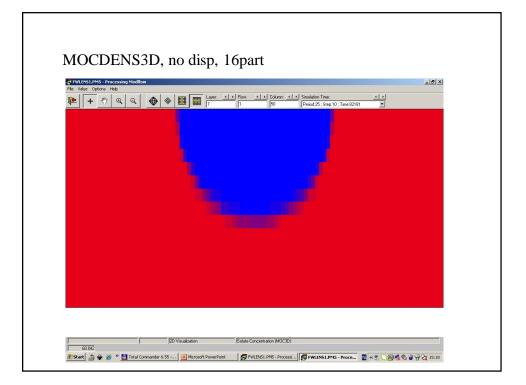
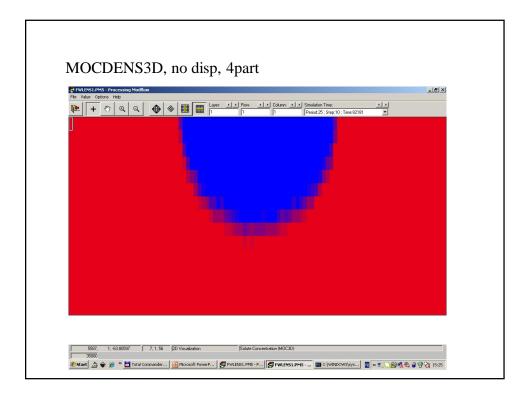
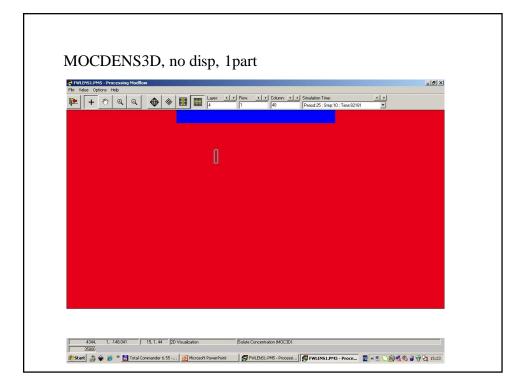
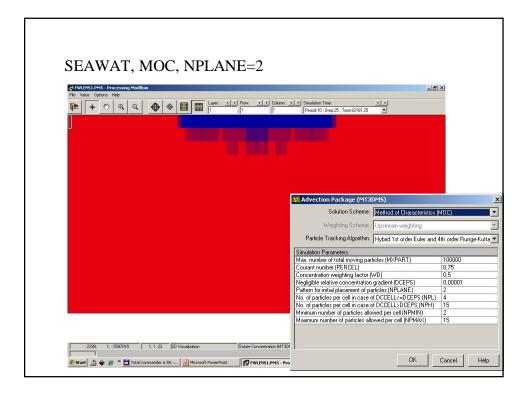


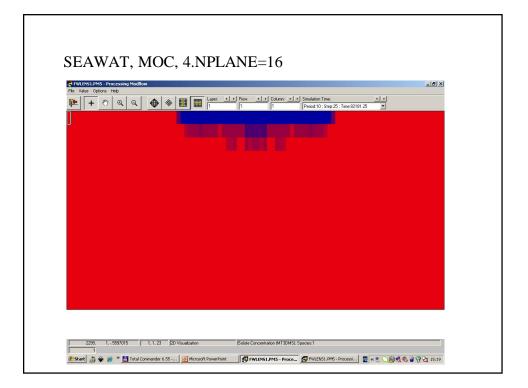
Case 2: De Natural groundwater rechar of the structure of the structure p, the structure of the structure sature groundwater	ge f	of a freshwater I	ens
Parameters			
Layers	15	K _{hor}	20 m/d
Rows	1	Т	200 m/d
	100	Anisotropy K _{hor} /K _{ver}	
Columns	100	Anisouopy R _{hor} /R _{ver}	10
Columns Δx	100 m	ne	0.35
Δx	100 m	ne	0.35
Δx Δy	100 m 10 m	ne αL	0.35 0 m
Δx Δy Δz	100 m 10 m 10 m	ne αL αT	0.35 0 m 0 m

