

IHE 2018

# Density dependent groundwater flow in the coastal zone

Gualbert Oude Essink, PhD

Lecture set-up:

- PowerPoint sheets
- Lecture Notes
- Practicals numerical modelling

<http://freshsalt.deltares.nl>



Deltarès  
Unit Subsurface and Groundwater Systems  
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13-14-15 June 2018

Introduction

## Curriculum Vitae

- Delft University of Technology, Civil Engineering: till 1997  
Ph.D.-thesis: Impact of sea level rise on groundwater flow regimes
- Utrecht University, Earth Sciences: till 2002
- Free University of Amsterdam, Earth Sciences: till 2004
- Deltarès
- Utrecht University (Associate Professor): from 2014

### Qualifications:

- Groundwater resources management
- Density-dependent groundwater flow and coupled solute transport
- Salt water intrusion in coastal aquifers
- Assessment of climate change on groundwater resources
- Numerical Modeling
- Teaching and training

<http://freshsalt.deltares.nl>  
Deltarès: gualbert.oudeessink@deltares.nl

# Colleagues at Deltares

## Groundwater in the Coastal Zone

<http://zoetzout.deltares.nl>  
<http://freshsalt.deltares.nl>



Gualbert Oude Essink Joost Delsman



Link Joost Delsman Pieter Pauw



Pieter Pauw



Perry de Louw



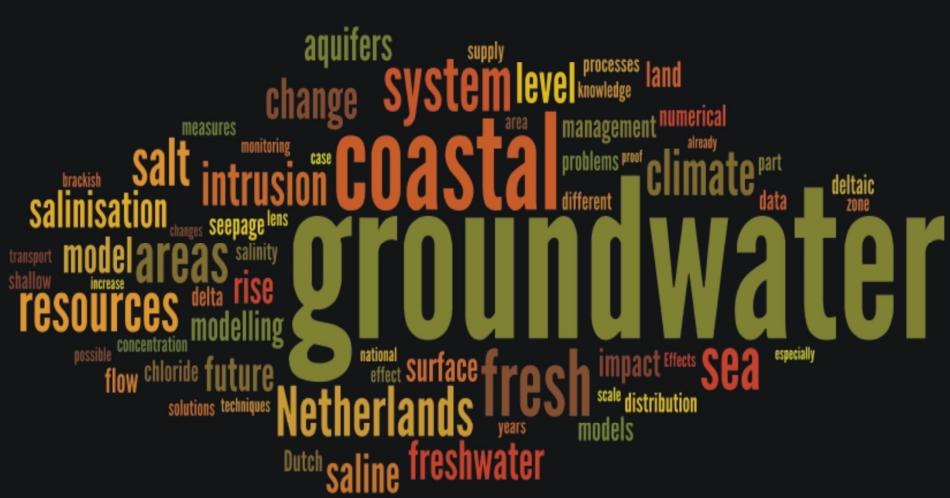
Esther van Baaren



Jarno Verkaik



Marta Faneca



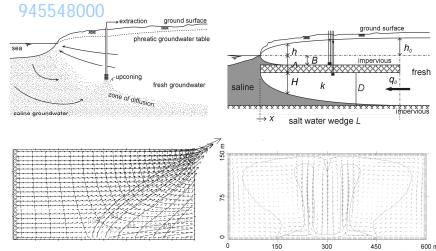
## Research on groundwater in the coastal zone

- 18 years experience in modelling variable-density dependent groundwater flow and coupled solute transport in the coastal zone
- Incorporating monitoring campaigns results in numerical modeling tools
- Research on new fresh-saline phenomenae: salty seepage boils and shallow freshwater lenses in saline environments
- Knowledge on creating 3D initial chloride distribution, based on geostatistics and geophysical data (analyses, VES, borehole measures, AEM)
- Quantifying effects of climate change and sea level rise on fresh groundwater resources
- Developing adaptive and mitigative measures to stop salinization in the coastal groundwater system (e.g. ASR, MAR: fresh keeper, coastal collectors, freshwater storage underground)

Lecture notes, practicals and ppt on [freshsalt.deltares.nl](http://freshsalt.deltares.nl)

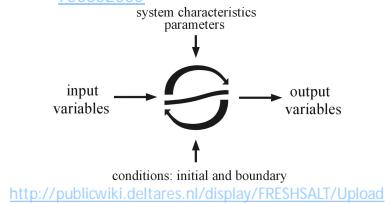
### 1. Density dependent groundwater flow

<http://publicwiki.deltares.nl/download/attachments/22183944/gwm2.pdf?version=1&modificationDate=1268945548000>



### 2. Groundwater modelling

<http://publicwiki.deltares.nl/download/attachments/22183944/gwm1.pdf?version=1&modificationDate=1268750652000>



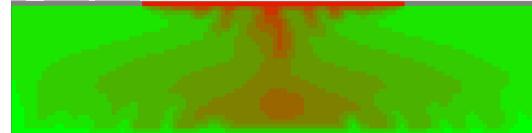
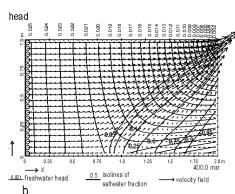
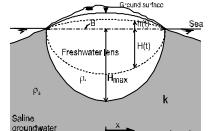
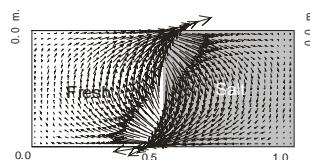
## Practicals numerical modelling

- PMWIN
  - SEAWAT
  - Cases:
    - Rotating sharp interface
    - Freshwater lens
    - Henry's case
    - (Elder's case)
  - Setup practicals:
    - work in small groups of two persons
    - short report of findings (make screenshots)
    - deliver within one week after finish last lectures

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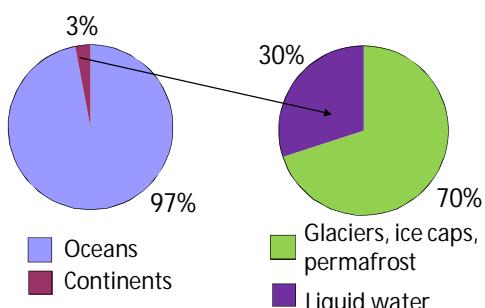
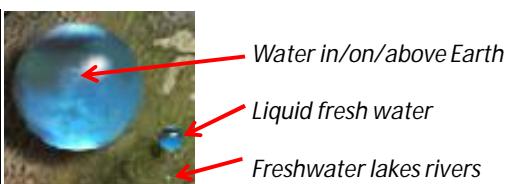
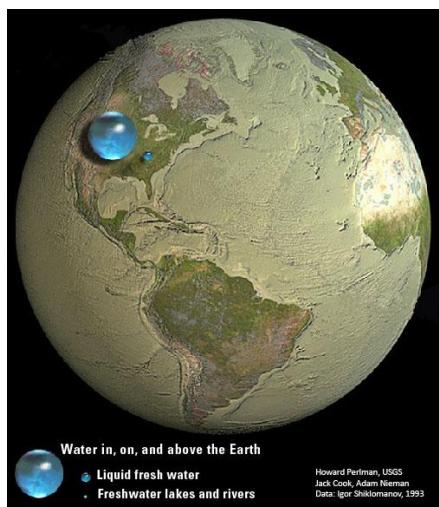
## Practicals

- Rotating sharp interface
  - Freshwater lens
  - Henry's case
  - (Elder's case)





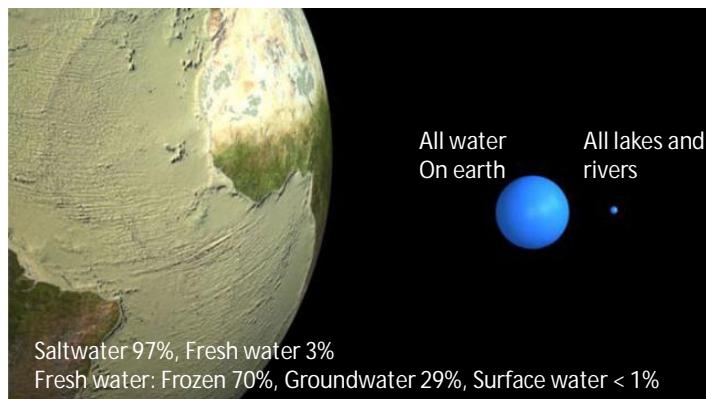
## Volumes of water on Earth: a scarce product



Source: Perlman, USGS; Shiklomanov, 1993

## Water Energy Food Nexus Global water scarcity

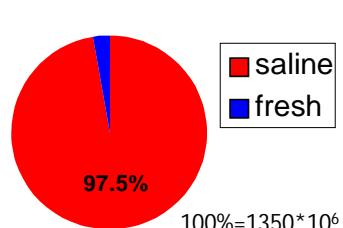
Fresh water is a scarce resource...



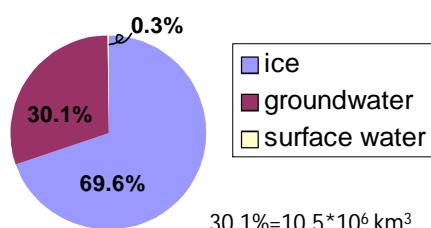
## Introduction

### Water on Earth

Total water on Earth



Total fresh water on Earth

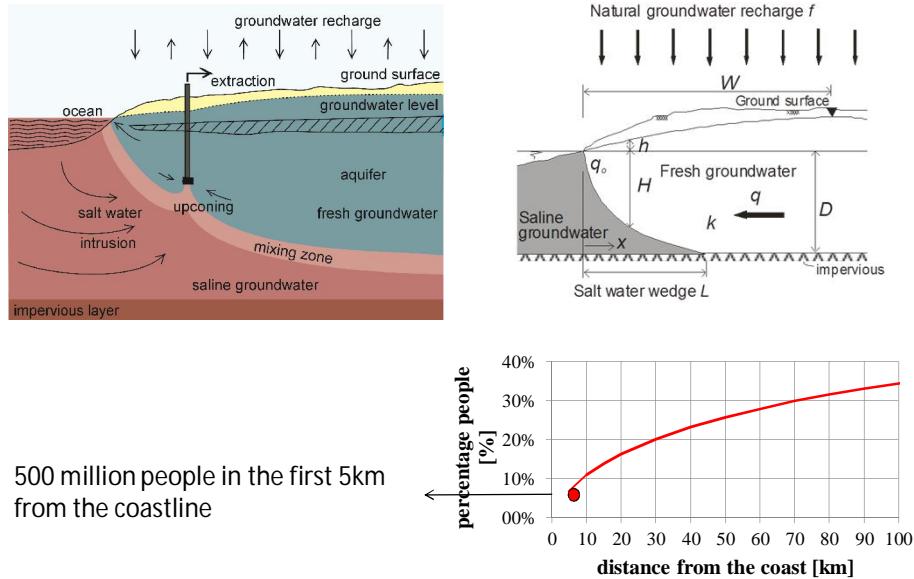


Demand for groundwater (now 30%) increases due to:

- increase world population & economical growth
- loss of surface water due to contamination
- great resource: available in large quantities
- still unpolluted (relative to surface water)

(Source: Cheng, 1998)

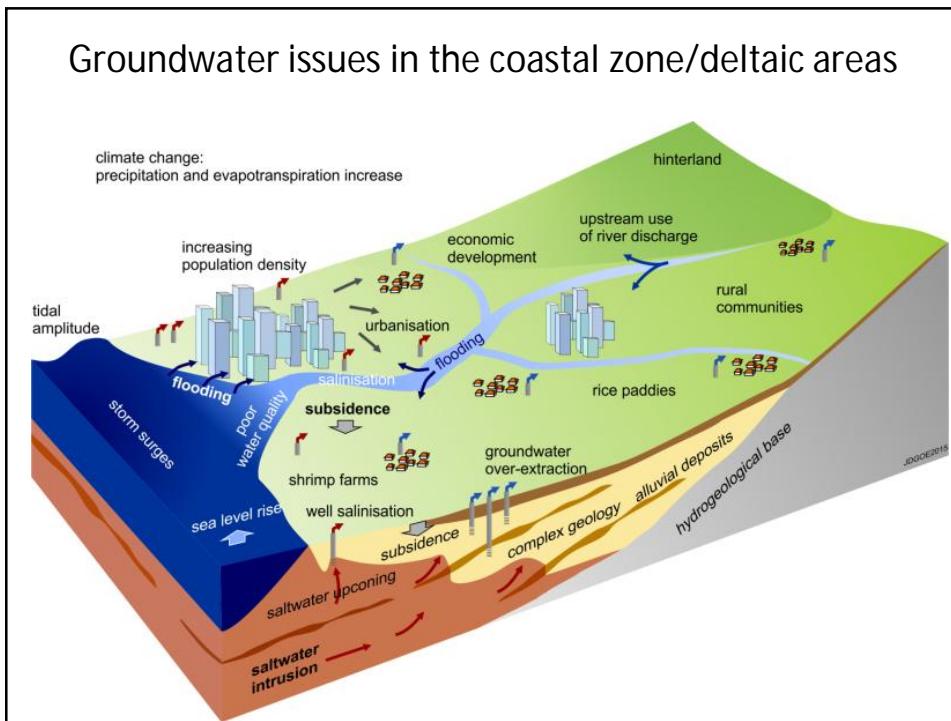
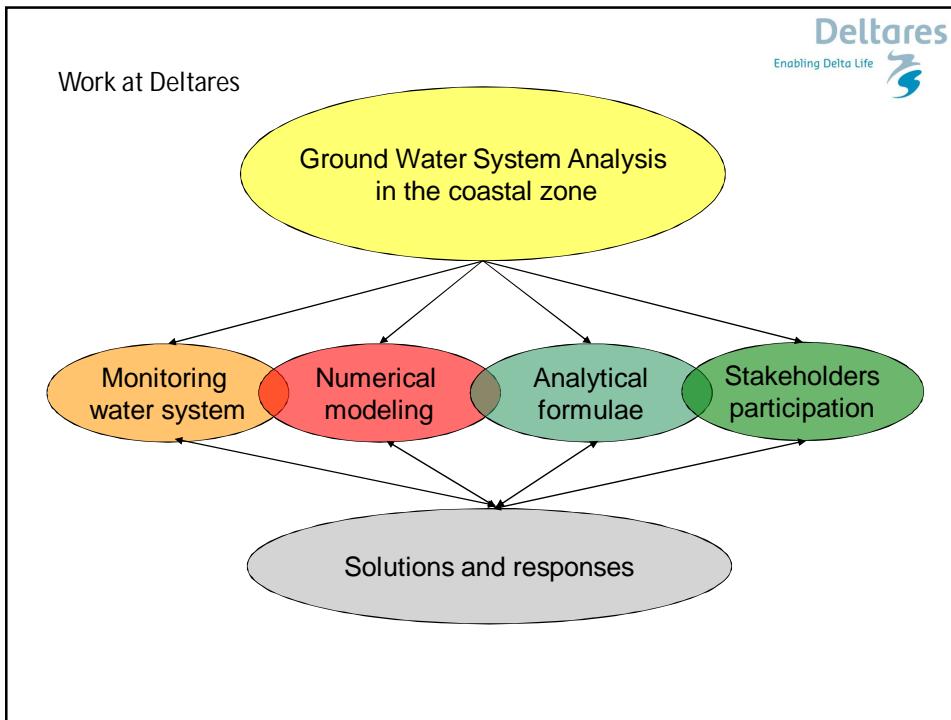
## Groundwater in the coastal zone



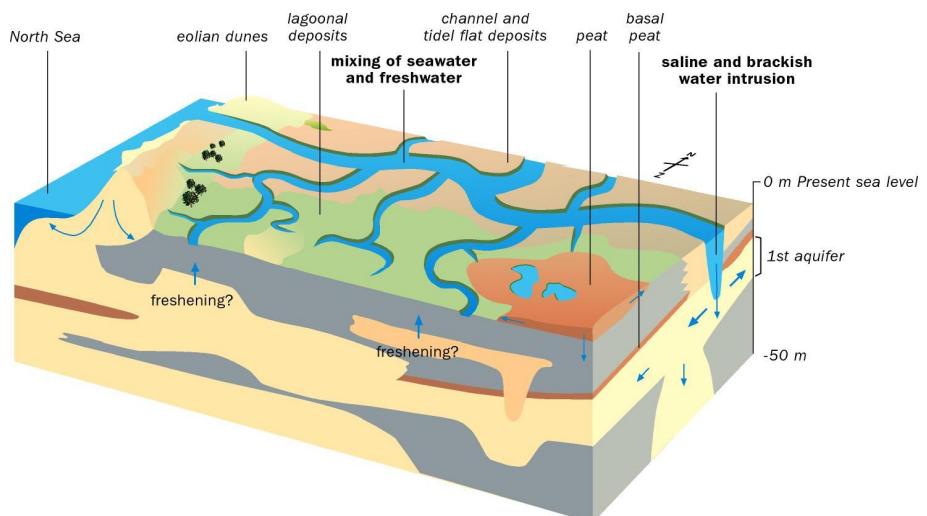
Introduction

### Topics of density driven groundwater flow

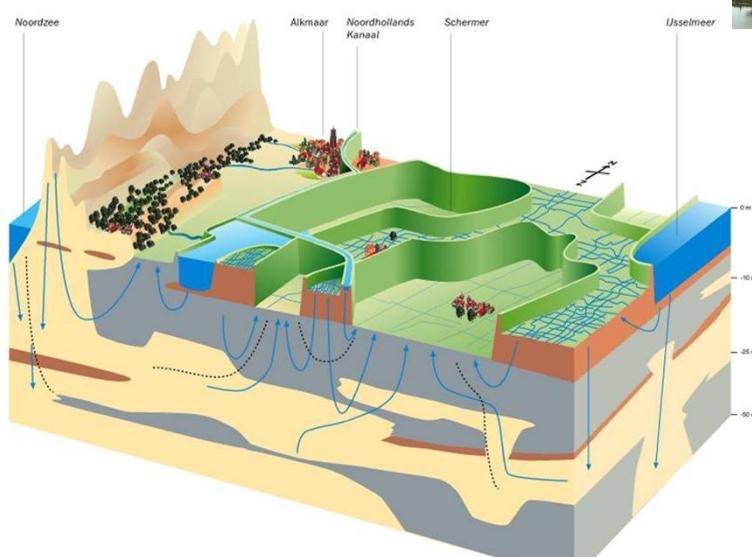
1. Introduction
  - water on earth
  - salt water intrusion
  - freshwater head
2. Interface between fresh and saline groundwater
  - analytical formulae (Badon Ghyben-Herzberg)
  - upconing example
3. Numerical modelling
  - mathematical background
  - Benchmark problems: Henry, Elder, Hydrocoin, etc.
4. Case-studies
  - hypothetical cases
  - 2D, 3D cases
  - real cases (Dutch coastal zone)



## Past, before man



## The polders in the Nederland



## Groundwater in the future

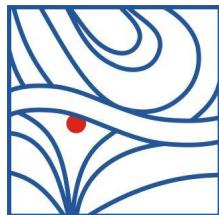
We have to cope with....:

- We have to cope with....:
- Groundwater extractions
- Development energy use/production (heat-cold)
- Climate change
- Land subsidence
- Development spatial land use
- Politics, Policy & Watermanagement

*Direct anthropogenic influence on groundwater is more important than climate effect*

Salt Water Intrusion Meeting, since 1968

## Salt Water Intrusion Meeting, since 1968



<http://www.swim-site.org/>

### Themes

- Water system analysis
- Monitoring
- Modelling
- Effects
- Solutions



### Salt Water Intrusion Meeting (SWIM)

[Home](#)   [History](#)   [Philosophy](#)   [Next meeting](#)   [Proceedings](#)   [Links](#)

#### Welcome to the homepage of the Salt Water Intrusion Meeting

The Salt Water Intrusion Meeting (SWIM) conference series has been held in different countries on a biennial basis since 1968. Although the main focus has traditionally been on seawater intrusion, contributions related to saline groundwater more broadly are also considered. The meetings are attended by a multidisciplinary group of people with a wide variety of expertise, including chemistry, engineering, geology, geophysics, mathematics, physics, and management.



The long-lived success of the conference series reflects the relevance of managing saline groundwater problems around the world, especially in densely populated coastal areas. These include:

- increased demand due to economic development and population growth
- over-exploitation of water resources, especially in arid and semi-arid areas
- contamination and quality deterioration of water resources
- characterization of groundwater systems and movement of saline groundwater
- management and prevention of salinization
- natural and man-made environmental change

[www.swim-site.org](http://www.swim-site.org)

The main aims of this web site are to be the central and permanent source of information for people interested in the SWIM and to increase awareness and provide access of the excellent work that is presented at the SWIM meetings

**Salt Water Intrusion Meeting (SWIM)**

Home | History | Philosophy | Next meeting | **Proceedings** | Links

**The proceedings of the Salt Water Intrusion Meeting**

The SWIM proceedings span a period of almost 40 years. The proceedings of the first informal meeting consisted of a few pages in German. Successive meetings all had regular proceedings. They provide an excellent overview of the developments in the research of saline groundwater over the past decades.

At the 18th SWIM in Cartagena it was agreed that efforts will be undertaken to make all SWIM proceedings available through the internet. Currently, the proceedings of the 9th, 12th, 13th, 15th, 16th, 17th, 18th, 20th, and 21st SWIM and the abstracts of the 18th SWIM are available from this web site. The proceedings of other meetings will become available as soon as they have been digitized. Some hardcopies of proceedings can still be ordered from various publishers. Links to these are provided on this page.

**Available for download:**

- 24th SWIM Cairns, Australia, 2016
- 23rd SWIM Husum, Germany, 2014
- 22nd SWIM, Buzios, Brazil, 2012
- 21st SWIM, S. Miguel Azores, Portugal, 2010
- 20th SWIM, Naples, Florida, USA, 2008 (abstracts)
- 19th SWIM, Cagliari, Italy, 2006
- 18th SWIM, Cartagena, Spain, 2004
- 18th SWIM, Cartagena, Spain, 2004 (abstracts)
- 17th SWIM, Delft, The Netherlands, 2002
- 16th SWIM, Wolin Island, Poland, 2000
- 15th SWIM, Ghent, Belgium, 1998
- 14th SWIM, Malmö, Sweden, 1996
- 13th SWIM, Cagliari, Italy, 1994
- 12th SWIM, Barcelona, Spain, 1992
- 11th SWIM, Danzig, Poland, 1990
- 10th SWIM, Ghent, Belgium, 1988
- 9th SWIM, Delft, The Netherlands, 1986
- 8th SWIM, Bari, Italy, 1983
- 7th SWIM, Uppsala, Sweden, 1981
- 6th SWIM, Hanover, Germany, 1979
- 5th SWIM, Wednesham, United Kingdom, 1977
- 4th SWIM, Ghent, Belgium, 1974
- 3rd SWIM, Copenhagen, Denmark, 1972
- 2nd SWIM, Vogelzang, The Netherlands, 1970
- 1st SWIM, Hannover, Germany, 1968

**For sale (external links)**

- Proceedings of the 12th Salt Water Intrusion Meeting, Barcelona, Spain, 1992
- Proceedings of the 8th Salt Water Intrusion Meeting, Hannover, Germany, 1979

**www.swim-site.org**

**Salt Water Intrusion Meeting (SWIM)**

Home | History | Next meeting | **Proceedings** | Links | About this site

[Back to all proceedings](#)

**Proceedings of the 24th Salt Water Intrusion Meeting, Cairns, Australia, 2016**

Preface  
A.D. Werner

Posters

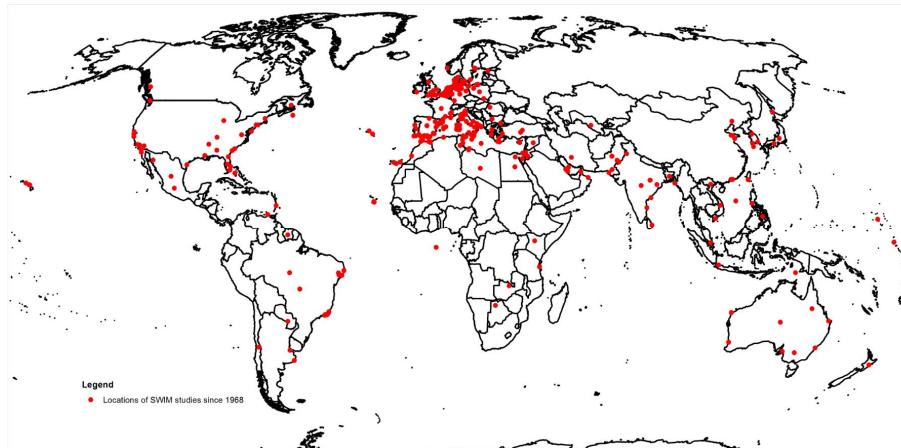
S. Fatema, A. Marandi, C. Schüth Seawater Intrusion of the Coastal Groundwater: A Case Study in Cox's Bazar, Bangladesh  
A. Kawachi, C. Uchida, M. Kefi, J. Tarhouni, K. Kashiwagi Effect of Surface Water Use on Mitigation of GW Salinization in a Semi-Arid Coastal Shallow Aquifer Setting: A Case Study of Lower Lebna Watershed, Tunisia  
D. Vandeveldé Increasing the Availability of Freshwater for Agriculture by Improving Local Hydro(geo)logical Conditions  
Elhajer, A. E., Luc Lebbe, F. Sadooni, Hamad Al Saad Potential Influence of Climate Change and Anthropogenic Effects, on Groundwater Resources in the Northern Groundwater Project, Qatar  
J. van Erp, G.H.P. Oude Essink, M.F.P. Bierens Fresh Groundwater Reserves in 40 Major Deltae Under Global Change  
Bernard Simon, Esther van Baaren, Willem Dabekkussen, Joost Delsman, Jan Cuninkink, Marjorie Kersebaum, Perry G.B. de Louw, G.H.P. Oude Essink, Pieter Pauw, Annika Steuer HEM Survey in Zeeland (NL) to Deliniate 3D Groundwater Salinity Distribution - Pilot Study, Canal Zone Gent-Terneuzen  
Kees-Jan van der Made, Frans Schraars, Michel Groen Geophysical Field Measurements for Characterizing Sea Water Intrusion  
Koujingt Chen, Jili Jimmy Liap Hydrochemical Evolution of Groundwater in a Coastal Reclaimed Land in Shenzhen, China  
Georg J. Houben, Willem Jan Zaaasdorff, Klaus Hinsby, Lars Troldborg Water Supply on the Frisian Islands, North Sea  
Victoria Trigavnik, C. Robinson, Dean Morrow, Darren White, Viviane Paquin, Kela Weber Effect of Tides, Waves and Precipitation on Groundwater Flow Dynamics on Sable Island, Canada  
Perry G.B. de Louw, Guus Hesselman, Vincent Klap, Corstiaan Kempenaar, Edvard Ahnrichs, Jean-Pierre van Wesemael, Joost Delsman In Search for a Salt Tolerant Potato to Reduce the Freshwater Demand in Saline Coastal Areas  
Yongcheol Kim, Heesung Yoon, Gi-Pyo Kim Case Study on an Effective Method for Monitoring Temporal Change in the Freshwater-Saltwater Interface Location and Freshwater Lens Thickness  
J. van Erp, Thoman, Leanne K. Morgan, Tony Miller, Adrian D. Werner Vulnerability of Offshore Fresh Groundwater to Anthropogenic Impacts: Investigation Using Analytic and Numerical Modelling Techniques  
A. Saha, W.K. Lee, A. Brionne-Taine, V. Babovic, L. Vanhogen-Peeters, Esther van Baaren, P. Vermeulen, G.H.P. Oude Essink, J.R. Valstar, G. de Lange, R.M. Hoogendoorn, S. On Utilization of Reclaimed Island as Groundwater Reservoir  
M.L. Calavache, J.P. Sánchez-Ubeda, Carlos Duque, M. López-Chicano The Influence of the Heterogeneity and Variable Density in Theis and Cooper-Jacob Interpretation of Pumping Tests: The Case of Motril-Salobreña Aquifer (SE Spain)  
J.P. Sánchez-Ubeda, M.L. Calavache, Carlos Duque, M. López-Chicano Modelling Sea-Aquifer Contact in Salt Water Intrusion Scenarios: Conditions and Possibilities  
J.P. Sánchez-Ubeda, M.L. Calavache, Carlos Duque, M. López-Chicano Estimation of Hydraulie Diffusivity Using Tidal-Extracted Oscillations from Groundwater Head Affected by Tide  
Elad Leyvanov, Eyal Shalev, Yoseph Yechiel, Haim Gvirtzman The Mechanism of Groundwater Fluctuations Induced by Sea Tides in Unconfined Aquifers  
Gang Li, Haiping Li, Chunmiao Zheng, Kai Xiao, Manhua Luo, Meng Zhang A Comparative Study of Two Transects at Dan'ao River's Estuary in Daya Bay, China  
Xuejing Wang, Haiping Li, Chunmiao Zheng Seasonal Distribution of Radium Isotopes and Submarine Groundwater Discharge in Laizhou Bay, China  
Ke Li, Haiping Li, Chunmiao Zheng, Yanman Li, Manhua Luo A Preliminary Study on Influence of Seawater-Groundwater Exchange on Nutrient Dynamics in a Tidal Mangrove Swamp in Daya Bay, China  
Astraf Ahmed, Robert Gantry, Antoff Abdoullahli The Effect of Cutoff Walls on Saltwater Intrusion in Stratified Coastal Aquifers: An Experimental and Numerical Study  
Andrew C. Knight, Leanne K. Morgan, Adrian D. Werner Offshore Hydro-Stratigraphy of the Gambier Embayment and the Potential for an Offshore Groundwater Resource  
J. Oz, Eyal Shalev, Yoseph Yechiel, Haim Gvirtzman Saltwater Circulation Patterns Within the Freshwater-Saltwater Interface in Coastal Aquifers  
Sang Kil Park, Do Hoan Kim, Hong Bum Park The investigation of Sea Water Intrusion on Opening Estuary Barrage of Nakdong River Using Numerical Simulation Model  
Chenqi Shen, Pei Xin, Chenming Zhang, Ling Li Initiation of Unstable Flow in Salt Marshes

Session 1 - Managing Coastal Groundwater I

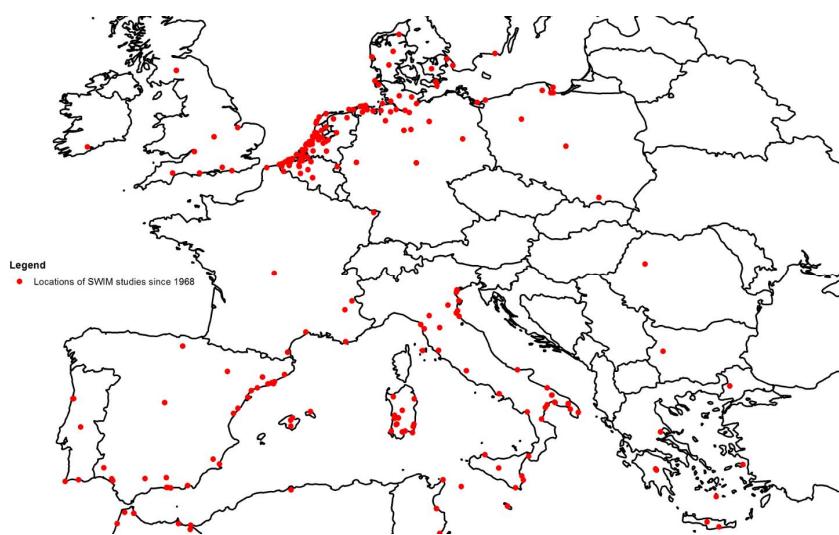
G.H.P. Oude Essink Fresh Groundwater Resources in Deltaic Areas Under Climate and Global Stresses, with Examples from Vietnam, Egypt, Bangladesh and The Netherlands

**www.swim-site.org**

## Location of SWIM studies since 1968



## Location of SWIM studies since 1968

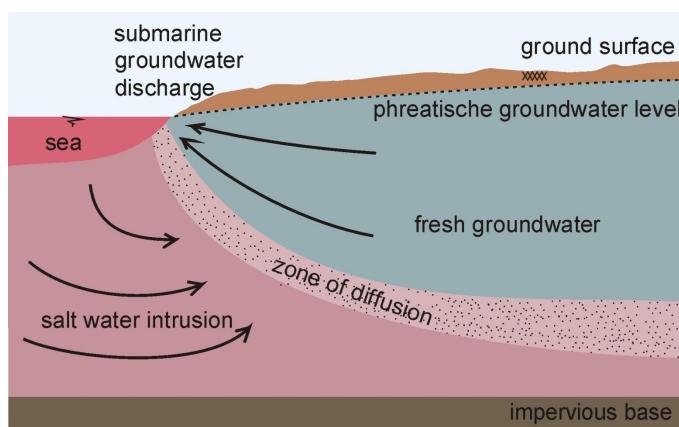


# Introduction SWI

Introduction

## Definition of salt water intrusion

*Inflow of saline water into an aquifer which contains fresh water*



## Origin of saline groundwater in the subsoil

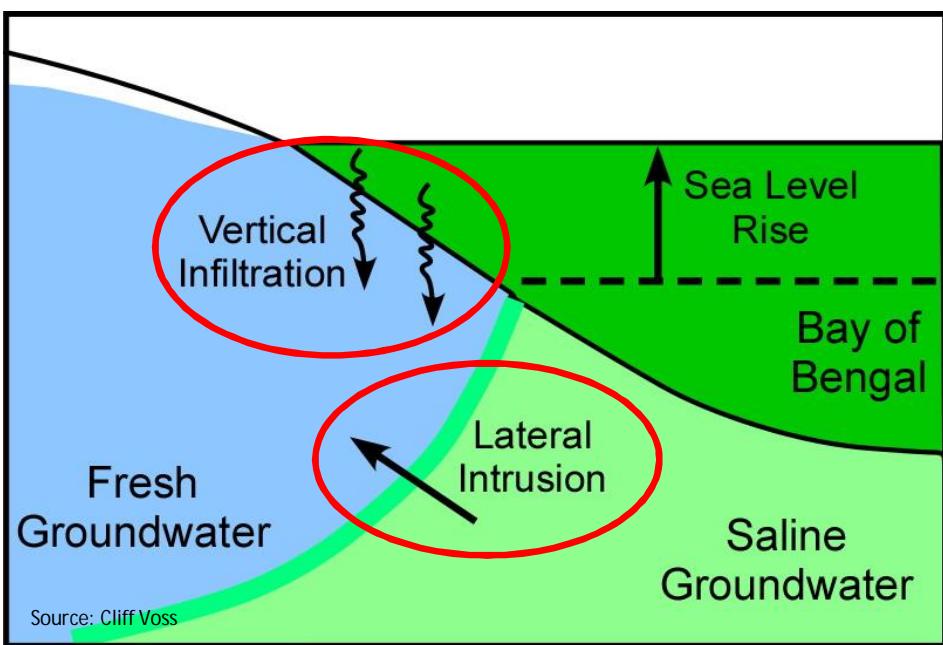
### Geological causes:

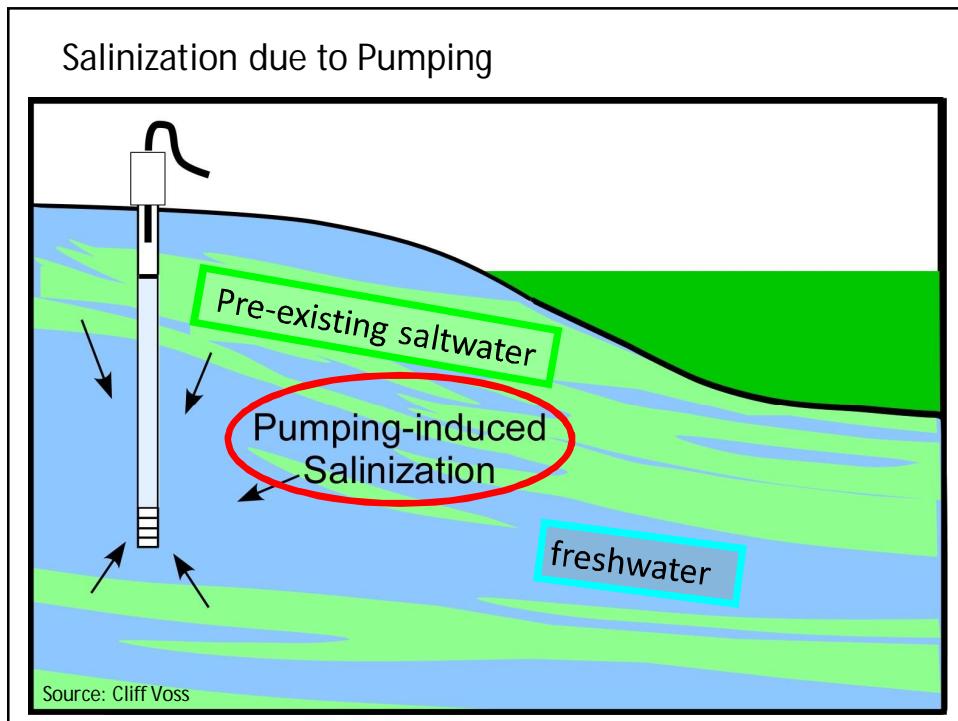
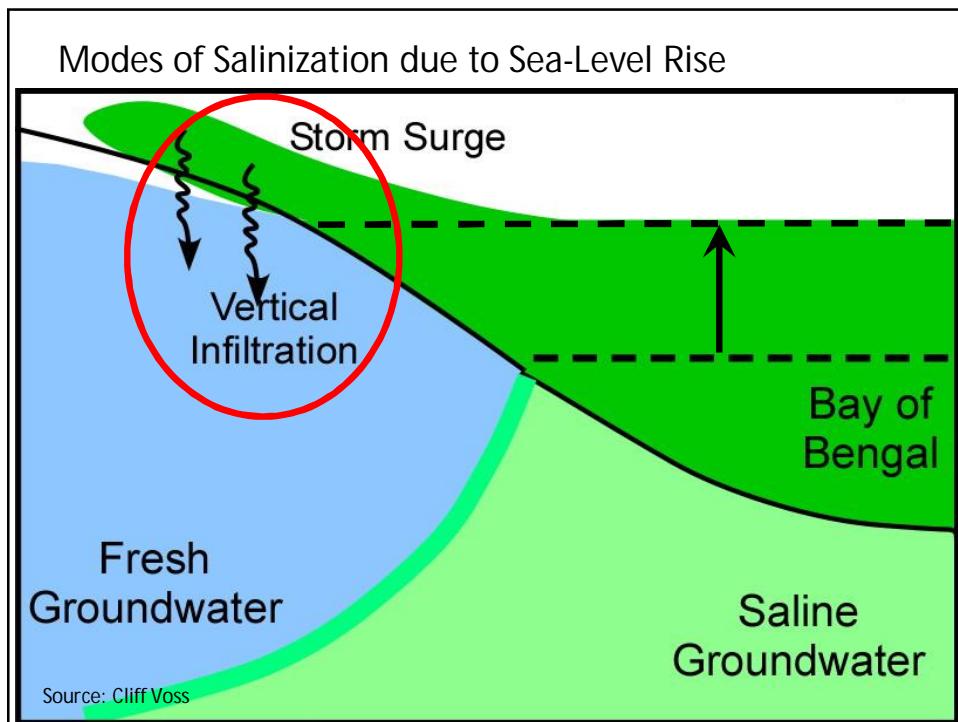
- marine deposits during geological times
- trans- and regressions in coastal areas (deltas)
- salt/brine dome

### Anthropogenic causes:

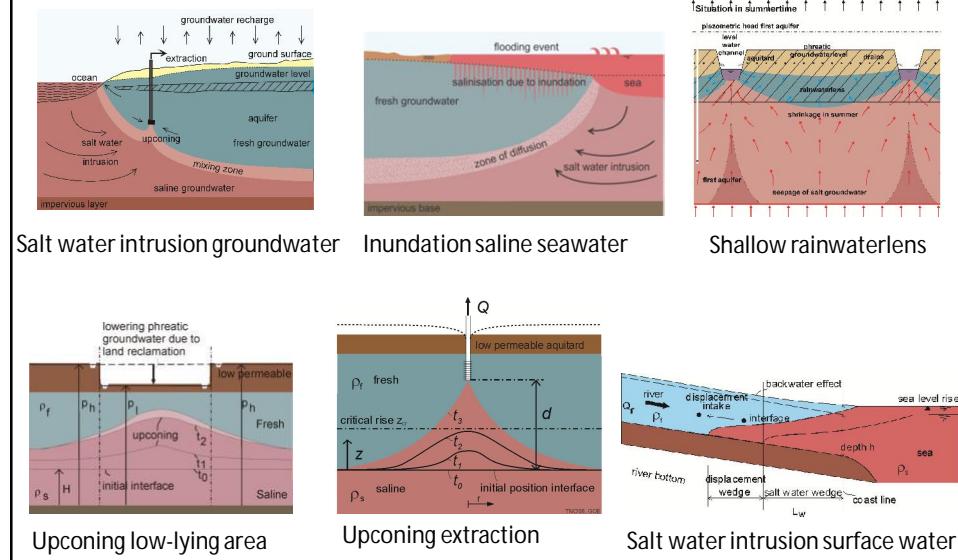
- agriculture/irrigation (salt damage Middle East & Australia)
- upconing under extraction wells throughout the world
- upconing under low-lying areas (e.g. Dutch polders)

## Modes of Salinization due to Sea-Level Rise

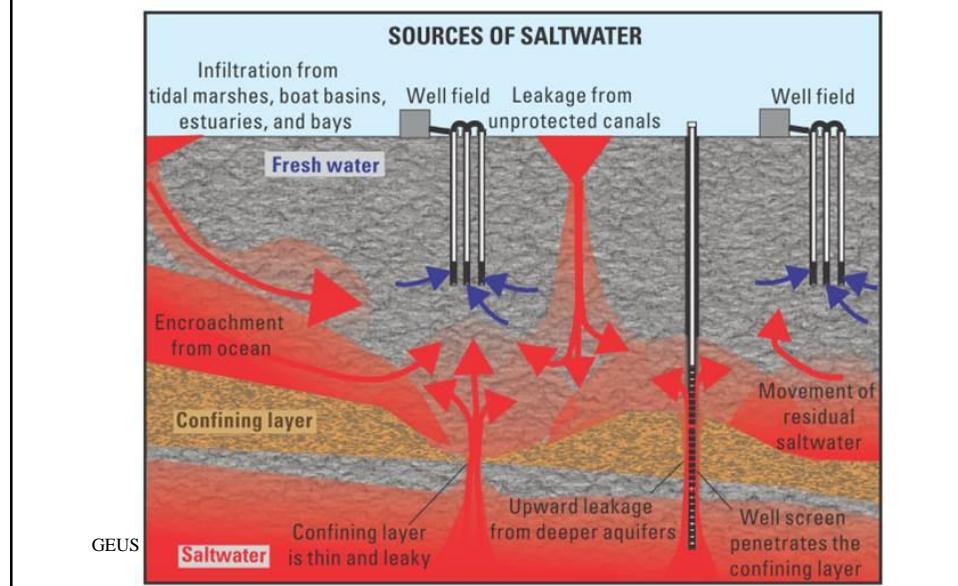


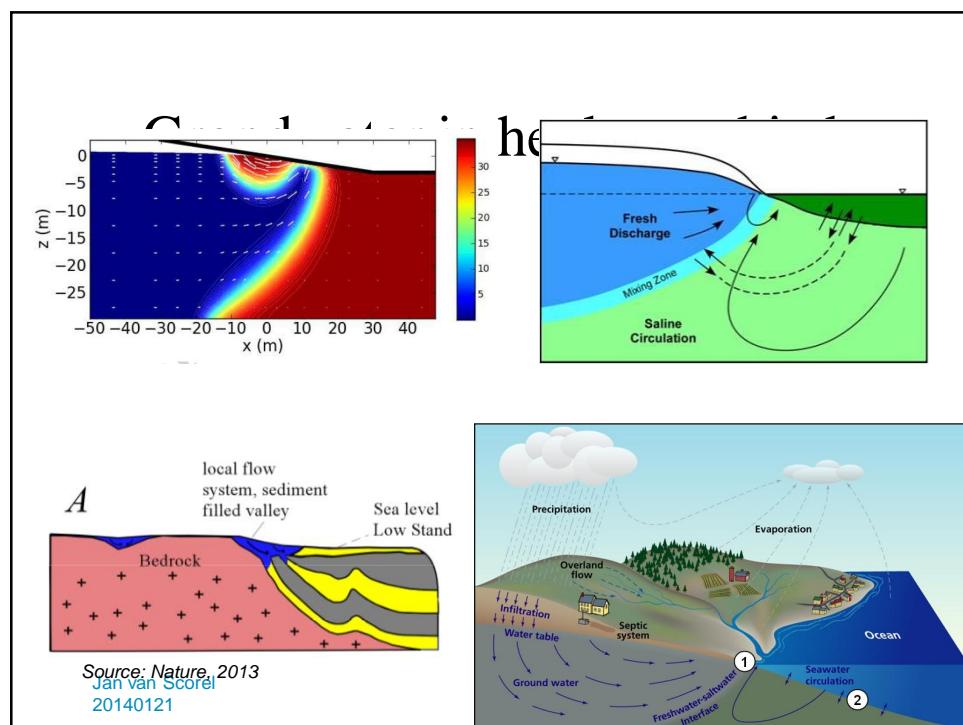
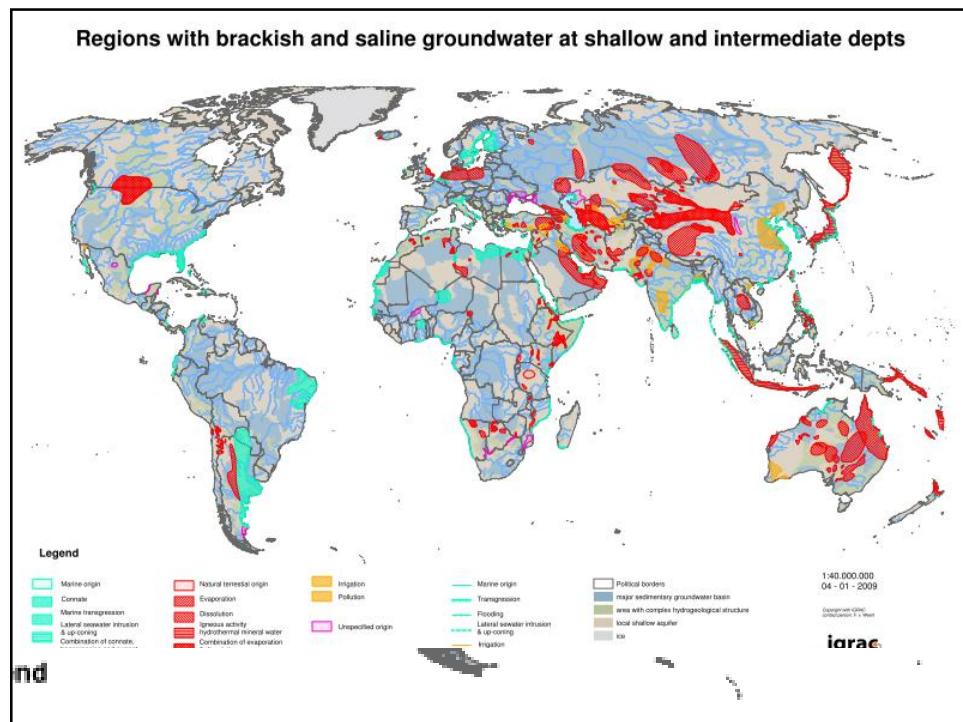


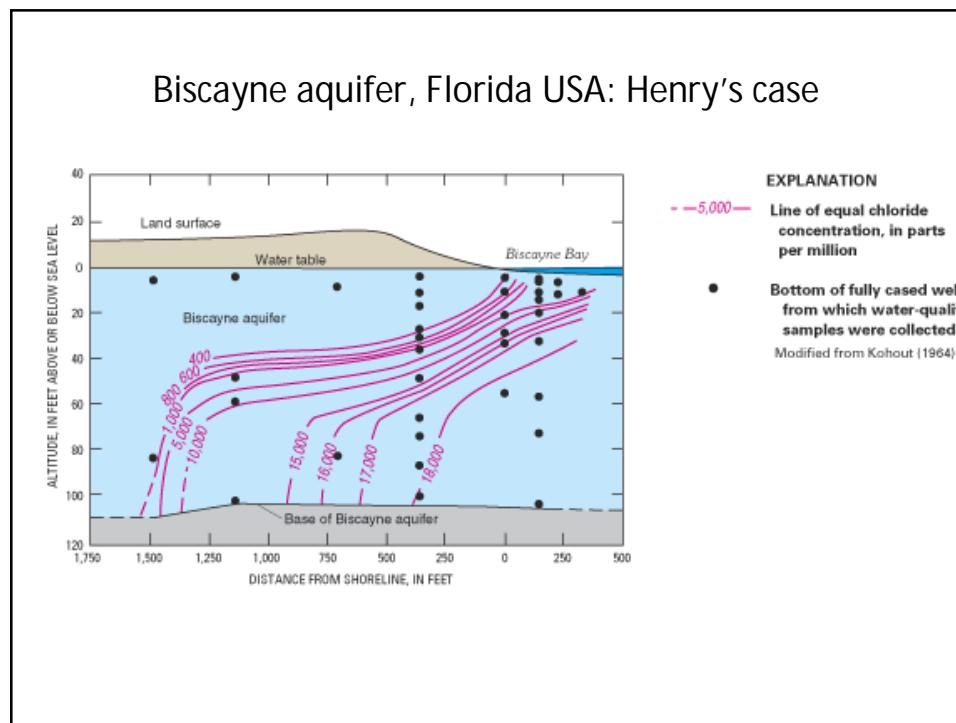
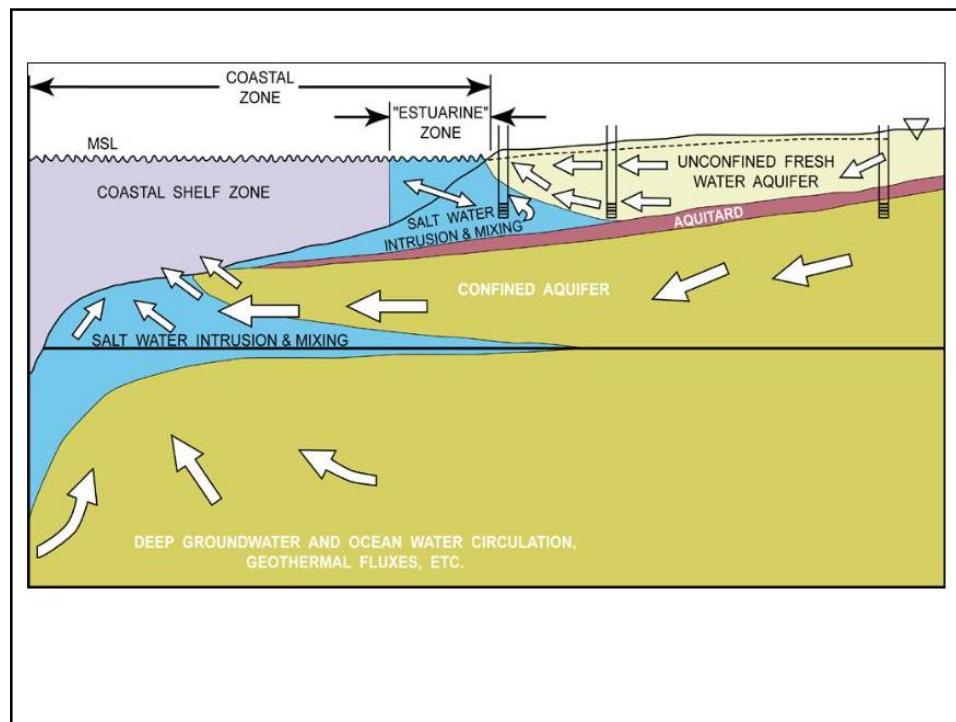
## Salinisation processes at local scale



## Salinization processes in the coastal zone: combination

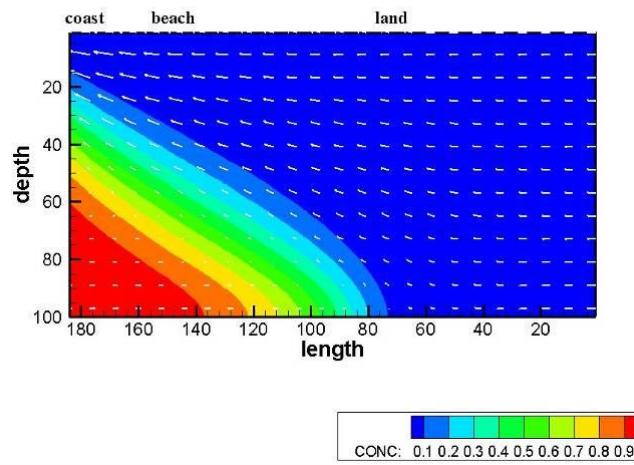






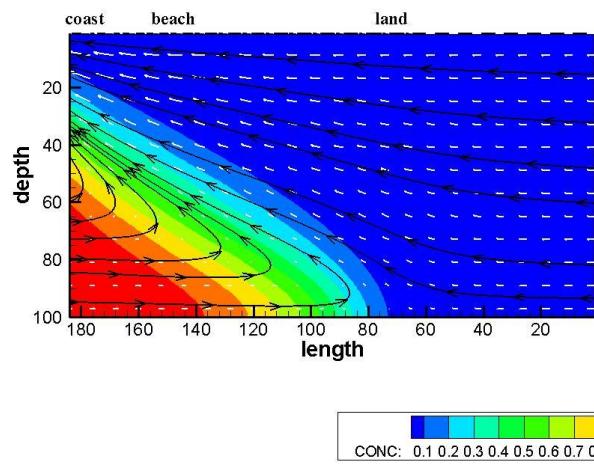
## Definition of salt water intrusion

Numerical model: Henry's case



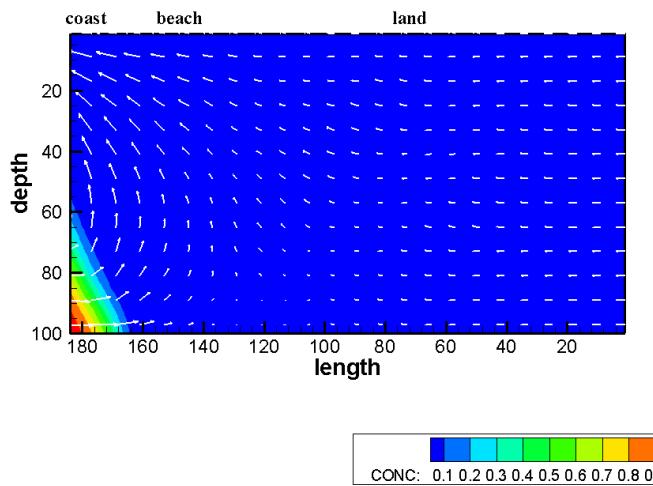
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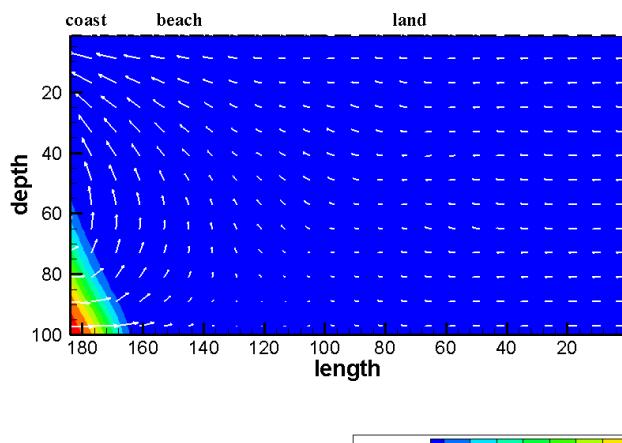
## Sea level rise and salt water intrusion

### Effect sea level rise on groundwater system in coastal zone

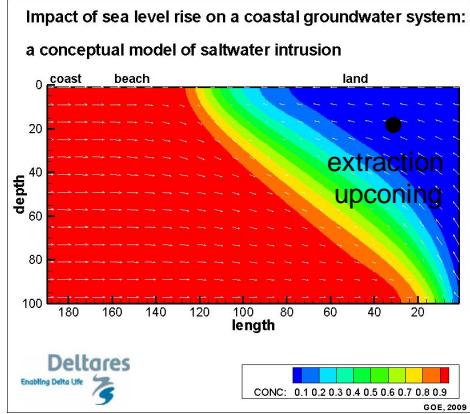
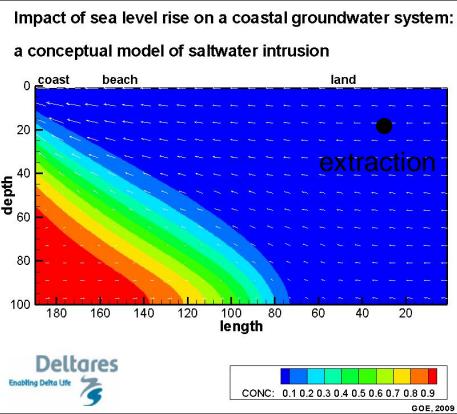


## Sea level rise and salt water intrusion

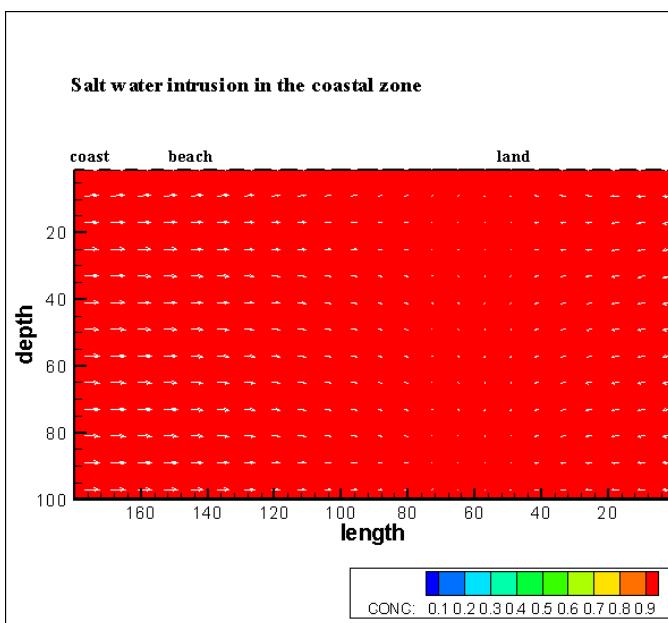
### Effect sea level rise on groundwater system in coastal zone

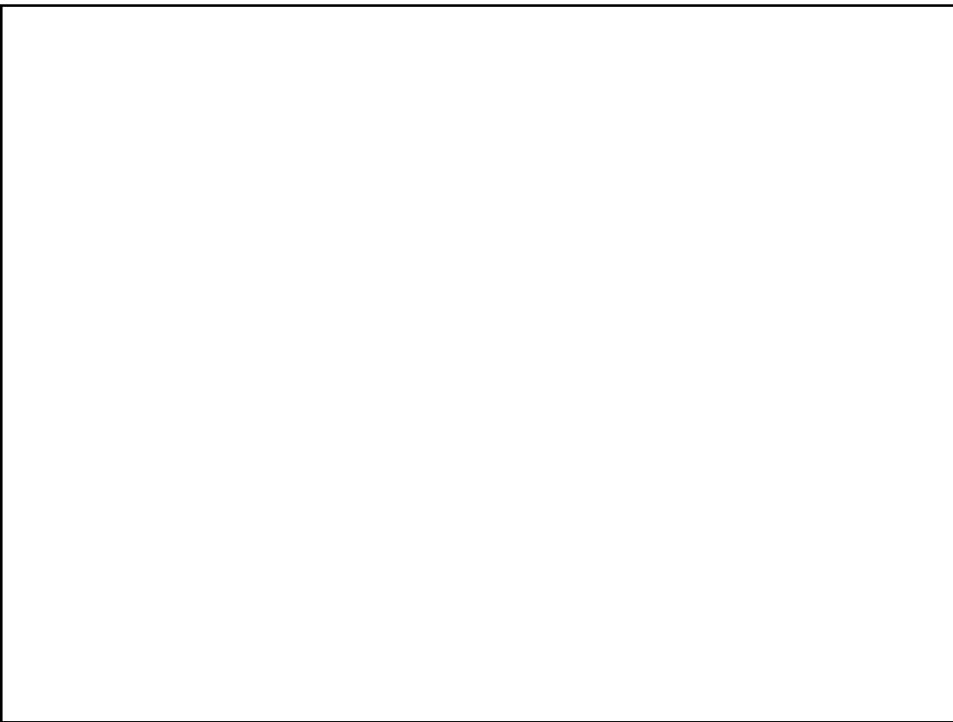


## Sea level rise and salt water intrusion



## Salt water intrusion





Introduction

## Water on Earth

Some serious developments:

*"shortage of drinking water will be one of the biggest problems of the 21<sup>th</sup> century"*

*"in 2025, two third of world population will face shortage of water"*



In 1 liter ocean: about 35 gr salt



In 1 liter ocean: about 35 gr salt



In 1 liter Dead Sea water (Jordan/Israel) : about 280 gr salt



In 1 liter drinking water: about 0.15 gr salt is allowed



Jan van Scorel  
20140121



Grass can grow well in water with a salt content equal to about 6.5 gr salt in 1 liter water



### Fresh-brackish-saline groundwater

Ions	[mg/L]
Negative ions	
$Cl^-$	19000
$SO_4^{2-}$	2700
$HCO_3^-$	140
$Br^-$	65
Total negative ions	21905
Positive ions	
$Na^+$	10600
$Mg^{+2}$	1270
$Ca^{+2}$	400
$K^+$	380
Total positive ions	12650
Total Dissolved Solids (TDS)	34555

## Definition fresh-brackish-saline groundwater

Main type of groundwater	Chloride concentration [mg Cl <sup>-</sup> /L]
oligohaline	0 - 5
oligohaline-fresh	5 - 30
fresh	30 - 150
fresh-brackish	150 - 300
brackish	300 - 1000
brackish-saline	1000 - 10.000
saline	10.000 - 20.000
hyperhaline or brine	≥ 20.000

Type	[mS/cm]	[mg TDS/L]	Drinking- or irrigation water
Non-saline or fresh water	<0.7	<500	Drinking and irrigation water
Slightly saline	0.7 - 2	500-1.500	Irrigation water
Moderately saline	2 - 10	1.500-7.000	Primary drainage water and groundwater
Highly saline	10 - 25	7.000-15.000	Secondary drainage water and groundwater
Very highly saline	25 - 45	15.000-35.000	Seawater is about 35000 TDS mg/L
Brine	>45	>35.000	n.a.

