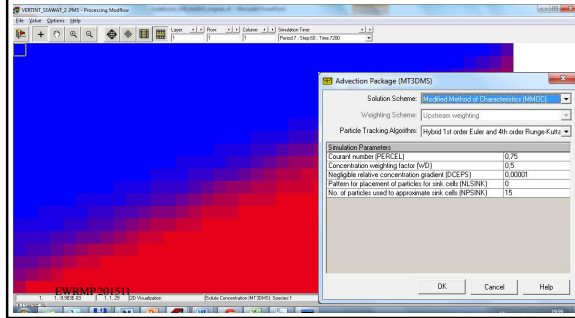
The effect of numerical solvers on the salt transport

Examples

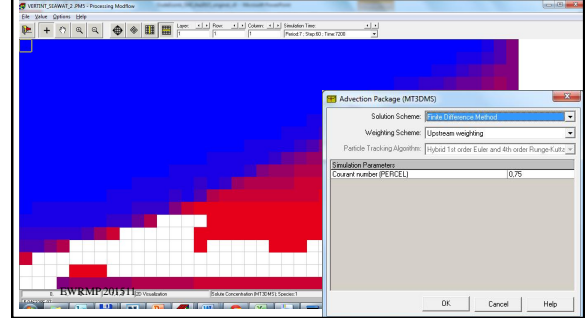
EWMP 201511



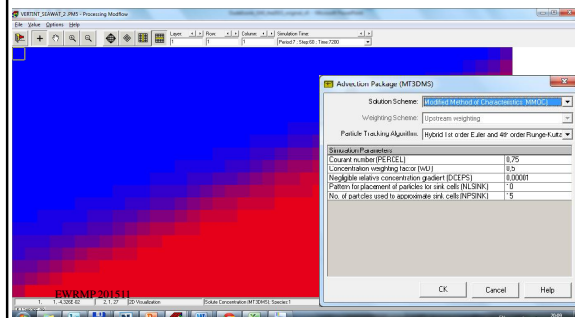
MMOC, NPLANE=0



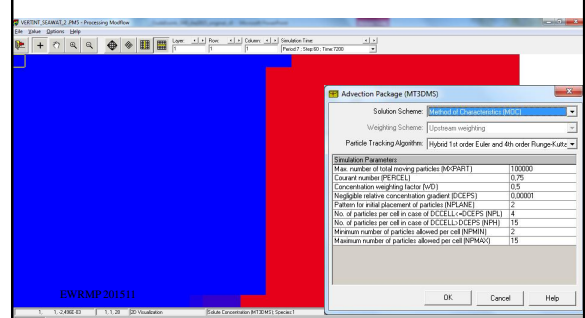
Finite Difference Method



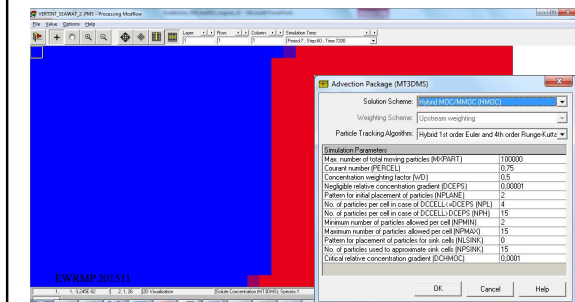
MMOC, NPLAN=10



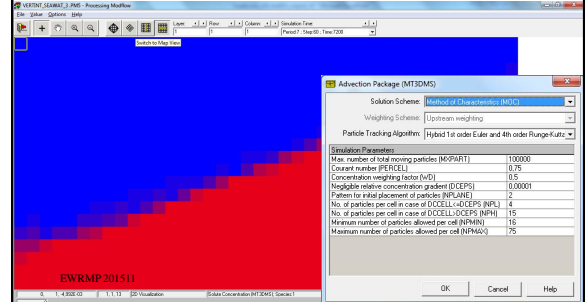
MOC

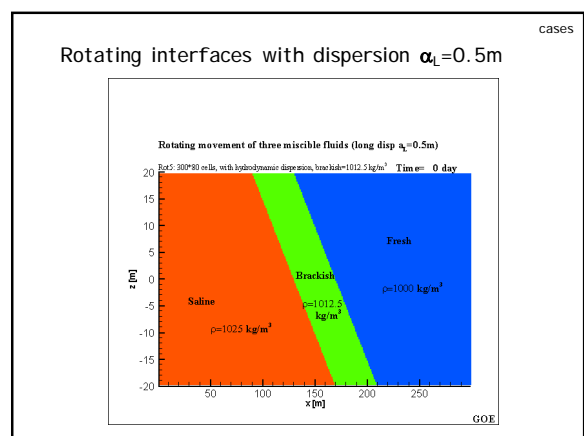
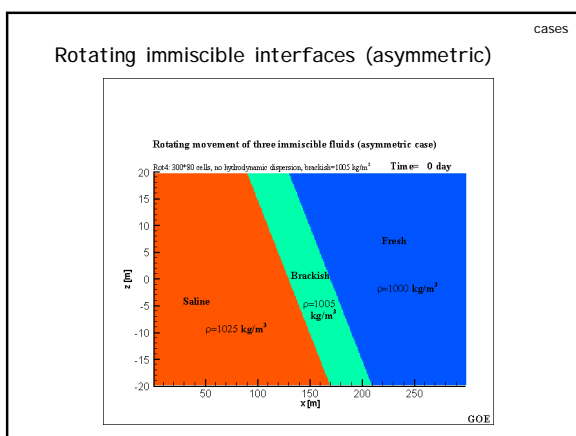
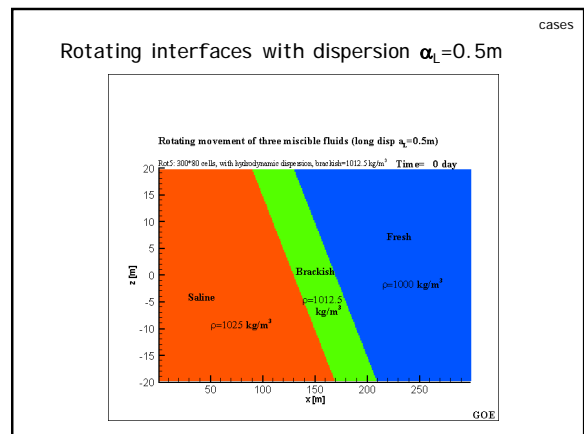
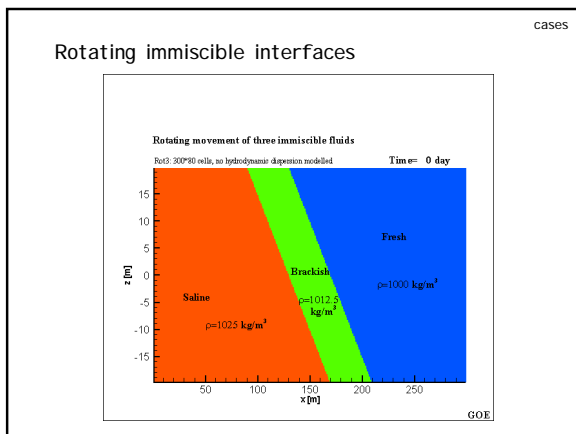
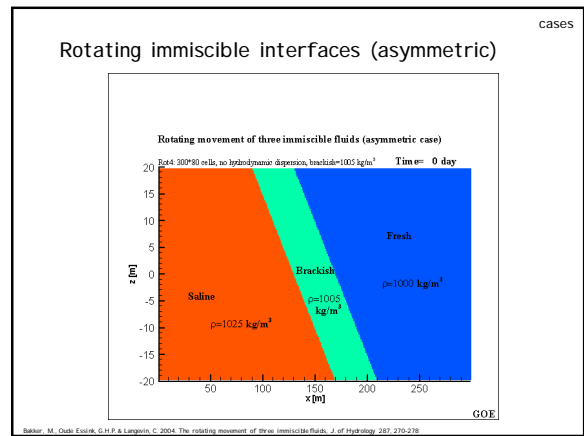
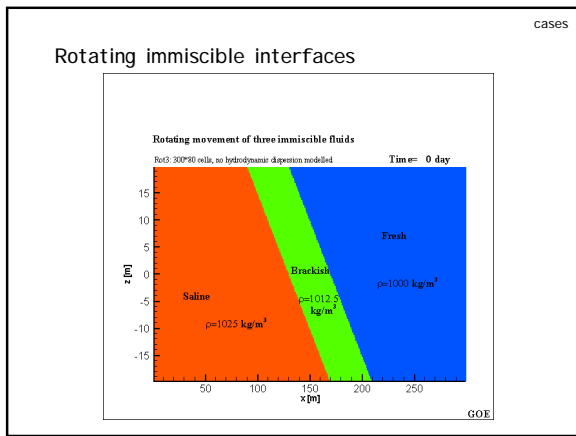


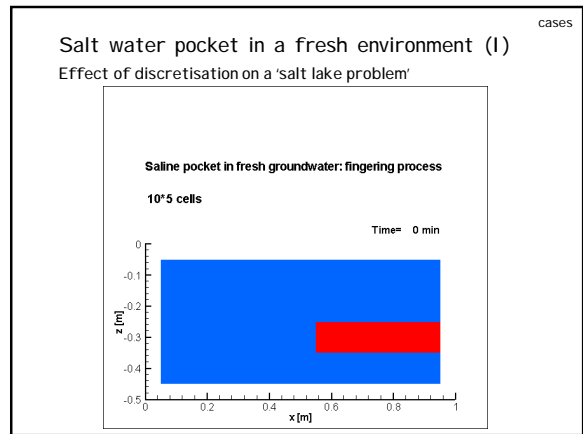
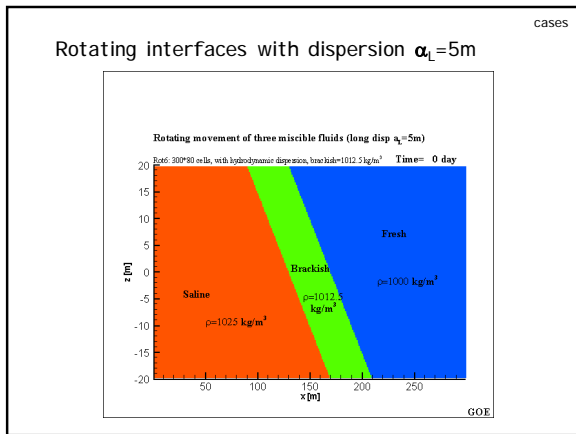
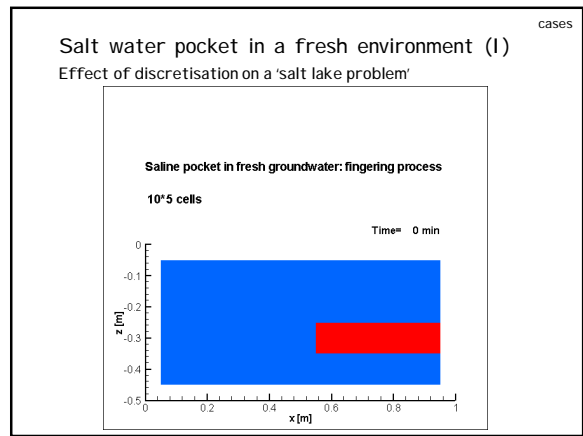
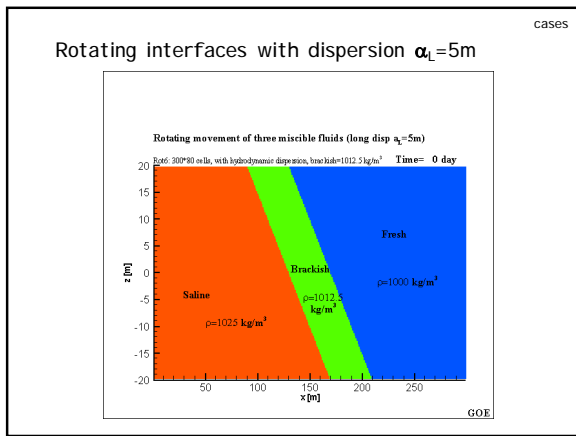
HMOC



MOC

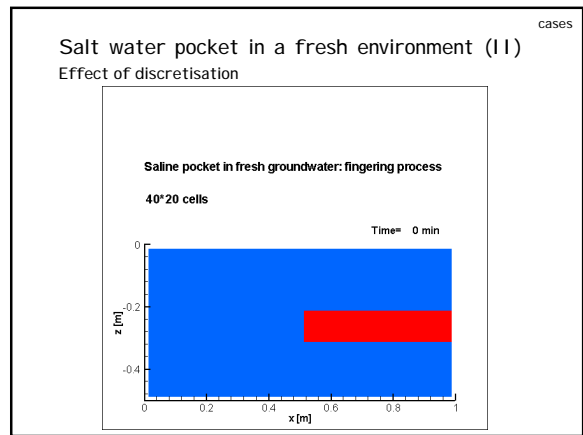


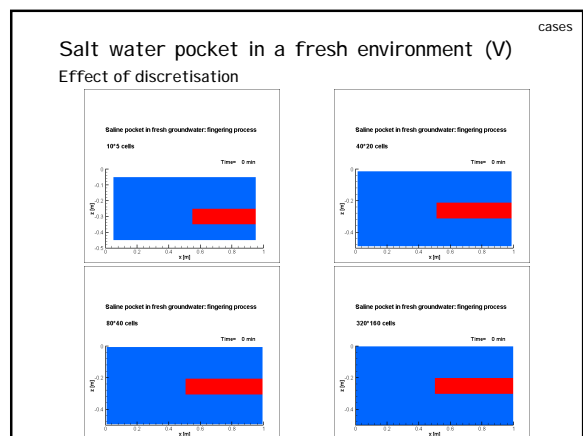
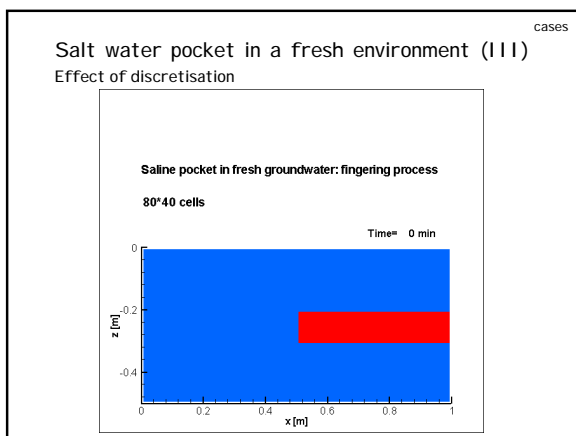
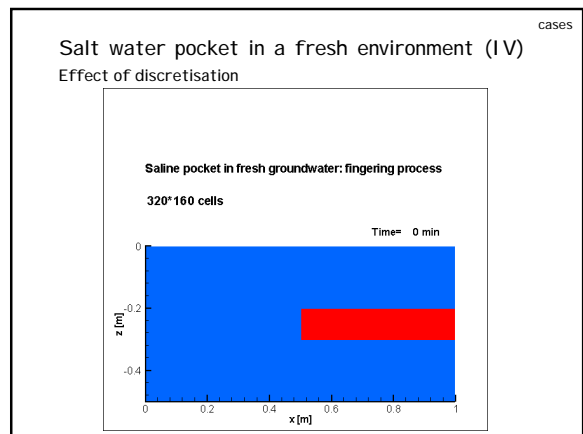
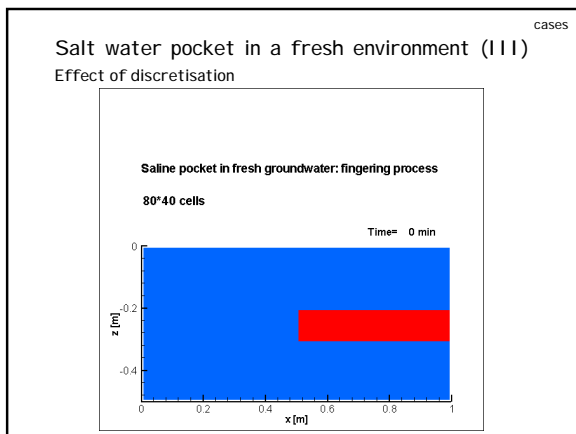
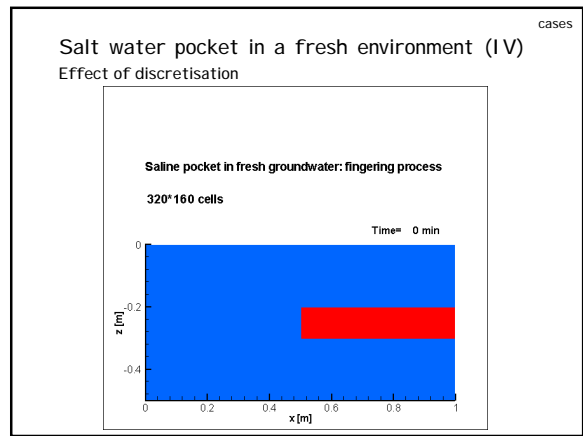
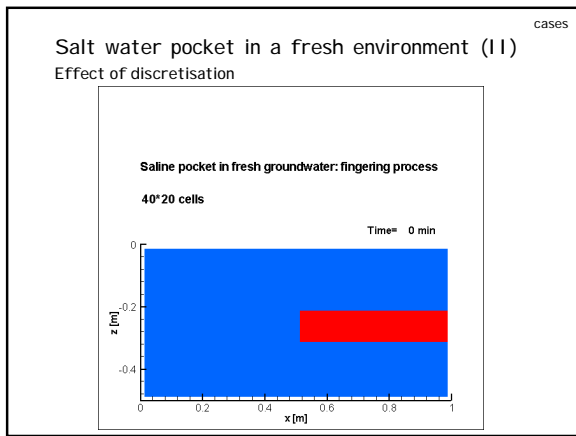


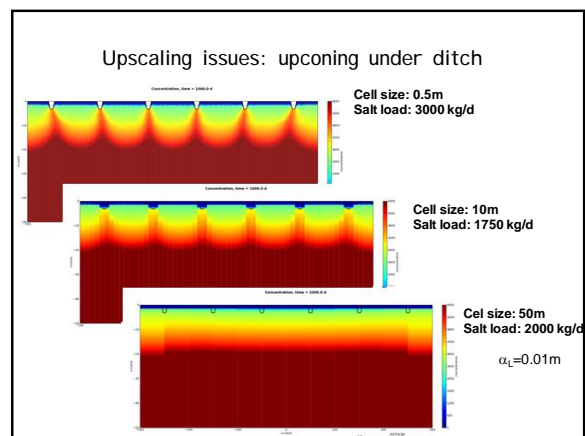
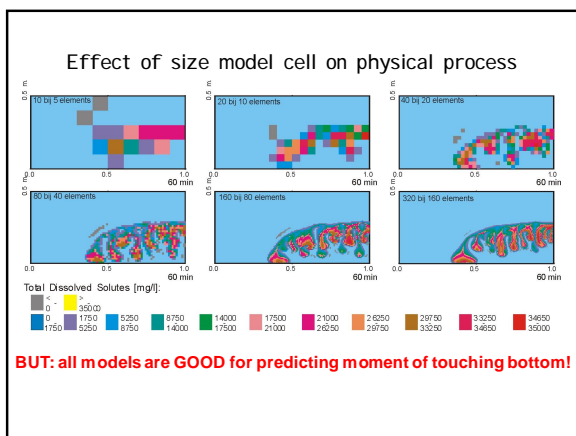
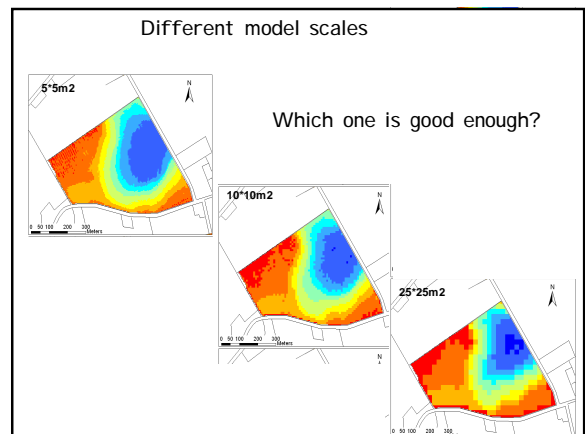
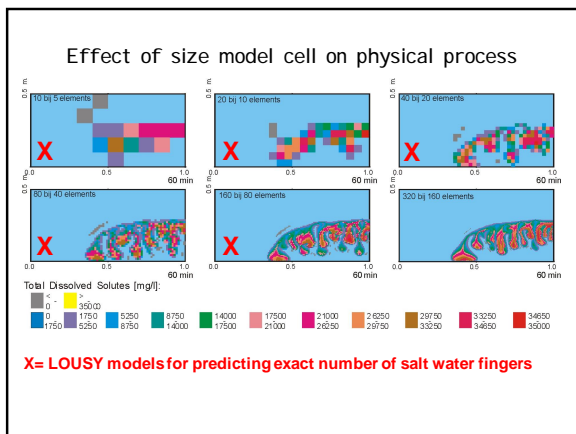
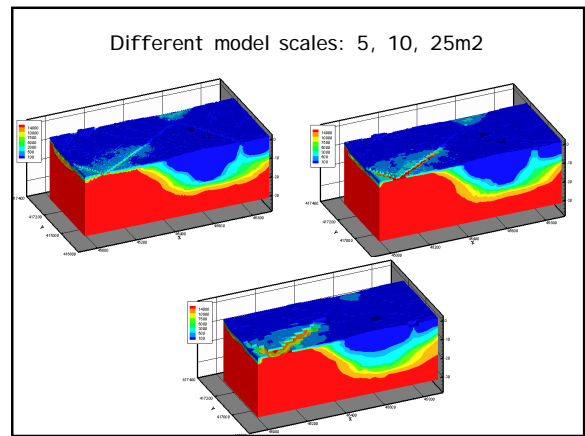
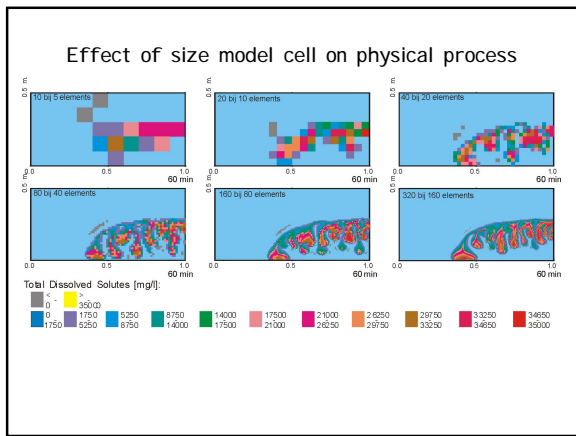


Salt water pocket in a fresh environment

Grid convergence
Time step





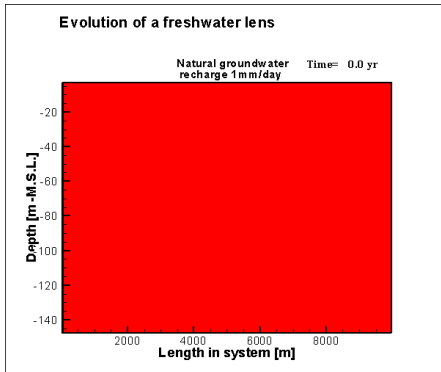


Salt water pocket in a fresh environment (VI)

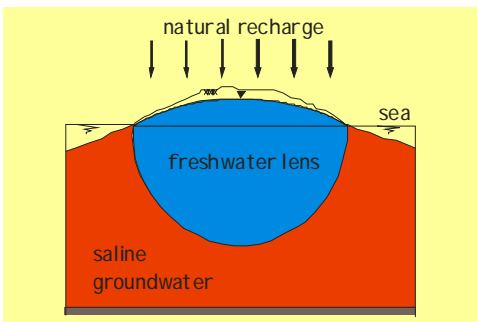
Conclusion:

- For some physical processes, a large number of cells is necessary
- Check always grid convergence!

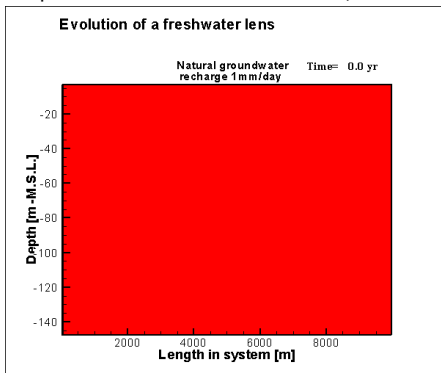
Concept: evolution freshwater lens (not Griend!)



Evolution of a freshwater lens



Concept: evolution freshwater lens (not Griend!)



Question:

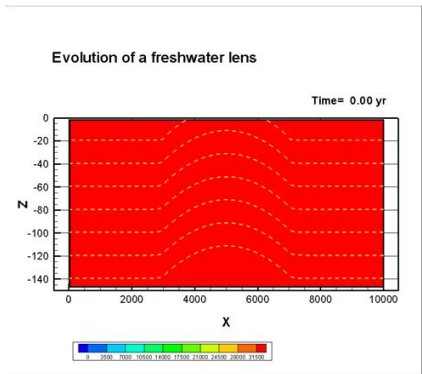
How long does it take before the volume of a freshwater lens is filled?:

- a. 5 years
- b. 25 years
- c. 100 years
- d. 500 years

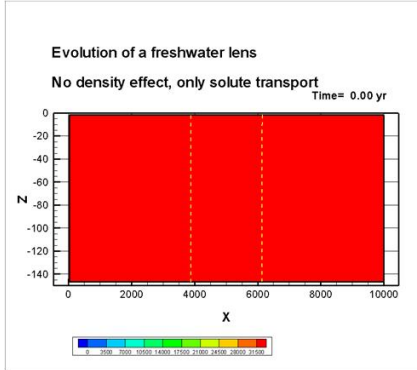
T = specific time scale
 T = time period before the lens has reached 95% of its final form

In the Netherlands: T = 75-200 jaar,
 depends on:
 • width dune area
 • natural groundwater recharge
 • hydraulic conductivity soil

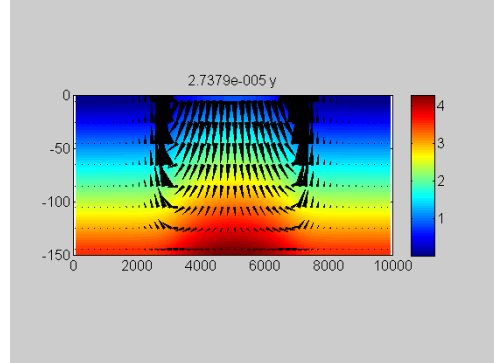
Evolution freshwater lens



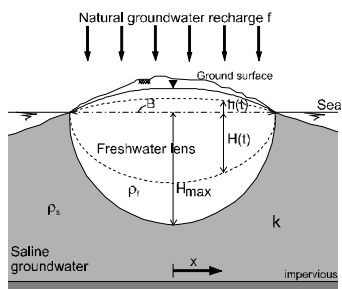
Evolution freshwater lens: no density effects



Evolution freshwater head

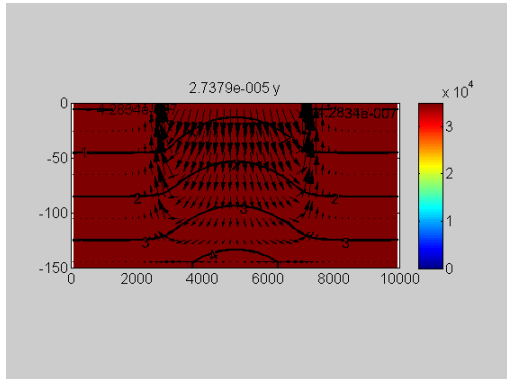


Case 2: Development of a freshwater lens



Evolution freshwater head

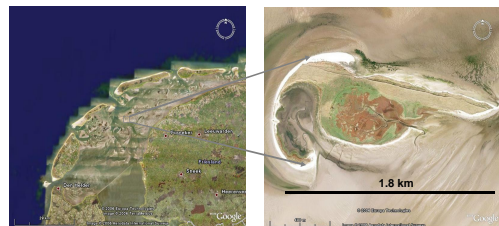
Evolution lens



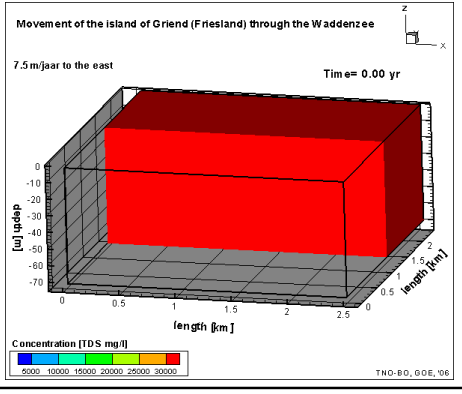
The island of Griend

Issues:

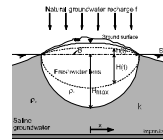
1. Small island moves ~ 7.5 m per year to the east
2. Effect on the volume of the freshwater lens:
 - Can a lens be developed?
 - What is the thickness of the lens?



Movement of De Griend and creation of the lens

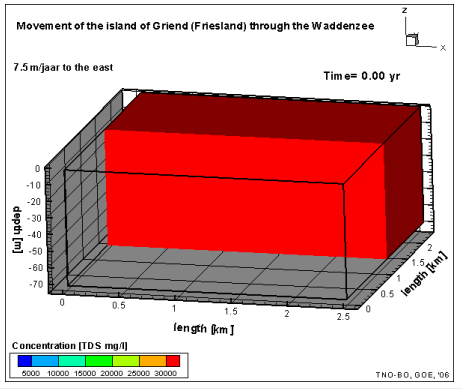


Case 2: Development of a freshwater lens

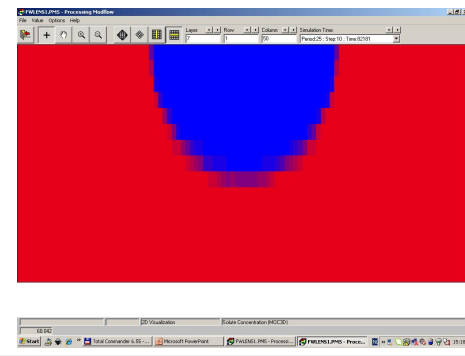


Parameters			
Layers	15	K_{hor}	20 m/d
Rows	1	T	200 m/d
Columns	100	Anisotropy K_{hor}/K_{ver}	10
Δx	100 m	ne	0.35
Δy	10 m	αL	0 m
Δz	10 m	αT	0 m
Stress periods	10	recharge	360 mm/y
Initial concentration	35000 mg/l	Recharge concentration	0 mg/l
bouyancy	0.025		

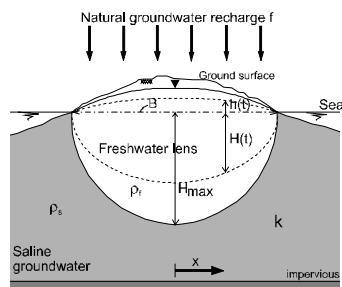
Movement of De Griend and creation of the lens



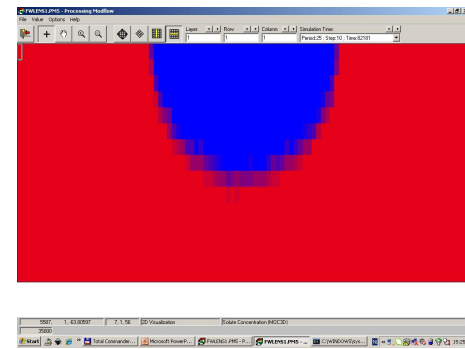
MOCDENS3D, no disp, 16part



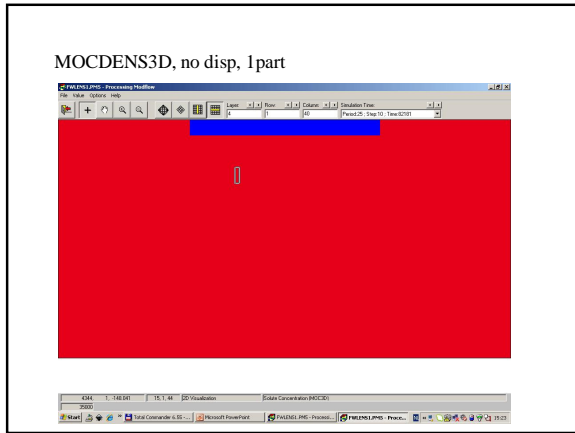
Case 2: Development of a freshwater lens



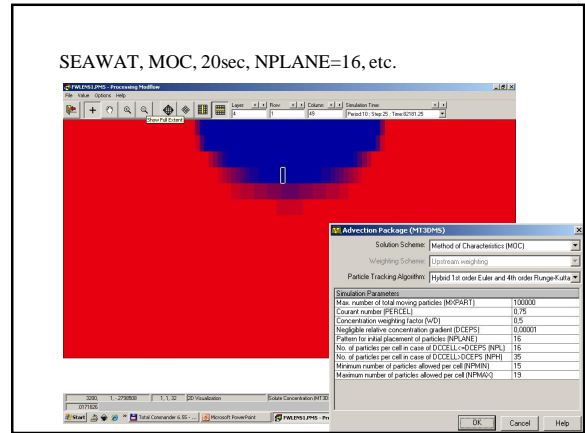
MOCDENS3D, no disp, 4part



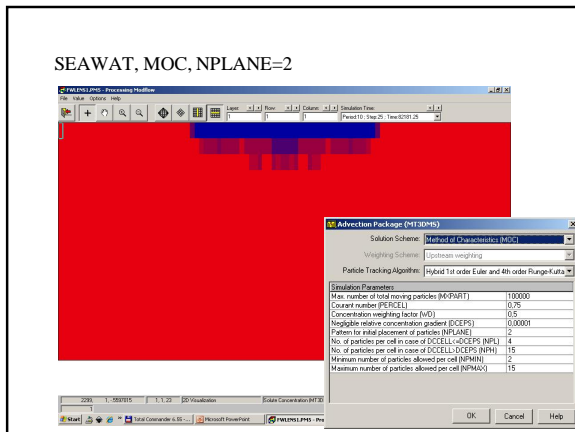
MOCDENS3D, no disp, 1part



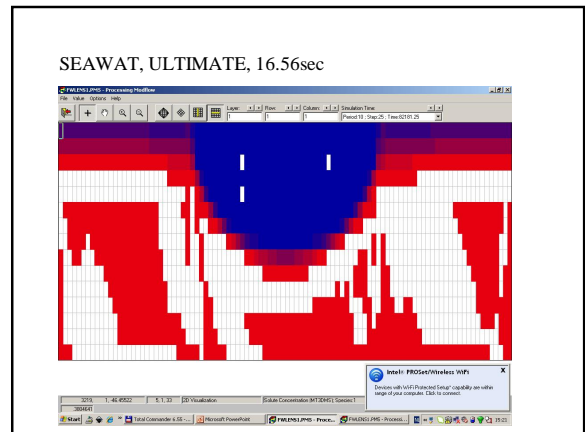
SEAWAT, MOC, 20sec, NPLANE=16, etc.