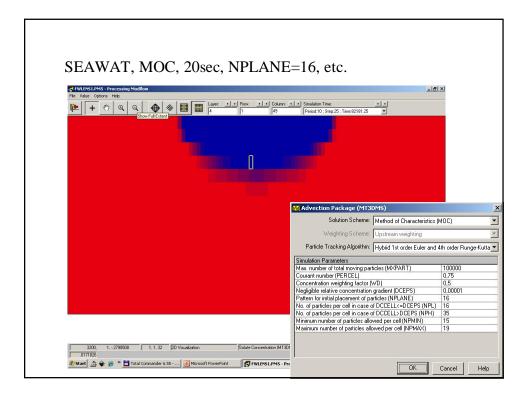


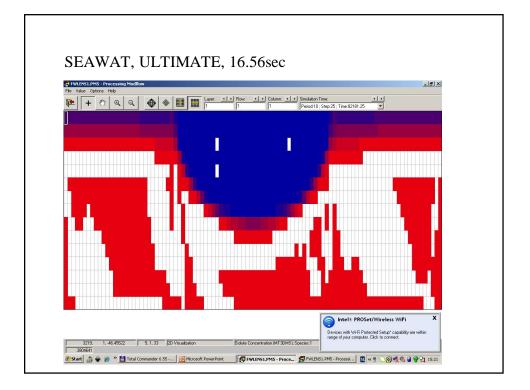


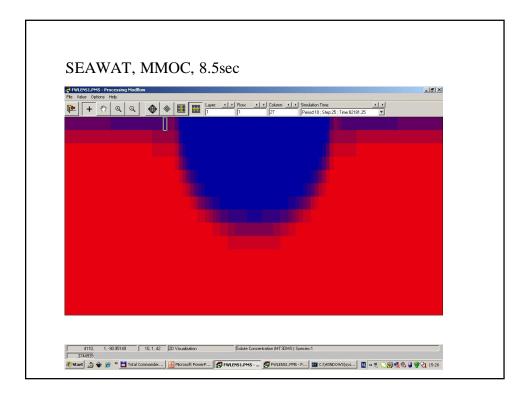


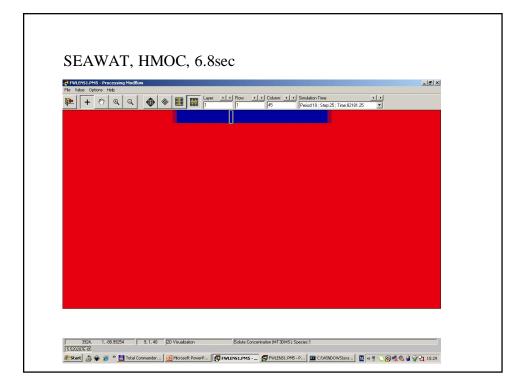


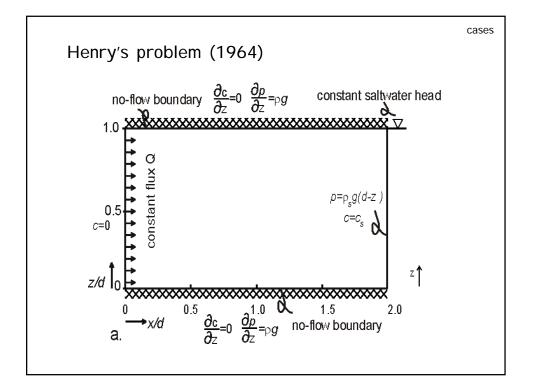


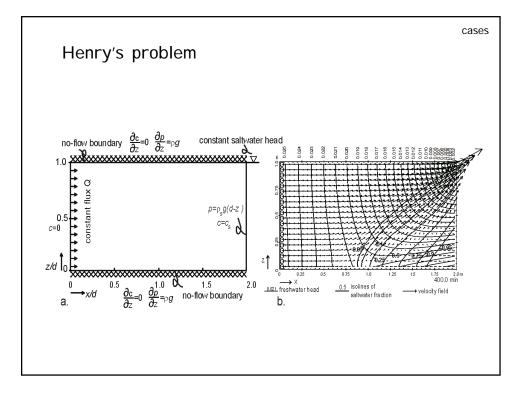


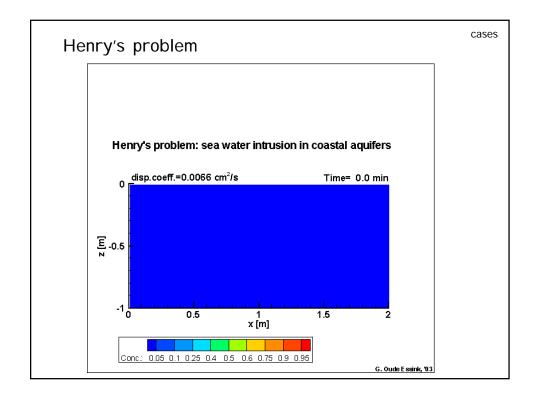


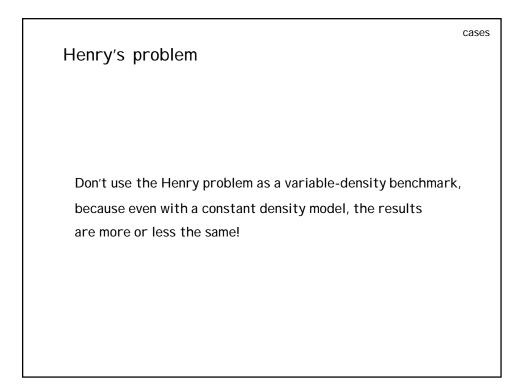


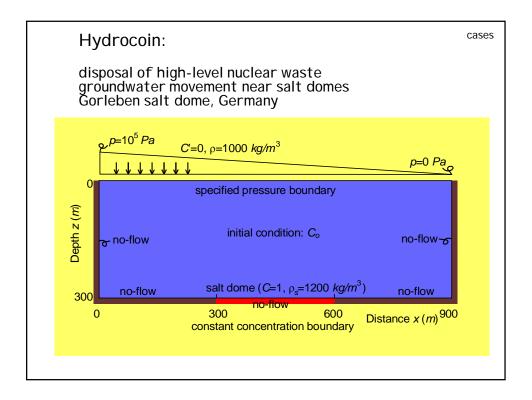


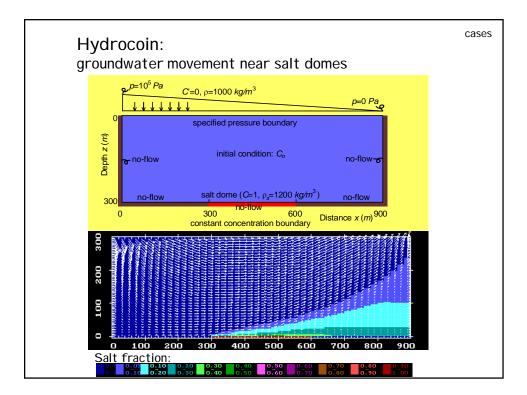


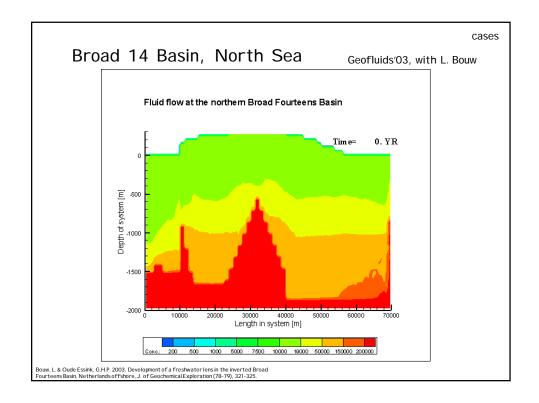


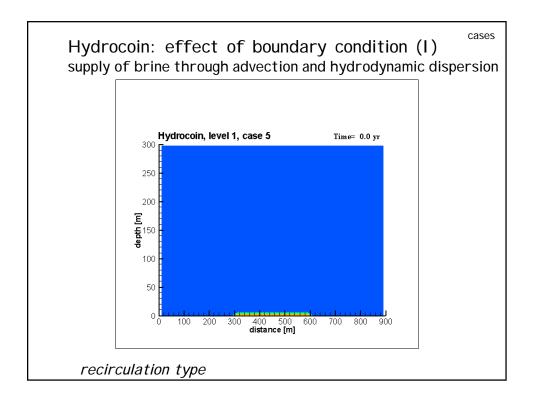


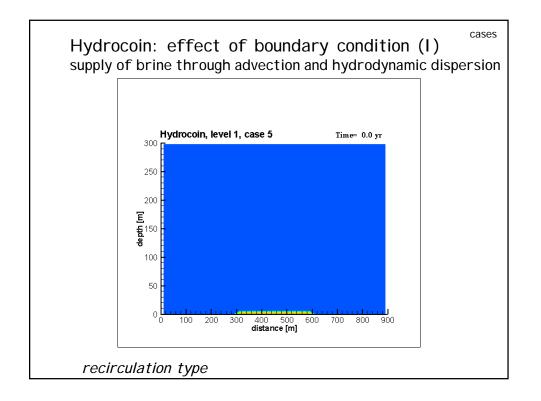


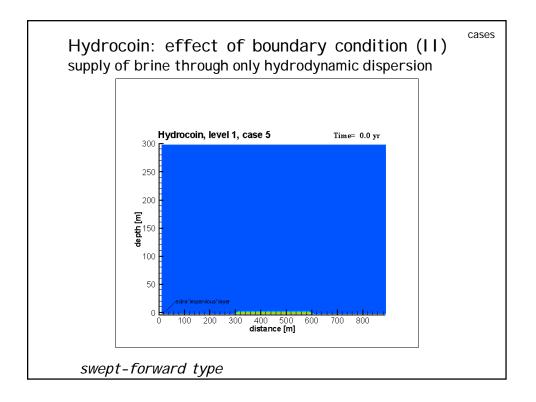


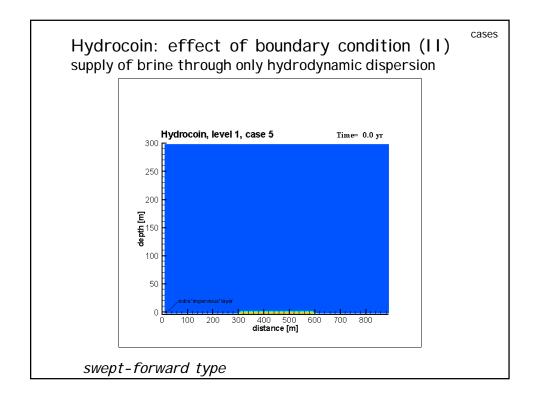


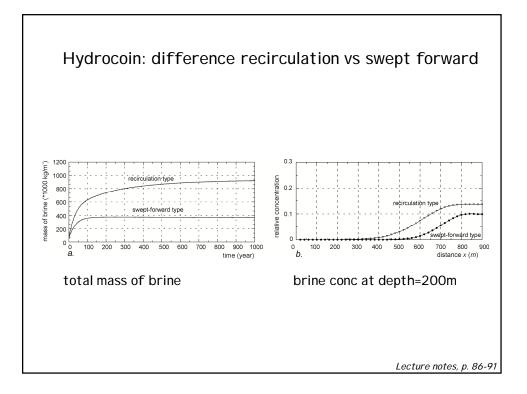


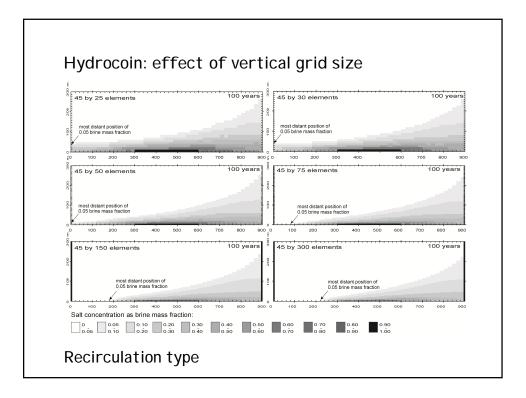


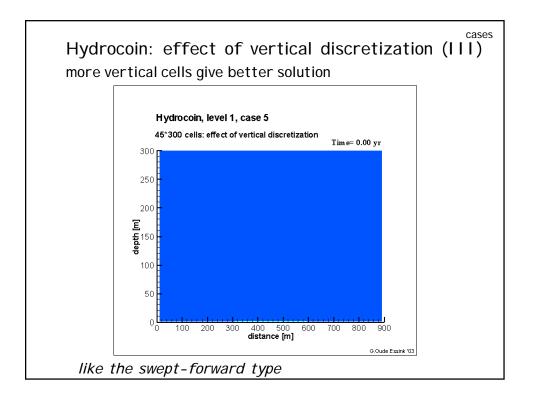


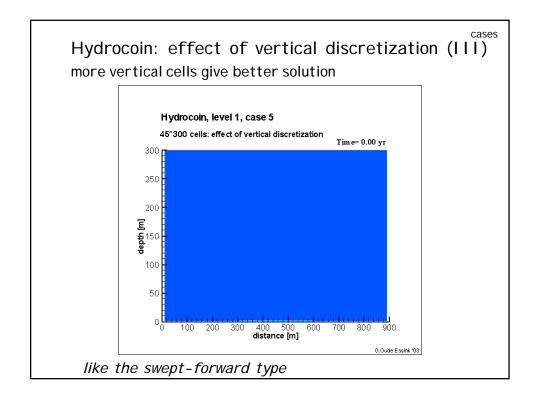


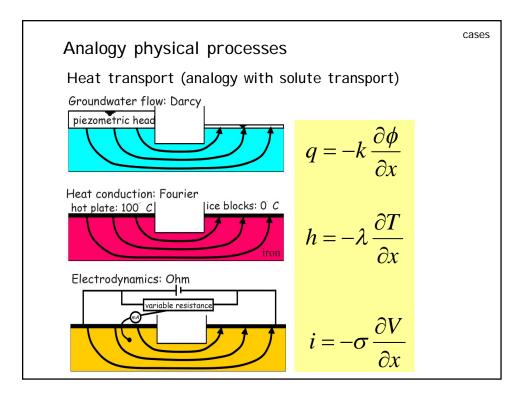


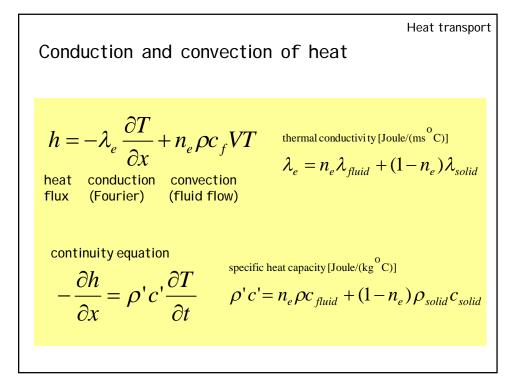


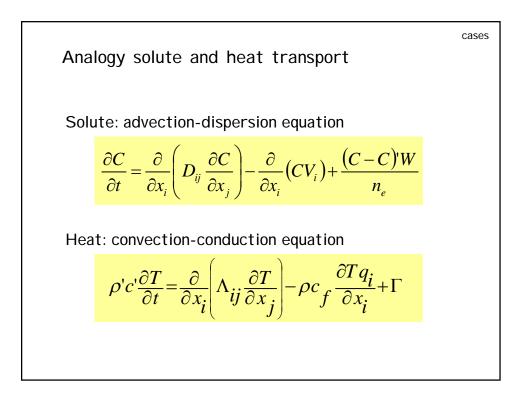


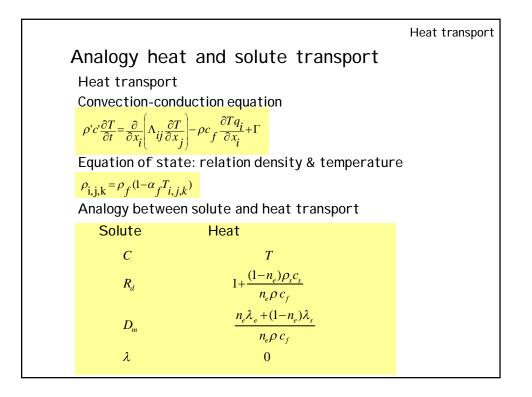


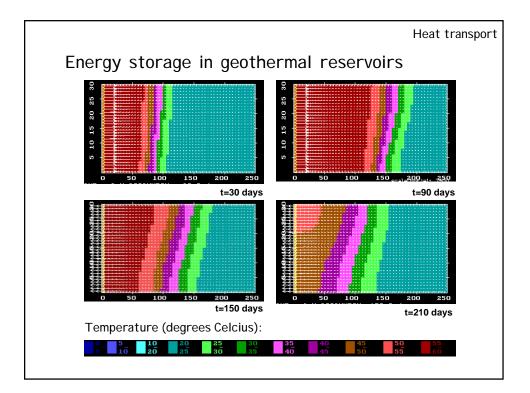


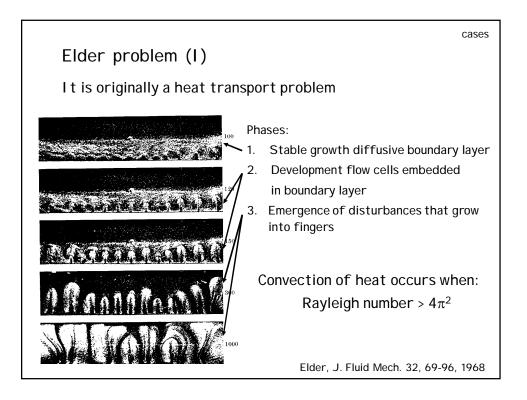


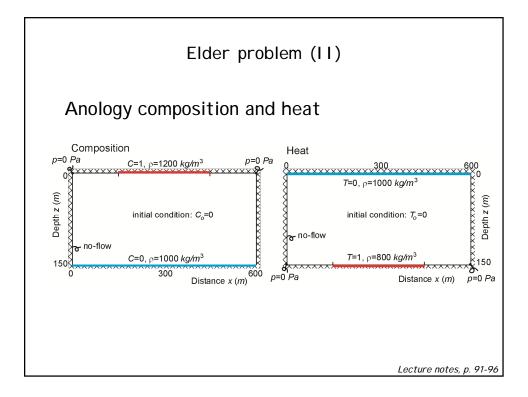


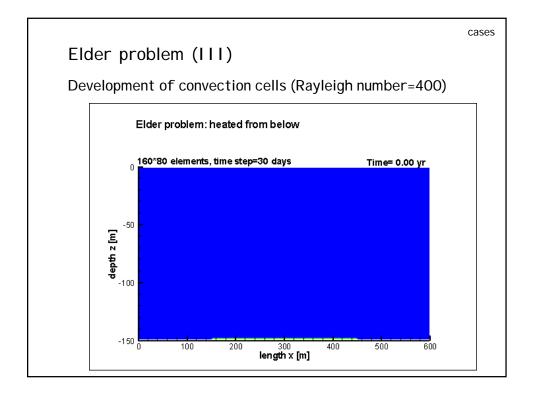


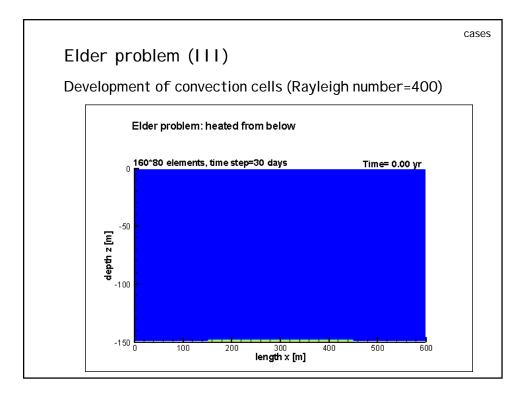