EOS

## Examples of equations of state

Knudsen (1902)

$$\rho_{(S,T)} = 1000 + 0.8054S - 0.0065(T - 4 + 0.2214S)^2$$

T<15 °C, S<20 ppt

Linear (concentration)

$$\rho_{(C)} = \rho_f [1 + \alpha \frac{C_i}{C_s}] \quad \text{where } \alpha = \text{relative density difference}$$

Linear (temperature)

$$\rho_{(T)} = \rho_f [1 - \beta(T - T')]$$

Exponential (temperature, pressure, salt)

$$\rho_{(T,p,\omega)} = \rho_f e^{-\alpha(T-T_0) + \beta(p-p_0) + \gamma\omega}$$

## Equation of state (SEAWAT)

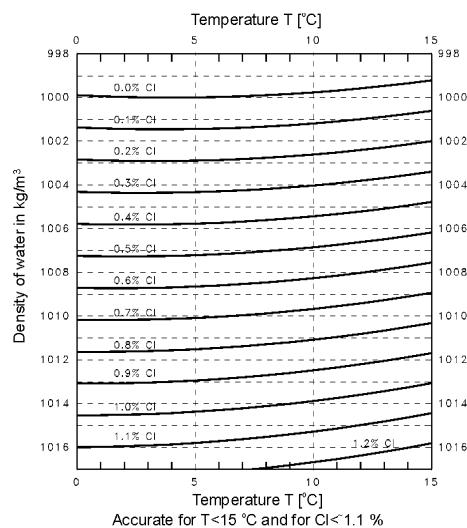
$$\rho_{i,j,k} = \rho_f + \frac{\partial \rho}{\partial C} C_{i,j,k}$$

e.g.:

1. conc=35 TDS g/l: DRHODC=0.7143
2. conc=19000 mg Cl-/l: DRHODC=0.001316  
(as 1025=1000+0.001316\*19000)
3. conc=1: DRHODC=25 (example practicals)

EOS

Density depends on salinity and temperature

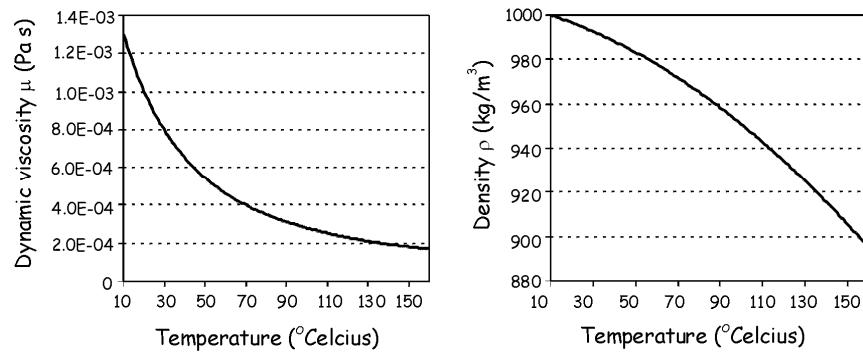


Accurate for  $T < 15$   $^\circ\text{C}$  and for  $\text{Cl} < 1.1$  %

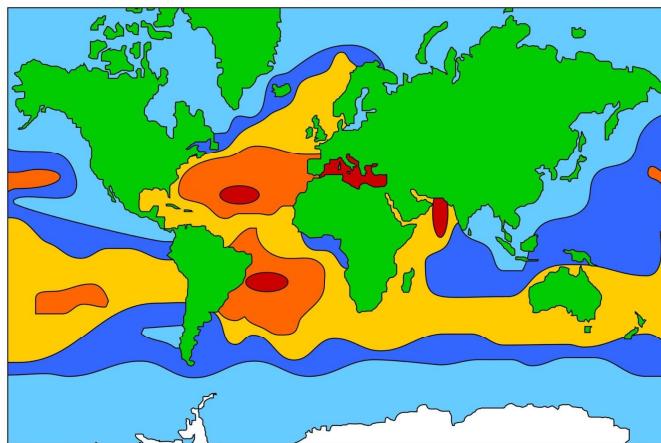
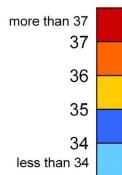
$$\rho_{(S,T)} = 1000 + 0.8054S - 0.0065(T - 4 + 0.2214S)^2 \quad \text{Knudsen (1902)}$$

EOS

## Density and viscosity depend on temperature (10°C-160 °C)

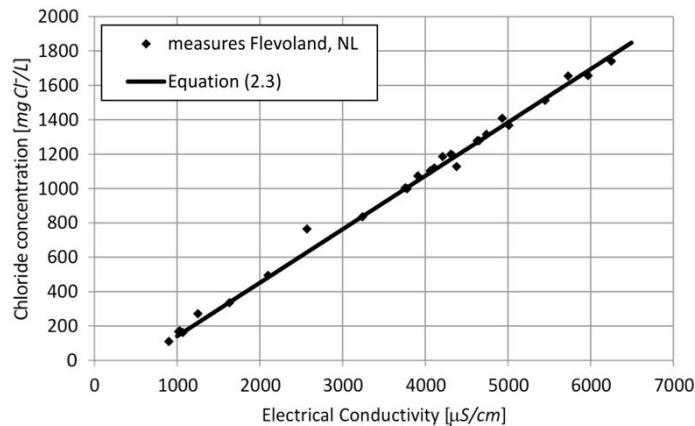


Salinity (ppt)



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### Close relation between chloride concentration and Electrical Conductivity



$$Cl^- (\text{mg / L}) = EC_w (\mu\text{S} / \text{cm}) \cdot 0.305 - 137$$

### Close relation between chloride concentration and Electrical Conductivity

$$10^6 \mu\text{S}/\text{cm} = 10^3 \text{ mS}/\text{cm} = 1 \text{ S}/\text{cm}$$

$$1 \mu\text{S}/\text{cm} = 100 \mu\text{S}/\text{m}$$

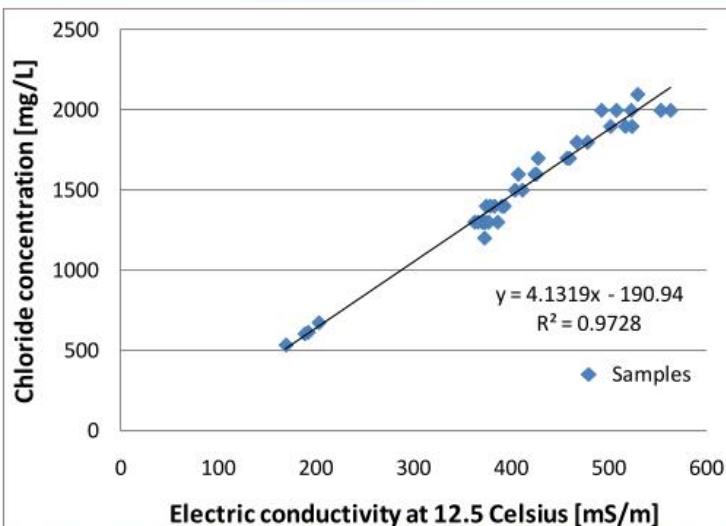
ocean water:

~19000 mg Cl<sup>-</sup>/L or ~34555 mg TDS/L

~5 S/m or ~48 mS/cm

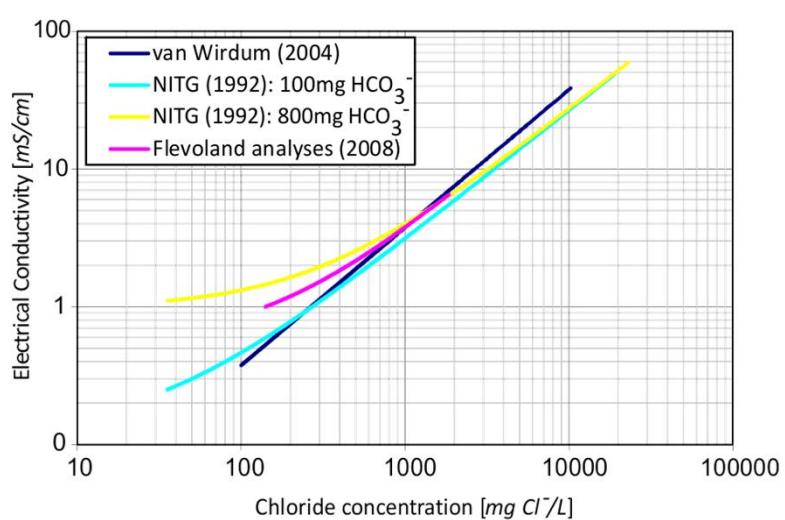
the ratio Cl<sup>-</sup> over TDS equal to ~0.554, under stable normal seawater environments

A fresh-keeper for Noard Burgum  
*The new future for a salinated well field?*

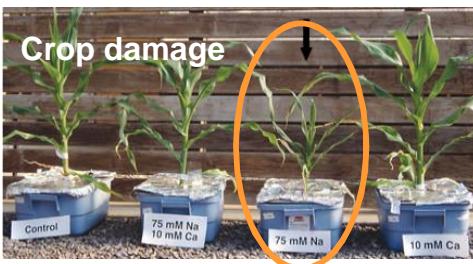
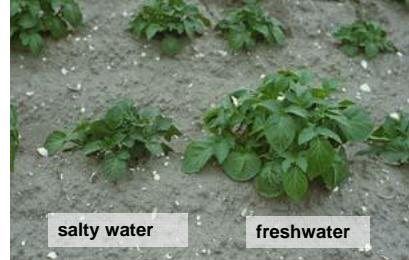


Appendix figure 11: Relation between the electric conductivity and the chloride concentration. For this relation samples from observation well B06D1114 and B06D1087 in between 23-sept-2009 and 9-okt-2010 were plotted.

### EC-Chloride



## Salt in water is a problem



Introduction

Salt in water is a problem for different water management sectors:

-drinking water:

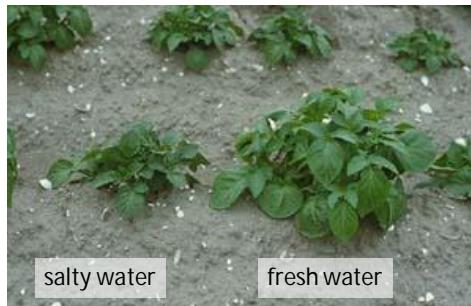
- taste (100-300 mg Cl<sup>-</sup>/l)
- long term health effect
- norm: EC& WHO=150 mg Cl<sup>-</sup>/l (live stock=1500 mg Cl<sup>-</sup>/l)

-industry:

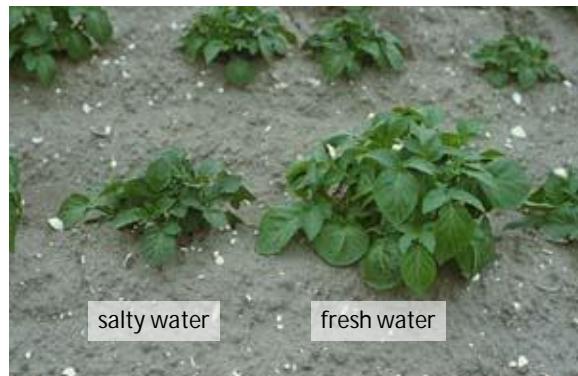
- corrosion pipes
- preparation food

-irrigation/agriculture:

- production crops
- salt damage

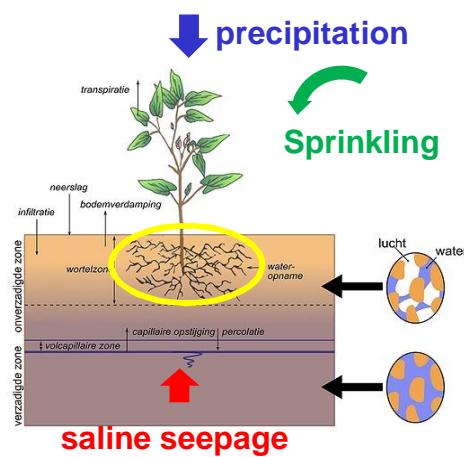


## Effects salinisation: salt damage

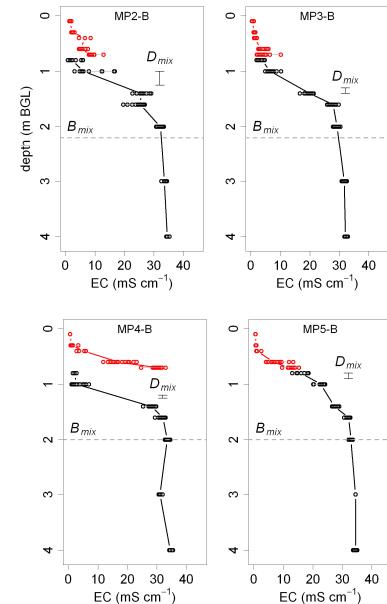


Source: Proefstation voor de Akkerbouw en Groenteteelt, Lelystad

## Salt-resistant crops



**Important parameter:**  
Chloride concentration root zone  
Land use  
Sensitivity crops



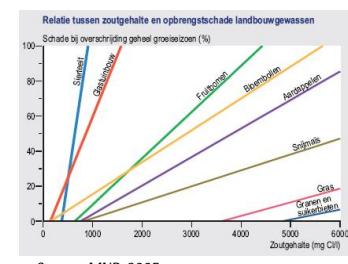
## Salt damage to crops

Important parameters:

- Chloride concentration in the root zone
- Land use
- Sensitivity crops

Land use	Threshold value root zone (mg Cl-/l)	Gradient root zone (-)
Grass	3606	0.0078
Potatoes	756	0.0163
Beet	4831	0.0057
Grains	4831	0.0058
Horticulture	1337	0.0141
Orchard (trees)	642	0.0264
Bulb	153	0.0182

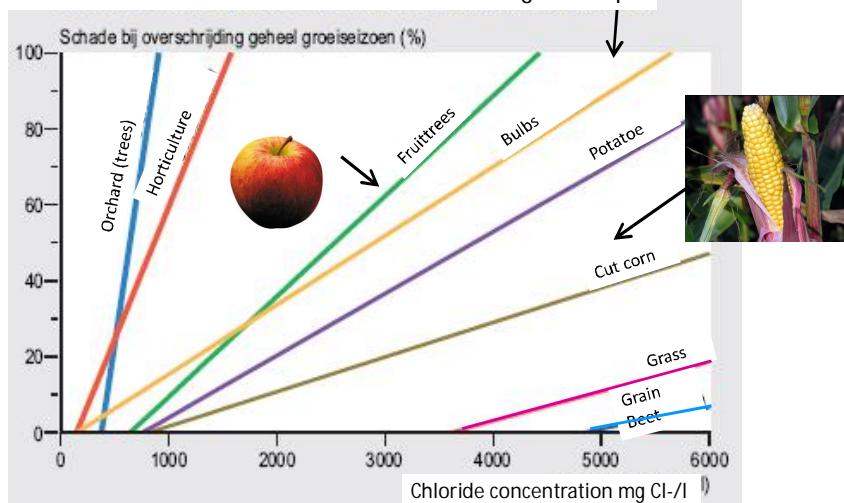
Source: Roest et al., 2003 en Haskoning



## Salt damage to crops



Relation between salt concentration and damage to crops

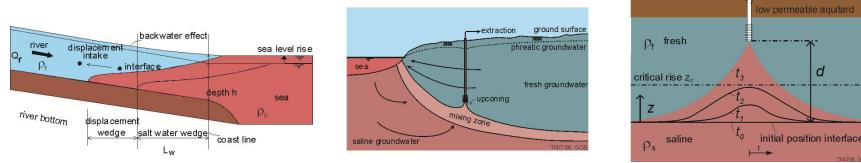


	Soil moisture		Irrigation water	
	Limi	Gradient	Limit	Gradient
Crop	mg/l Cl	%/mg/l Cl	mg/l Cl	%/mg/l Cl
Potatoe	756	0.0163	202	0.0610
Grass	3606	0.0078	962	0.0294
Sugar beat	4831	0.0057	1288	0.0212
Cut Corn	815	0.0091	217	0.0343
Grains	4831	0.0058	1288	0.0218
Fruit trees	642	0.0264	171	0.0991
Orchard (trees)	378	0.1890	101	0.7086
Vegetables	917	0.0158	245	0.0591
Horticulture	1337	0.0141	356	0.0527
Bulbs	153	0.0182	41	0.0683

## Introduction

### Why is salinisation a pressing problem?

- 30% of world population lives <100 km from coastline
- economic and tourist activities increase
- enormous increase in extraction
- irreversible process
- increase saltwater intrusion problem world-wide:
  - upconing
  - salt water wedge
  - decrease outflow  $q_0$
- climate change:
  - sea level rise
  - natural groundwater recharge



Processes that accelerate salt water intrusion:

- Sea level rise
- Land subsidence
- Human activities

Threats for:

- drinking water supply in dunes:  
upconing of saline groundwater  
decrease of fresh groundwater resources  
recharge areas reduction
- agriculture:  
salt damage to crops: salt load and seepage
- water management low-lying areas:  
flushing water channels
- ecology



## The water footprint of products

global averages

**1 kg wheat      1 m<sup>3</sup> water**



**1 kg rice      3 m<sup>3</sup> water**

**1 kg milk      1 m<sup>3</sup> water**

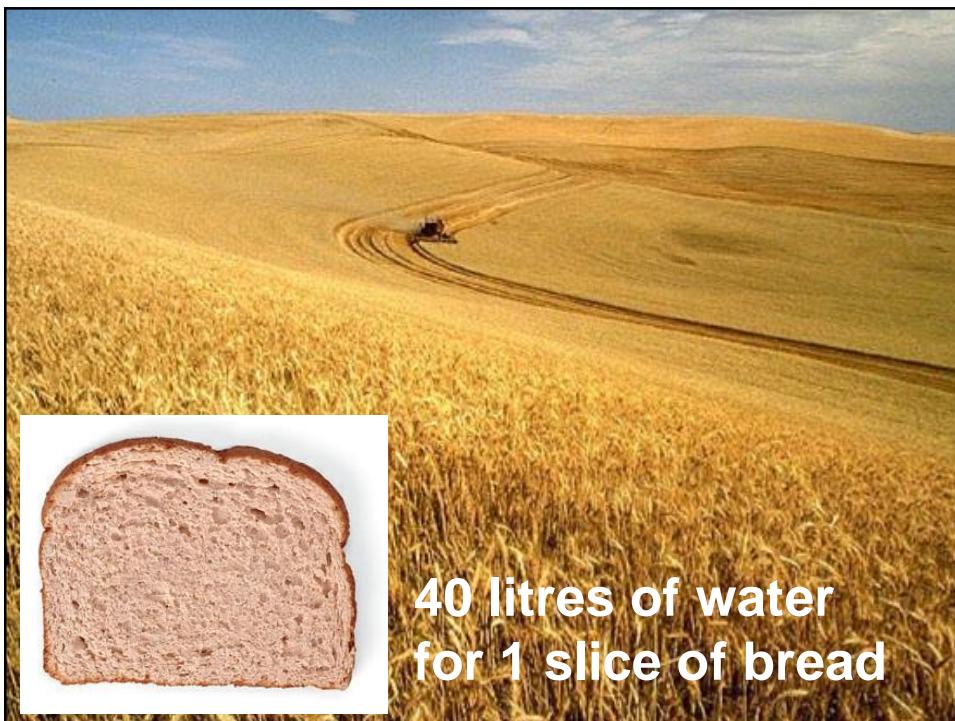


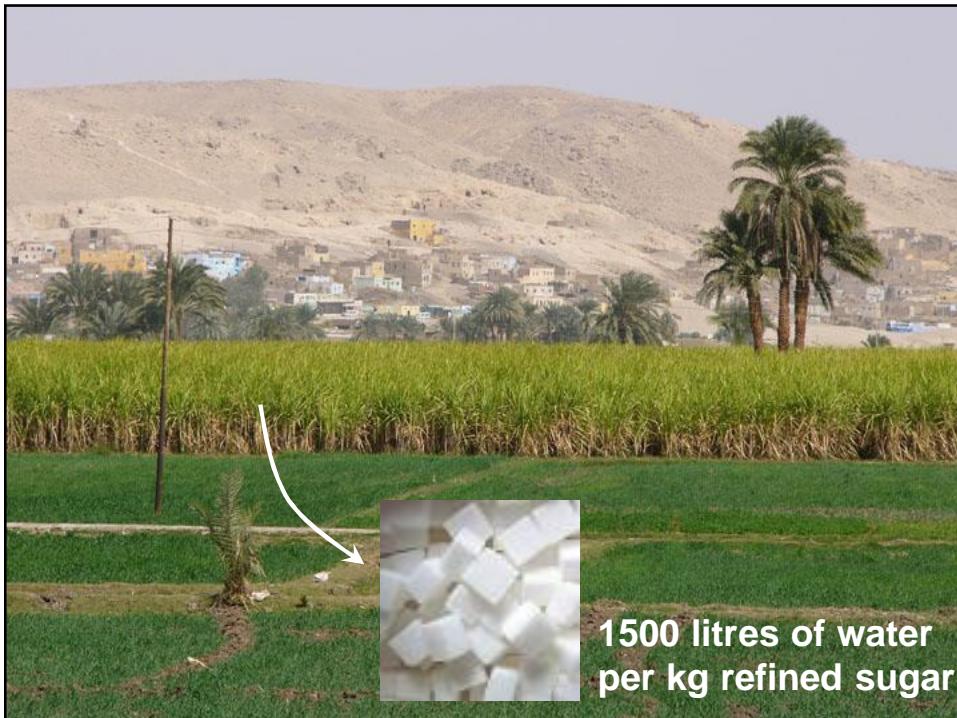
**1 kg cheese      5 m<sup>3</sup> water**

**1 kg pork      5 m<sup>3</sup> water**

**1 kg beef      15 m<sup>3</sup> water**

[Hoekstra & Chapagain, 2008]





**1500 litres of water  
per kg refined sugar**



**2400 litres of water  
for 1 hamburger**



**= 140 litres of water**



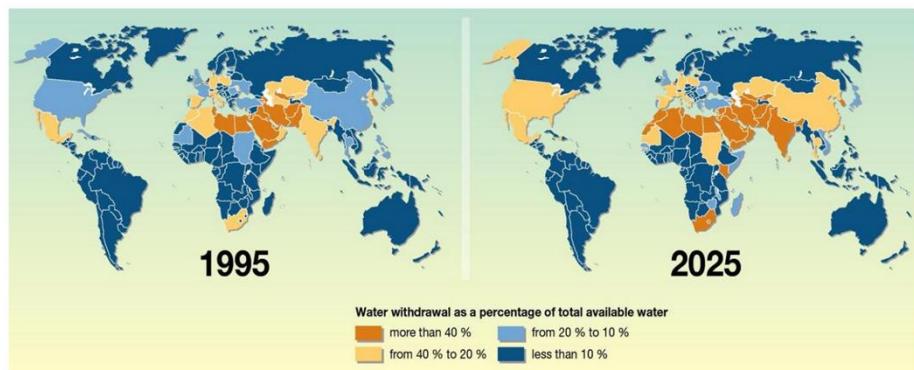
**10 litres of water  
for 1 sheet of A4-paper**

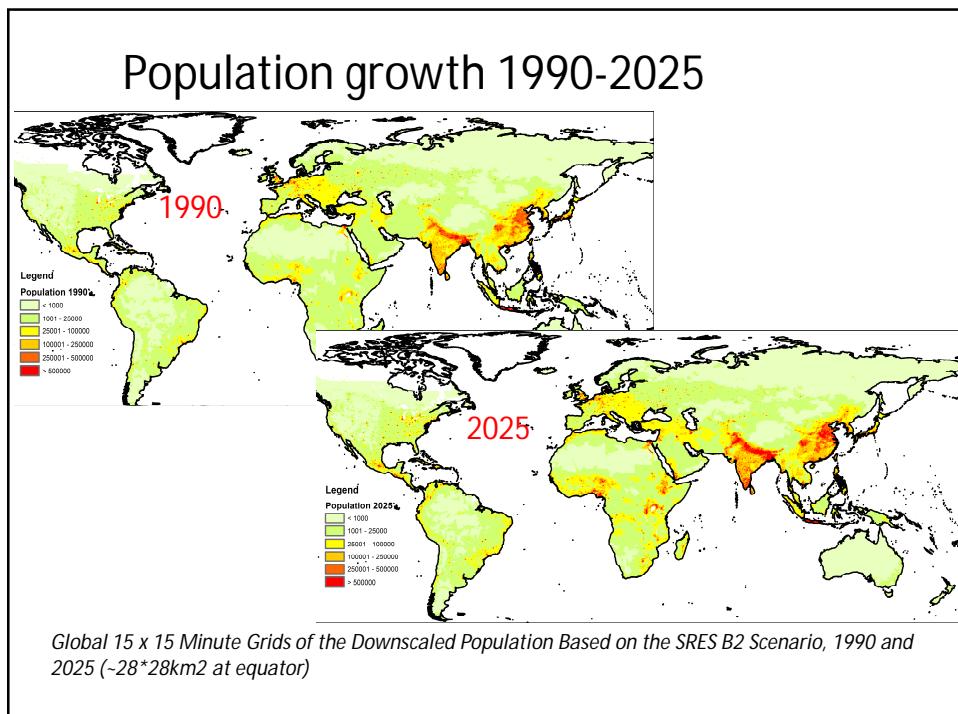
Question:

*Demand fresh water per capita per day?:*

- a. 10 litre/day
- b. 25 litre/day
- c. 100 litre/day
- d. 200 litre/day

Water withdrawal as % of total available water





## Introduction

### Reasons and drawbacks of using groundwater

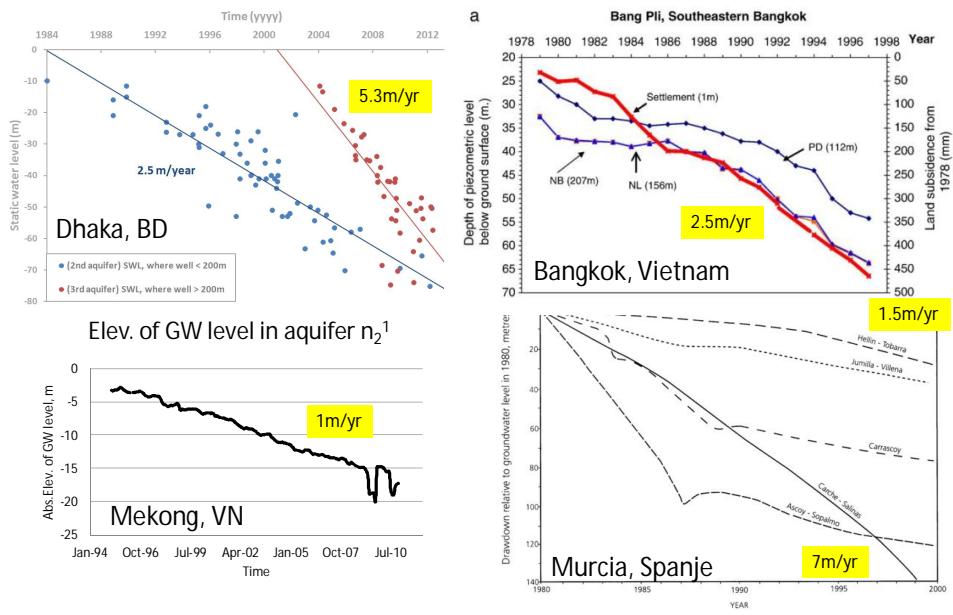
#### Advantage:

- no seasonal effects
- high quality
- low storage costs
- large quantities
- no spatial limitations

#### Disadvantage:

- high extraction costs
- local droughts
- high mineral content
- land subsidence....
- salt water intrusion !

## Serious overexploitation coastal aquifers worldwide



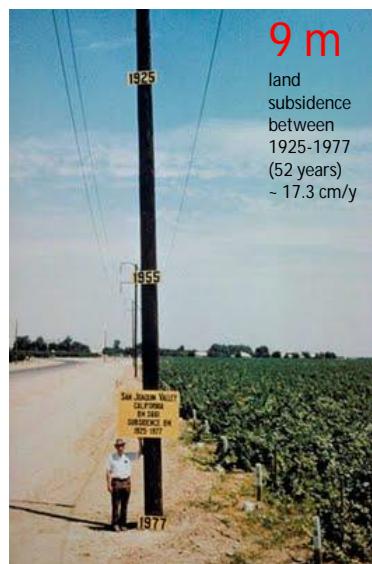
## Groundwater overexploitation in Mekong Delta



## Land subsidence

Megacity	Maximum subsidence [m]	Date commenced
Shanghai	2.80	1921
Tokyo	5.00	1930's
Osaka	2.80	1935
Bangkok	1.60	1950's
Tianjin	2.60	1959
Jakarta	0.90	1978
Manila	0.40	1960
Los Angeles	9.00	1930's

## Land subsidence San Joachim Valley, CA, USA



9 m since 1930s



# What causes the land to subside?

Natural causes (geological processes):

- *Loading* of the earth's crust by ice sheets, sediment (delta's), the ocean/sea
- *Compaction* of older sediments after sedimentation

Anthropogenic causes (human-induced processes):

- Oil/gas *extraction* (usually relatively deep)
- Groundwater *extraction* (usually moderately deep)
- *Drainage* of soils ⇒ oxidation of peat, soil compaction

Why discriminating between human-induced and natural processes?

- Magnitude
- Cooping strategy (mitigation versus adaptation)



## Impacts



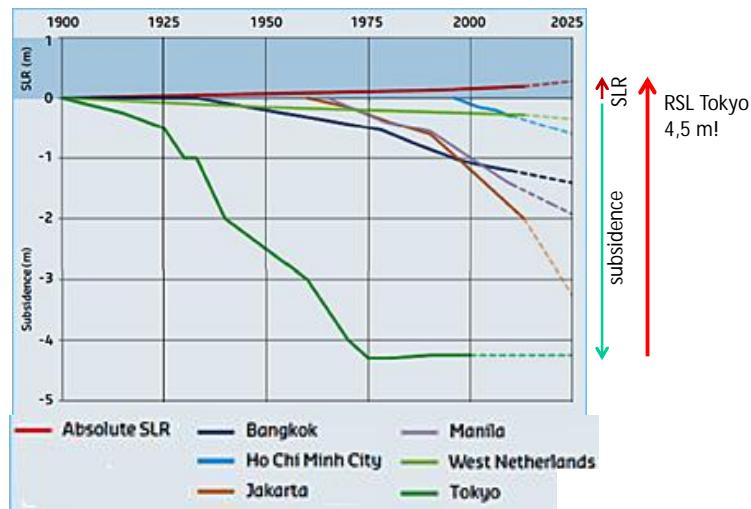
## Sinking delta cities

**Relative sea level rise = Absolute sea level rise + Subsidence**

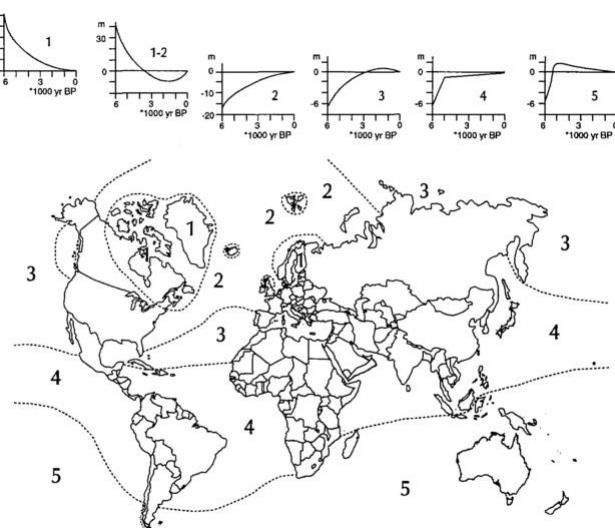


## Examples of some major coastal cities

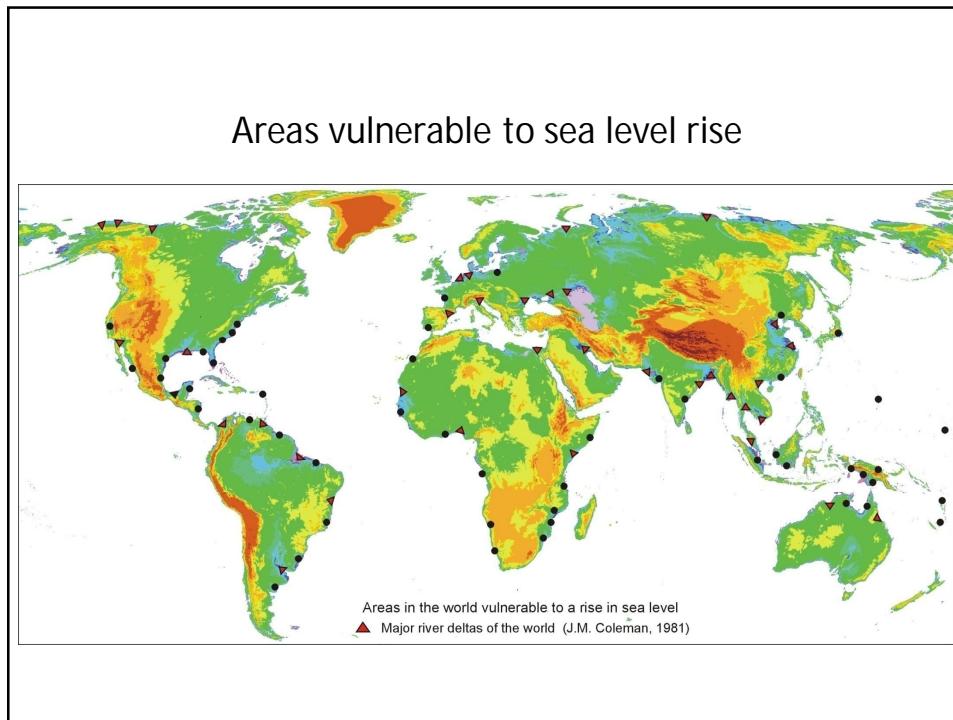
The subsidence issue is underestimated



## Regional distribution of Holocene Sea-level Changes

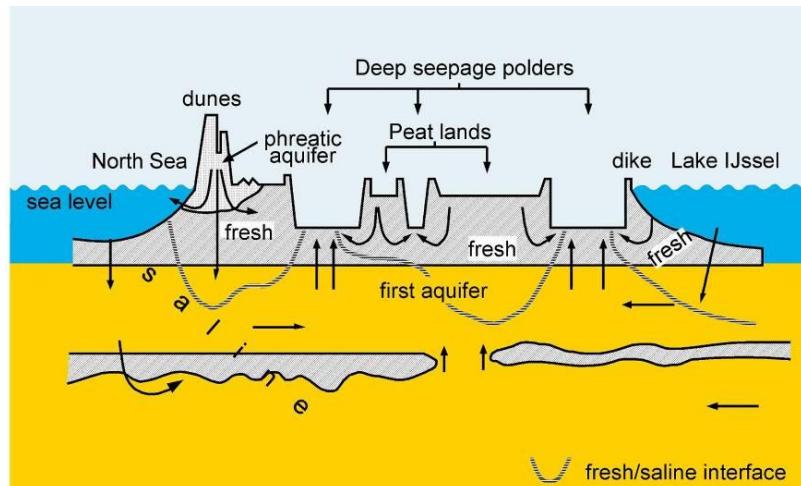


Source: Pirazzoli, P.A. & Pluet, J., 1991. *World Atlas of Holocene Sea-level Changes*. Elsevier Oceanography Series, Vol. 58

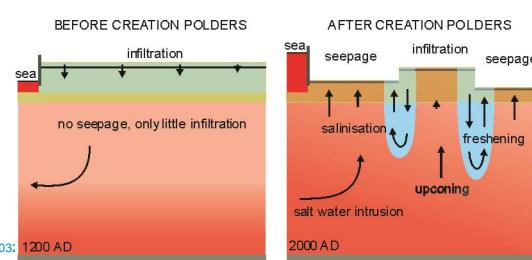
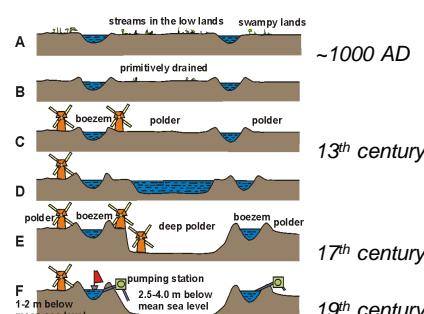
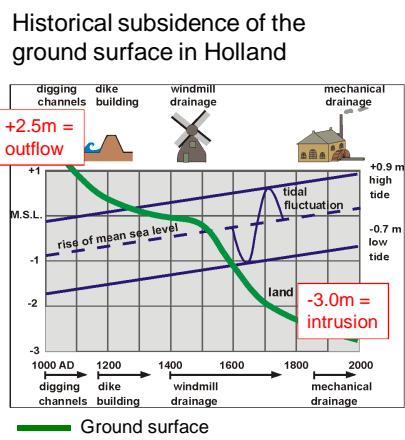


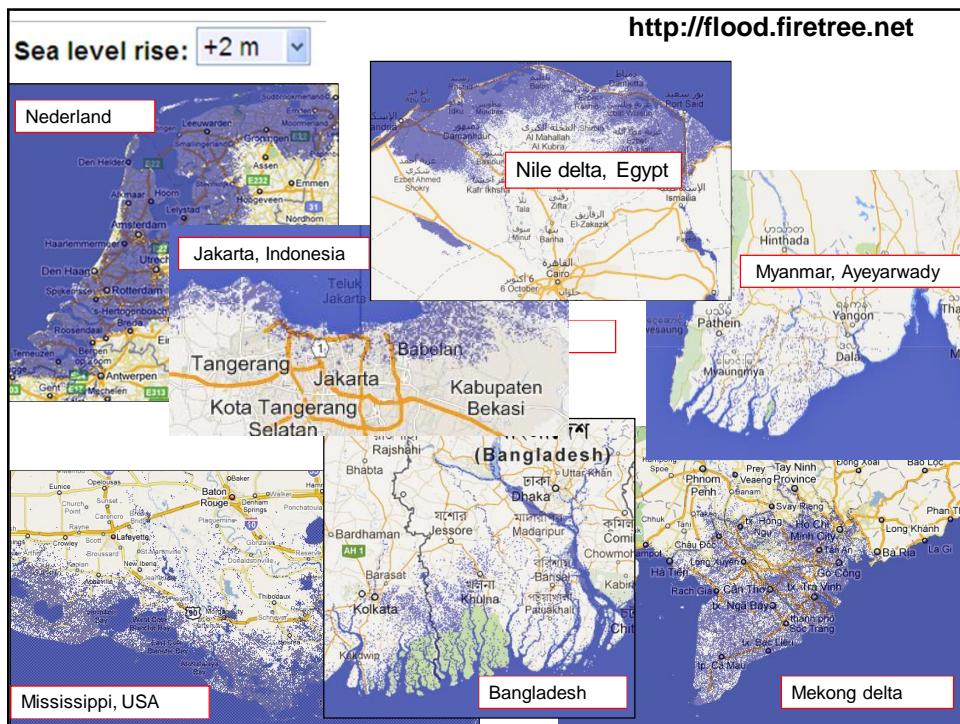
## Saline seepage leads to:

- Salinization and eutrophication of surface waters
- Salinization of shallow groundwater
- Salinization of root zone (crop damage)

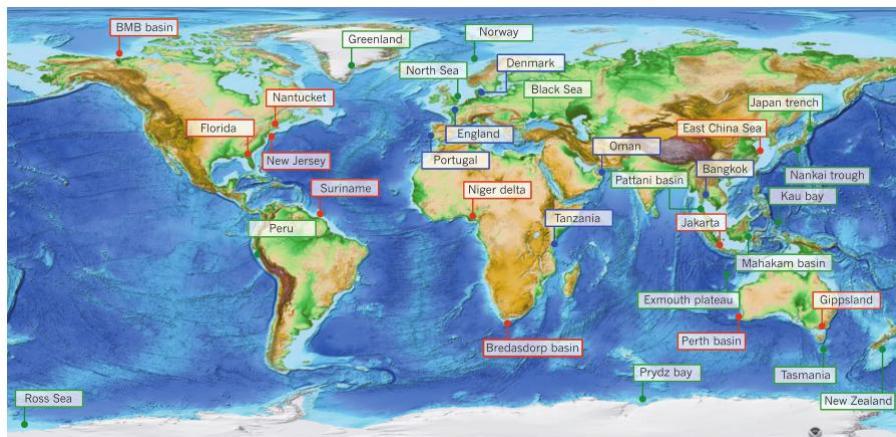


## From fresh water outflow to salt water inflow

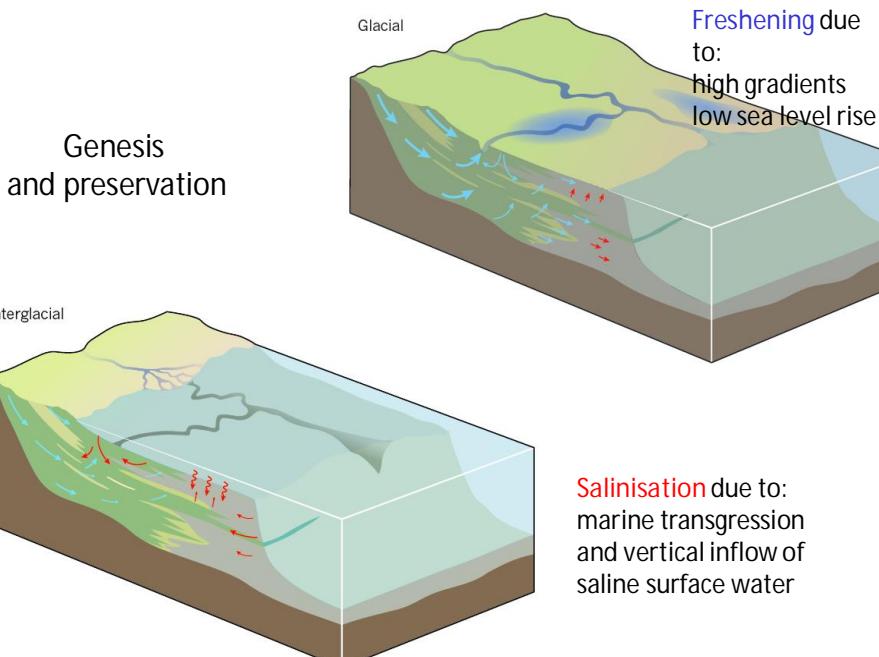




World map of topography and bathymetry showing known occurrences of fresh and brackish offshore groundwater

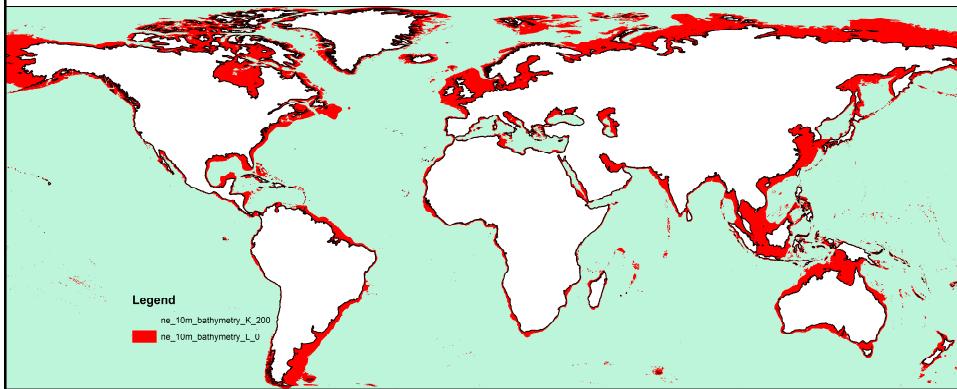


Post et al., Nature, 2013



Source: Nature, 2013

## Possible locations of offshore (submarine) groundwater

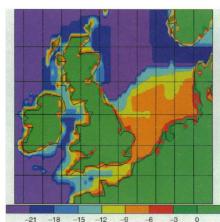


## Coastal zone cases around the world Occurrence related to dynamic sea-levels and coastlines

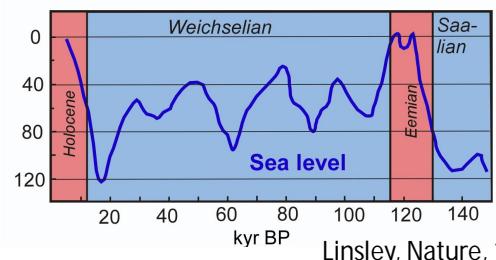


Exposed continental shelves

Peltier, *Science*, 1994

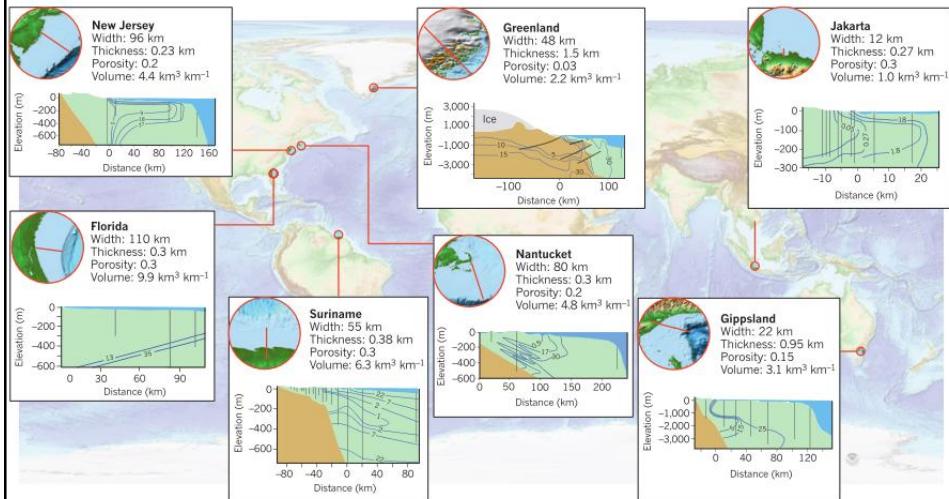


Inundated (kyr BP)



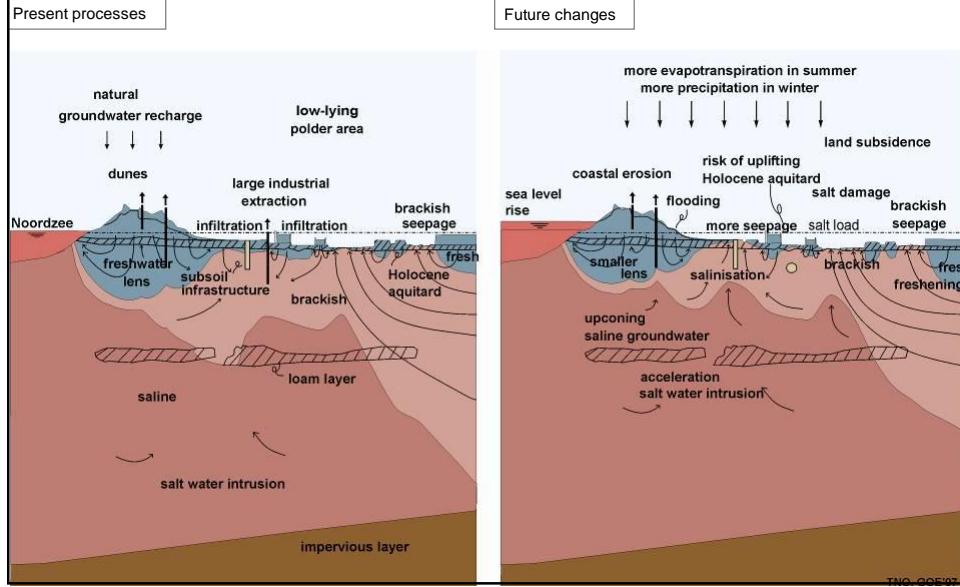
Linsley, *Nature*, 1996

## Global overview of inferred key metrics and cross sections of well-characterised vast meteoric groundwater reserves

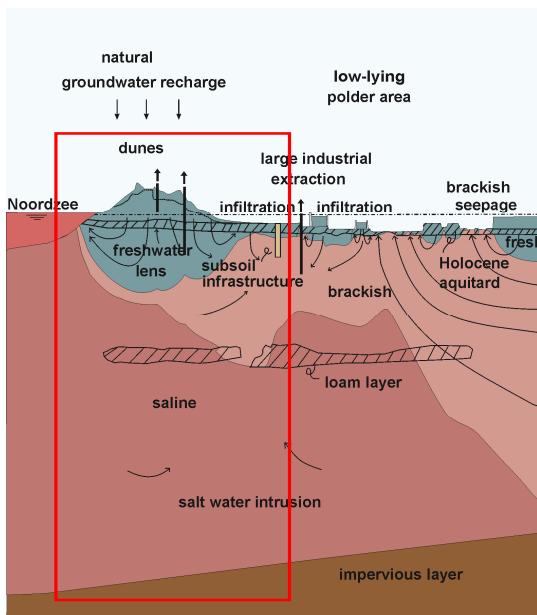


My first density dependent groundwater flow and solute transport model in 1990!