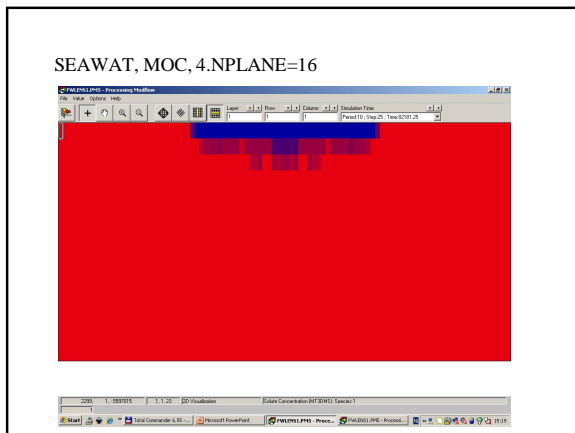
SEAWAT, MOC, NPLANE=2



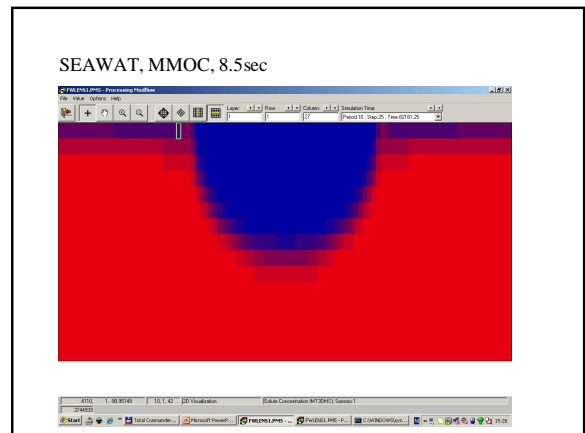
SEAWAT, ULTIMATE, 16.56sec

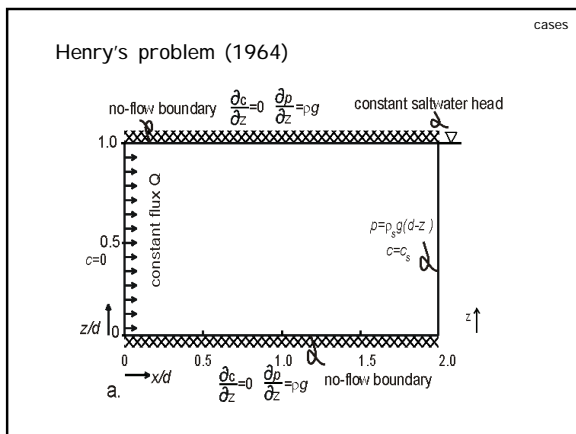
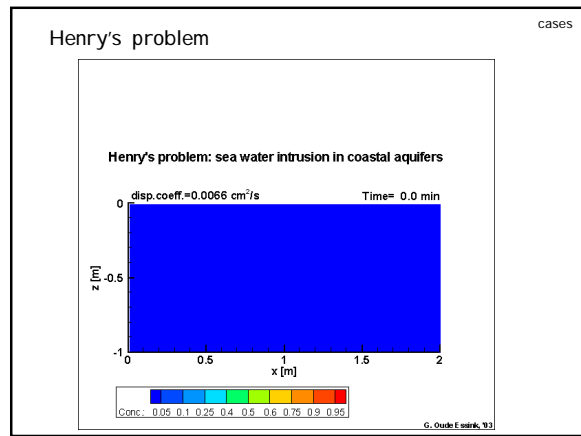
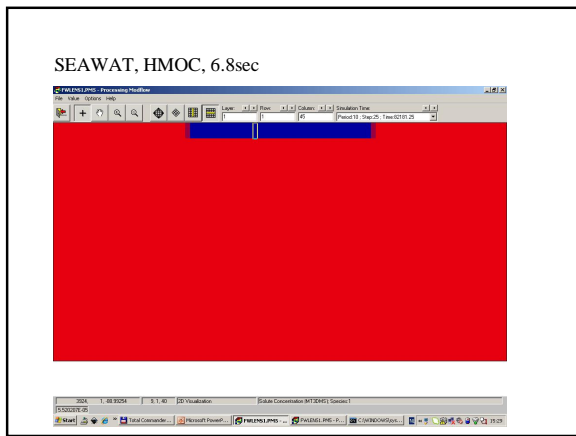


SEAWAT, MOC, 4.NPLANE=16



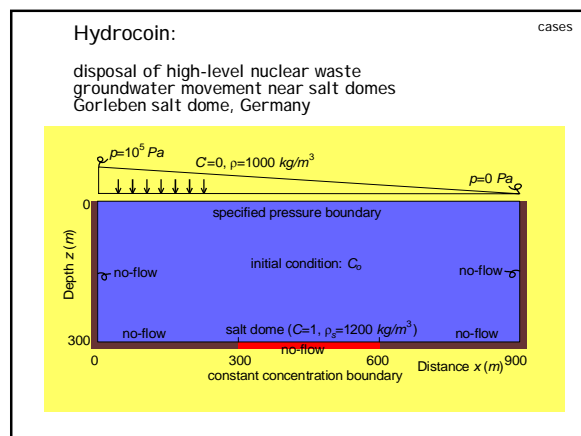
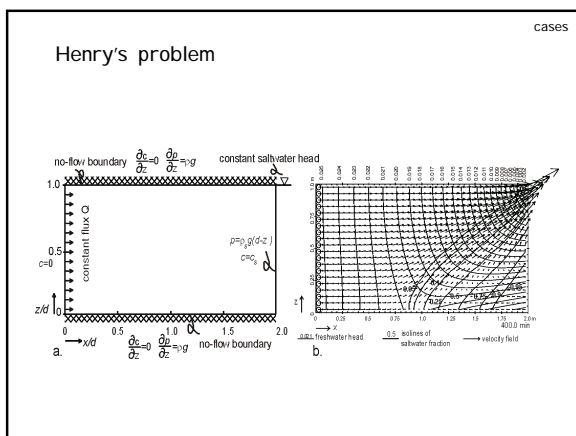
SEAWAT, MMOC, 8.5sec

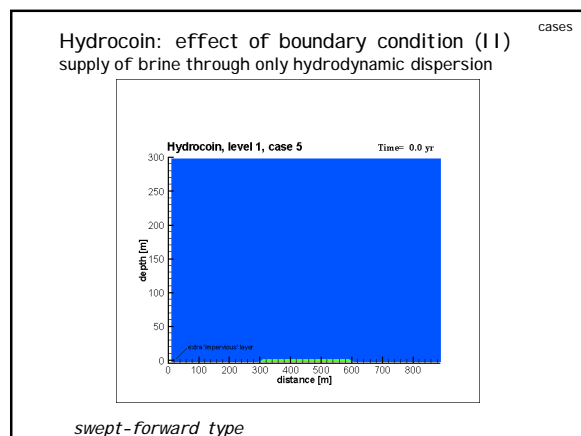
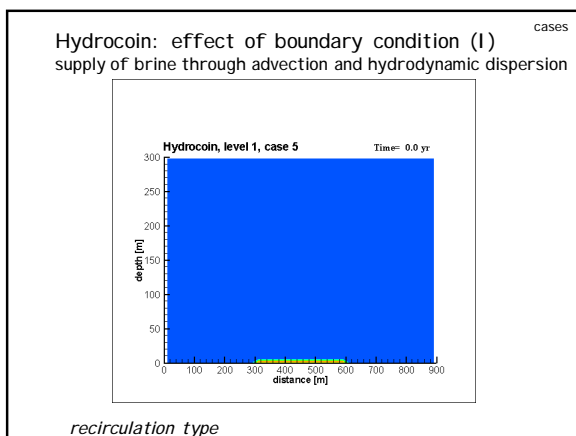
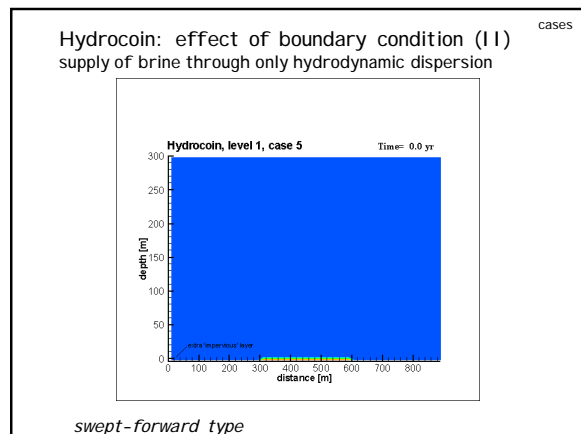
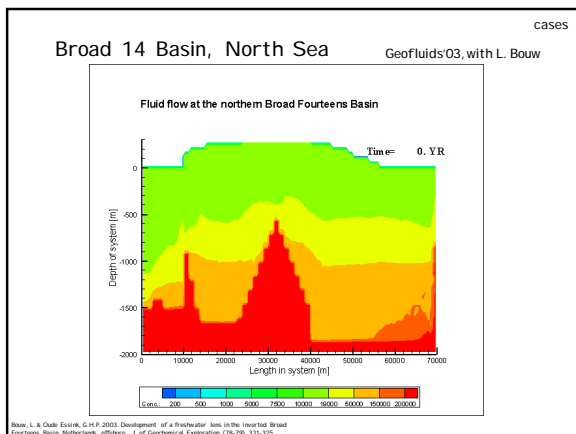
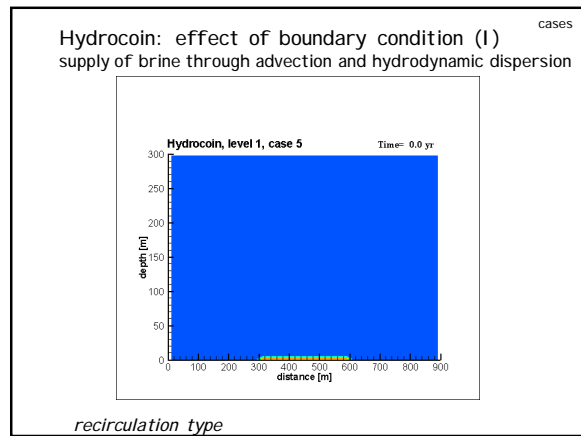
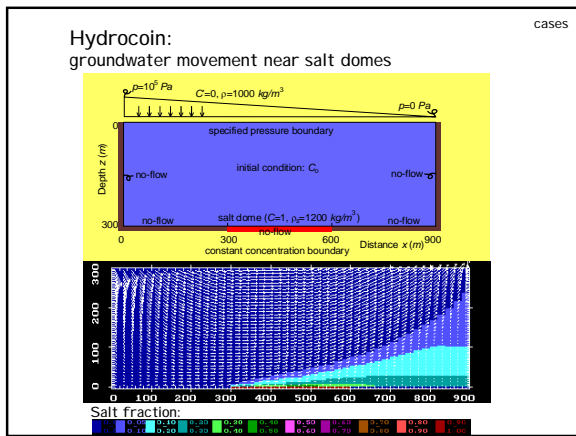


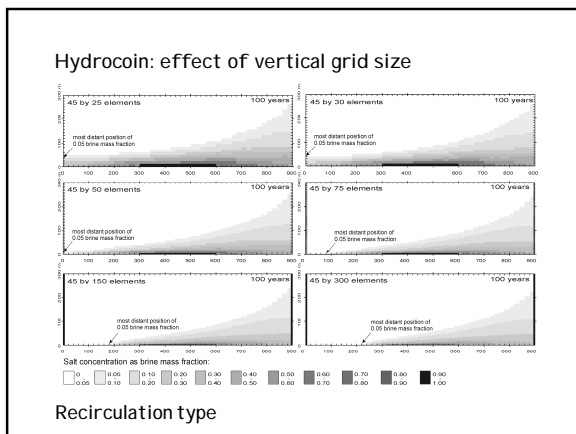
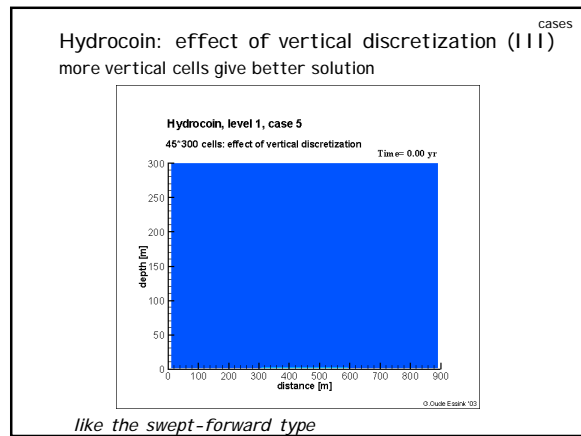
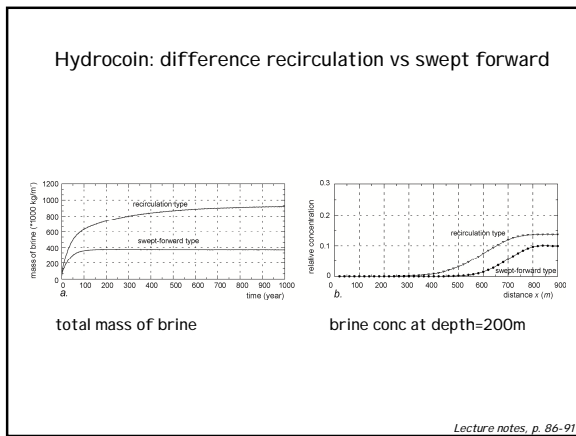


Henry's problem

Don't use the Henry problem as a variable-density benchmark, because even with a constant density model, the results are more or less the same!







Analogy physical processes cases

Heat transport (analogy with solute transport)

Groundwater flow: Darcy

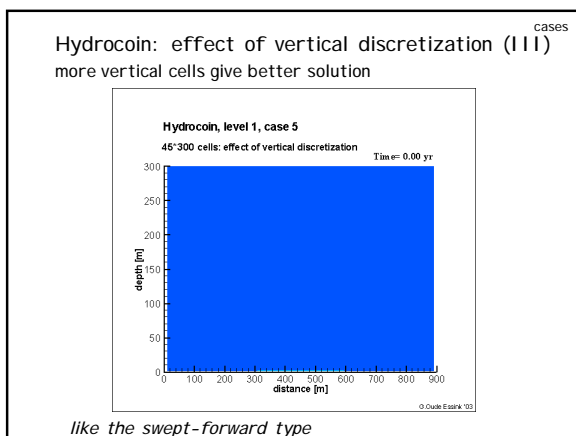
$$q = -k \frac{\partial \phi}{\partial x}$$

Heat conduction: Fourier

hot plate: 100 C | ice blocks: 0 C

$$h = -\lambda \frac{\partial T}{\partial x}$$

Electrodynamics: Ohm

$$i = -\sigma \frac{\partial V}{\partial x}$$


Conduction and convection of heat Heat transport

$$h = -\lambda_e \frac{\partial T}{\partial x} + n_e \rho c_f VT$$

thermal conductivity [Joule/(ms °C)]

$$\lambda_e = n_e \lambda_{fluid} + (1 - n_e) \lambda_{solid}$$

heat conduction flux (Fourier) | convection (fluid flow)

continuity equation

$$-\frac{\partial h}{\partial x} = \rho' c' \frac{\partial T}{\partial t}$$

specific heat capacity [Joule/(kg °C)]

$$\rho' c' = n_e \rho c_{fluid} + (1 - n_e) \rho_{solid} c_{solid}$$

cases

Analogy solute and heat transport

Solute: advection-dispersion equation

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (C V_i) + \frac{(C-C)W}{n_e}$$

Heat: convection-conduction equation

$$\rho' c' \frac{\partial T}{\partial t} = \frac{\partial}{\partial x_i} \left(\Lambda_{ij} \frac{\partial T}{\partial x_j} \right) - \rho c_f \frac{\partial T q_i}{\partial x_i} + \Gamma$$

cases

Elder problem (I)

It is originally a heat transport problem

Phases:

1. Stable growth diffusive boundary layer
2. Development flow cells embedded in boundary layer
3. Emergence of disturbances that grow into fingers

Convection of heat occurs when:
Rayleigh number $> 4\pi^2$

Elder, J. Fluid Mech. 32, 69-96, 1968

Heat transport

Analogy heat and solute transport

Heat transport
Convection-conduction equation

$$\rho' c' \frac{\partial T}{\partial t} = \frac{\partial}{\partial x_i} \left(\Lambda_{ij} \frac{\partial T}{\partial x_j} \right) - \rho c_f \frac{\partial T q_i}{\partial x_i} + \Gamma$$

Equation of state: relation density & temperature

$$\rho_{i,j,k} = \rho_f (1 - \alpha_f T_{i,j,k})$$

Analogy between solute and heat transport

Solute	Heat
C	T
R_d	$1 + \frac{(1-n_e)\rho c_s}{n_e \rho c_f}$
D_m	$\frac{n_e \lambda_e + (1-n_e) \lambda_s}{n_e \rho c_f}$
λ	0

Elder problem (II)

Analogy composition and heat

Lecture notes, p. 91-96

Heat transport

Energy storage in geothermal reservoirs

Temperature (degrees Celsius):

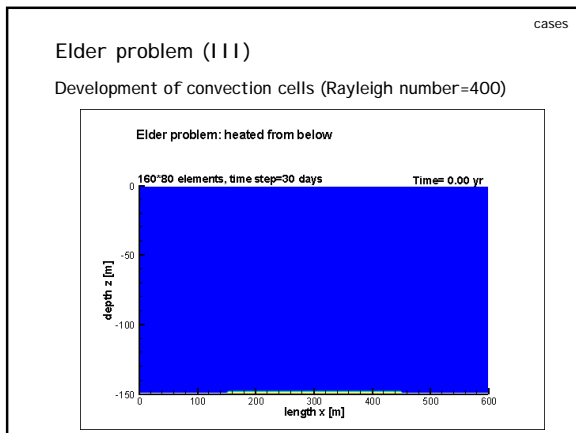
30 35 40 45 50 55 60

cases

Elder problem (III)

Development of convection cells (Rayleigh number=400)

160*80 elements, time step=30 days
Time= 0.00 yr

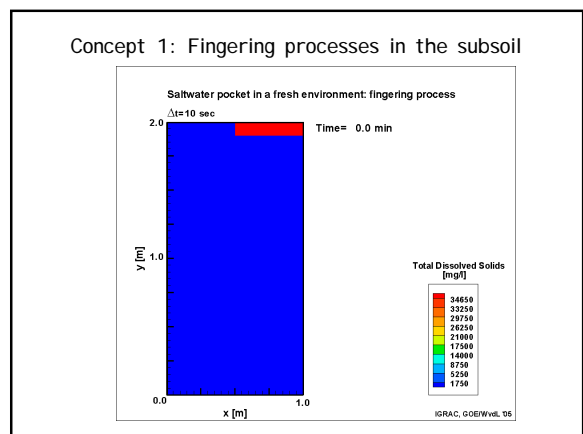
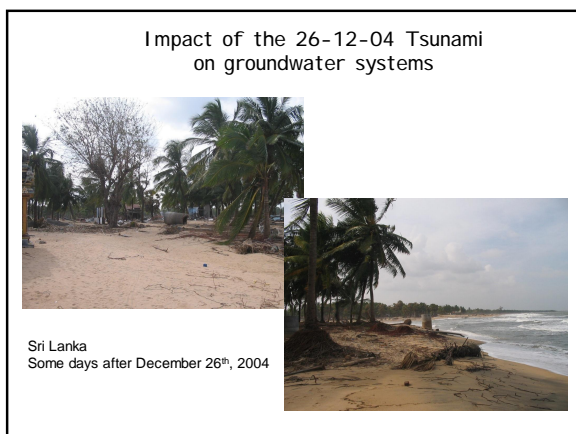
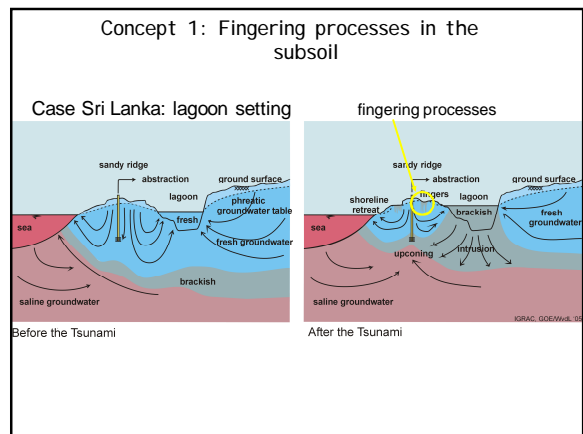
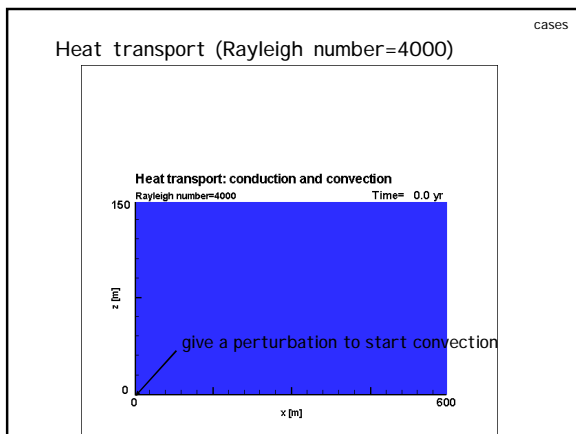


Impact of the 26-12-04 Tsunami on groundwater systems

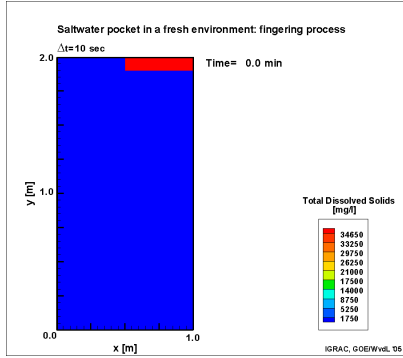
Impression of relevant salinisation processes by conceptual models of salt water intrusion in coastal aquifers:

1. Fingering processes in the subsoil
2. Evolution of a freshwater lens after flooding by sea water
3. Freshwater lens in a coastal aquifer with a brackish lagoon

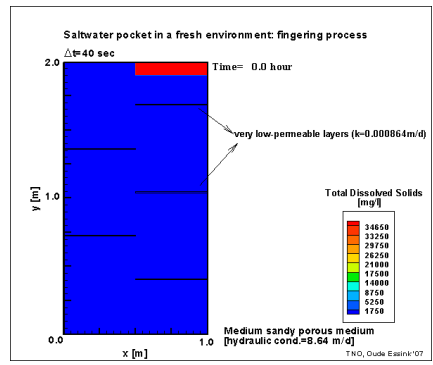
Next step:
quantifying processes in real situations, using topographic and hydrogeological data, and ending up with vulnerability maps



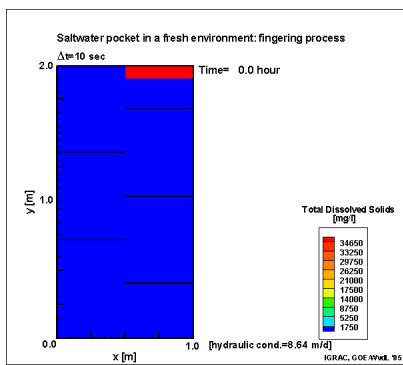
Concept 1: Fingering processes in the subsoil



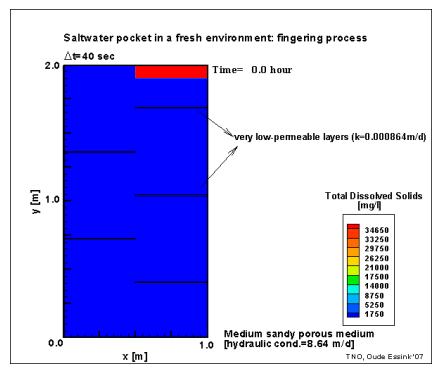
Concept 1: Fingering processes in the subsoil



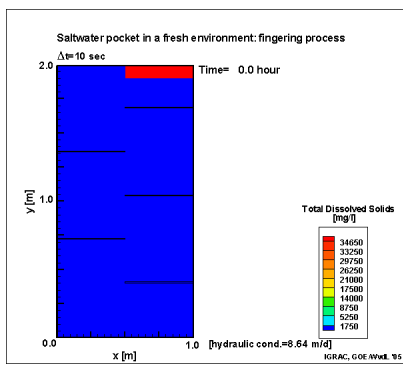
Concept 1: Fingering processes in the subsoil



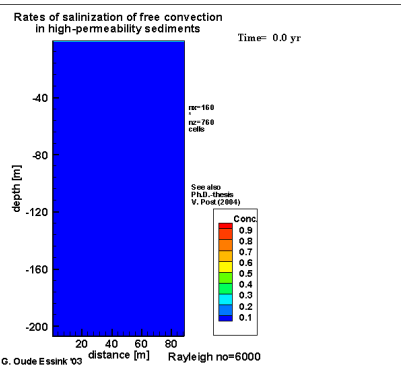
Concept 1: Fingering processes in the subsoil



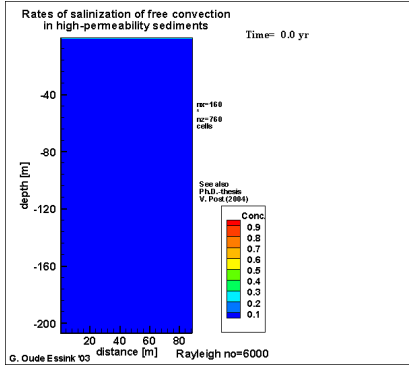
Concept 1: Fingering processes in the subsoil



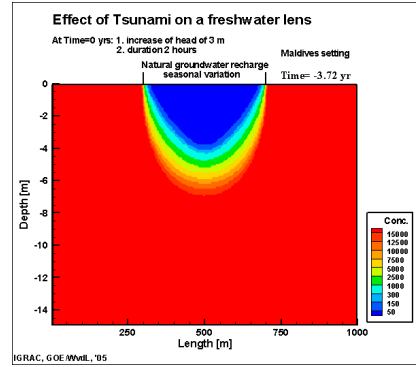
Concept 1: Fingering processes in the subsoil



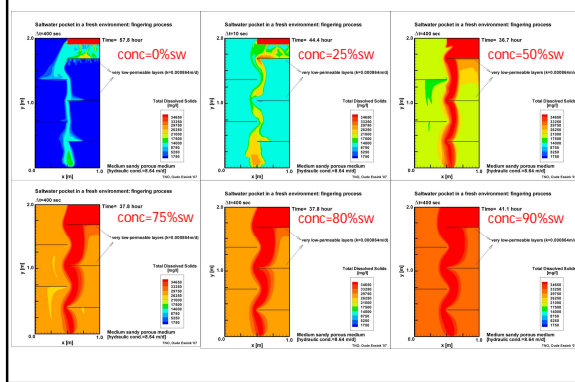
Concept 1: Fingering processes in the subsoil



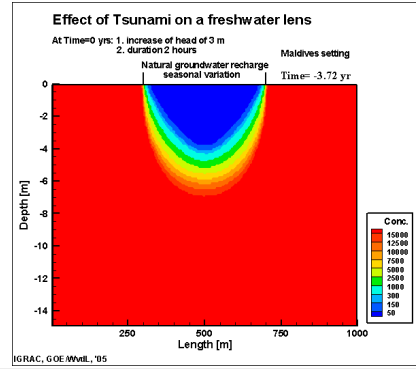
Concept 2: Evolution of a freshwater lens after flooding



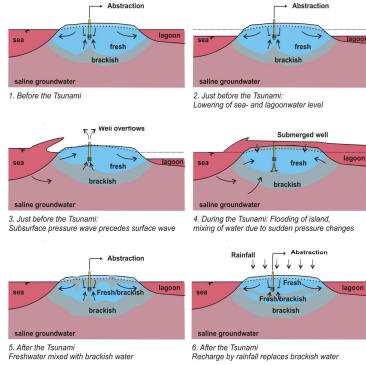
Fingering processes in the subsoil



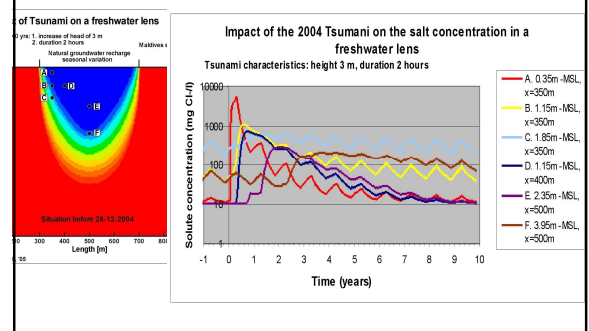
Concept 2: Evolution of a freshwater lens after flooding

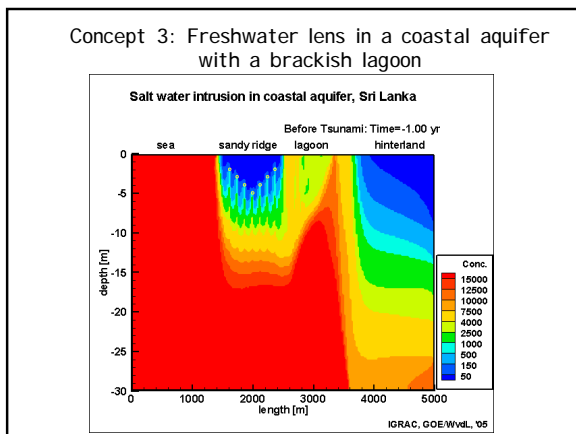
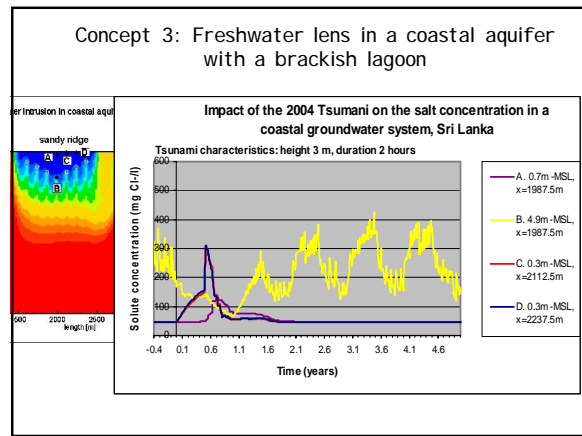
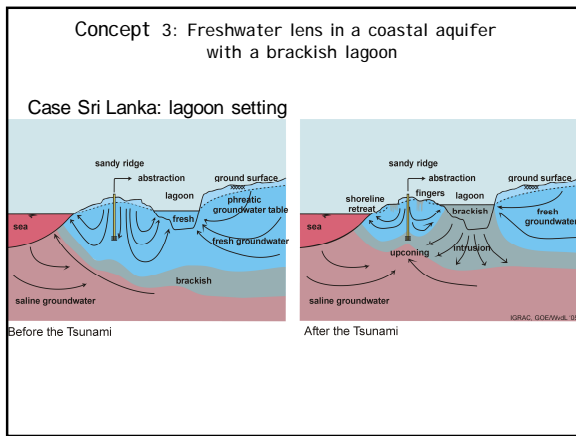


Concept 2: Evolution of a freshwater lens after flooding

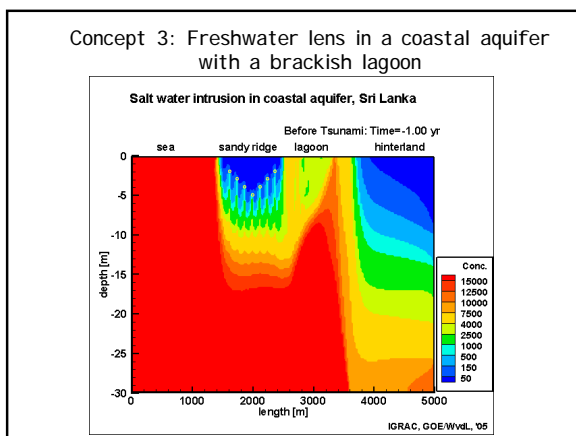


Concept 2: Evolution of a freshwater lens after flooding

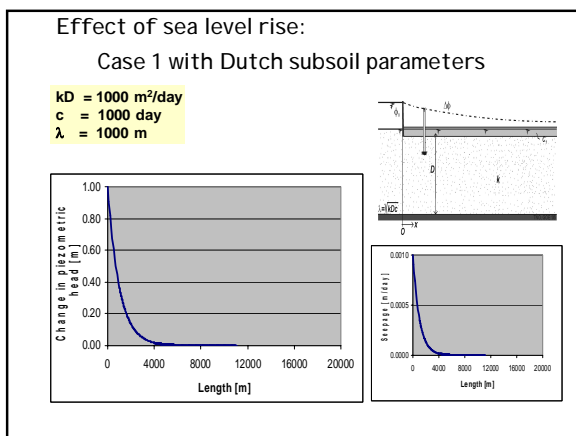
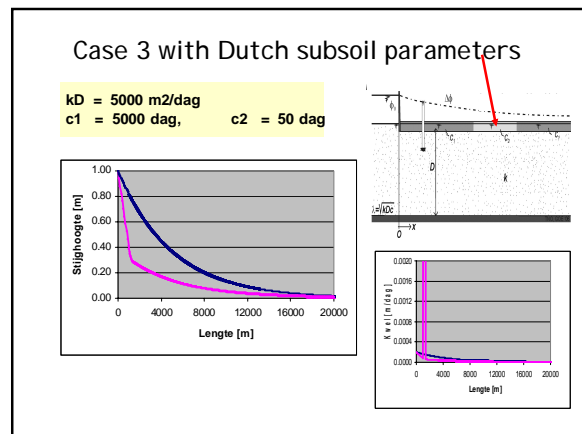
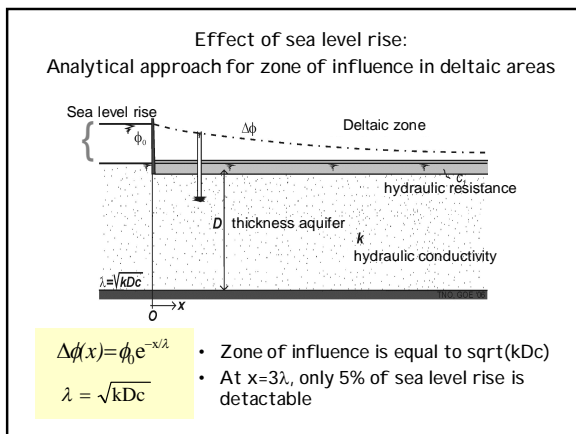
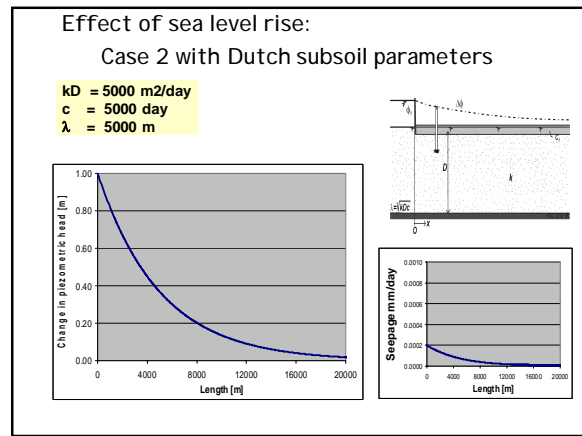
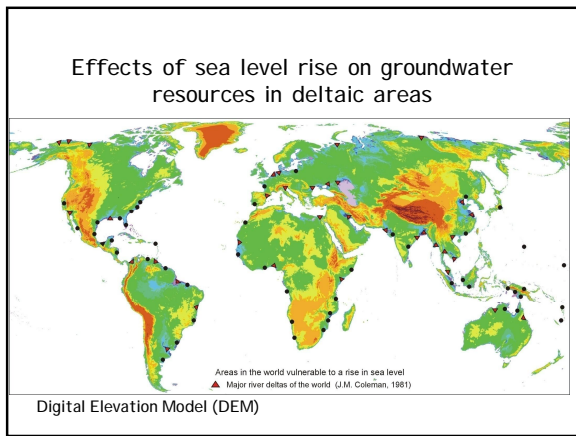


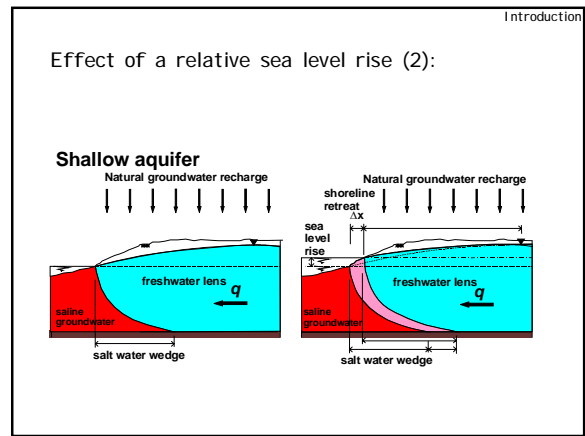
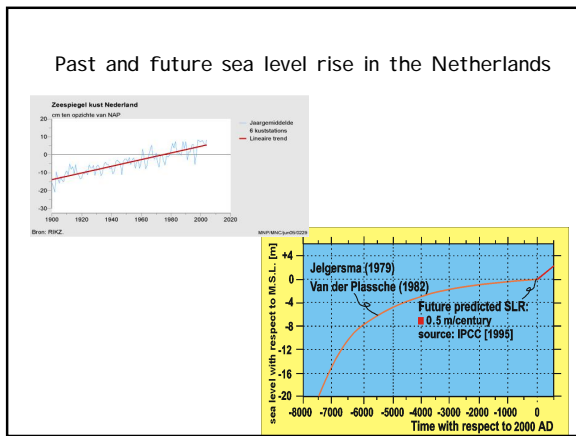