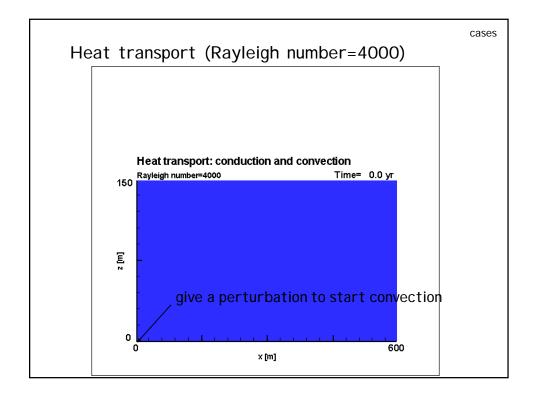


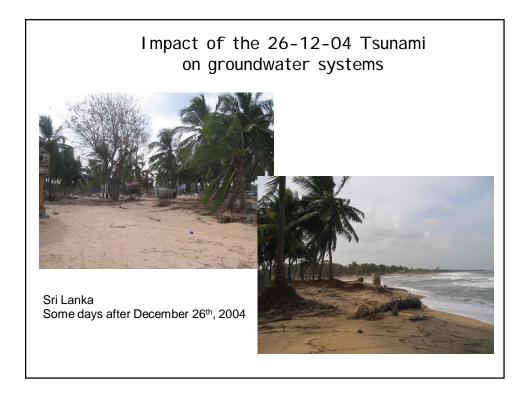


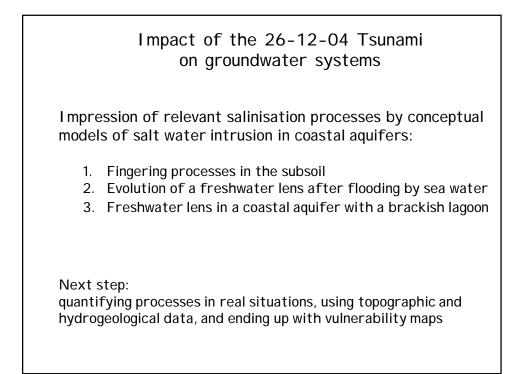


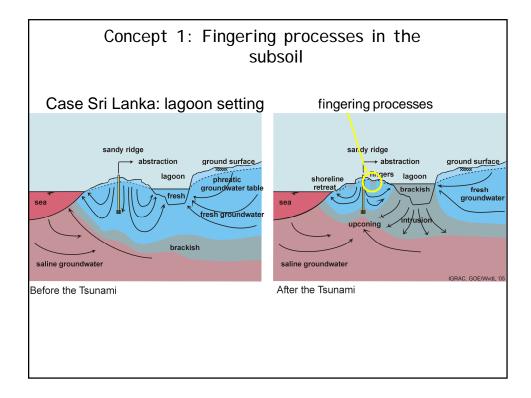


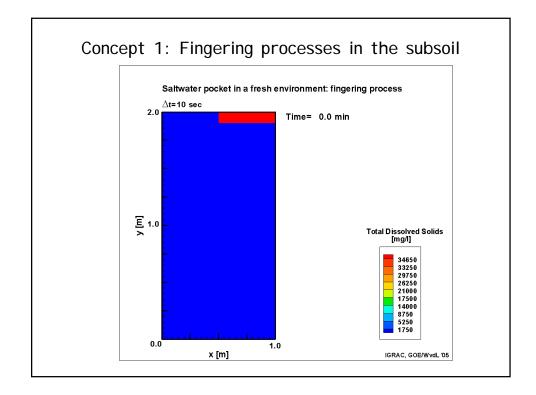


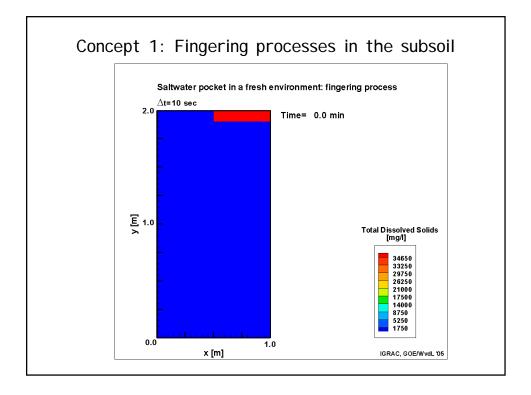


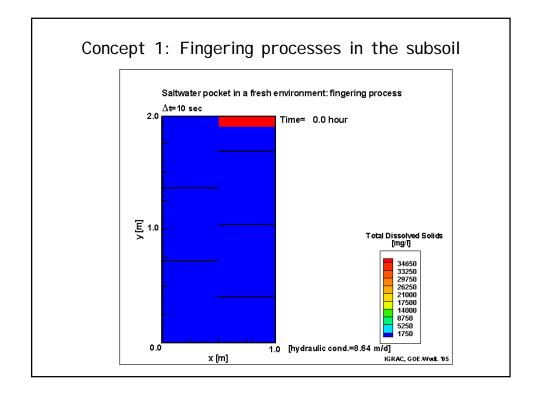


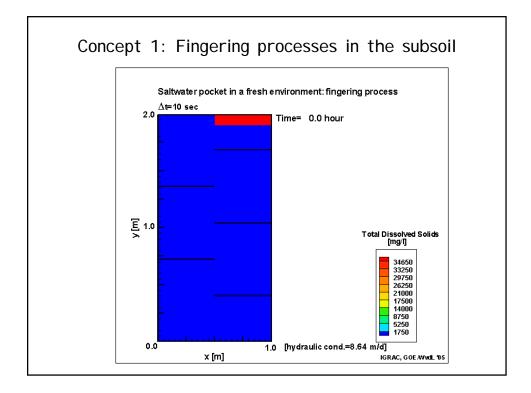


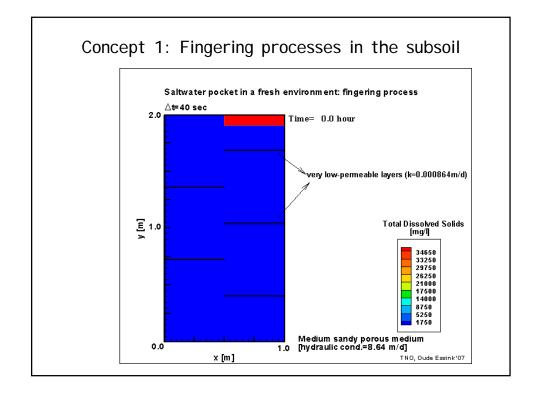


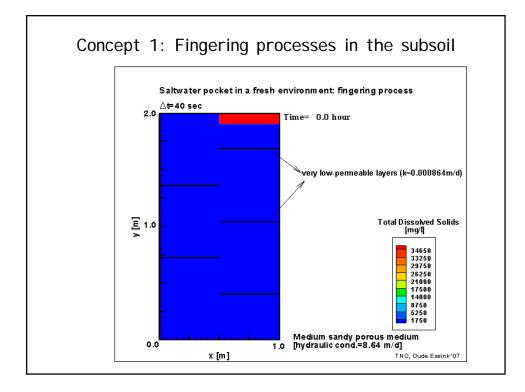


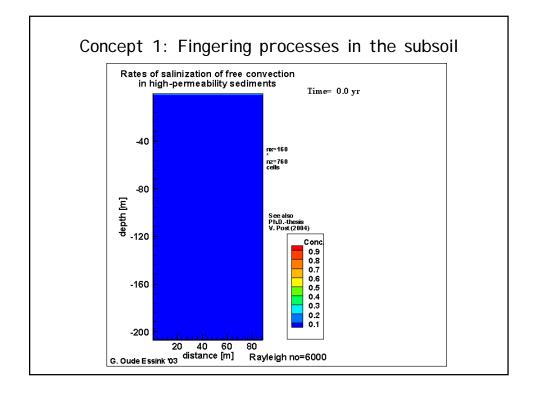


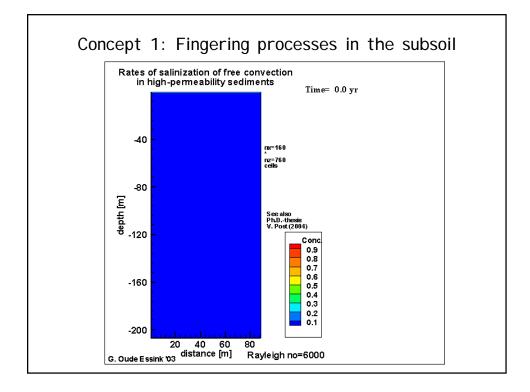


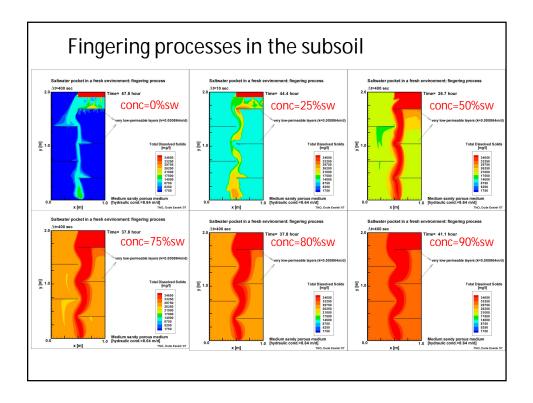


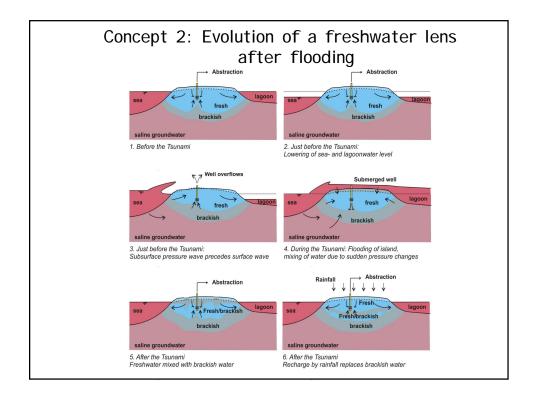


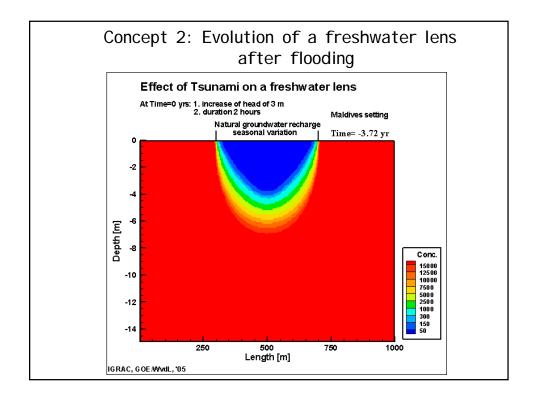


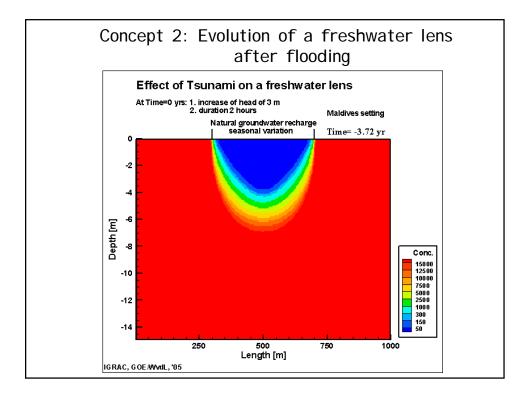


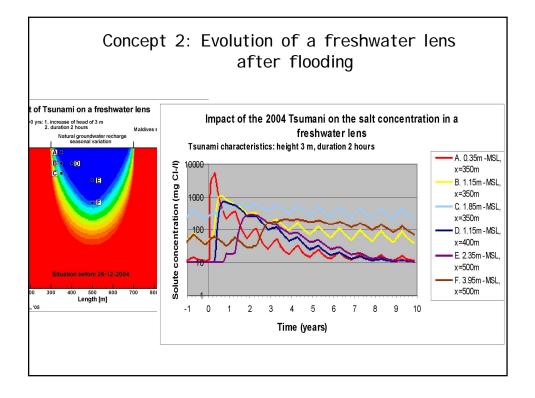


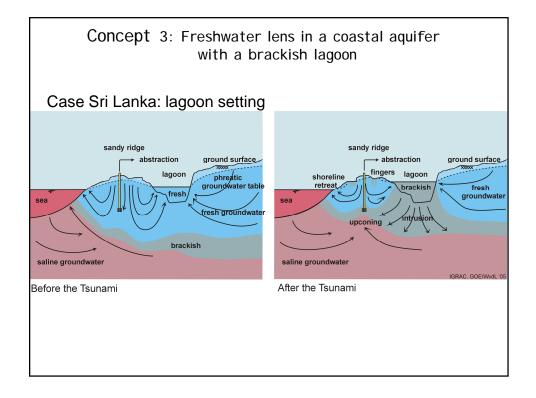


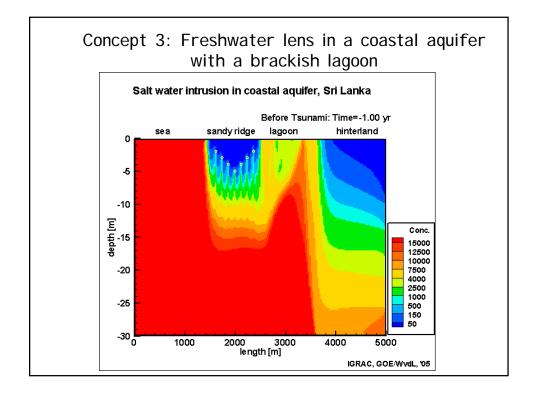


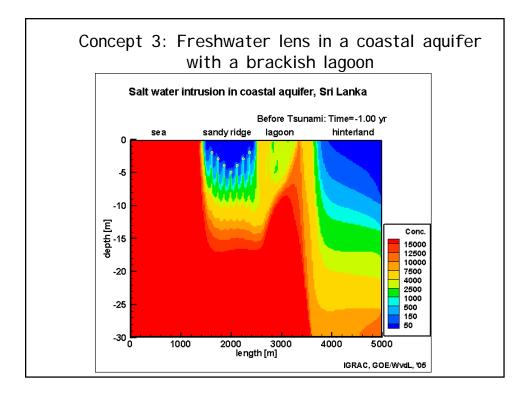


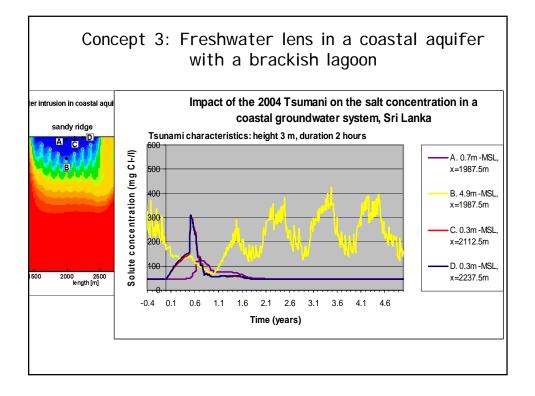


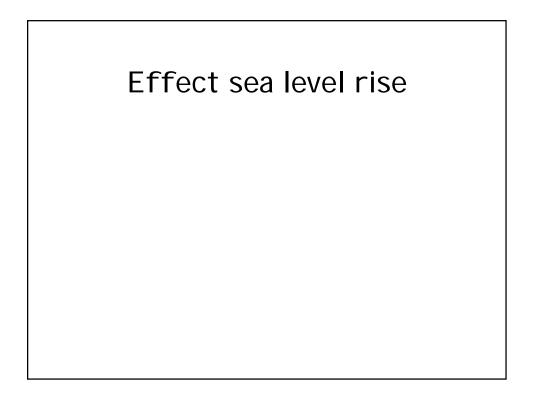






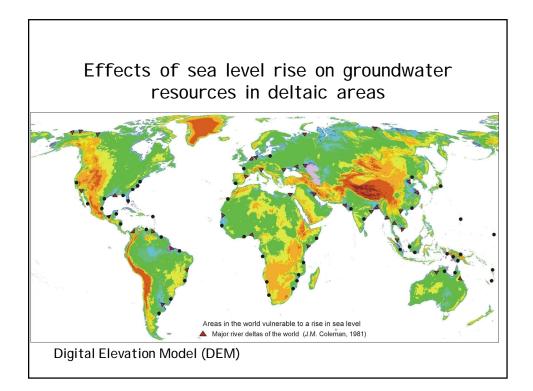


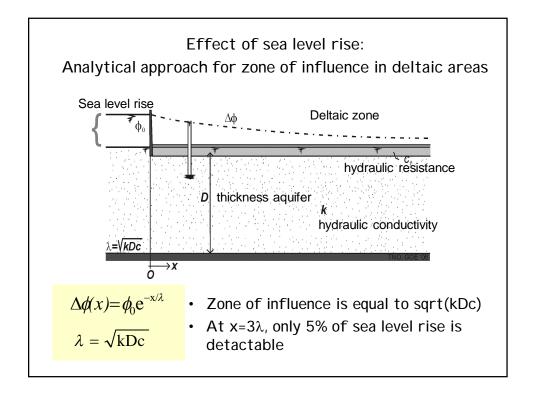


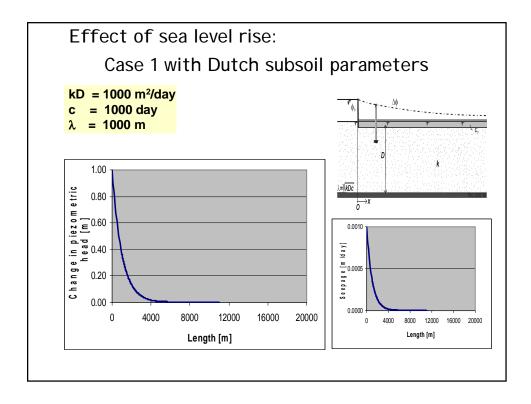


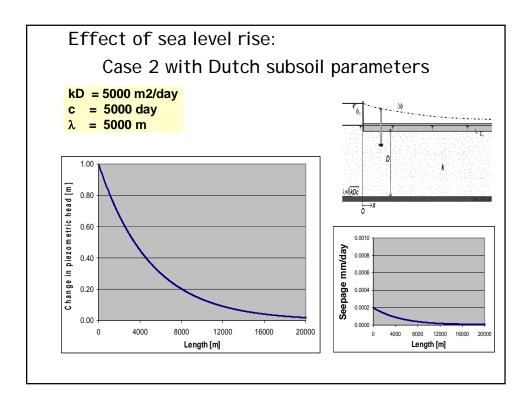
Effects of sea level rise on groundwater resources in deltaic areas