## The Dutch groundwater system under stress

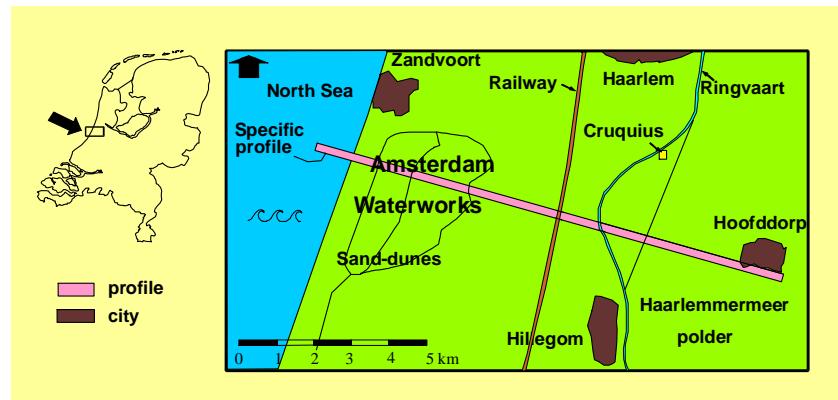


## Saltwater intrusion in the Netherlands



## Saltwater intrusion in the Dutch coastal zone

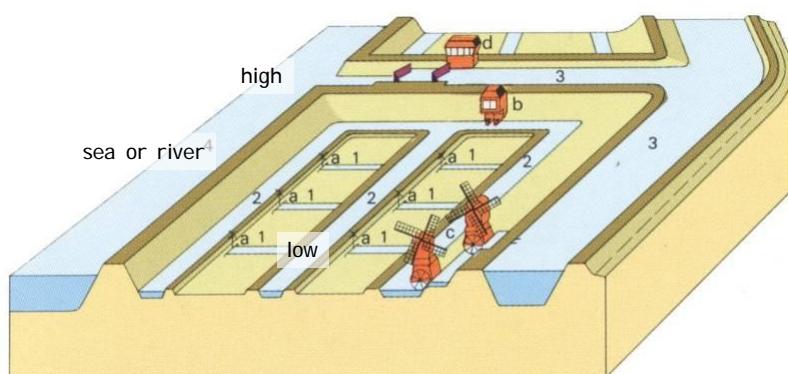
Position profile through Amsterdam Waterworks, Rijnland polders and Haarlemmermeer polder



## The polder system

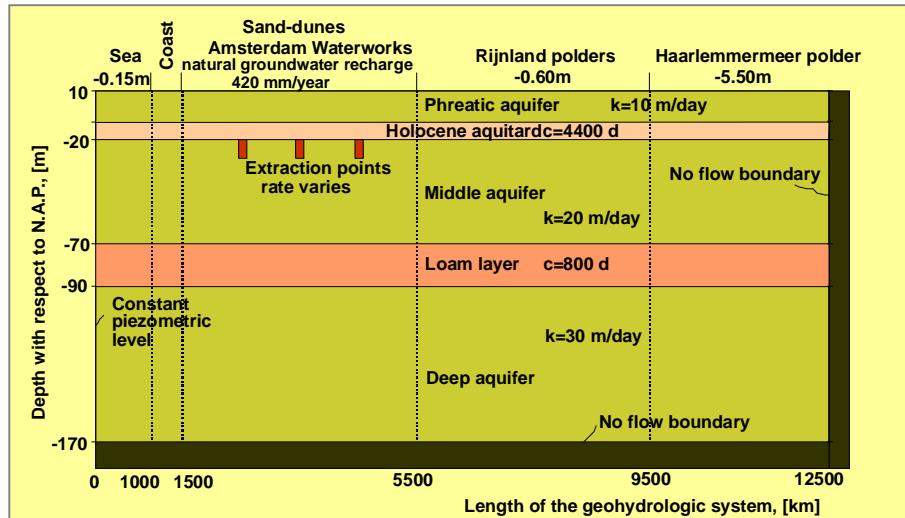
A polder is:

*a sophisticated system to drain the excess of water  
in a low-lying area*



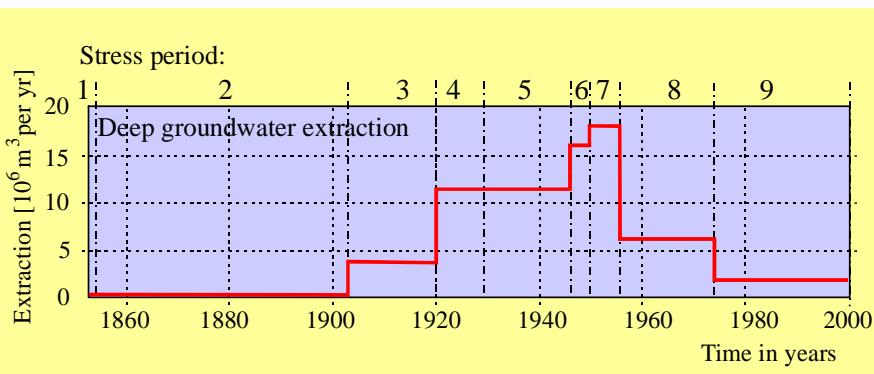
Upcoming example

## Geometry, subsoil parameters, boundary conditions

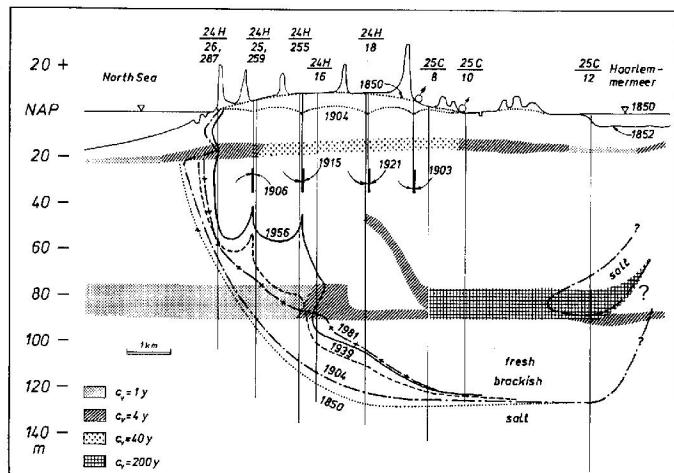
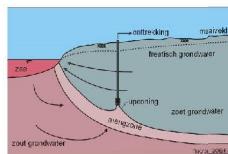


## Saltwater intrusion in the Dutch coastal zone

Groundwater extractions out of the middle aquifer in the sand-dune area of Amsterdam Waterworks

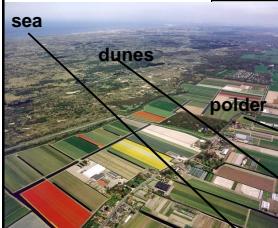


## Upconing of brackish-saline groundwater



Stuyfzand, 1993

## Saltwater intrusion in the Dutch coastal zone

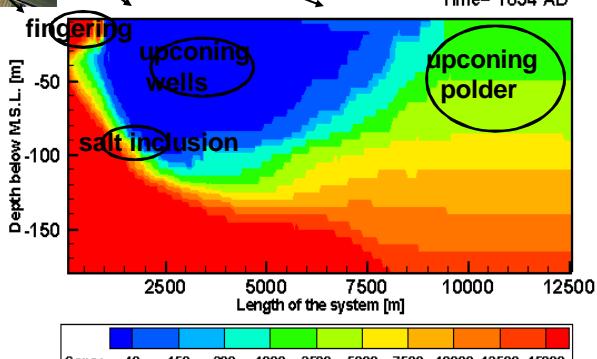


### Salinisation of the groundwater flow system

caused due to groundwater extractions and lowering of the ground surface of the Haarlemmermeer polder

Profile Amsterdam Waterworks-Haarlemmermeerpolder

Time= 1854 AD



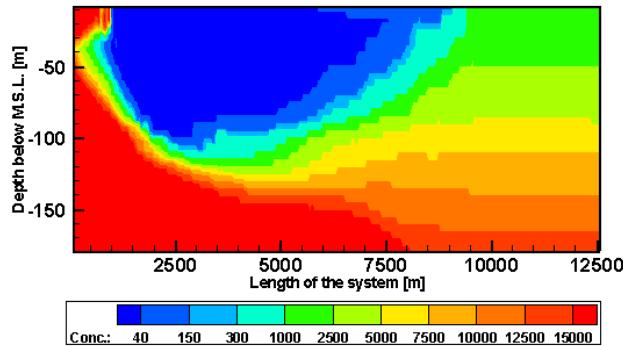
## Saltwater intrusion in the Dutch coastal zone

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Profile Amsterdam Waterworks-Haarlemmermeerpolder

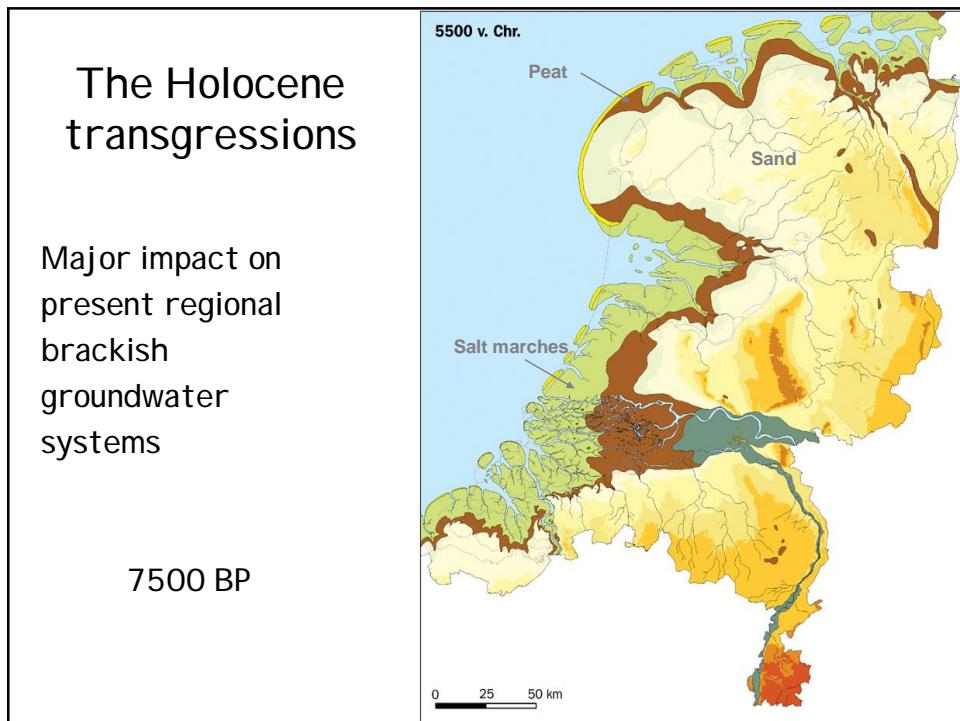
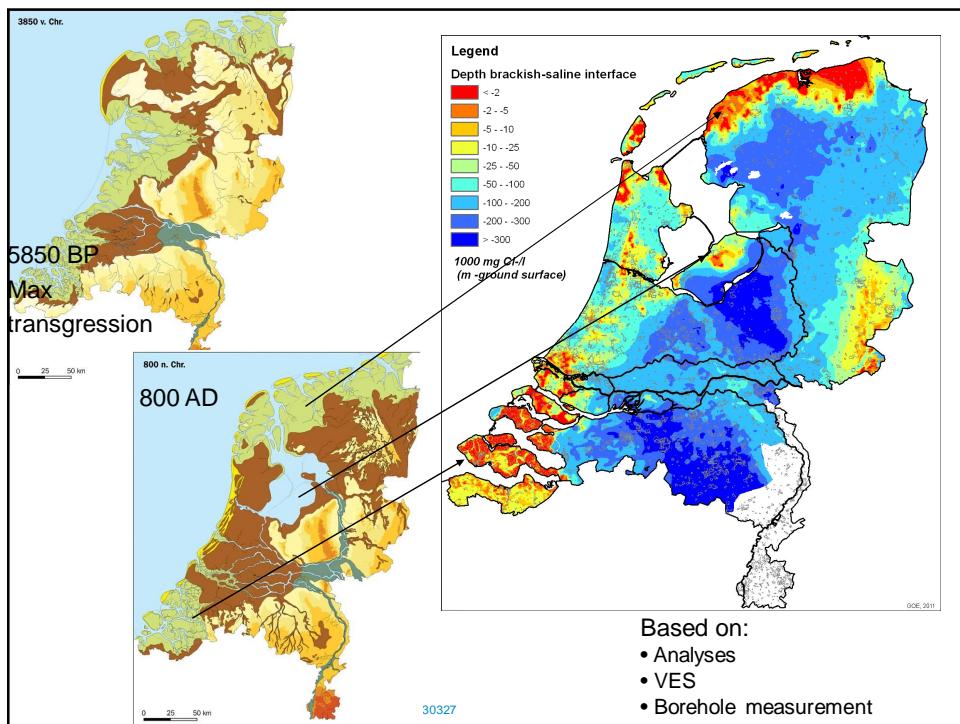
Time= 1854 AD

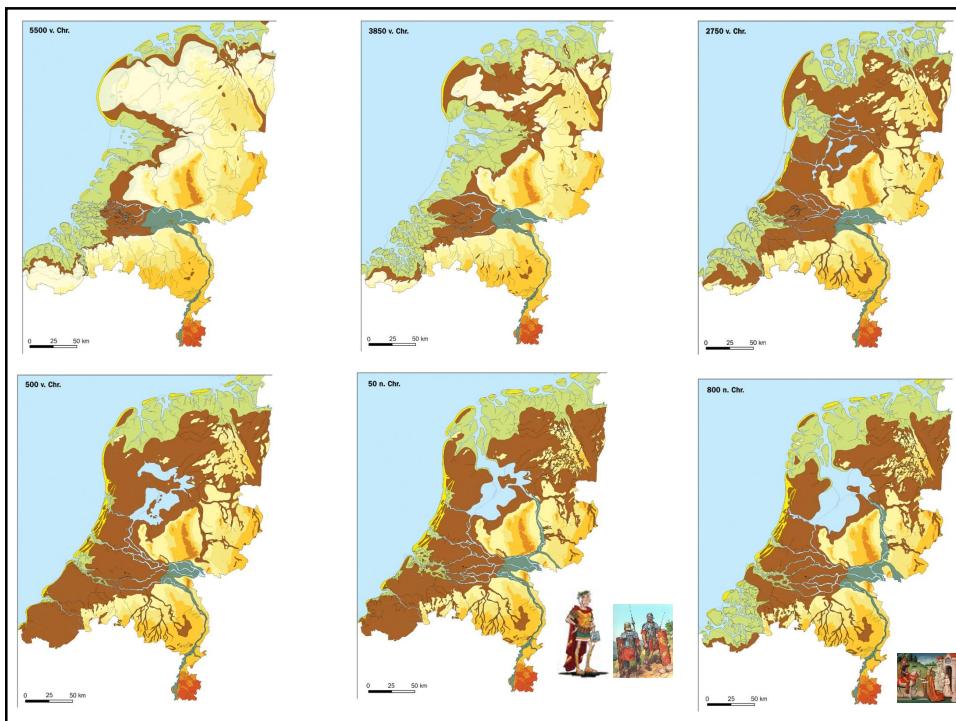
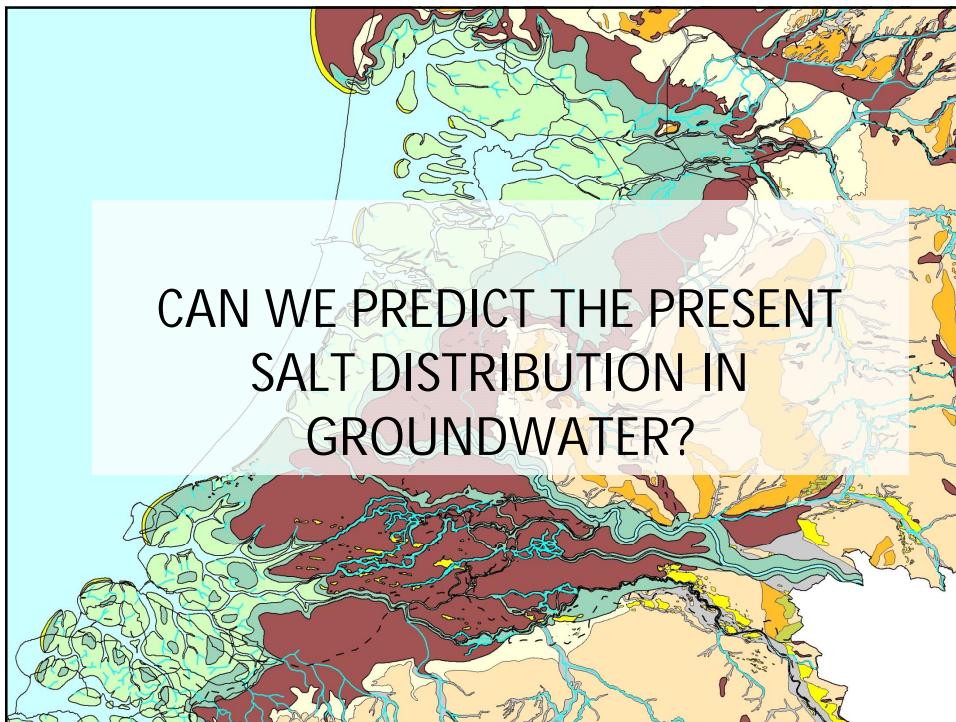


## Palaeo hydrogeological modelling

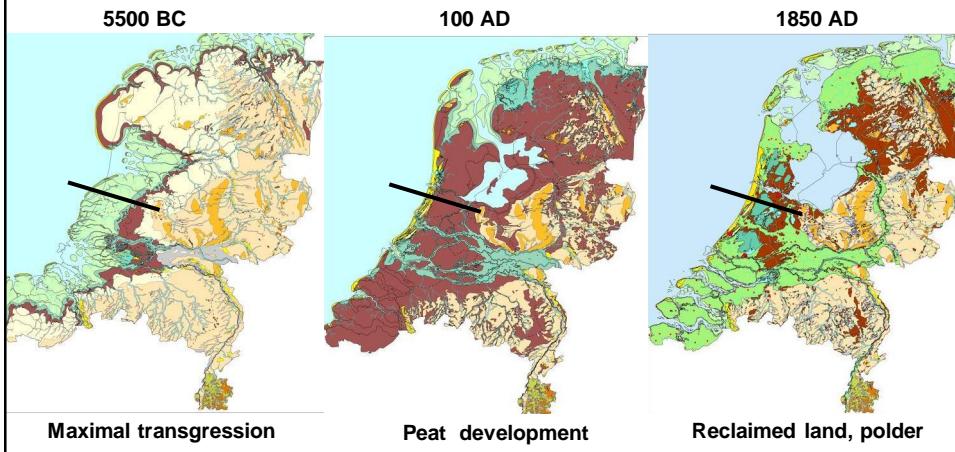
### Palaeo-modeling salt water intrusion during the Holocene: an application to the Netherlands

*J.R. Delsman, K. Hu-a-ng, P.C. Vos, P.G.B. de Louw, G.H.P. Oude Essink and M.F.P. Bierkens*





## Palaeogeographical development

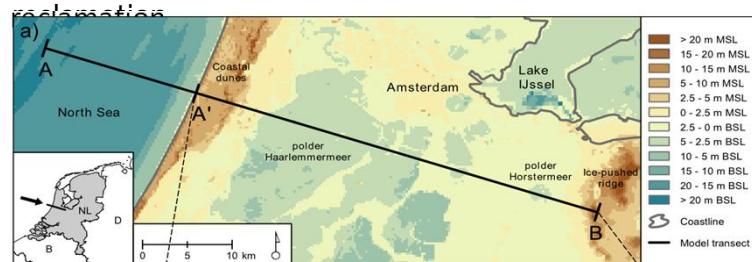


Delsman, J.R., Hu-a-ng, K.R.M., Vos, P.C., De Louw, P.G.B., Oude Essink, G.H.P., Stuyfzand, P.J. and Bierkens, M.F.P. 2013, Palaeo-modelling of coastal salt water intrusion during the Holocene: an application to the Netherlands, *Hydrol. Earth Syst. Sci. Discuss.*, 10, 13707–13742

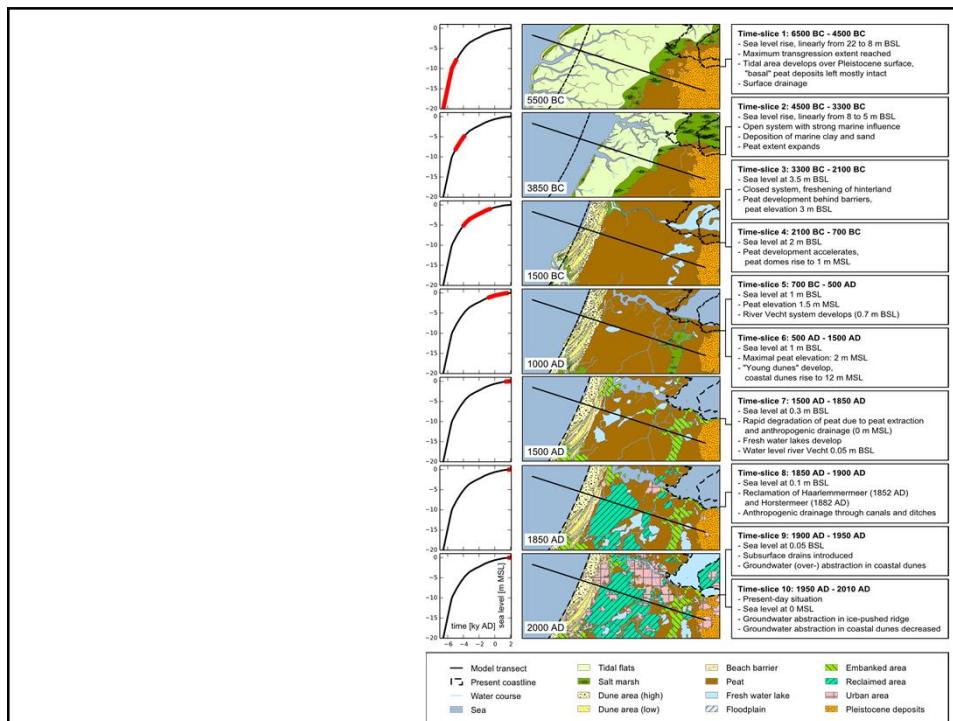
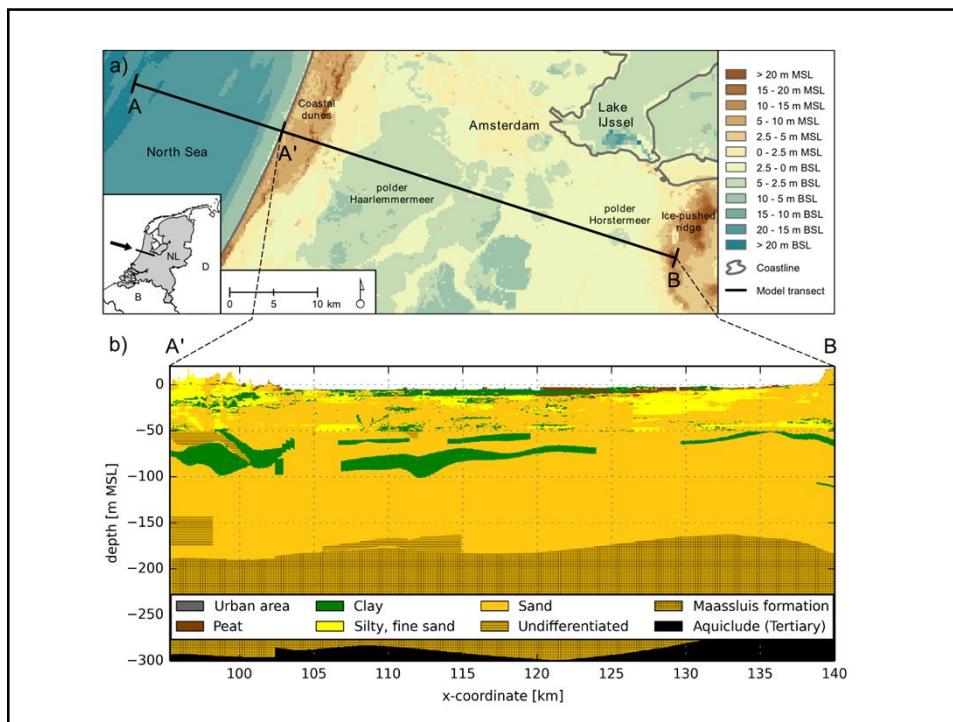
Atlas NL in het Holoceen (Vos et al, 2011)

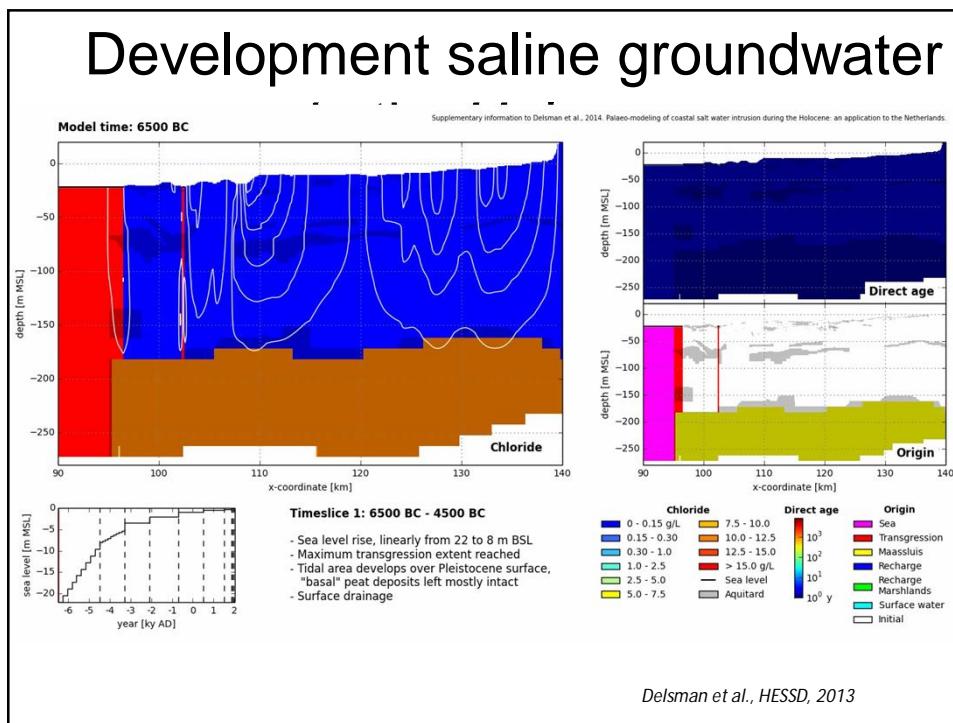
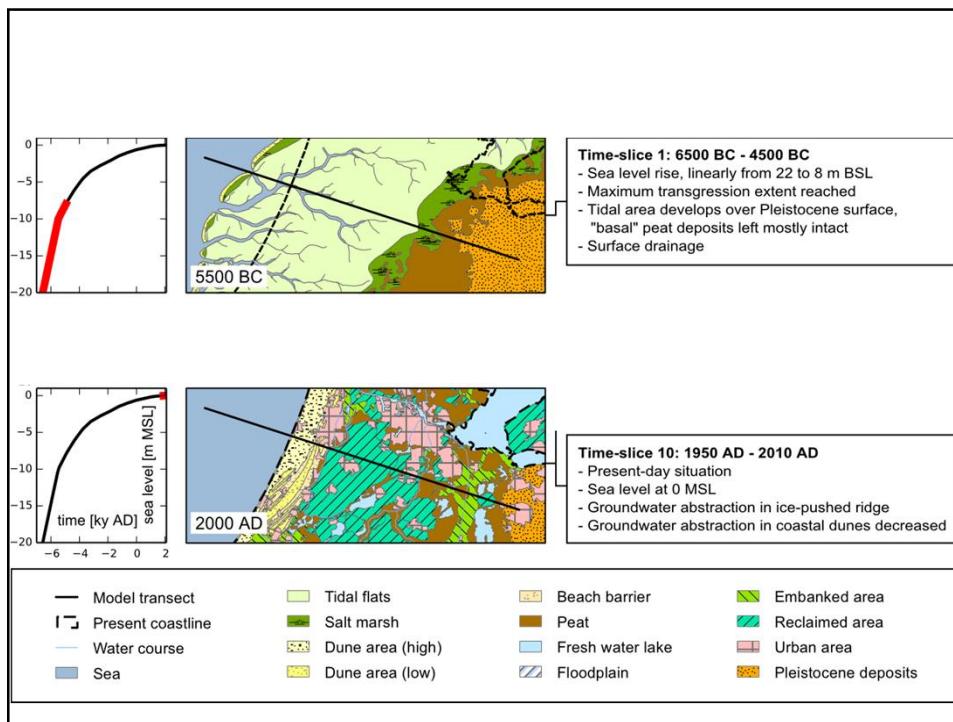
## Occurrence of salt under the polder Haarlemmermeer

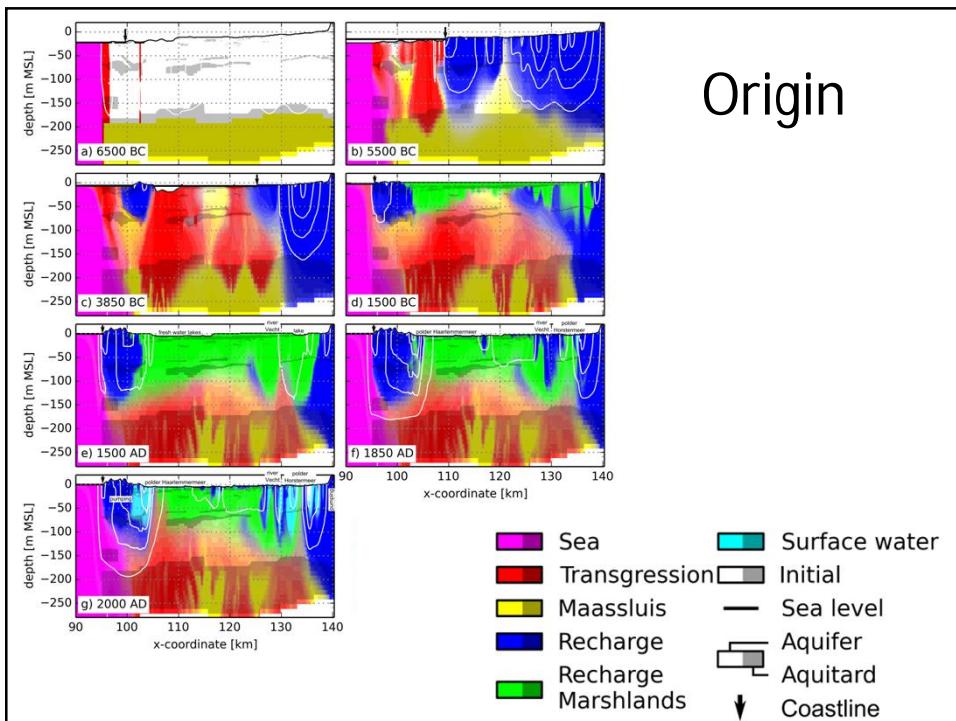
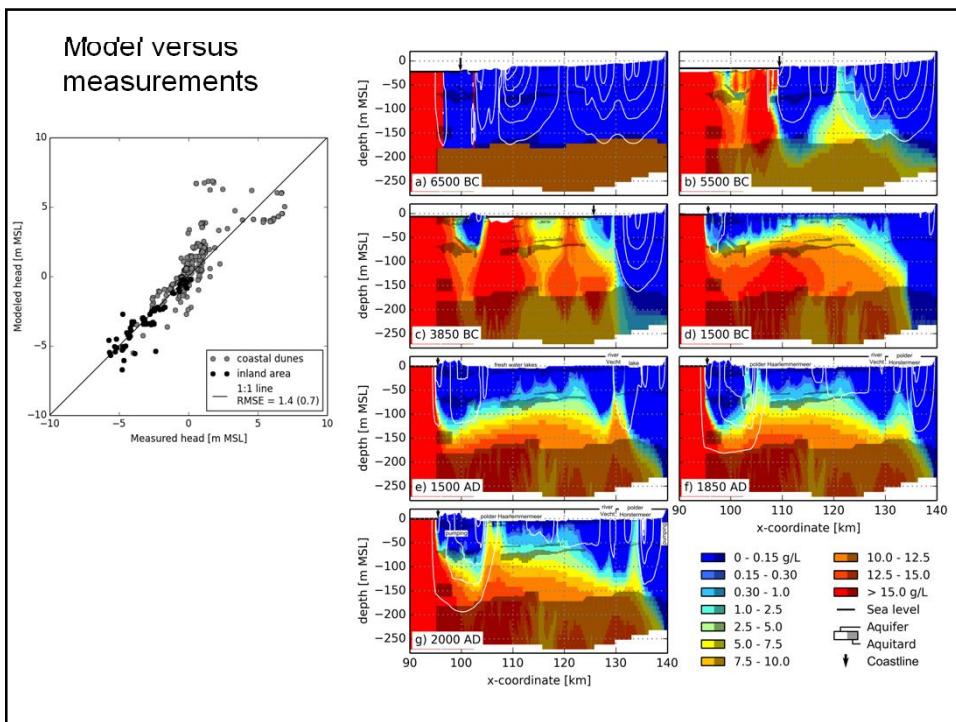
- Model profile Zandvoort - Hoofddorp – Hilversum
- Palaeogeographical development (Vos et al, 2011)
- 6500 BC - 2010 AD
- marine transgression
- Peat development, peat degradation, drainage, ~~reclamation~~

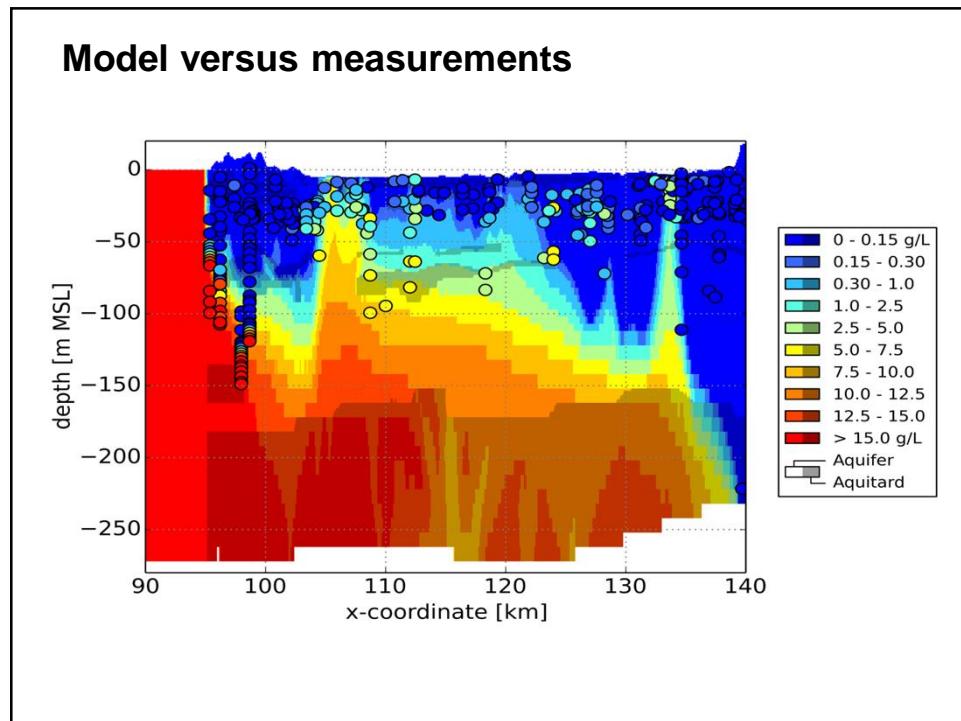
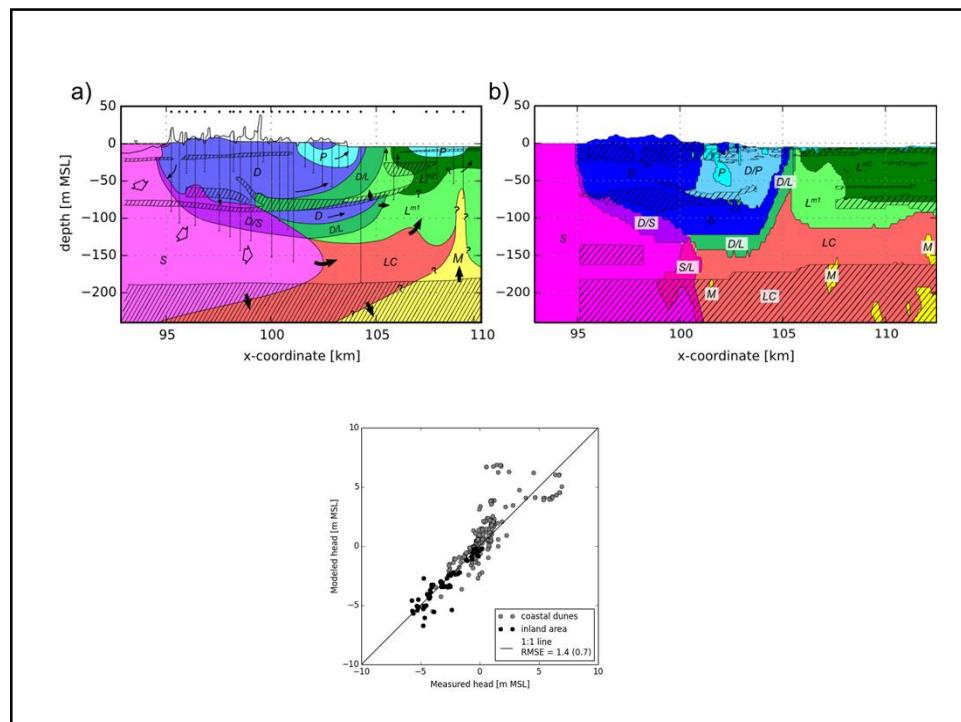


Delsman et al., HESS, 2013









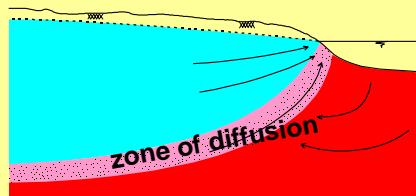
# Sharp interface between fresh and saline groundwater

Introduction

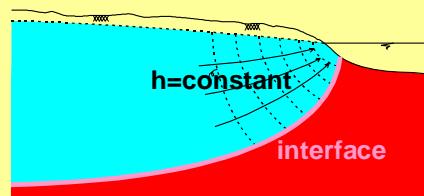
## Badon Ghyben-Herzberg principle

Difference between reality and Badon Ghyben-Herzberg approximation

**concept: mixing zone in reality**



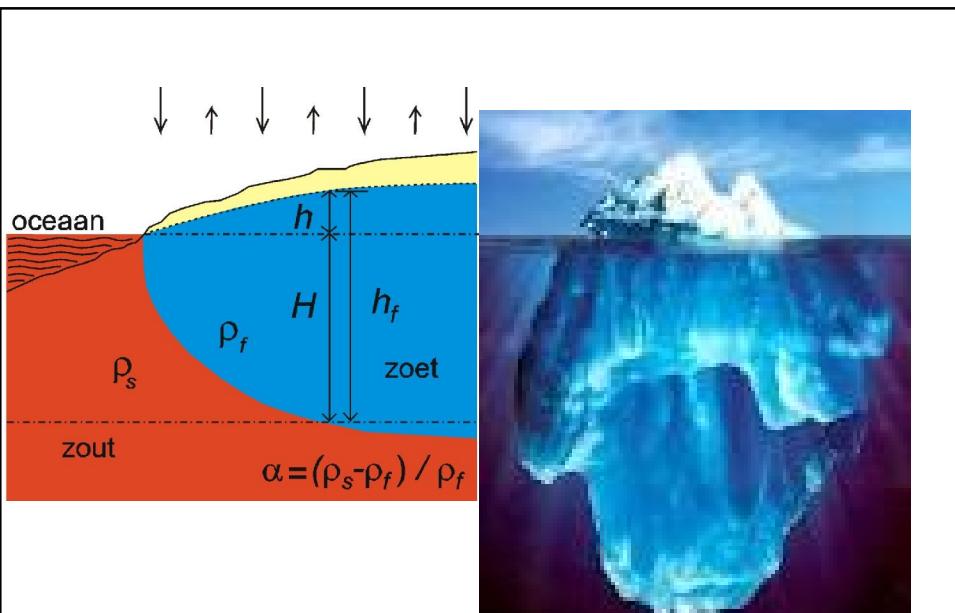
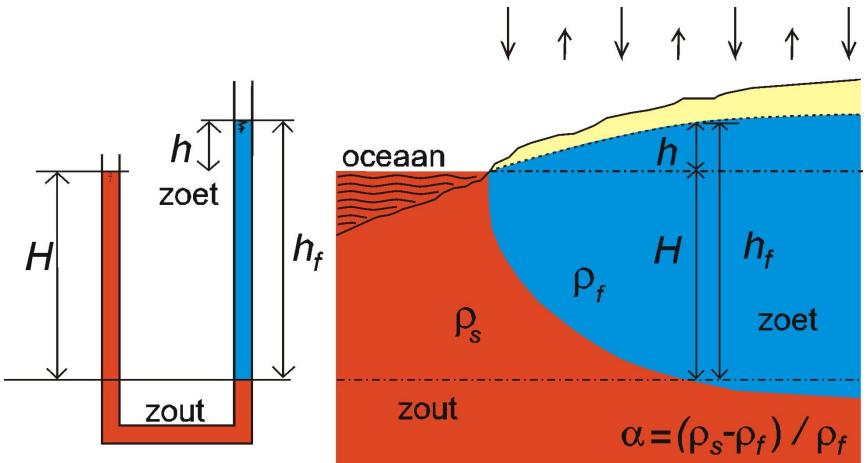
**concept: interface between fresh and saline groundwater**



## Badon Ghijben-Herzberg principle

The principle suggests an interface between fresh and saline groundwater

Analogy: iceberg & saline ocean and granite tectonic plate & basalt base

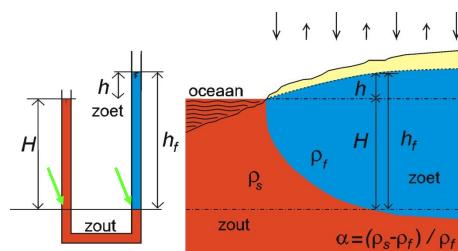


pressure saline groundwater = pressure fresh groundwater

$$\rho_s H g = \rho_f (H + h) g$$

$$h = \frac{\rho_s - \rho_f}{\rho_f} H$$

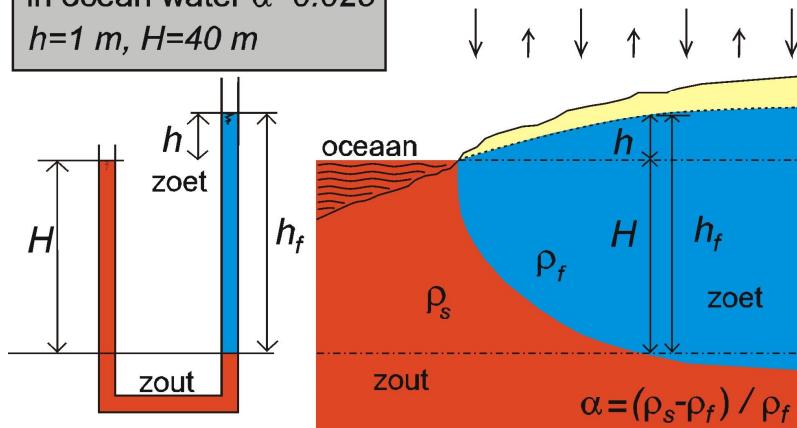
$$h = \alpha H$$



$$h = \alpha H$$

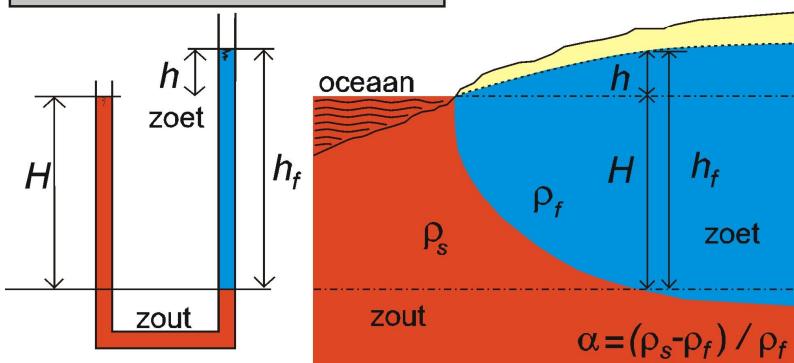
$$h = \alpha H$$

in ocean water  $\alpha = 0.025$   
 $h = 1 \text{ m}, H = 40 \text{ m}$



$$h = \alpha H$$

$h = \alpha H$   
 Mediterranean Sea  $\alpha = 0.028$   
 $h = 1 \text{ m}, H = 35.7 \text{ m}$



### Badon Ghyben-Herzberg principle

- gives analytical solutions (see later and lectures)
- educational
- interface is a simple approximation
- dispersion zone <10m
- relative simple geometries

## Badon Ghyben-Herzberg principle

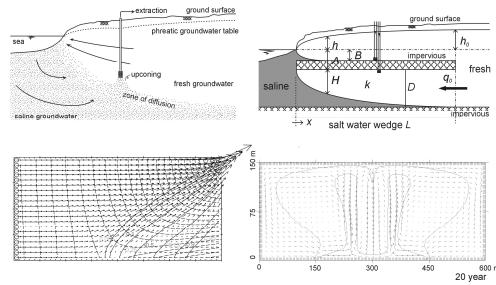
What is the case then  $h \neq \alpha H$ ?