Effect sea level rise



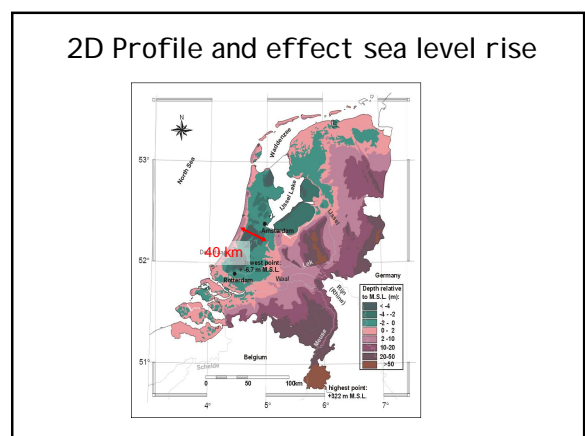
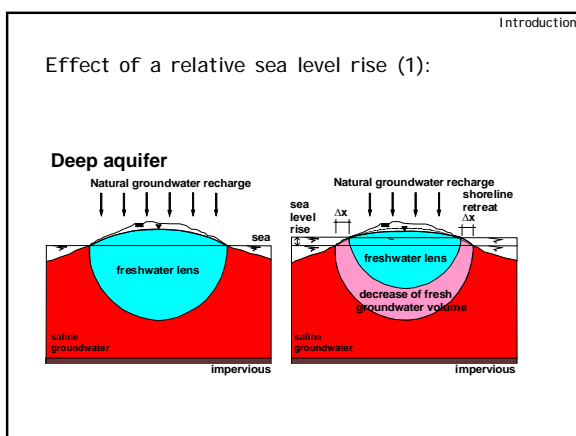
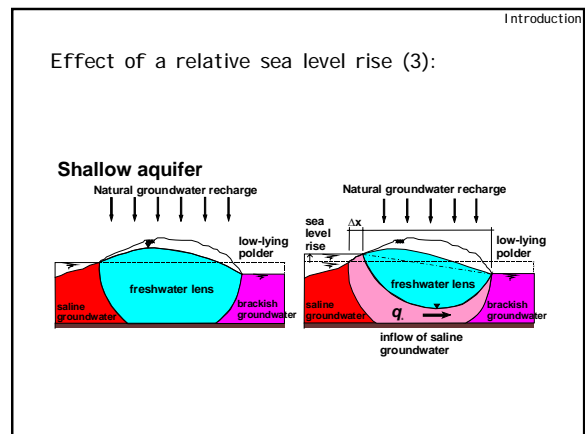
- Effects of sea level rise on groundwater resources in deltaic areas
1. Increase of salt water intrusion
 2. Increase of upconing under groundwater extraction wells
 3. Increase of piezometric head
 4. Increase of seepage and salt load to the surface water system
 5. Risk of instable Holocene aquitards
 6. [Decrease of fresh groundwater reservoirs due to decrease in natural groundwater recharge]

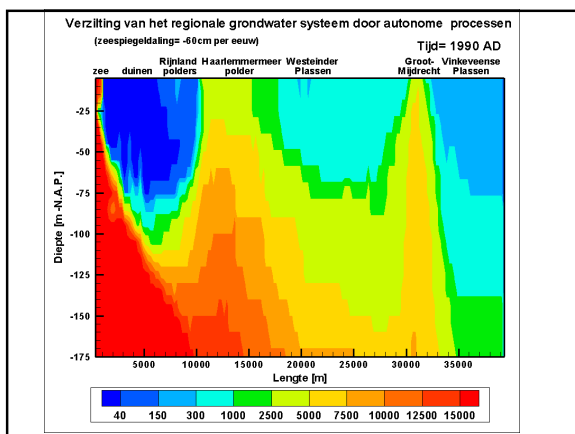
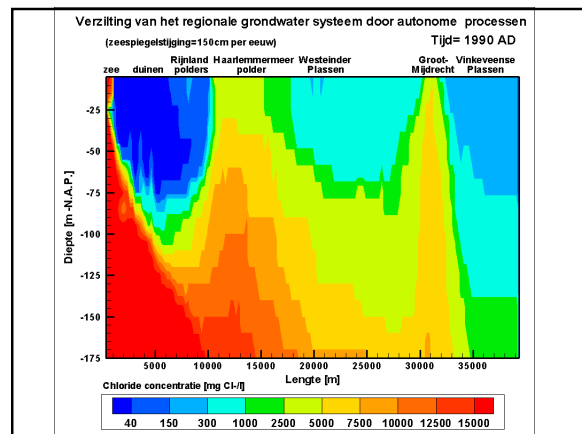
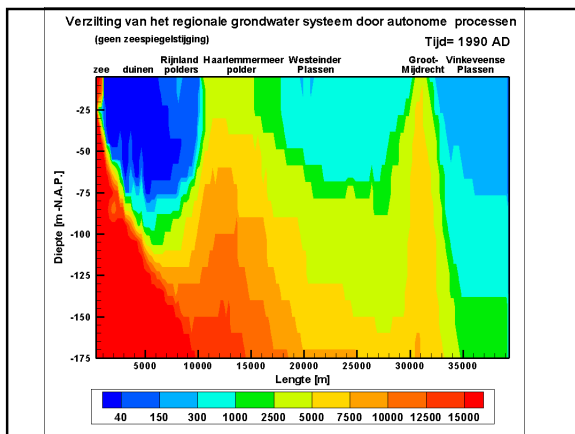
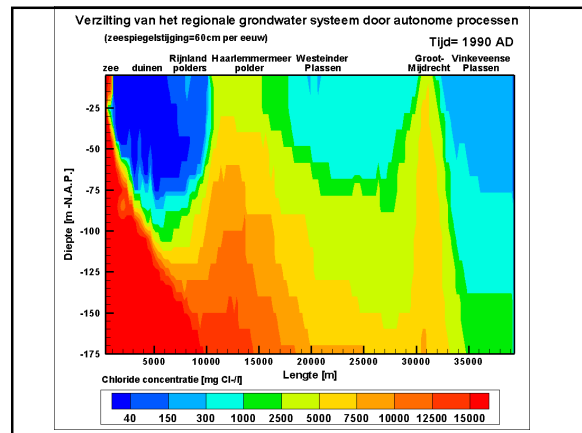
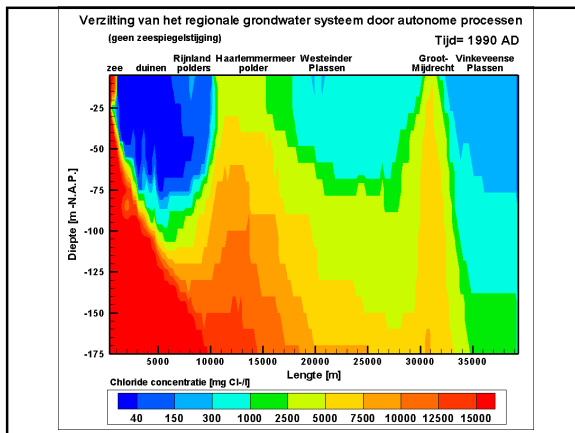




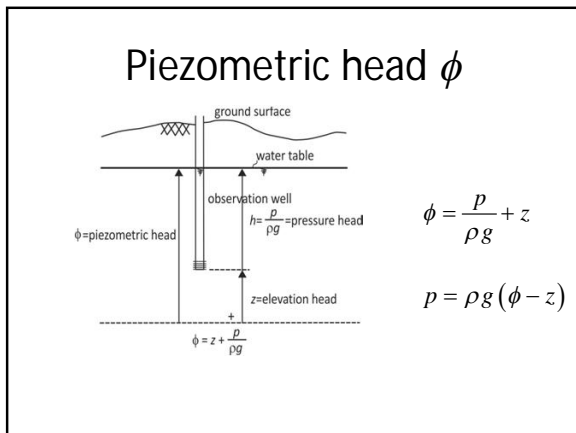
Implementing new KNMI 06 climate scenarios

2100	G	G+	W	W+	C	C+
Worldwide temperature rise in 2050	+1°C	+1°C	+2°C	+2°C	+3°C	+3°C
Worldwide temperature rise in 2100	+2°C	+2°C	+4°C	+4°C	+6°C	+6°C
Change in airstream pattern Western Europe	no	yes	no	yes	no	yes
Winter						
Average temperature	+1,8°C	+2,3°C	+3,6°C	+4,6°C	+5,4°C	+6,9°C
Coldest winter day each year	+2,1°C	+2,9°C	+4,2°C	+5,8°C	+6,3°C	+7,8°C
Average precipitation	7%	14%	14%	28%	21%	42%
Summer						
Average temperature	+1,7°C	+2,8°C	+3,4°C	+5,6°C	+5,1°C	+8,4°C
Hottest summer day each year	+2,1°C	+3,8°C	+4,2°C	+7,6°C	+6,3°C	+11,4°C
Average precipitation	6%	-19%	12%	-38%	18%	-57%
Sea level rise						
Absolute rise (cm)	35-60	35-60	40-85	40-85	45-110	45-110





Point water head
and
Freshwater head ϕ_f



Special case: hydrostatic pressure: $q_z=0$

$$q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right) \quad \text{no vertical flow}$$

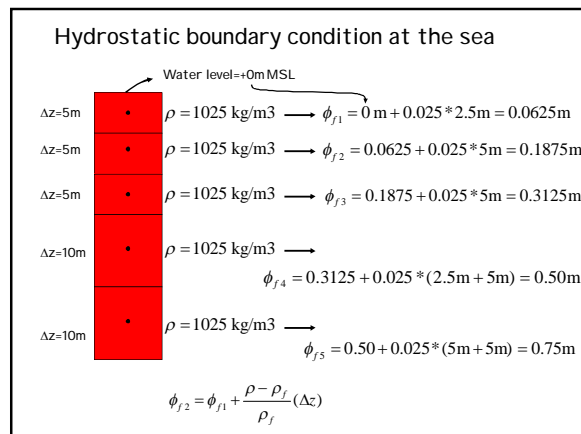
$$0 = \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$\frac{\partial \phi_f}{\partial z} = -\frac{\rho - \rho_f}{\rho_f} \frac{\partial z}{\partial z}$$

$$\phi_{f2} = \phi_{f1} - \frac{\rho - \rho_f}{\rho_f} (z_2 - z_1)$$

$$\phi_{f2} = \phi_{f1} + \frac{\rho - \rho_f}{\rho_f} (\Delta z)$$

- ### Freshwater head ϕ_f
- $$\phi_f = \frac{p}{\rho_f g} + z$$
1. Groundwater with different densities can be compared
 2. Fictive parameter
 3. Hydrologists like to use heads instead of pressures
 4. Pressure sometimes better
 5. Confusing (heads not perpendicular to streamlines)



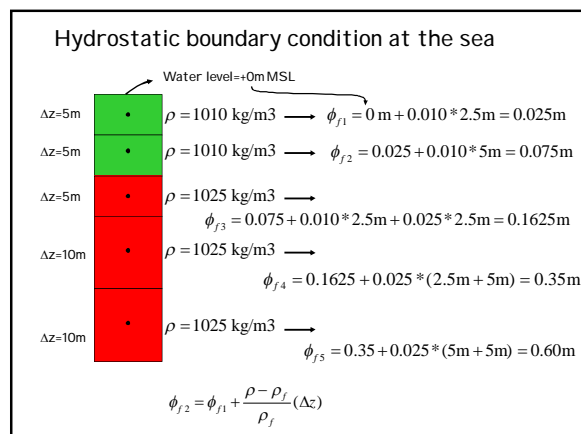
Freshwater head ϕ_f

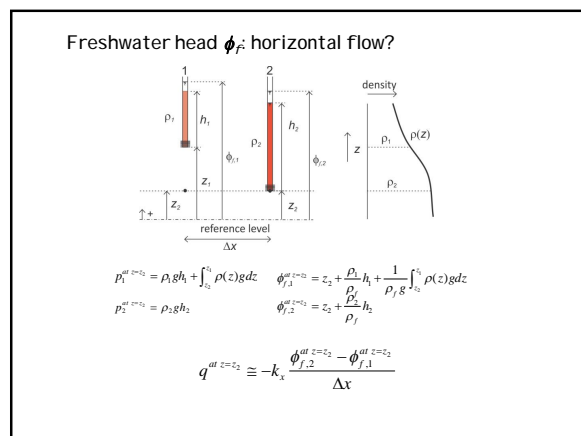
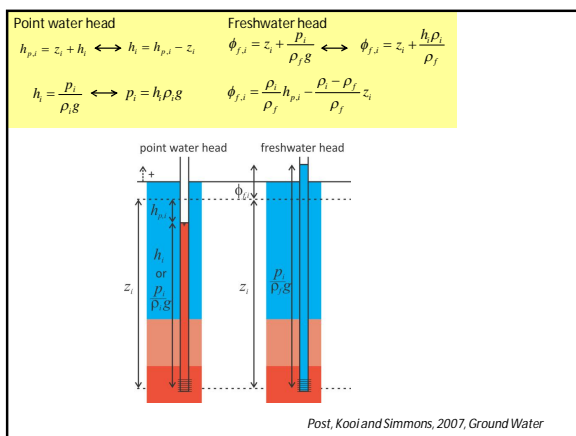
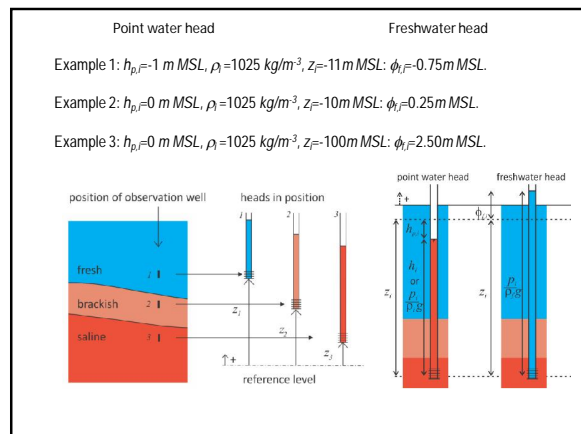
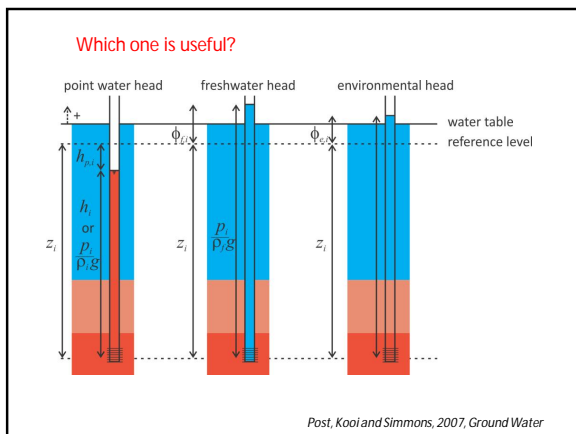
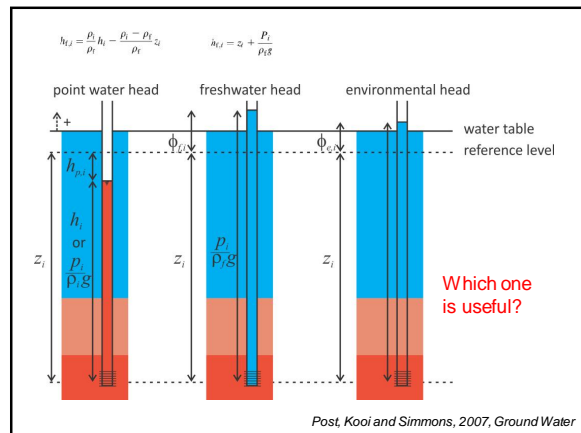
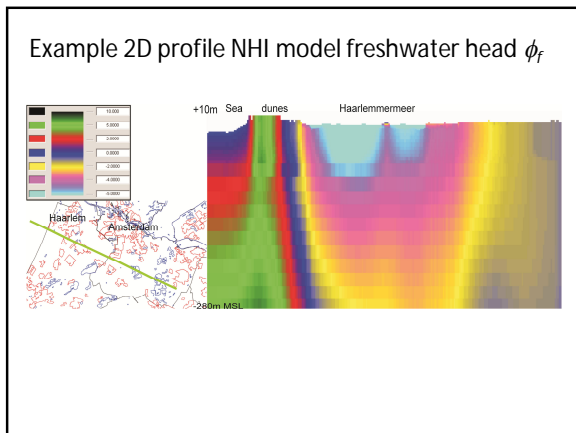
$$h_f = \frac{\rho}{\rho_f} h$$

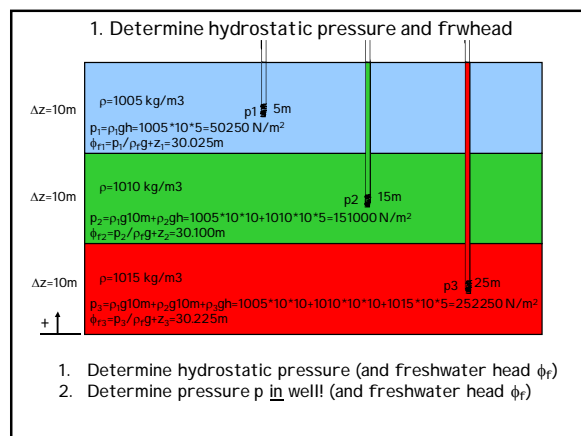
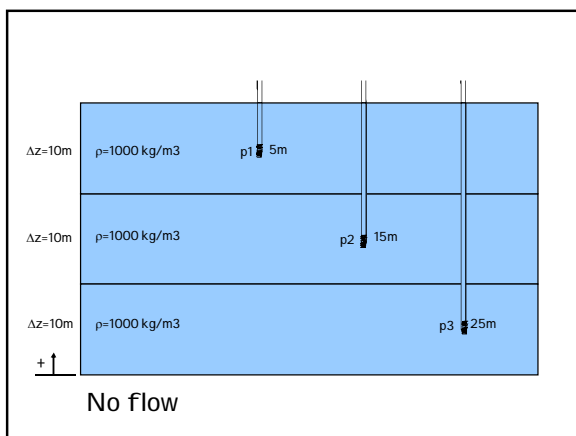
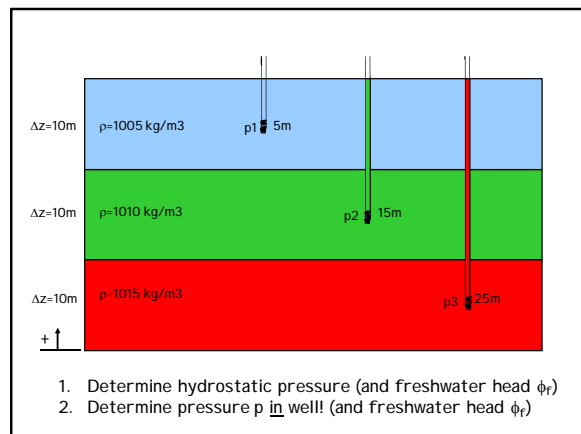
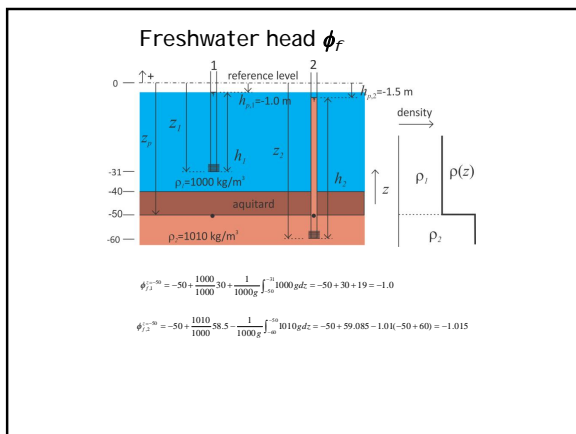
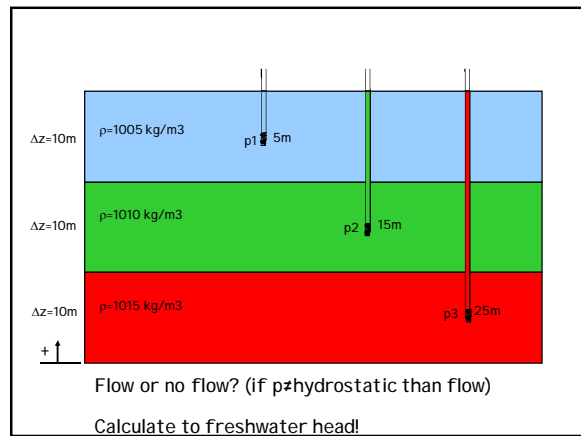
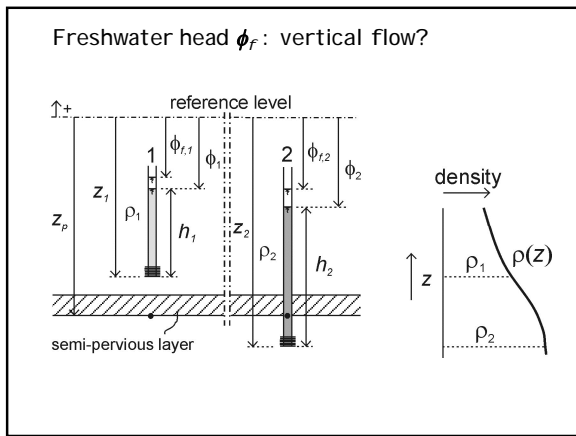
$$\phi_f = h_f + z$$

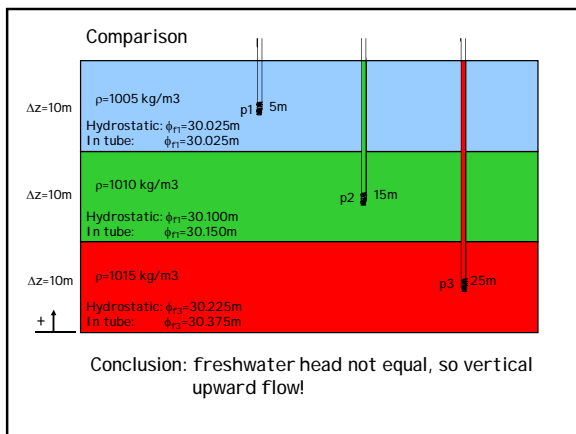
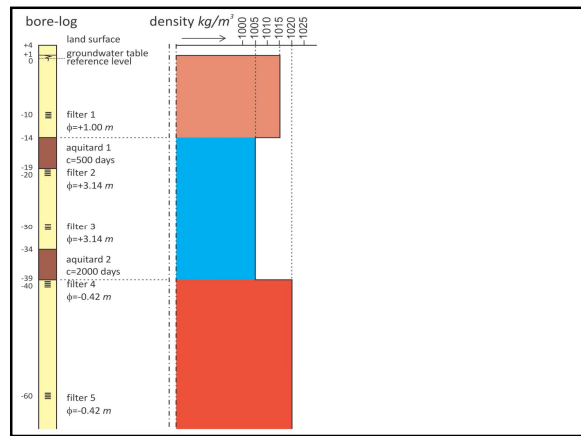
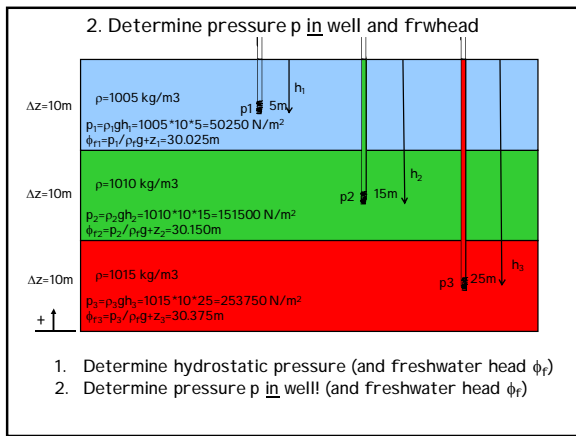
$$\phi_f = \frac{\rho}{\rho_f} h + z$$

e.g.:
 $\rho_s = 1025 \text{ kg/m}^3$
 $h = 10 \text{ m}$
 $\phi_f = 10.25 \text{ m}$



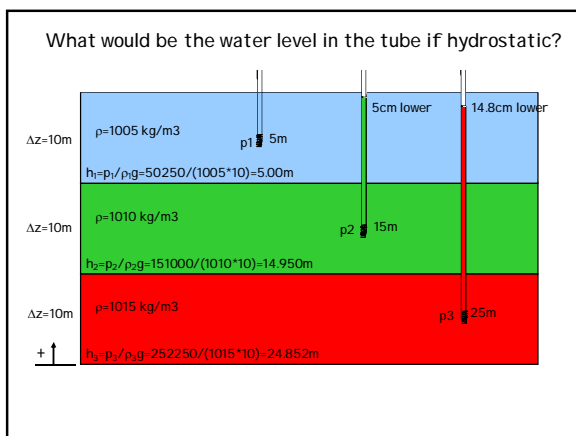




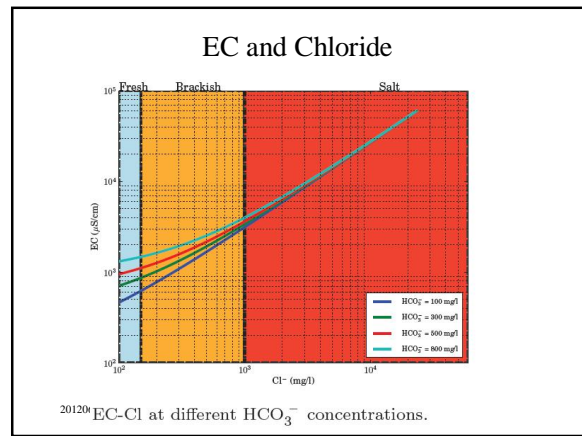
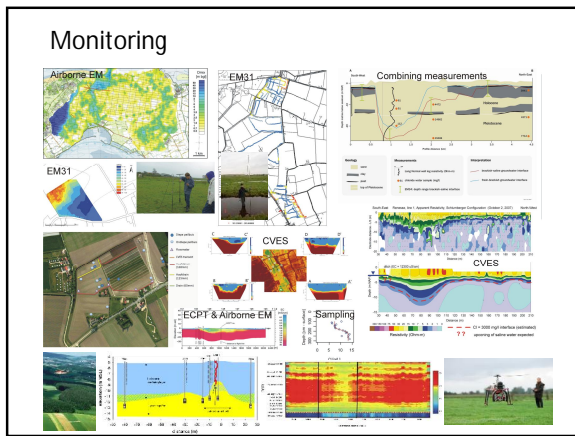


Take home message

- In coastal area (with fresh-brackish-saline groundwater), always measure head and Electrical Conductivity (EC)
- Convert EC to density
- Determine freshwater head with lecture notes and ppt
- Determine flow



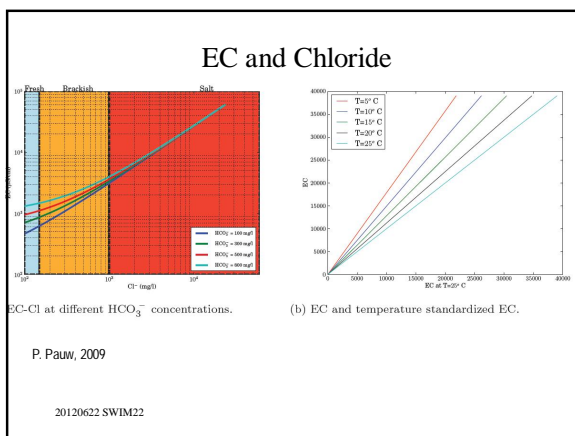
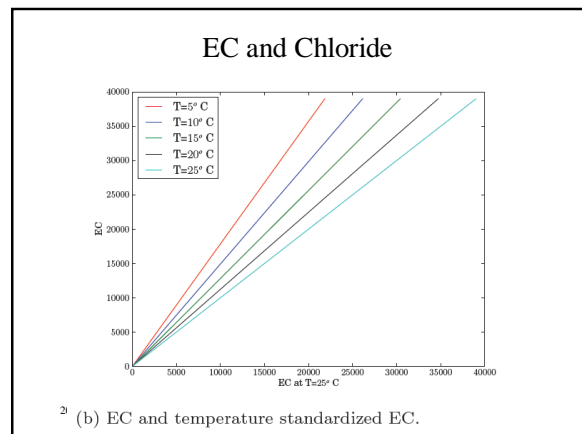
Monitoring



Monitoring salt in groundwater

- Why monitoring?
 - Mapping salt concentrations in the groundwater
 - Detection of trends (upconing near pumping stations)
 - System and process knowledge
 - Input for a groundwater model
- Methods:
 - Direct: water sample available
 - Indirect: conductance of the subsol

Source: V. Post, 2007



Airborne measurements

Measuring system	Physical parameter	Geology/terrain information
radar	EM traveltime	Terrain elevation
Infrared photography	Infrared radiation	Surface temperature
Time domain EM Frequency domain EM	Electr. resistivity from induced EM fields	Lithology Water salinity
Magnetic gradiometer	Magnetic field (variations)	Lithology (magnetite) Artefacts Steel/Iron objects
Spectral gamma	Radiation (gamma)	Soil type Surface lithology Recent disturbance

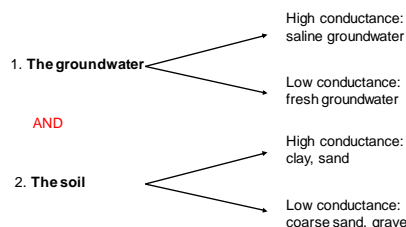
Source: Koos Groen

Surface measurements

Measuring system	Physical parameter	Geology/terrain information
Ground penetrating radar	EM travelttime, diaelectric constant,	Lithology Soil moisture
ERT	Electr. resistivity	Lithology Water salinity
Time domain EM Frequency domain EM	Electr. resistivity	Lithology Water salinity
Magnetometer (total field, gradiometer)	Magnetic field (variations) magnetic susceptibility	Lithology (magnetite) Artefacts Steel/Iron objects (UXO)
Spectral gamma	Radiation (gamma)	Soil type Surface lithology Recent disturbance

Monitoring salt in groundwater: Indirect methods

Indirect methods measure the **conductance** of:



Hence information about the lithology (sand, clay etc) is needed!

Source: V. Post, 2007

Cone Penetration Tests

Measuring system	Physical parameter	Geology/terrain information
mechanical CPT	Cone resistance Friction resistance	Lithology Geotechnical parameters
Electrical conductivity	Electrical formation conductivity	Water salinity
Continuous water pressure	Water pressure	Lithology Piezometric head
Water pressure dissipation in clay layers	Water pressure in time	Permeability clays
BAT sampling in CPT casing		Water chemistry
ROST, MIP		Contamination of hydrocarbons (high concentration)
Camera sonde	Visual view	Lithology, contamination, gas

Source: Kees Groen

Monitoring salt in groundwater: Indirect methods

Method	Advantages	Disadvantages
1. Electrical conductance measurements	•High resolution (3D) •Depth ~200 m	•Time consuming
2. Electromagnetic measurements	•Fast	•Limited vertical resolution •Sensitive for underground conductors (pipes)
3. Satellites	•Suitable for large areas	•Small vertical resolution •Low accuracy

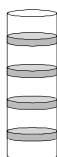
Source: V. Post, 2007

Monitoring salt in groundwater: Direct methods

Method	Advantage	Disadvantage
1. Observation well	•High accuracy •Detection trends	•Costly •Point measurement
2. Well screens in observation well	•High accuracy •Detection trends •High vertical resolution	•Costly
3. Sediment sample (extraction milliliters of water)	•High accuracy •High vertical resolution	•Very costly and time consuming



Direct methods 1 and 2

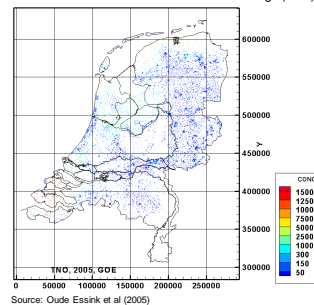


Source: V. Post, 2007

Method used at Deltares

- Combination of:
- Direct measurements
 - Electrical conductance measurements
 - Surface (VES)
 - Borehole

Number of measurements bottom Holocene top layer: direct methods and Vertical Electric Soundings (VES)



Source: Oude Essink et al (2005)

Electrical conductance measurements

1. Measuring:

- Inside a borehole
- From surface level
- From the air

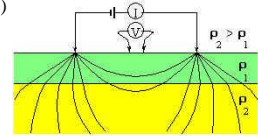


Source: TNO

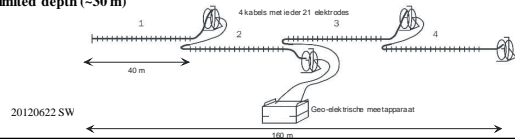
Source: V. Post, 2007

Types geo-electrical measurements

- I Vertical Electrical Sounding (VES)
- 4 electrodes at surface
- 1D electrical resistivity profile
- Labor intense
- Accurate, great depths
- Deep hydrogeology



- II Continue Vertical Electrical Sounding (CVES)
- >80 electrodes at surface
- 2D electrical resistivity subsurface
- Limited depth (~30 m)



20120622 SW

Electrical conductance measurements

1. Measuring:

- Inside a borehole
- From surface level (depth ~ 200 m)
- From the air



Source: Vitens

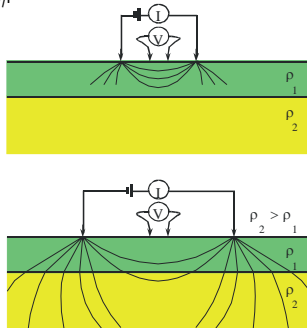
Source: V. Post, 2007

VES measurement end 1950s/begin 1960s



Principle geo-electrical measurement

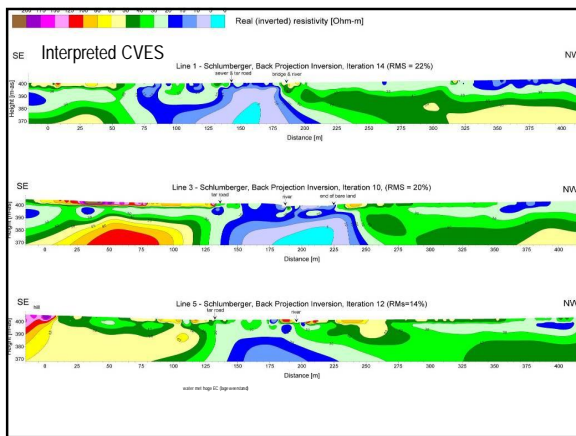
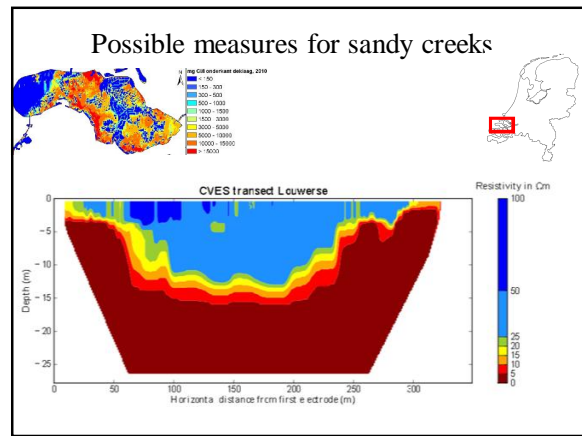
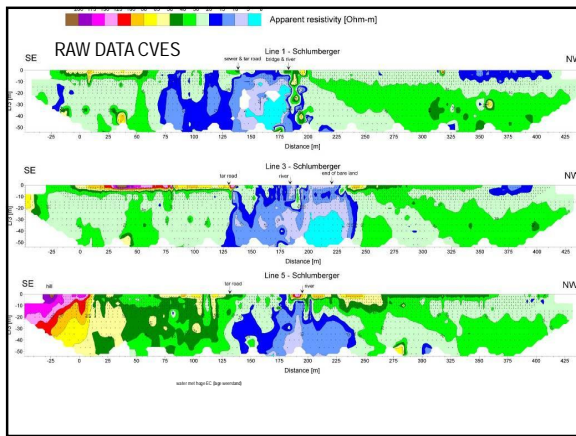
I: currentelektrode, V: potentialelektrodes, Ra: appearant electrical resistivity
 $R_a = \text{constant} \cdot V/I$



20120622 SWIM22

CVES measurements 2010s



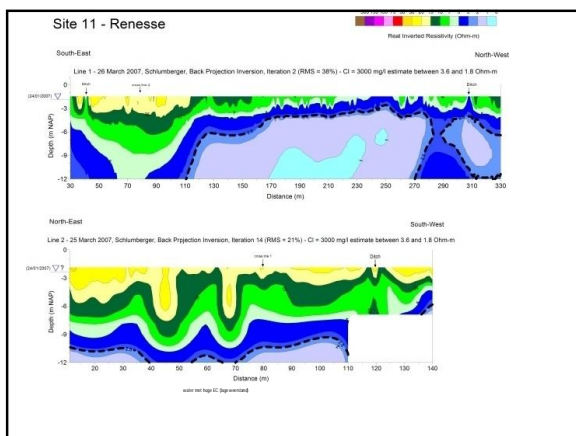


Electrical conductance measurements

1. Measuring:

- Inside a borehole
- From surface level
- From the air

Source: V. Post, 2007



Monitoring salt in groundwater: Indirect methods

- Electrical conductance measurements

$$\rho_s = F \cdot \rho_w$$

ρ_s = resistance subsoil & groundwater
 ρ_w = resistance groundwater
 F = formation factor

Lithology	F
Gravel with sand	7
Coarse sand	5
Sand with silt	2-3
Clay	1-3*
peat	1*

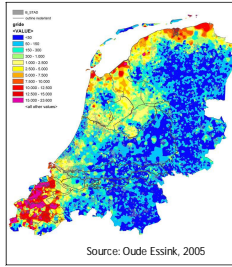
F varies with the resistance of the groundwater

If the lithology is known AND the measurement is in an aquifer
→ ρ_w can be calculated

VES measurements are used in combination with borehole logging

Source: Oude Essink, 2005

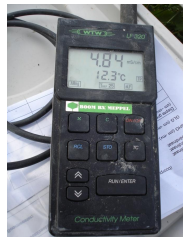
Result: chloride concentration bottom Holocene toplayer



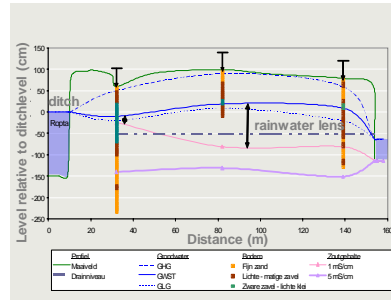
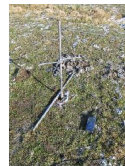
- Software Geological Survey of the Netherlands (TNO) is used to determine the salt concentration of the groundwater in the measurements
- Inter- and extrapolation is used to make a continuous field
- 2D Result is an combination of:
 1. Direct measurements (3500)
 2. Electrical conductance in boreholes (2000)
 3. Vertical Electric Sounding (VES) measurements (10.000)



T-EC probe

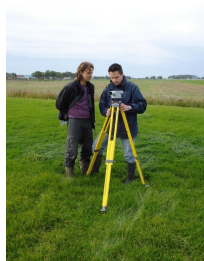


Use field measurements to understand the process

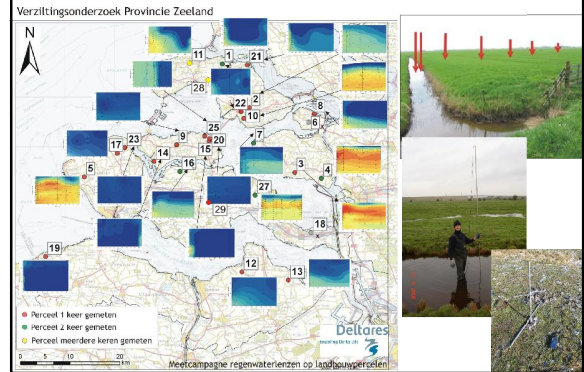


T EC fieldwork

Altitude measurements



TEC-probe Monitoring campaign 2005-2009



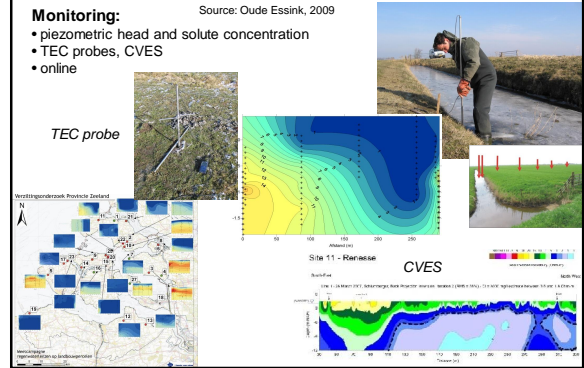
CliWat www.cliwat.eu

- Transnational project in the North Sea Region
- Main objectives:
 - to evaluate the physical and chemical impacts of climate change on groundwater and surface water systems
 - to provide data for adaptive and sustainable water management and infrastructure.
- Different innovative monitoring techniques (Helicopter EM, CVES, CPT, TEC-probe) are used to map the salinization status of the coastal groundwater system.