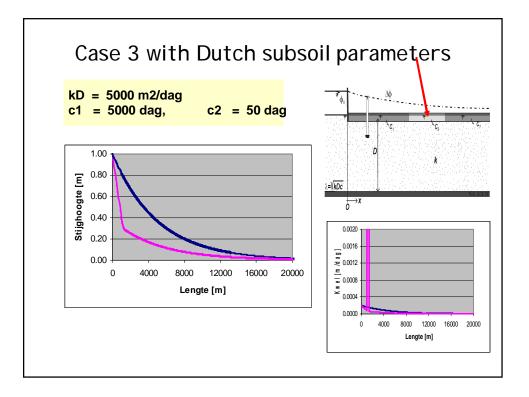
- 1. Increase of salt water intrusion
- 2. I ncrease of upconing under groundwater extraction wells
- 3. Increase of piezometric head
- 4. I ncrease of seepage and salt load to the surface water system
- 5. Risk of instable Holocene aquitards
- 6. [Decrease of fresh groundwater reservoirs due to decrease in natural groundwater recharge]



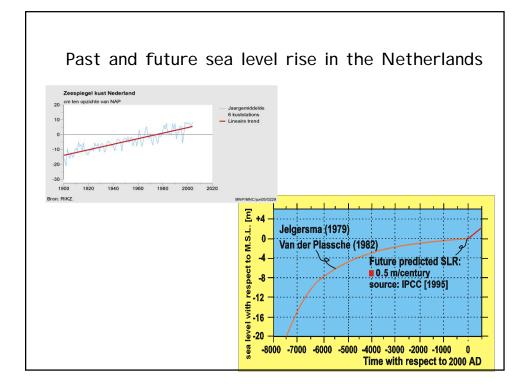




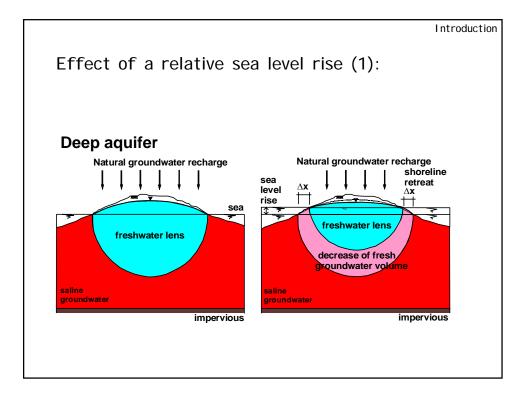


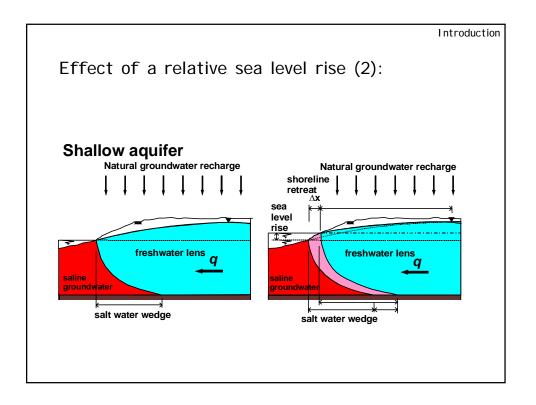


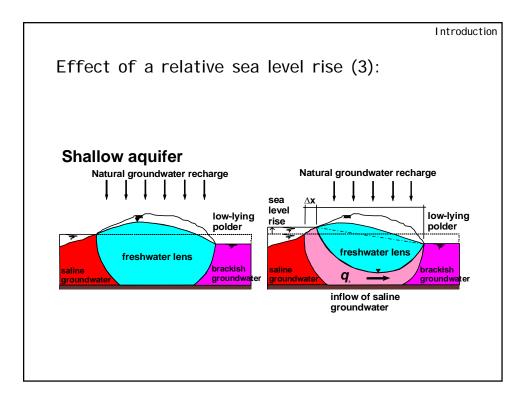


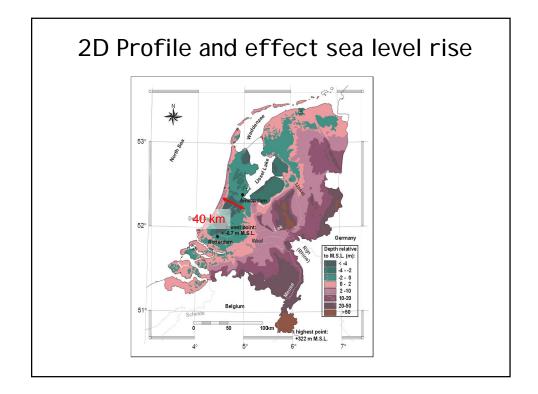


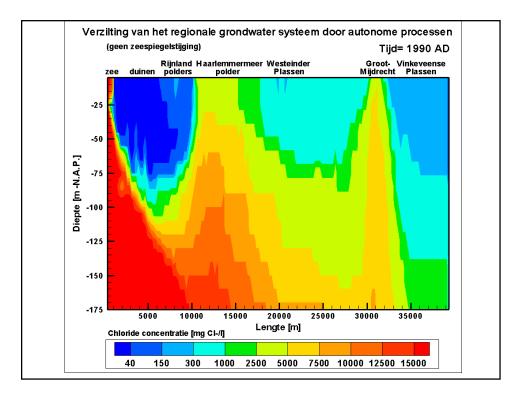
	0.0		C		***	G	C
21	00	G	G+	W	W+	C	C+
Worldwide temperature rise in 2050		+1°C	+1°C	+2°C	+2°C	+3°C	+3°C
Worldwide temperature rise in 2100		+2°C	+2°C	+4°C	+4°C	+6°C	+6°C
Change in airstream pattern Western Europa		no	yes	no	yes	no	yes
Winter	Average temperature	+1,8°C	+2,3°C	+3,6°C	+4,6°C	+5,4°C	+6,9°C
	Coldest winter day each year	+2,1°C	+2,9°C	+4,2°C	+5,8°C	+6,3°C	+7,8°C
	Average precipitation	7%	14%	14%	28%	21%	42%
Summer	Average temperature	+1,7°C	+2,8°C	+3,4°C	+5,6°C	+5,1°C	+8,4°C
	Hottest summer day each year	+2,1°C	+3,8°C	+4,2°C	+7,6°C	+6,3°C	+11,4° C
	Average precipitation	6%	-19%	12%	-38%	18%	-57%
Sea level rise	Absolute rise (cm)	35-60	35-60	40-85	40-85	45-110	45-110

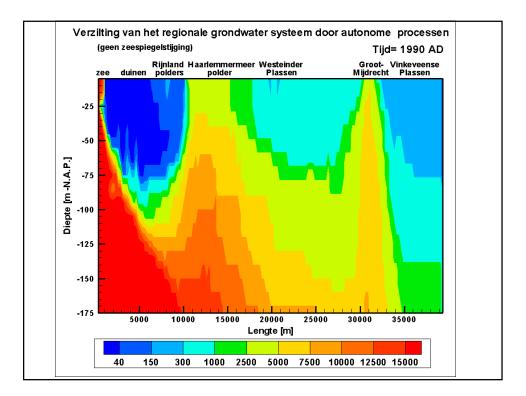


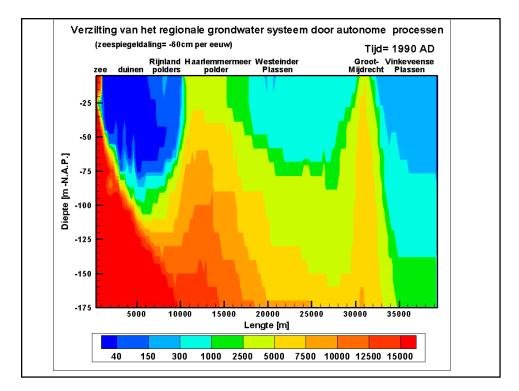


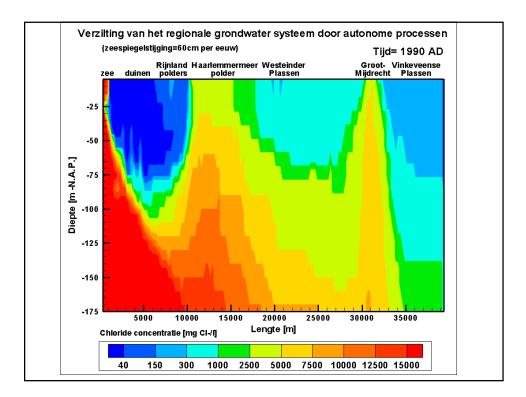


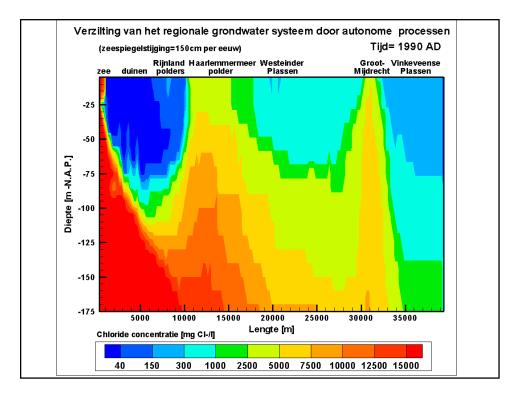


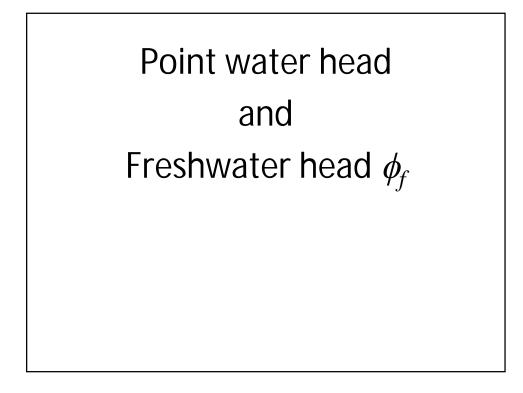


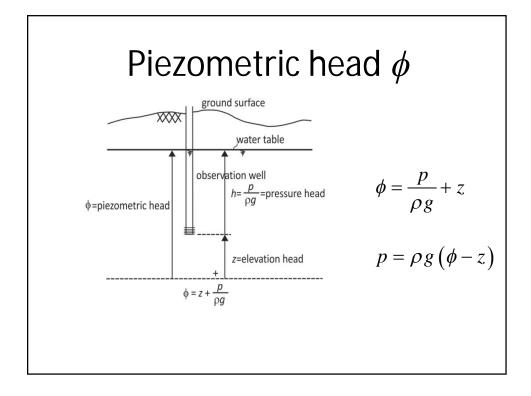


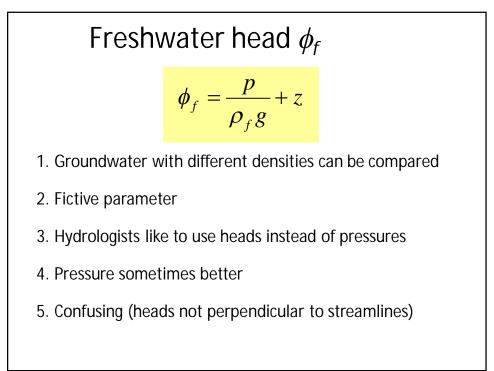










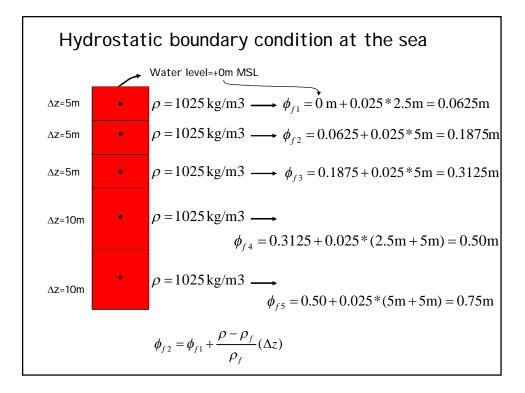


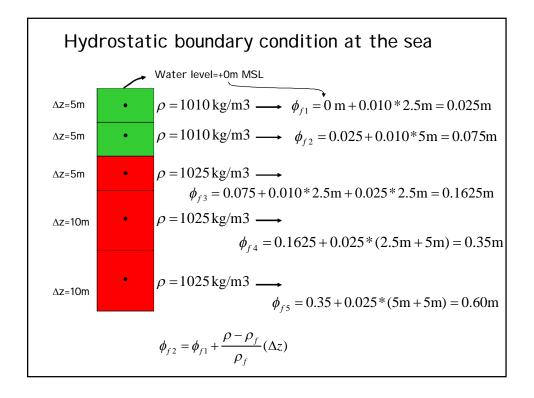
Freshwater head
$$\phi_f$$

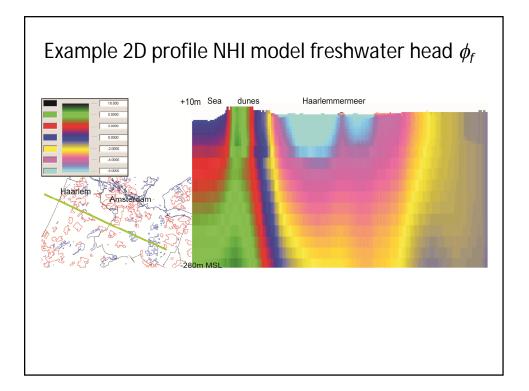
 $h_f = \frac{\rho}{\rho_f} h$
 $\phi_f = h_f + z$
 $\phi_f = \frac{\rho}{\rho_f} h + z$
 $\phi_f = \frac{\rho}{\rho_f} h + z$
 $h=10m$
 $\phi_f = 10.25 \text{kg/m3}$
 $h=10.25 \text{m}$

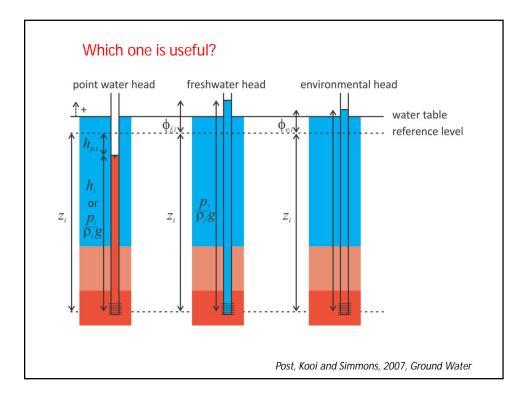
Special case: hydrostatic pressure:
$$q_z = 0$$

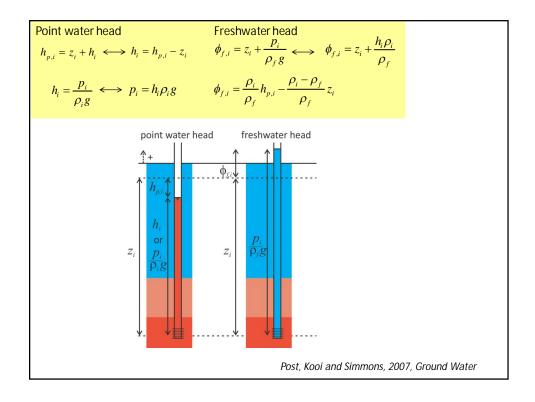
 $q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$ no vertical flow
 $0 = \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$
 $\partial \phi_f = -\frac{\rho - \rho_f}{\rho_f} \partial z$
 $\phi_{f2} = \phi_{f1} - \frac{\rho - \rho_f}{\rho_f} (z^2 - z^4)$
 $\downarrow + \qquad \phi_{f2} = \phi_{f1} + \frac{\rho - \rho_f}{\rho_f} (\Delta z)$