1. still dynamic situation
2. occurrence resistance layer
3. natural groundwater recharge not constant
4. relative density difference  $\alpha$  is not ok
5. occurrence shallow bedrock
6. groundwater extractions

## Analytical solutions

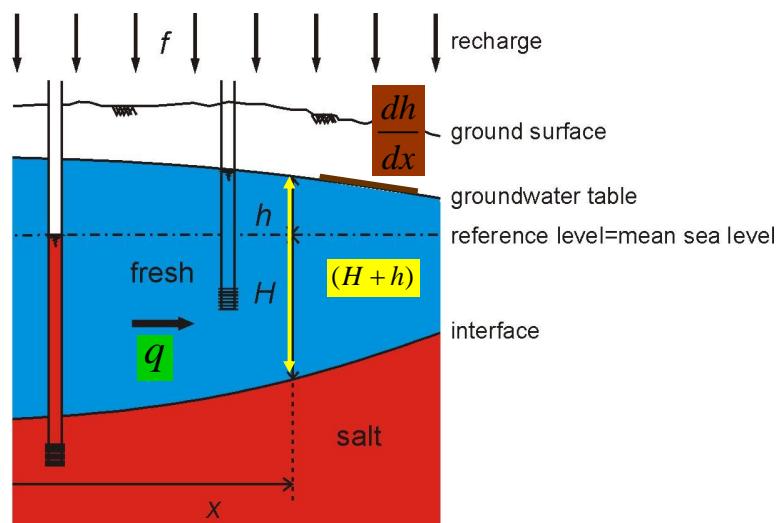
## Analytical solutions

See lecture notes *Density dependent groundwater flow* (p. 29-48)



<http://public.deltares.nl/display/FRESHSALT/Download>

## Unconfined aquifer (1D situation)



## Unconfined aquifer (1D situation)

(I) Darcy       $q = -k(H + h) \frac{dh}{dx}$

(II) Continuity     $dq = f dx$

(III) BGH         $h = \alpha H$

## Unconfined aquifer (1D situation)

$$dq = f dx \quad \text{integration gives} \quad q = fx + C1$$

$$-k(H + h) \frac{dh}{dx} = fx + C1$$

$$h = \alpha H \rightarrow -k(H + \alpha H) \alpha \frac{dH}{dx} = fx + C1$$

$$H dH = -\frac{fx + C1}{k\alpha(1 + \alpha)} dx$$

## Unconfined aquifer (1D situation)

$$HdH = -\frac{fx + C1}{k\alpha(1+\alpha)} dx$$

integration  
gives

$$\frac{1}{2}H^2 = \frac{-\frac{1}{2}fx^2 - C1x + C2}{k\alpha(1+\alpha)}$$

$$H = \sqrt{\frac{-fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}}$$

## Unconfined aquifer (1D situation)

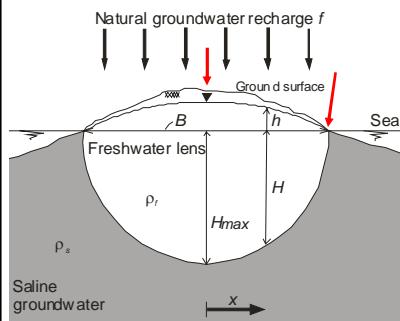
$$H = \sqrt{\frac{-fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}}$$

$$h = \alpha H$$

$$q = fx + C1$$

## Example 1: Elongated island

$$H = \sqrt{\frac{-fx^2 - 2C1x + 2C2}{k\alpha(1+\alpha)}} \quad q = fx + C1$$

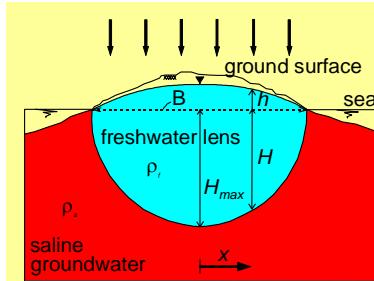


Boundary conditions

$$x = 0 : q = 0 \rightarrow C1 = 0$$

$$x = 0.5B : H = 0 \rightarrow C2 = fB^2 / 8$$

## Example of analytical solutions (I)



Depth of fresh-saline interface  $H$

$$H = \sqrt{\frac{f(0.25B^2 - x^2)}{k\alpha(1+\alpha)}}$$

$$h = \alpha H$$

Maximal thickness lens

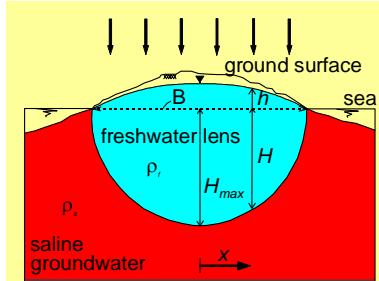
$$H_{\max} = \frac{1}{2} B \sqrt{\frac{f}{k\alpha(1+\alpha)}}$$

Volume lens

$$V = \frac{1}{4} \pi (1+\alpha) H_{\max} B n_e$$

$$\text{Characteristic time } T = \frac{\text{volume of water in lens}}{\text{inflow of water}} = \frac{\pi n_e B}{8} \sqrt{\frac{(1+\alpha)}{k f \alpha}}$$

## Example of analytical solutions (I)



**Depth of fresh-saline interface H**

$$B = 2000\text{m}, f = 0.001\text{m/day}$$

$$k = 10\text{m/day}, \alpha = 0.025$$

$$n_e = 0.35$$

Maximal thickness lens

Volume lens (wrong in lectures notes)

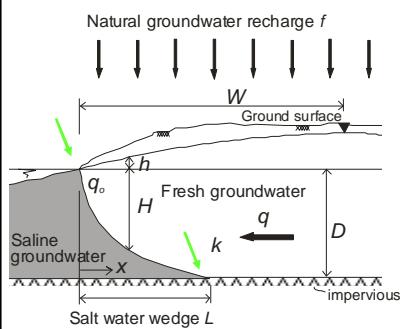
$$H_{\max} = 62.5\text{m}, h_{\max} = 1.56\text{m} \quad V = 35203\text{m}^3/\text{m}'$$

$$\text{Characteristic time } T = \frac{35203}{2} \text{ days} = 48.2 \text{ years}$$

Lecture notes p. 32

## Example 2: salt water wedge

$$H = \sqrt{\frac{-fx^2 - 2C_1x + 2C_2}{k\alpha(1+\alpha)}} \quad q = fx + C_1$$



Boundary conditions

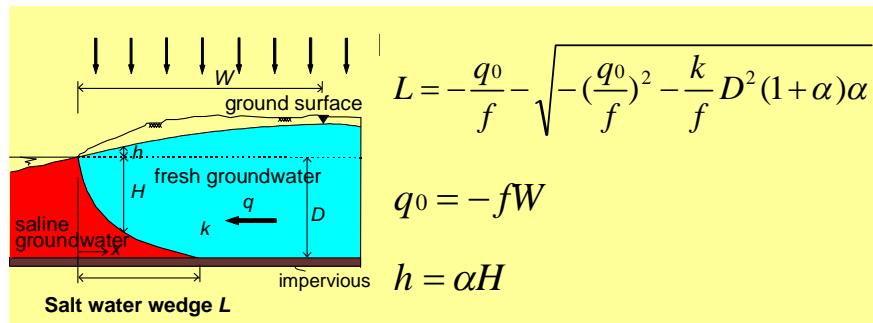
$$x = 0 : q = q_0 \rightarrow q_0 = -fW \rightarrow C_1 = q_0$$

$$x = 0 : H = 0 \rightarrow C_2 = 0$$

Length of salt water wedge

$$x = L : H = D$$

## Example of analytical solutions (II)



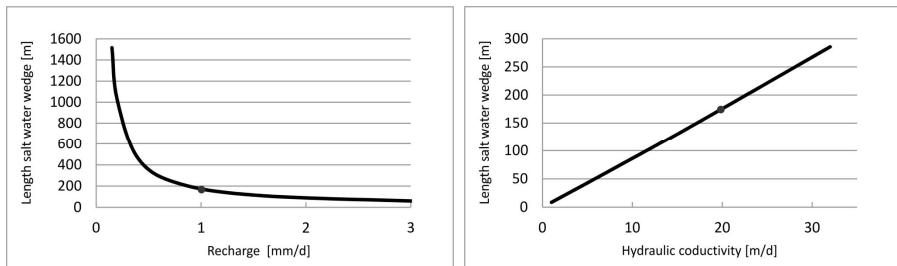
Example:

$$W = 3000\text{m}, f = 0.001\text{m/day}, \alpha = 0.020, k = 20\text{m/day}, D = 50\text{m}$$

$$L = 175.1\text{m}$$

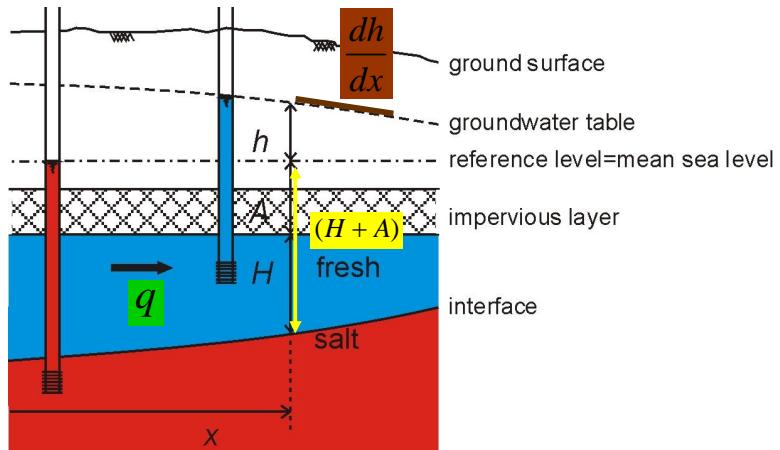
Lecture notes p. 33

*Length of the salt water wedge as a function of a. recharge and b. hydraulic conductivity*



*the dots resample with the example mentioned above*

## Confined aquifer (1D situation)



## Confined aquifer (1D situation)

(I) Darcy      
$$q = -kH \frac{dh}{dx}$$

(II) Continuity    
$$q = q_o$$

(III) BGH      
$$h = \alpha(H + A)$$

## Confined aquifer (1D situation)

$$-kH \frac{dh}{dx} = q_0$$

$$HdH = -\frac{q_0}{k\alpha} dx$$

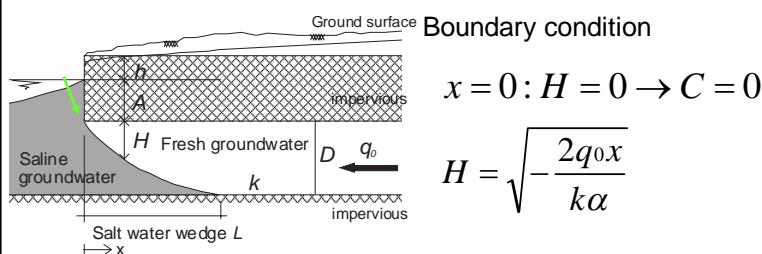
integration gives

$$\frac{1}{2} H^2 = \frac{q_0 x}{k\alpha} + C$$

$$H = \sqrt{-\frac{2q_0 x}{k\alpha} + 2C}$$

## Example 3: salt water wedge confined aquifer

$$H = \sqrt{-\frac{2q_0 x}{k\alpha} + 2C}$$



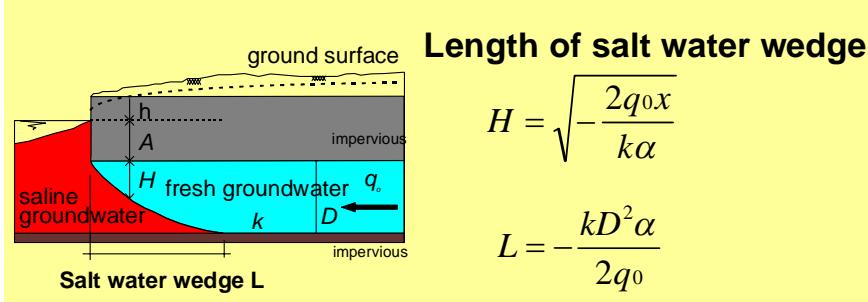
$$x = 0 : H = 0 \rightarrow C = 0$$

$$H = \sqrt{-\frac{2q_0 x}{k\alpha}}$$

Length of salt water wedge  $x = L : H = D$

$$L = -\frac{kD^2\alpha}{2q_0}$$

### Example of analytical solutions (III)



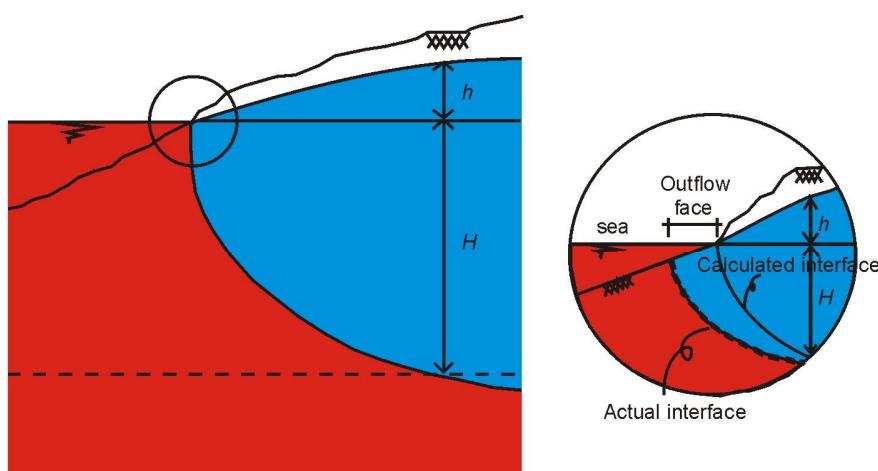
Example:

$$W = 2000\text{m}, f = 0.001\text{m/day}, \alpha = 0.025, k = 25\text{m/day}, D = 40\text{m}$$

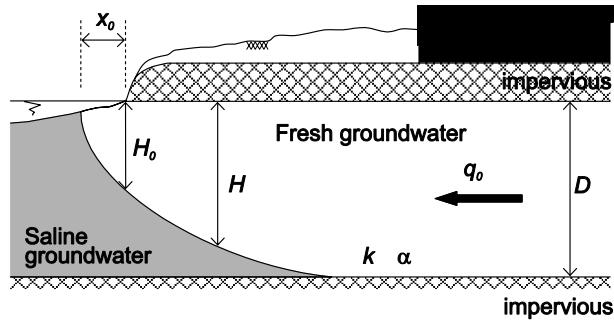
$$L = 250\text{m}$$

Lecture notes p. 35-36

### Outflow face (Submarine Groundwater Discharge)



### Outflow face (Submarine Groundwater Discharge)



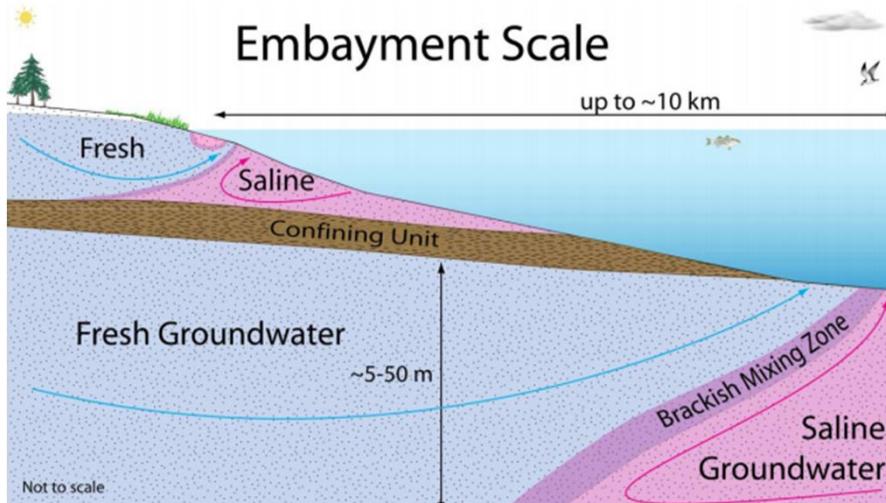
$$x_0 = \frac{q_0}{2k\alpha} \quad H_0 = \frac{q_0}{k\alpha} \quad \text{Glover (1959)}$$

Example:

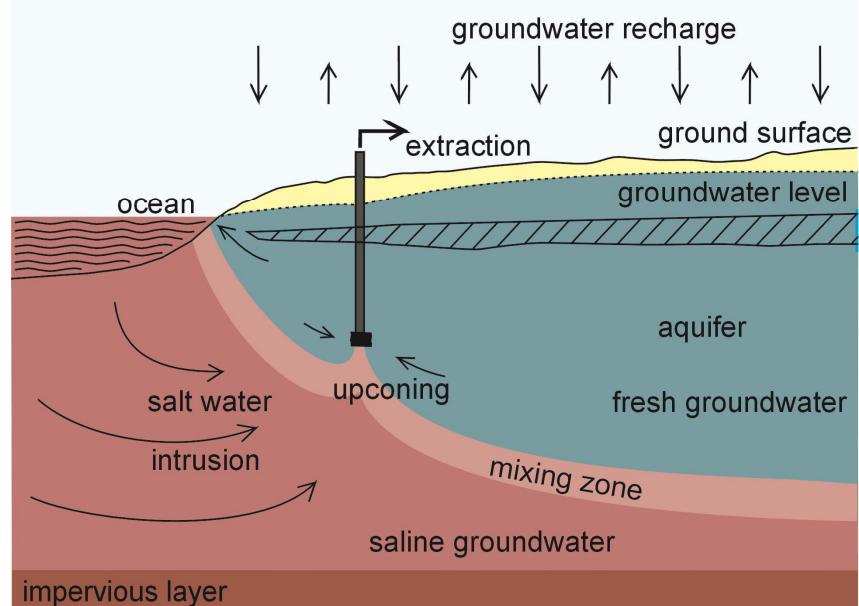
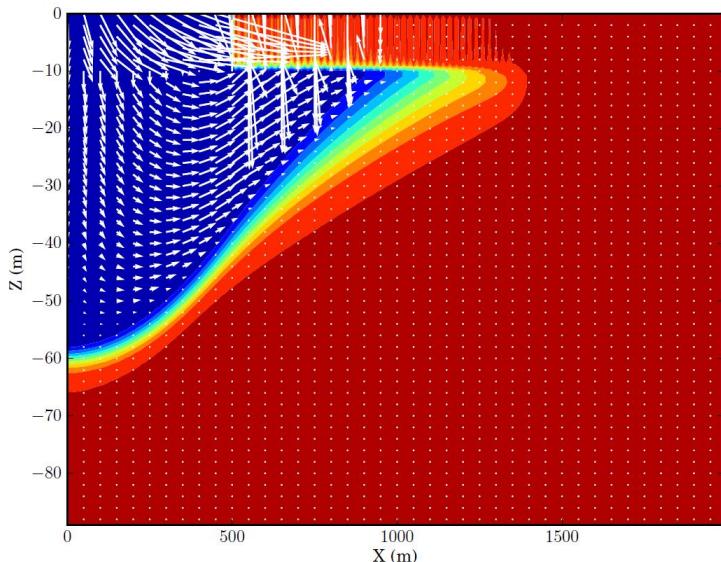
$$x_0 = f^* L / (2ka) = 0.001m/d * 20000m / (2 * 20 * 0.025) = 20m \text{ (only!)}$$

Note: no resistance layer offshore

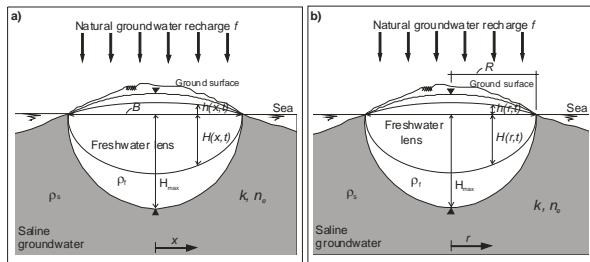
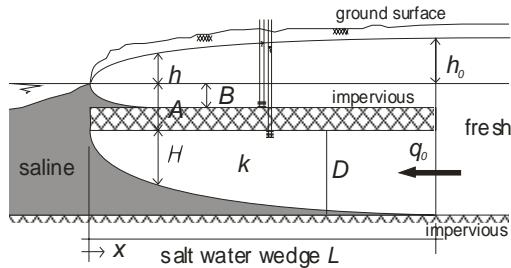
### Outflow face (Submarine Groundwater Discharge)



### Outflow face (Submarine Groundwater Discharge)



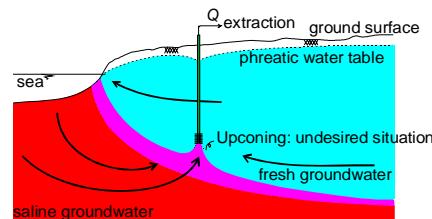
See the lectures for more cases



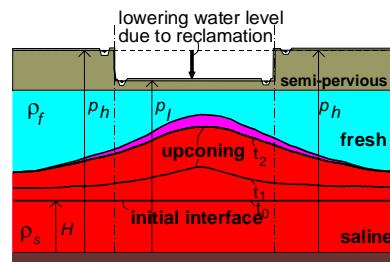
Upconing processes

## Upconing of saline groundwater

### Under an extraction well



### Under a low-lying polder area

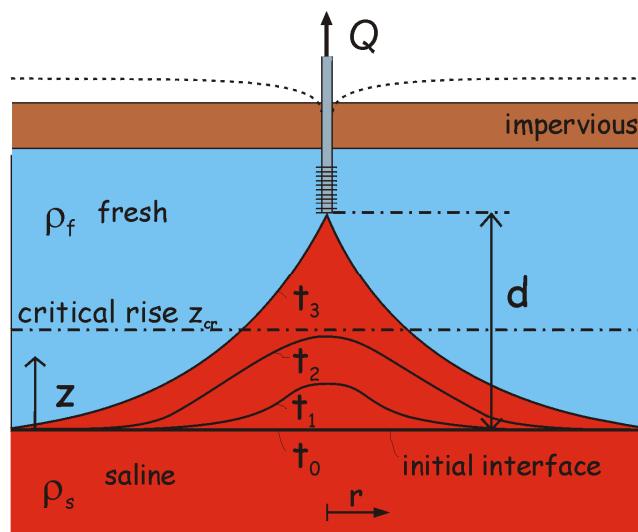


- movement of saline groundwater to extraction wells
- increase in salinity ( $>150-200 \text{ mg Cl-l}$ )
- lowering of the piezometric head (leads to land subsidence: e.g. Los Angeles: 9 m in the 1930's)

'Solutions': reduce extraction rate, abandon well, inundate polder

## Examples of analytical solutions (IV)

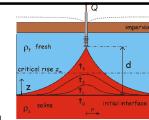
### Upconing of saline groundwater under an extraction well



Lecture notes p. 44

## Examples of analytical solutions (IV)

Upconing of saline groundwater under an extraction well



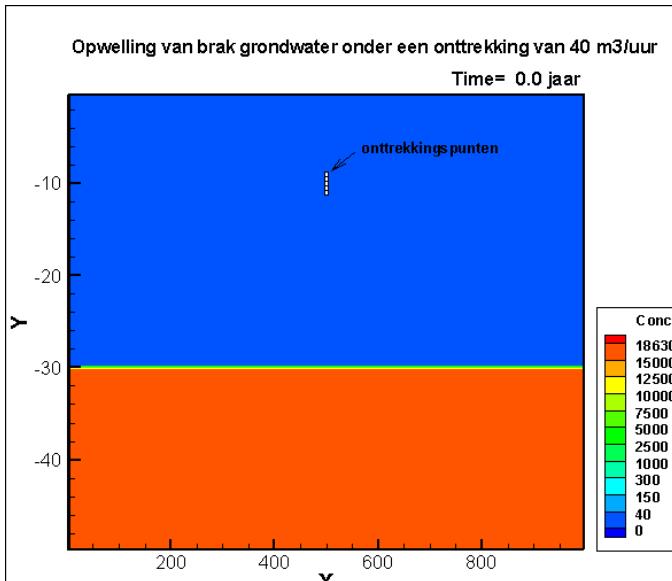
$$z(r, t) = \frac{Q}{2\pi\alpha k_x d} \left[ \frac{1}{(1 + R'^2)^{1/2}} - \frac{1}{[(1 + \gamma')^2 + R'^2]^{1/2}} \right]$$

$$R' = \frac{r}{d} \frac{k_z}{k_x}^{1/2} \quad \gamma' = \frac{\alpha k_z}{2n_e d} t$$

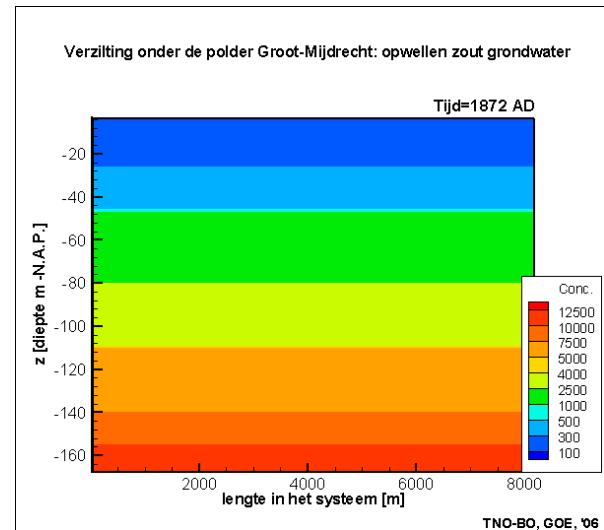
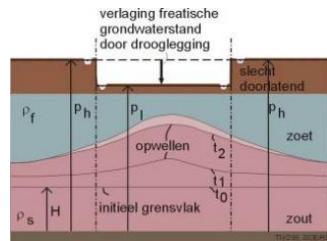
Dagan & Bear, 1968, J. Hydraul. Res 6, 1563-1573

Lecture notes p. 44

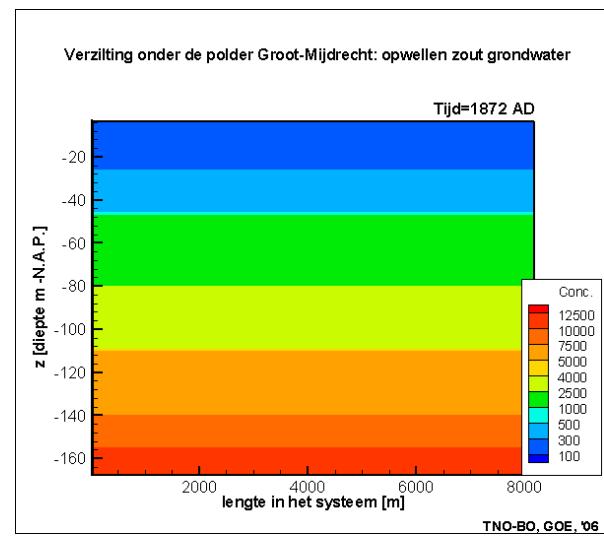
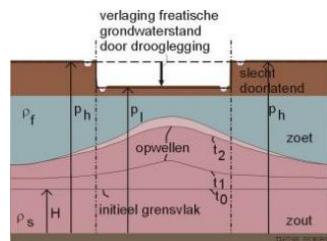
## Upconing of salt under an extraction



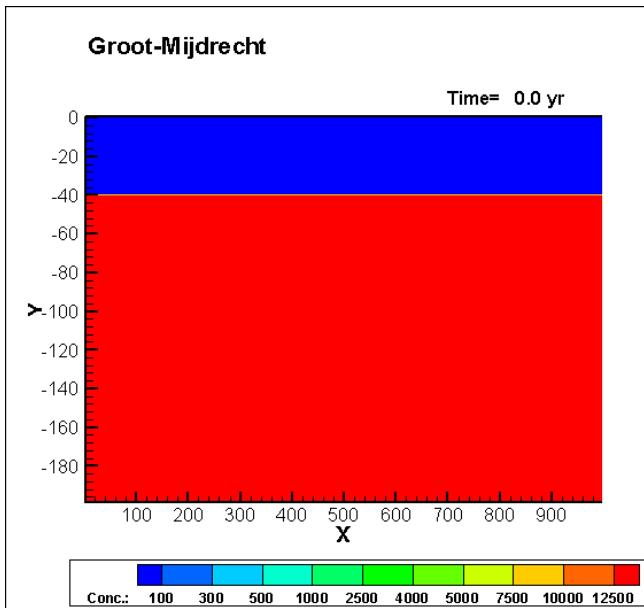
## Upconing under a low-lying polder (Groot-Mijdrecht)



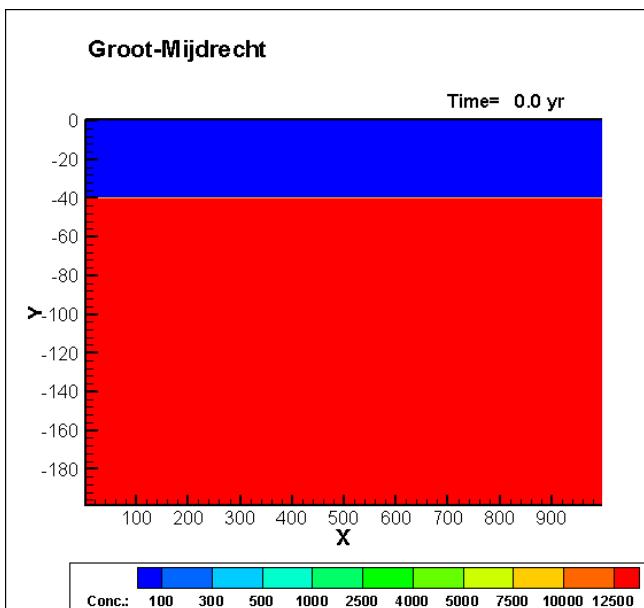
## Upconing under a low-lying polder (Groot-Mijdrecht)



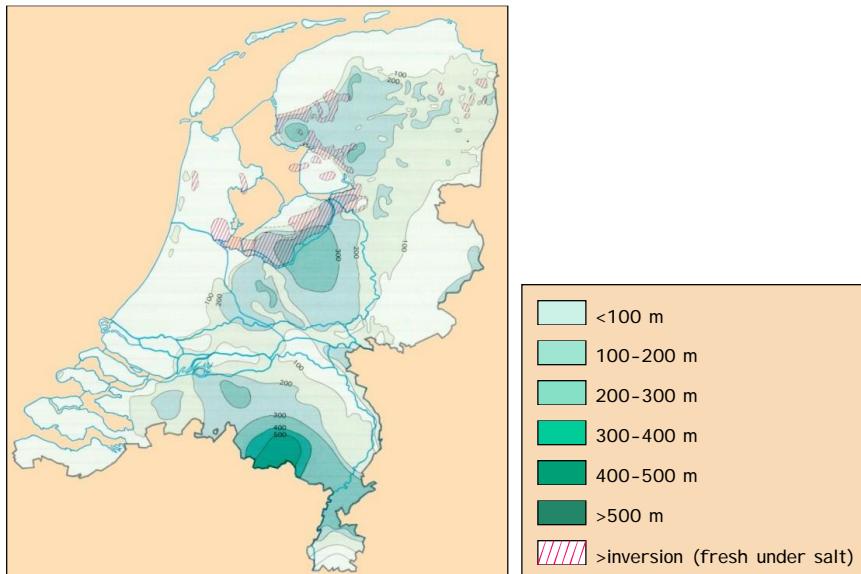
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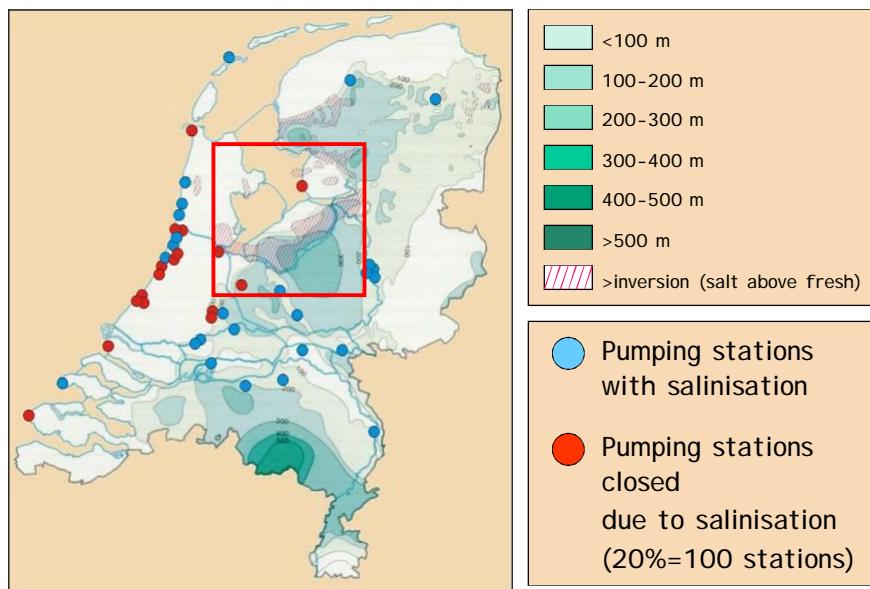
### Upconing under a low-lying polder (Groot-Mijdrecht)



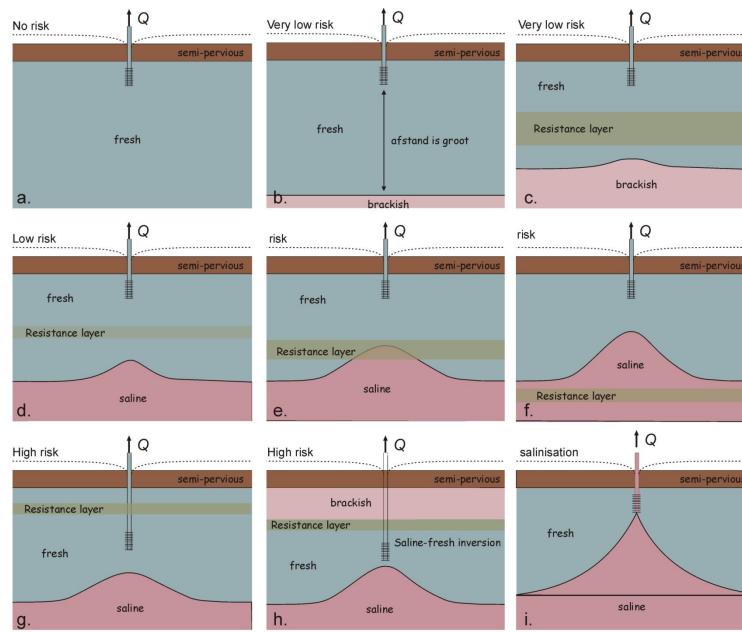
### Fresh-salt interface ( $150 \text{ mg Cl}^-/\text{l}$ )



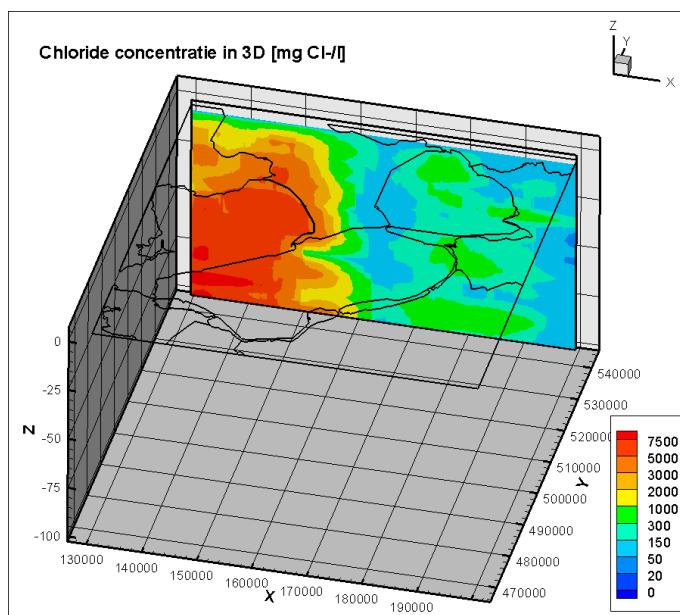
### Availability of fresh groundwater



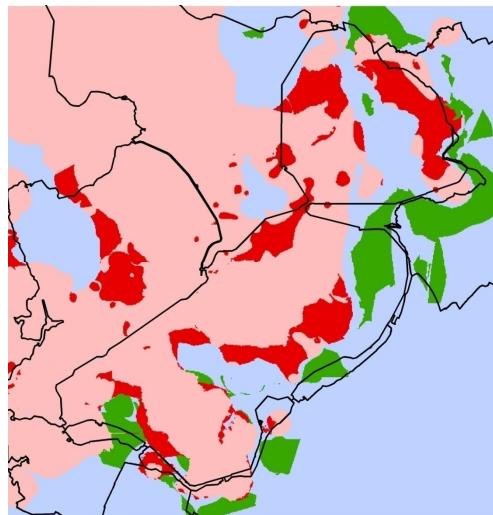
## Different risks of upconing saline groundwater



## Animation 3D Chloride concentration



## Upconing in Flevoland



Risk depends on:

- Initial position interface
- Resistance layers
- Existance inversion
- Extraction rate and scheme

High risk

Low risk

Very low risk

## Compensating measures

### Possible solutions to stop salt water intrusion:

- Restriction of groundwater extractions through permits
- Co-operation between authorities and water users
- Desalination of saline water
- Technical countermeasures of salt water intrusion
  - six examples

### Tools to understand salt water intrusion:

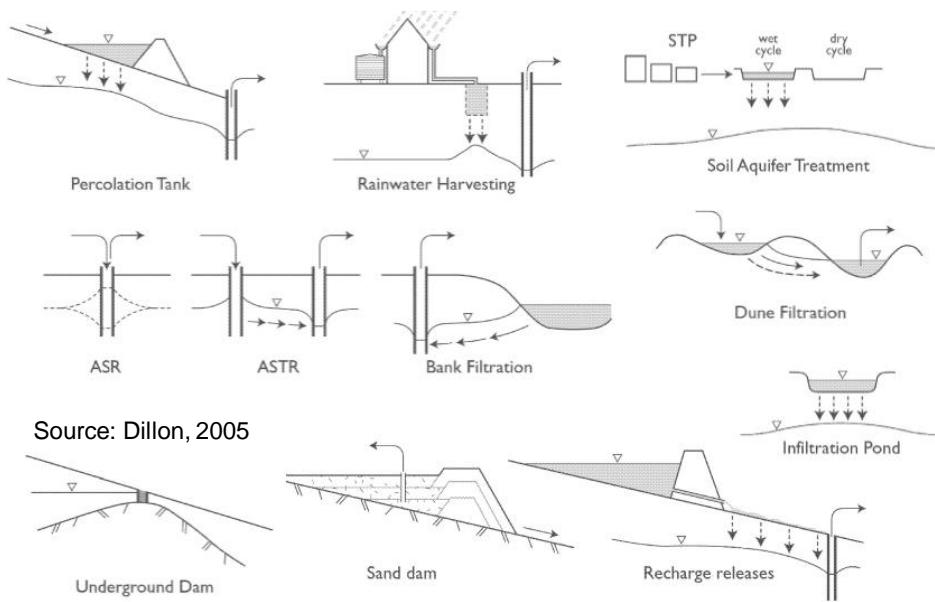
- Monitoring of salinities and piezometric levels
- Numerical modelling of salt water intrusion

### Measures to compensate salt water intrusion

- 'The Fresh Holder'
- Extraction of saline/brackish groundwater
- Infiltration of fresh surface water
- Modifying pumping rates
- Land reclamation in front of the coast
- Creating physical barriers (crystallisation or biosealing)

## Aquifer Storage and Recovery

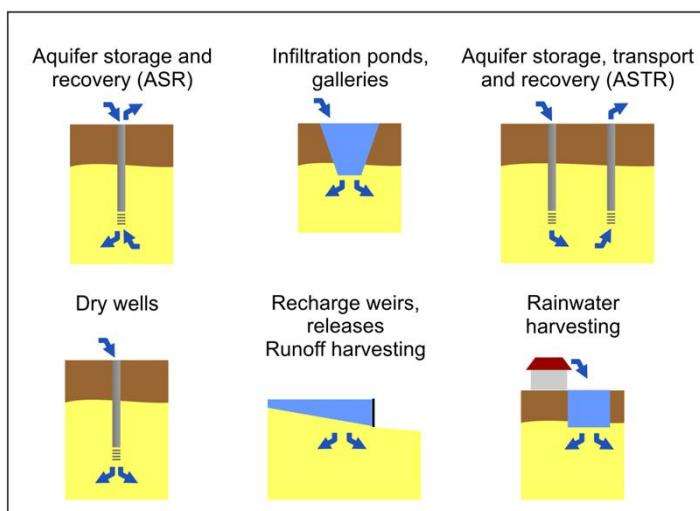
*"potential to be a major contribution to UN Millennium Goals for Water Supply"*



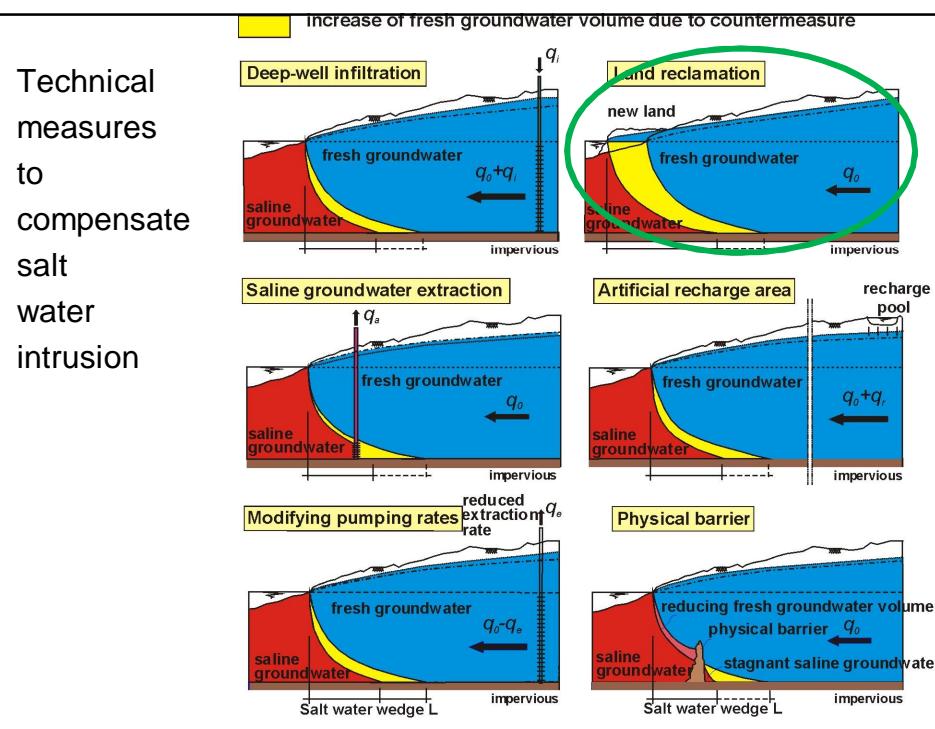
Source: Dillon, 2005

## Aquifer Storage and Recovery / Managed Aquifer Recharge

*"potential to be a major contribution to UN Millennium Goals for Water Supply"*

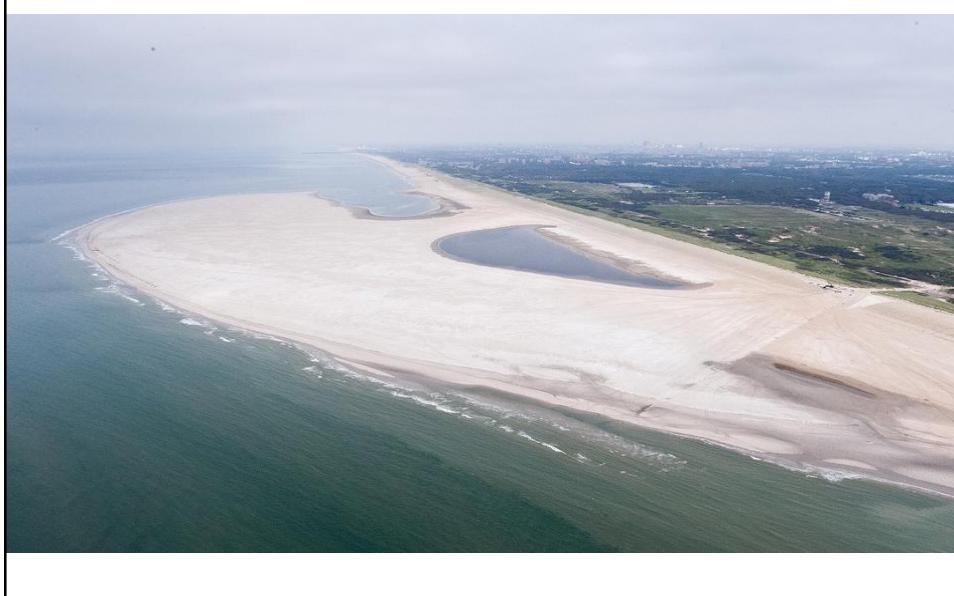


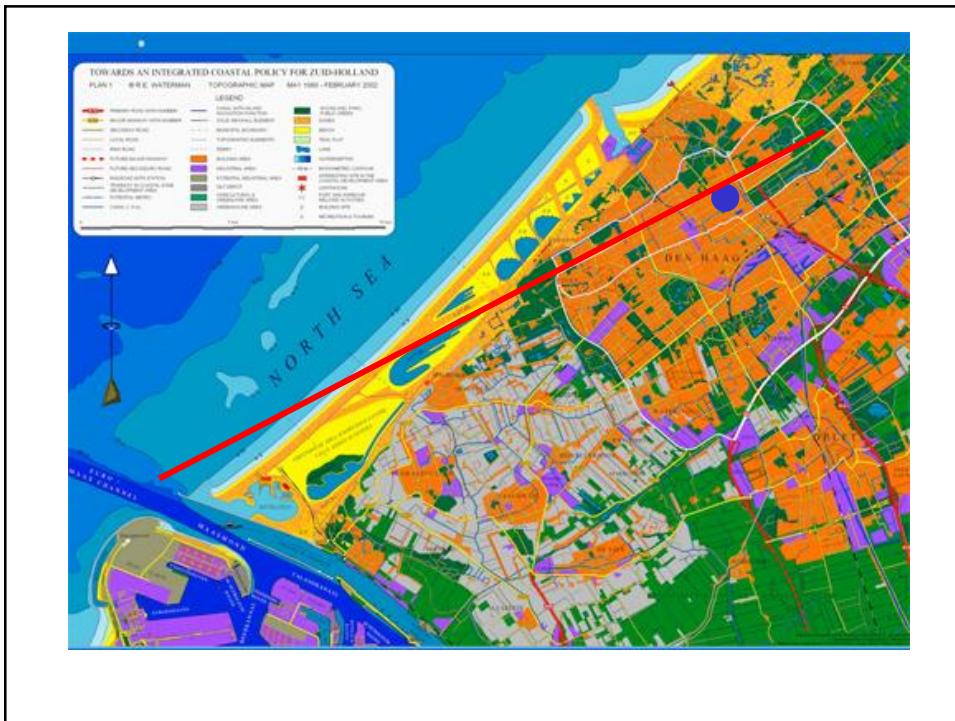
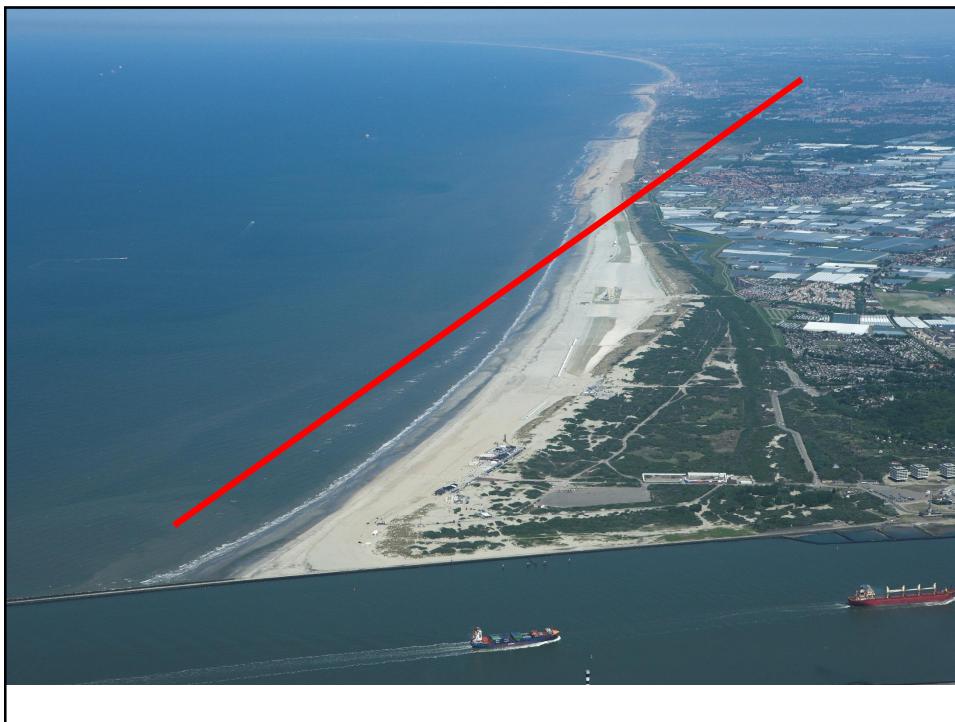
Source: Dillon, 2005



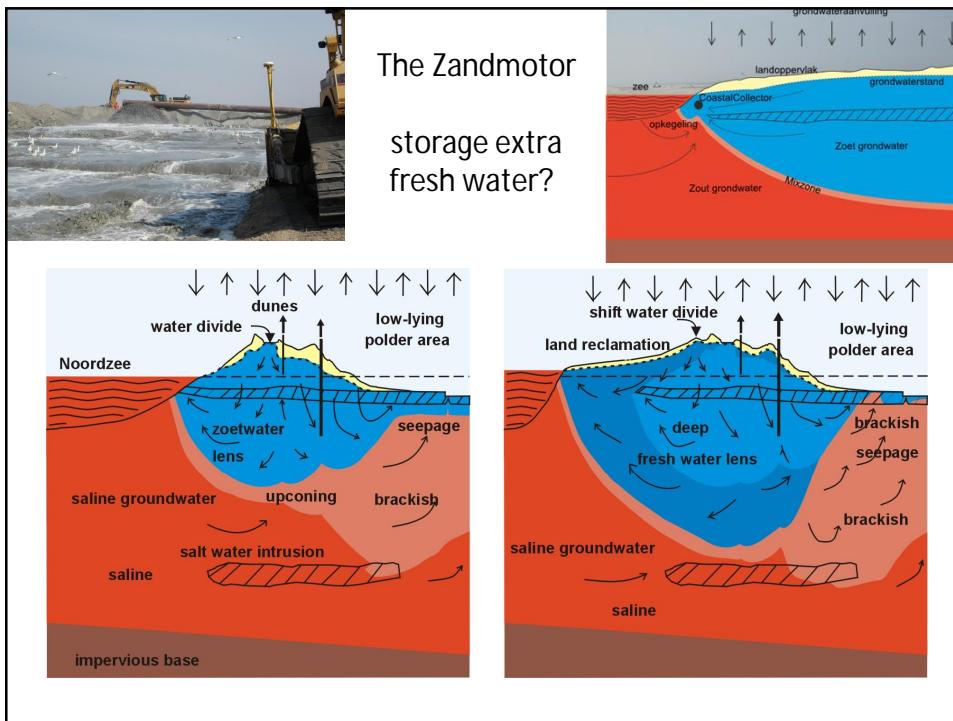
## Land reclamation

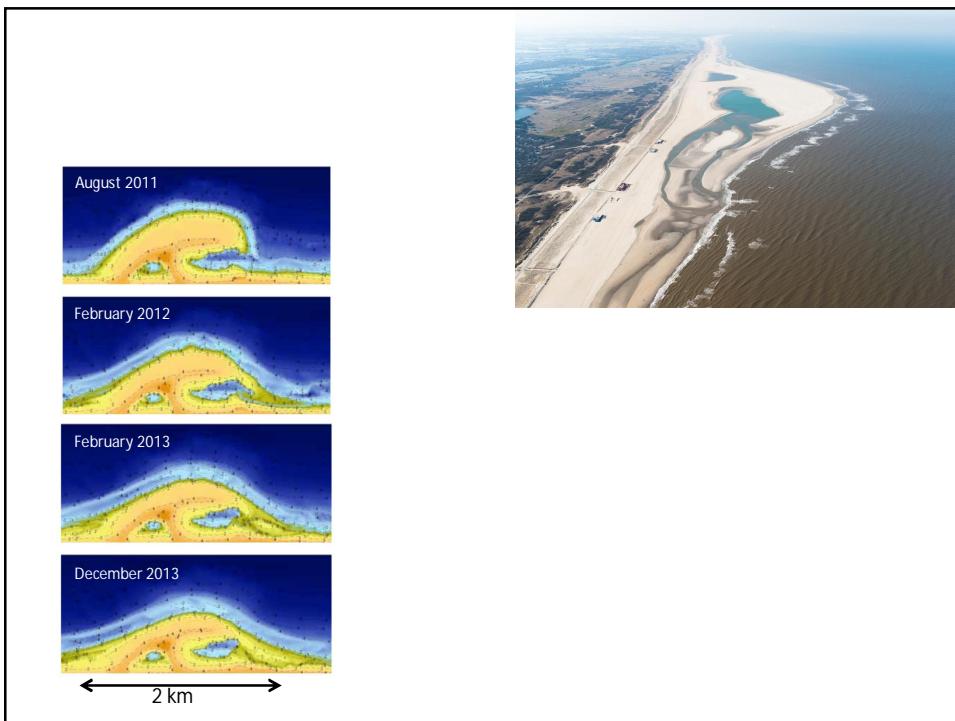
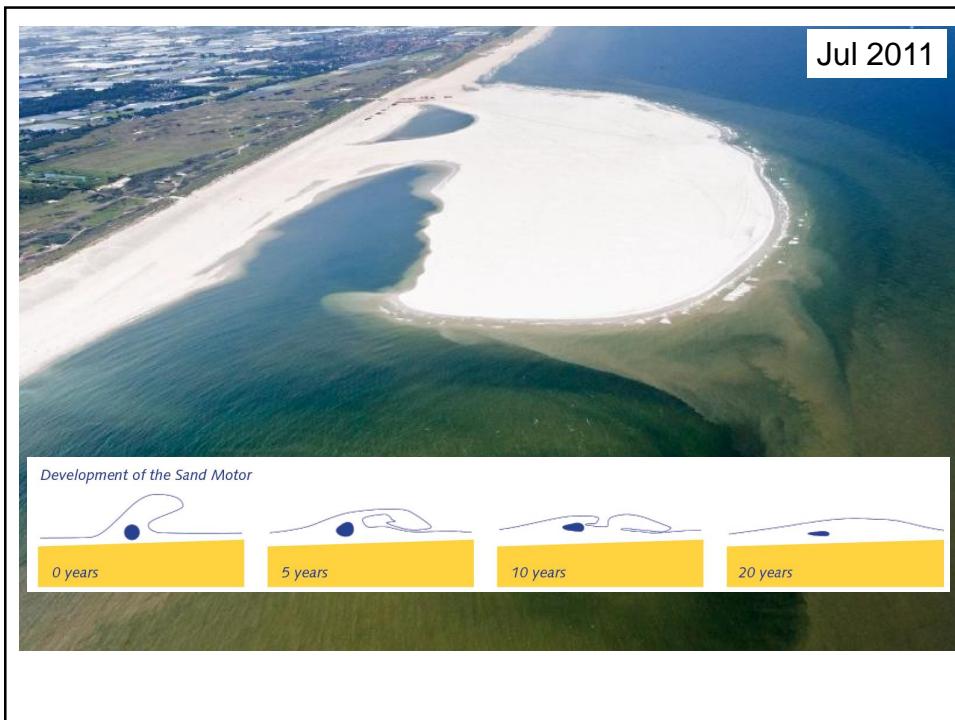
### The Zandmotor: effects at the hinterland?