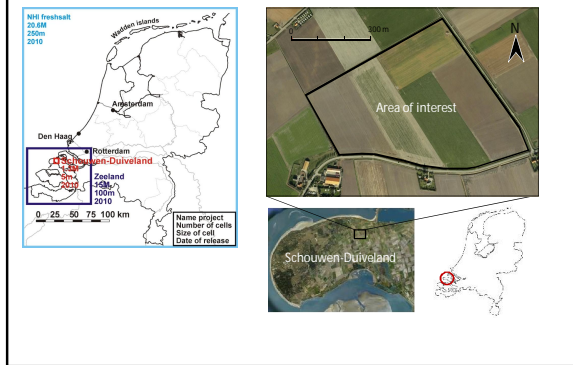


Example: Assessing effect of climate change on salt water intrusion

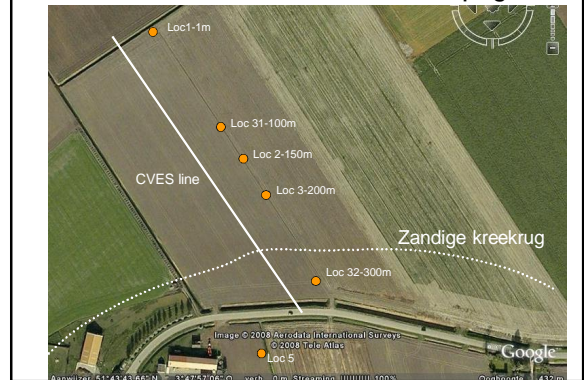
- Source: Oude Essink, 2009
- Monitoring:**
- piezometric head and solute concentration
 - TEC probes, CVES
 - online



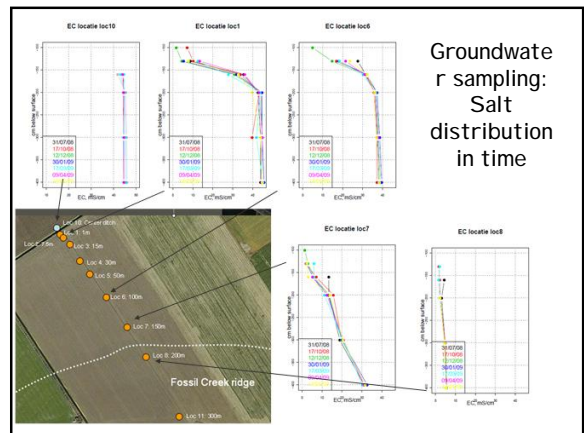
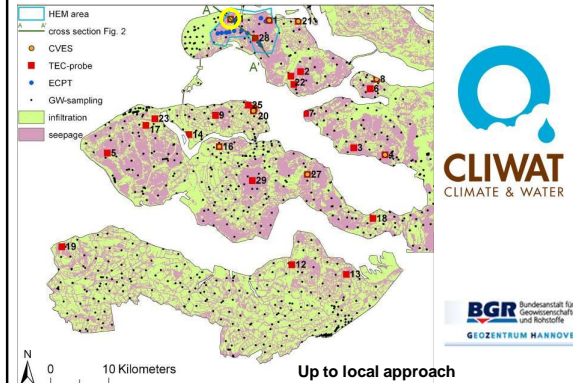
Description local area



Site 11: from infiltration to seepage

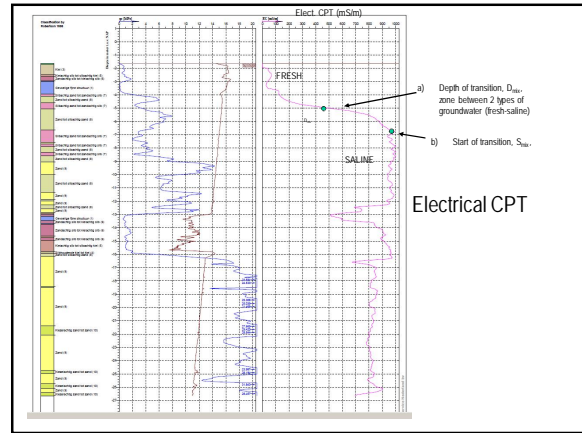
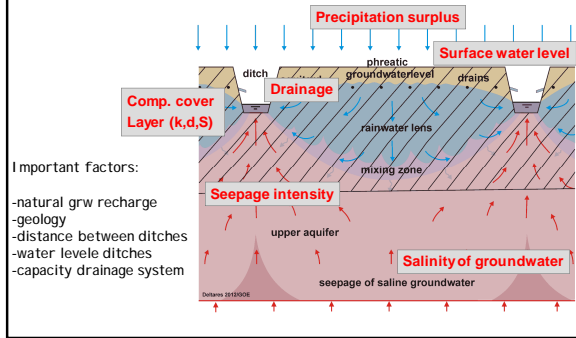


Monitoring network in our Pilot Area Zeeland

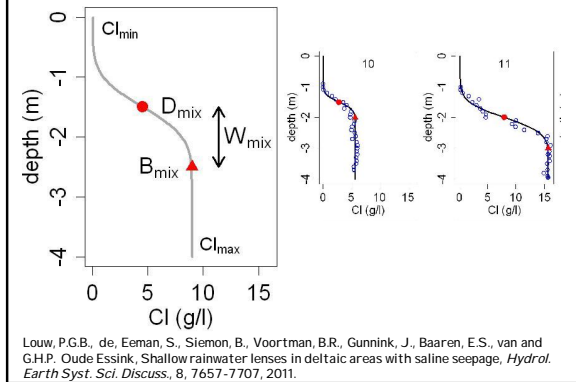


Groundwater sampling:
Salt distribution in time

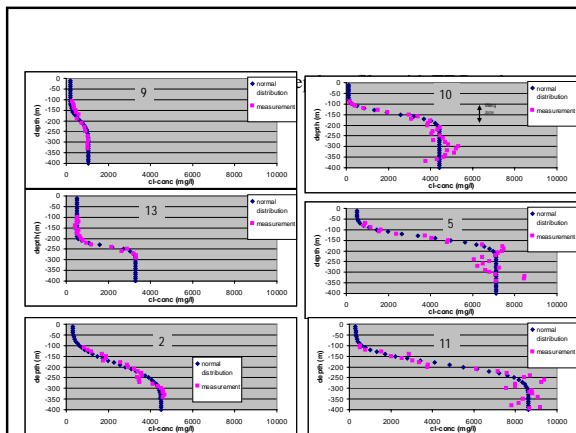
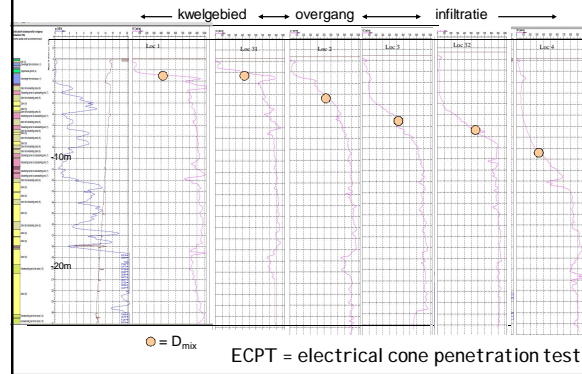
Factors controlling fresh-salt interface



Lens characteristics

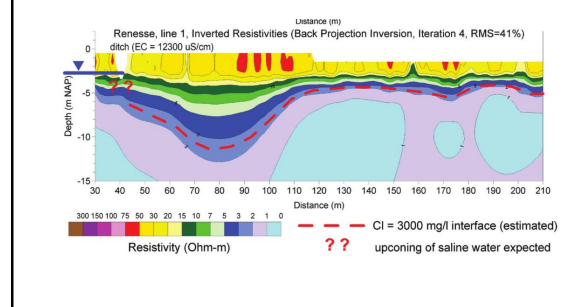


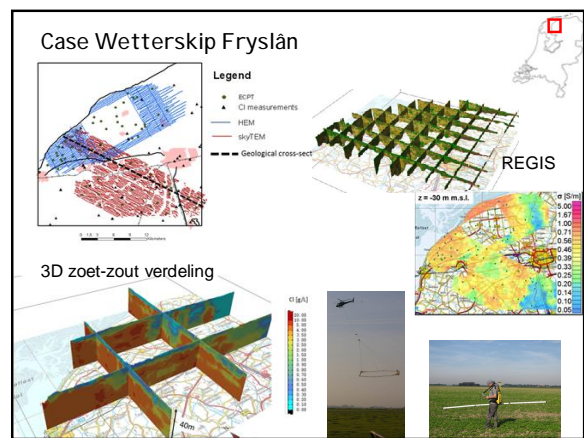
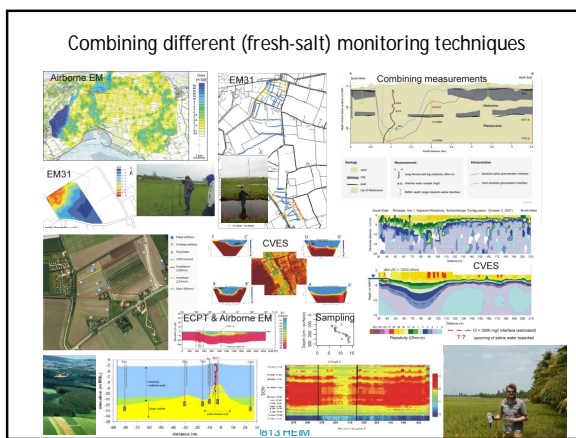
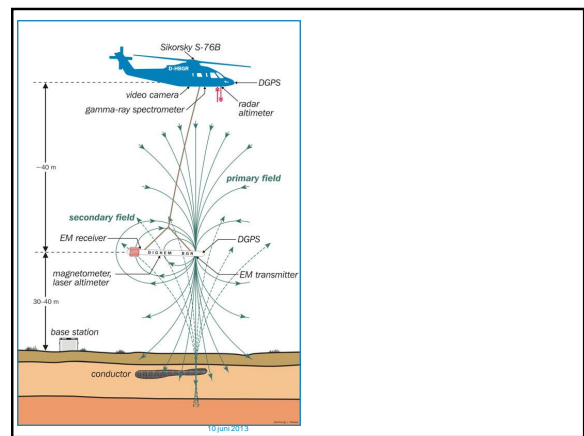
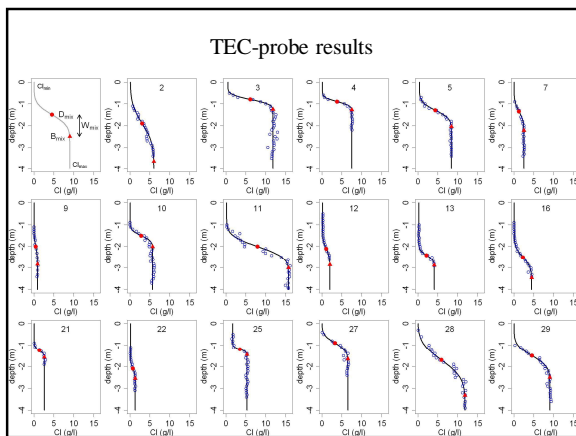
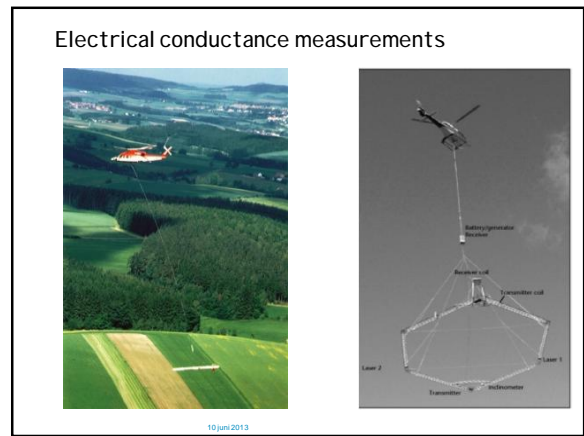
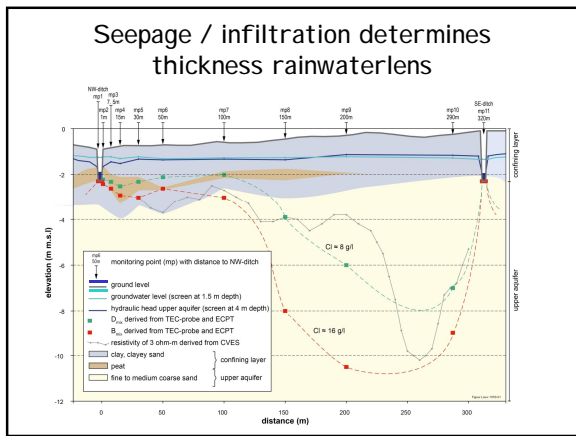
Results from ECPT's (soundings)

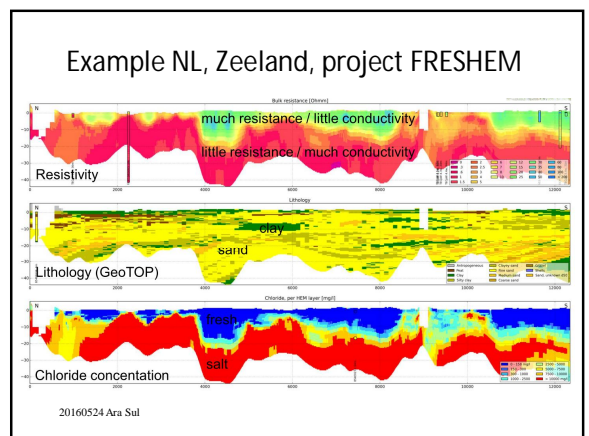
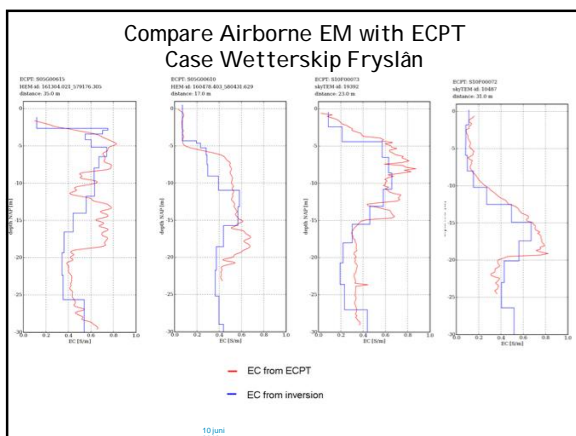
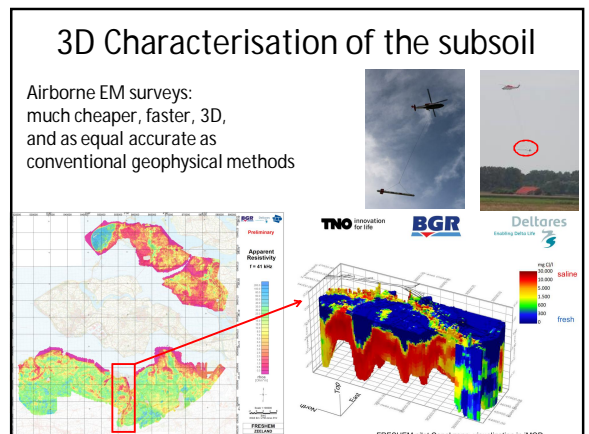
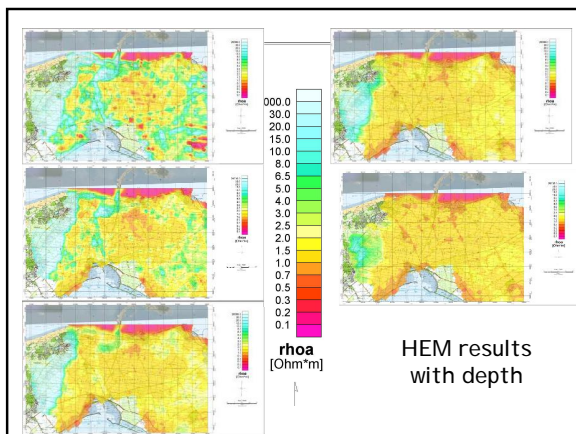
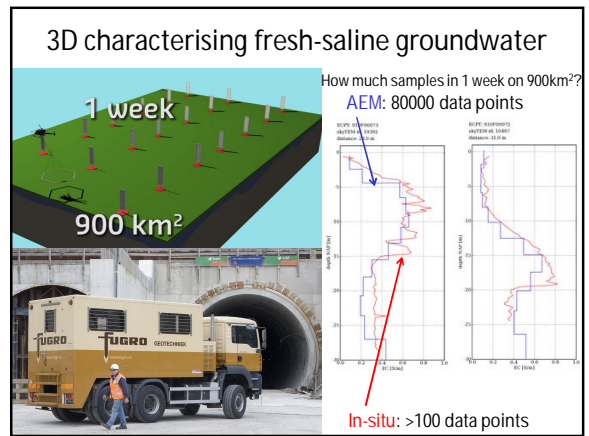
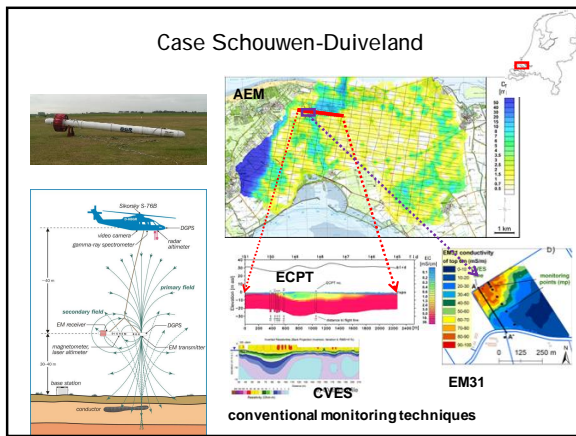


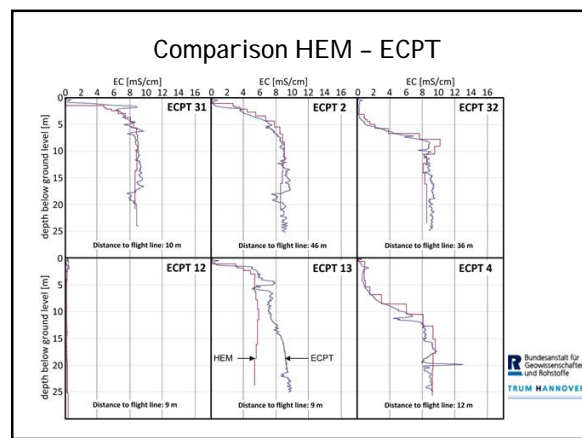
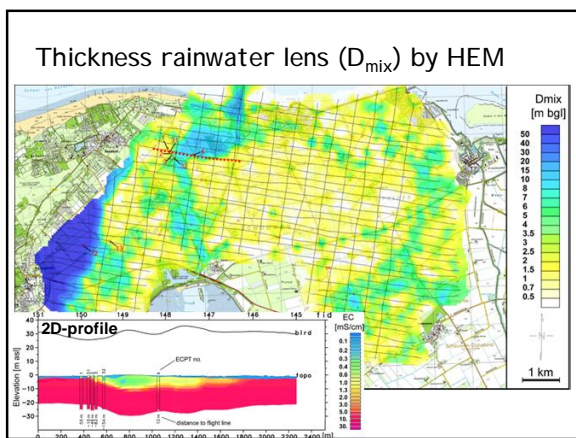
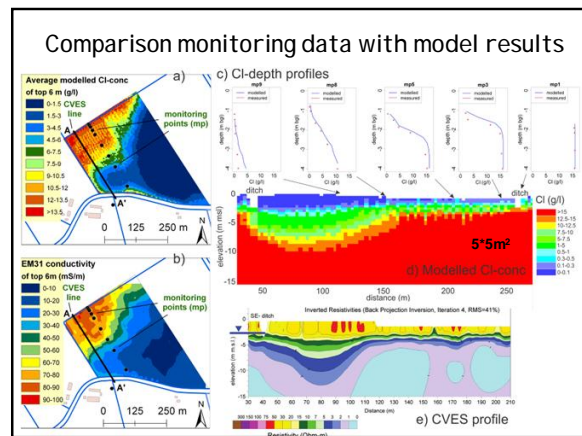
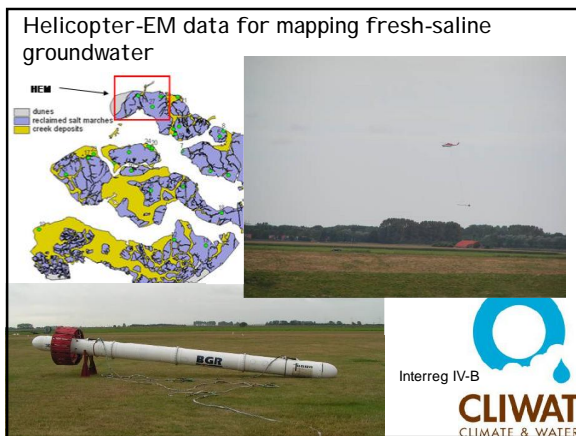
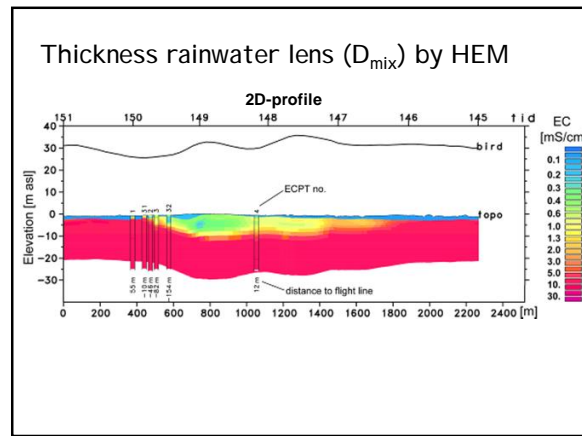
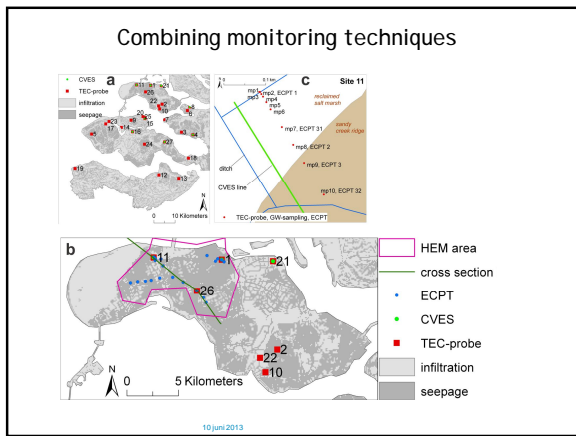
CVES

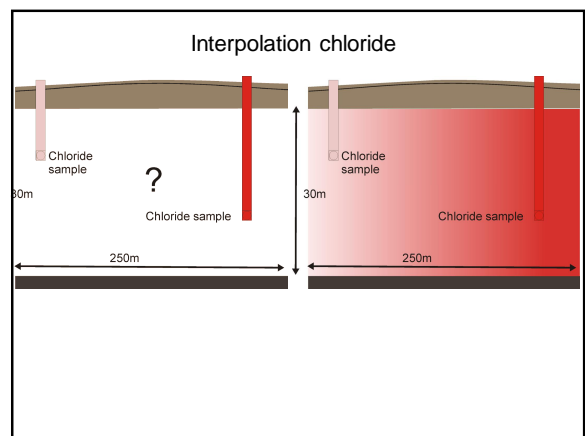
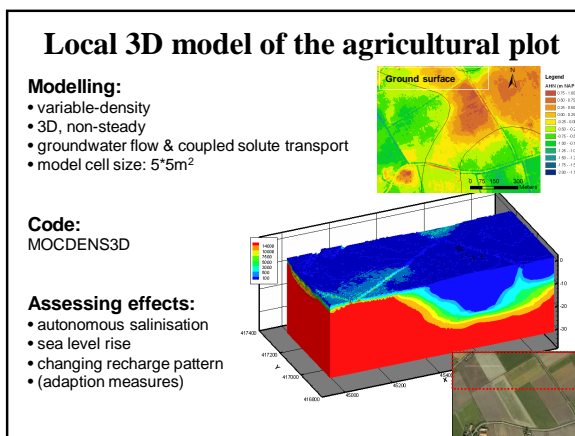
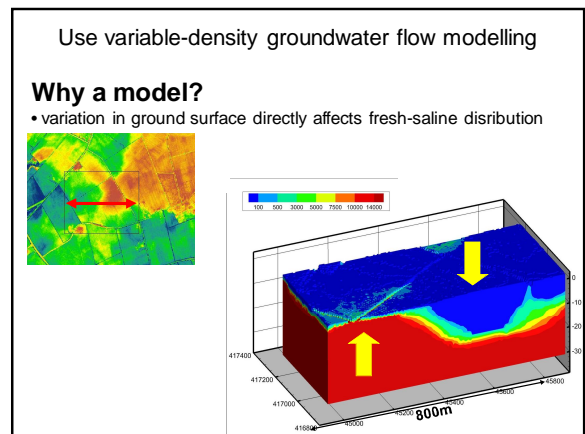
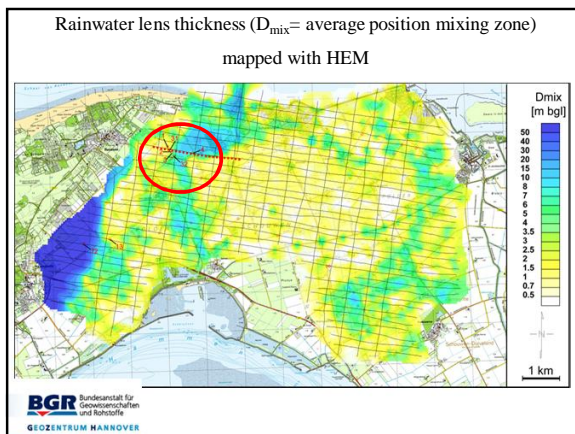
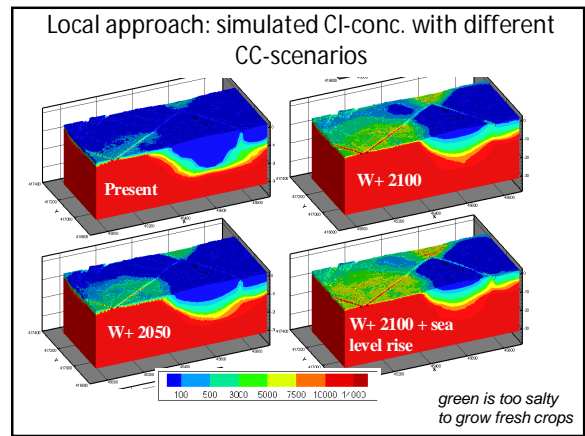
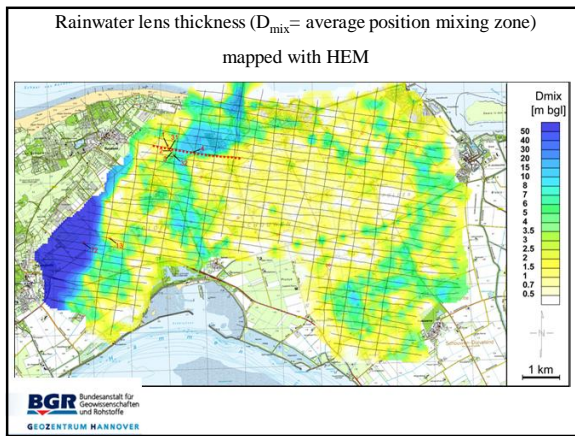
CVES: continuous vertical electrical sounding

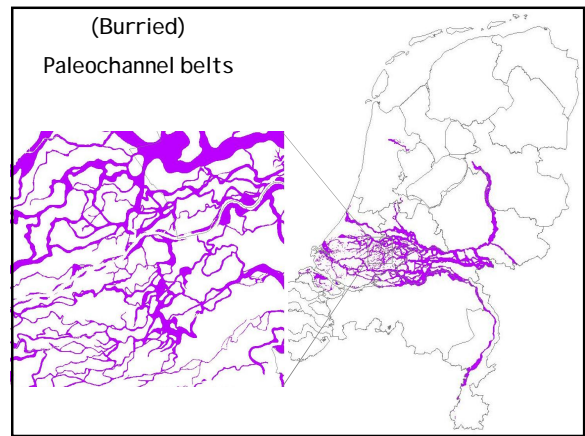
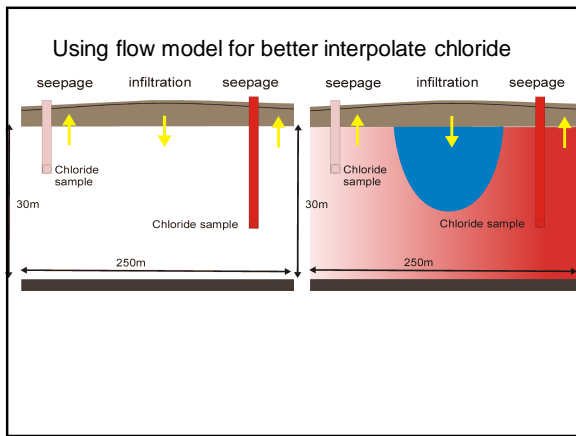






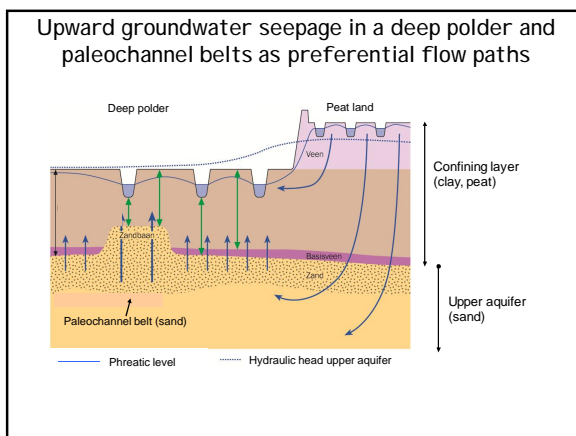
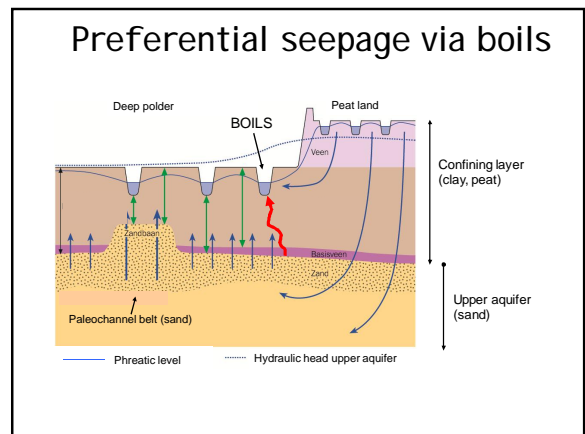






Salty boils

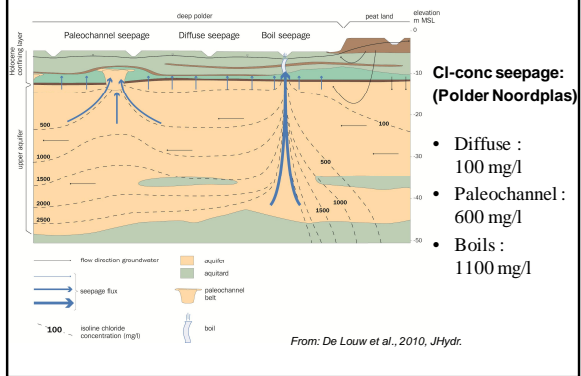
Louw, P.G.B., de Oude Essink, G.H.P., Stuyfzand, P.J., Zee, van der, S.E.A.T.M., 2010, Upward groundwater flow in boils as the dominant mechanism of salinization in deep polders, The Netherlands, J. Hydrol. 394, 494-506.