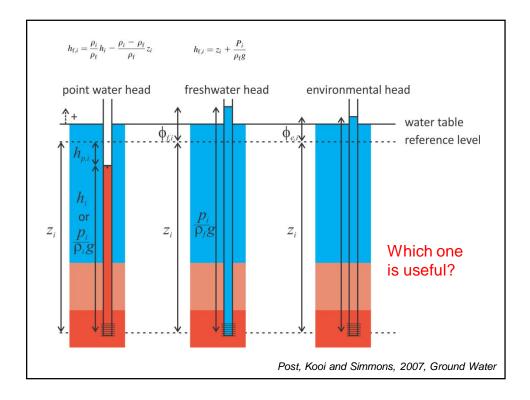


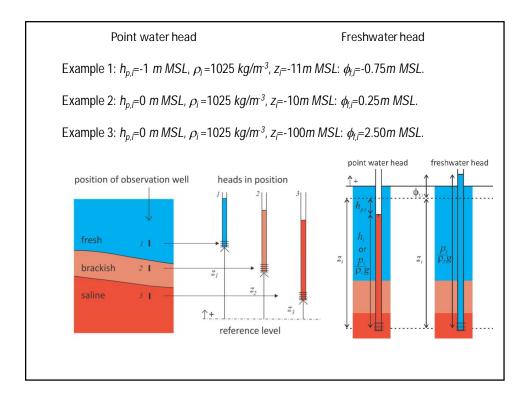


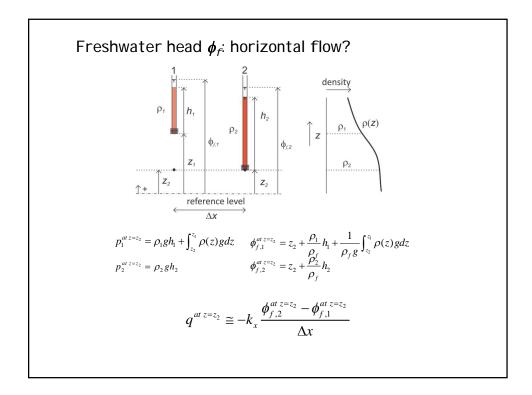


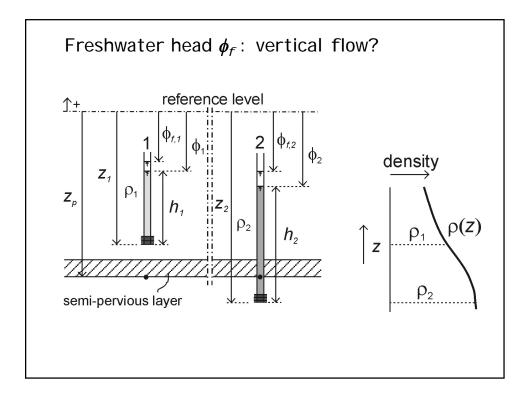


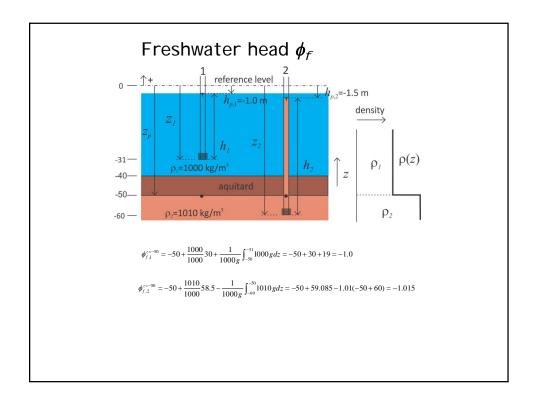


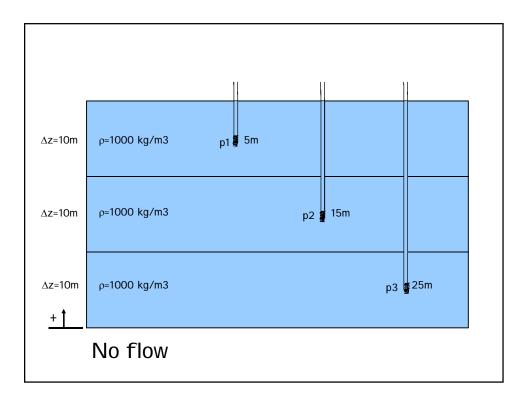


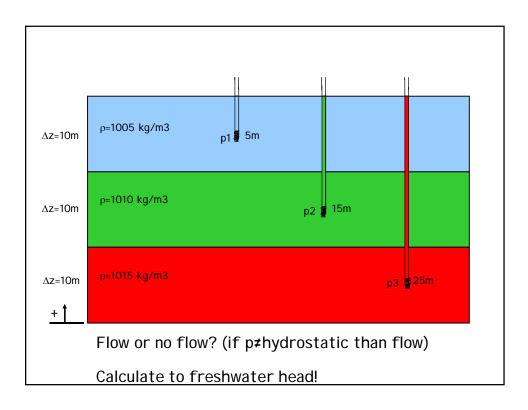


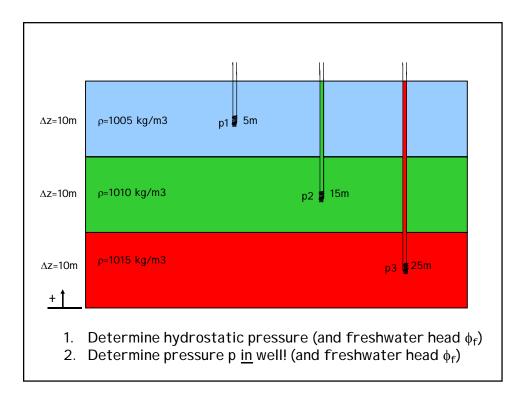


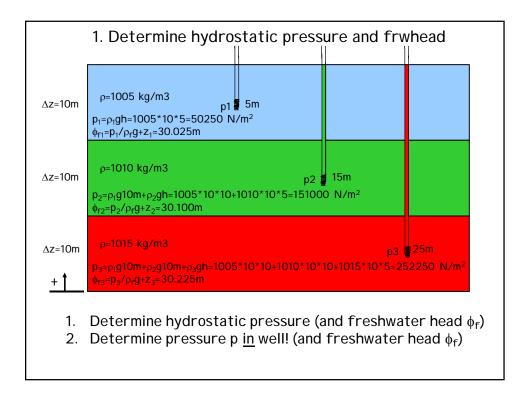


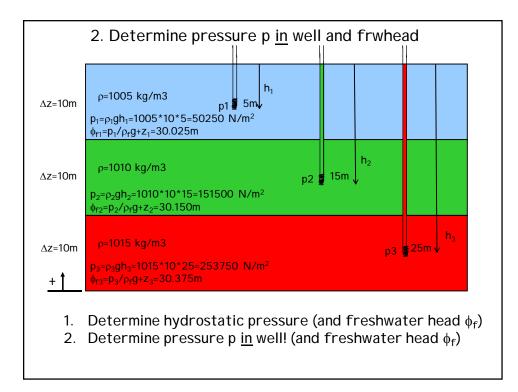


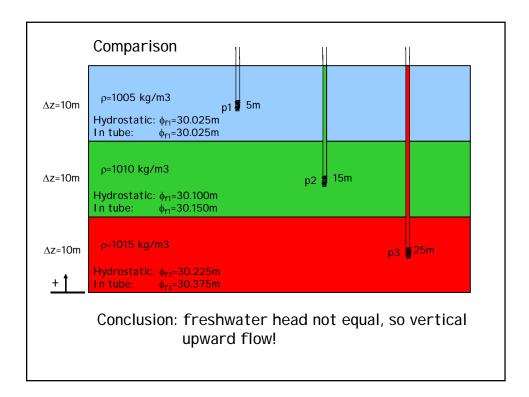


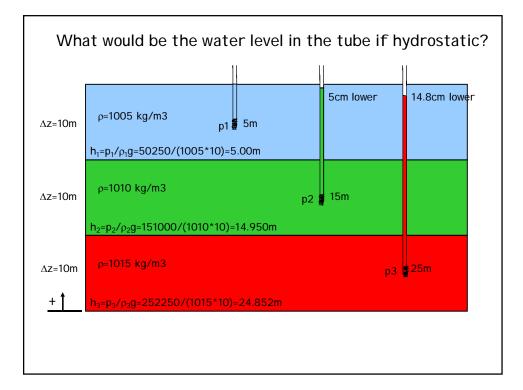


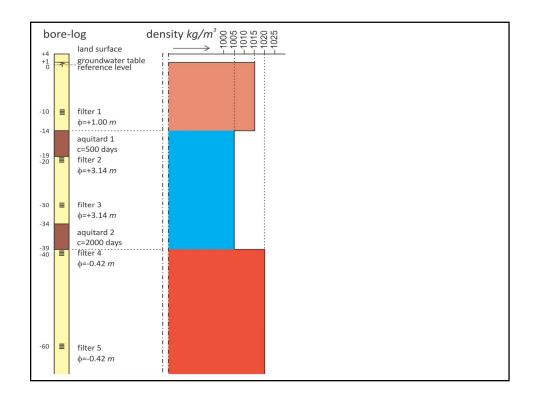




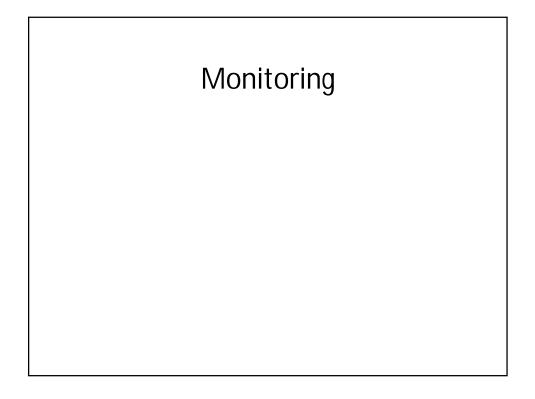


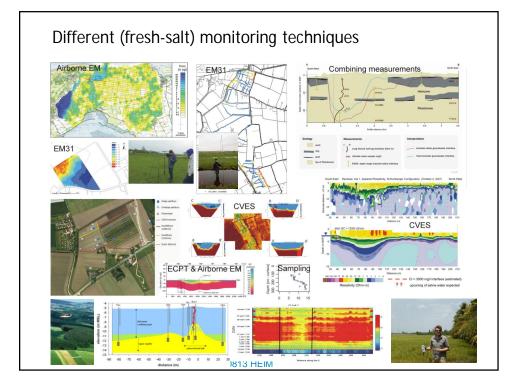


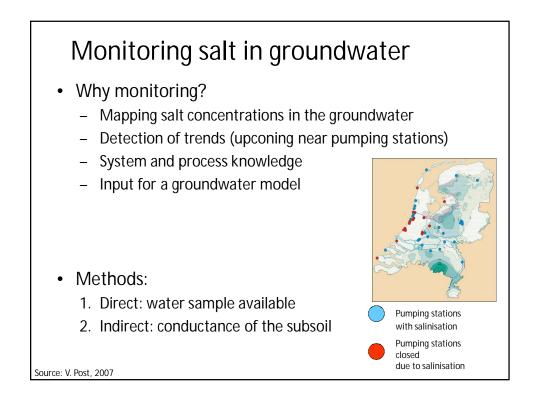


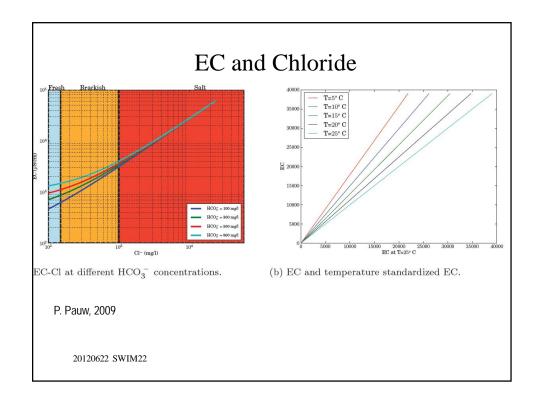


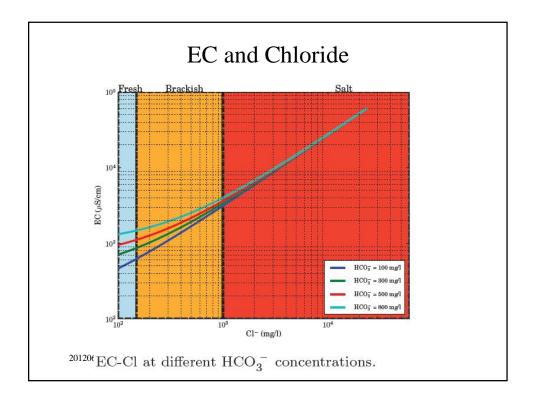
In coastal area (with fresh-brackish-saline groundwater), always measure head and Electrical Conductivity (EC) Convert EC to density Determine freshwater head with lecture notes and ppt Determine flow

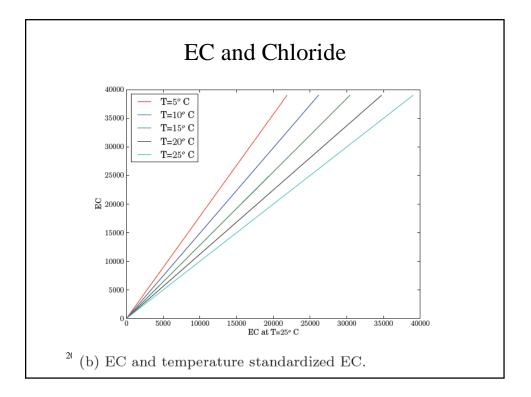












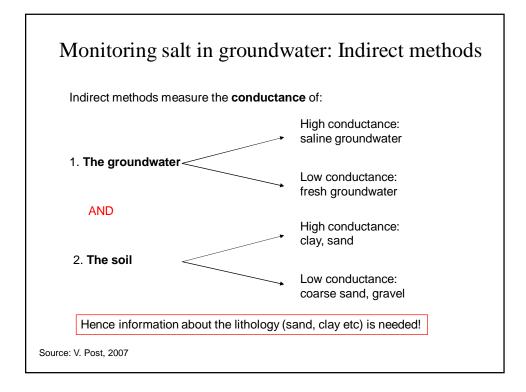
Measuring system	Physical parameter	Geology/terrain information
radar	EM traveltime	Terrain elevation
Infrared photography	Infrared radiation	Surface temperature
Time domain EM Frequency domain EM	Electr. resistivity from induced EM fields	Lithology Water salinity
Magnetic gradiometer	Magnetic field (variations)	Lithology (magnetite) Artefacts Steel/Iron objects
Spectral gamma	Radiation (gamma)	Soil type Surface lithology Recent disturbence

Surfa	Surface measurements	
Measuring system	Physical parameter	Geology/terrain information
Ground penetrating radar	EM traveltime, diaelectric constant,	Lithology Soil moisture
ERT	Electr. resistivity	Lithology Water salinity
Time domain EM Frequency domain EM	Electr. resistivity	Lithology Water salinity
Magnetometer (total field, gradiometer)	Magnetic field (variations) magnetic susceptibility	Lithology (magnetite) Artefacts Steel/Iron objects (UXO)
Spectral gamma	Radiation (gamma)	Soil type Surface lithology Recent disturbence

Measuring system	Physical parameter	Geology/terrain informatio
mechanical CPT	Cone resistance Friction resistance	Lithology Geotechnical parameters
Electrical conductivity	Electrical formation conductivity	Water salinity
Contnuous water pressure	Water pressure	Lithology Piezometric head
Water pressure dissipation in clay layers	Water pressure in time	Permeability clays
BAT sampling in CPT casing		Water chemistry
ROST, MIP		Contamination of hydrocarbons (high concentration)
Camera sonde	Visual view	Lithology, contamination, ga

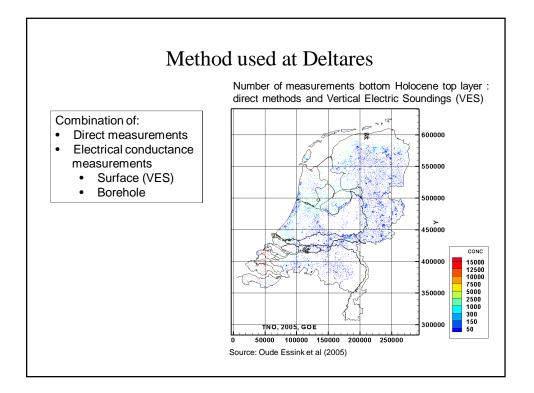
Monitoring salt in groundwater: Direct methods
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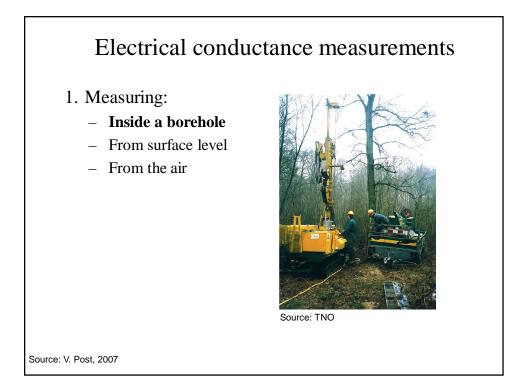
Method	Advantage	Disadvantage
1. Observation well	•High accuracy	•Costly
	•Detection trends	•Point measurement
2. Well screens in	•High accuracy	•Costly
observation well	 Detection trends 	
	•High vertical resolution	on
3. Sediment sample	 High accuracy 	•Very costly and time
(extraction milliliters of water)	•High vertical resolution	on consuming
	Direct methods 1 and 2	
		Source: V. Post, 20

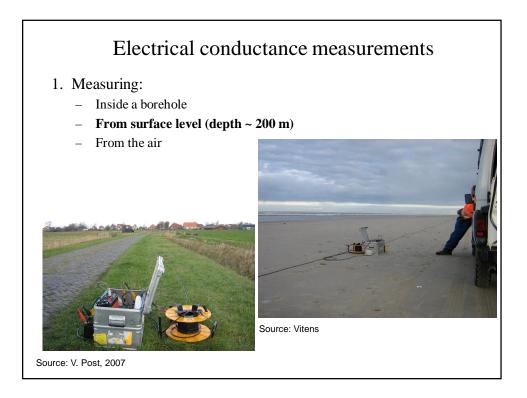


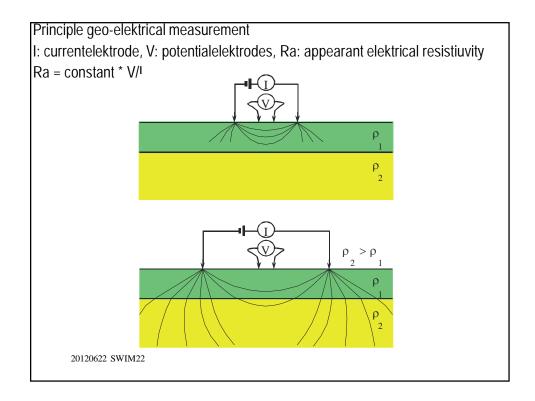
Method	Advantages	Disadvantages
1. Electrical conductance measurements	•High resolution (3D) •Depth ~200 m	•Time consuming
2. Electromagnetic measurements	•Fast	•Limited vertical resolution •Sensitive for underground conductors (pipes)
3. Satellites	•Suitable for large areas	•Small vertical resolution •Low accuracy