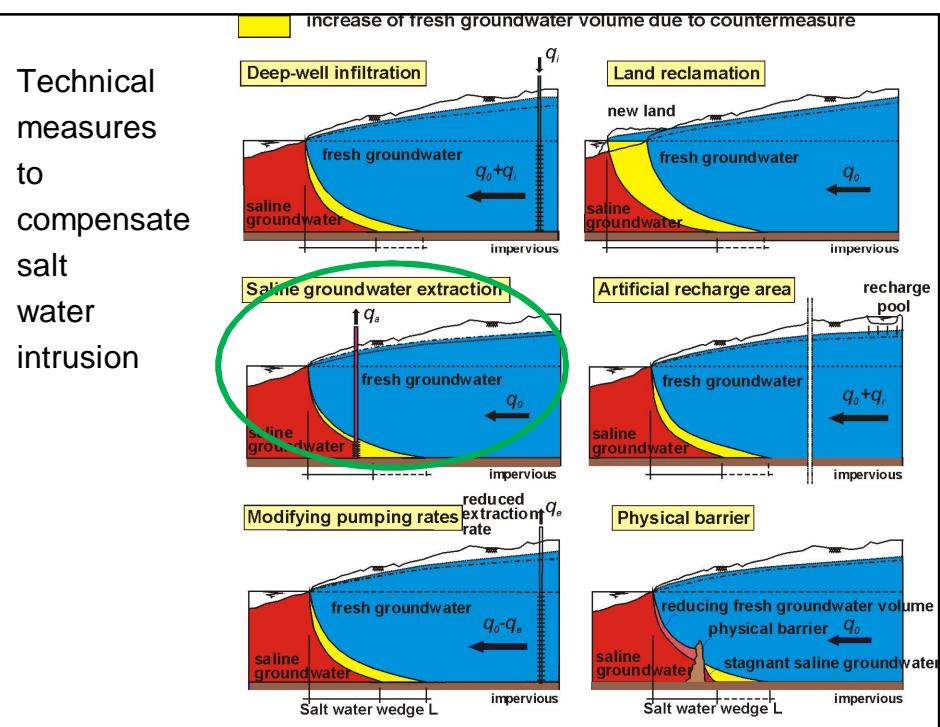
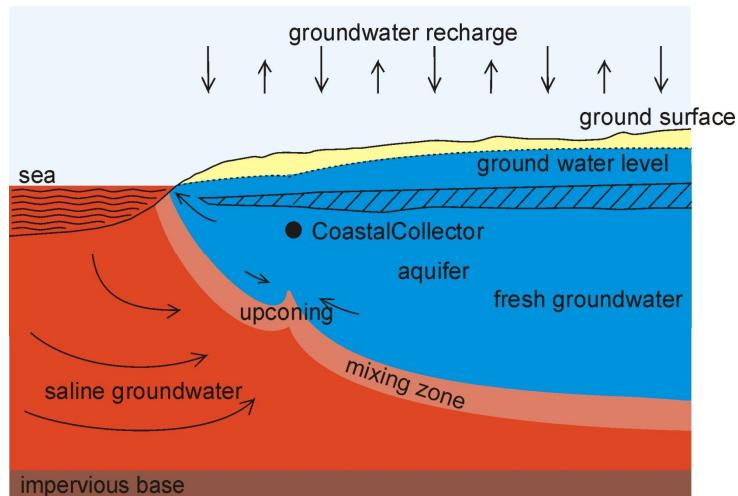


## The Zandmotor: effects at the hinterland?

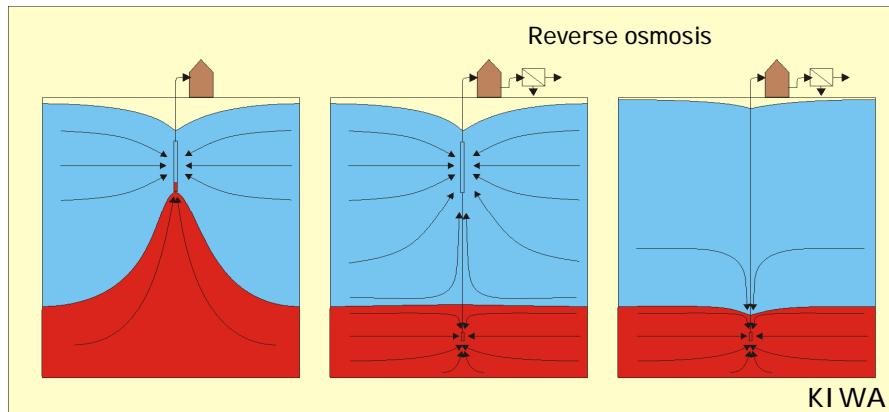




## The Coastal Collector



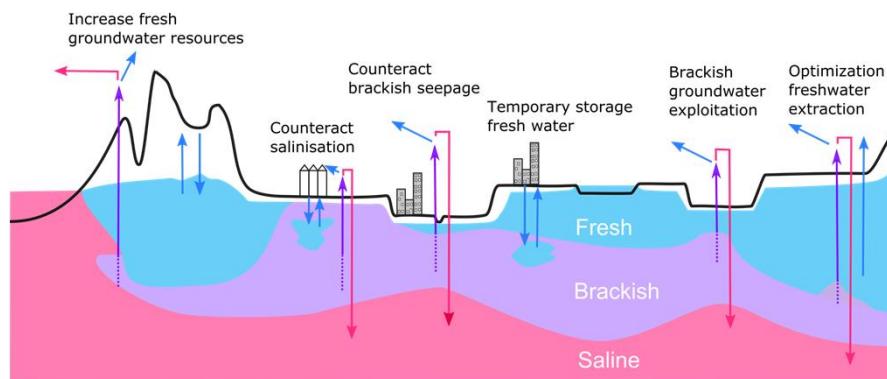
### Solution: The Fresh Holder



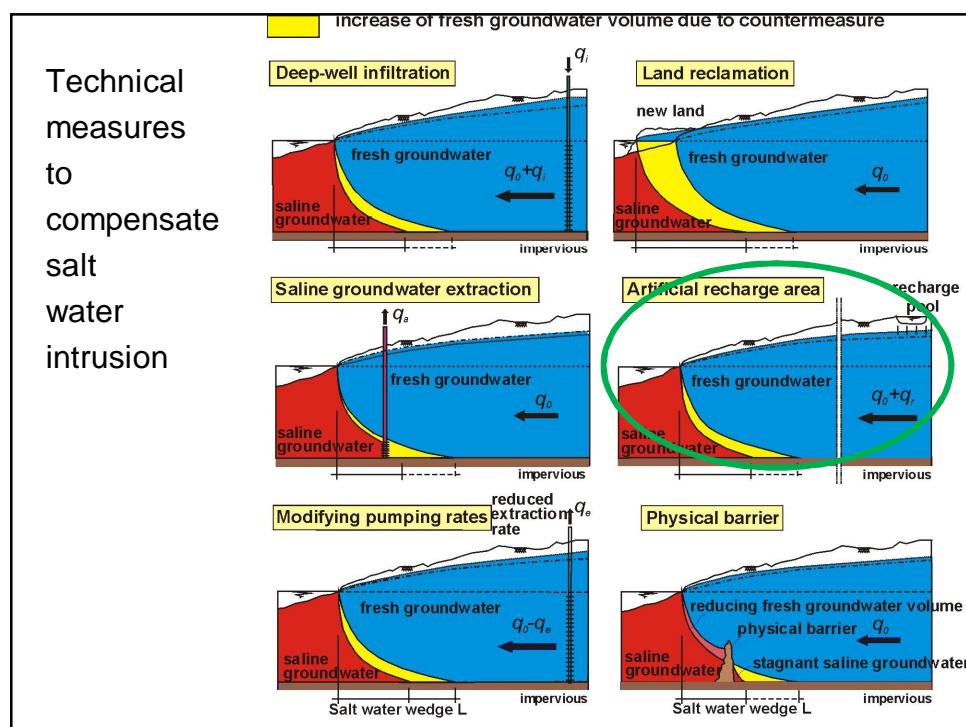
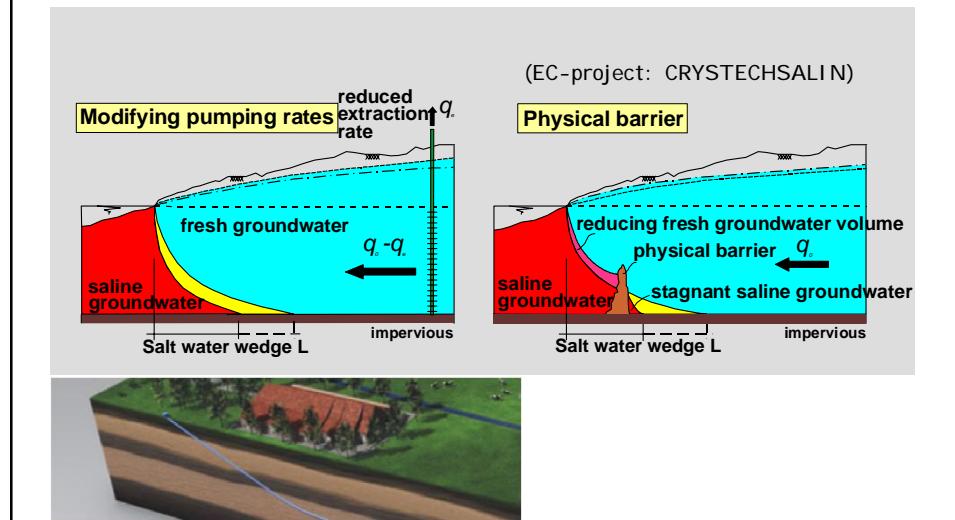
Upconing can be prevented by the extraction of brackish groundwater

This brackish groundwater can be transformed to water of agricultural water quality by using the membrane filtration technique

### COASTAR: COastal Aquifer STorage And Recovery



## Countermeasures of salt water intrusion

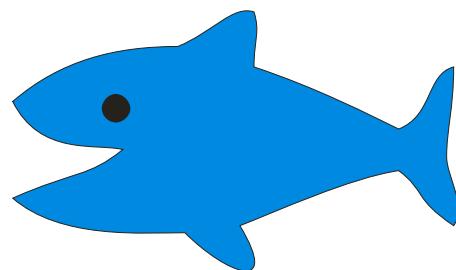


## Base idea

Many local solutions for fresh groundwater supply can have regional impact

## Starring

solution fresh groundwater supply



# **Starring**

Local solution fresh groundwater supply



# **Starring**

climate and global change



# **Starring**

climate and global change



# **Solutions and responses**

Local solution fresh  
groundwater supply

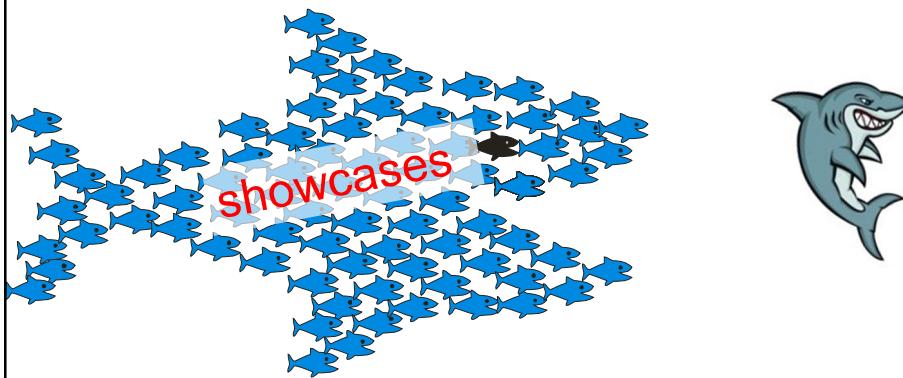
climate and global change



## What should be the response?

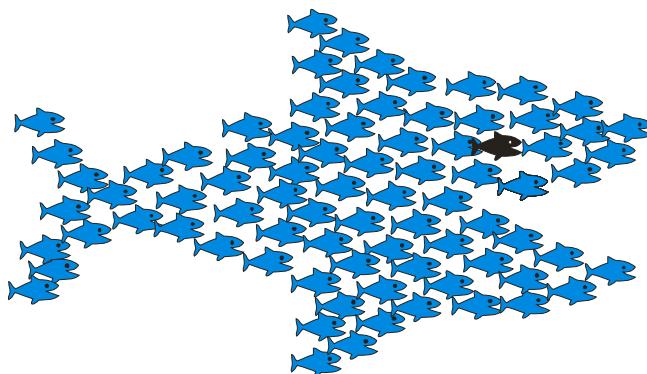
Many local solutions fresh groundwater supply

climate and global change



Many local solutions for fresh groundwater supply can have regional impact!

- upscaling local cases to regional strategy
- assess economical feasibility
- increase impact: communicate our showcases
- working together



## Aquifer Storage and Recovery in the coastal zone



### Goal:

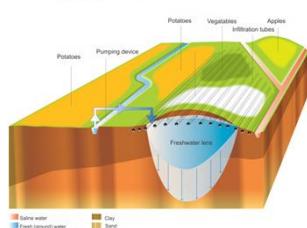
Increase fresh groundwater resources in saline seepage areas in the southwestern part of the Dutch Delta

[www.go-fresh.info](http://www.go-fresh.info)

### Methods:

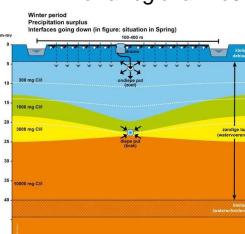
3 pilot studies: infiltration of fresh water in times of water excess and extraction in times of droughts

*Many small local solutions together can be enough for a regional fresh water supply*



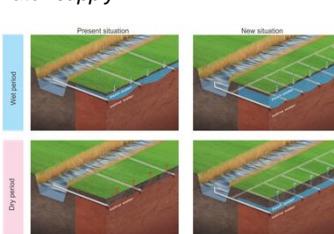
### Creekridge Infiltration Test

Increase fresh water in creek ridge by injection of fresh surface water and extraction of saline groundwater



### The Freshmaker

Increase fresh water volume in creek ridge by passive infiltration via drainage

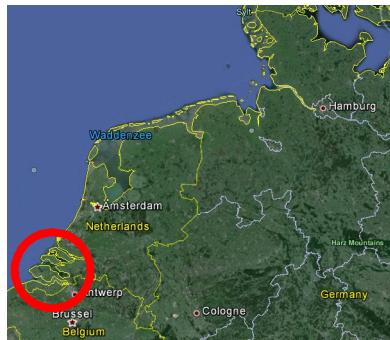


### Drains2Buffer

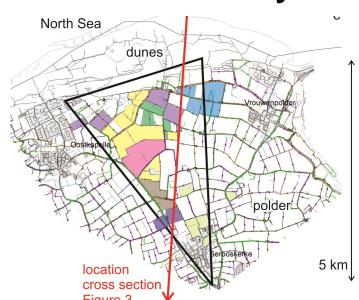
Maintain fresh water volume in shallow rainwater lenses by smart deep controlled drainage

## Problem statement

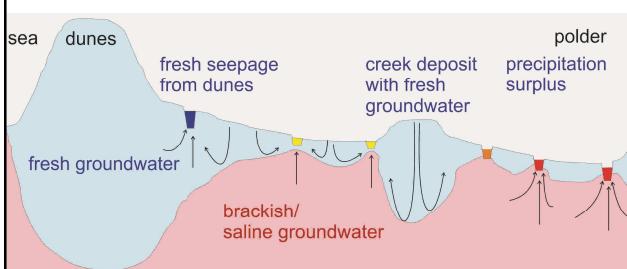
- Crop damage southwestern part of the Netherlands
- Fresh groundwater below creek ridges



## Case study: Water Farm

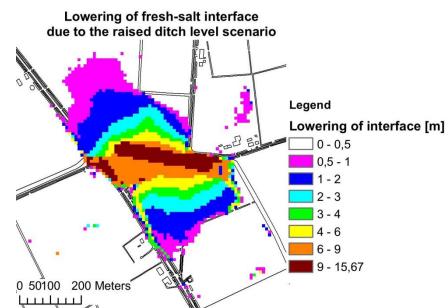


- 3 km<sup>2</sup> area
- 8 farms
  - 4 arable farming
  - 2 horticulture
  - 2 fruit
- start case study 2010



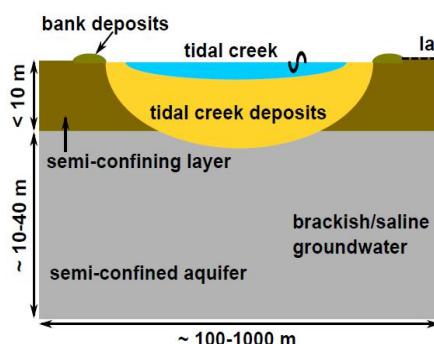
- codesign measures
- communication to outside world

Researchers: scenario analysis

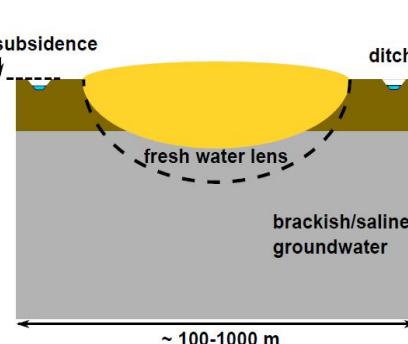


## Creek ridges

1200 AD; before land reclamation

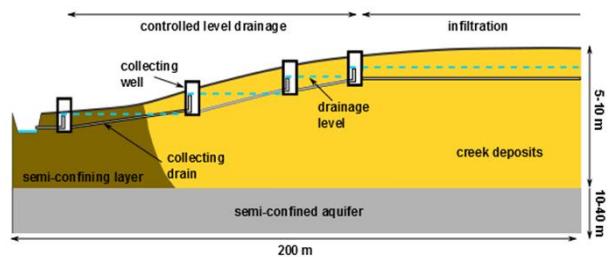


current situation

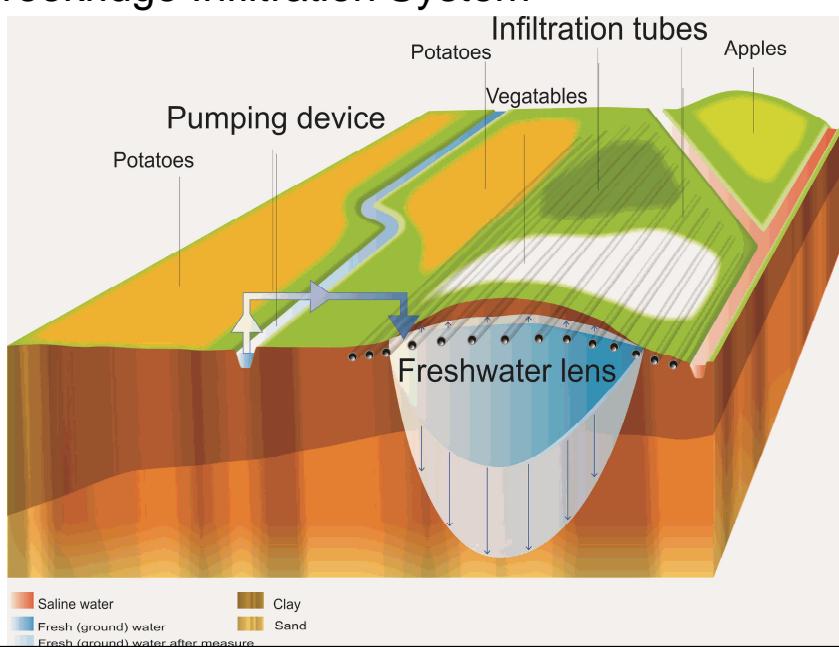


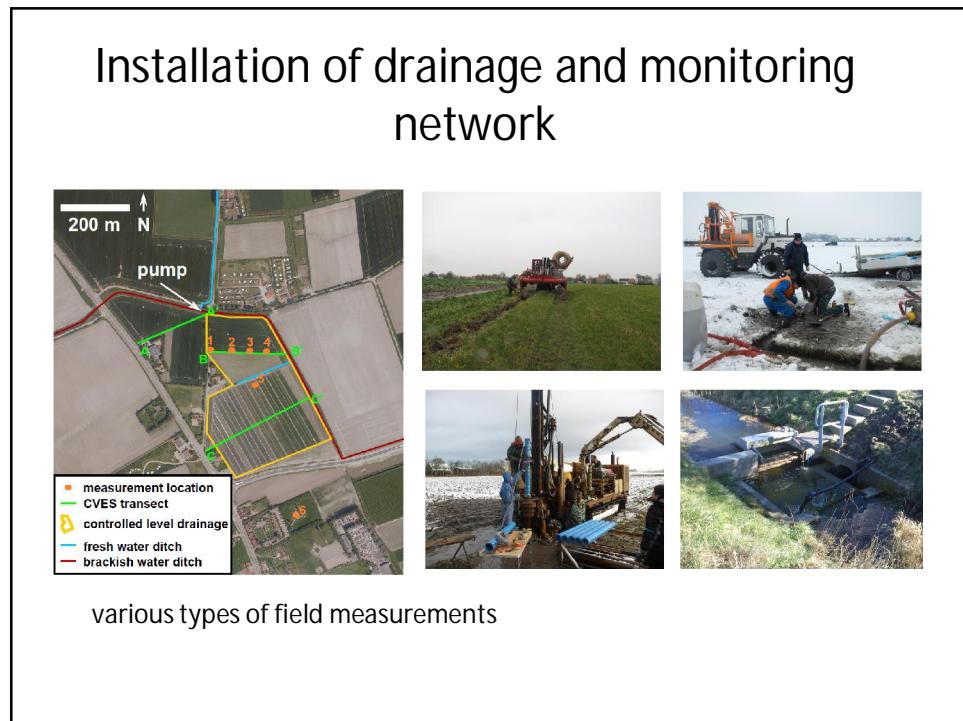
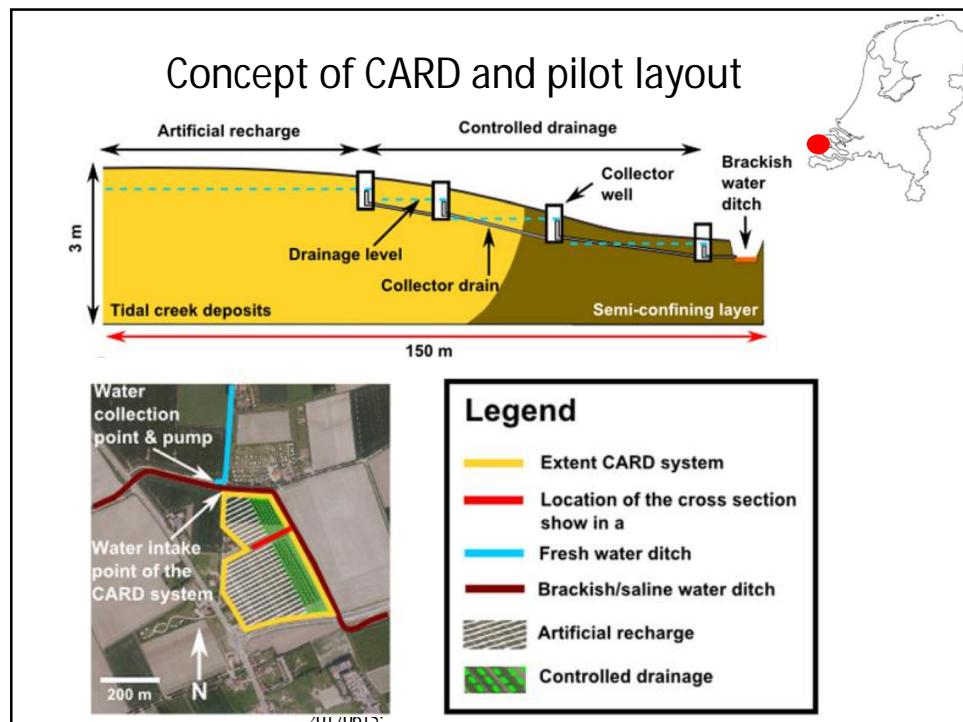
## Measure

- Controlled level drainage
- Increase groundwater level



## Creekridge Infiltration System

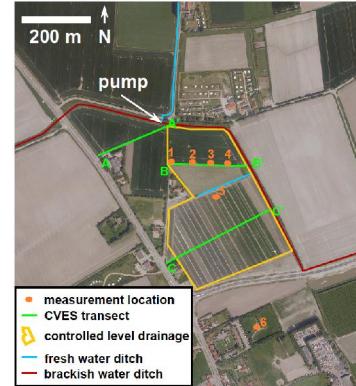




## Different types of field measurements applied

Measurement type	Purpose
Pressure transducers <sup>a</sup>	Groundwater levels
Sampling using piezometer nest	$EC_{w20}$
SLIMFLEX <sup>b</sup>	$EC_{bulk}$
CPT <sup>c</sup>	Lithology and $EC_{bulk}$
CVES <sup>d</sup>	$EC_{bulk}$
SMD <sup>e</sup>	$EC_{bulk}$

- a. Schlumberger, The Netherlands (type ' Diver ' )
- b. Deltares, The Netherlands
- c. Fugro, The Netherlands
- d. ABEM, Sweden
- e. Imageau, France

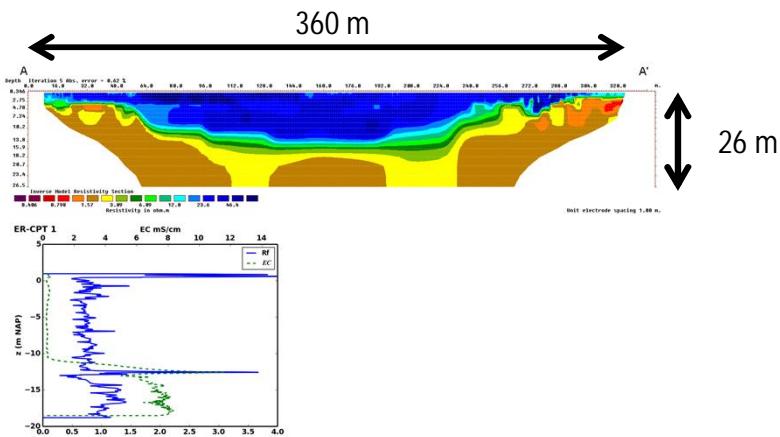


imaGéau  
INSTITUUT VOOR GEOWISSENSCHAFTEN

FUGRO

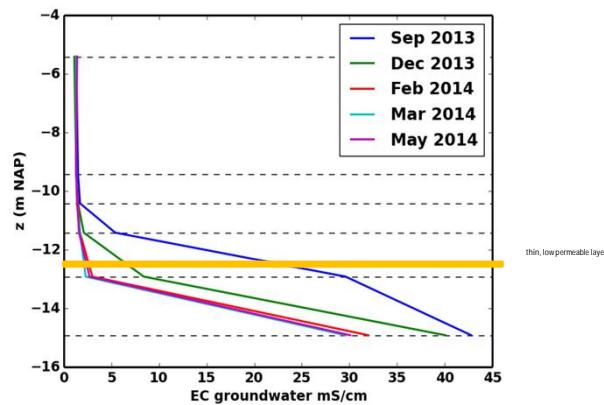
## Key field observations (1)

- Fresh groundwater up to -12 m NAP

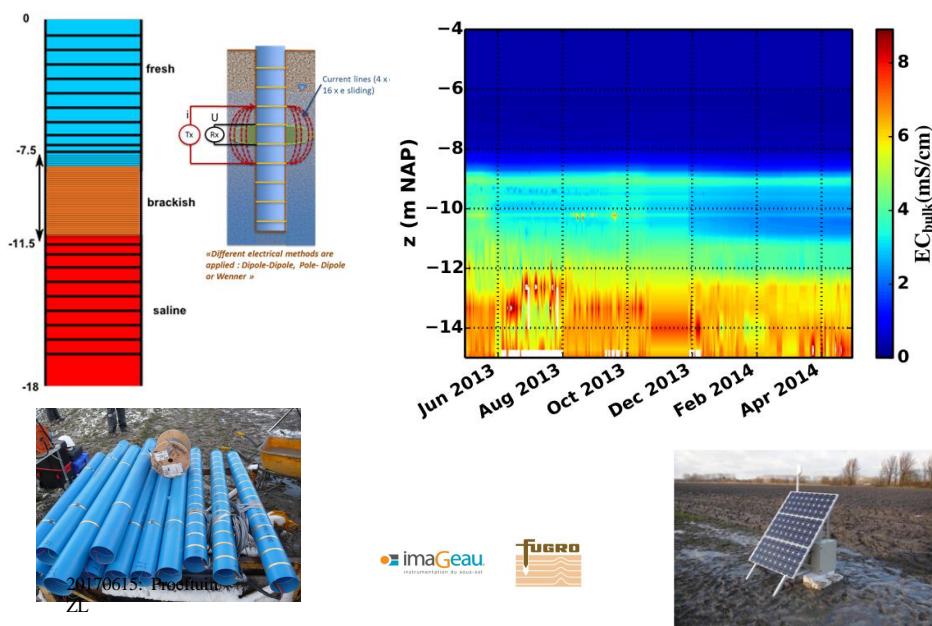


## Key field observations (2)

- Freshening up to 2m

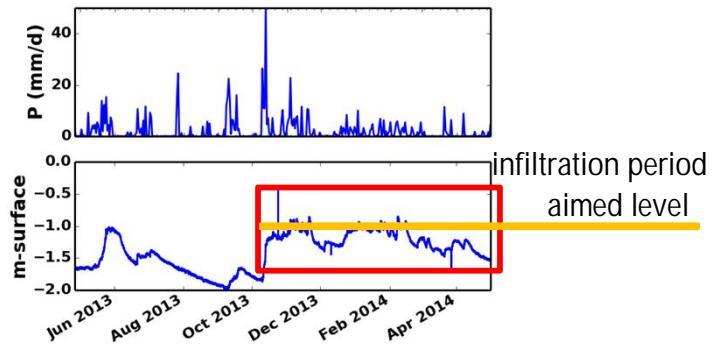


Subsurface Monitoring Device (SMD): Monitoring salinities



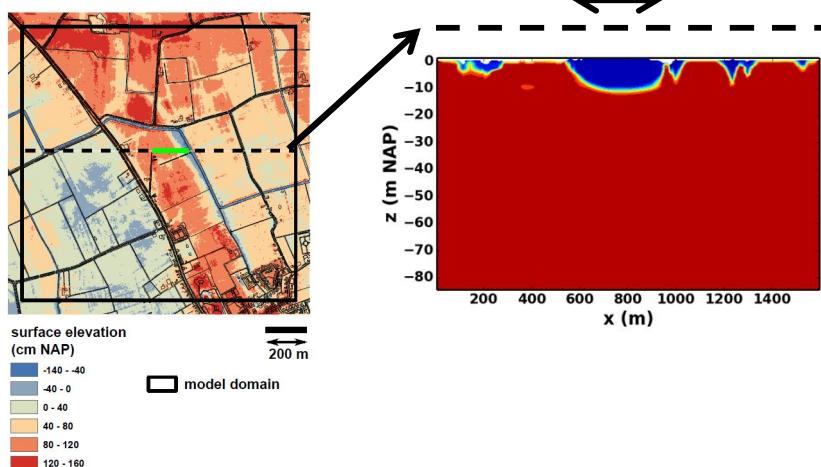
## Key field observations (3)

- Groundwater levels and precipitation

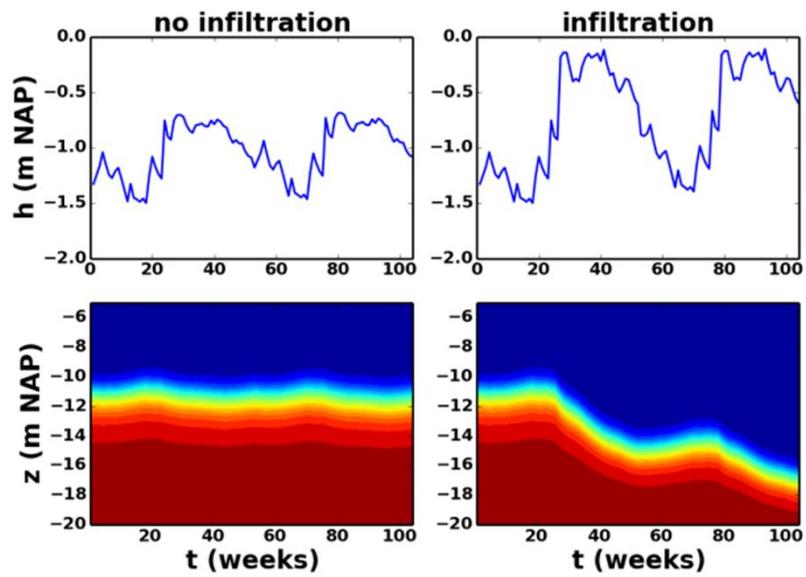


## Modeling

creek ridge

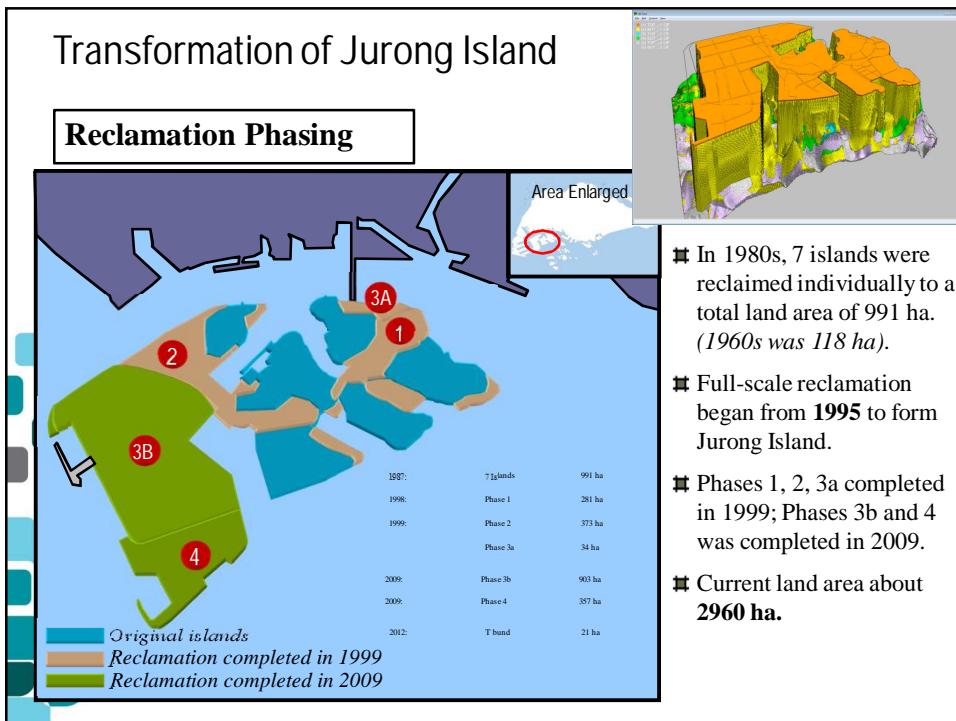
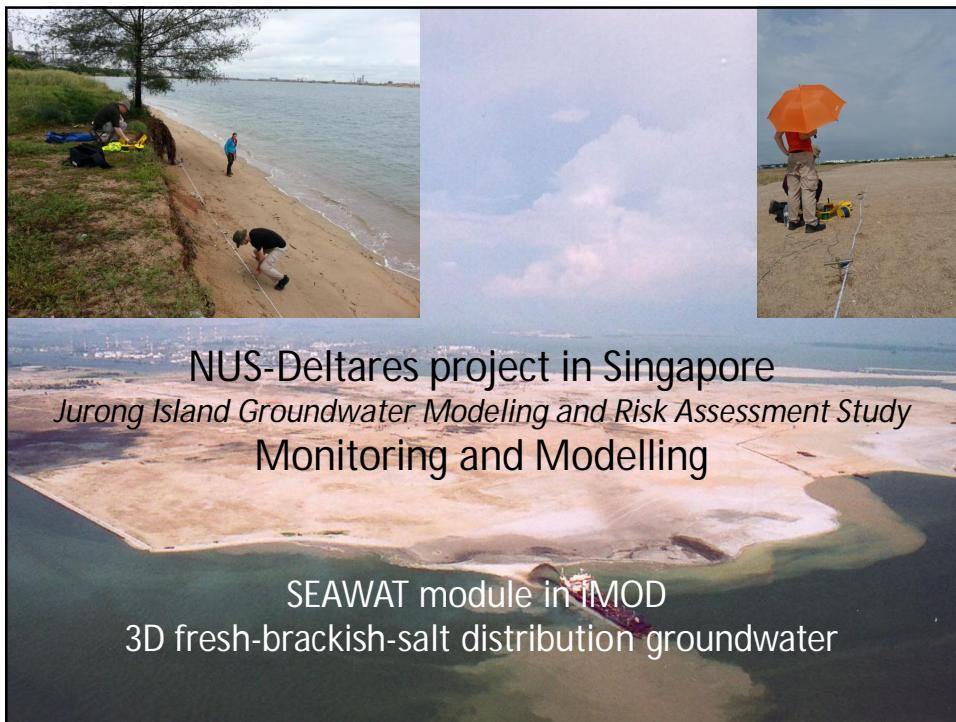


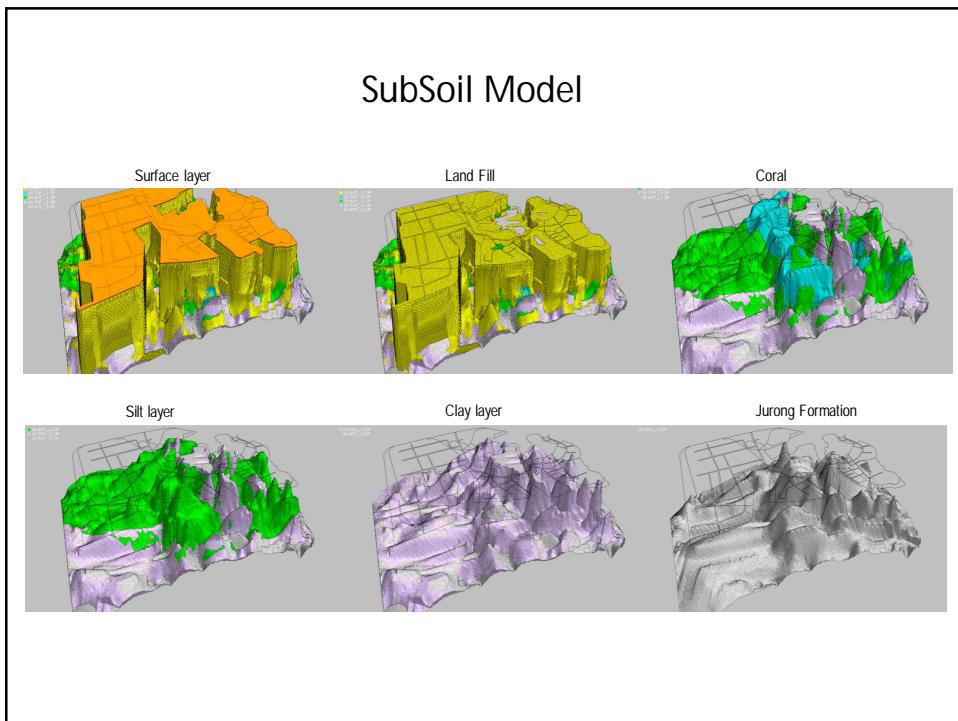
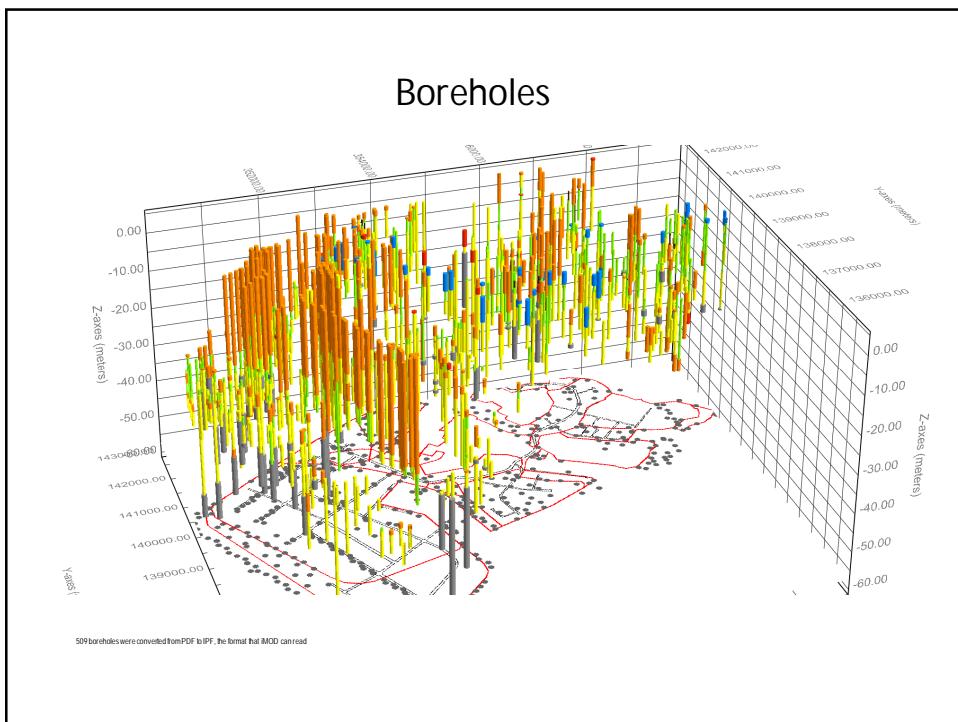
## Influence of infiltration



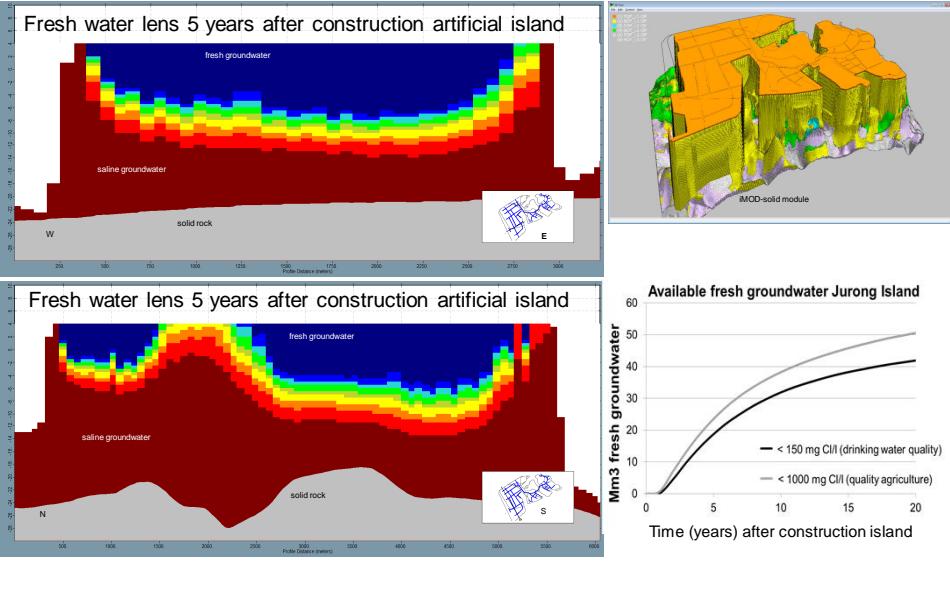
Singapore Jurong Island

Aquifer Storage and Recovery



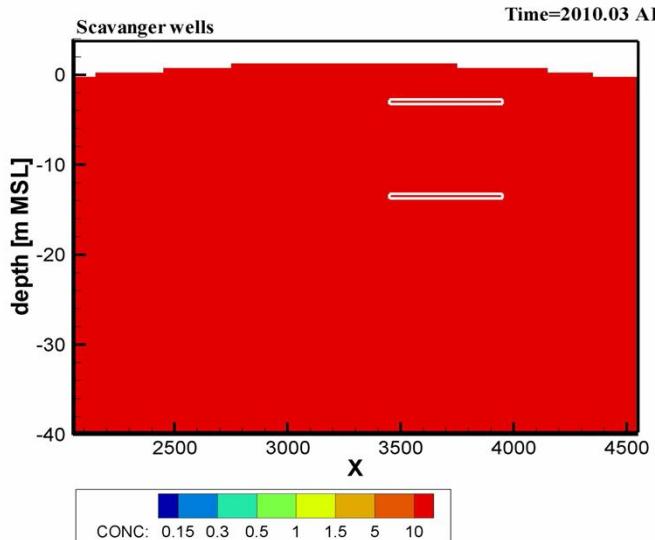


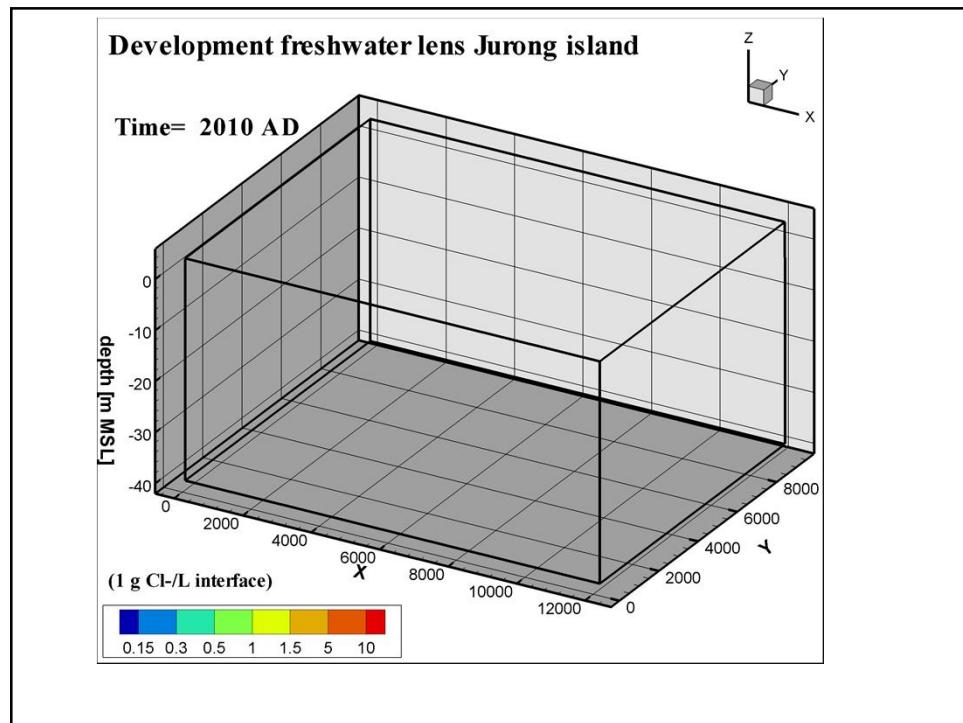
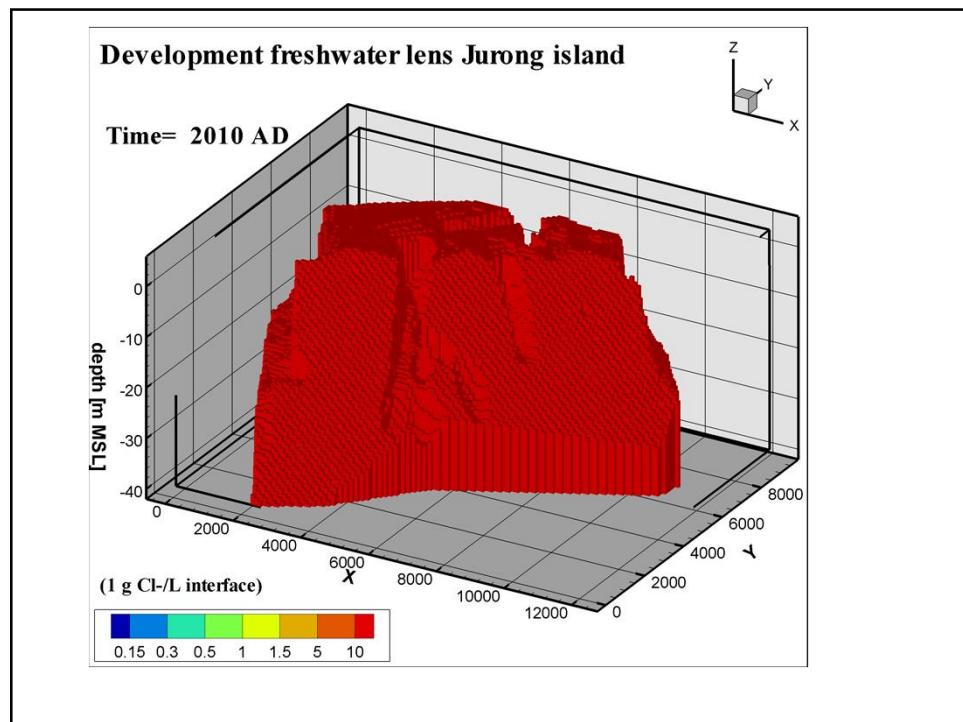
## iMOD-SEAWAT Jurong Island Singapore



## Animation scavenger wells

### Development freshwater lens: scenario 1B





Example NL:  
Salt resistant crops on salty boils



Cl-conc seepage:

(Polder Noordplas)

Diffuse : 100 mg/l

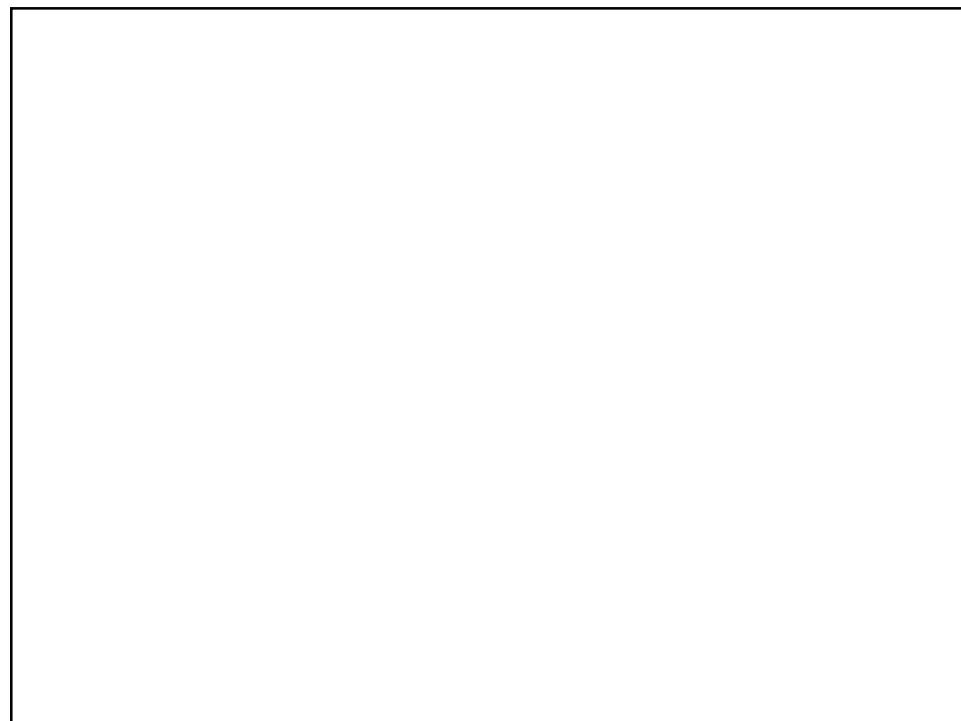
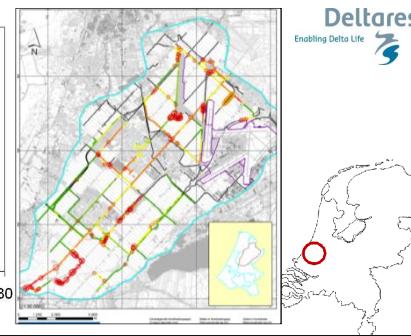
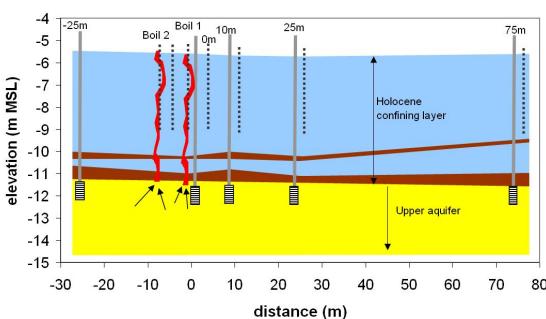
Paleochannel : 600 mg/l

Boils : 1100 mg/l

**Meijer**   
FOR SURE

Deltares

Enabling Delta Life



# Modelling

salt water intrusion  
density dependent groundwater flow

modelling

Why mathematical modelling anyway?

A model is only a schematisation of the reality!