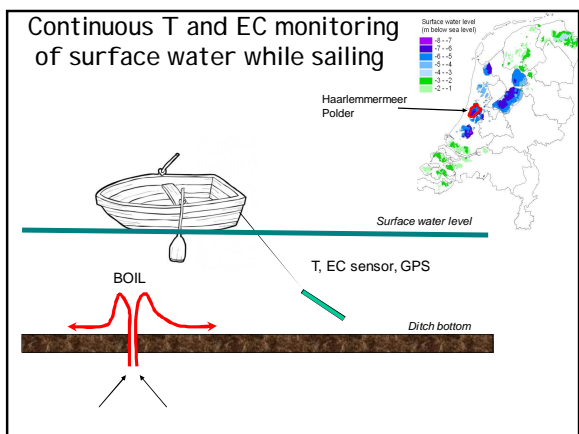
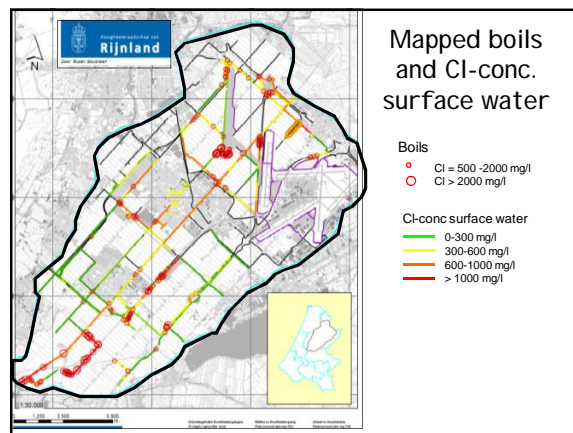


Preferential saline seepage via boils



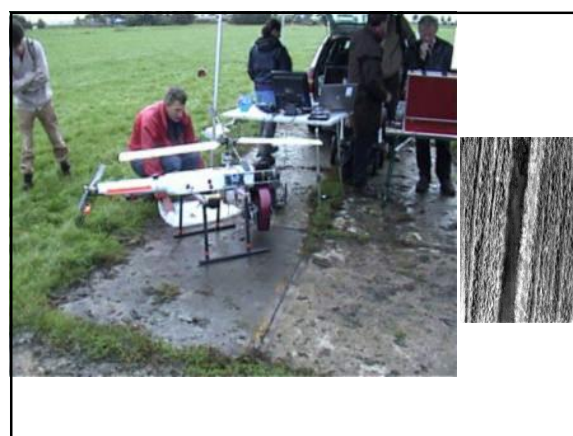
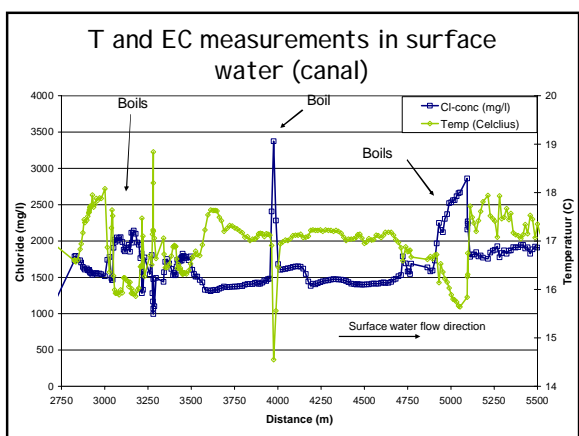
Three types of upward groundwater seepage



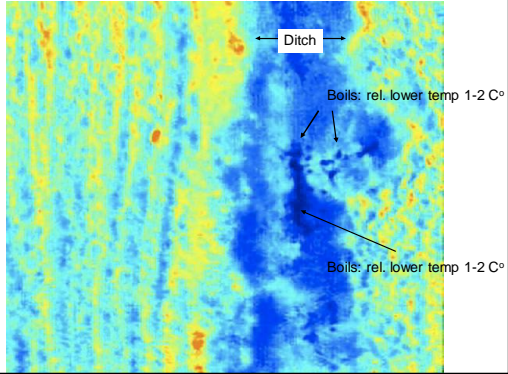


LARS technology (TNO Industry): Thermal Infra-red

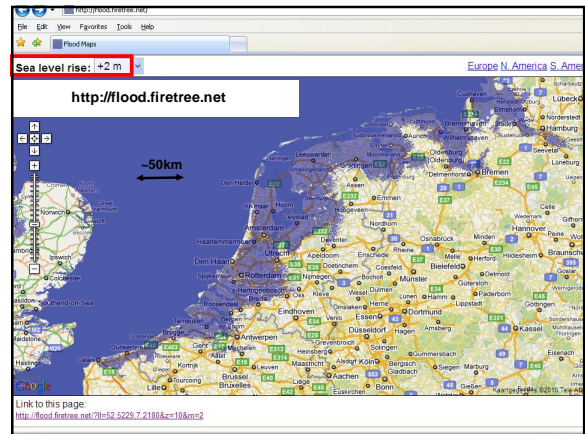
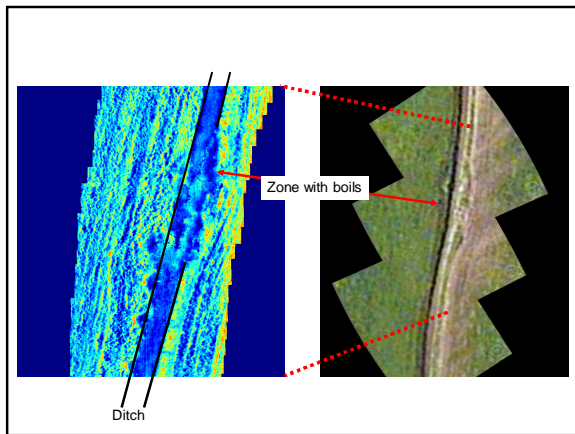
- Altitude: 0-150 m
- Temp-detection using Thermal Infra Red sensors (only surface !)



Thermal infra-red results (blue is cold, red is warm)



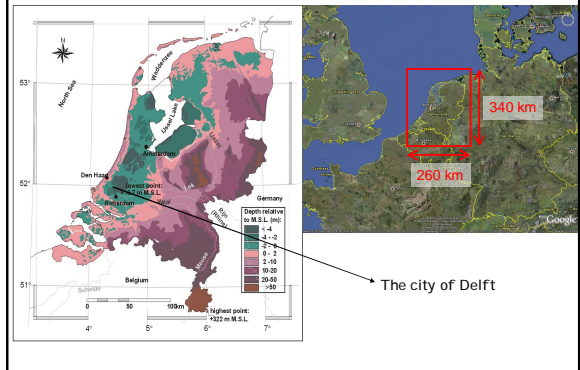
Salt water intrusion in the Netherlands



To get an idea about the possible future effects of sea level rise and climate change in your delta ...

evaluate of the past water management in the Dutch delta

The 'low-lying lands: Netherlands



Case study: The Netherlands

The Dutch coastal zone is already theathened by sea level rise and land subsidence for many centuries

Intensive water management system

Coping with salt water intrusion problems since 1950's



Infrastructure to protect our low-lying land from flooding



The 'low-lying' lands: Netherlands

The facts:

- a deltaic area with 3 rivers: Meuse, Scheldt & Rhine
- 25% of land surface is lying below mean sea level
- 65 % would be flooded regularly if there were no dunes and dikes
- 8 million people would be endangered



River flooding in 1995

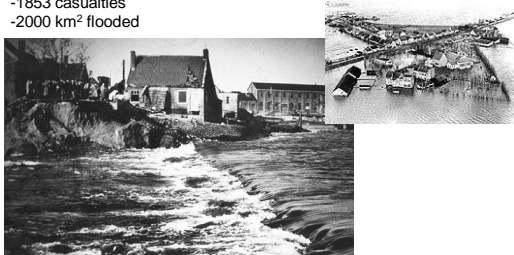
Combination of heavy rains upstream the catchment & short retention time



The Great Flooding in february 1953

Combination of high tide and heavy storm:

- 1853 casualties
- 2000 km² flooded



Dike collapse 2003

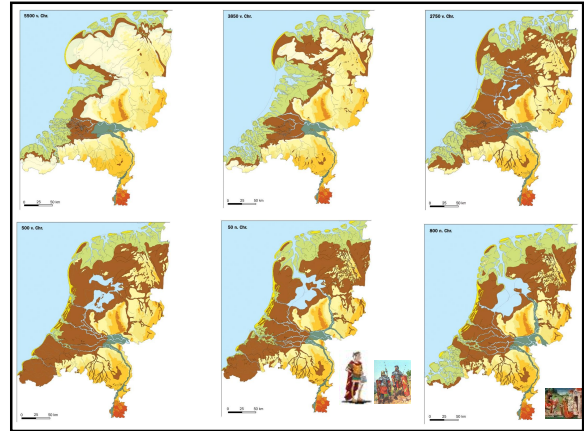
Combination of peat dike instability and very dry summer



Estimated water management costs 'to keep our feet dry'

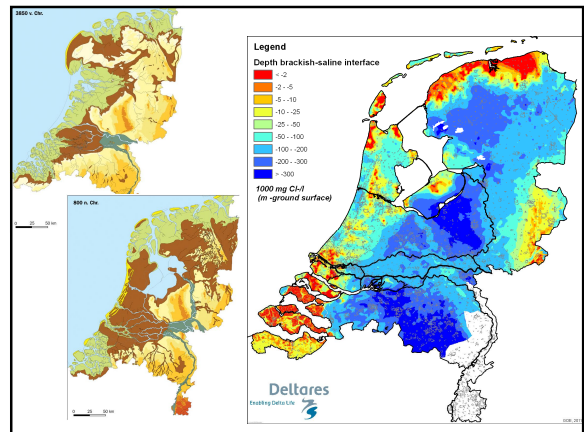
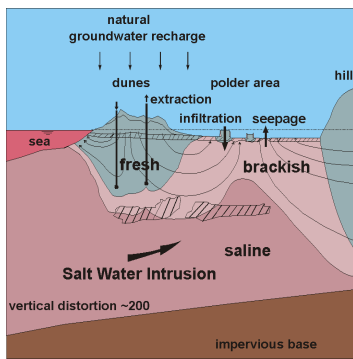
Costs up till 2050 in billion euros:

rivers: upper part	5.7
rivers: lower part	5.6
low-lands	1.7
coastal zone	8.0
infrastructure	3.5
purchase of ground	2.0
	-----+
	26.5 billion euros

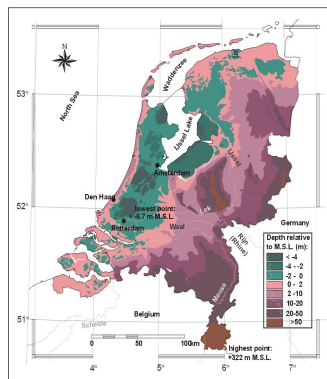


Salt water intrusion in the Netherlands

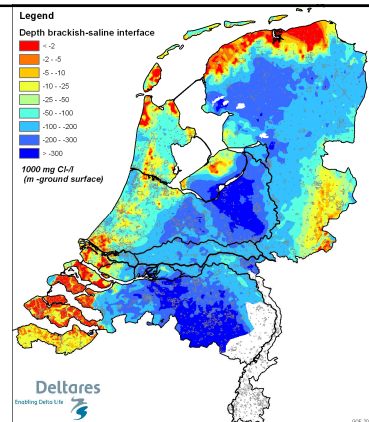
Dutch setting

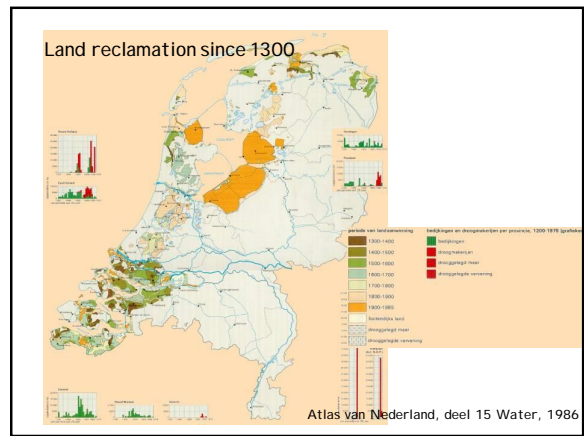
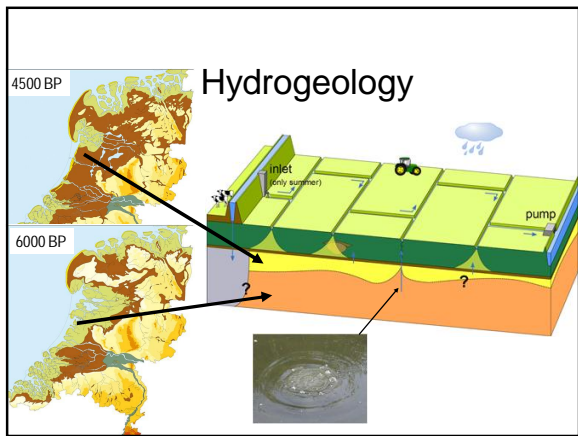


Present ground surface in the Netherlands



Fresh-Salt interface





Dutch setting

Salinisation of the Dutch subsurface

Physical transport processes:

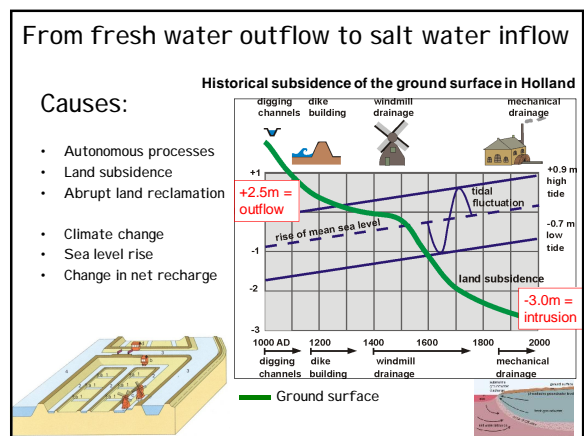
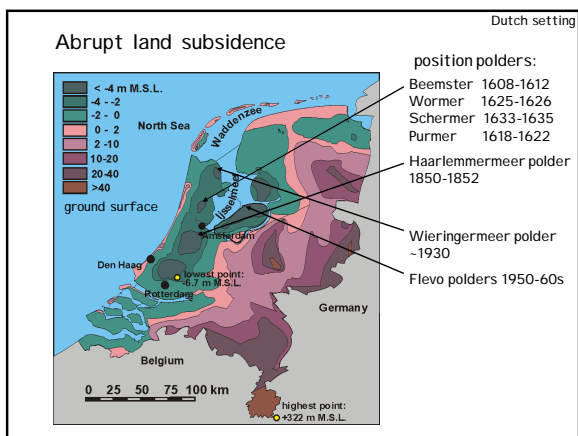
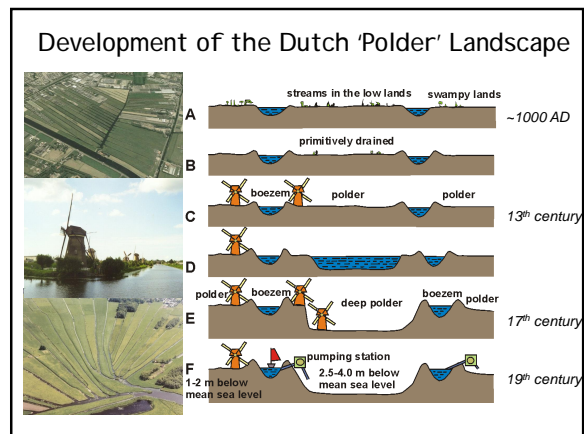
- advective: e.g. trans- and regressions
- dispersive: mixing with marine deposits
- diffusive: e.g. IJsselmeer lake
- chemical: solution, precipitation, ion-exchange

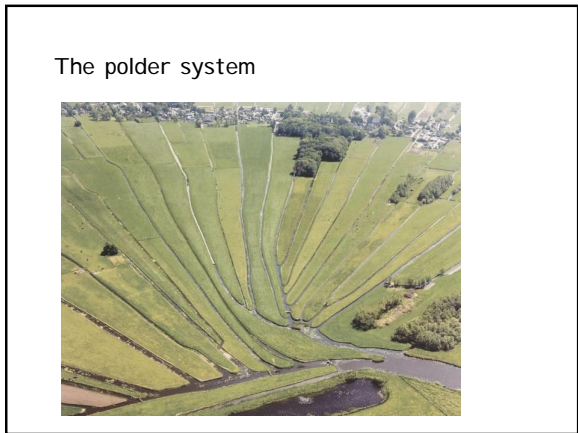
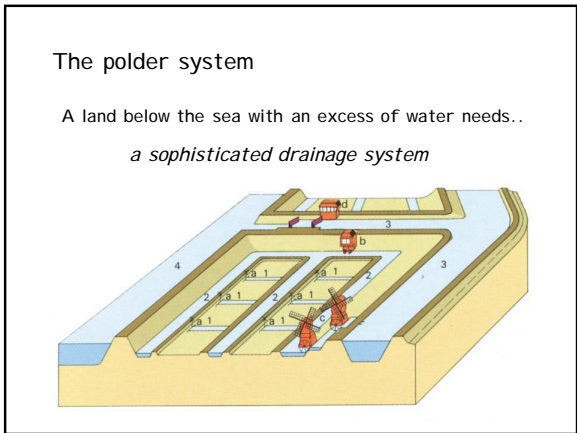
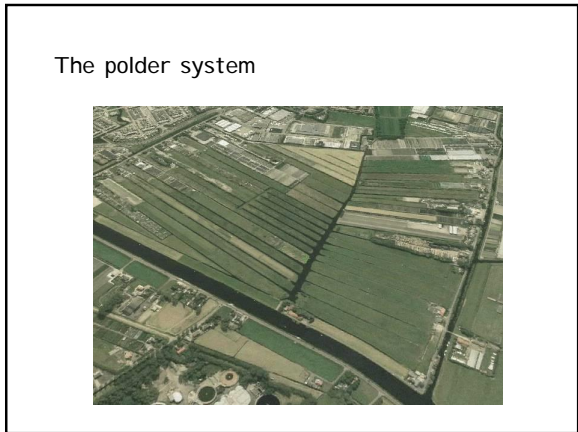
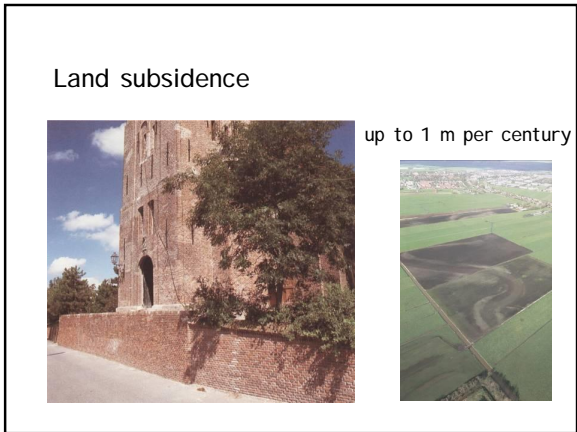
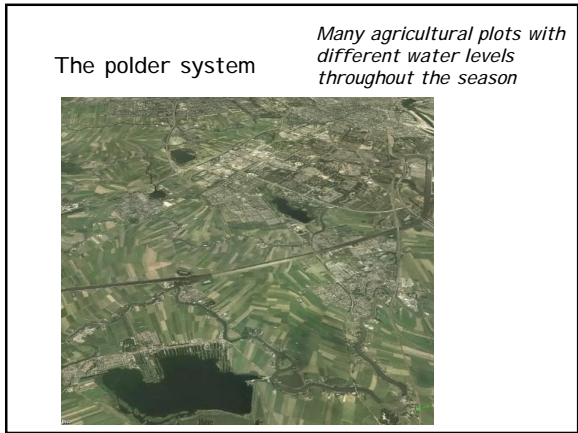
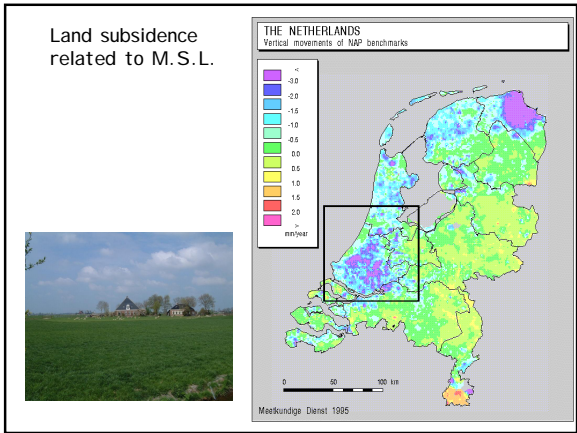
Anthropogenic causes:

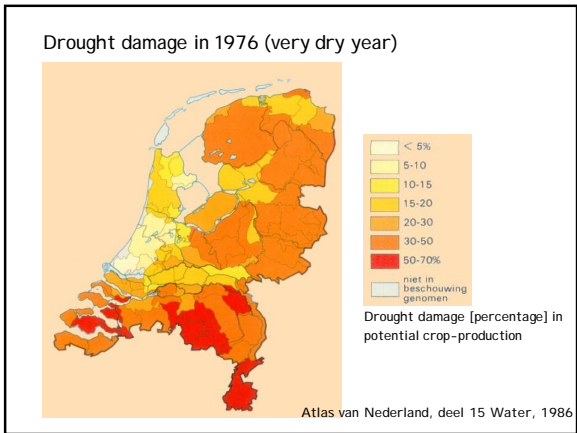
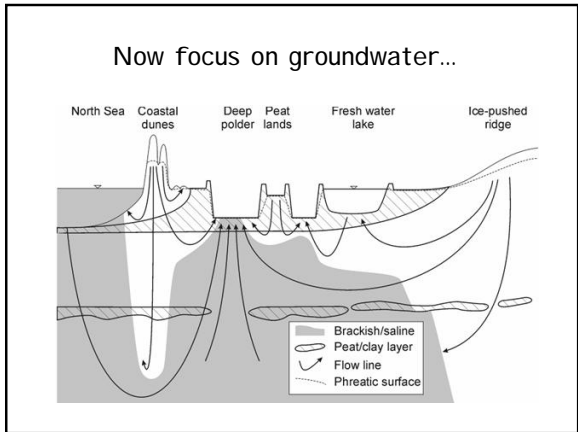
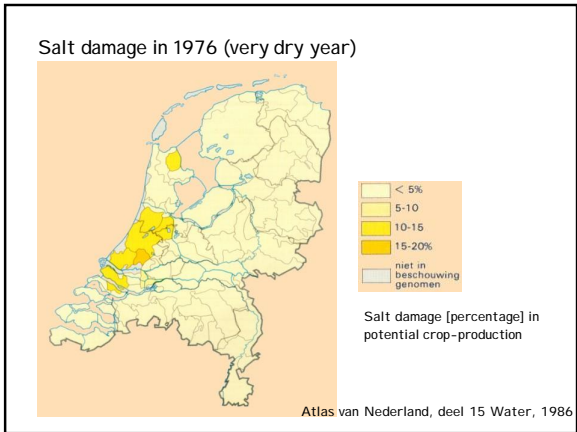
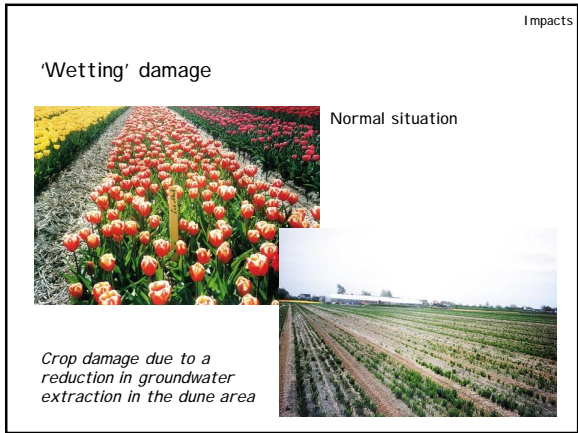
- land subsidence
- polder level lowering
- groundwater extractions

Future developments (climate change):

- sea level rise
- changes in recharge







Threats to water management due to climate change:

Short term threats:

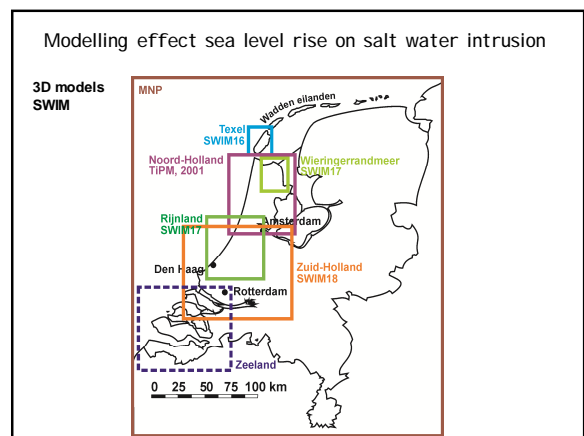
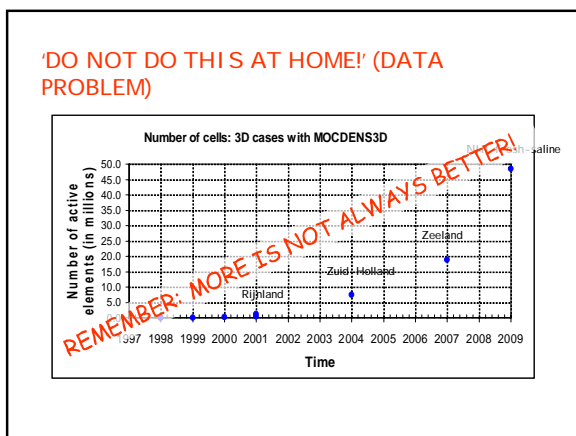
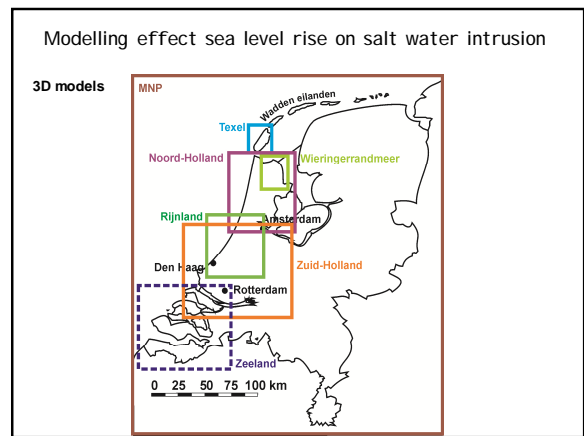
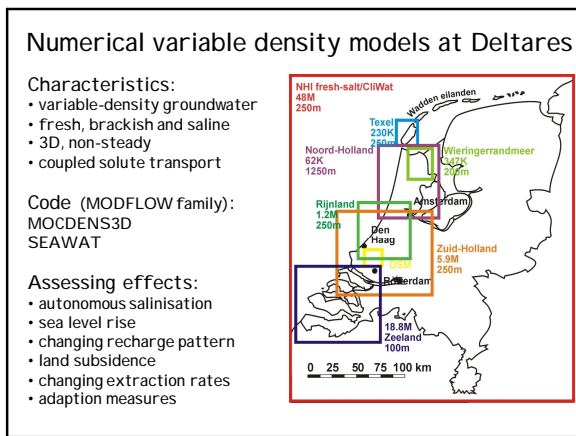
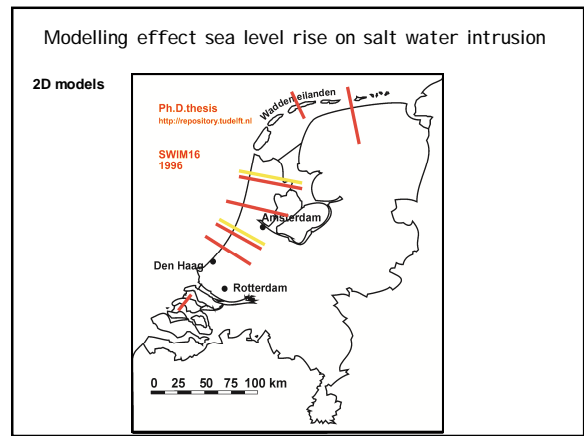
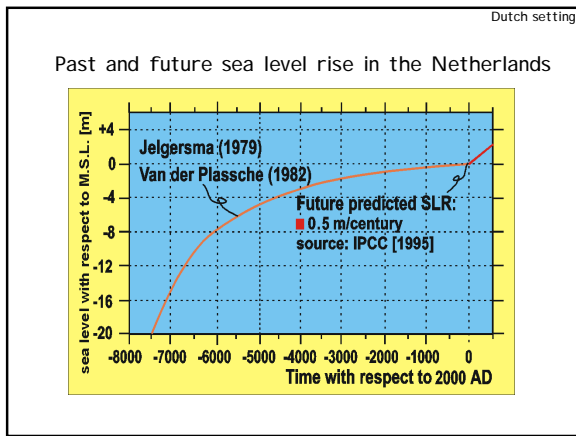
- flooding
- dike collapse
- drought

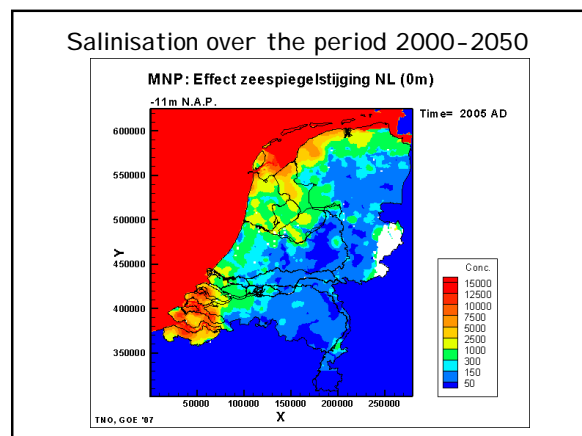
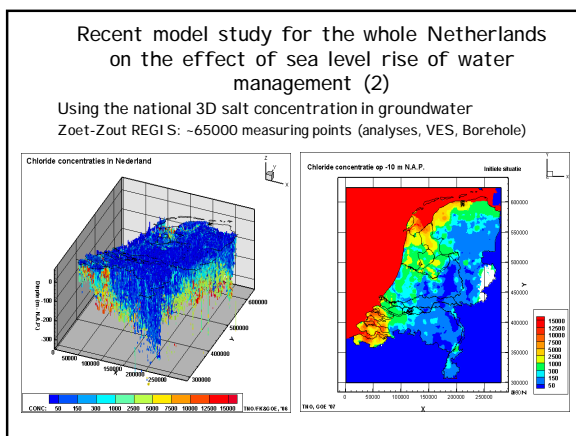
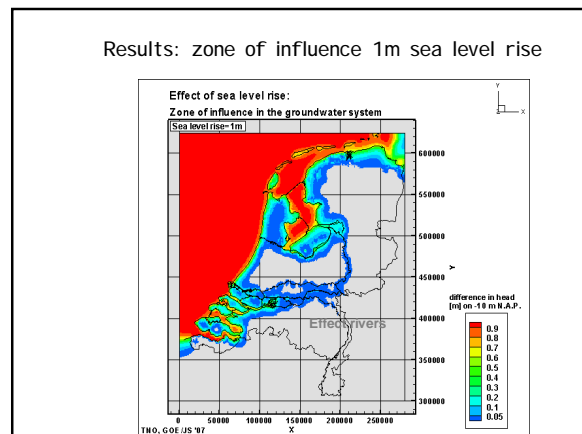
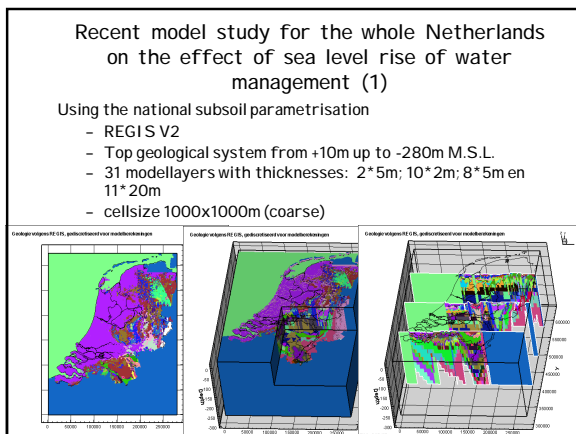
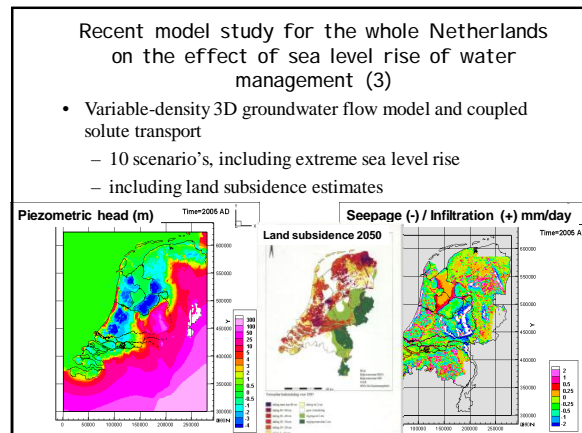
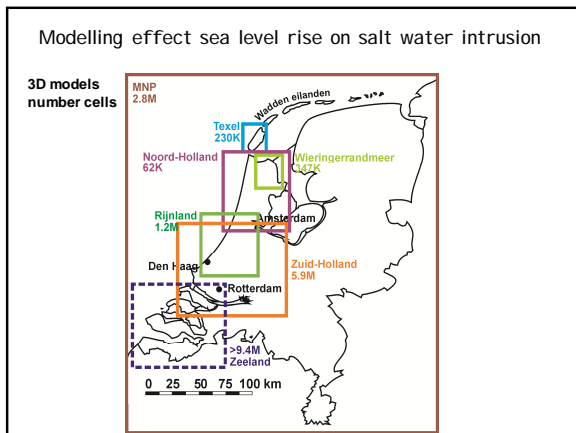
asks for operational water management

Long term threats:

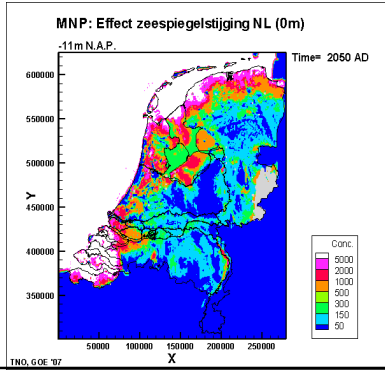
- salt water intrusion
- land subsidence
- smaller fresh groundwater resources

asks for strategic water management



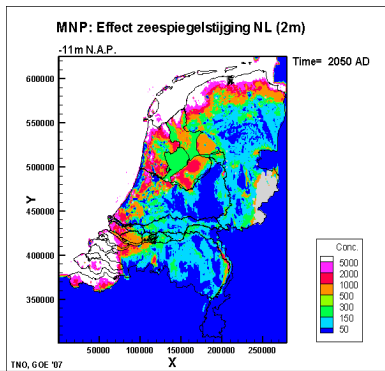


Salinisation subsoil at 0m sea level rise in 2050

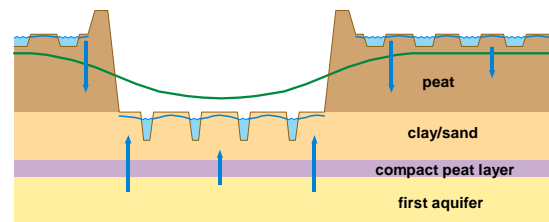


Salty wells

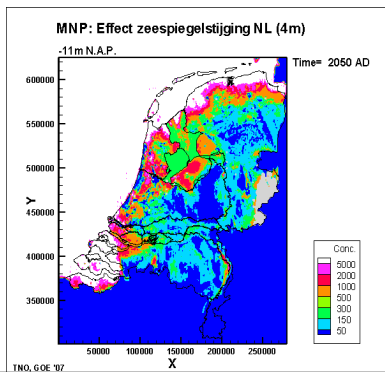
Salinisation subsoil at 2m sea level rise in 2050



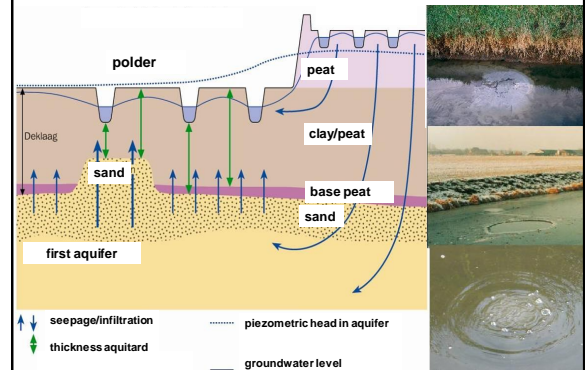
Seepage and infiltration situation around deep polders

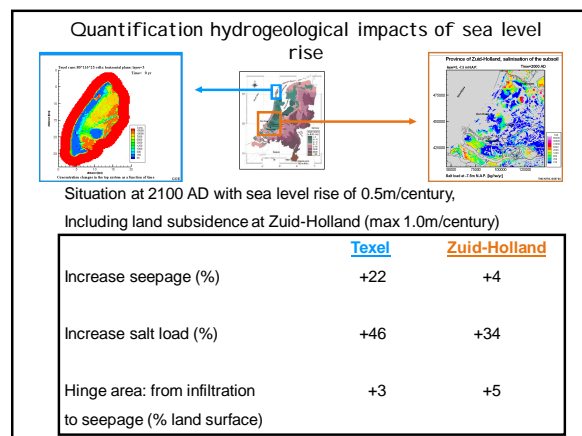
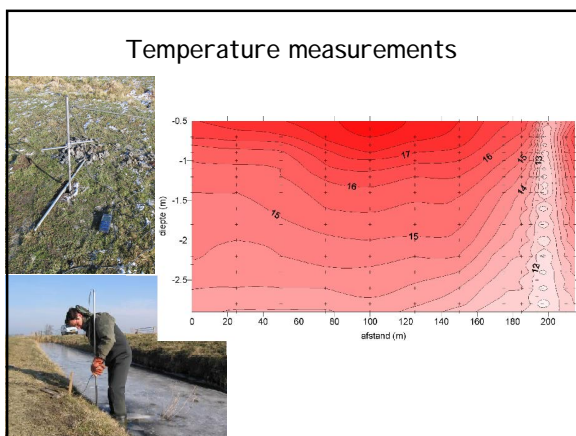
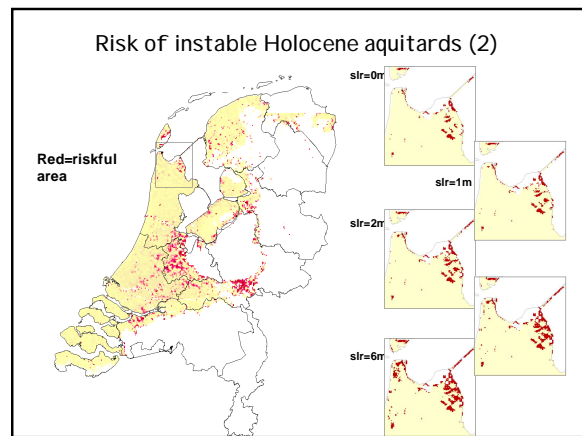
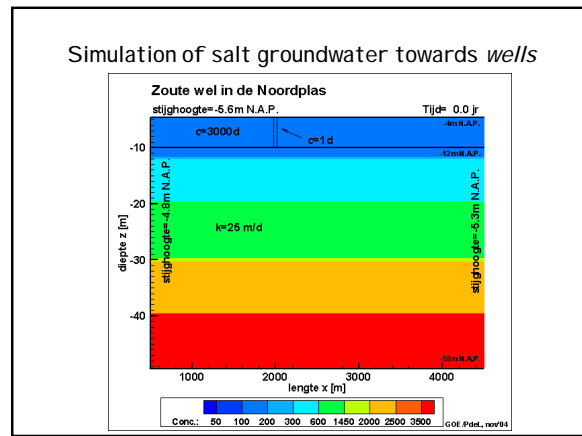
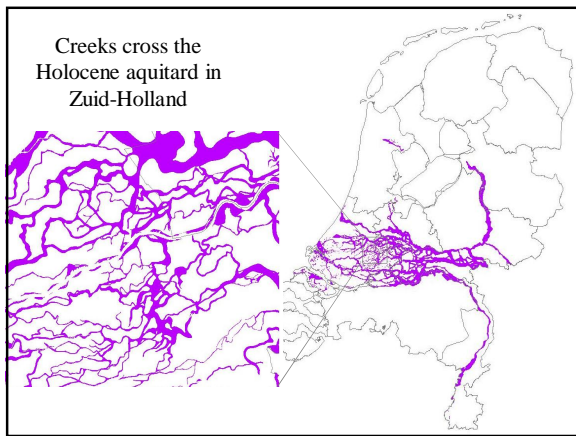


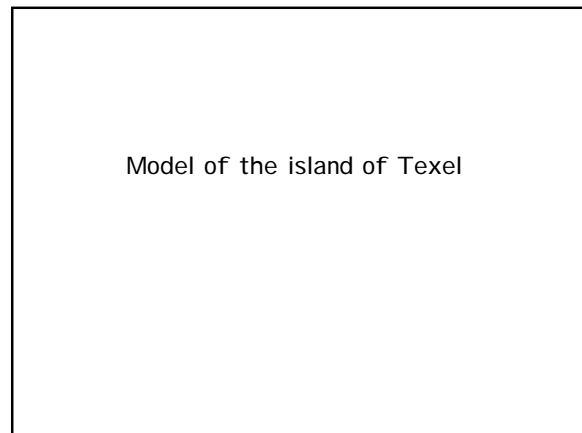
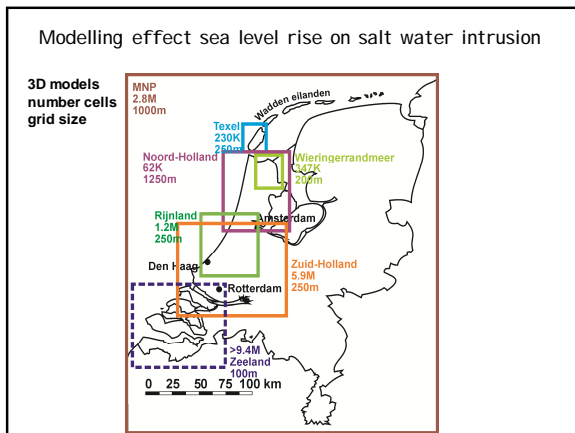
Salinisation subsoil at 4m sea level rise in 2050



Risk of instable Holocene aquitards (1)





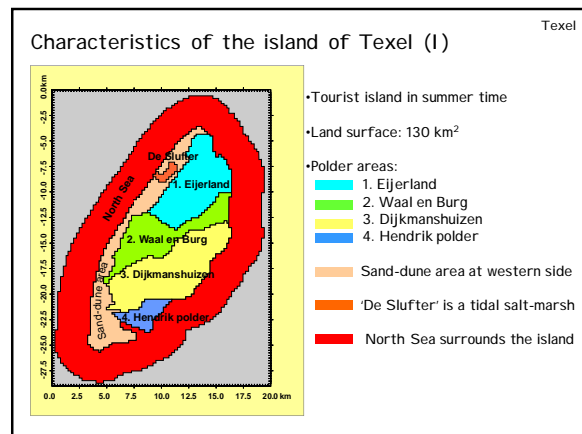


3D modelling

Characteristics 3D Cases (I): geometry & soil

Case	Kop van Noord-Holland	Texel	Wieringer-meerpolder	Rijnland
total land surface [km ²]	2150	130	200	1100
L _x *L _y modelled area [km]	65*51	20*29	23*27	52*60
depth system [m-N.A.P.]	290	302	385	190
aquifer hydr. cond. [m/d]	5-70	5-30	15-40	12-70
aquitarid hydr. cond. [m/d]	0.12-0.001	0.01-1	0.012-0.056	2.5E-4-0.8
porosity	0.35	0.3	0.25	0.25
anisotropy [k _z /k _x]	0.4	0.4	0.25	0.1
long. dispersivity α _l [m]**	2	2	2	1
# head&conc. observations	not applicable*	111	95	1632
characteristics head calibration	not applicable*	Δφ =0.24 m σ=0.77 m	Δφ =0.34 m σ=0.21 m	Δφ =0.60 m σ=0.77 m

* calibration with seepage & salt load in polders
**molecular diffusion=10⁻⁹ m²/s; trans. disp.=1/10 long. disp.