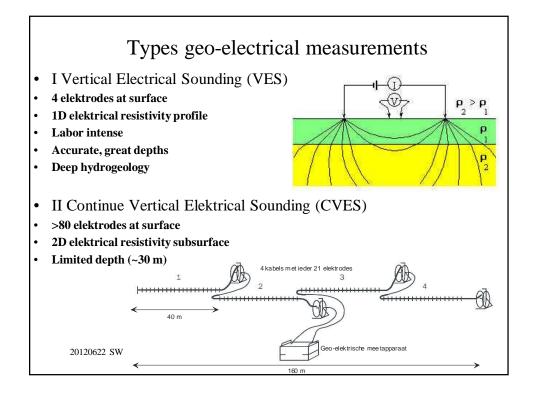
Source: V. Post, 2007



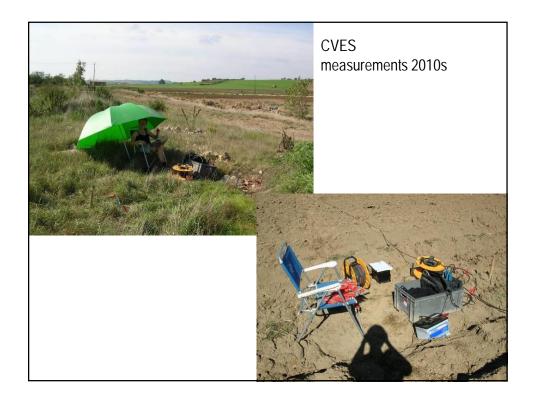


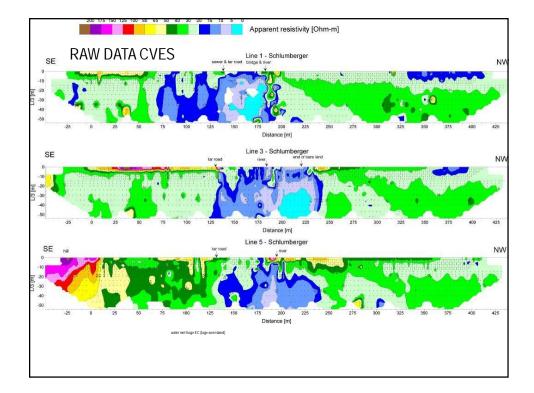


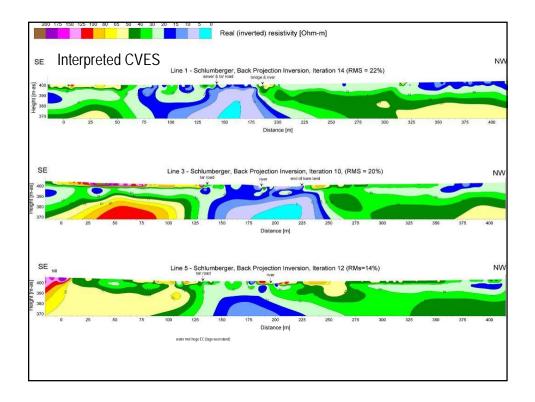


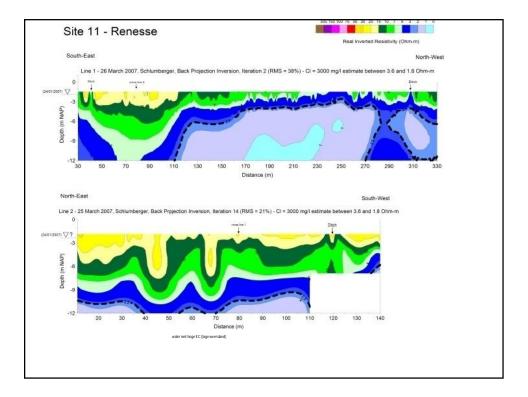


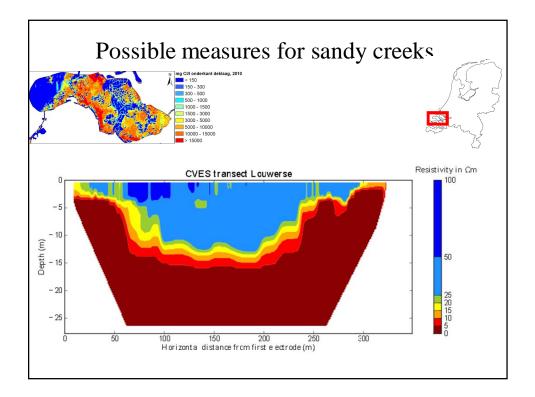


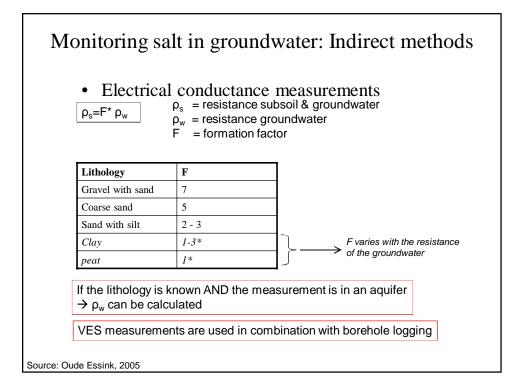


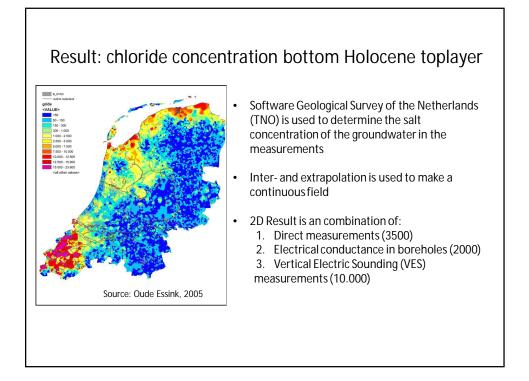


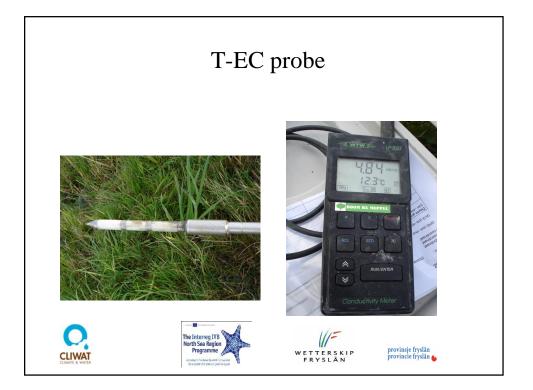


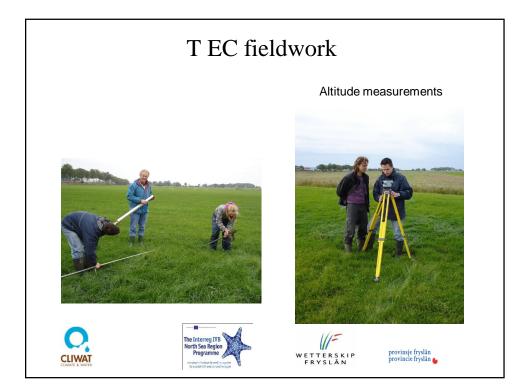




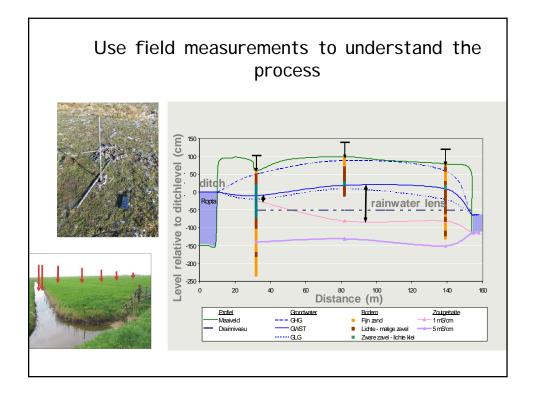


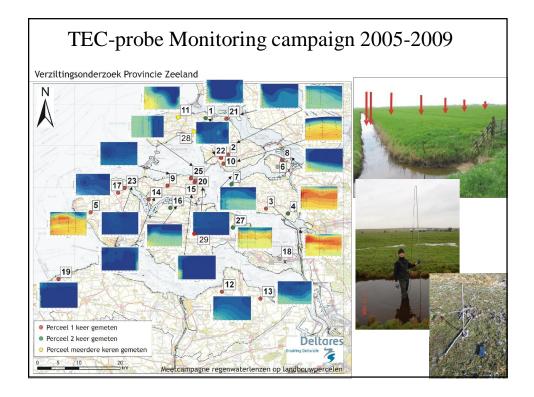


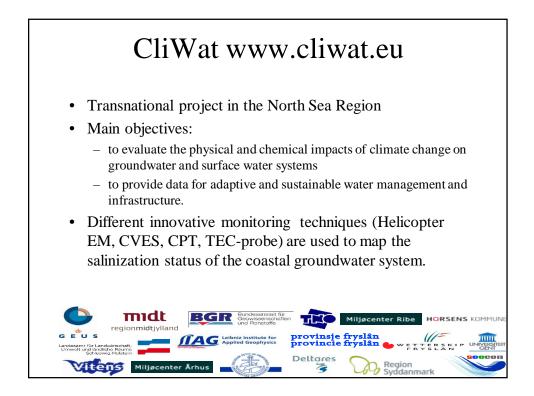


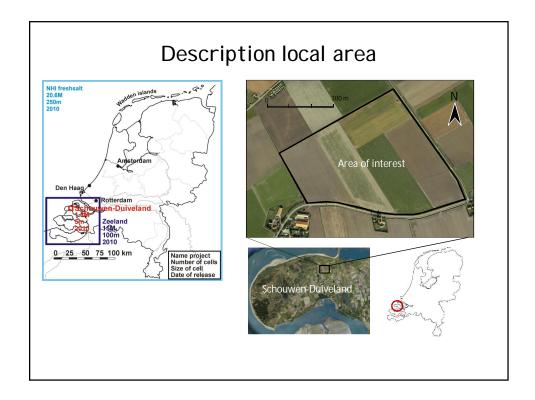


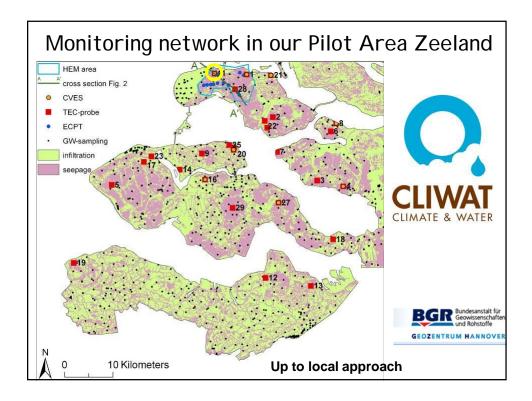


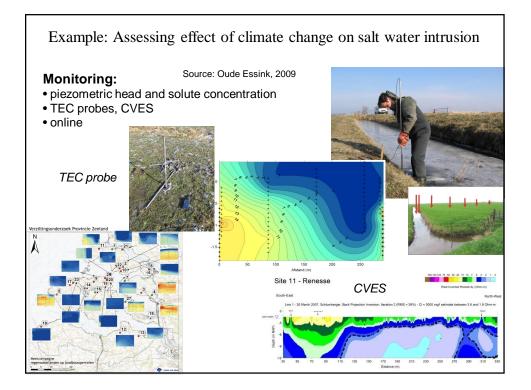




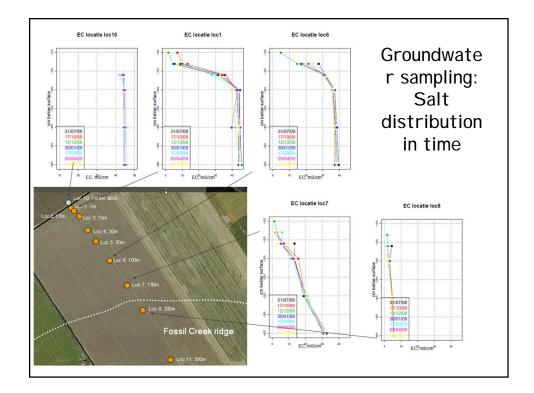


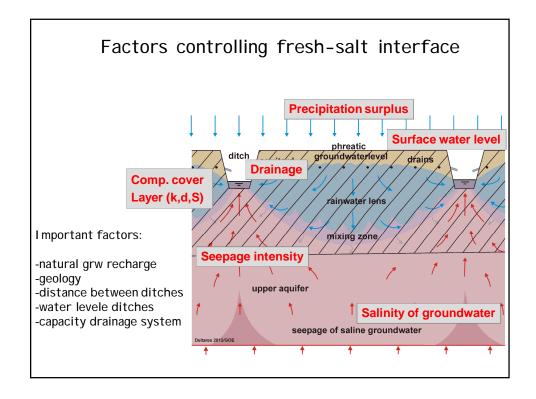


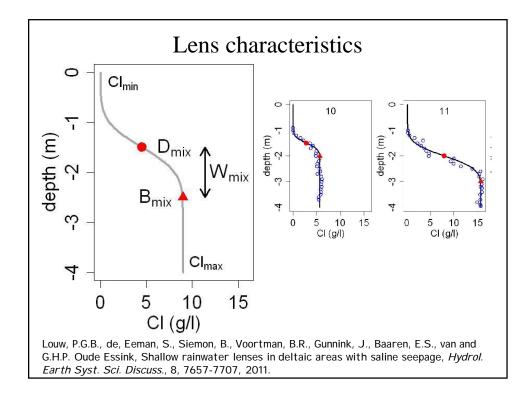


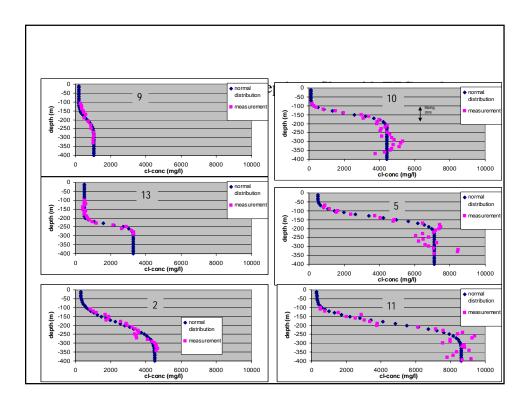


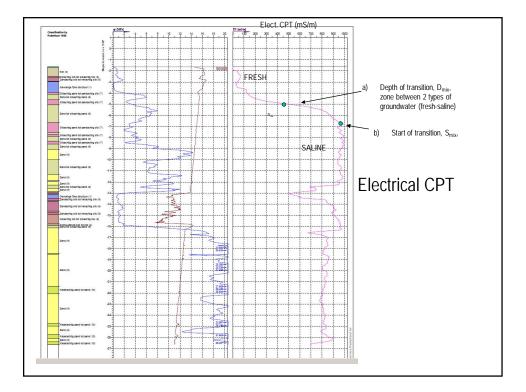


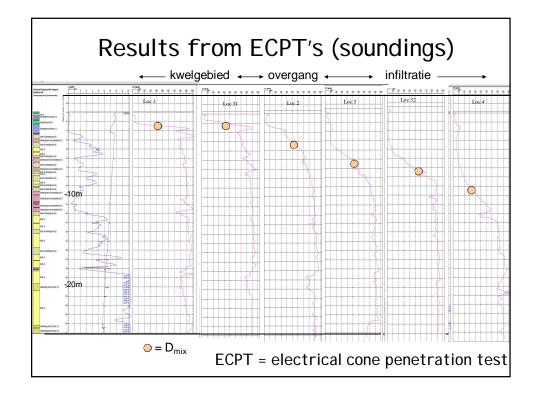


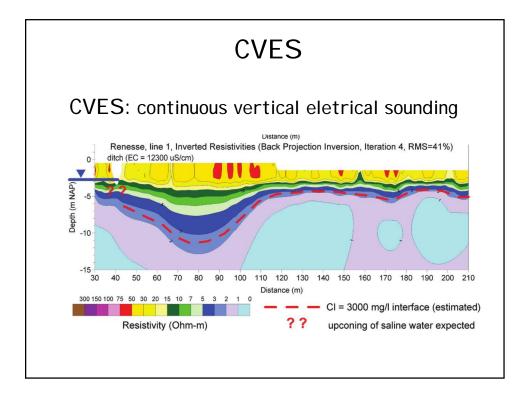


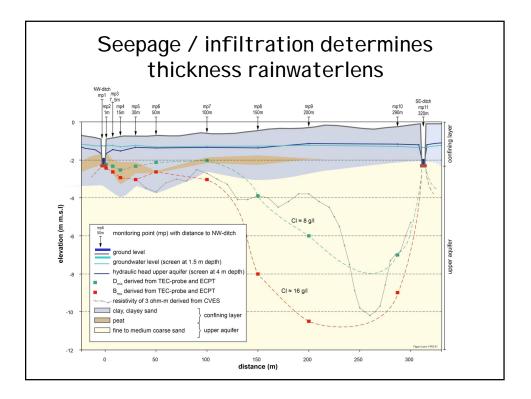


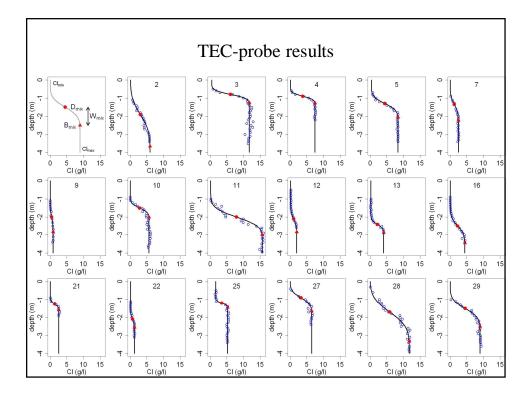


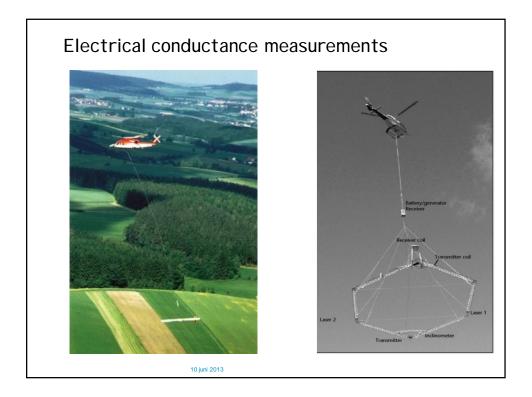


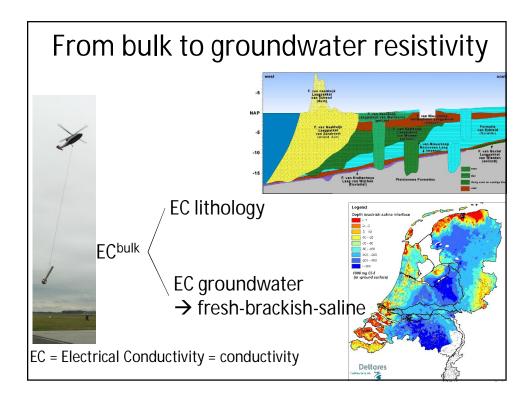


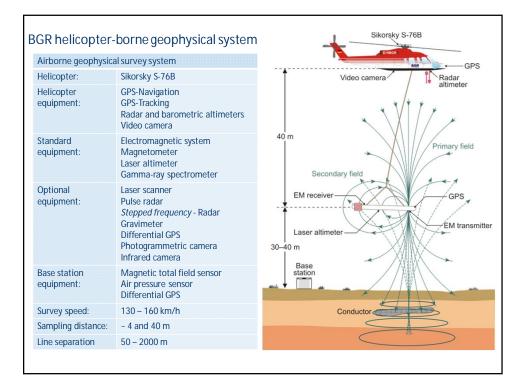


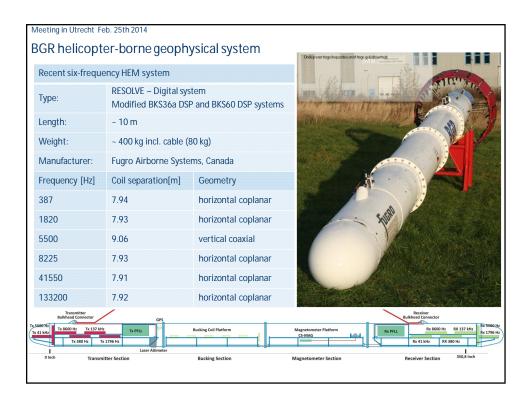


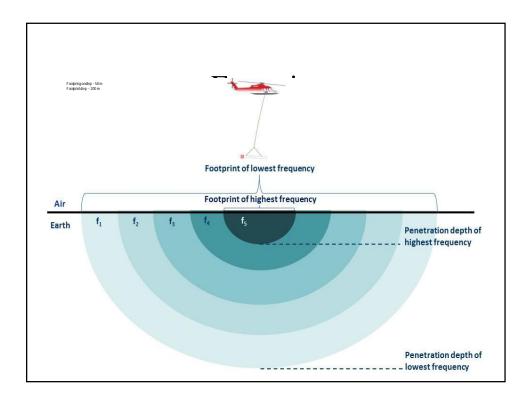


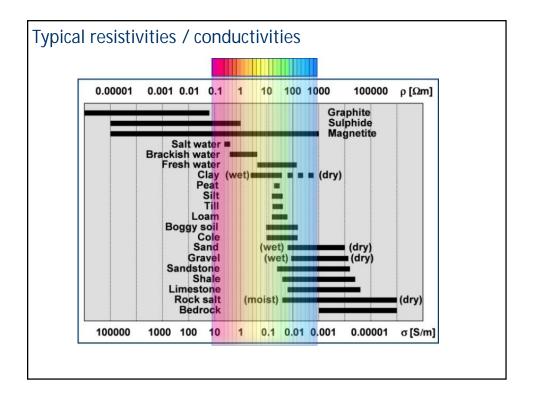


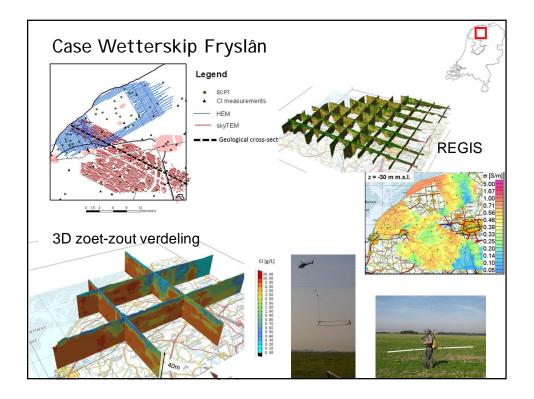


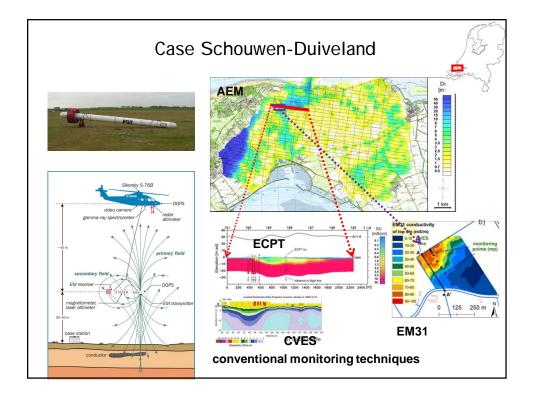


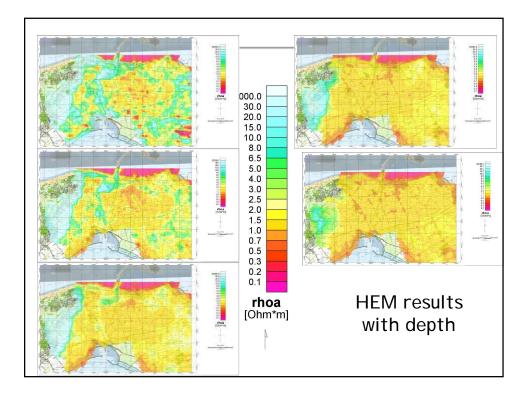


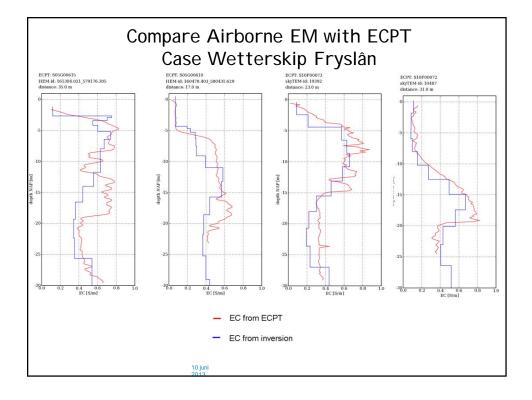


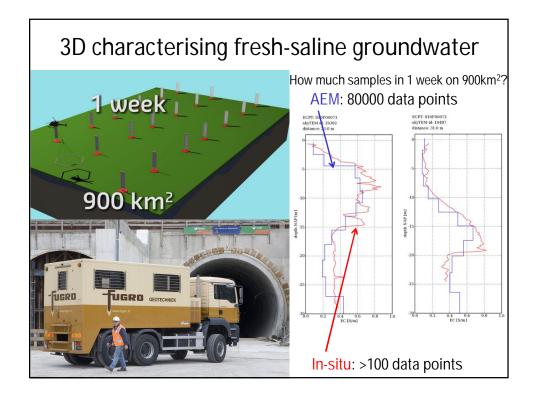


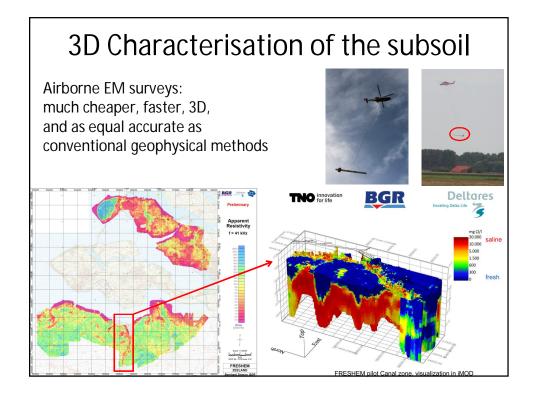


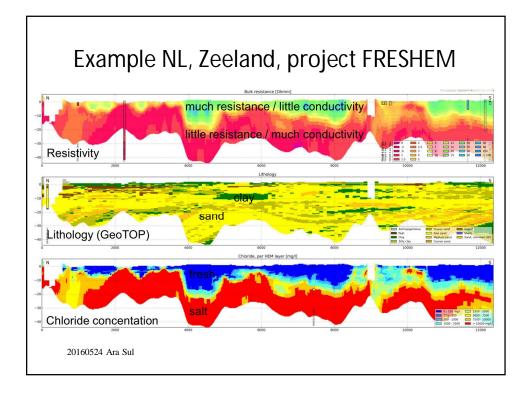


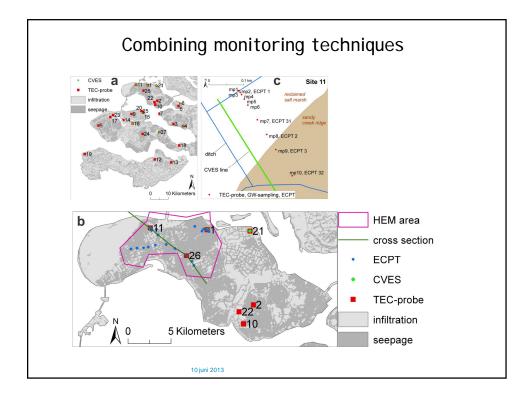


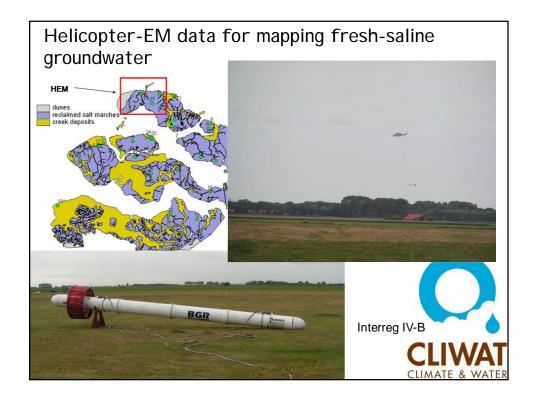