## Why mathematical modelling anyway?

+:

- cheaper than scale models
- analysis of very complex systems is possible
- a model can be used as a database
- to increase knowledge about a system (water balances)

-:

- simplification of the reality
- only a tool, no purpose on itself
- garbage in=garbage out: (field)data important
- perfect fit measurement and simulation is suspicious

## Numerical modelling variable density flow

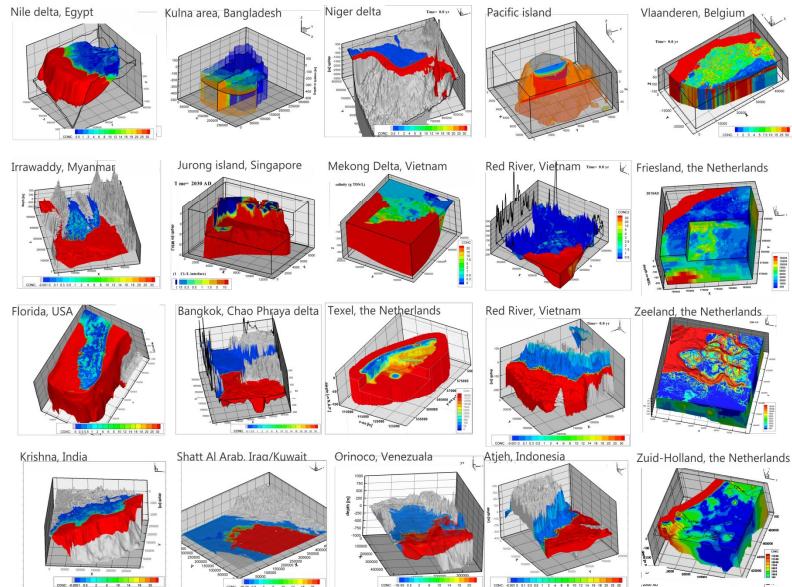
Type:

- sharp interface models
- solute transport models

State of the art:

- three-dimensional
- solute transport
- transient

## 3D numerical models groundwater coastal zone



modelling

Some existing 3D codes which simulate variable density groundwater flow in porous media:

SEAWAT (*Guo & Bennett, 98*)  
 METROPOL (*Sauter, '87*)  
 FEFLOW (*Diersch, '94*)  
 MVAEM (*Strack, '95*)  
 D3F (*Wittum et al., '98*)  
 MOCDENS3D (*Oude Essink, '98*)  
 HydroGeoSphere (*Therrien, '92*)

SWICHA (*Huyakorn et al., '87*)  
 SWIFT (*Ward, '91*)  
 FAST-C 3D (*Holzbecher, '98*)  
 MODFLOW+MT3D96 (*Gerven, '98*)  
 HST3D (*Kipp, '86*)  
 SUTRA (beta-version, *Voss, '02*)

## Restrictions 3D salt water intrusion modelling

- the data problem:
  - not enough hydrogeological data available
  - e.g. the initial density distribution
  - especially important issue in data-poor countries
- the computer problem:
  - modelling transient 3D systems: computer only good enough at high costs
- the numerical dispersion problem:
  - numerical dispersion is large in case of coarse grid

## Restrictions 3D salt water intrusion modelling now

- the data problem:
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- the computer problem:
  - modelling transient 3D systems: computer only good enough at high costs
- the numerical dispersion problem:
  - numerical dispersion is large in case of coarse grid

variable density

### Stability criteria for solute transport equation (I)

1. Neumann criterion:

$$\frac{D_{xx}\Delta t_s}{\Delta x^2} + \frac{D_{yy}\Delta t_s}{\Delta y^2} + \frac{D_{zz}\Delta t_s}{\Delta z^2} \leq 0.5$$
$$\Delta t_s \leq \frac{0.5}{\frac{D_{xx}}{\Delta x^2} + \frac{D_{yy}}{\Delta y^2} + \frac{D_{zz}}{\Delta z^2}}$$

variable density

### Stability criteria for solute transport equation (II)

2. Mixing criterion:

$$\Delta t_s \leq \frac{n_e b_{i,j,k}^k}{Q_{i,j,k}}$$

Change in concentration in element is not allowed to be larger than the difference between the present concentration in the element and the concentration in the source

variable density

### Stability criteria for solute transport equation (III)

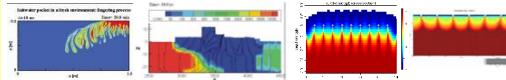
3. Courant criterion:

$$0 < \xi \leq \sim 1$$

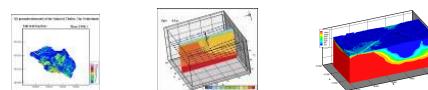
$$\Delta t_s \leq \frac{\xi \Delta x}{V_{x,\max}} \quad \Delta t_s \leq \frac{\xi \Delta y}{V_{y,\max}} \quad \Delta t_s \leq \frac{\xi \Delta z}{V_{z,\max}}$$

### Modelling fresh-salt groundwater on different scales

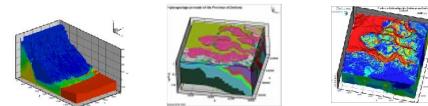
**Sub-local:** fingering, salty sand boils  
Sri Lanka (Tsunami 2004),  
Zandmotor  
**cell size=1cm-1m**



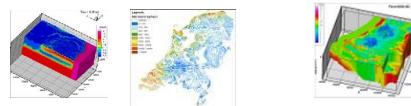
**Local:** rainwaterlenses, heat-cold  
Tholen, Schouwen-Duiveland  
**cell size=5-25m**



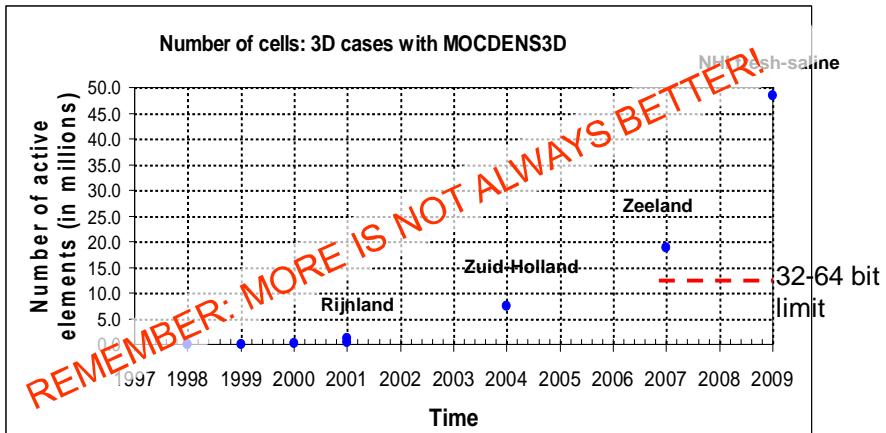
**Regional:**  
Zealand, Gujarat/India, Philippines  
**cell size=100m**



**National:** salt load  
Bangladesh, Zuid-Holland, NHI  
**cell size=250m-2km**



**Goal:**  
To take largest cell size possible to accurately model relevant salinisation processes



**DO NOT DO THIS AT HOME (IF YOU HAVE NOT ENOUGH DATA)**

## Modelling effect climate change on fresh-salt groundwater

### Modelling:

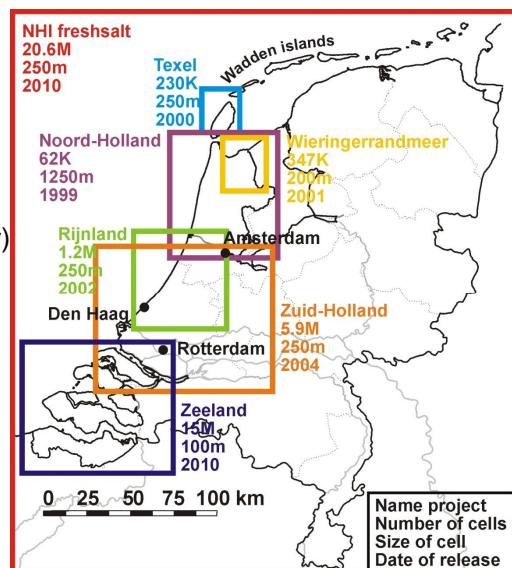
- variable-density
- 3D, non-steady
- groundwater flow
- coupled solute transport

### Code:

MOCDENS3D (MODFLOW family)  
similar to SEAWAT

### Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- land subsidence
- changing extraction rates
- adaption measures



## Fields of application of fresh-saline groundwater models

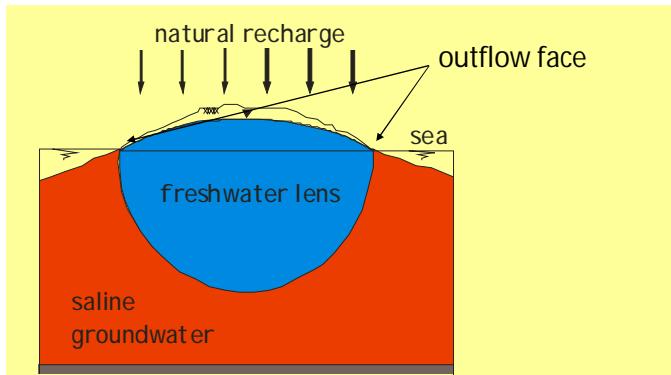
- Water system analysis in brackish-saline environments (salt loads, salt boils, freshwater lenses)
- Quantifying effects of climate change & sea level rise
- Drinking water issues: upconing saline groundwater under extraction wells
- Developing measurements to stop salinization groundwater systems (e.g. fresh keeper, coastal collectors, freshwater storage underground)
- Impact of the disasters as tsunamis on fresh groundwater resources
- Submarine Groundwater Discharge (marine water pollution, Harmful Algae)

variable density

### Difficulties with variable density groundwater flow

- Initial density distribution (effects on velocity field) !
- Velocities freshwater lens at the outflow face near the sea
- Boundary conditions (especially concentration boundaries)
- Choice of element size
- Length of flow time step to recalculate groundwater flow

Outflow face at the coast is difficult to model



Flow converges and thus velocities are very high at the outflow face

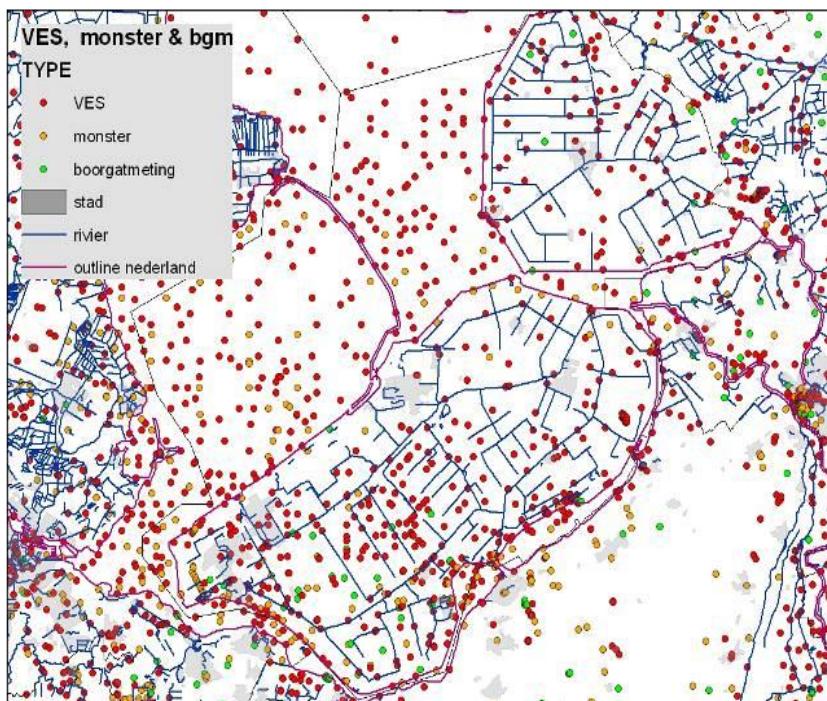
This is numerically difficult to handle

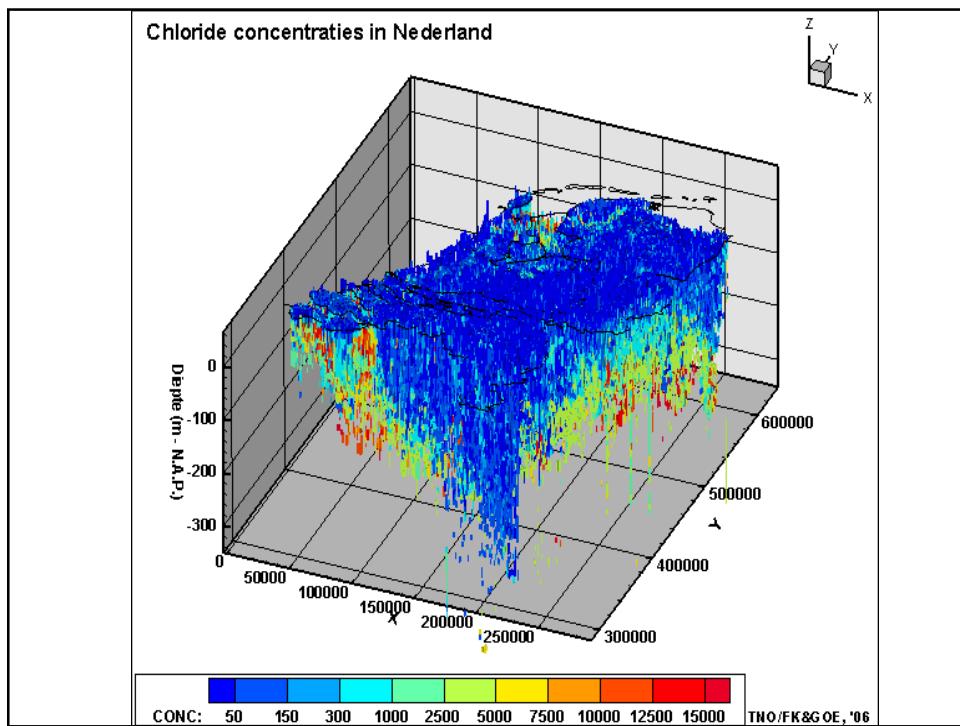
### A good initial density distribution is essential

- Because groundwater and solute transport are coupled, the density influences groundwater velocities
- Numerous density measurements are necessary to get a reliable 3D density matrix

'Procedure' to improve initial density distribution

- Implement all chloride data
  - Analyses, Borehole, VES, Airborne techniques (HEM, SkyTem)
  - Better old then nothing
  - Better VES then nothing
- Interpolate and extrapolate
  - Sea = easy (salt)
  - Inland = fresh?
- Start with simulation (10/20/30 years) with  
mol.diffusion\*1000 to smooth out artificial densities



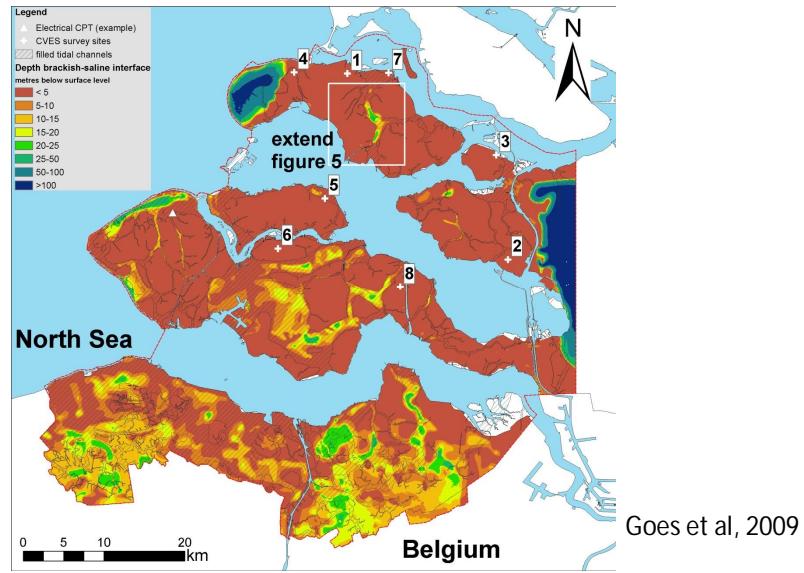


## Mapping brackish-saline interface Zeeland

Combining different types of data sources:

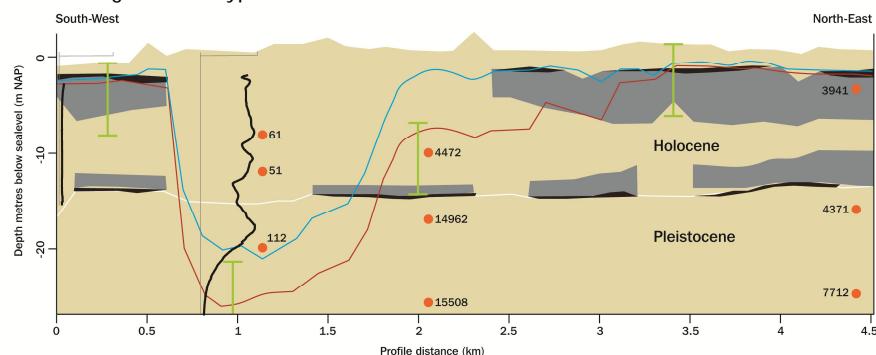
Data type	Characteristics of measurement	# Data	Determined	Accuracy depth of interfaces
Groundwater Samples	0D in situ	721	Chloride concentration	Depends on positions of screens
Geo-electrical borehole logs	1D in situ	149	1D chloride profile, Depth fresh-brackish and brackish-saline interface, Inversions.	±1 m
Electrical CPT	1D in situ (max. depth 50 m)	71	Borehole log	±1 m
VES	1D from surface	1113	Depth brackish-saline interface, Major inversions, (1D chloride profile).	±20% of depth
EM34	1D from surface	3251	Depth brackish-saline interface	ranges of 7.5, 15 or 30 m (accuracy decreases with depth)
Groundwater Abstractions	0D in situ	716	Depth brackish-saline interface	a range depending on screen depth
<b>Unique locations</b>		<b>6021</b>		

## Mapping brackish-saline interface



## Mapping brackish-saline interface

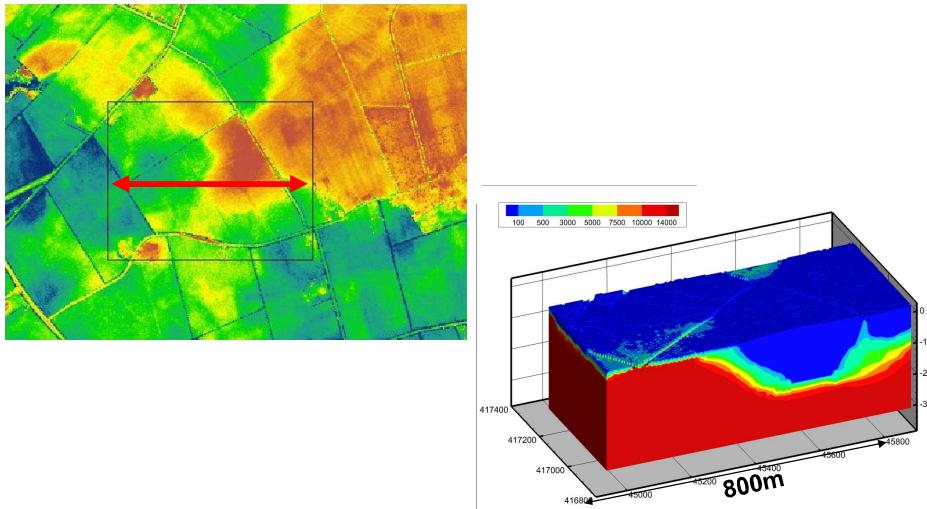
Combining different types of data sources



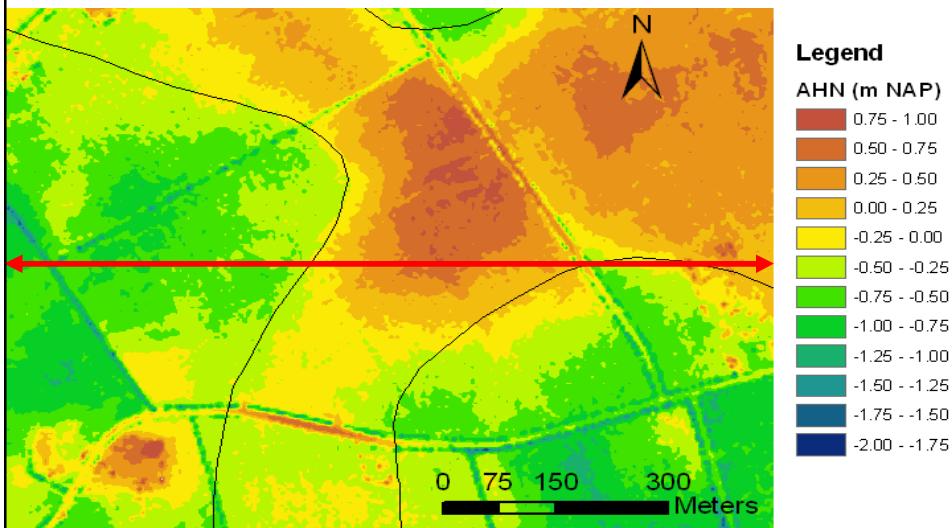
## Use variable-density groundwater flow modelling

### Why a model?

- variation in ground surface directly affects fresh-saline distribution



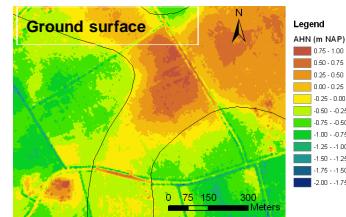
## Use variable-density groundwater flow modelling



## Local 3D model of the agricultural plot

### Modelling:

- variable-density
- 3D, non-steady
- groundwater flow & coupled solute transport
- model cell size:  $5 \times 5 \text{ m}^2$

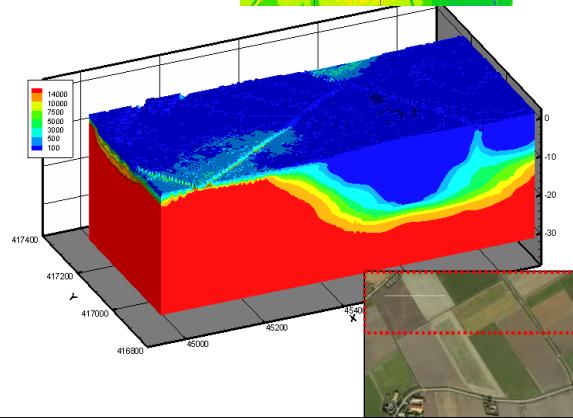


### Code:

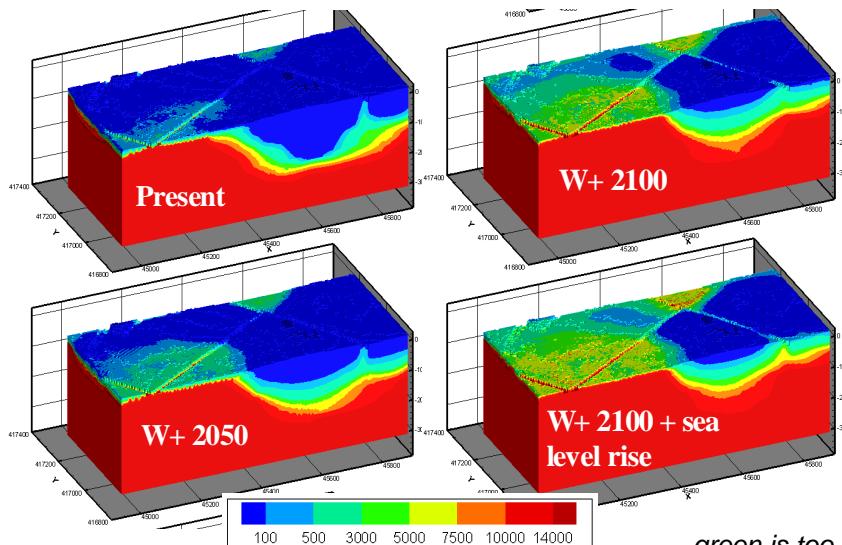
MOCDENS3D

### Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- (adaption measures)



## Local approach: simulated Cl-conc. with different CC-scenarios

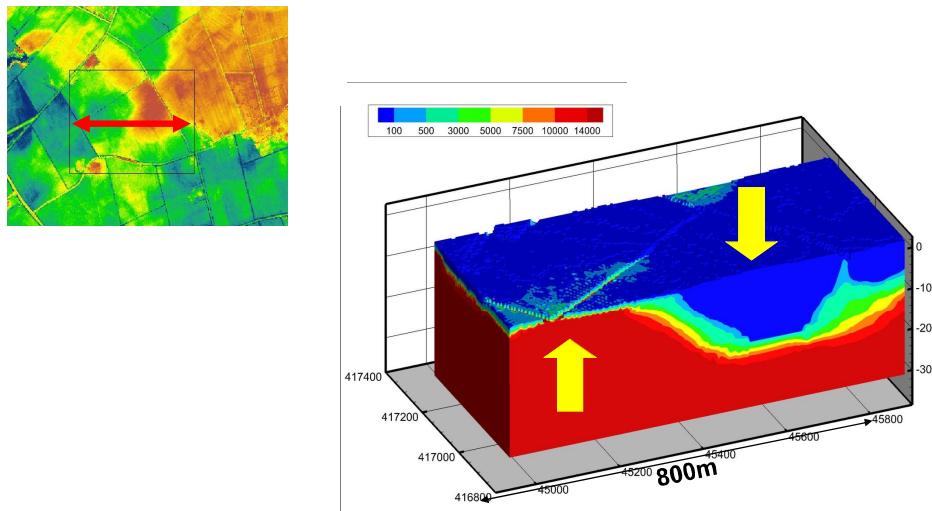


*green is too salty  
to grow fresh crops*

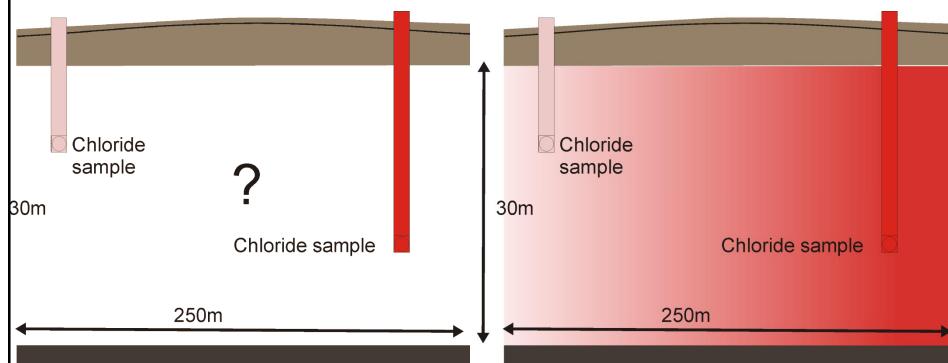
## Use variable-density groundwater flow modelling

### Why a model?

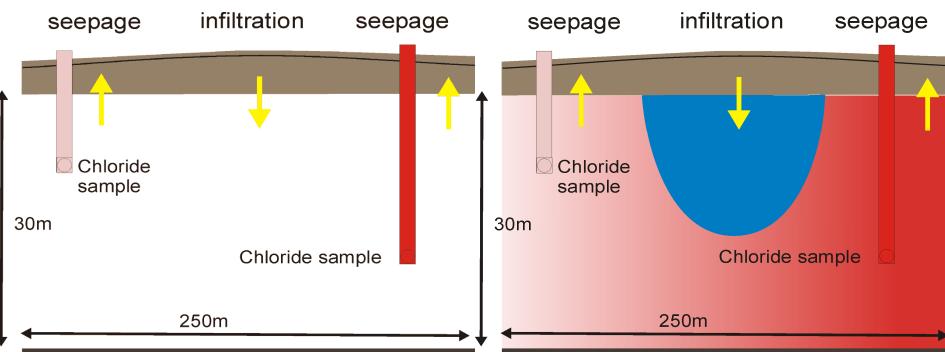
- variation in ground surface directly affects fresh-saline distribution



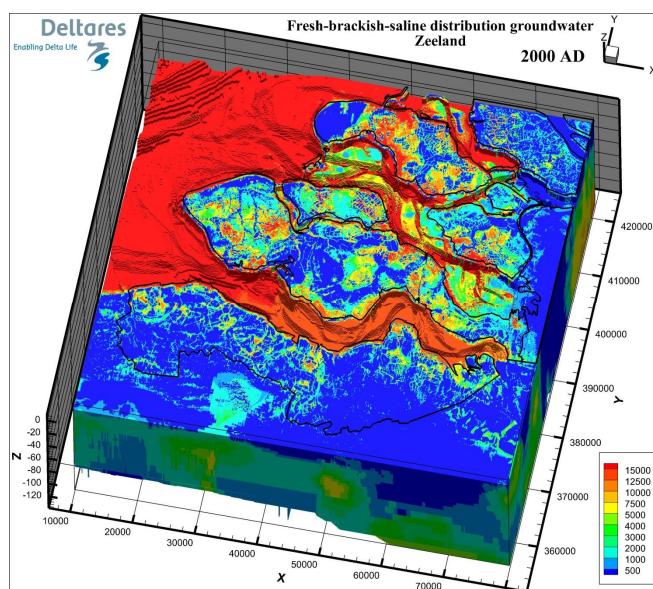
### Interpolation chloride



## Using flow model for better interpolate chloride

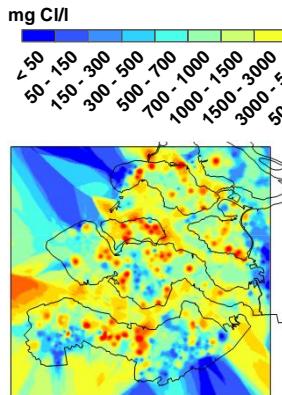


## 3D fresh-saline groundwater distribution



# Regional groundwater model:

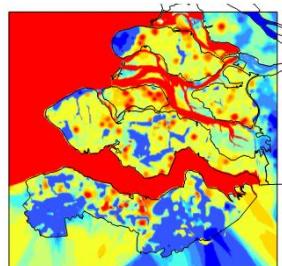
From chloride measurements to a 3D distribution



## Step 1: interpolating data:

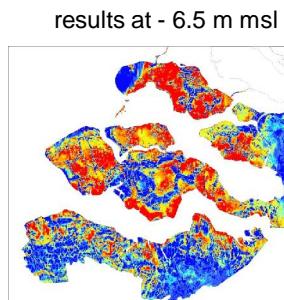
- Groundwater samples
- Geo-electrical borehole logs
- (C)VES, EM, electrical CPT

EWRMP 201511



## Step 2: including interfaces

- Mapped fresh-brackish
- Mapped brackish-salt



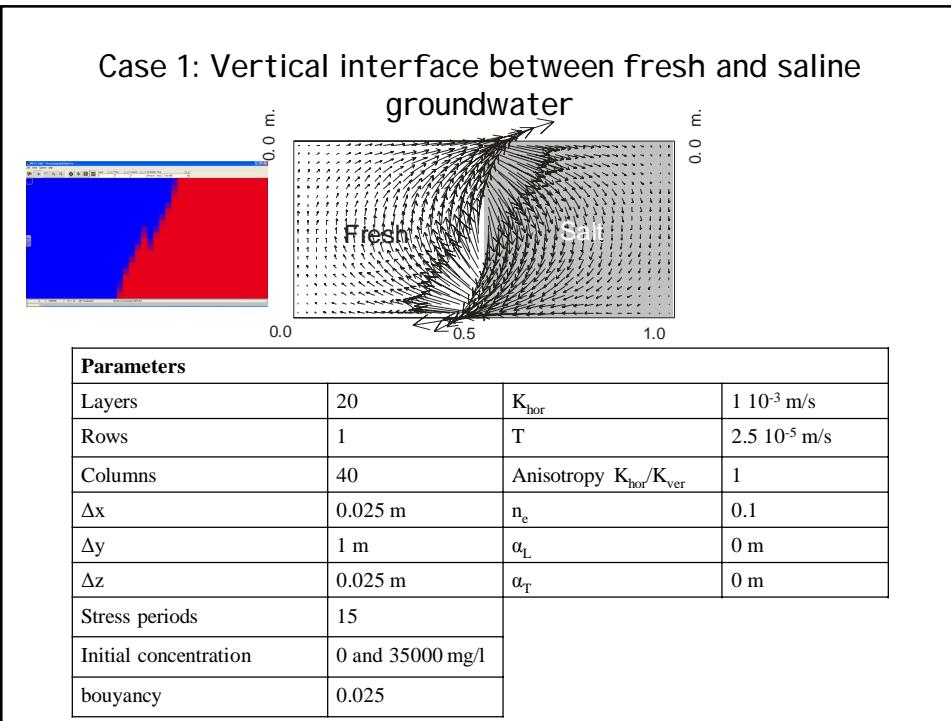
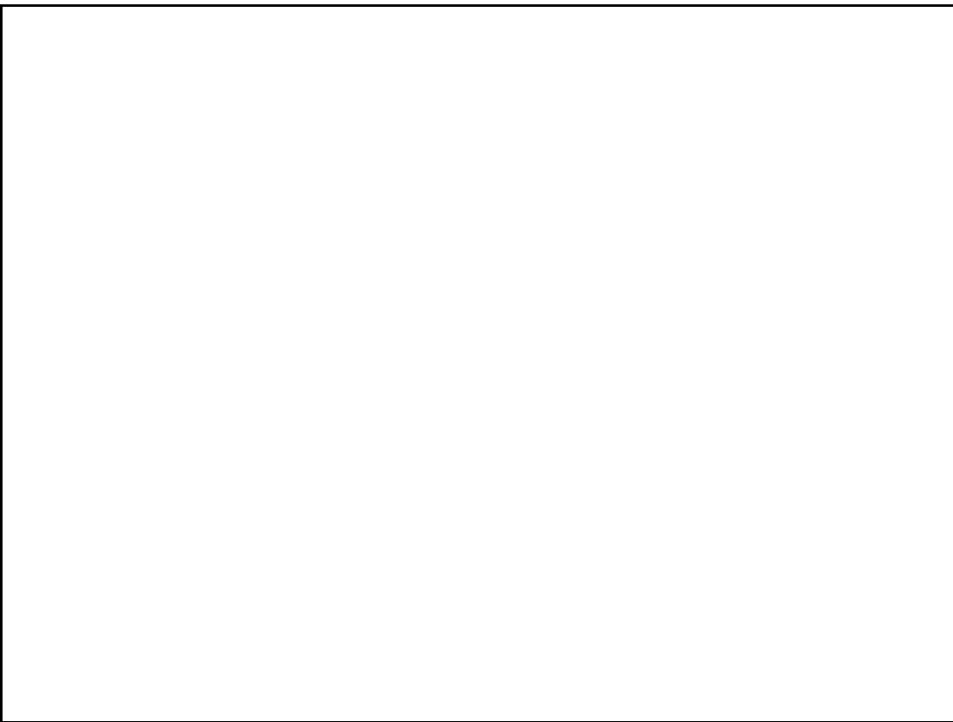
## Step 3: model result 2010:

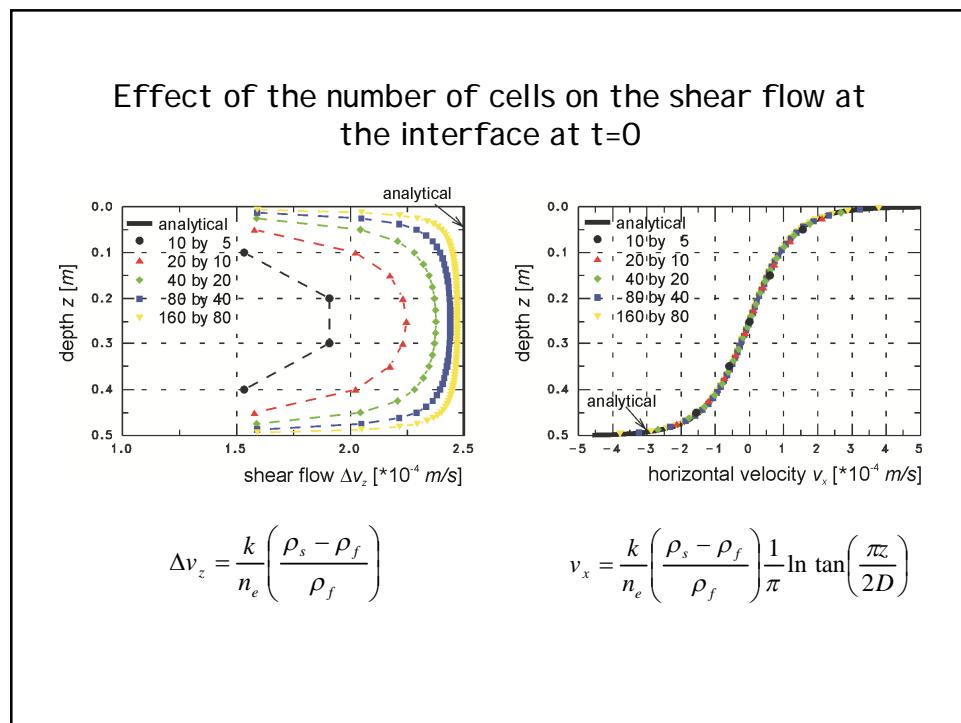
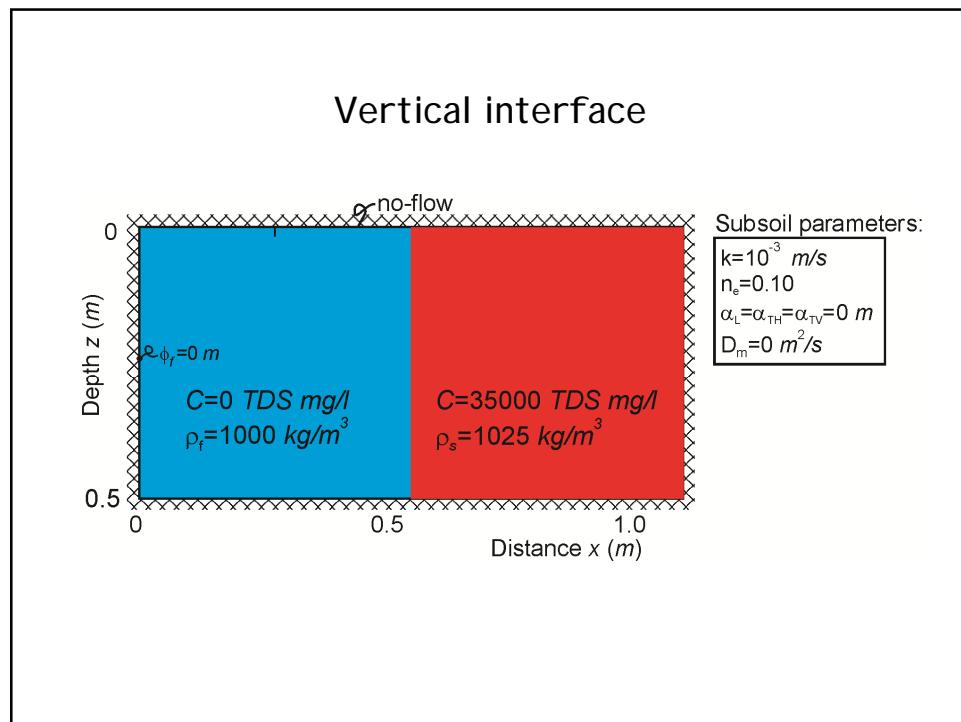
- Model as interpolator

modelling

## Examples of variable-density groundwater flow

- Rotating immiscible interface
- Henry's problem
- Evolution freshwater lens
- Hydrocoin
- Salt water pocket
- Broad 14 Basin, North Sea
- Heat transport: Elder and Rayleigh=4000
- 5 Dutch 3D cases
- Freshwater lenses
- Effect of Tsunami on groundwater resources



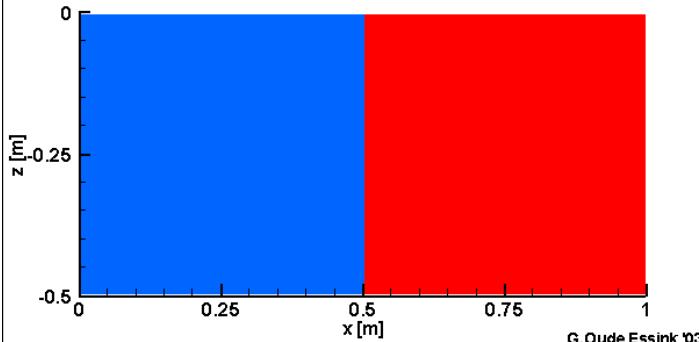


### Vertical interface

Fresh-saline vertical interface

160\*80 cells

Time= 0 min

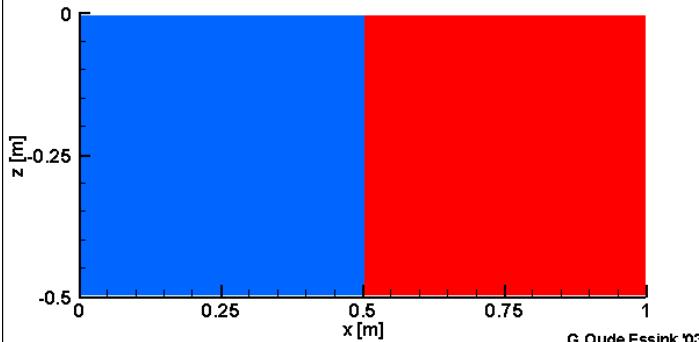


### Vertical interface

Fresh-saline vertical interface

160\*80 cells

Time= 0 min

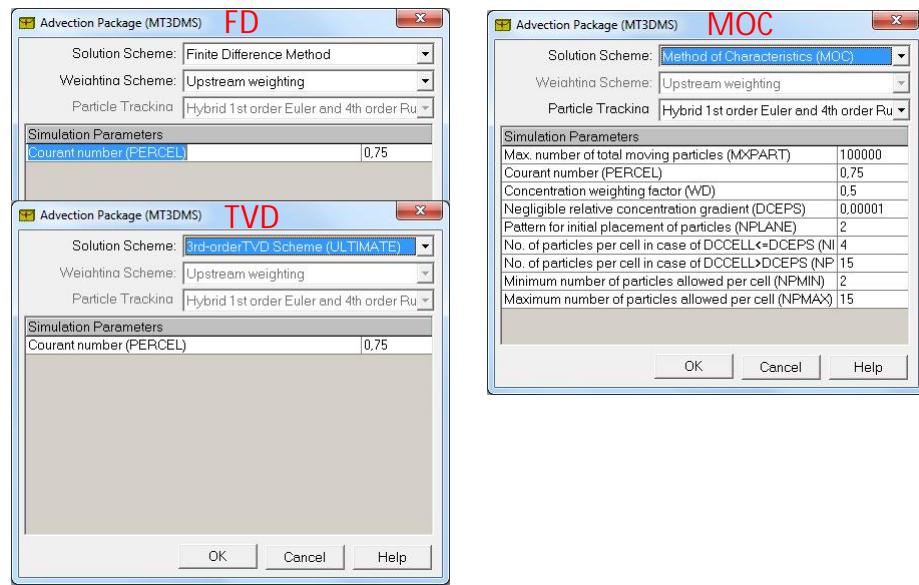


# The effect of numerical solvers on the salt transport

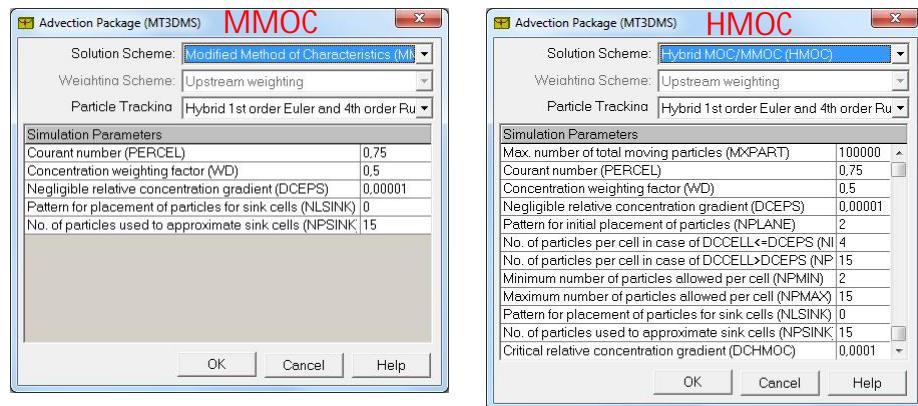
## Examples

EWRMP 201511

### Default parameters solvers



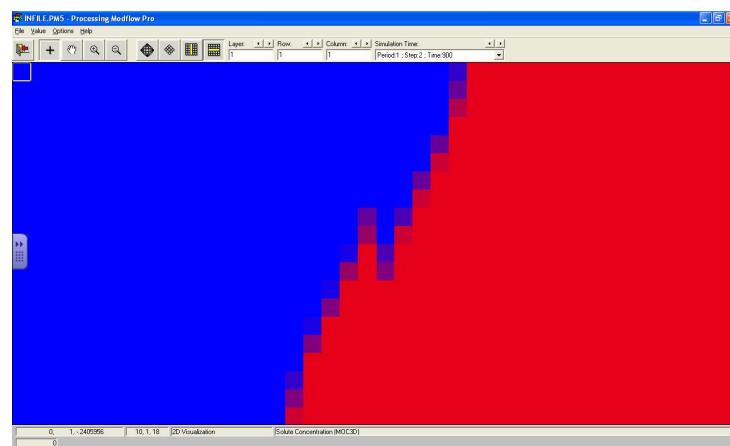
## Default parameters solvers



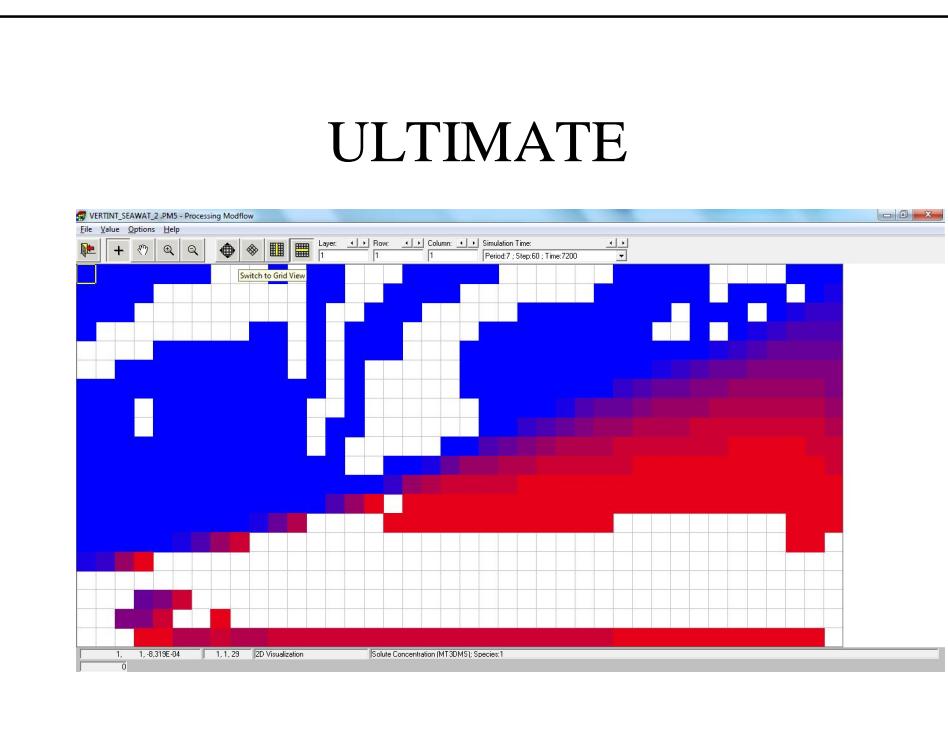
More information:

Zheng, C., & Wang, P. (1999). MT3DMS: A modular three-dimensional multispecies transport model for simulation of advection, dispersion, and chemical reactions of contaminants in groundwater systems. Technical report, Waterways Experiment Station, US Army Corps of Engineers.

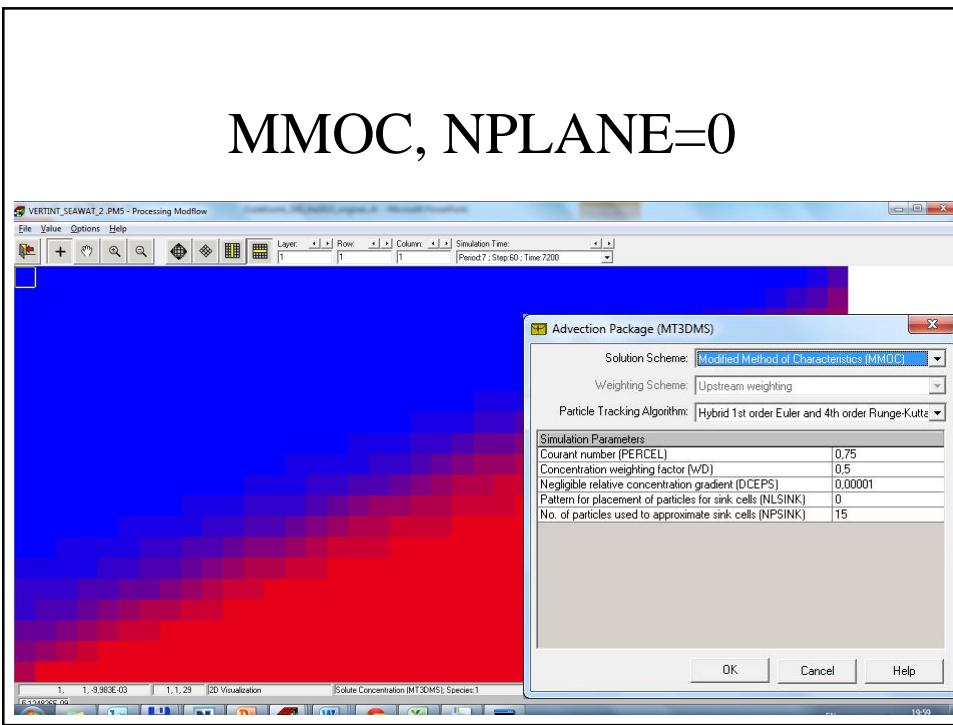
1 particle per cell



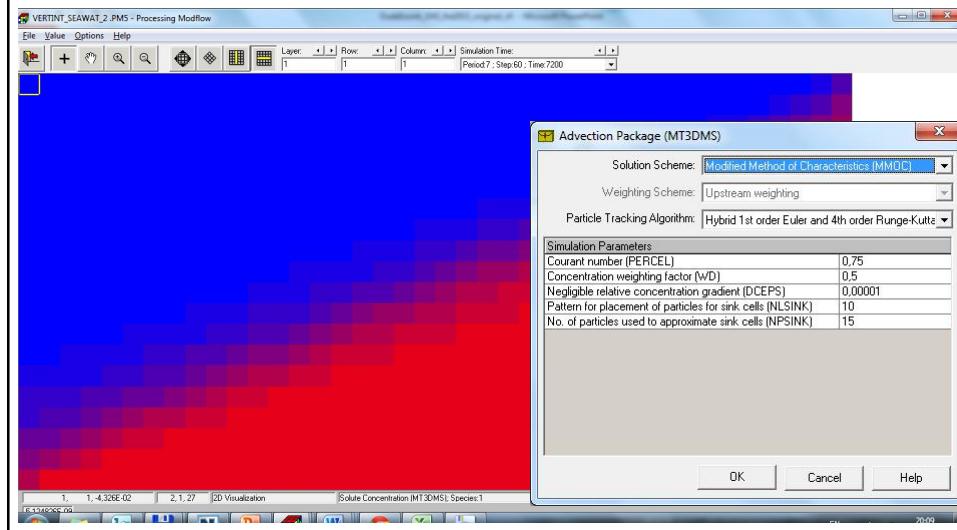
# ULTIMATE



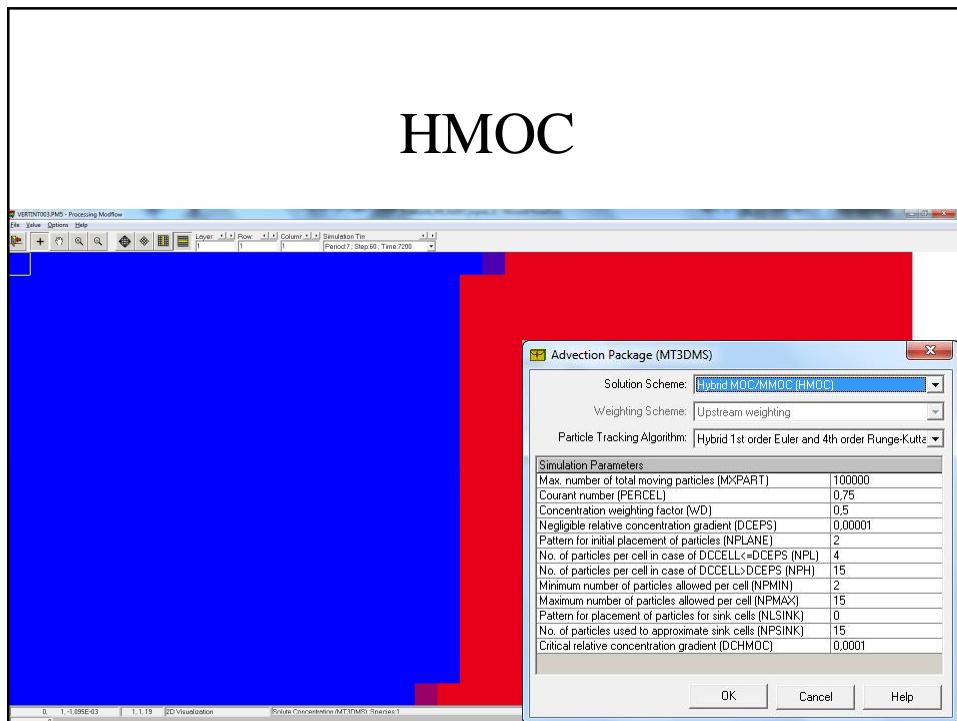
# MMOC, NPLANE=0



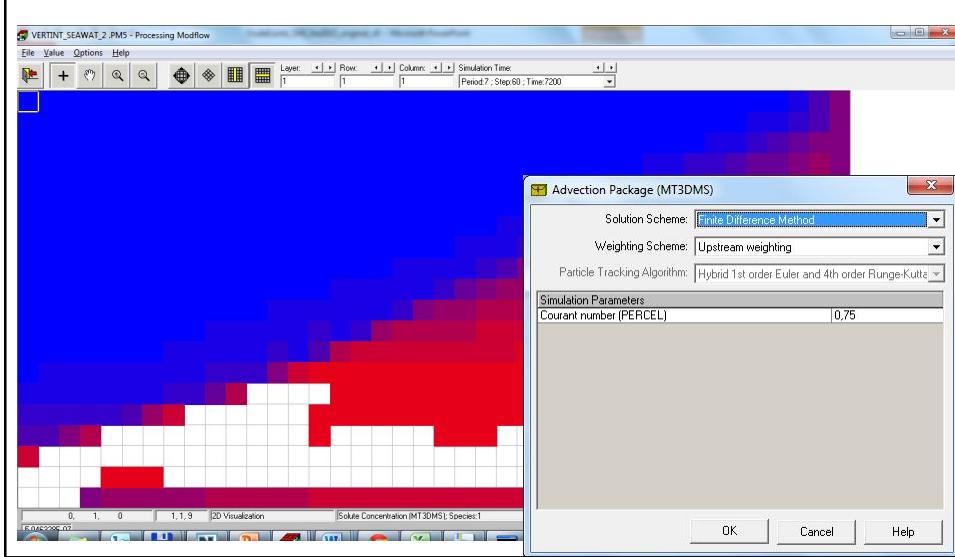
## MMOC, NPLANE=10



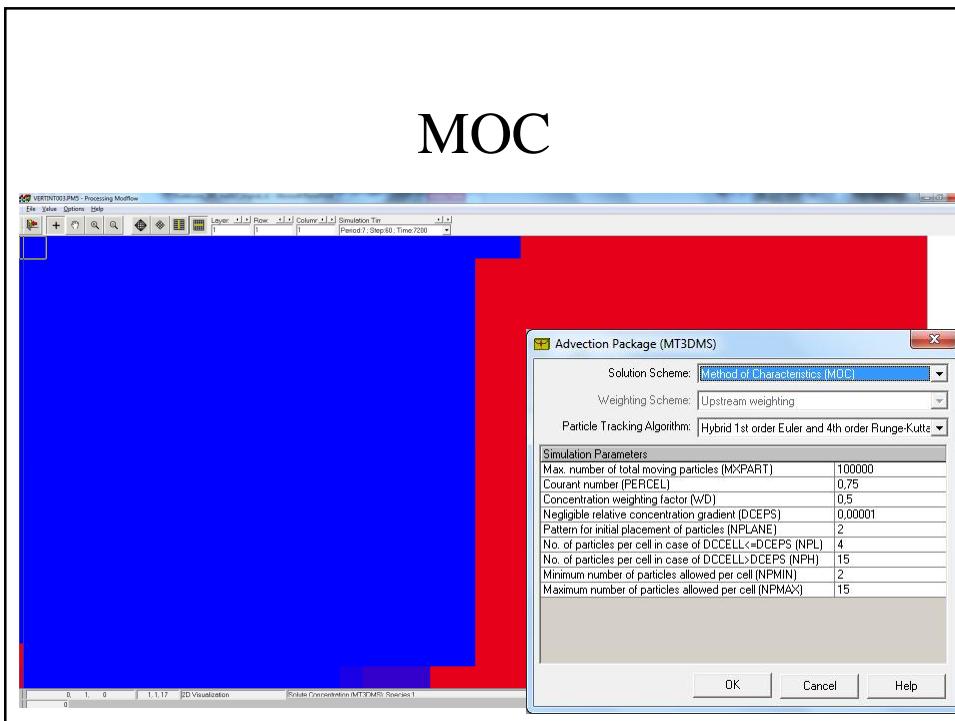
## HMOC



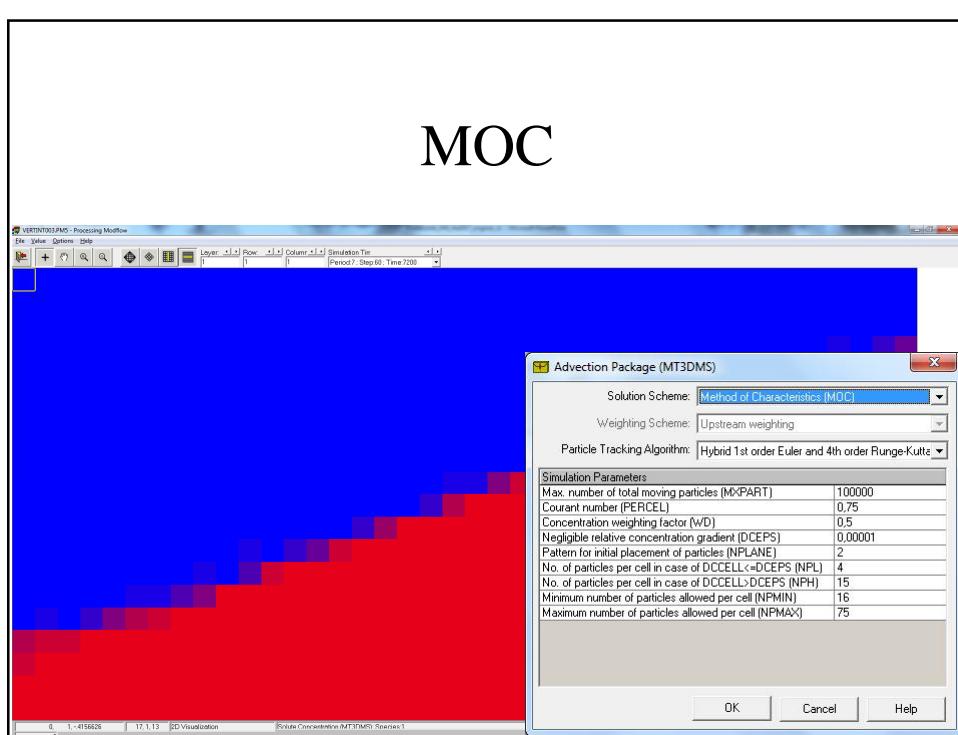
# Finite Difference Method



# MOC

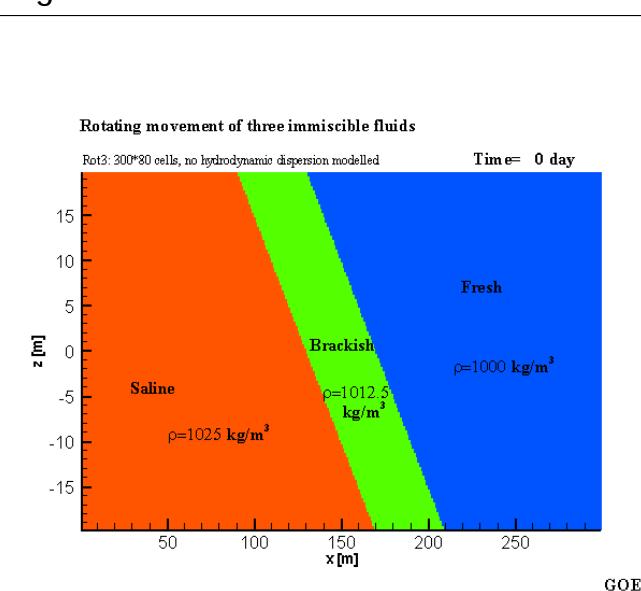


# MOC



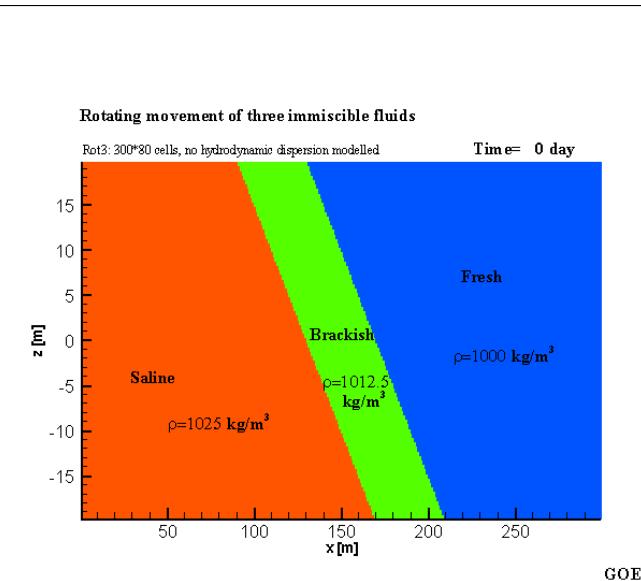
cases

## Rotating immiscible interfaces



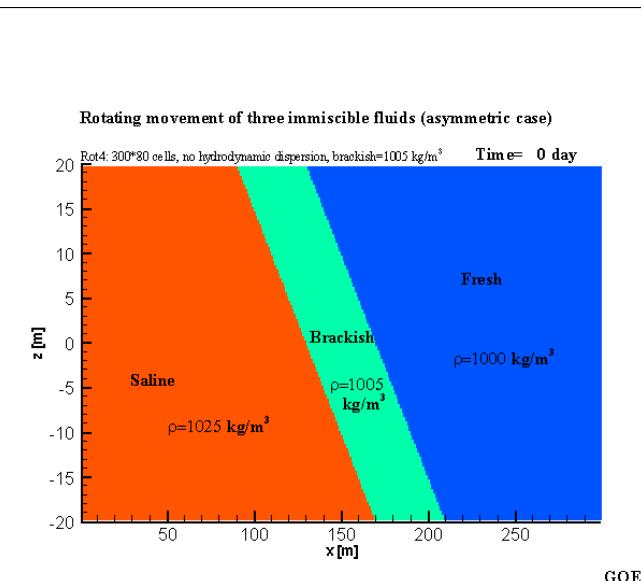
cases

## Rotating immiscible interfaces



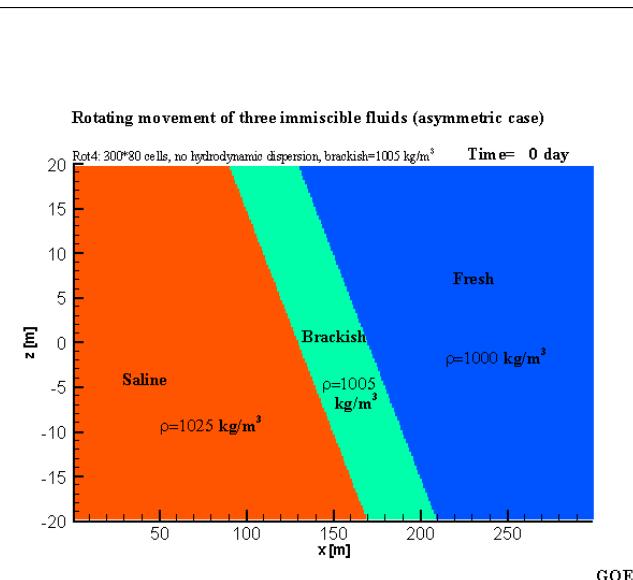
cases

## Rotating immiscible interfaces (asymmetric)



cases

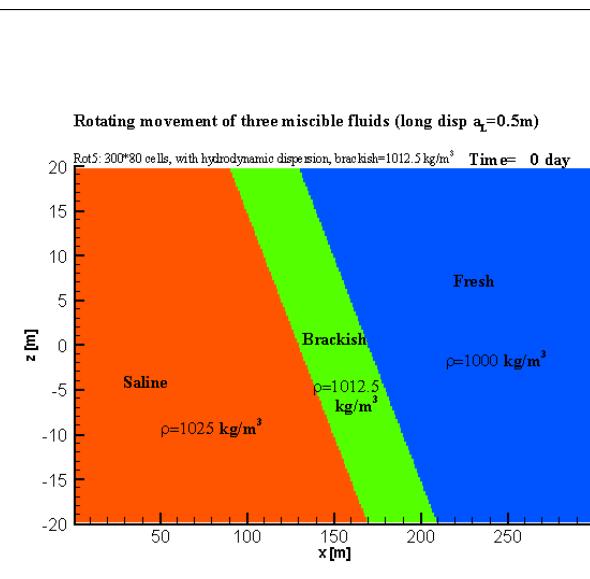
## Rotating immiscible interfaces (asymmetric)