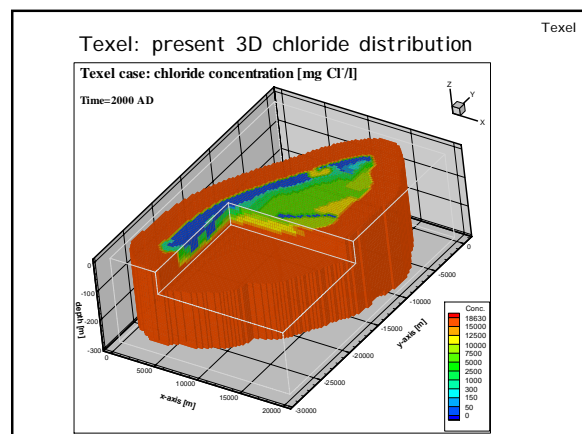


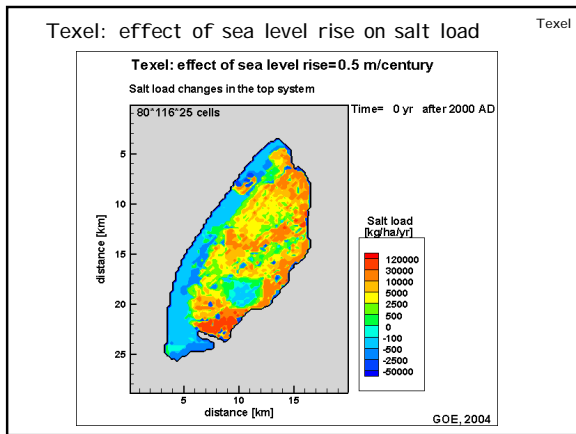
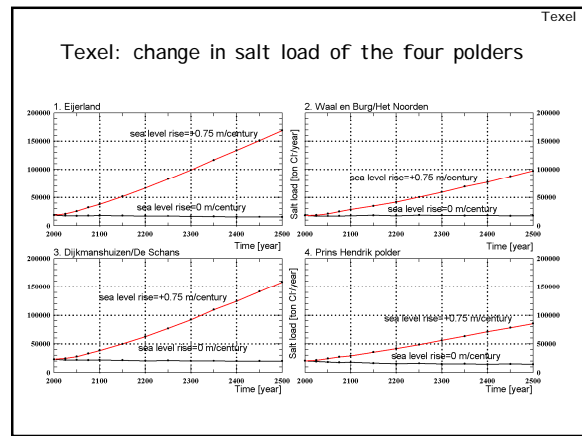
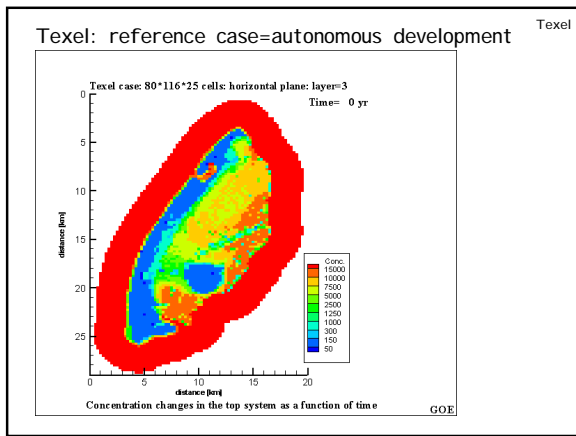
3D modelling

Characteristics 3D Cases (II): model parameters

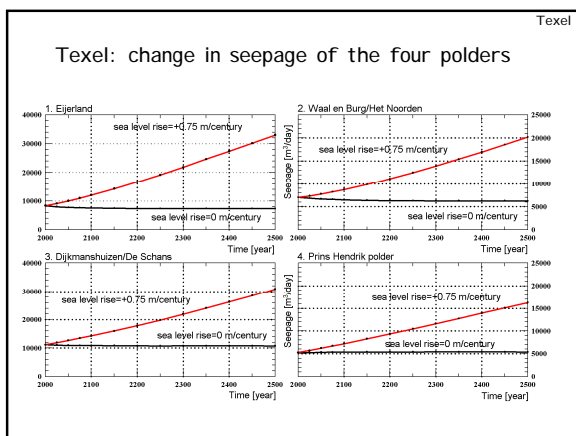
Case	Kop van Noord-Holland	Texel	Wieringer-meerpolder	Rijnland (=391 EM RAM)
horizontal cell size [m]	1250*1250	250*250	200*200	250*250
vertical cell size [m]	10	1.5 to 20	2 to 70	5 to 10
total # active cells	-40.000	-126.000	-312.000	-1.200.000
# cells	41*52*29	80*116*23	116*136*22	209*241*24
# particles per cell	27	8	8	8
total time [yr]	1000	500	50	500

convergence head criterion=10⁻⁵/10⁻⁴ m
flow time step Δt=1 year





Model of the Province of Zuid-Holland



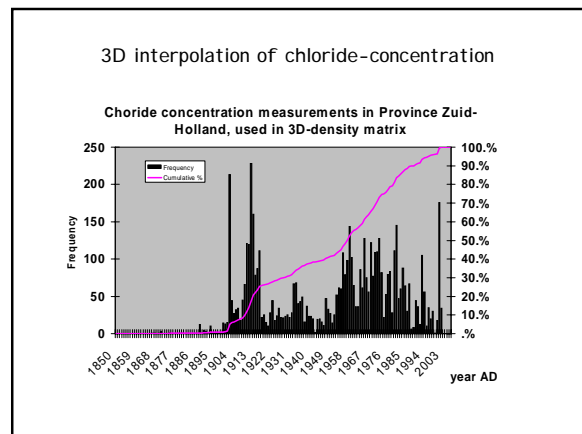
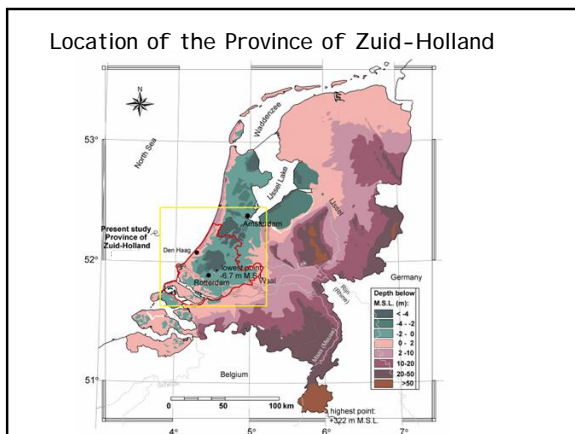
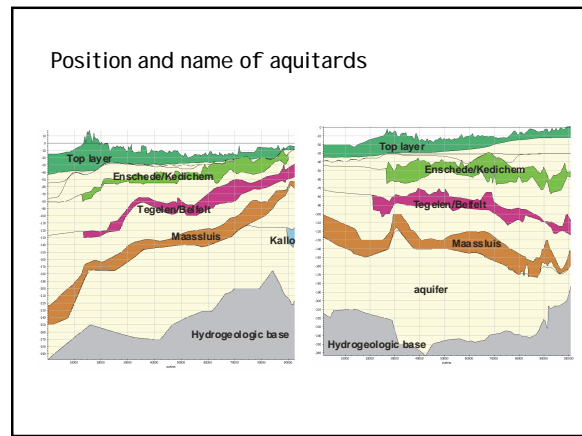
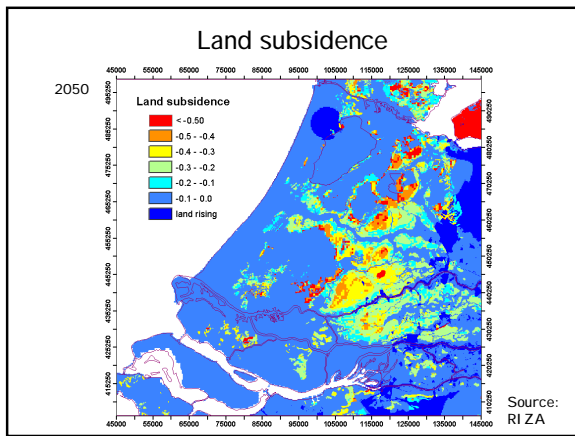
Case study: Province of Zuid-Holland

European water framework directive
"in 2015, state of all groundwaters and surface waters must be good"

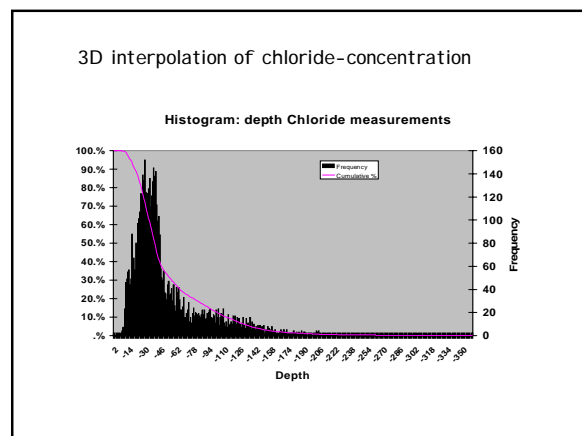
Identification of all fresh groundwater bodies in the province

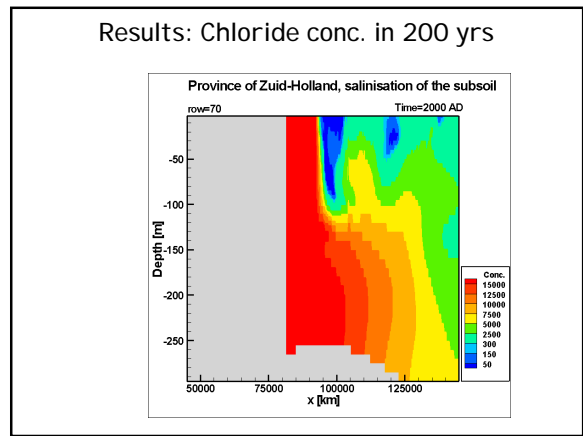
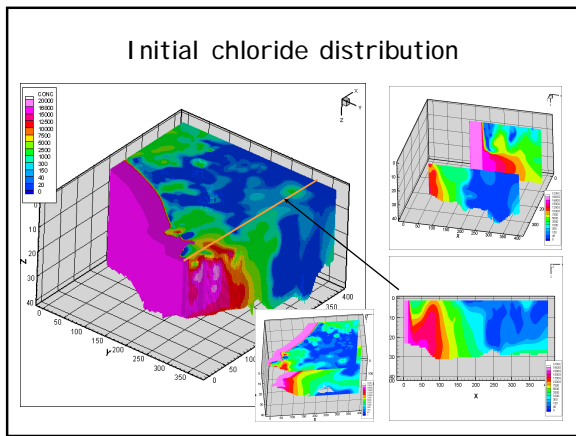
How fast is the salinisation process?

More seepage, more salt load?



- ### Numerical model description
- variable-density groundwater flow
 - coupled solute transport
 - MOCDENS3D
 - area: 100km * 92.5km * 300m depth
 - 400 * 370 cells, 40 layers
 - ~4 million active cells
 - uses most accurate Dutch 3D subsurface schematization available
 - 9 aquifers and aquitards
 - uses 5772 chloride concentration measurements

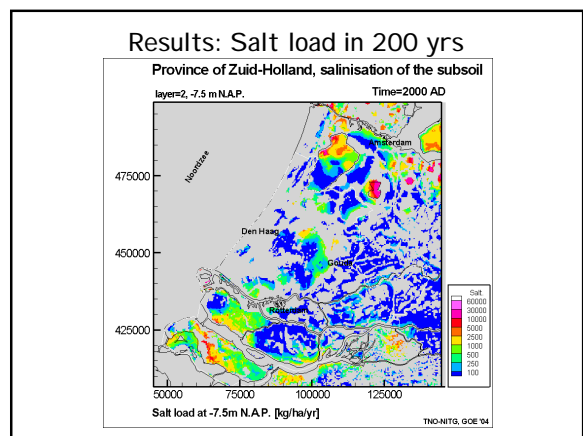
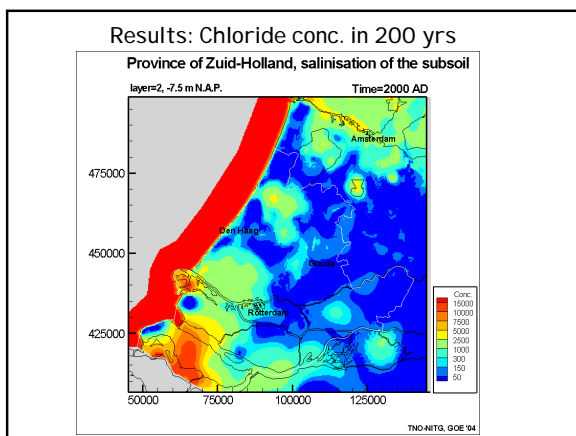
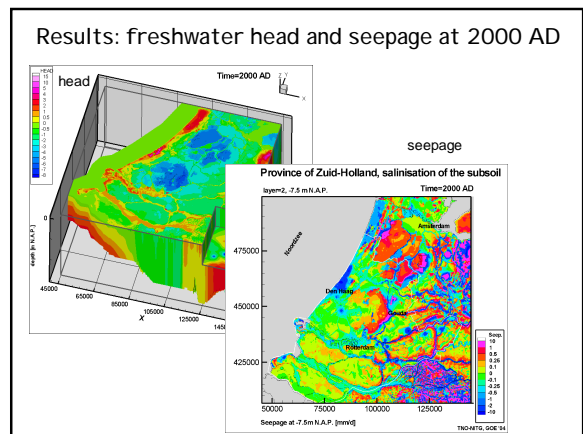




Present freshwater volume

27 billion m³

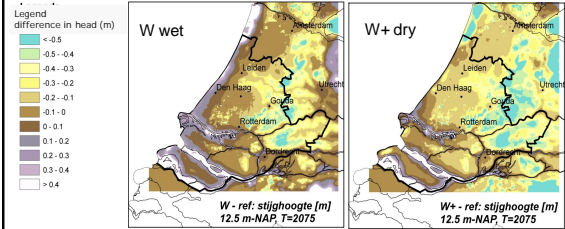
36% fresh, 14% brackish, 50% saline



Effect sea level rise, change in natural groundwater recharge and land subsidence on freshwater head in aquifer

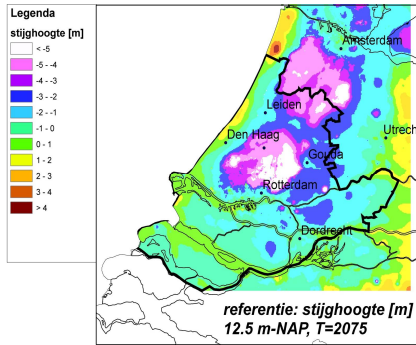
Some regional modelling results

Difference in freshwater head on -12.5 N.A.P.: W scenarios

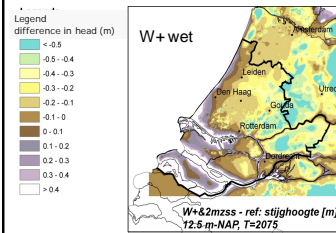


Sea level rise is 85 cm

Freshwater head at -12.5 M.S.L.

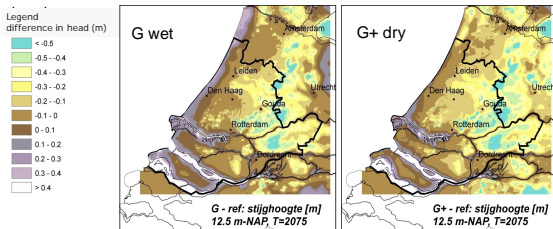


Difference in freshwater head on -12.5 N.A.P.: W scenarios



Sea level rise is 200 cm

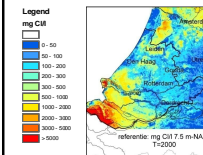
Difference in freshwater head on -12.5 N.A.P.: G scenarios



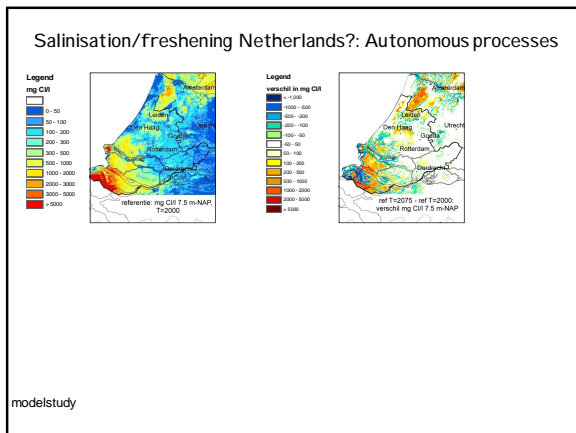
Sea level rise is 60 cm

Including change in natural groundwater recharge

Salinisation/freshening Netherlands?: Present situation



modelstudy

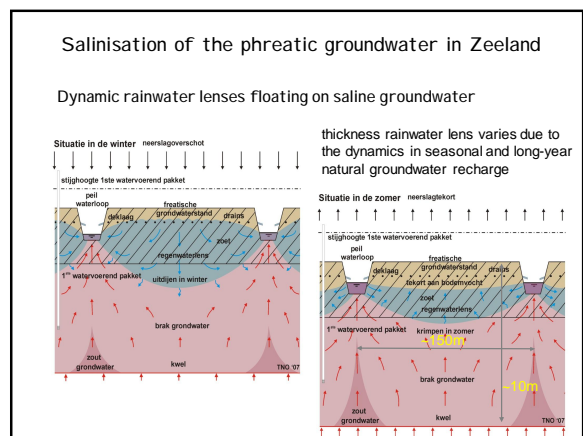
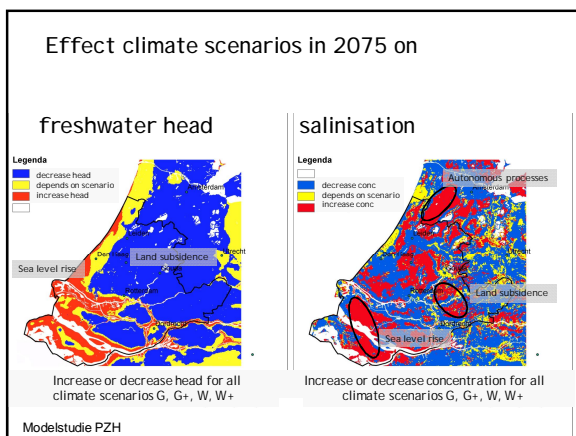
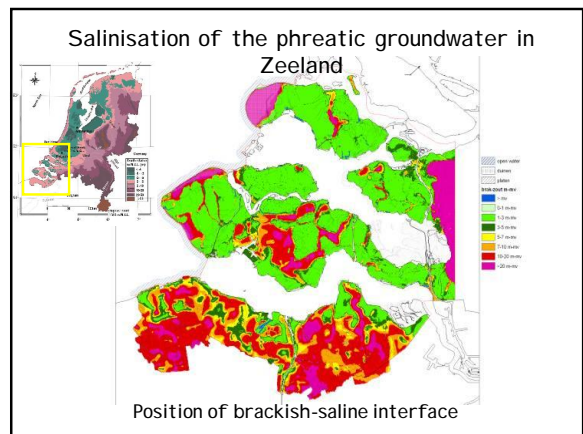
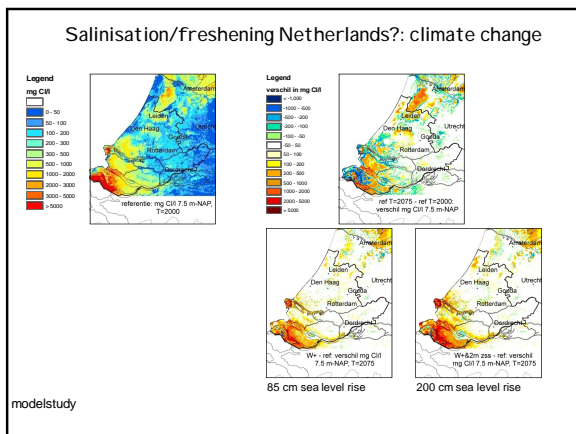


Rainwater lens

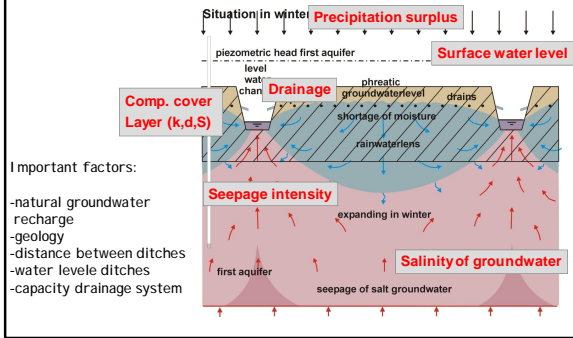
Rainwater lenses in an agricultural setting

Shallow dynamic freshwater bodies flowing upon brackish-saline groundwater

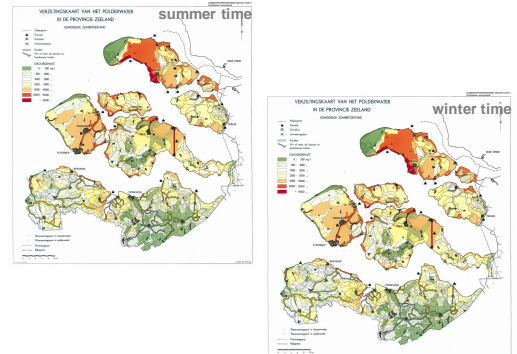
- density dependent
- dynamics: seasonal & long-year



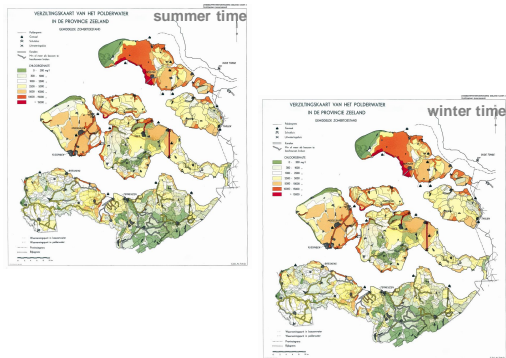
Factors controlling fresh-salt interface



Salinisation surface water



Salinisation surface water



Problem definition dynamic freshwater lenses



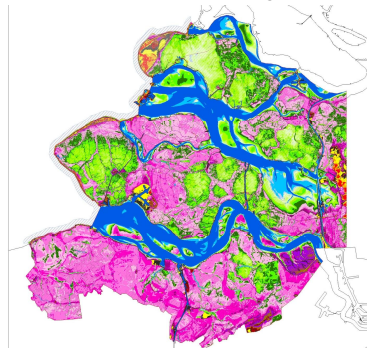
- Salt in the agricultural plots originates from:
- surface water system (irrigation water)
 - groundwater system (salt load to the root zone)

The salinisation will increase due to:

- sea level rise
- climate change
- water level management



Position of the ground surface



How to tackle the problem?

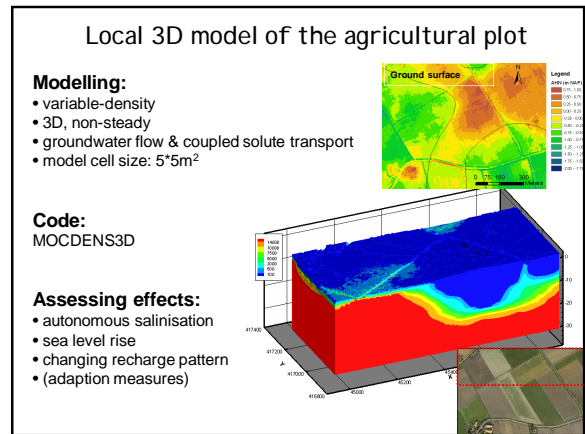
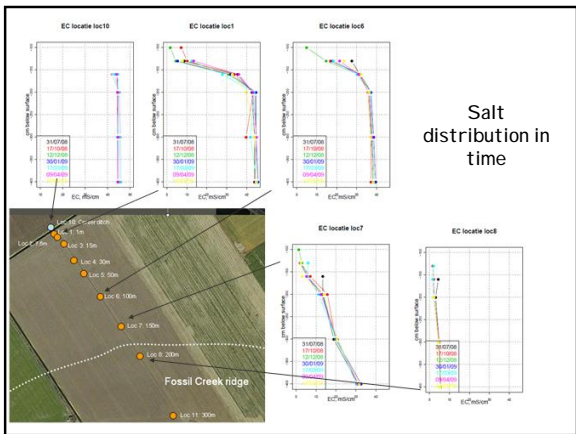
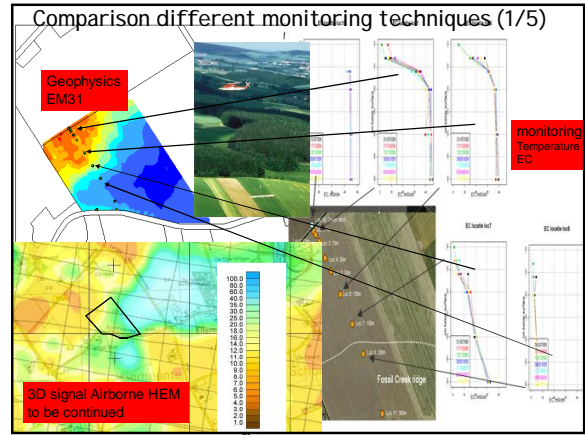
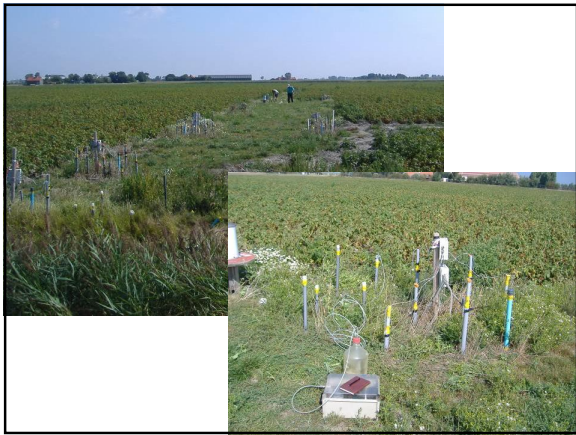
Field measurements at parcels

- fresh-brackish-salt interface at local scale using T-EC-probe and later CVES and ERT
- groundwater level and quality
- surface water level and quality

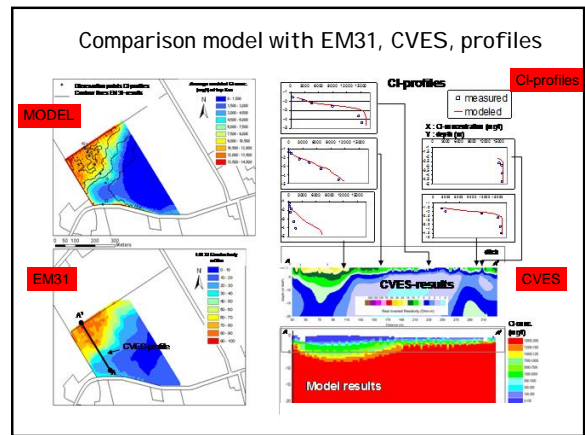
Modelling

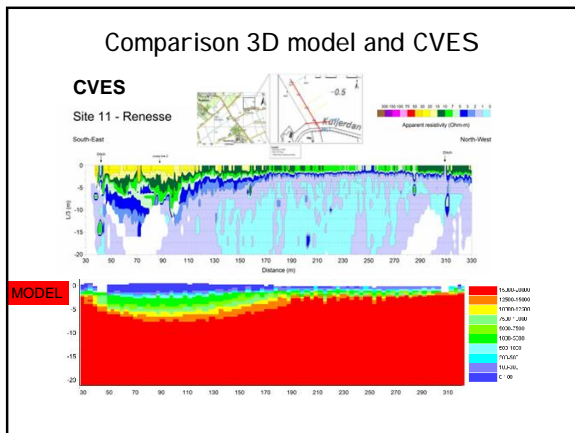
- density dependent groundwater flow
- two different scales:
 - regional scale: transect perpendicular at coast
 - local scale: parcel between two ditches



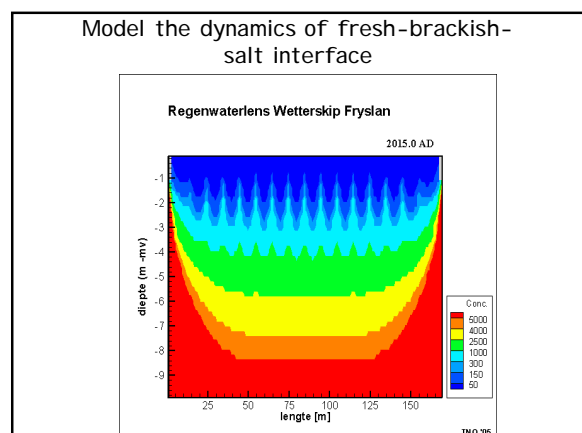
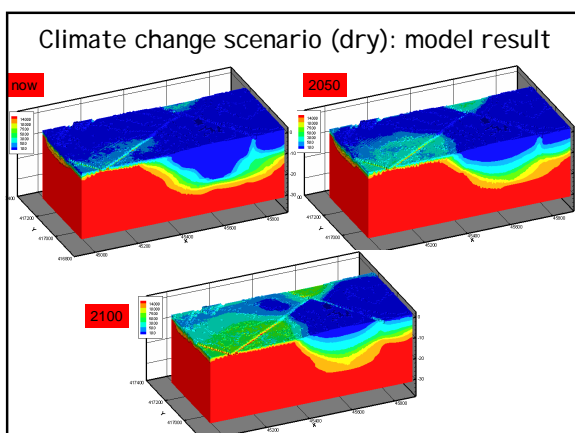
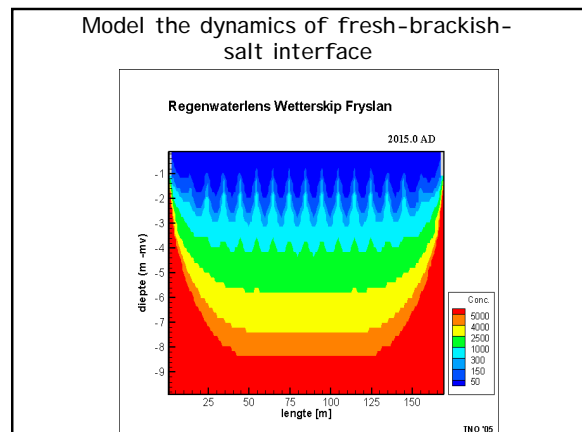
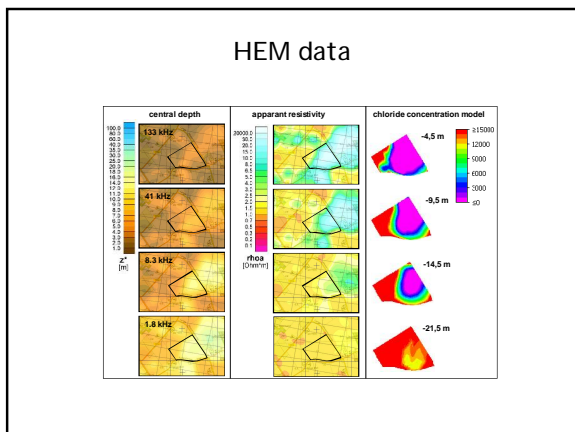