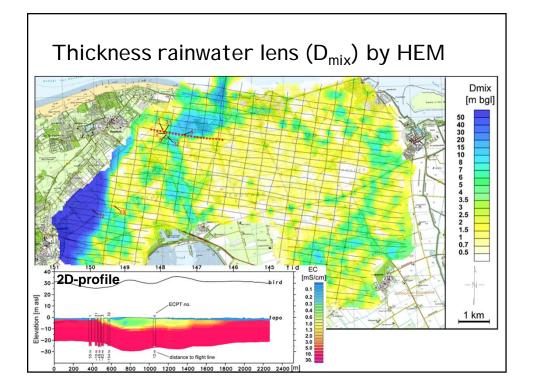


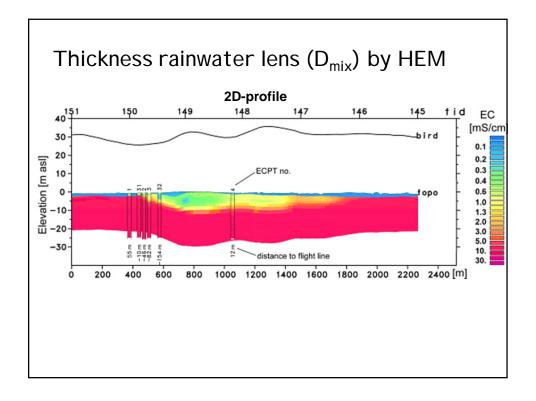


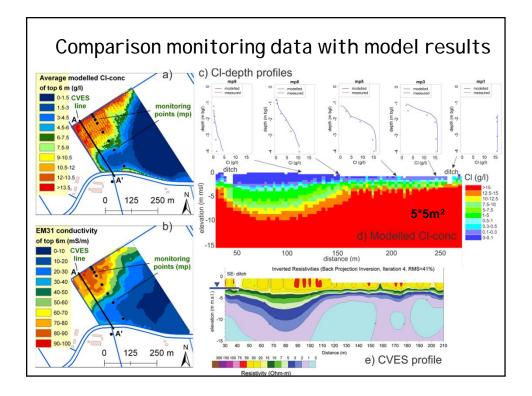


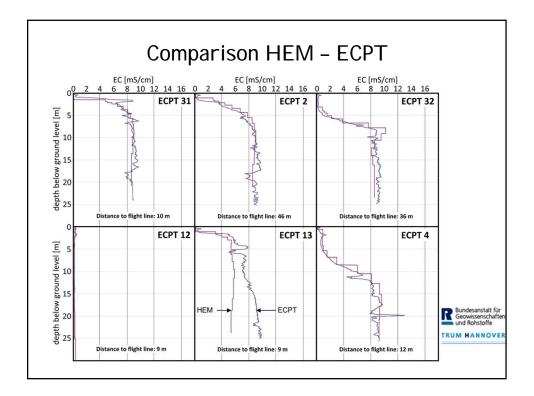


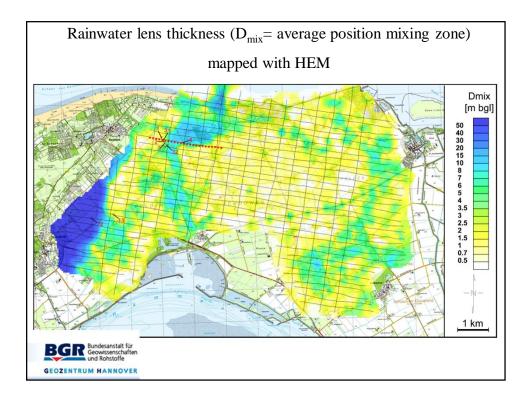


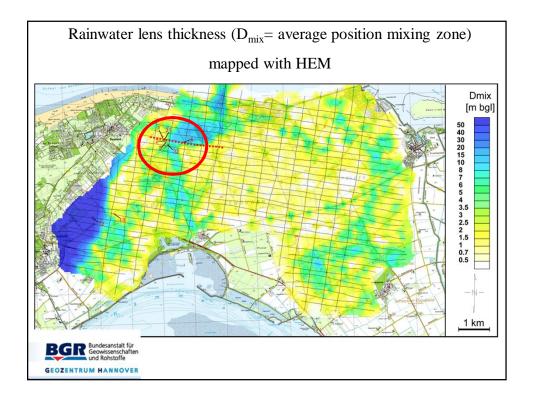


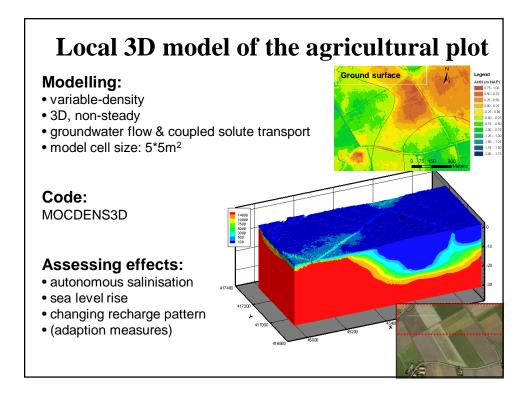


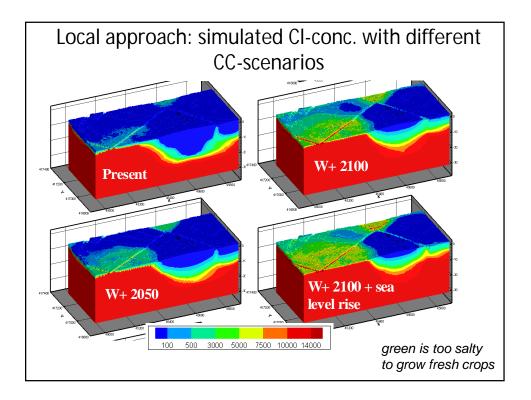


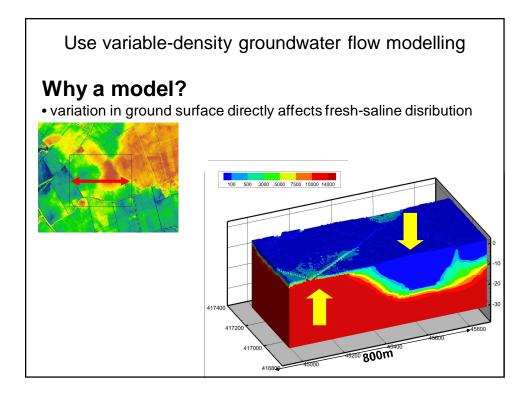


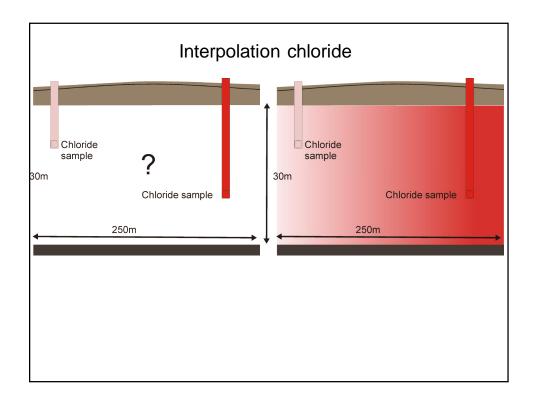


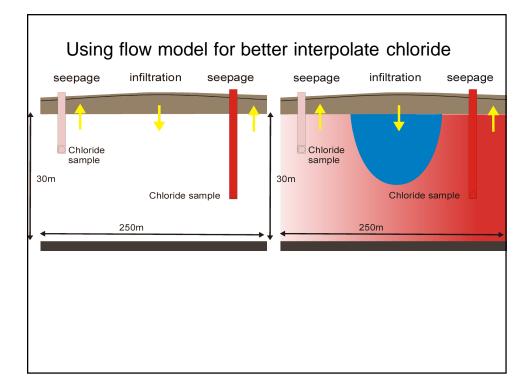


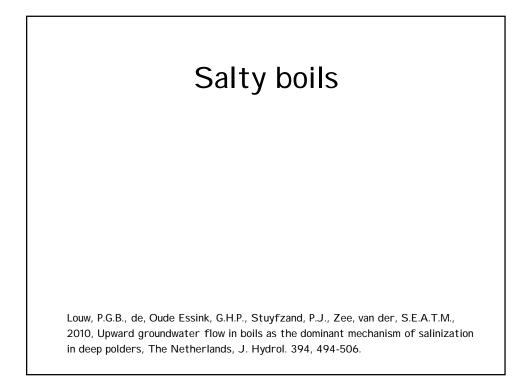


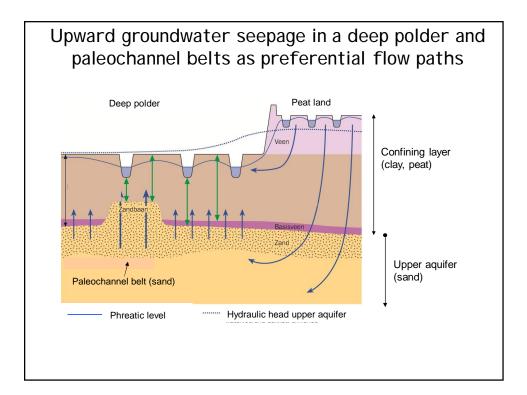


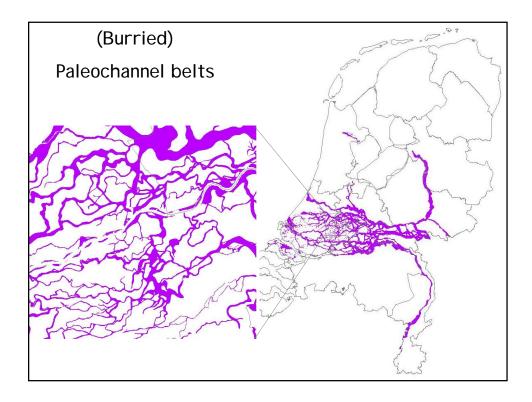


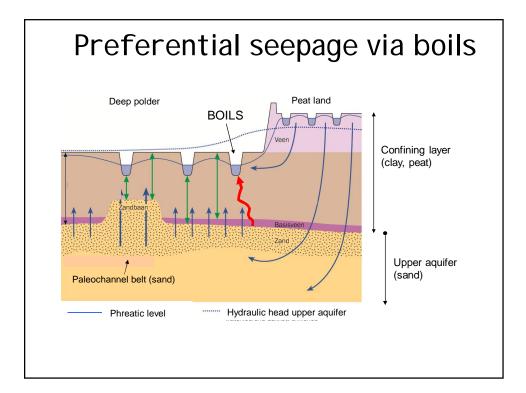




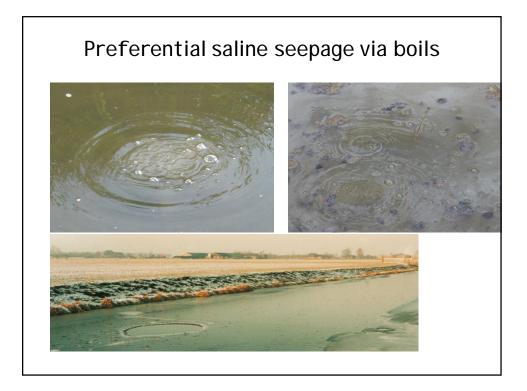


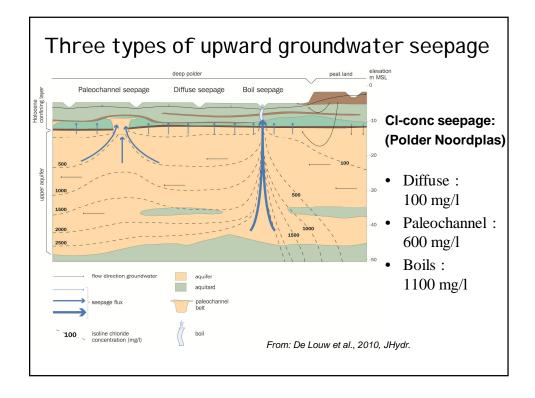








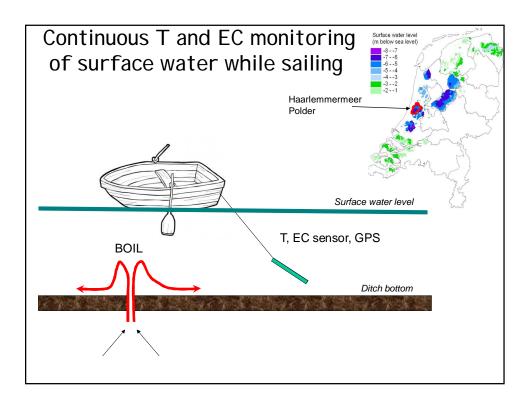


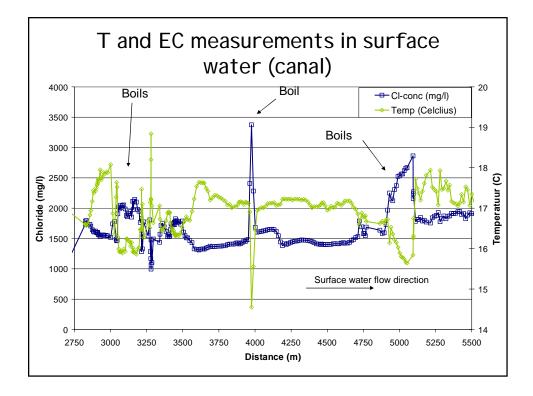


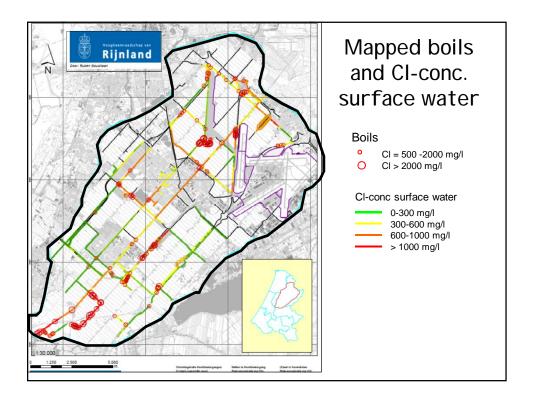


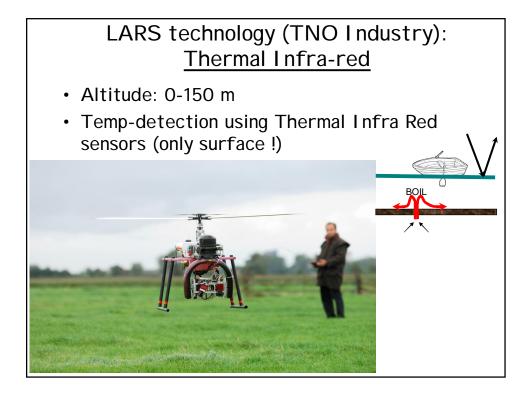




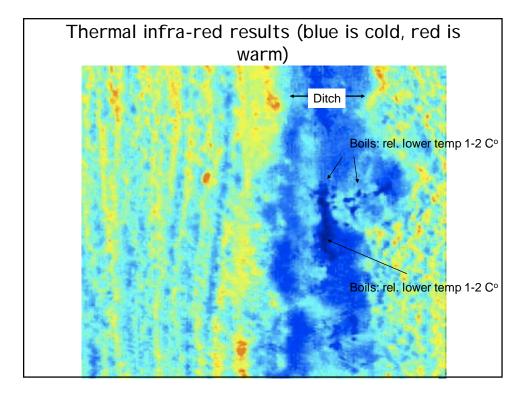


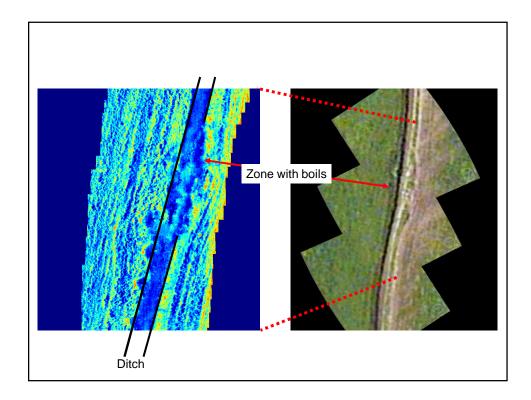


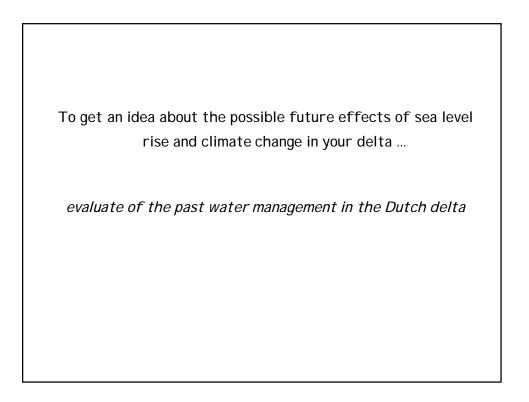


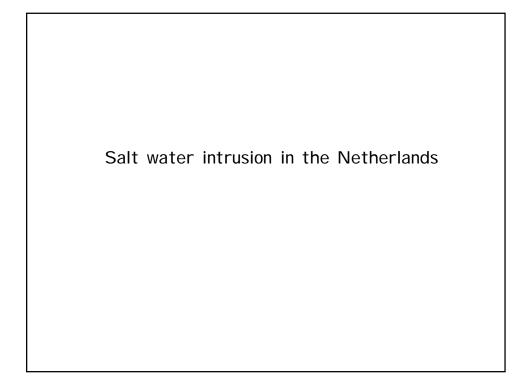




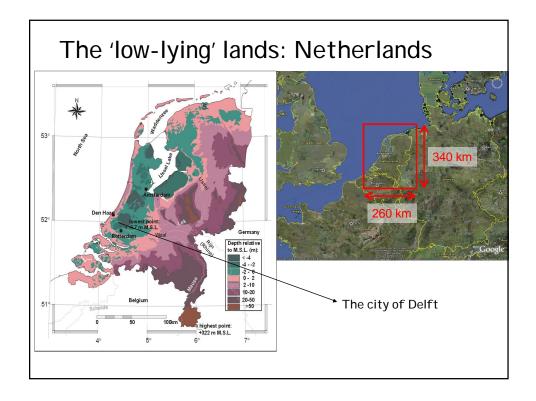




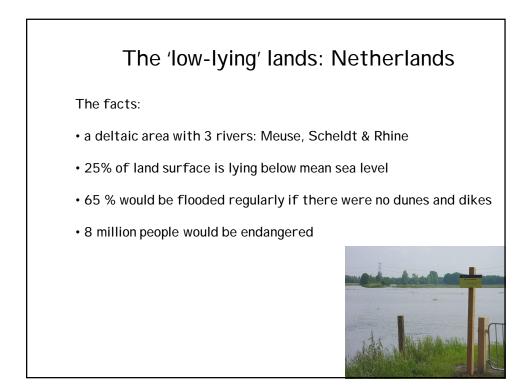


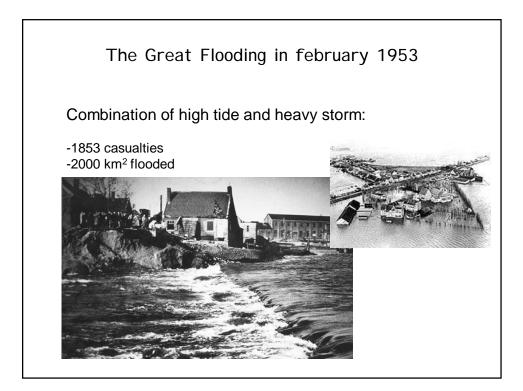




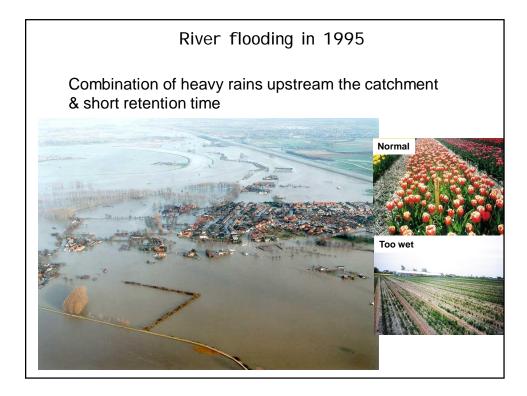


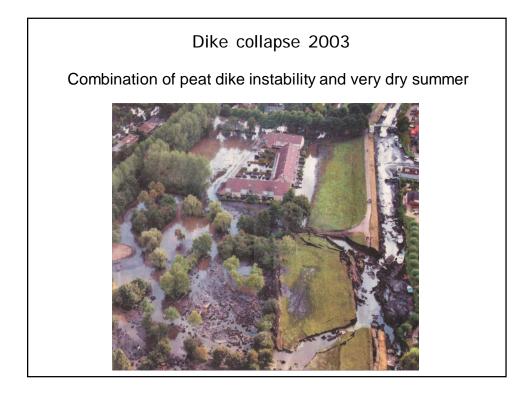




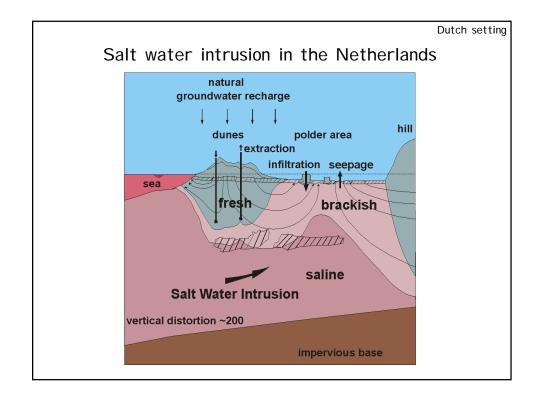


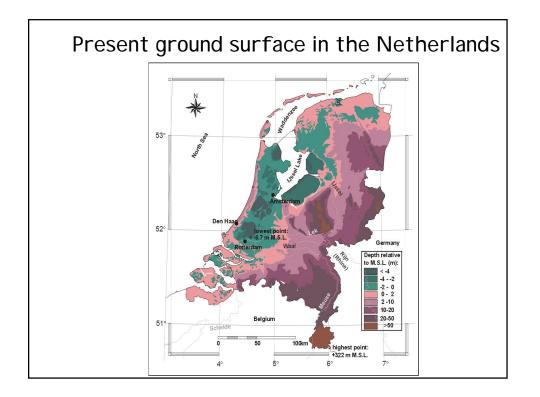


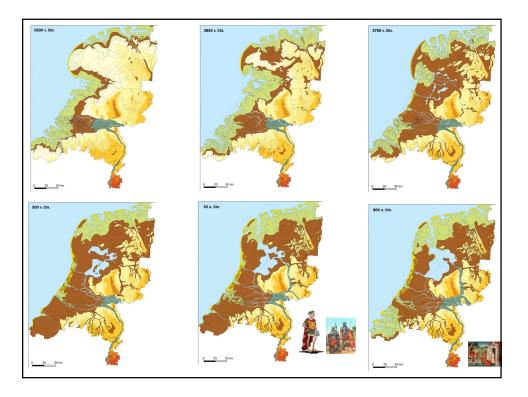


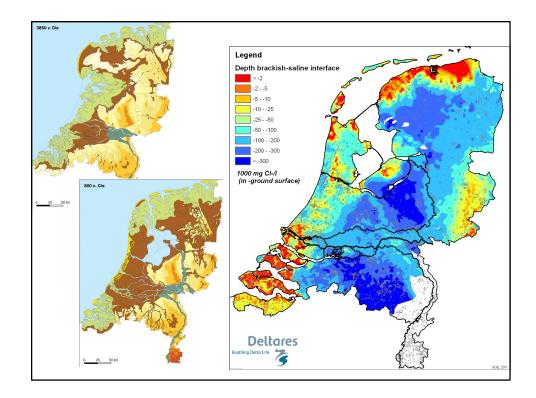


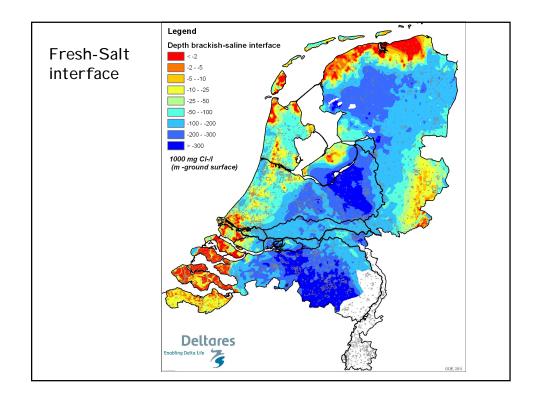
Estimated water ma 'to keep our	U
Costs up till 2050 in billic	on euros:
rivers: upper part	5.7
rivers: lower part	5.6
low-lands	1.7
coastal zone	8.0
infrastructure	3.5
purchase of ground	2.0
	+
	26.5 billion euros