Bakker, M., Oude Essink, G.H.P. & Langevin, C. 2004. The rotating movement of three immiscible fluids. J. of Hydrology 287, 270-278

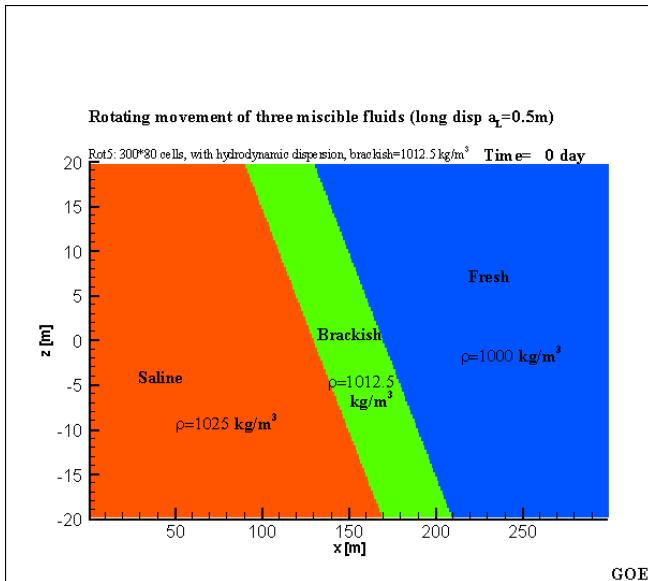
cases

## Rotating interfaces with dispersion $\alpha_L=0.5\text{m}$



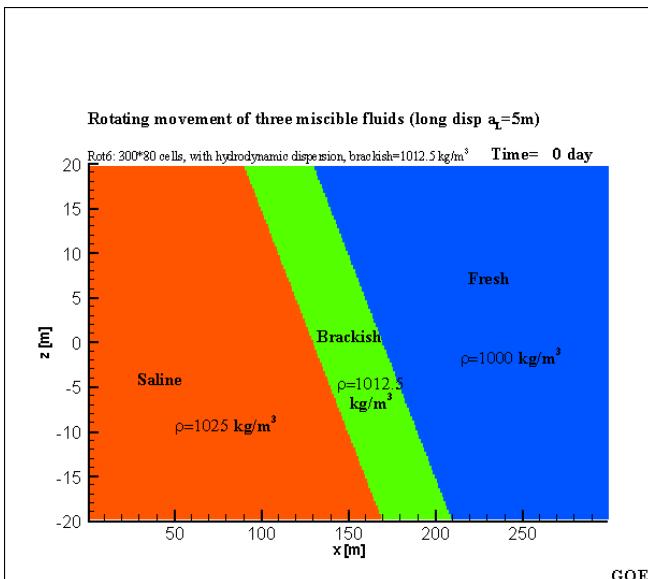
cases

### Rotating interfaces with dispersion $\alpha_L=0.5m$



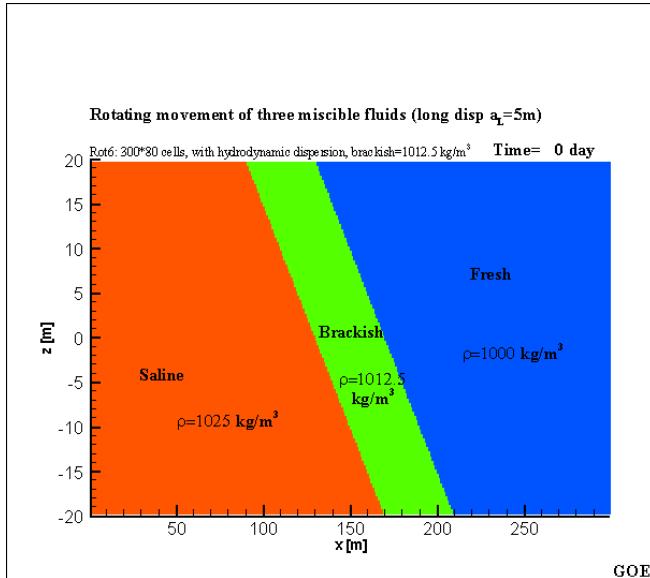
cases

### Rotating interfaces with dispersion $\alpha_L=5m$



cases

## Rotating interfaces with dispersion $\alpha_L=5m$



cases

## Rotating immiscible interfaces

### Conclusion:

To check the variable-density component of your code,  
this immiscible interface benchmark can be used.

Salt water pocket in a fresh environment

Grid convergence

Time step

Salt water pocket in a fresh environment (I)

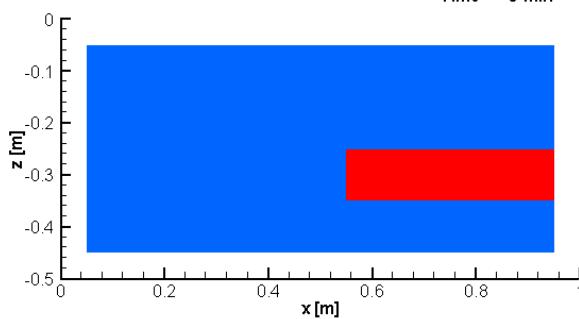
Effect of discretisation on a 'salt lake problem'

cases

**Saline pocket in fresh groundwater: fingering process**

**10\*5 cells**

Time= 0 min



cases

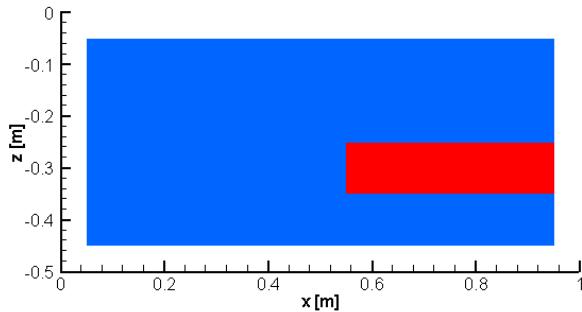
## Salt water pocket in a fresh environment (I)

Effect of discretisation on a 'salt lake problem'

Saline pocket in fresh groundwater: fingering process

10\*5 cells

Time= 0 min



cases

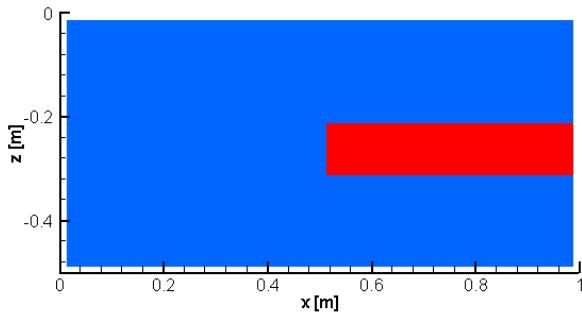
## Salt water pocket in a fresh environment (II)

Effect of discretisation

Saline pocket in fresh groundwater: fingering process

40\*20 cells

Time= 0 min



cases

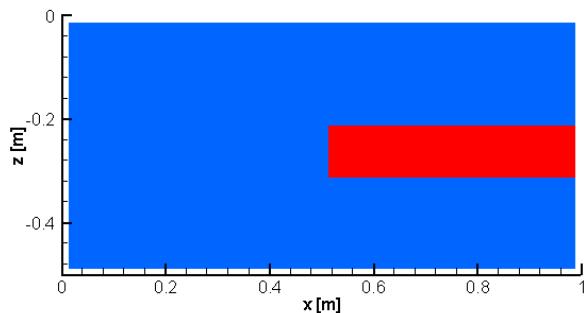
## Salt water pocket in a fresh environment (II)

Effect of discretisation

Saline pocket in fresh groundwater: fingering process

40\*20 cells

Time= 0 min



cases

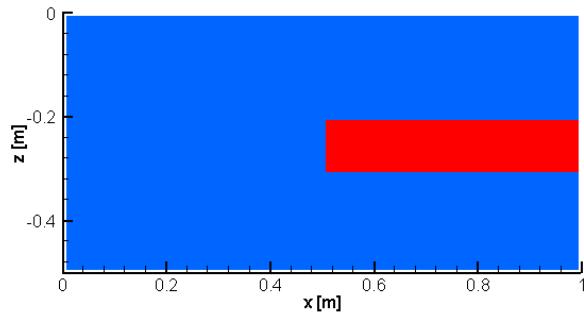
## Salt water pocket in a fresh environment (III)

Effect of discretisation

Saline pocket in fresh groundwater: fingering process

80\*40 cells

Time= 0 min



cases

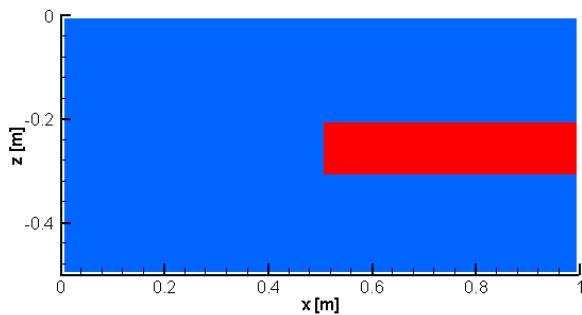
### Salt water pocket in a fresh environment (III)

Effect of discretisation

Saline pocket in fresh groundwater: fingering process

80\*40 cells

Time= 0 min



cases

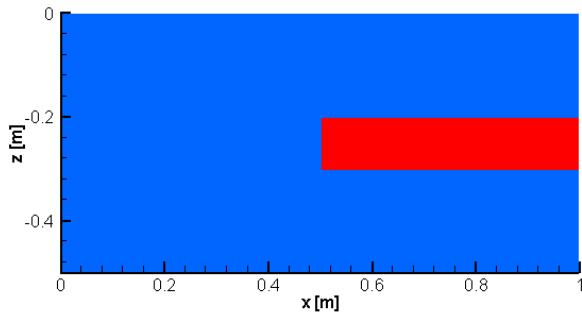
### Salt water pocket in a fresh environment (IV)

Effect of discretisation

Saline pocket in fresh groundwater: fingering process

320\*160 cells

Time= 0 min



cases

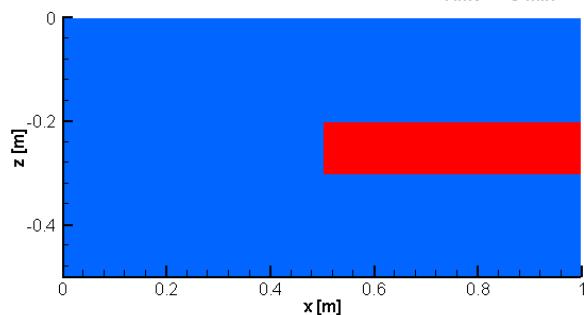
## Salt water pocket in a fresh environment (IV)

Effect of discretisation

Saline pocket in fresh groundwater: fingering process

320\*160 cells

Time= 0 min



cases

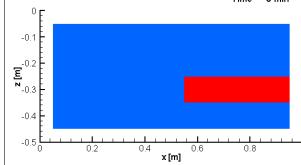
## Salt water pocket in a fresh environment (V)

Effect of discretisation

Saline pocket in fresh groundwater: fingering process

10\*5 cells

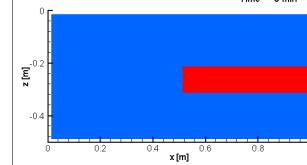
Time= 0 min



Saline pocket in fresh groundwater: fingering process

40\*20 cells

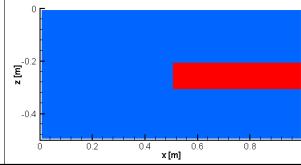
Time= 0 min



Saline pocket in fresh groundwater: fingering process

80\*40 cells

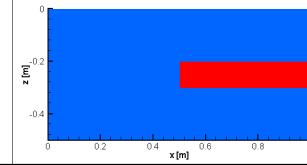
Time= 0 min



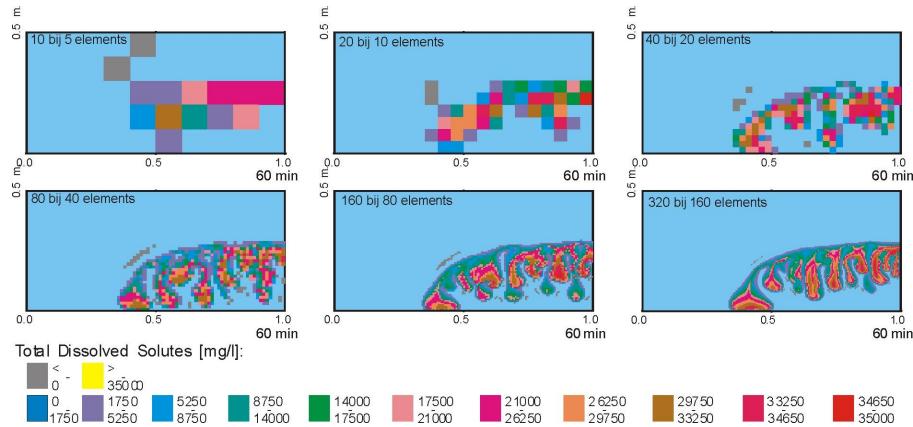
Saline pocket in fresh groundwater: fingering process

320\*160 cells

Time= 0 min

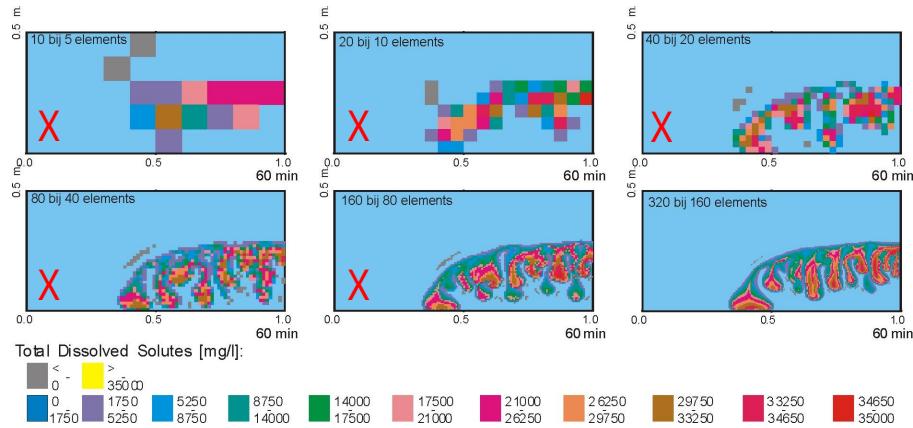


### Effect of size model cell on physical process

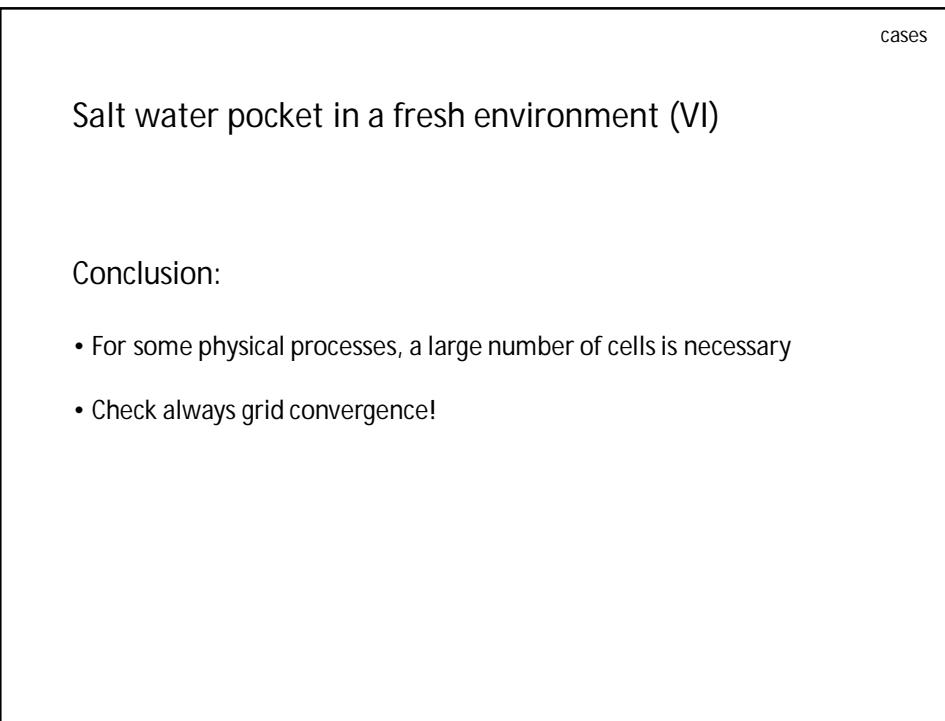
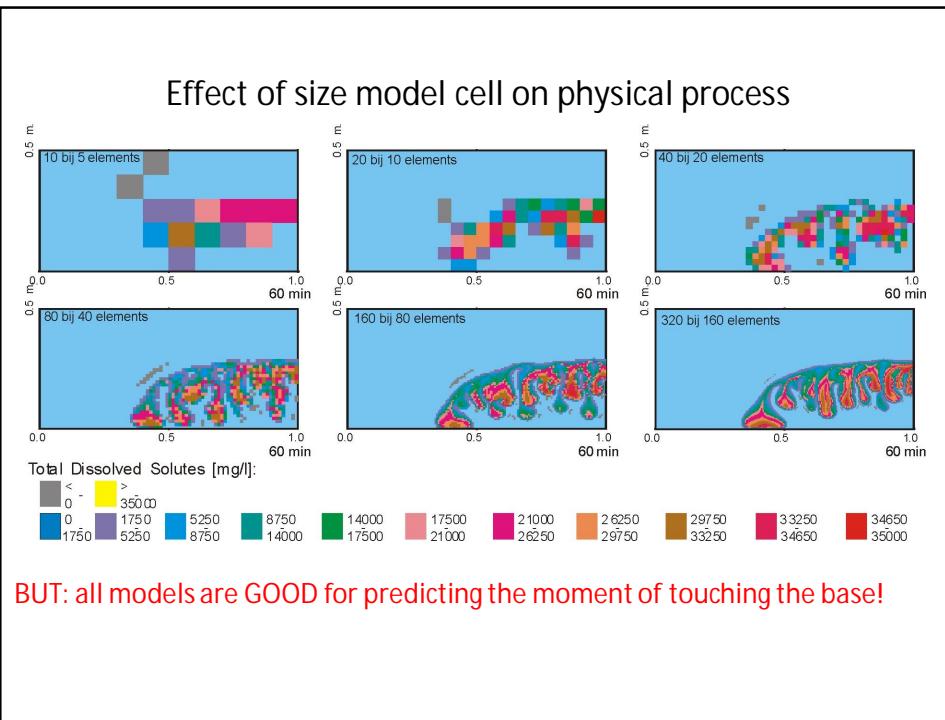


Size of cell has a large effect on modelling result!

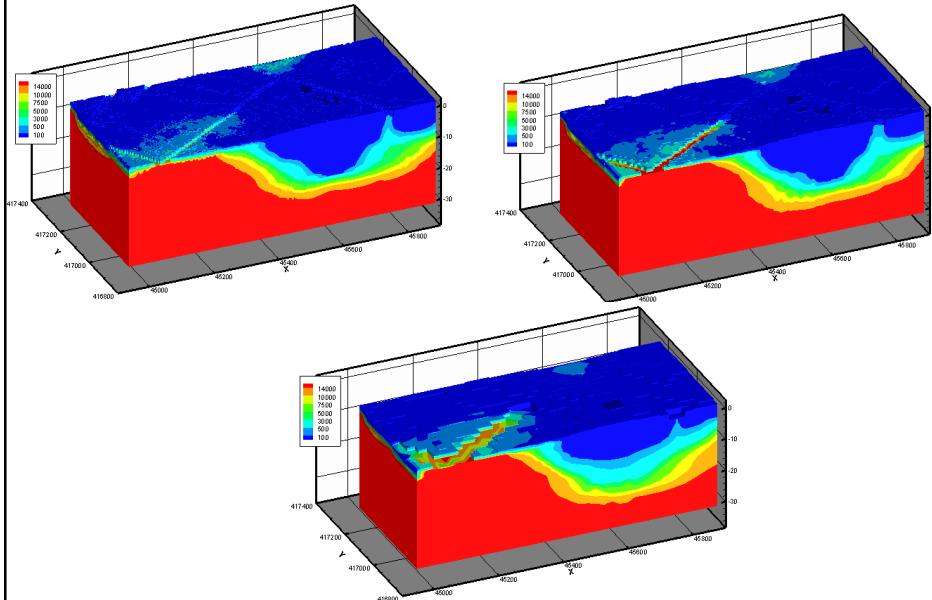
### Effect of size model cell on physical process



X= LOUSY models for predicting exact number of salt water fingers

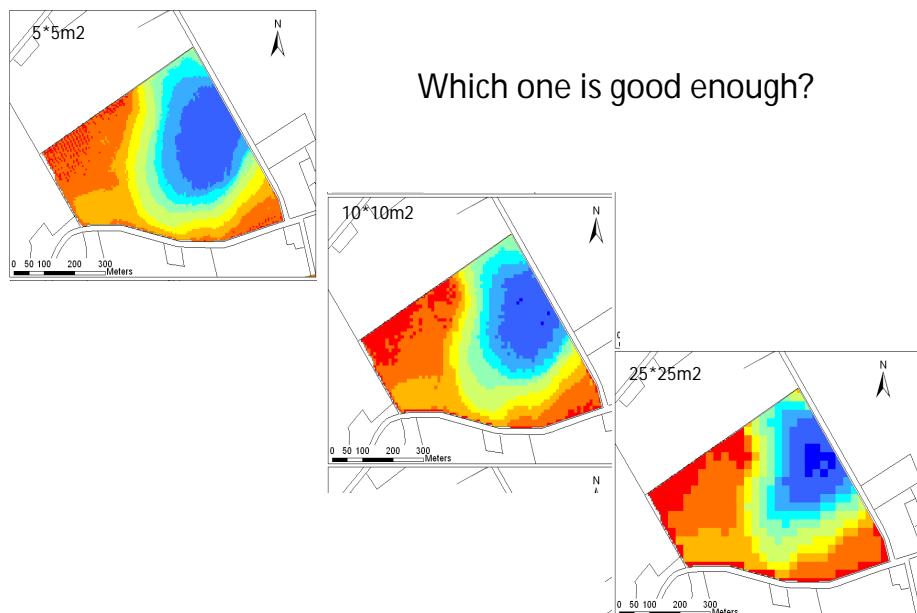


Different model scales: 5, 10, 25m<sup>2</sup>

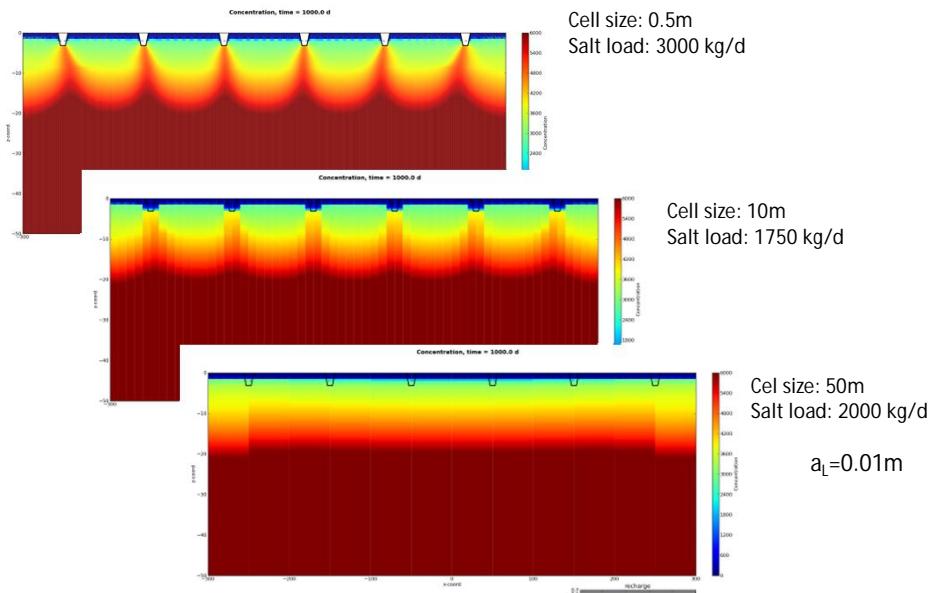


Different model scales

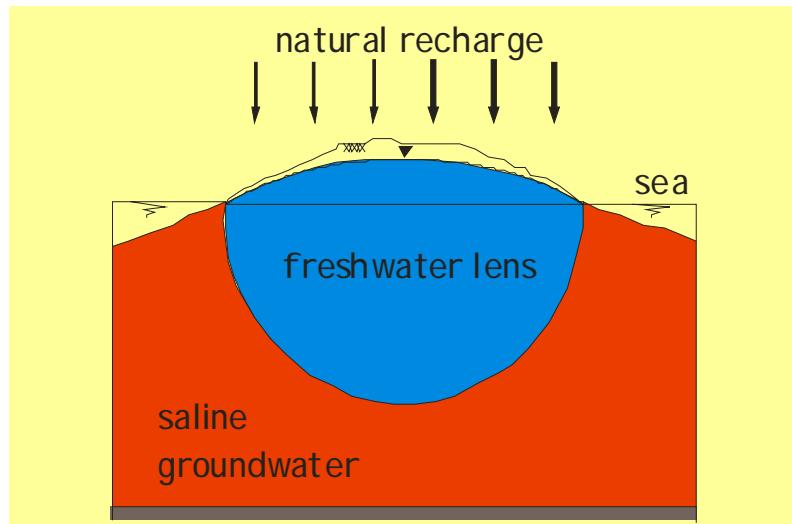
Which one is good enough?



### Upscaling issues: upconing under ditch



### Evolution of a freshwater lens



### Question:

*How long does it take before the volume of a freshwater lens is filled?:*

- a. 5 years
- b. 25 years
- c. 100 years
- d. 500 years

T = specific time scale

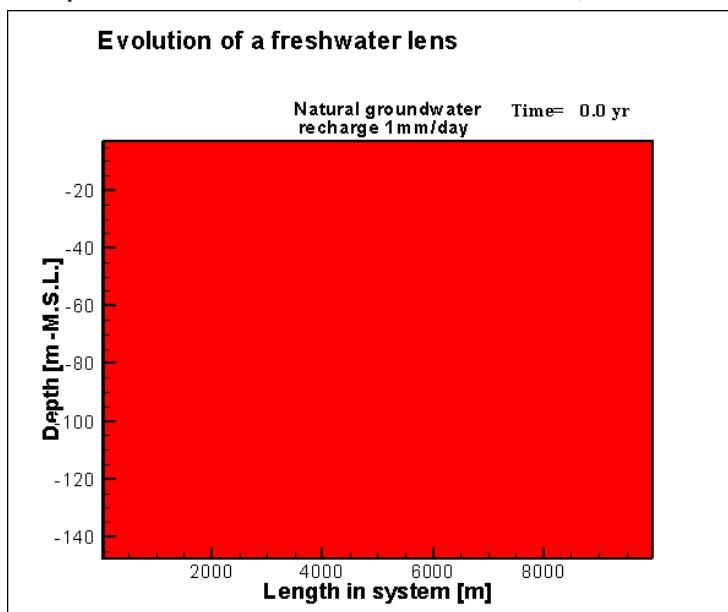
T = time period before the lens has reached 95% of its final form

In the Netherlands: T = 75-200 jaar,

depends on:

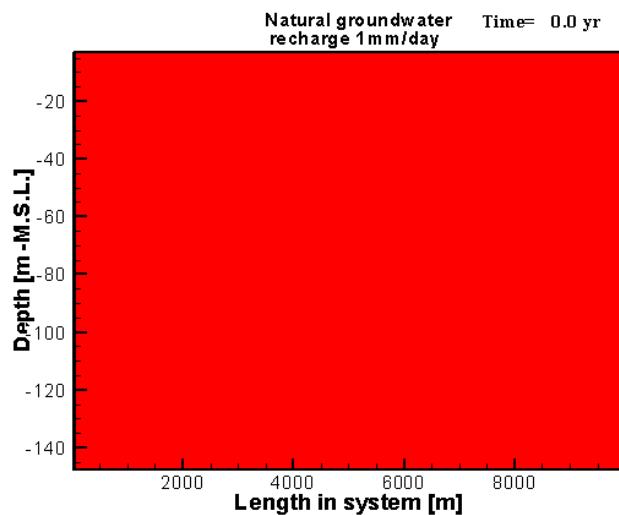
- width dune area
- natural groundwater recharge
- hydraulic conductivity soil

### Concept: evolution freshwater lens (not Griend!)



Concept: evolution freshwater lens (not Griend!)

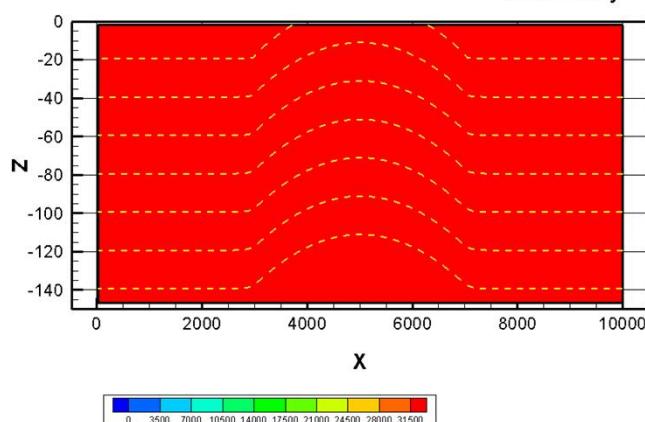
### Evolution of a freshwater lens



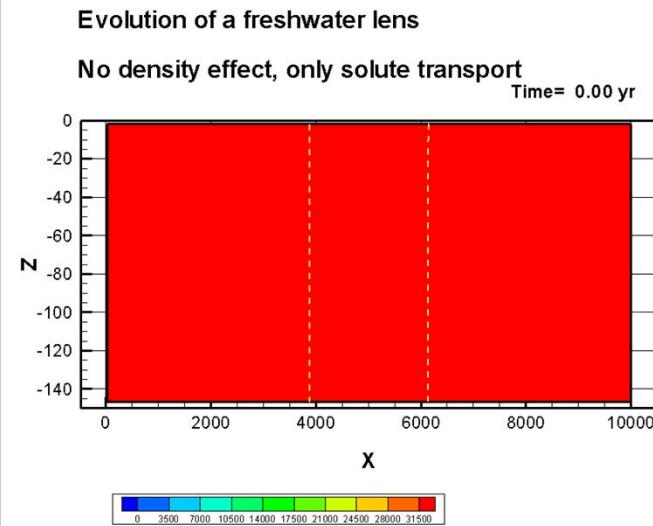
### Evolution freshwater lens

#### Evolution of a freshwater lens

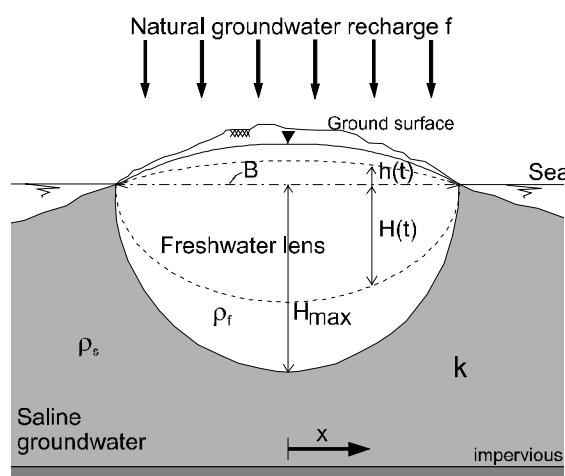
Time= 0.00 yr



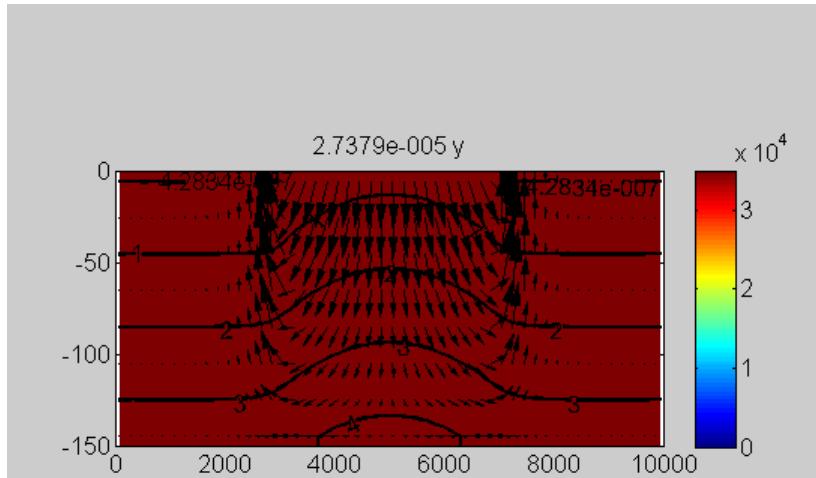
## Evolution freshwater lens: no density effects



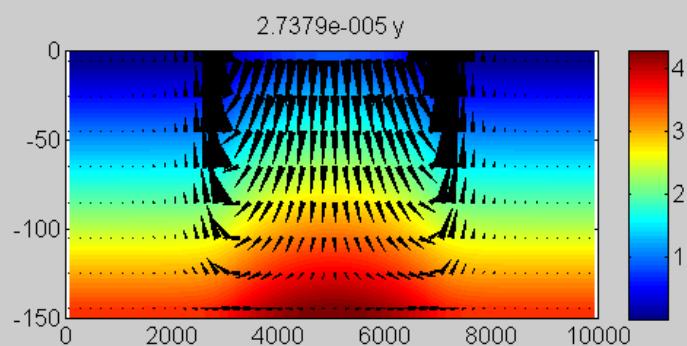
## Case 2: Development of a freshwater lens



Evolution lens



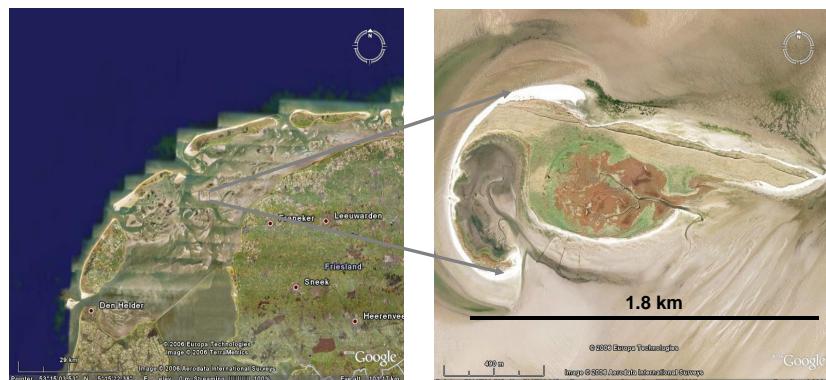
Evolution freshwater head



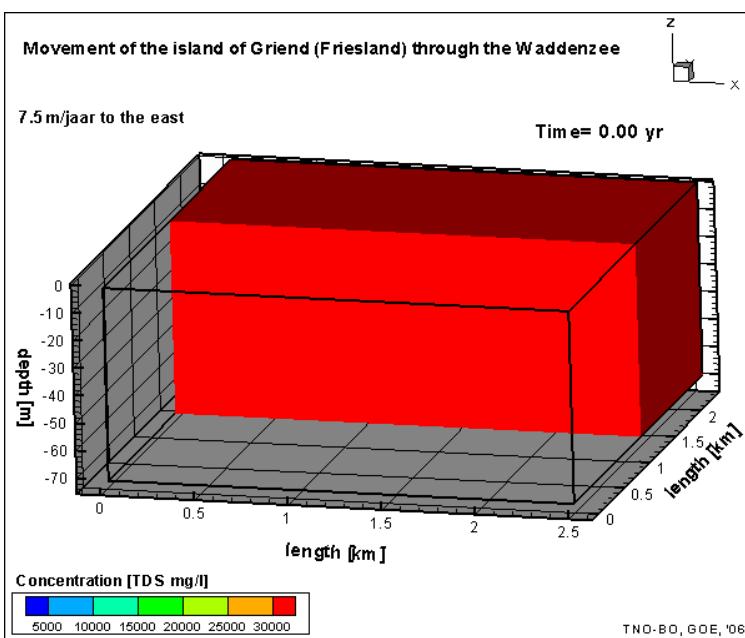
## The island of Griend

### Issues:

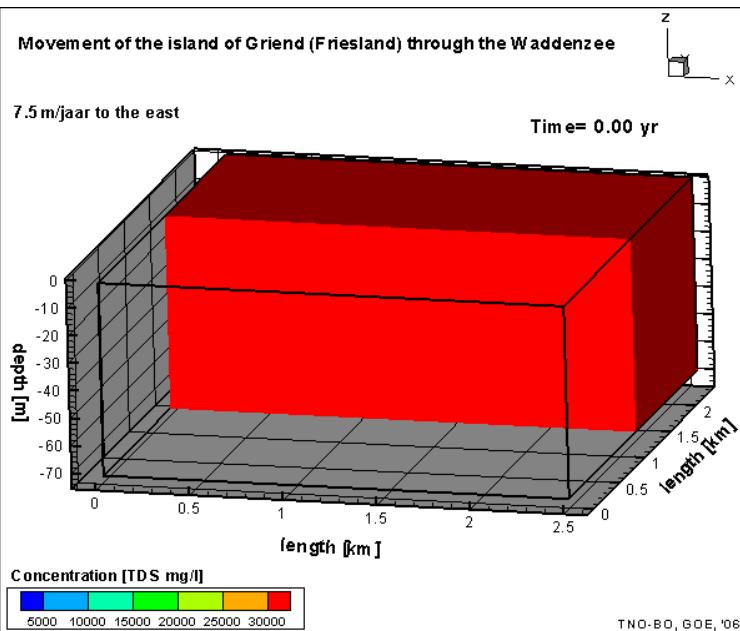
1. Small island moves ~7.5m per year to the east
2. Effect on the volume of the freshwater lens:
  - Can a lens be developed?
  - What is the thickness of the lens?



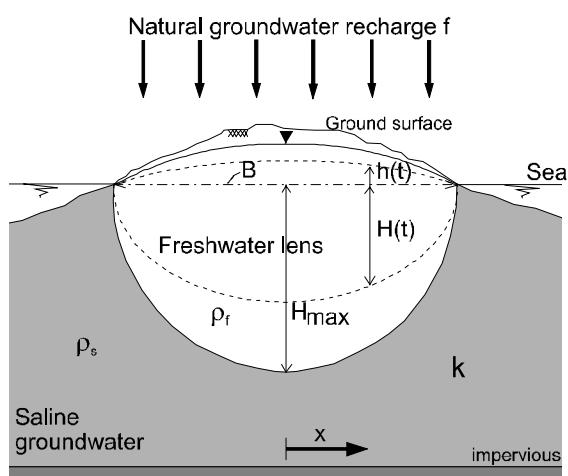
### Movement of De Griend and creation of the lens



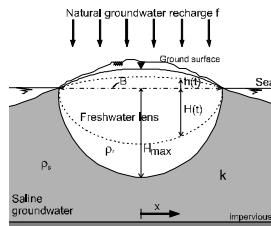
## Movement of De Griend and creation of the lens



## Case 2: Development of a freshwater lens



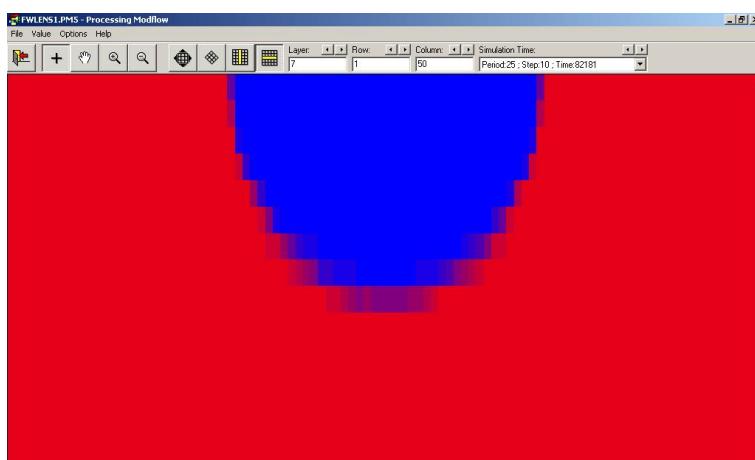
### Case 2: Development of a freshwater lens



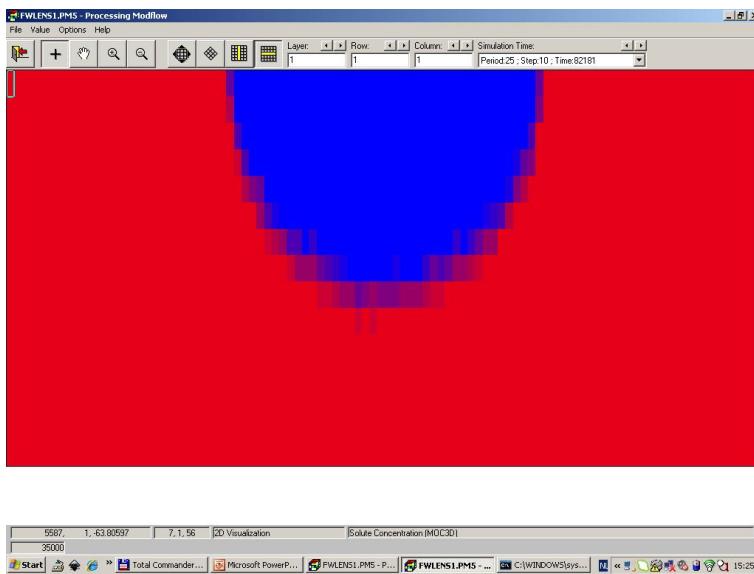
#### Parameters

Layers	15	$K_{\text{hor}}$	20 m/d
Rows	1	$T$	200 m/d
Columns	100	Anisotropy $K_{\text{hor}}/K_{\text{ver}}$	10
$\Delta x$	100 m	$n_e$	0.35
$\Delta y$	10 m	$\alpha L$	0 m
$\Delta z$	10 m	$\alpha T$	0 m
Stress periods	10	recharge	360 mm/y
Initial concentration	35000 mg/l	Recharge concentration	0 mg/l
bouyancy	0.025		

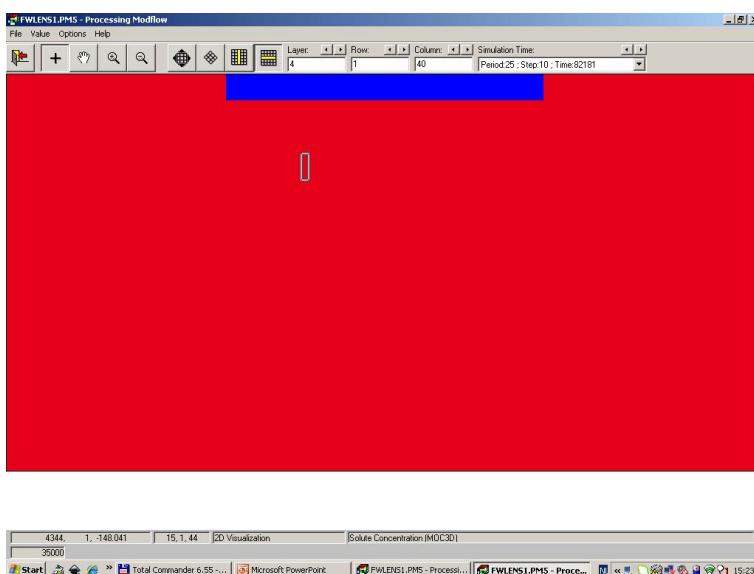
### MOCDENS3D, no disp, 16part



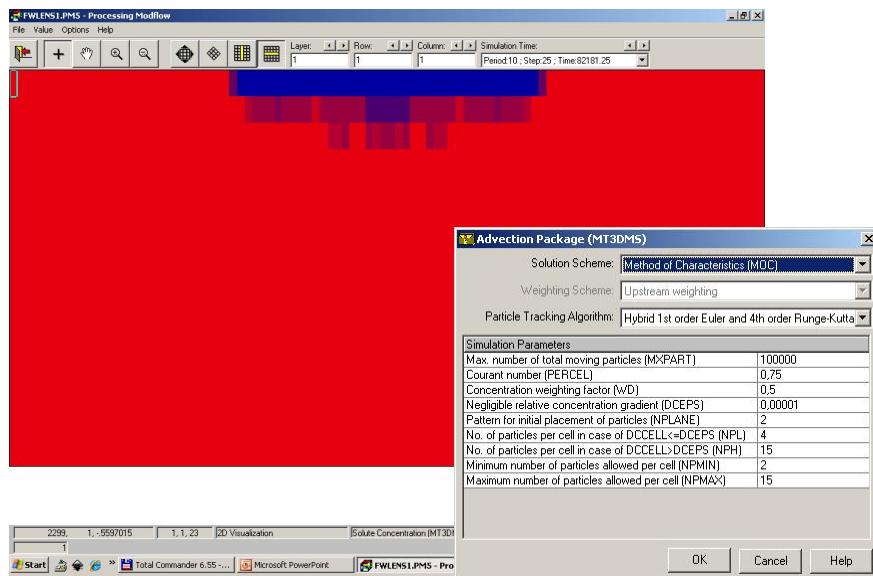
MOCDENS3D, no disp, 4part



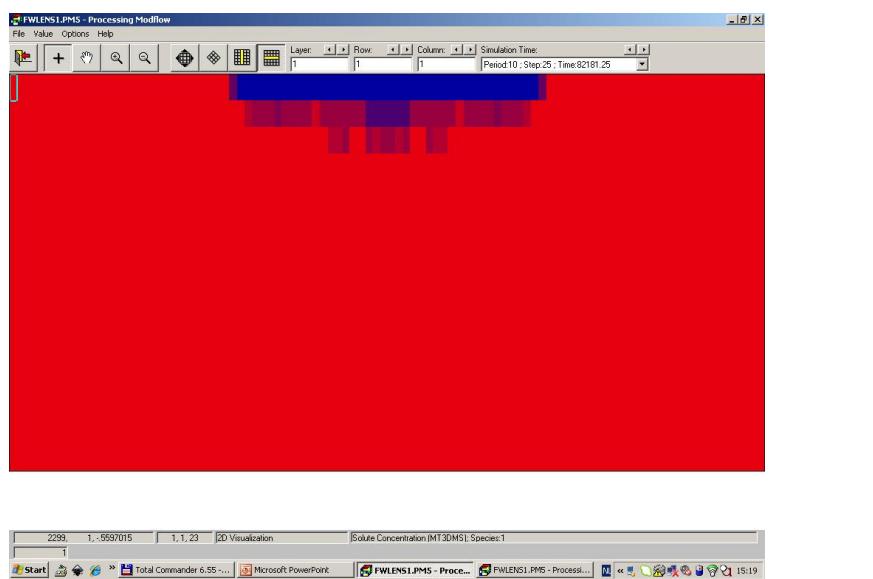
MOCDENS3D, no disp, 1part



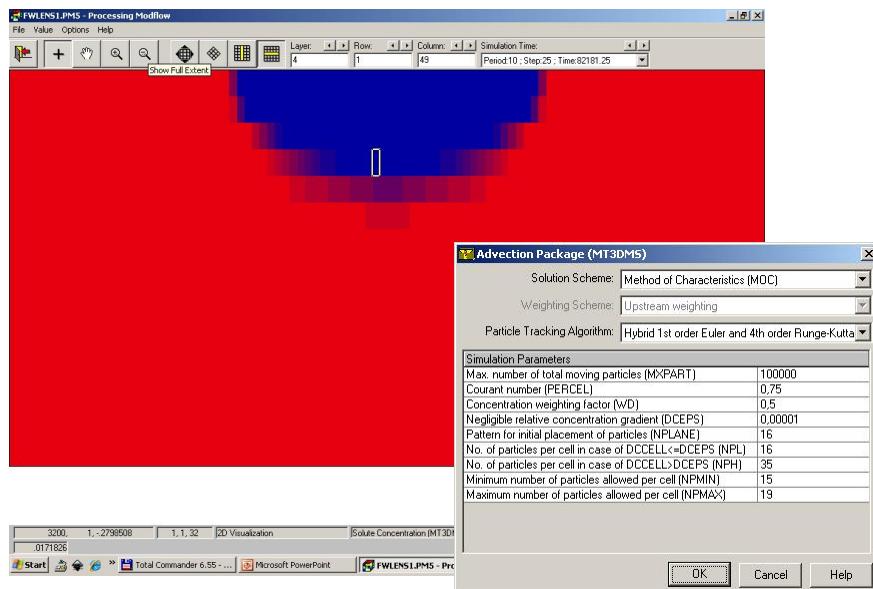
### SEAWAT, MOC, NPLANE=2



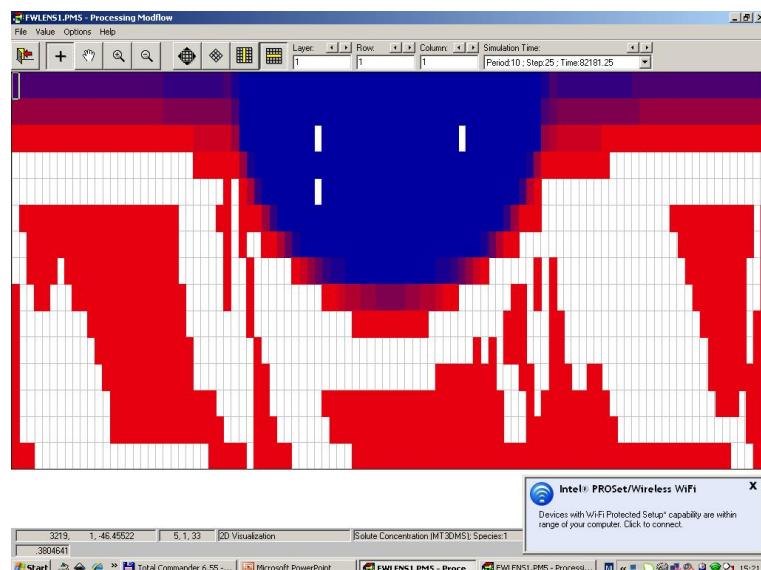
### SEAWAT, MOC, 4.NPLANE=16



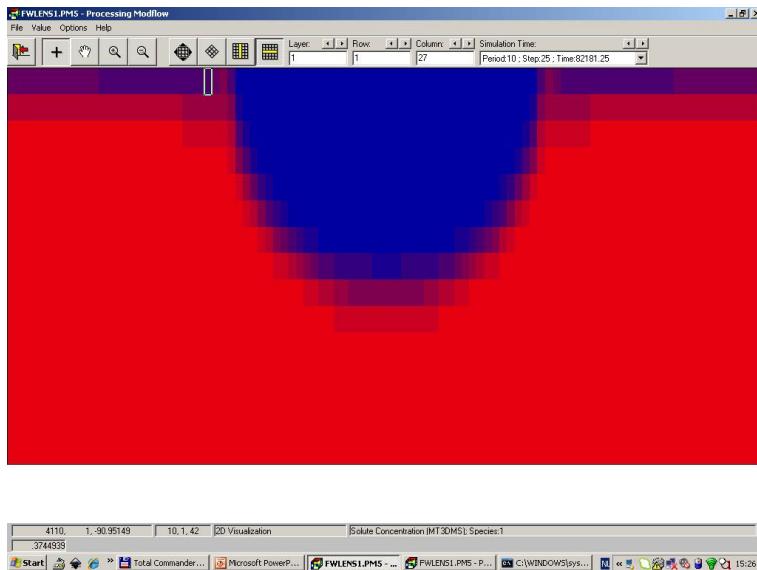
SEAWAT, MOC, 20sec, NPLANE=16, etc.