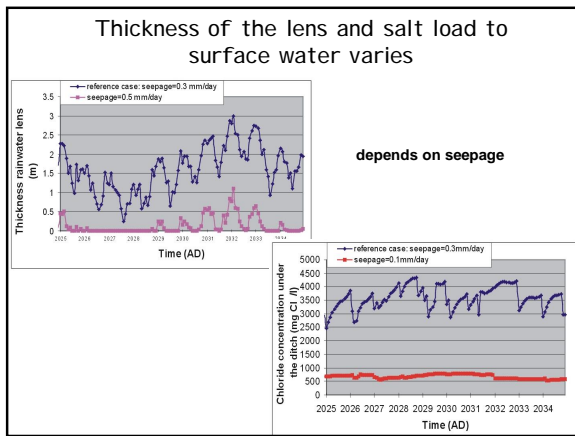
- TEC
- sampling
- EM31
- CVES
- HEM
- ECPT
- Numerical models (2D and 3D)





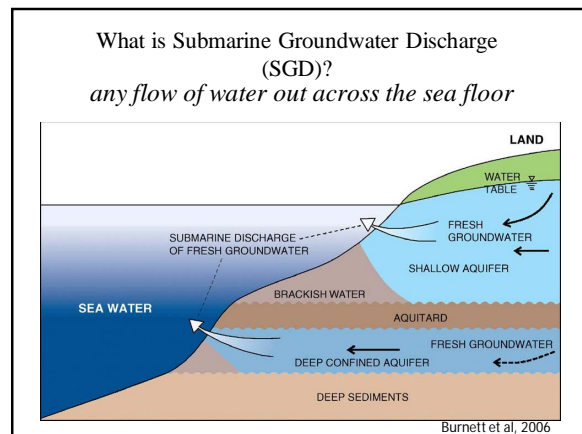
- ### To be continued...
- Implementing more realisations of 3D geology and initial 3D fresh-saline
 - Analyse the differences
 - Running climate change scenarios (on national and regional level)
 - Effect on surface water (salt load)
 - Effect on root zone (rainwater lenses)
 - Effect on freshwater volumes (drinking water)
 - Compare model results of different scales and give recommendations



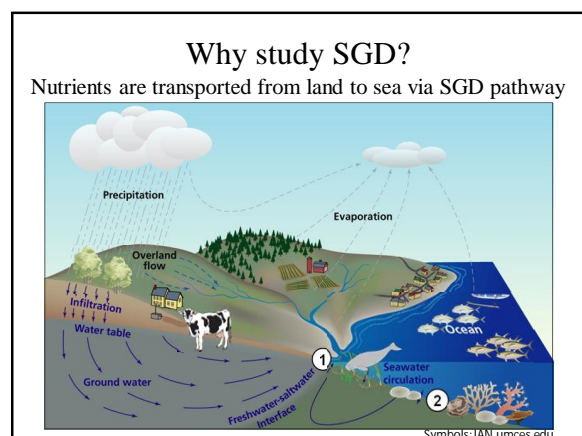


- ## International
- Philippines (submarine groundwater discharge)
 - Gujarat, India (evaluation anti-swi measures)
 - Maldives (effect dec 2004 Tsunami)

- ### Conclusions (salinisation Dutch aquifers):
- Salinisation in the Netherlands is a non-stationary process
 - Three physical processes threaten the Dutch aquifers:
 - autonomous development
 - land subsidence
 - sea level rise
 - Increase in seepage and salt load can be severe during the coming 50/100 years
 - Modelling techniques are available to assess possible effects

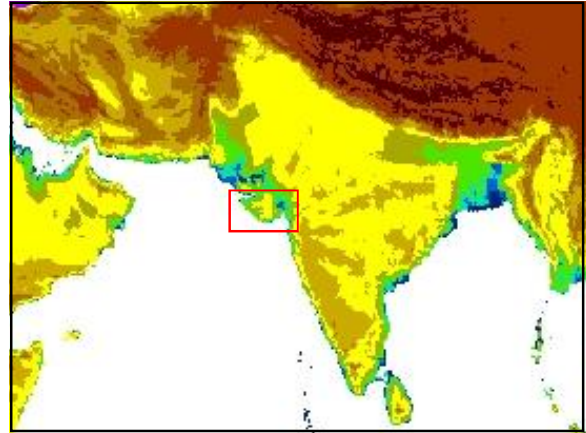
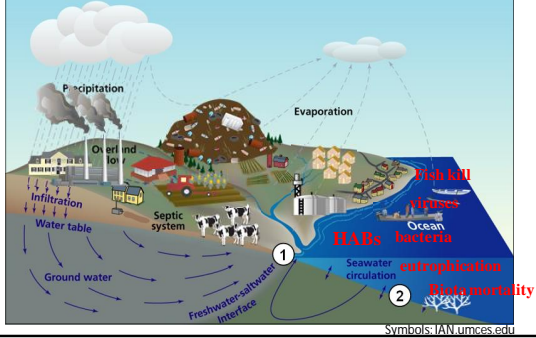


- ### Recommendations (salinisation Dutch aquifers):
- Number of quality measurements should be increased
 - Feasibility study is necessary to implement potential technical measures to compensate salt water intrusion



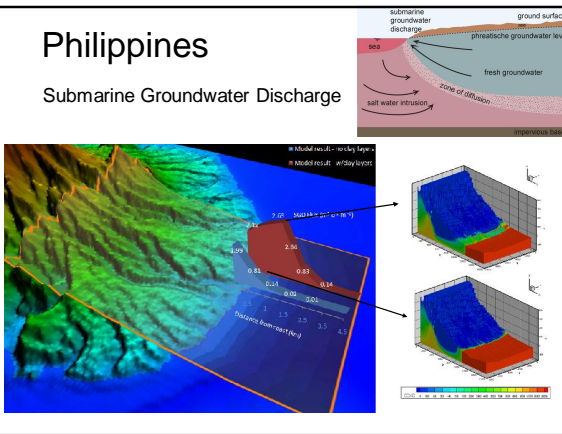
Why study SGD?

Nutrients are transported from land to sea via SGD pathway

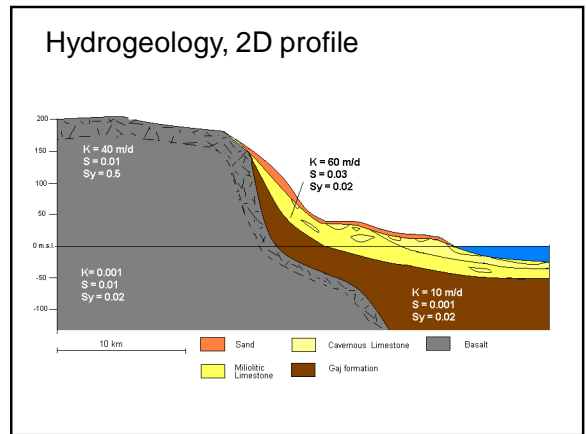


Philippines

Submarine Groundwater Discharge

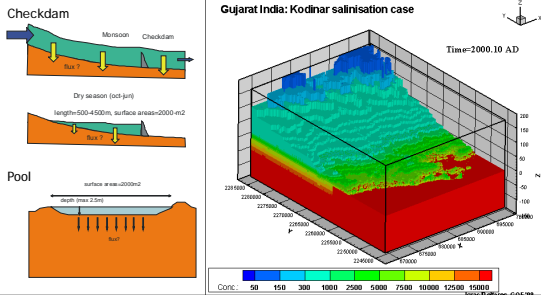


Hydrogeology, 2D profile

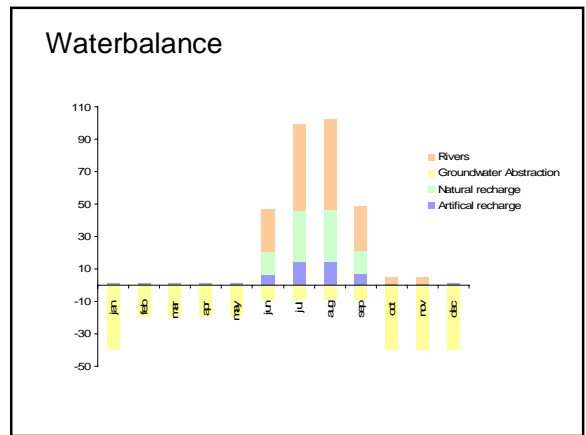


Gujarat, India

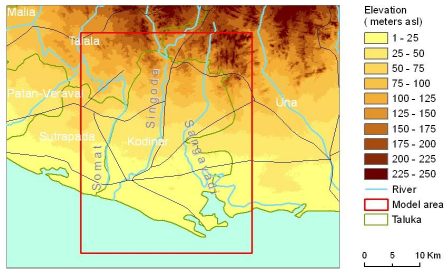
Learning from the Salinity Ingress Prevention Measures in the Coastal Area of Gujarat



Waterbalance

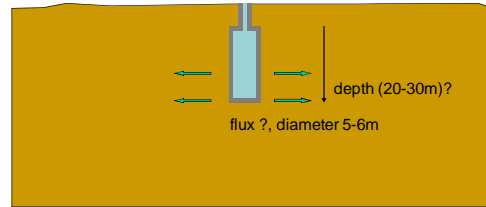


Topography, elevation

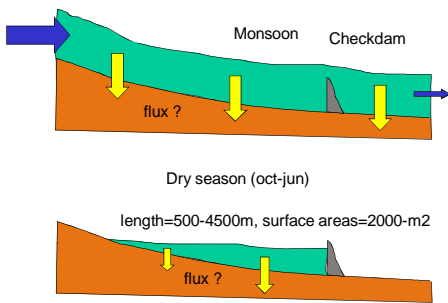


Concept Percolation tank

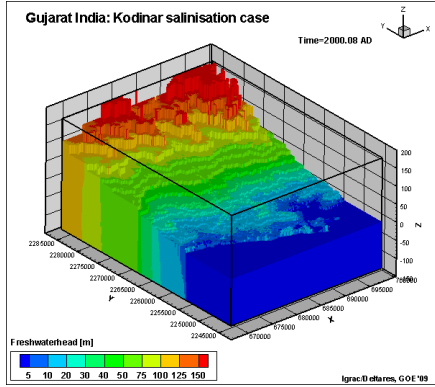
number of wells per village: ?



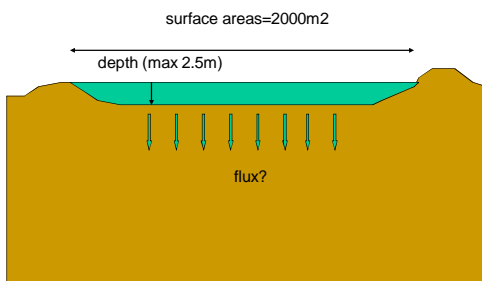
Concept Checkdam



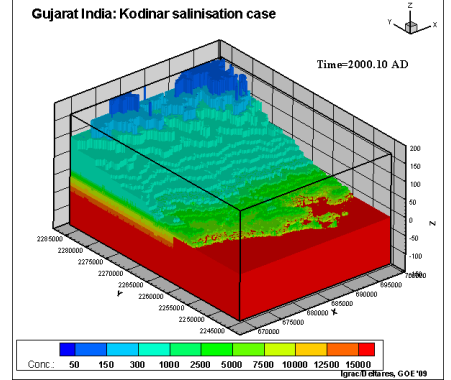
Freshwater head

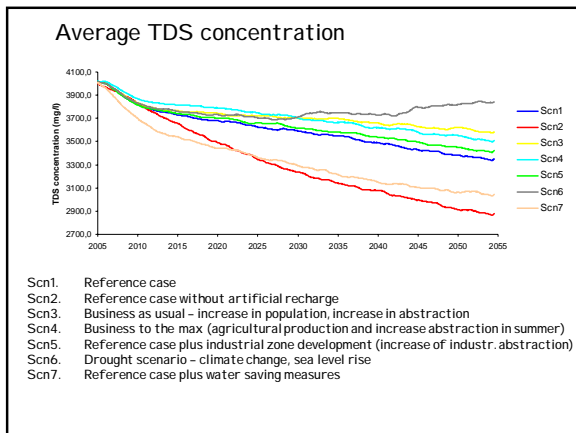


Concept Pond



Salinity





Model of the Kop van Noord-Holland, The Netherlands

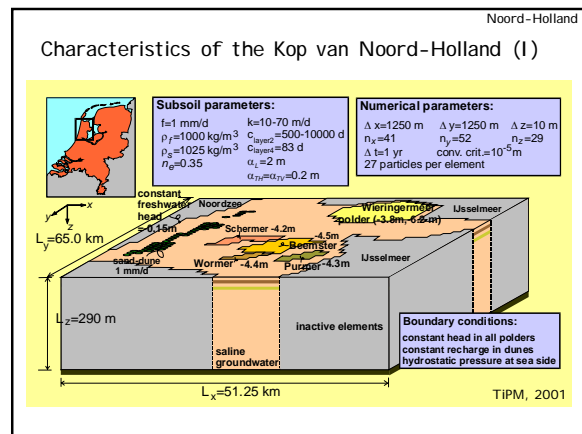
Oude Essink, G. H. P. 2001. Saltwater intrusion in 3D large-scale aquifers: a Dutch case. *Phys. & Chem. of the Earth* 26(4): 337-344.

Conclusions (modelling of variable-density flow)

- Don't use the Henry problem to test your variable-density code
- Use enough cells to model the Hydrocoid and Elder problem

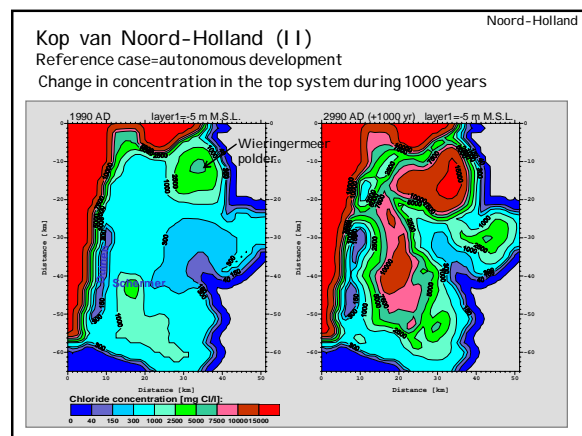
For modelling 3D systems:

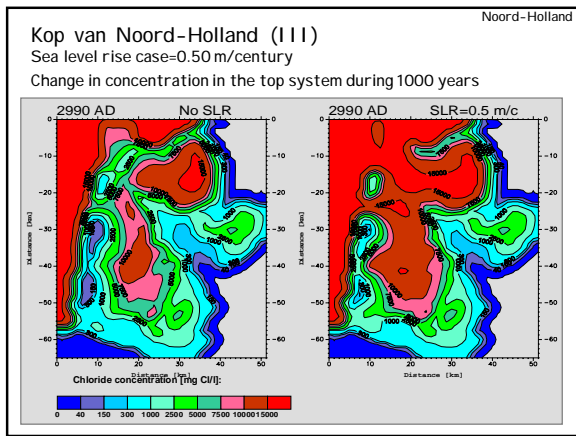
- Remember the Peclet discretisation limitation for cell sizes (unless you're using the method of characteristics!)
- Longitudinal dispersivity should not be too large (e.g. <10m)
- It's important to derive a very accurate density distribution (as that significantly effects the velocity field!)
- Watch out for numerical problems at the outflow face to the sea



Challenges for the future

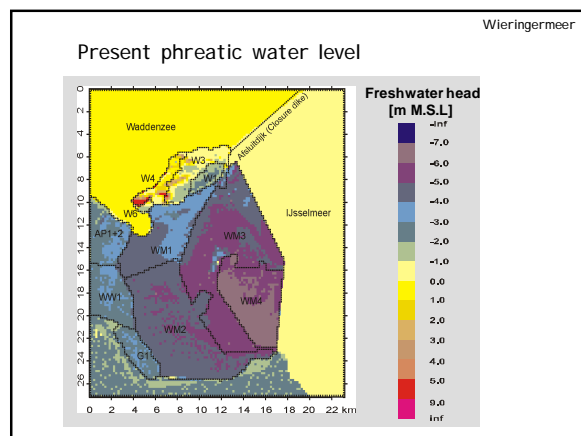
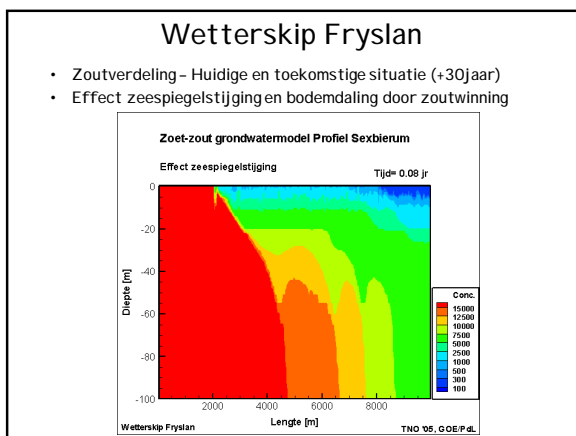
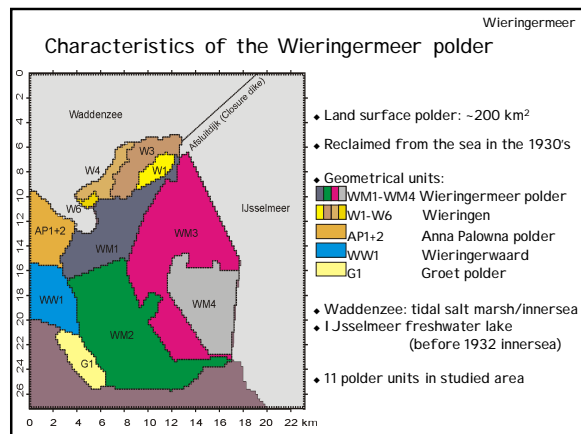
- Improve the 3D density matrix, e.g. by more types of measurements
- Implement effect of climate change and sea level rise on coastal aquifers
- Optimisation of (ground)water management in coastal aquifers by using 3D variable-density flow models
- Improve calibration of 3D models by using transient data of solute concentrations
- Incorporate reactive multicomponent solute transport

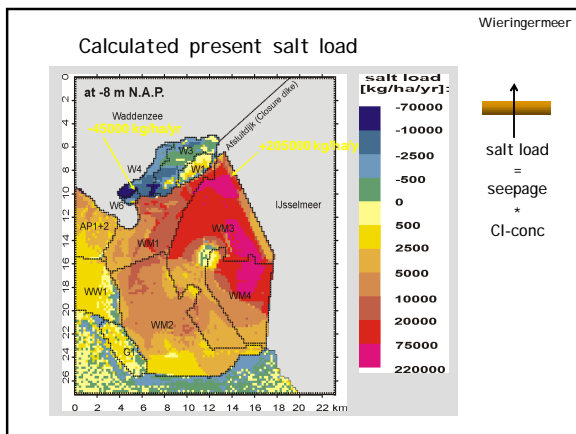
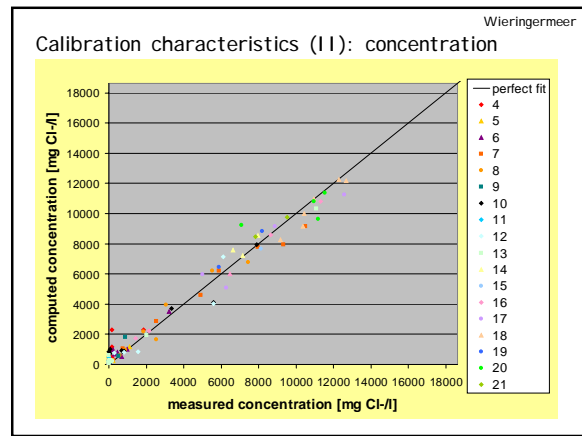
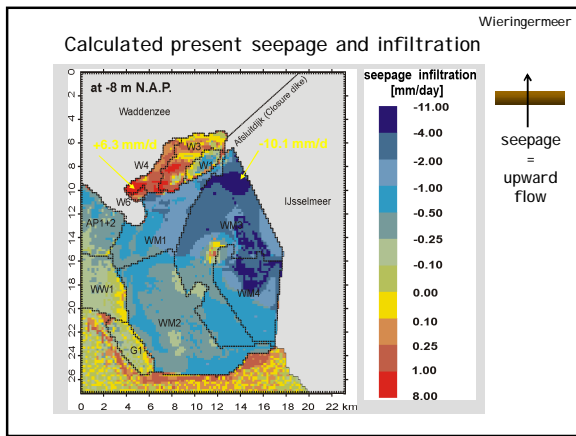




Model of the Wieringermeer polder

Model of the Wetterskip of Fryslan





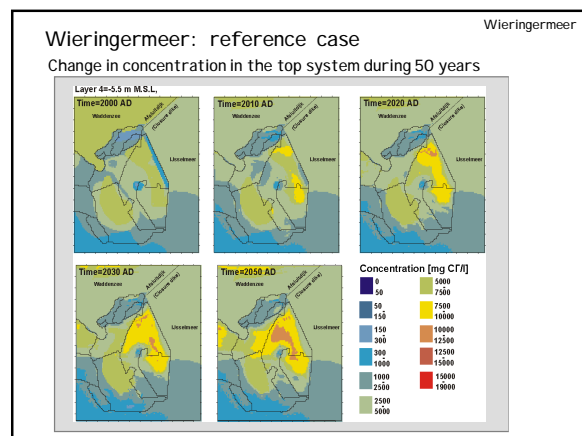
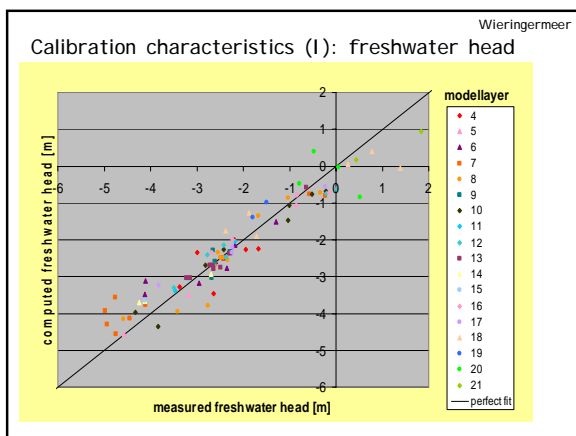
Wieringermeer

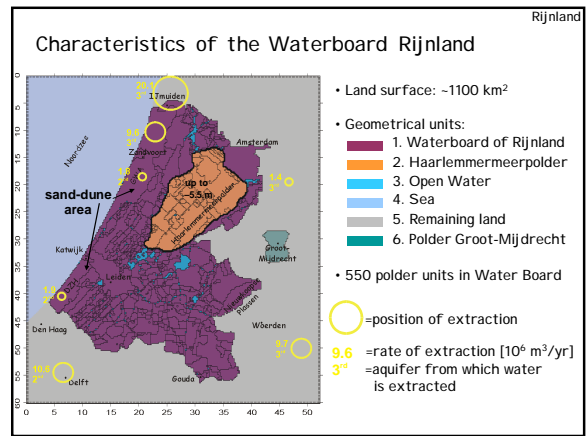
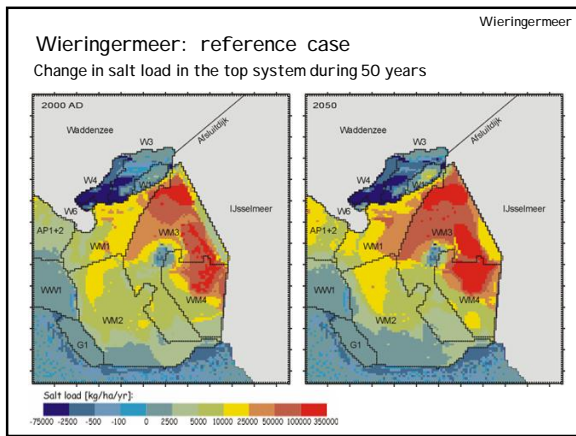
Two future scenarios (during 50 years):

- I Reference case
 - present mean sea level
 - autonomous development
- II Sea level rise case
 - relative sea level rise of 0.75 m/century

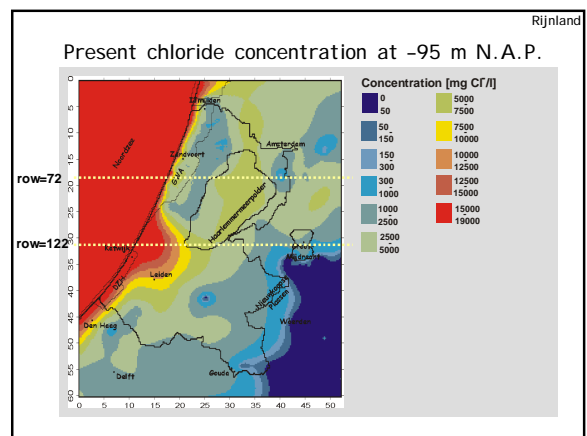
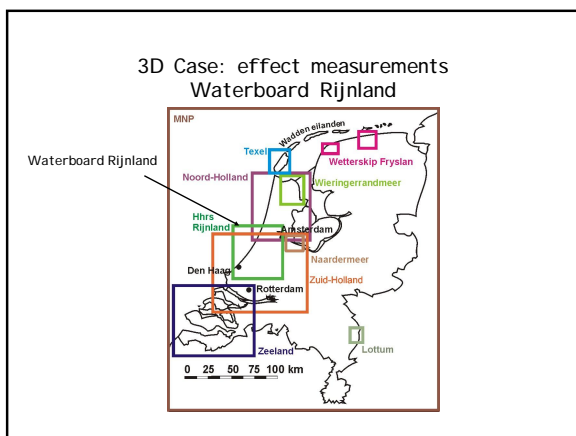
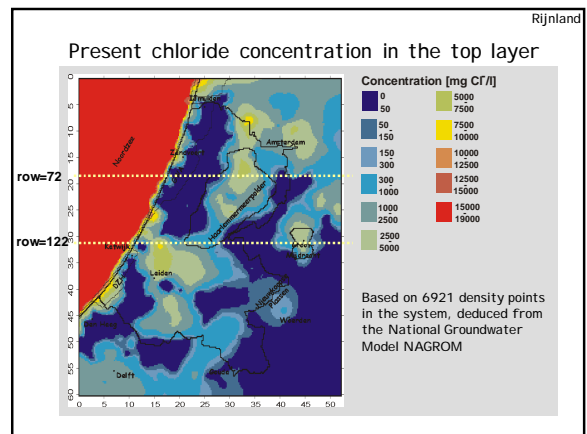
Interest is focused on:

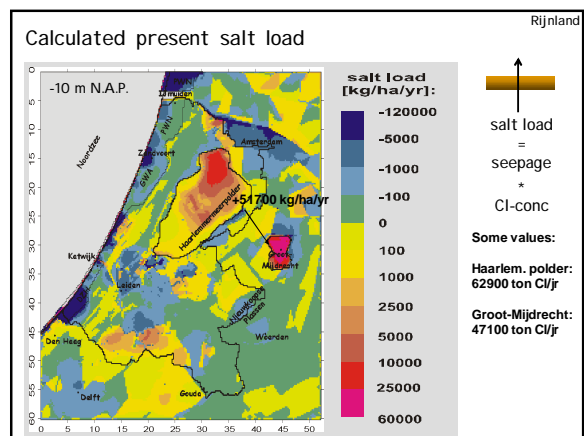
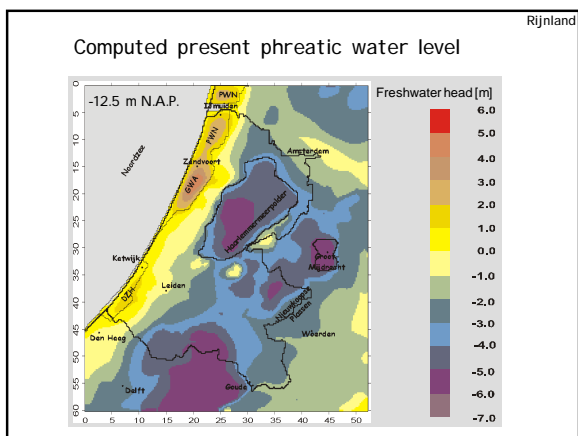
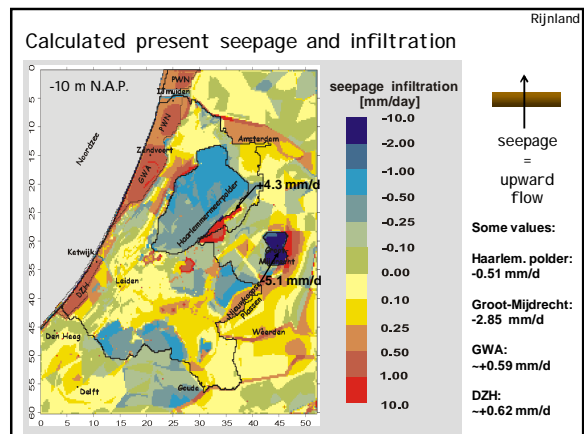
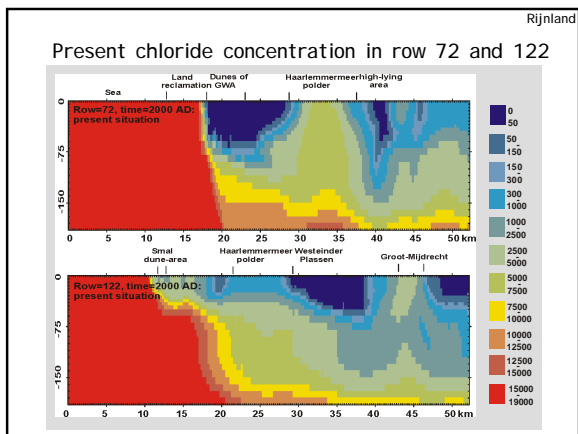
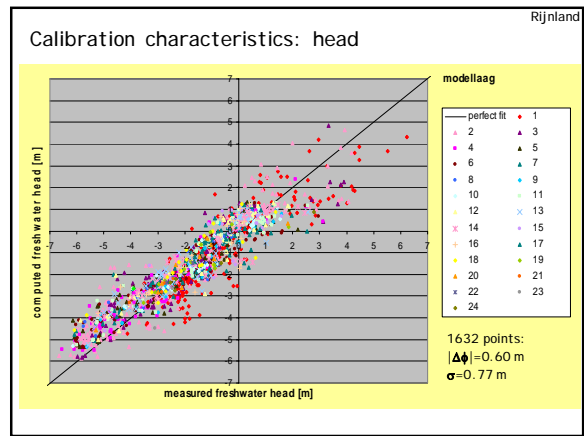
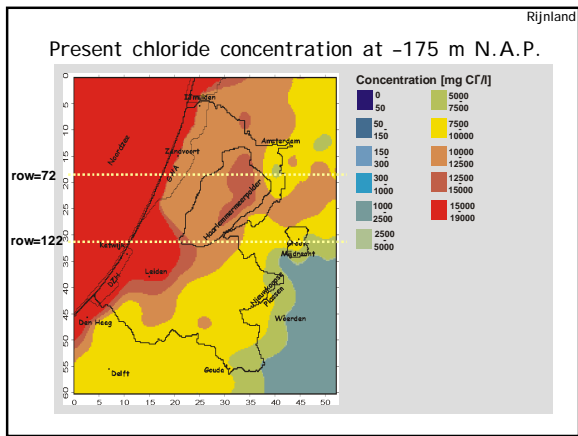
- A. Change in concentration in top layer
- B. Change in seepage in the polder
- C. Change in salt load in the polder





Model of the Waterboard Rijnland

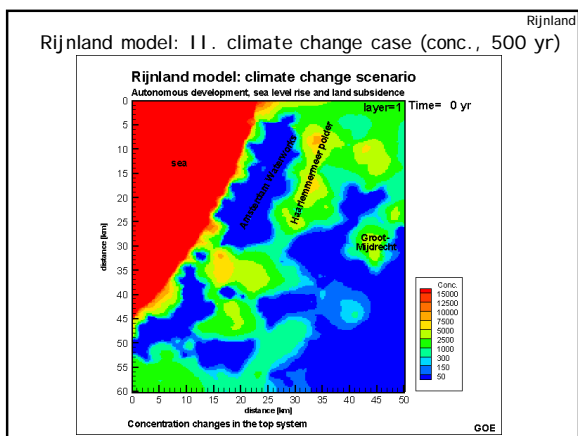
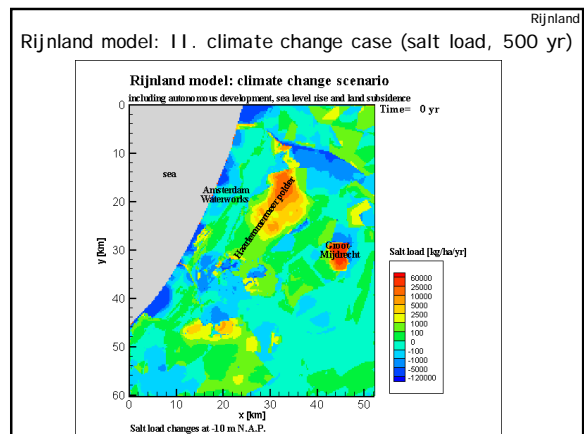
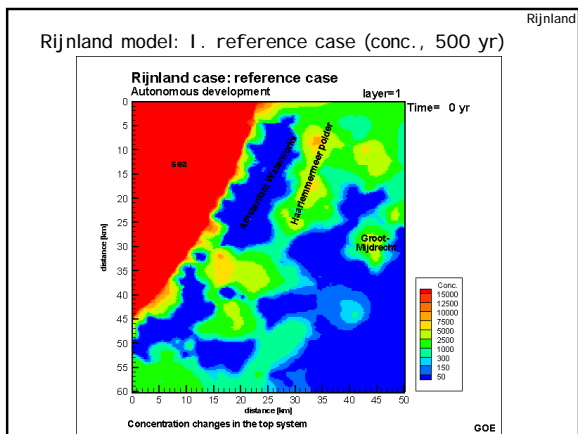
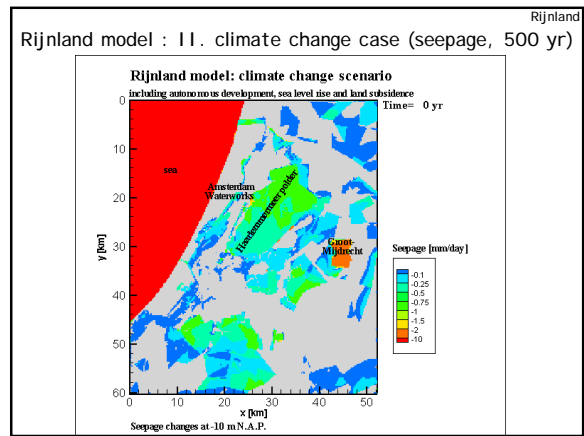




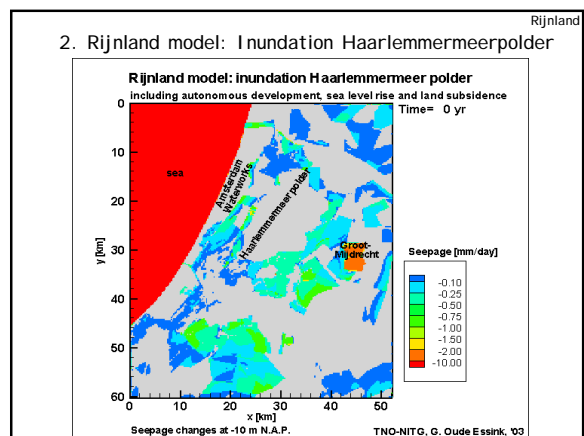
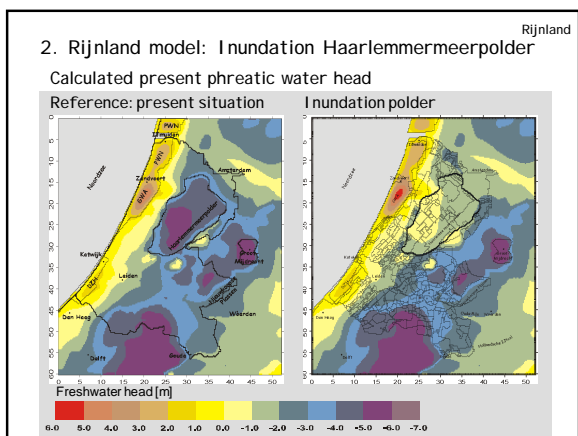
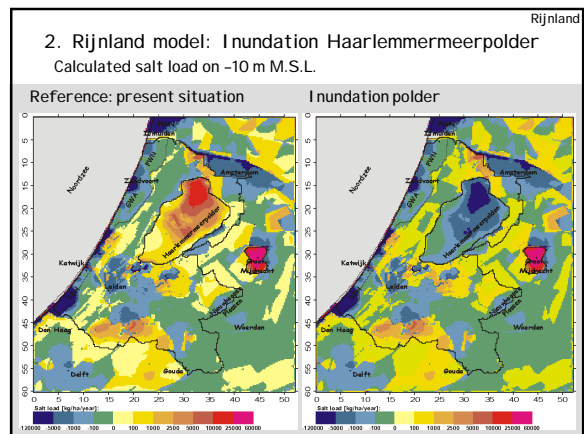
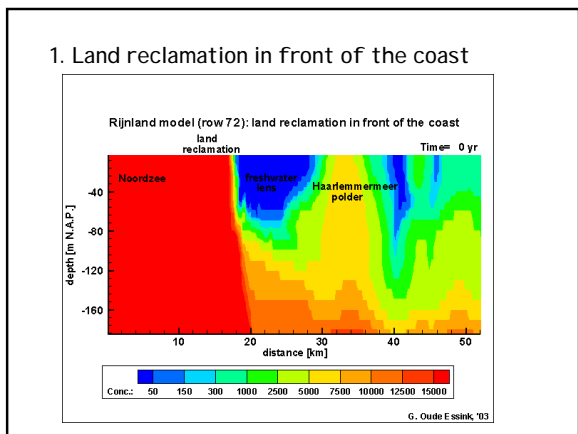
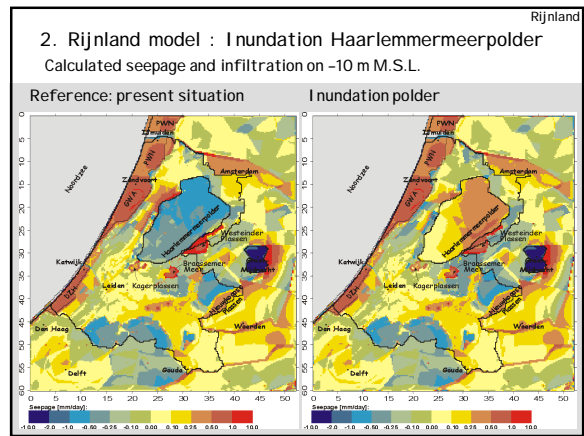
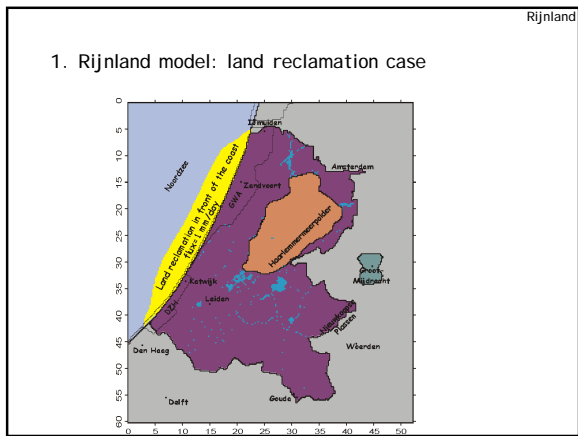
Rijnland

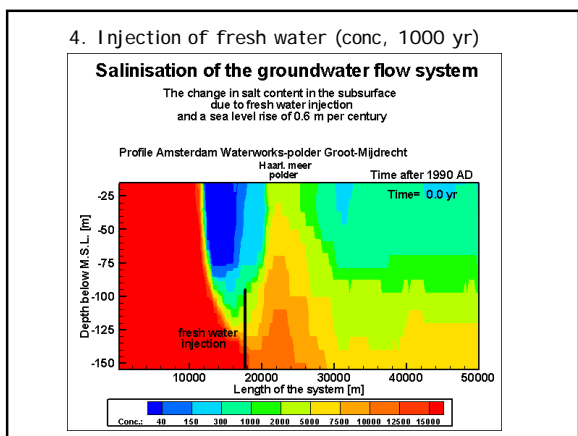
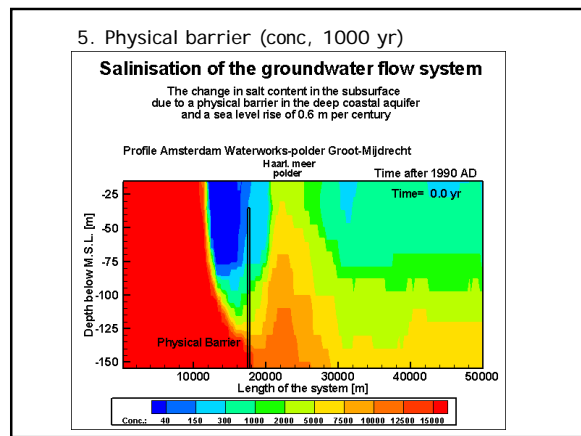
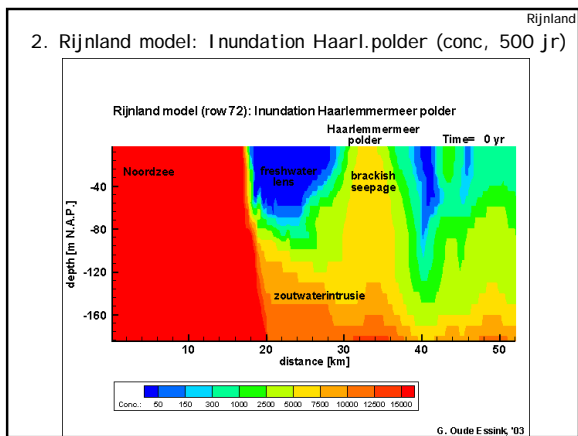
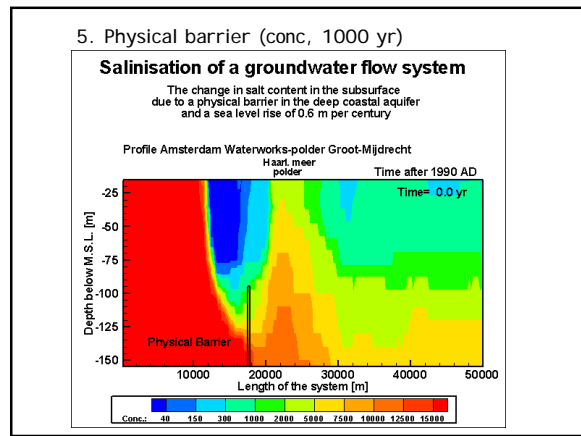
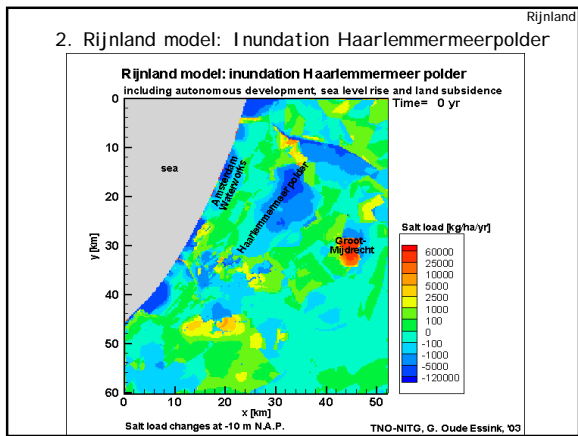
Four future scenarios (during 500 years):

- I. Reference case
 - to determine autonomous salt water intrusion
- II. Climate change case:
 - sea level rise of 0.9 m/century
 - increase of natural recharge in dunes with 6%
 - decrease of groundwater extraction in some sand-dunes
 - land subsidence in polder area: 0.3 and 1.0 m/century
- III. Compensating measures



- Solutions
- Possible measures to compensate salt water intrusion
1. Land reclamation in front of the coast
 2. Inundation of low-lying polders
 3. Extraction of saline/brackish groundwater
 4. Infiltration of fresh surface water
 5. Creating physical barriers





MOCDENS3D

MOCDENS3D is similar to SEAWAT

modelling

MOCDENS3D

non-steady 3D variable-density groundwater flow

- Genesis present salt-fresh distribution
- Upconing of saline groundwater under extraction wells
- Effects of land subsidence and climate change on groundwater systems

MOCDENS3D

Characteristics MOCDENS3D:

- integration of MODFLOW and MOC3D
- finite difference method for groundwater flow
- method of characteristics (particle tracking) for solute transport
- transient flow of groundwater

Advantage MOCDENS3D:

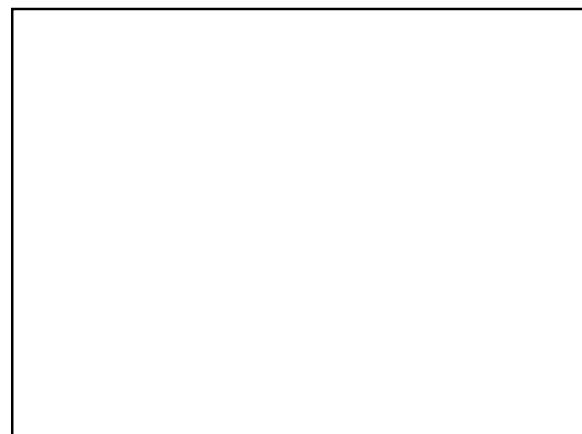
- no numerical problems if grid Peclet numbers are high
- large-scale geometries with limited number of elements are no problem

MOCDENS3D

MOCDENS3D

MOCDENS3D = MOC3D (*Konikow et al., 1996*)
but adapted for density differences

- density dependent groundwater flow
 - motion: Darcy
 - continuity: mass balance
- solute transport
 - advection
 - hydrodynamic dispersion: mixing of solutes
- fresh, brackish and saline groundwater
- relation between density & concentration



Solving the solute transport equation

MOC particle tracking

MOC3D

Advantage of the MOC approach by splitting up the advection-dispersion equation

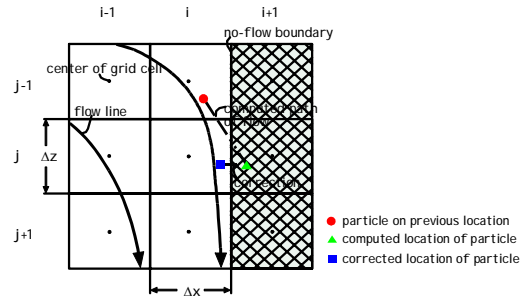
It is difficult to solve the whole advection-dispersion equation in one step, because the so-called Peclet-number is high in most groundwater flow/solute transport problems.

The Peclet number stands for the ratio between advection and dispersion

Procedure of MOC: advective transport by particle tracking

- Place a number of particles in each element
- Determine the effective velocity of each particle by (b)linear interpolation of the velocity field which is derived from MODFLOW
- Move particles during one solute time step Δt_{solute}
- Average values of all particles in an element to one node value
- Calculate the change in concentration in all nodes due to advective transport
- Add this result to dispersive/source changes of solute transport

Reflection in boundary



Steps in MOC-procedure

1. Determine concentration gradients at old timestep k-1
2. Move particles to model advective transport
3. Concentration of particles to concentration in element node
4. Determine concentration gradients on new timestep k*
5. Determine concentration in element node after advective, dispersive/source transport on timestep k

Konikow and Bredehoeft, 1978

Stability criteria (III)

3. Courant criterium

- * Node element
- Particle

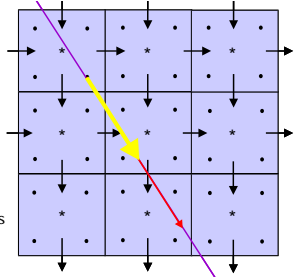
- Velocity direction
- Movement particles

$$0 < \xi \leq 1$$

$$\Delta t_s \leq \frac{\xi \Delta x}{V_{x,\max}}$$

$$\Delta t_s \leq \frac{\xi \Delta y}{V_{y,\max}}$$

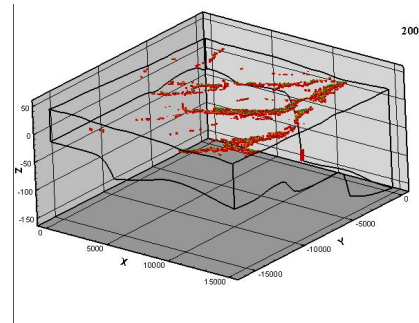
$$\Delta t_s \leq \frac{\xi \Delta z}{V_{z,\max}}$$

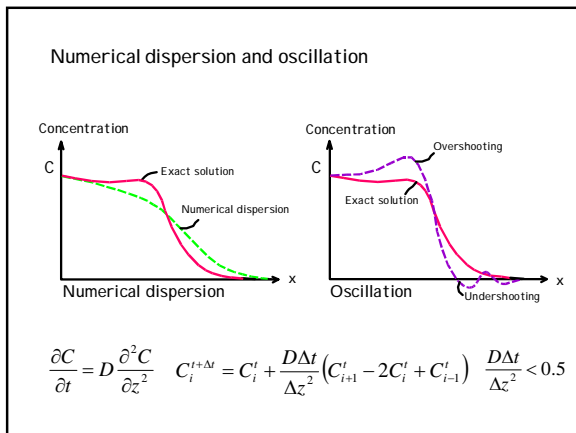


Causes of errors in MOC-procedure

1. Concentration gradients
2. Average from particles to node element, and visa versa
3. Concentration of sources/sinks to entire element
4. Empty elements
5. No-flow boundary: reflection in boundary

Courant criterion: places where timestep is smaller than 40 days





3D problems

Numerical dispersion problem (III)

Now follows an transient salt water intrusion case to demonstrate why in many coastal aquifers the longitudinal dispersivity α_L [L] should be small

3D problems

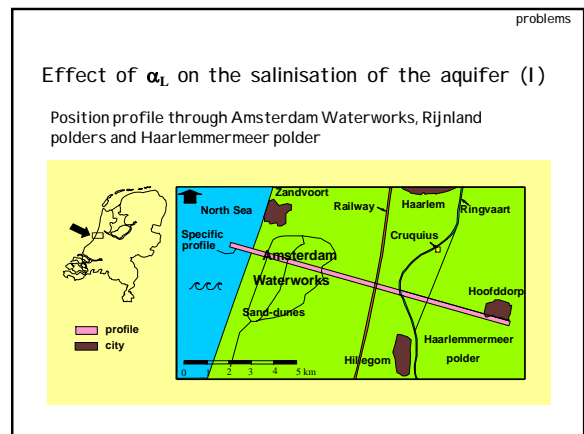
Numerical dispersion problem (I)

To solve the advection-dispersion equation, standard finite difference and element techniques should consider the following spatial discretisation criterion:

Peclet number $Pe \leq 2$ to 4

where: $Pe = \frac{V\Delta x}{D_h}$

V = effective velocity [L/T]
 Δx = dimension grid cell [L]
 D_h = hydrodynamic dispersion [L²/T]



3D problems

Numerical dispersion problem (II)

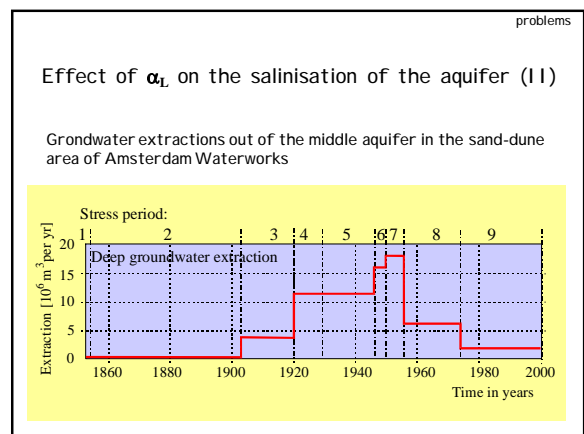
For advection dominant groundwater flow, the Peclet number can be rewritten as:

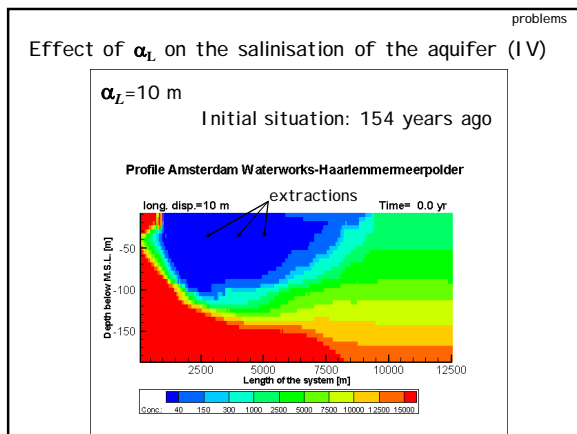
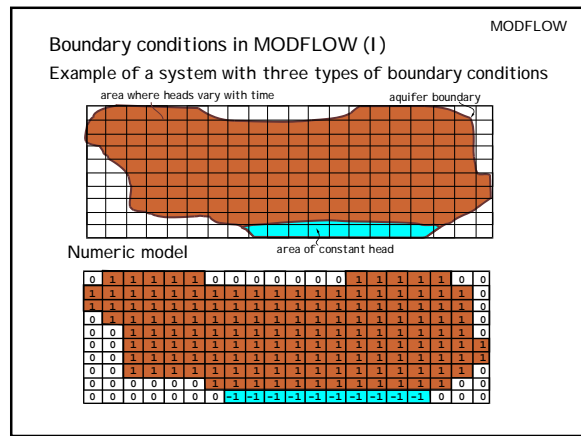
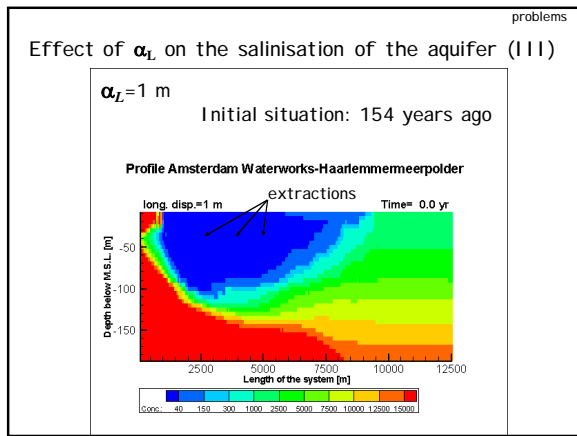
$\Delta x \leq 2\alpha_L$ to $4\alpha_L$

where α_L = longitudinal dispersivity [L]

What does that mean?

If α_L is small, then Δx should be small too!!





MODFLOW

Boundary conditions in MODFLOW (II)

For a constant head condition: IBOUND<0
 For a no flow condition: IBOUND=0
 For a variable head: IBOUND>0

MODFLOW

- MODFLOW
- Packages in MODFLOW
1. Well package
 2. River package
 3. Recharge package
 4. Drain package
 5. Evaporation package
 6. General head package

1. Well package

$$Q_{well} = Q_{i,j,k}$$

Example: an extraction of 10 m³ per day should be inserted in an element as:

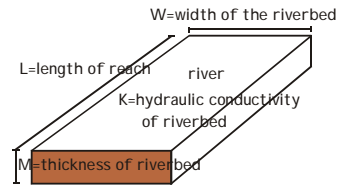
$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

$$Q_{ext,i,j,k} = -10 \quad (\text{in} = \text{positive})$$

$$Q'_{i,j,k} = -10$$

2. River package (III)

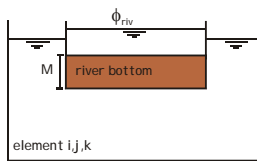
Determine the conductance of the river in one element:



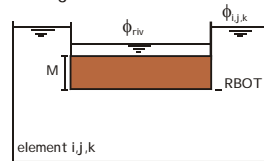
where $C_{riv} = \frac{KLW}{M}$ is the conductance [L²/T] of the river

2. River package (I)

river loses water



river gains water

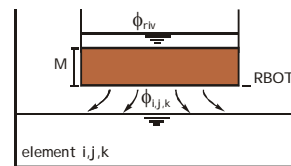


$$Q_{riv} = KLW \left(\frac{\phi_{riv} - \phi_{i,j,k}}{M} \right)$$

$$Q_{riv} = \frac{KLW}{M} (\phi_{riv} - \phi_{i,j,k}) \Leftrightarrow Q_{riv} = C_{riv} (\phi_{riv} - \phi_{i,j,k})$$

2. River package (IV)

Leakage to the groundwater system



Special case:

if $\phi_{i,j,k} < RBOT$, then $Q_{riv} = C_{riv} (\phi_{riv} - RBOT)$

2. River package (II)

$$Q_{riv} = C_{riv} (\phi_{riv} - \phi_{i,j,k})$$

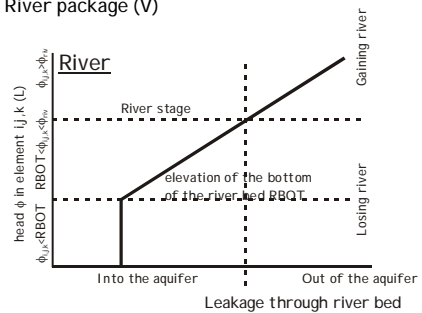
Example: the river conductance C_{riv} is 20 m²/day and the river level=3 m, then this package should be inserted in an element as:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

$$Q_{ext,i,j,k} = 20(3 - \phi_{i,j,k})$$

$$Q'_{i,j,k} = 60 \quad \text{and} \quad P_{i,j,k} = -20$$

2. River package (V)

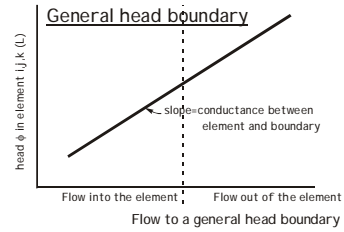
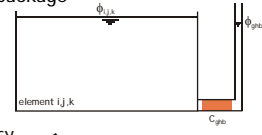


3. Recharge package

$$Q_{rec} = I\Delta x\Delta y$$

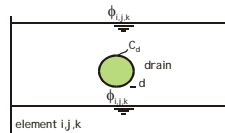
6. General head boundary package

$$Q_{ghb} = C_{ghb}(\phi_{ghb} - \phi_{i,j,k})$$



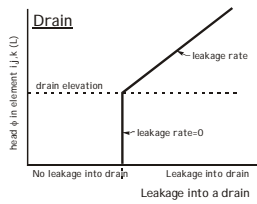
4. Drain package

$$Q_{dm} = C_{dm}(\phi_{i,j,k} - d)$$



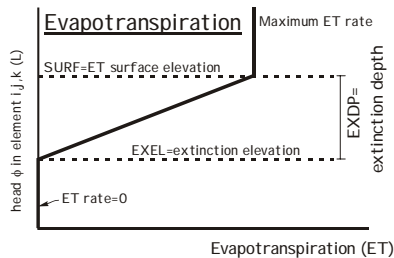
Special case:

if $\phi_{i,j,k} < d$ then $Q_{dm} = 0$



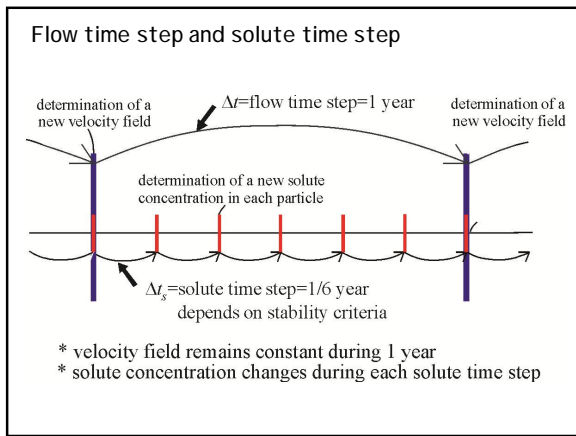
- 1 (name).bas-file
- 2 (name).bcf-file
- 3 (name).moc-file
- 4 (name).wel-file
- 5 (name).riv-file
- 6 (name).drn-file
- 7 (name).ghb-file
- 8 (name).sip-file
- 9 densin.dat-file
- 10 (name).nam-files

5. Evapotranspiration package



Time indication MODFLOW

- ! TMUNI =1: seconde
- ! TMUNI =2: minute
- ! TMUNI =3: hour
- ! TMUNI =4: day
- ! TMUNI =5: year

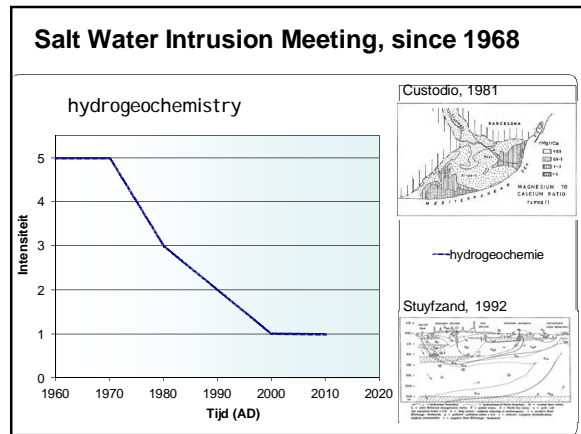
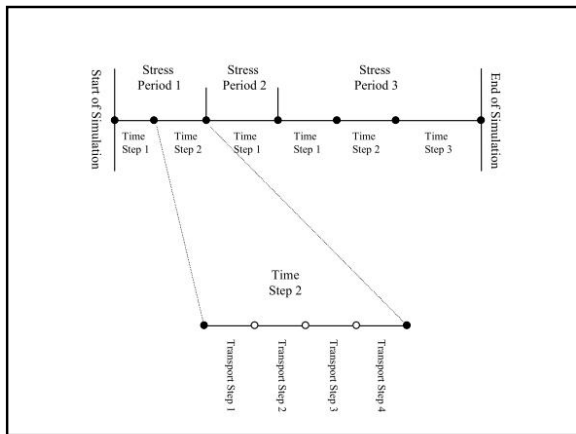


Salt Water Intrusion Meeting, since 1968

<http://www.swim-site.org/>

Subthemes:

- hydrogeochemistry
- monitoring (a.o. geophysical methods)
- fresh-saline interface modelling
- 2D modelling variable-density & solute transport
- submarine groundwater discharge
- sea level rise
- 3D modelling variable-density & solute transport
- solutions
- paleohydrogeology fresh-saline
- global analysis

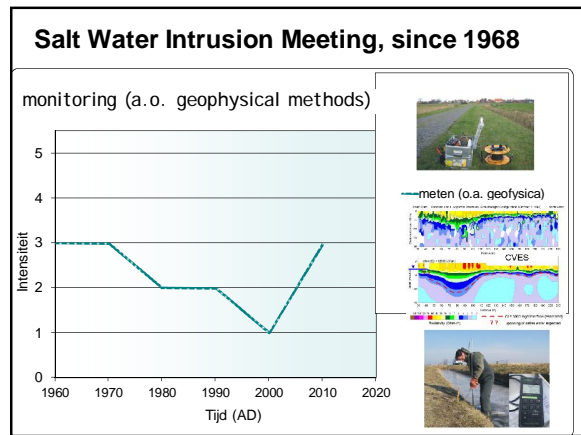


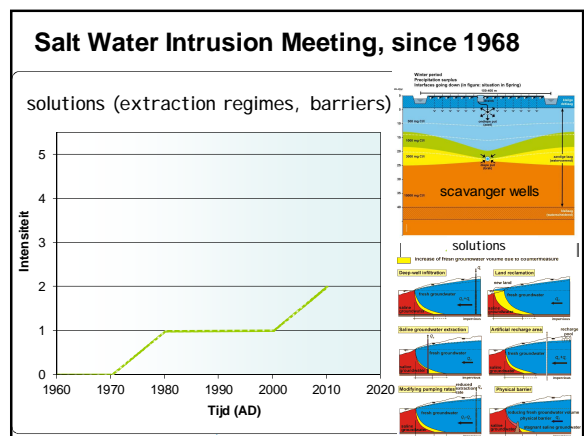
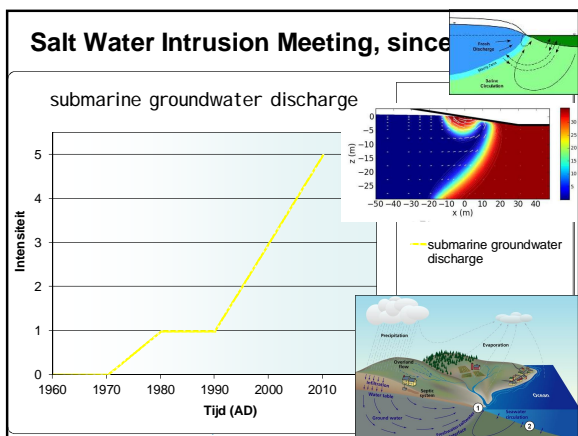
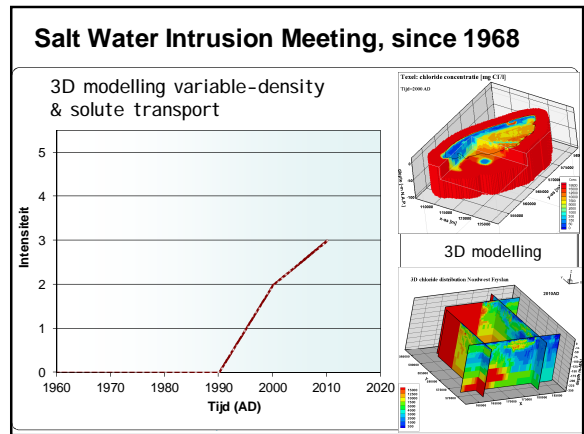
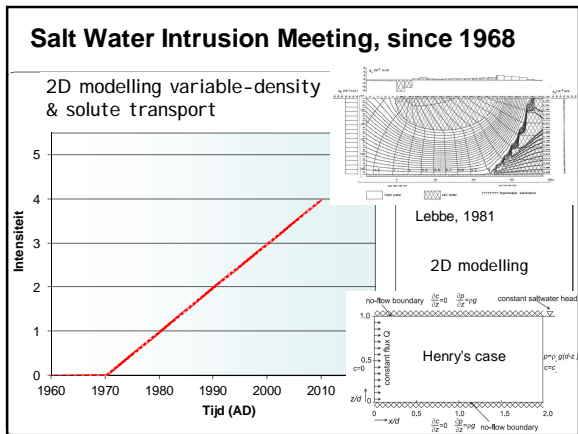
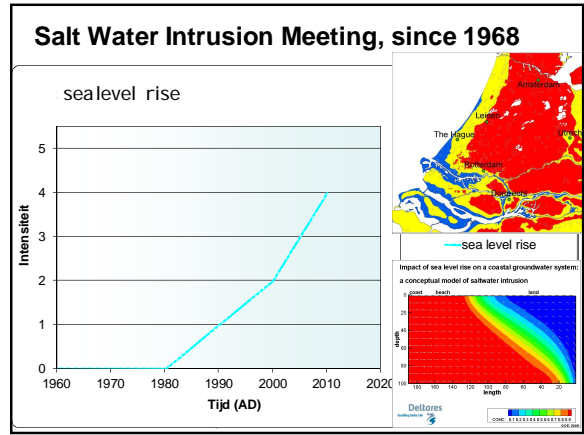
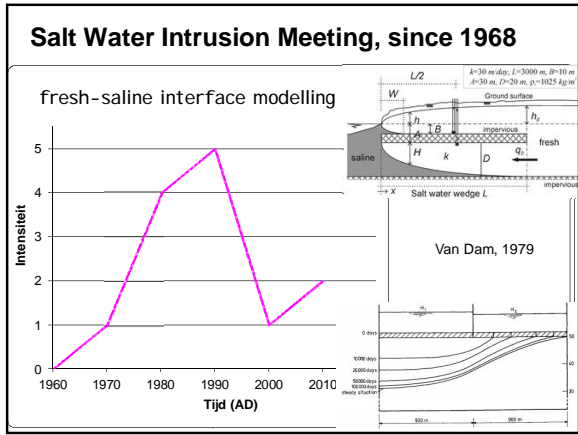
Salt Water Intrusion Meeting, since 1968

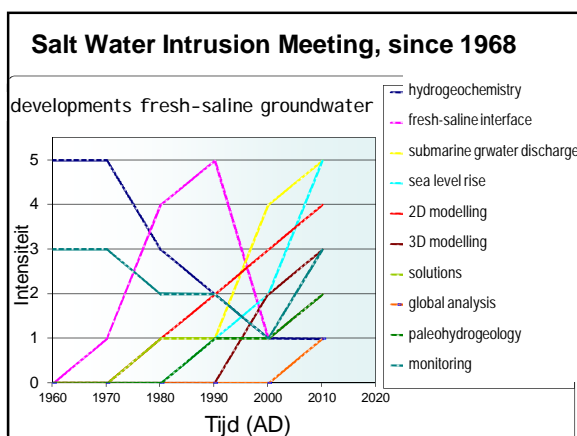
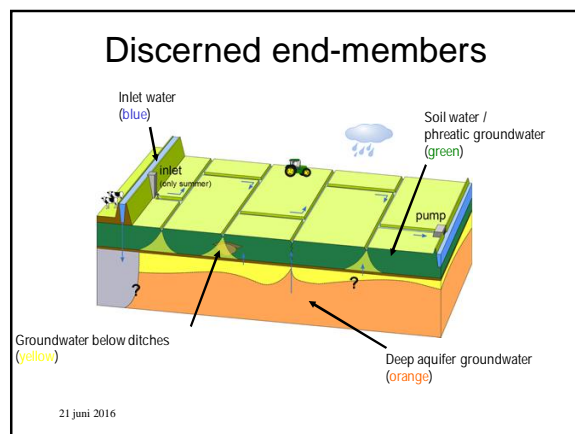
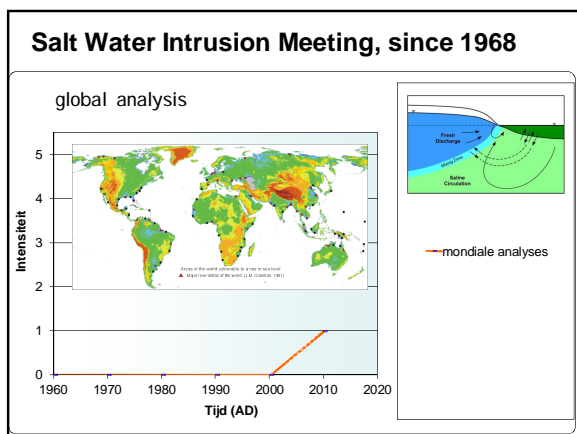
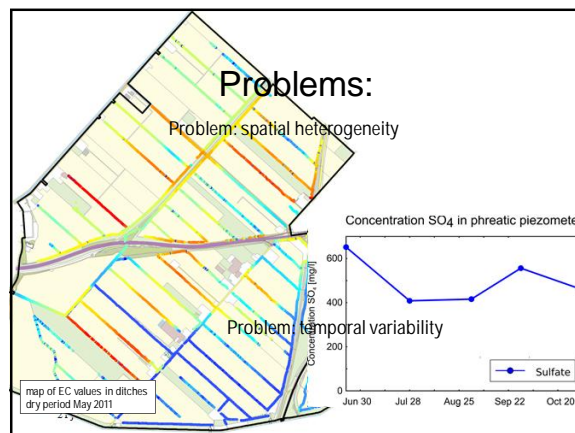
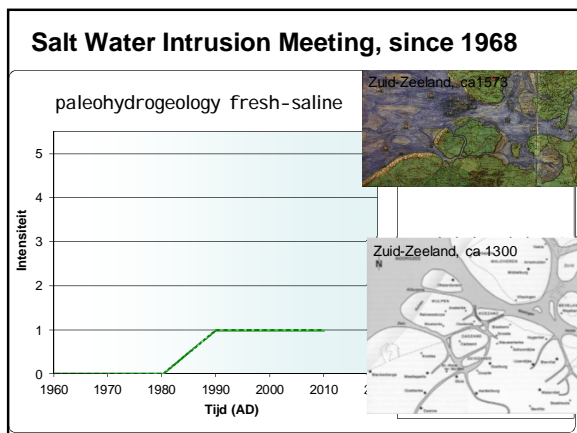
<http://www.swim-site.org/>

Themes

- Water system analysis
- Monitoring
- Modelling
- Effects
- Solutions



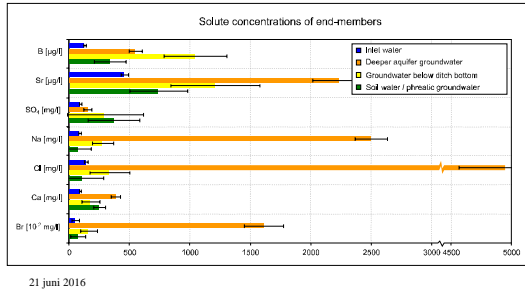




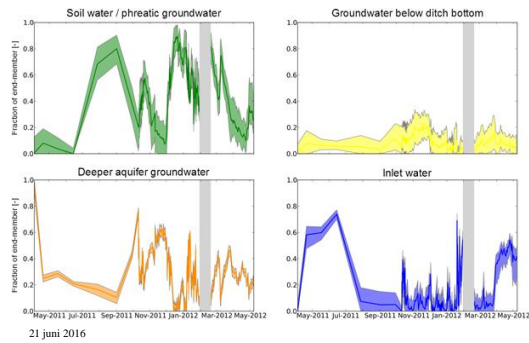
Sampling program

- Summer 2011: monthly sampling
 - Shallow piezometers
 - on fields
 - below ditch bottom
 - Intake water canal
 - Surface water in ditches
 - Precipitation
- October 2011: installation automatic sampler at catchment outlet
- Irregular sampling of end-member deep aquifer groundwater

End-member chemical signature



Result: End-member fractions +



End-member fractions