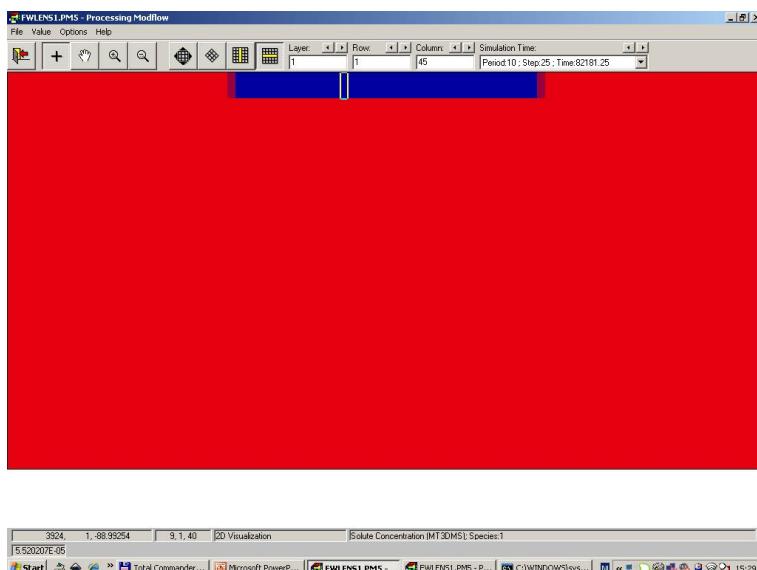
SEAWAT, ULTIMATE, 16.56sec



SEAWAT, MMOC, 8.5sec

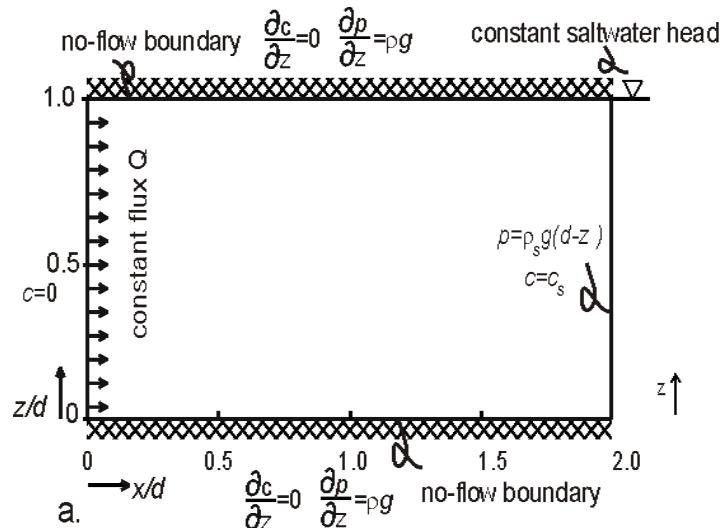


SEAWAT, HMOC, 6.8sec



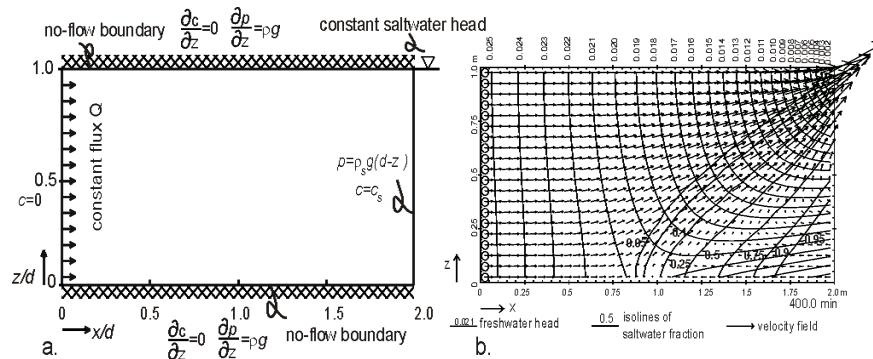
cases

### Henry's problem (1964)

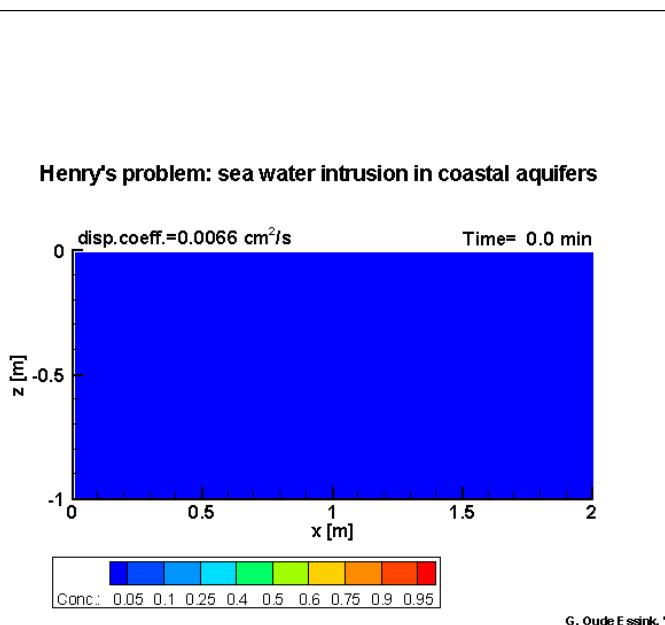


cases

### Henry's problem



## Henry's problem



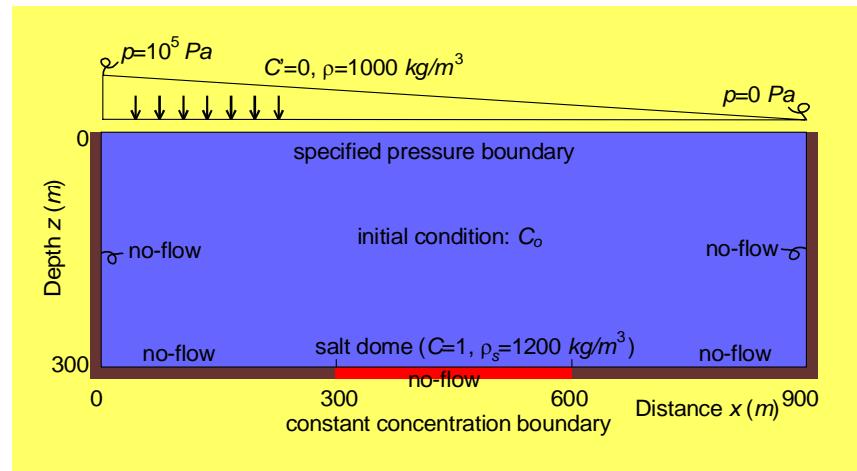
## Henry's problem

Don't use the Henry problem as a variable-density benchmark,  
because even with a constant density model, the results  
are more or less the same!

## Hydrocoin:

cases

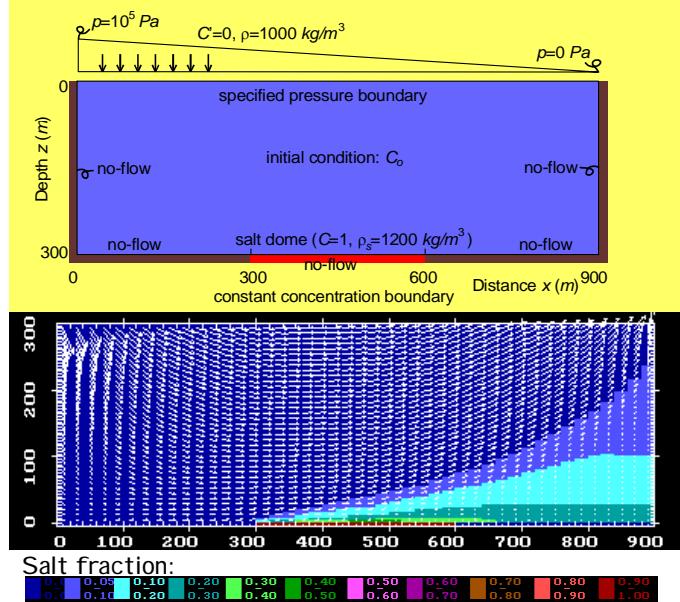
disposal of high-level nuclear waste  
groundwater movement near salt domes  
Gorleben salt dome, Germany



## Hydrocoin:

cases

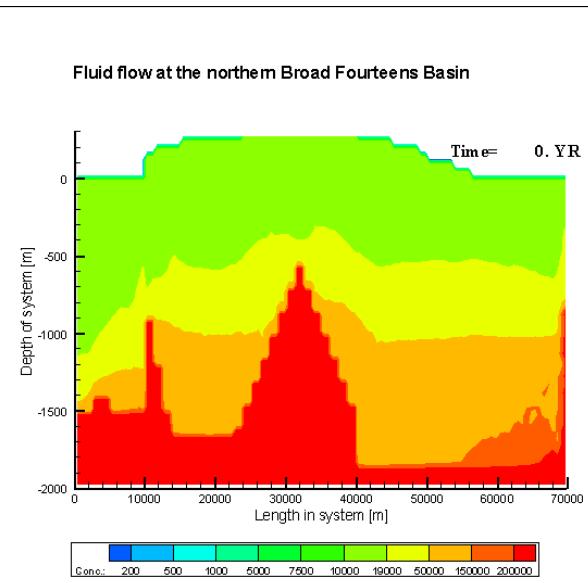
groundwater movement near salt domes



cases

## Broad 14 Basin, North Sea

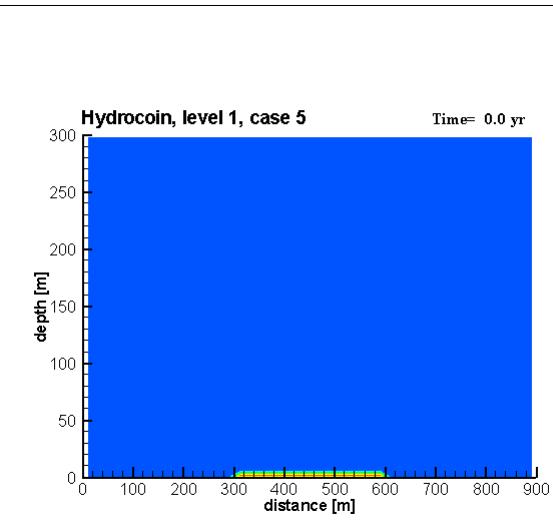
Geofluids'03, with L. Bouw



Bouw, L. & Oude Essink, G.H.P. 2003. Development of a freshwater lens in the inverted Broad Fourteens Basin, Netherlands offshore. J. of Geochemical Exploration (78-79), 321-325.

cases

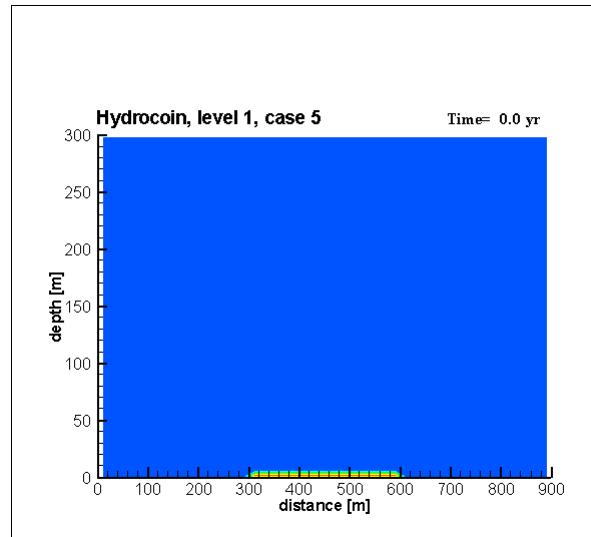
## Hydrocoin: effect of boundary condition (I) supply of brine through advection and hydrodynamic dispersion



*recirculation type*

cases

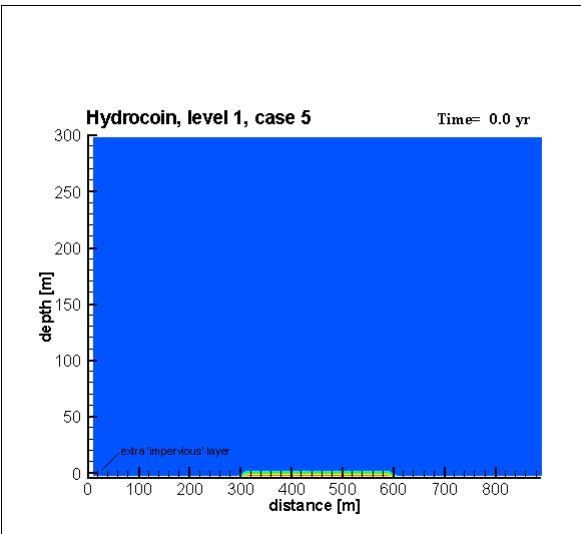
Hydrocoin: effect of boundary condition (I)  
supply of brine through advection and hydrodynamic dispersion



*recirculation type*

cases

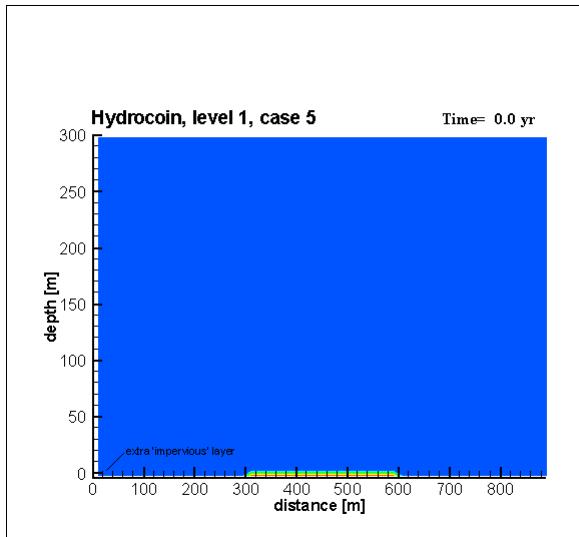
Hydrocoin: effect of boundary condition (II)  
supply of brine through only hydrodynamic dispersion



*swept-forward type*

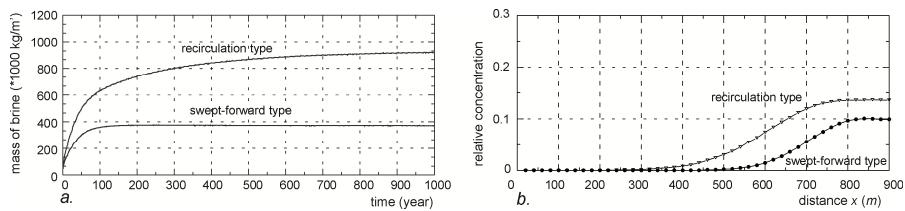
Hydrocoin: effect of boundary condition (II)  
supply of brine through only hydrodynamic dispersion

cases



*swept-forward type*

Hydrocoin: difference recirculation vs swept forward

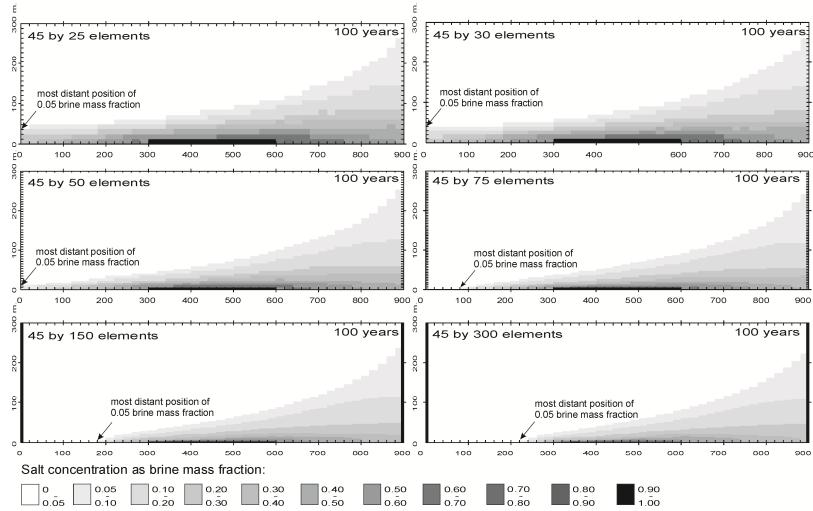


total mass of brine

brine conc at depth=200m

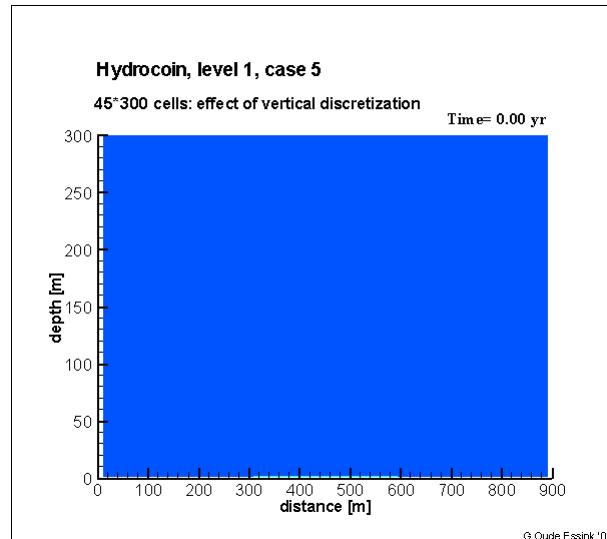
Lecture notes, p. 86-91

## Hydrocoin: effect of vertical grid size



Recirculation type

## Hydrocoin: effect of vertical discretization (III) cases more vertical cells give better solution

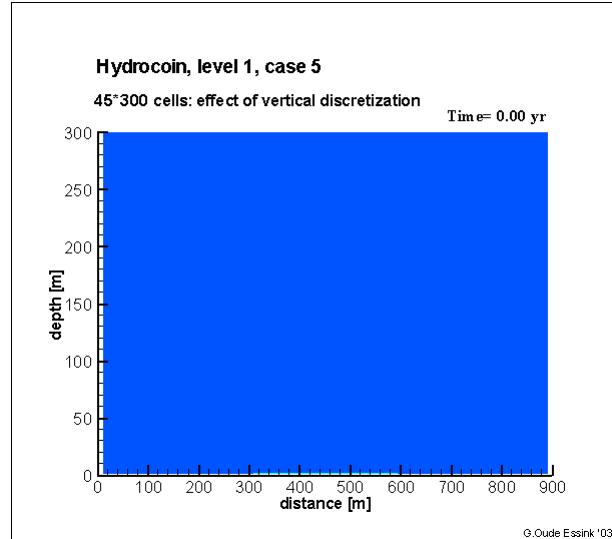


like the swept-forward type

cases

## Hydrocoin: effect of vertical discretization (III)

more vertical cells give better solution

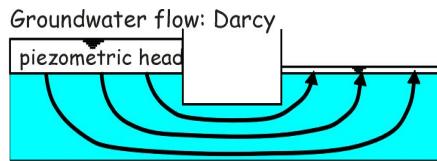


*like the swept-forward type*

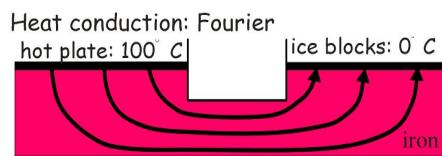
cases

## Analogy physical processes

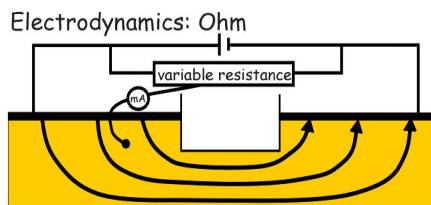
Heat transport (analogy with solute transport)



$$q = -k \frac{\partial \phi}{\partial x}$$



$$h = -\lambda \frac{\partial T}{\partial x}$$



$$i = -\sigma \frac{\partial V}{\partial x}$$

## Conduction and convection of heat

$$h = -\lambda_e \frac{\partial T}{\partial x} + n_e \rho c_f V T \quad \text{thermal conductivity [Joule/(ms °C)]}$$

heat conduction      convection  
 flux      (Fourier)      (fluid flow)

$$\lambda_e = n_e \lambda_{fluid} + (1 - n_e) \lambda_{solid}$$

continuity equation

$$-\frac{\partial h}{\partial x} = \rho' c' \frac{\partial T}{\partial t} \quad \text{specific heat capacity [Joule/(kg °C)]}$$

$$\rho' c' = n_e \rho c_{fluid} + (1 - n_e) \rho_{solid} c_{solid}$$

## Analogy solute and heat transport

Solute: advection-dispersion equation

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left( D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (CV_i) + \frac{(C - C')W}{n_e}$$

Heat: convection-conduction equation

$$\rho' c' \frac{\partial T}{\partial t} = \frac{\partial}{\partial x_i} \left( \Lambda_{ij} \frac{\partial T}{\partial x_j} \right) - \rho c_f \frac{\partial T q_i}{\partial x_i} + \Gamma$$

## Heat transport

### Analogy heat and solute transport

Heat transport

Convection-conduction equation

$$\rho' c \frac{\partial T}{\partial t} = \frac{\partial}{\partial x_i} \left( \Lambda_{ij} \frac{\partial T}{\partial x_j} \right) - \rho c_f \frac{\partial T q_i}{\partial x_i} + \Gamma$$

Equation of state: relation density & temperature

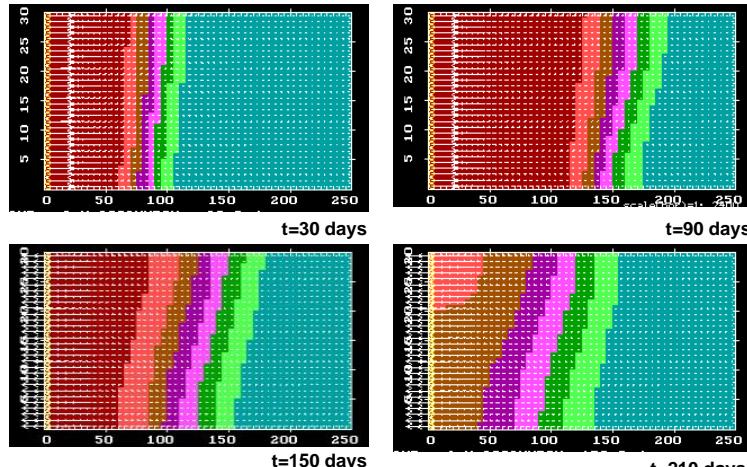
$$\rho_{i,j,k} = \rho_f (1 - \alpha_f T_{i,j,k})$$

Analogy between solute and heat transport

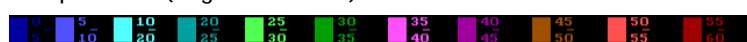
Solute	Heat
$C$	$T$
$R_d$	$1 + \frac{(1-n_e)\rho_s c_s}{n_e \rho c_f}$
$D_m$	$\frac{n_e \lambda_e + (1-n_e)\lambda_s}{n_e \rho c_f}$
$\lambda$	0

## Heat transport

### Energy storage in geothermal reservoirs



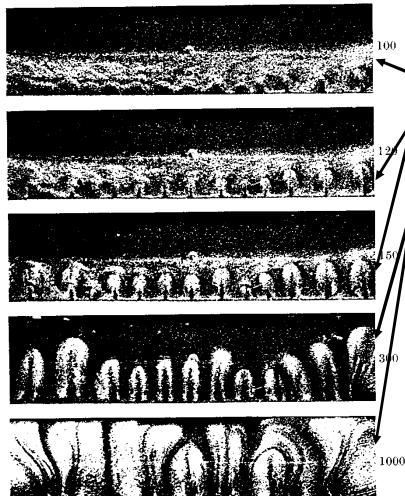
Temperature (degrees Celcius):



cases

## Elder problem (I)

It is originally a heat transport problem



Phases:

1. Stable growth diffusive boundary layer
2. Development flow cells embedded in boundary layer
3. Emergence of disturbances that grow into fingers

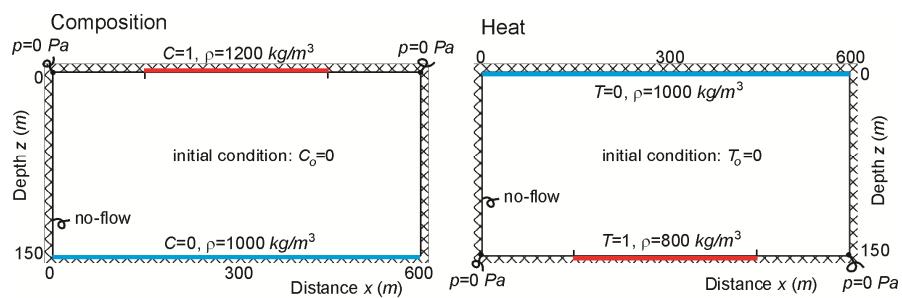
Convection of heat occurs when:

$$\text{Rayleigh number} > 4\pi^2$$

Elder, J. Fluid Mech. 32, 69-96, 1968

## Elder problem (II)

Analogy composition and heat

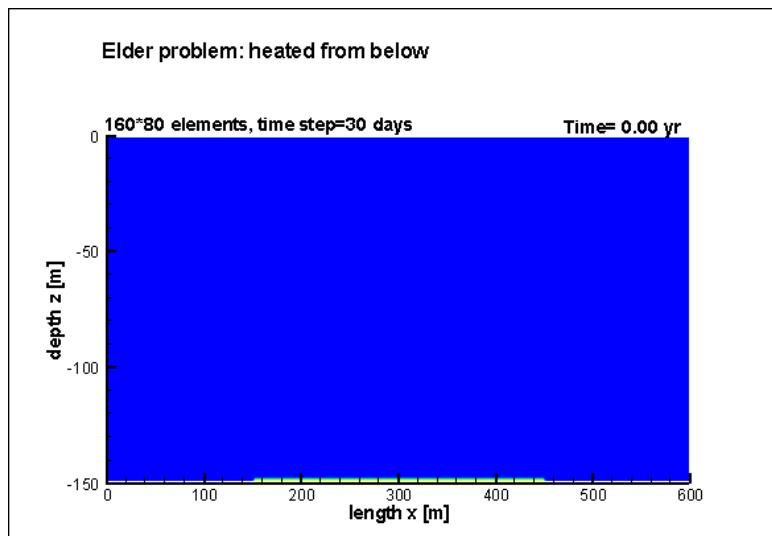


Lecture notes, p. 91-96

cases

### Elder problem (III)

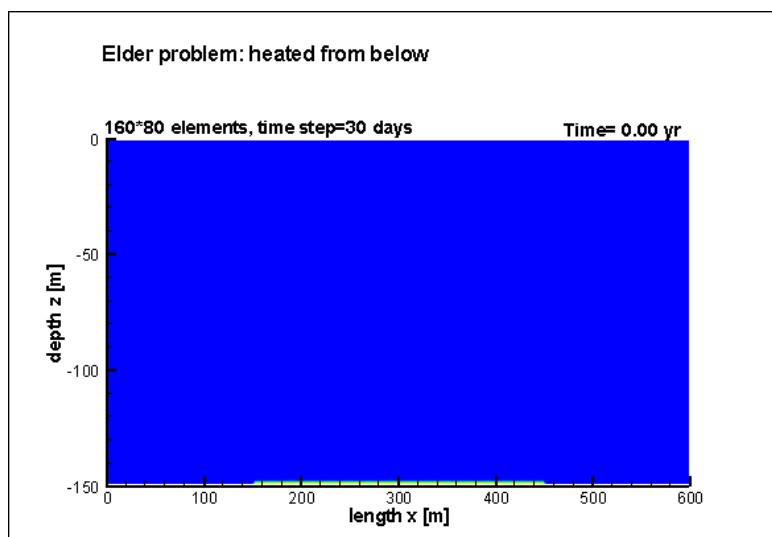
Development of convection cells (Rayleigh number=400)



cases

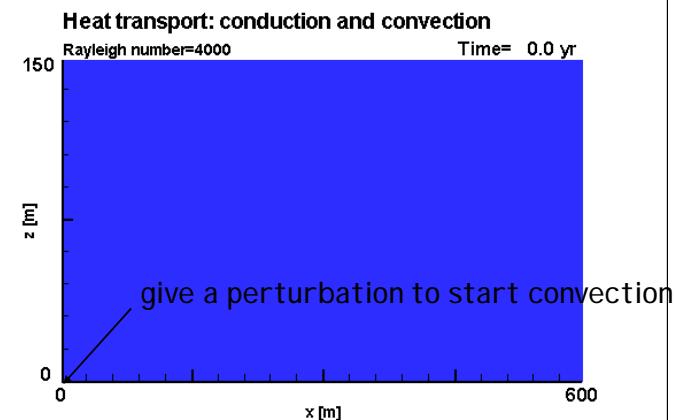
### Elder problem (III)

Development of convection cells (Rayleigh number=400)



cases

### Heat transport (Rayleigh number=4000)



### Impact of the 26-12-04 Tsunami on groundwater systems



Sri Lanka  
Some days after December 26<sup>th</sup>, 2004



## Impact of the 26-12-04 Tsunami on groundwater systems

Impression of relevant salinisation processes by conceptual models of salt water intrusion in coastal aquifers:

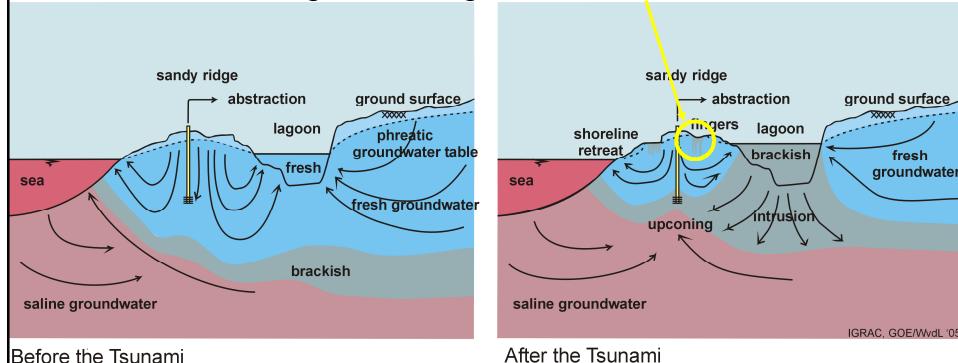
1. Fingering processes in the subsoil
2. Evolution of a freshwater lens after flooding by sea water
3. Freshwater lens in a coastal aquifer with a brackish lagoon

Next step:

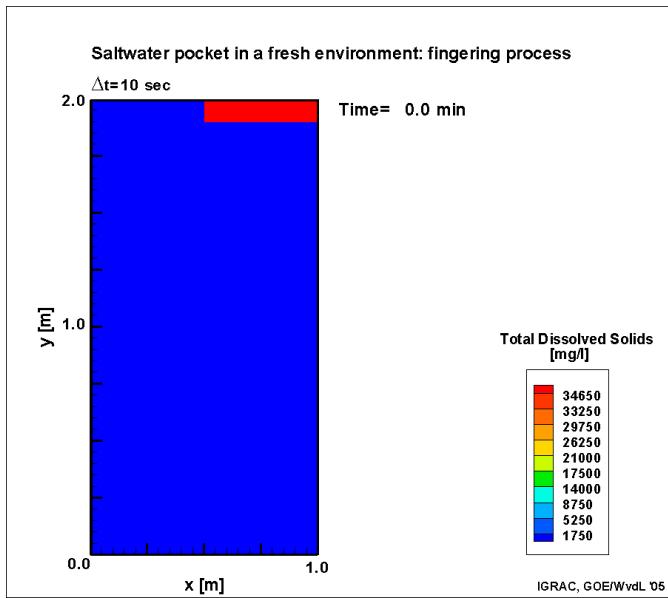
quantifying processes in real situations, using topographic and hydrogeological data, and ending up with vulnerability maps

### Concept 1: Fingering processes in the subsoil

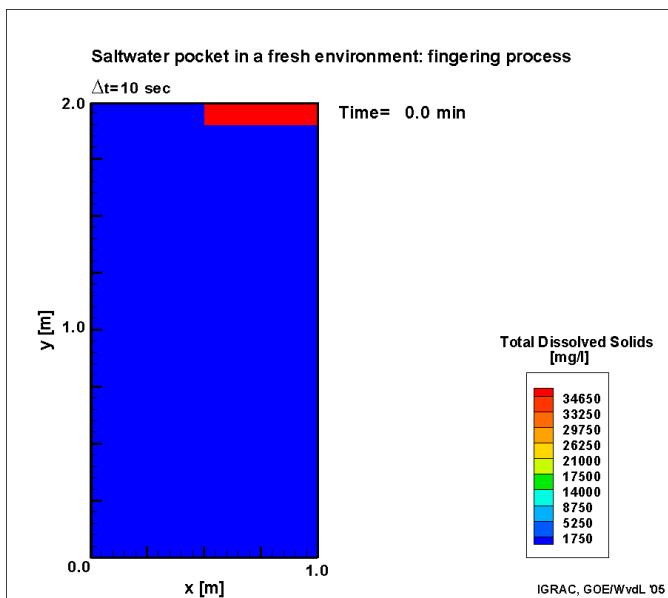
Case Sri Lanka: lagoon setting



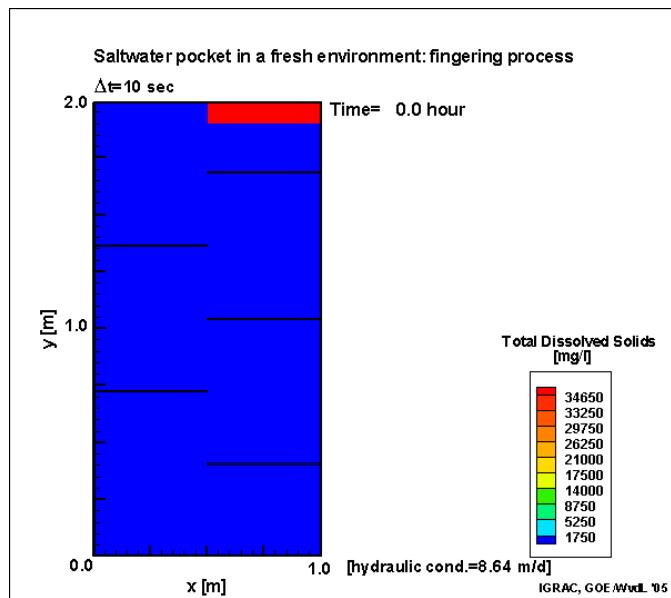
## Concept 1: Fingering processes in the subsoil



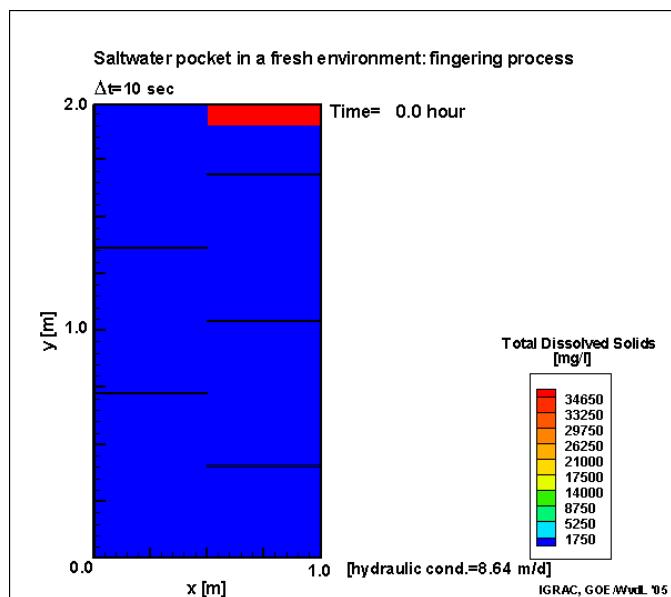
## Concept 1: Fingering processes in the subsoil



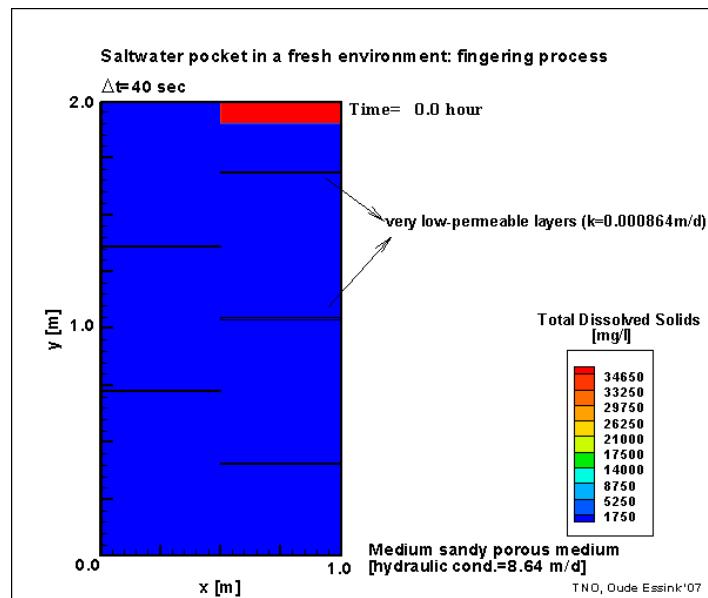
## Concept 1: Fingering processes in the subsoil



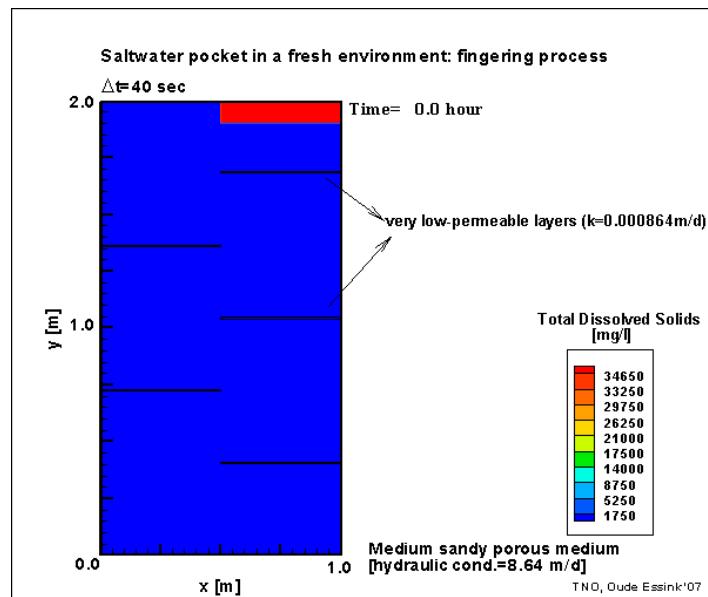
## Concept 1: Fingering processes in the subsoil



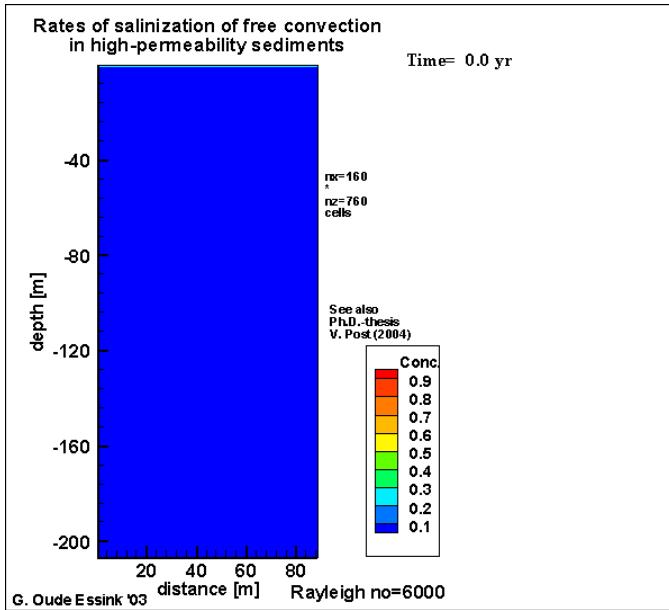
## Concept 1: Fingering processes in the subsoil



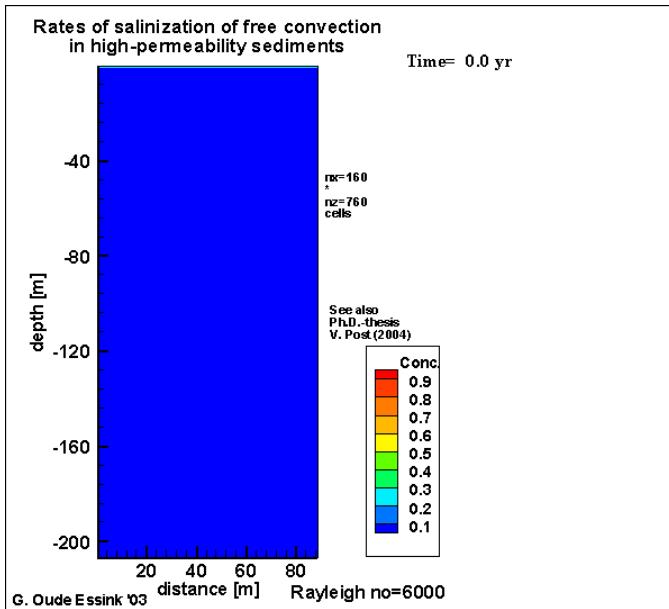
## Concept 1: Fingering processes in the subsoil



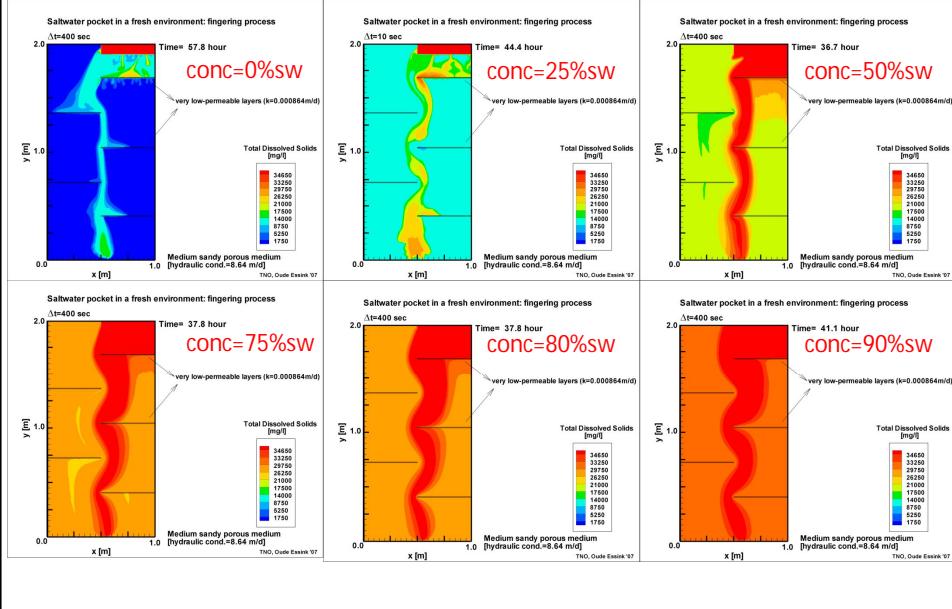
## Concept 1: Fingering processes in the subsoil



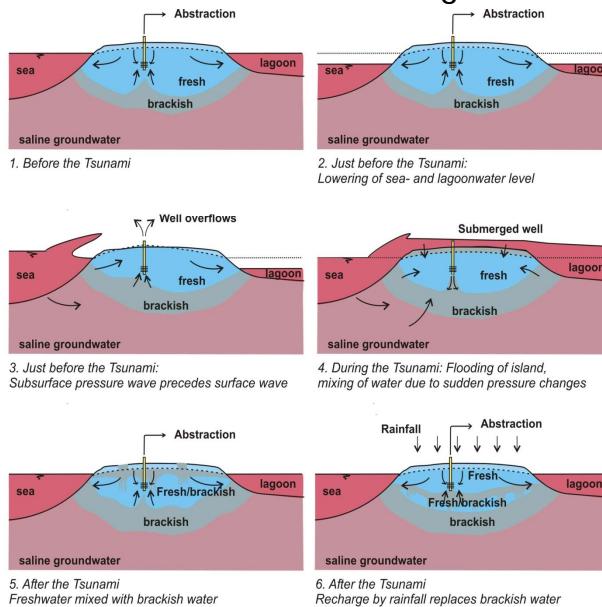
## Concept 1: Fingering processes in the subsoil



## Fingering processes in the subsoil



## Concept 2: Evolution of a freshwater lens after flooding



## Concept 2: Evolution of a freshwater lens after flooding

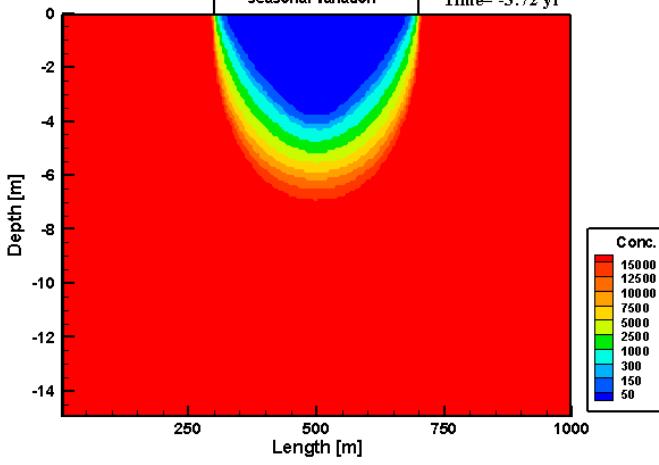
### Effect of Tsunami on a freshwater lens

At Time=0 yrs: 1. increase of head of 3 m  
2. duration 2 hours

Maldives setting

Natural groundwater recharge  
seasonal variation

Time= -3.72 yr



IGRAC, GOE/MWtL, '05

## Concept 2: Evolution of a freshwater lens after flooding

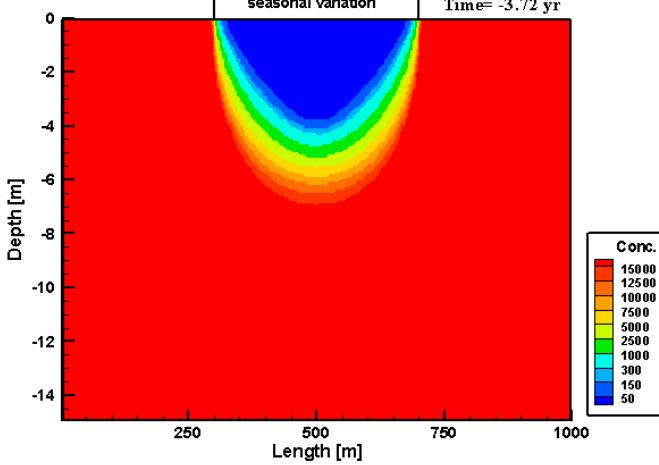
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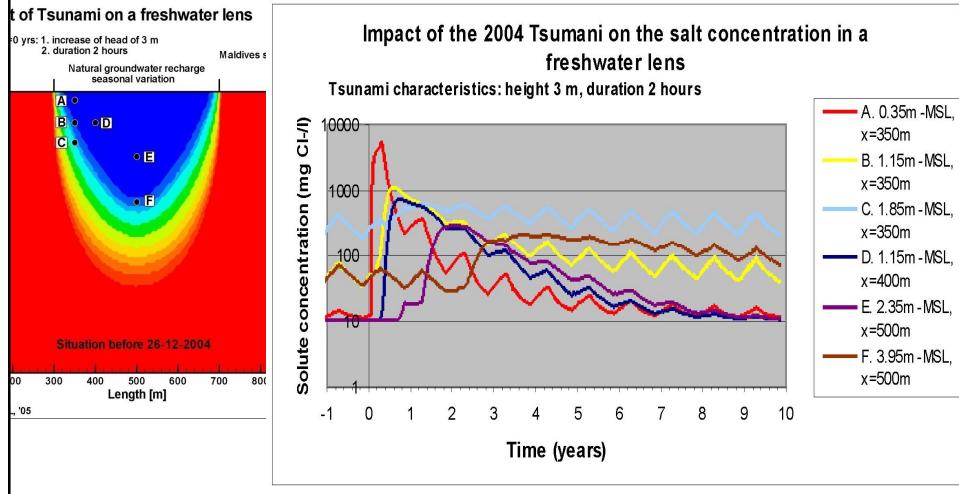
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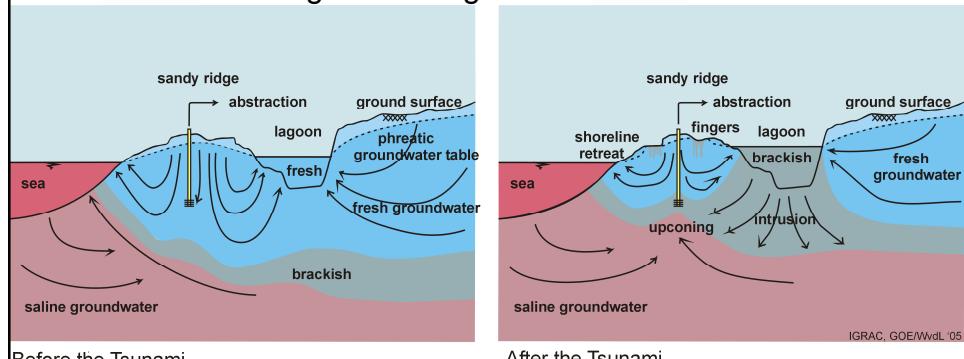
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## Concept 2: Evolution of a freshwater lens after flooding

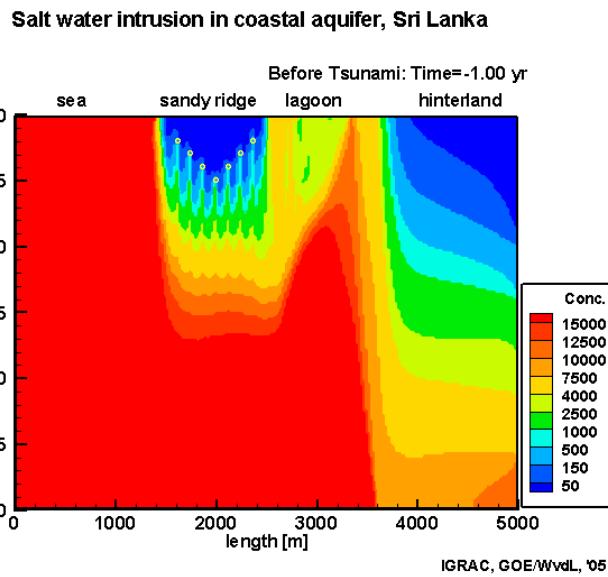


## Concept 3: Freshwater lens in a coastal aquifer with a brackish lagoon

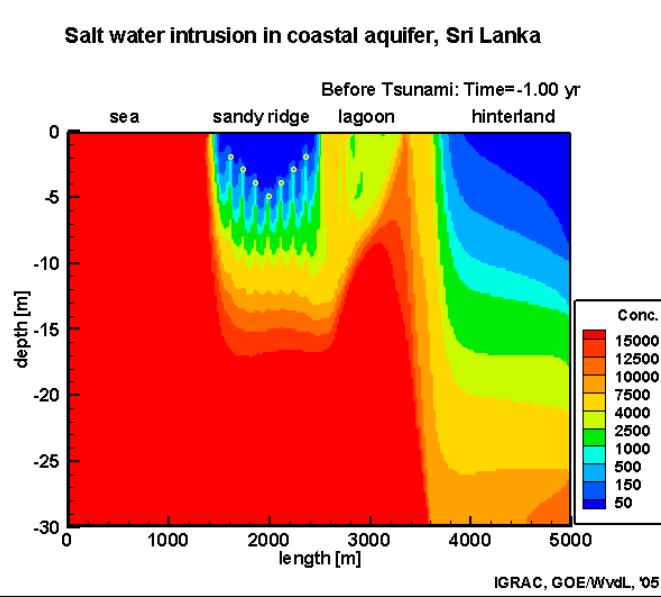
### Case Sri Lanka: lagoon setting



Concept 3: Freshwater lens in a coastal aquifer  
with a brackish lagoon



Concept 3: Freshwater lens in a coastal aquifer  
with a brackish lagoon



### Concept 3: Freshwater lens in a coastal aquifer with a brackish lagoon