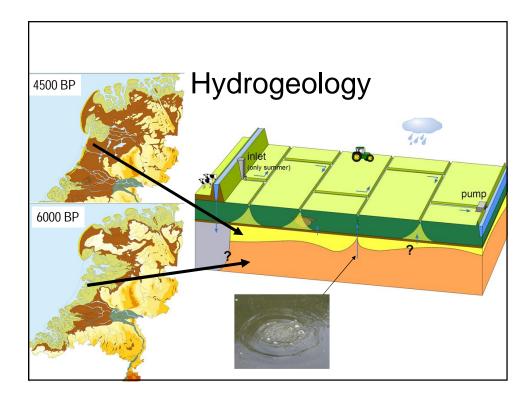




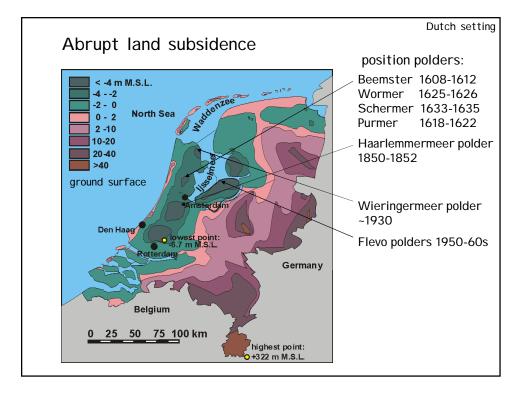


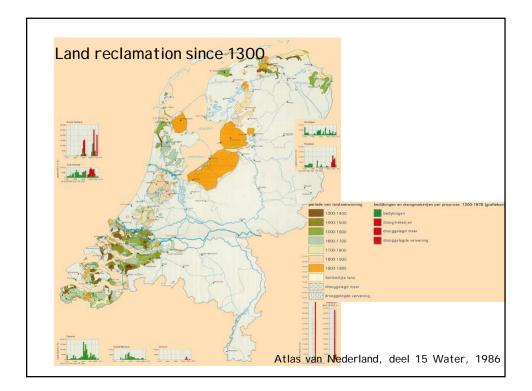


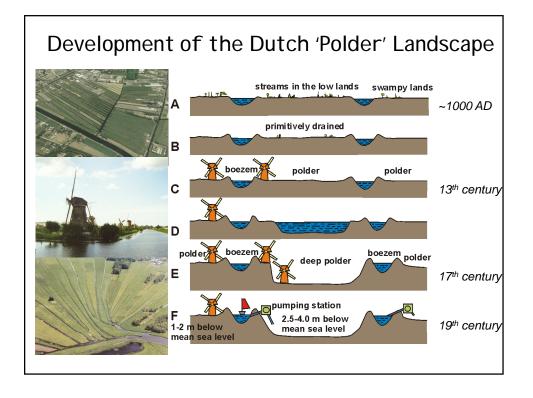


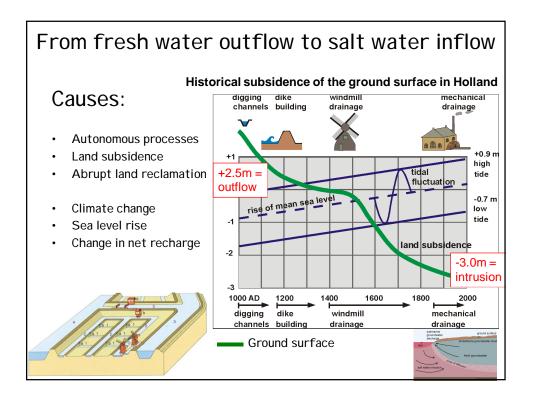


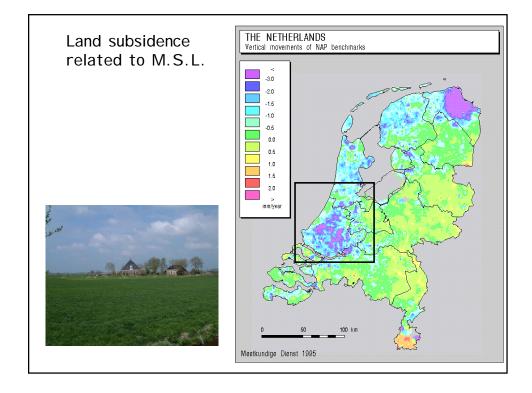




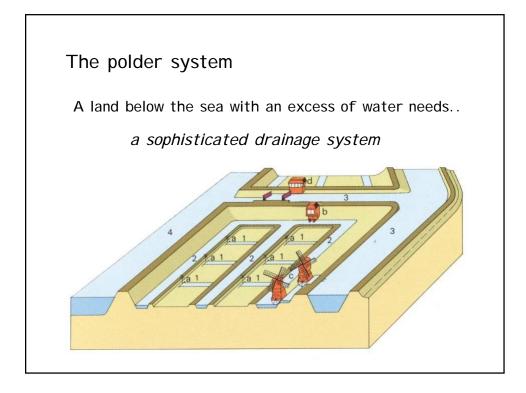


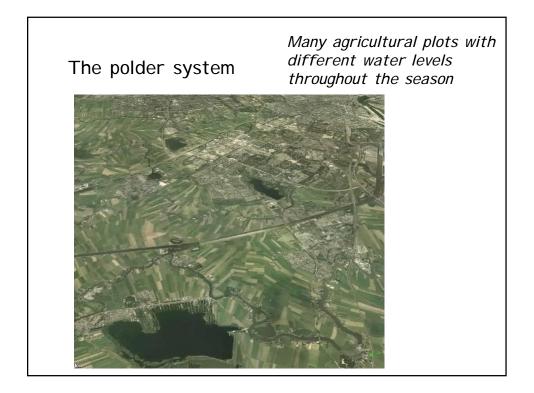


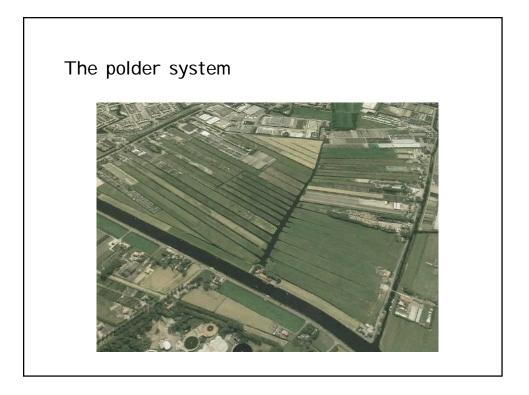


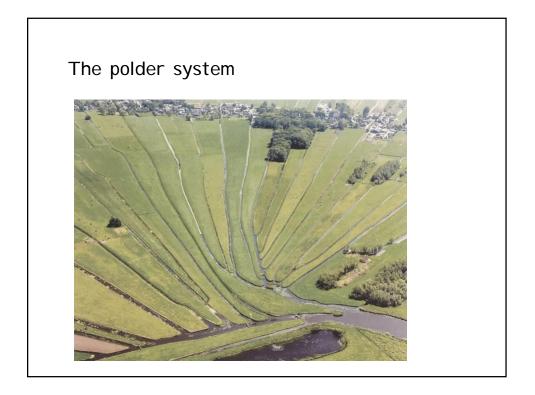


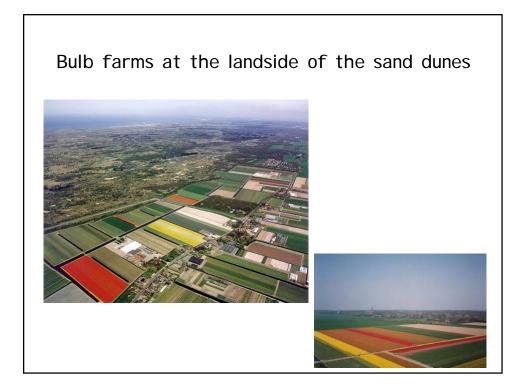


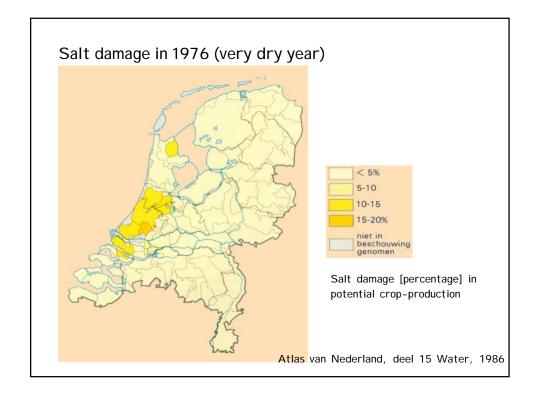


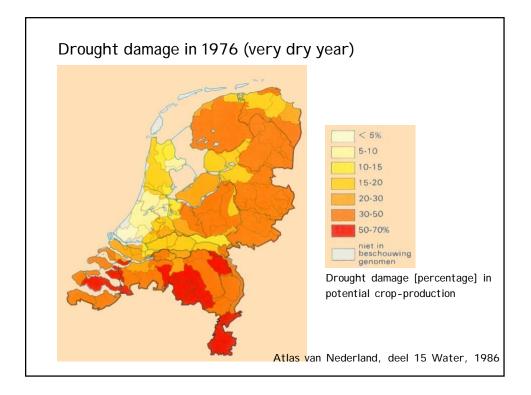


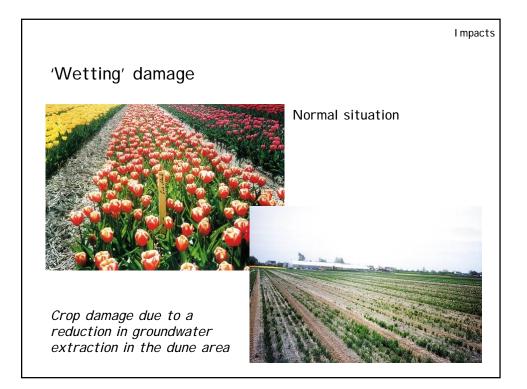


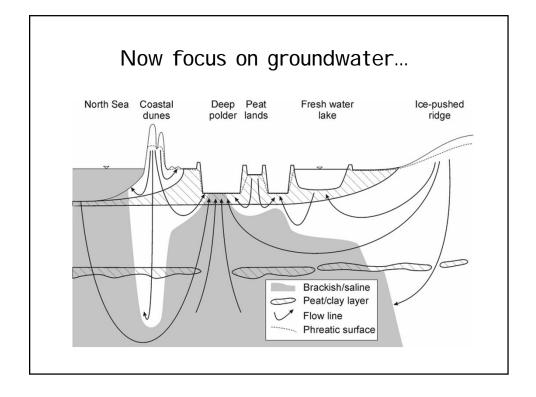


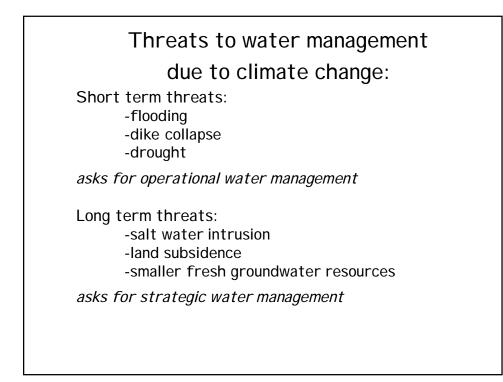


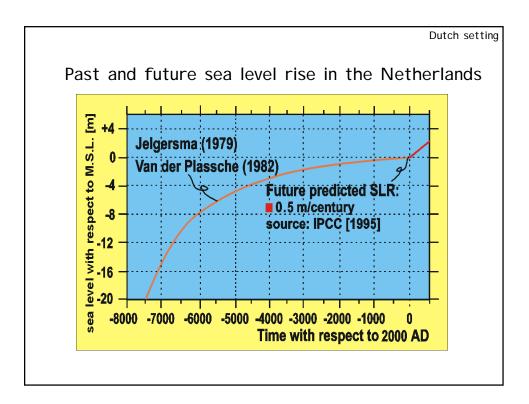


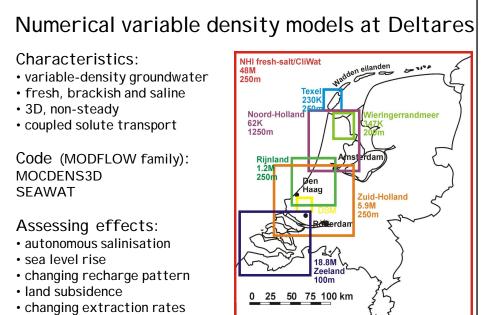




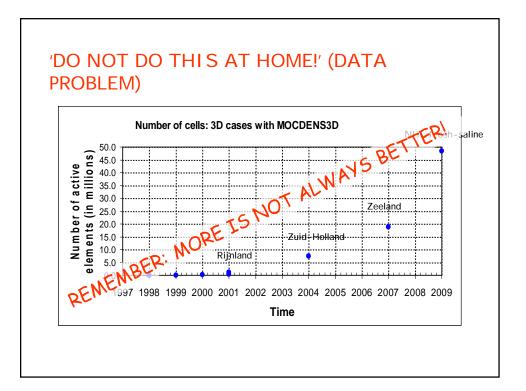


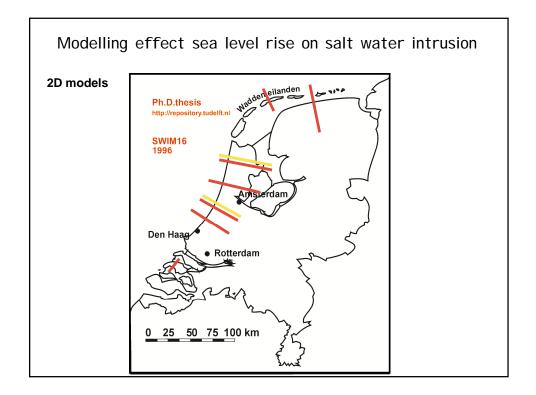


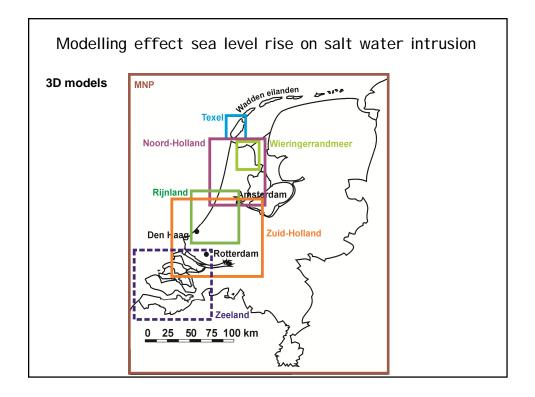


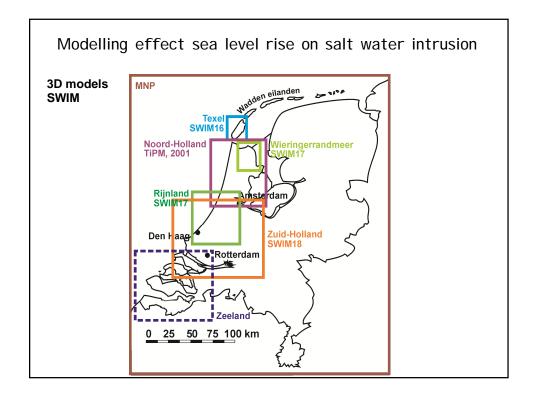


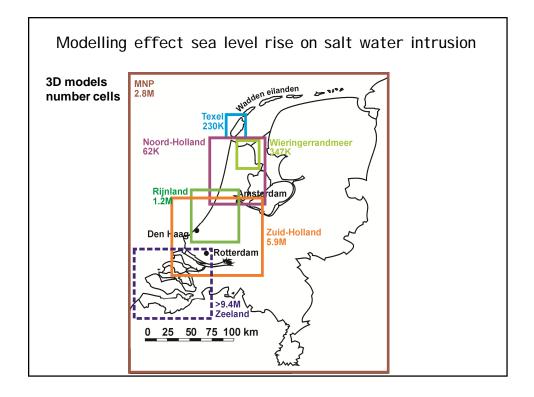
adaption measures

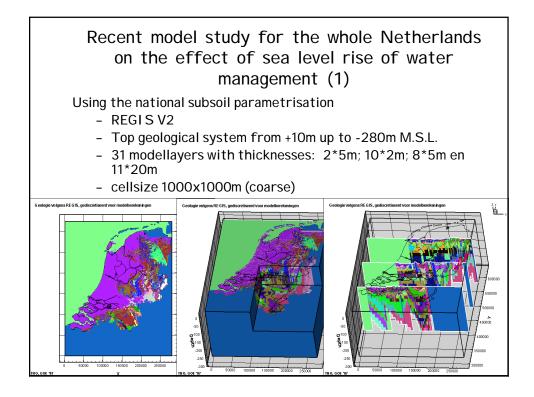


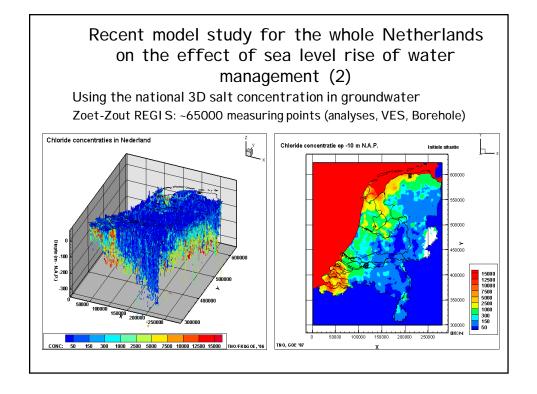


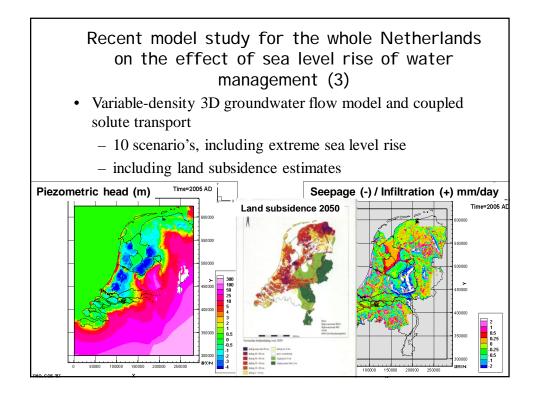


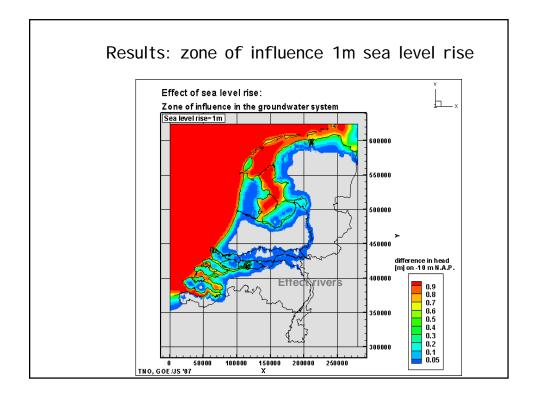


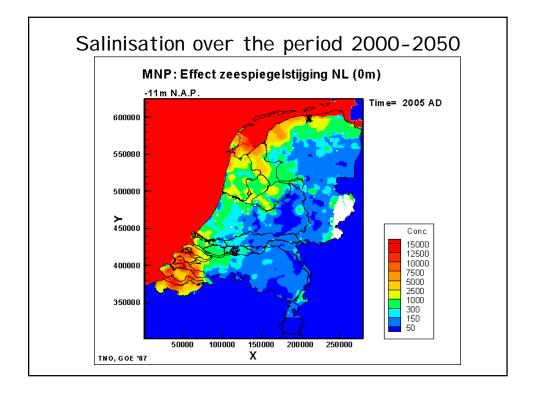


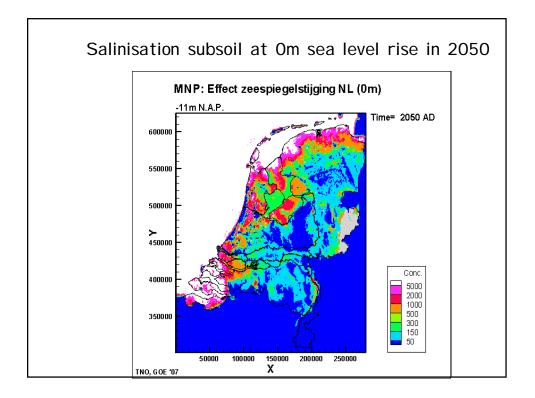


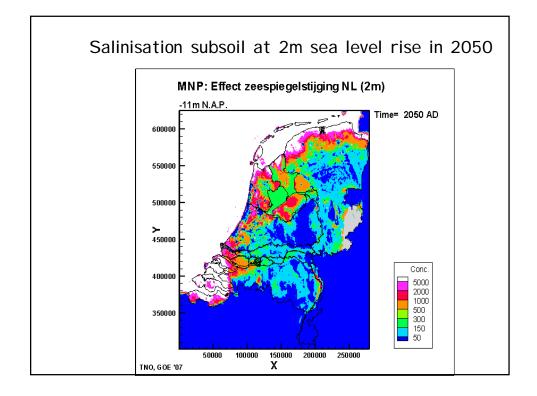


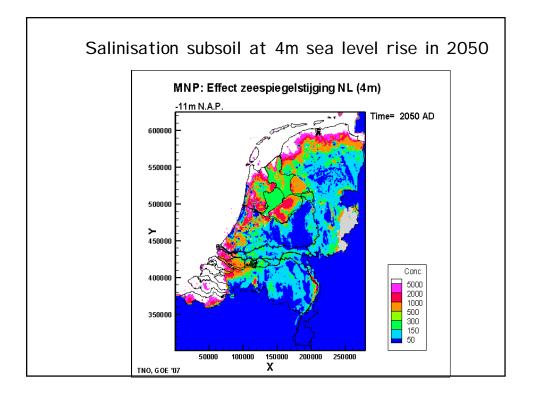


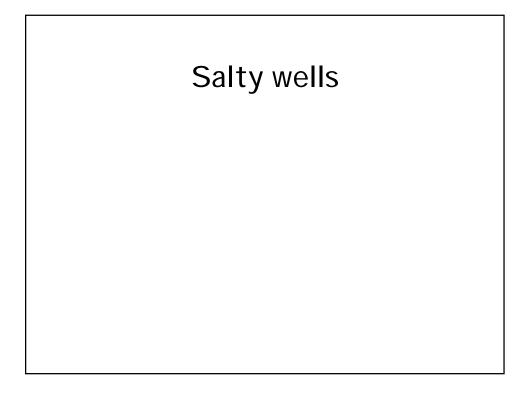


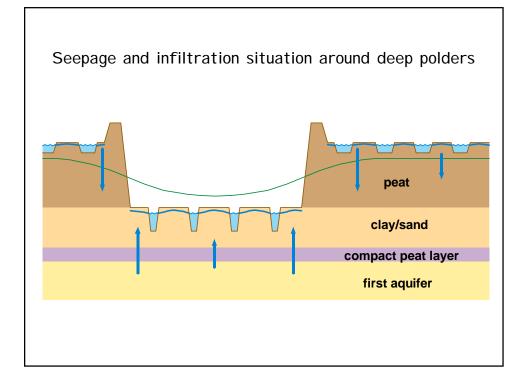


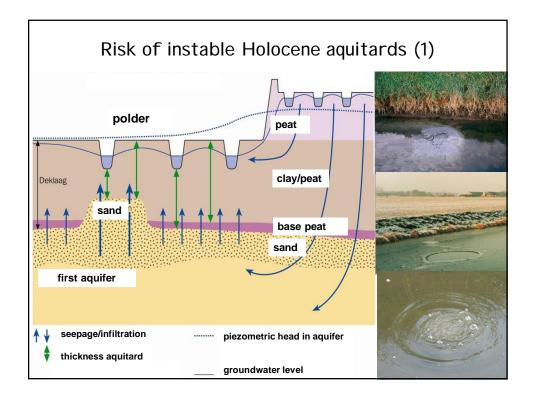


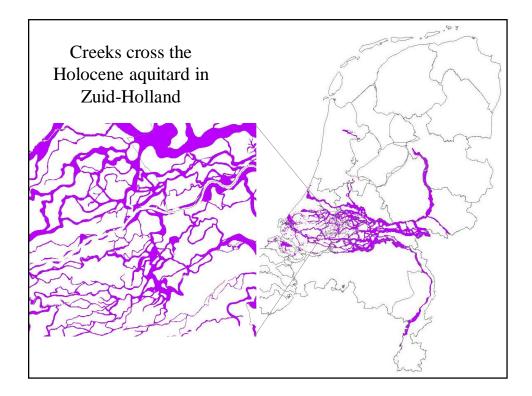




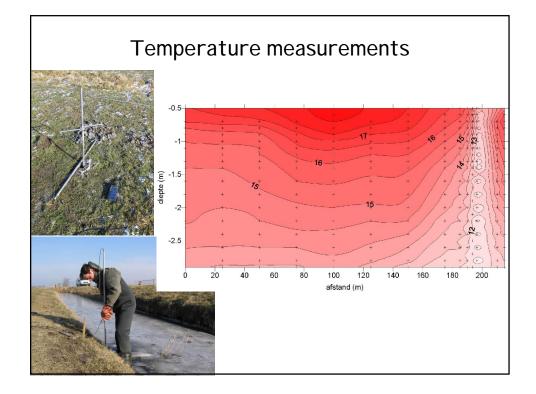


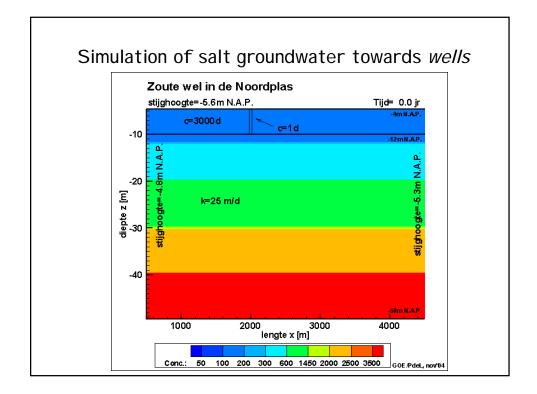


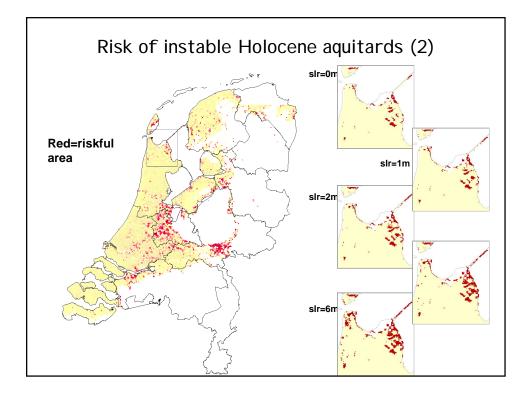


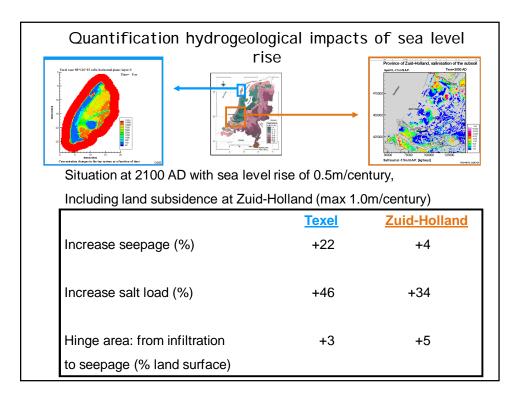


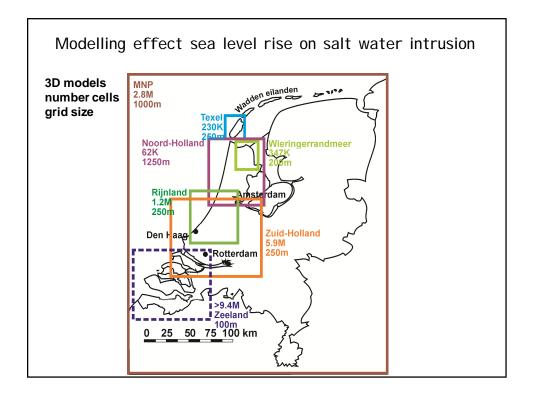








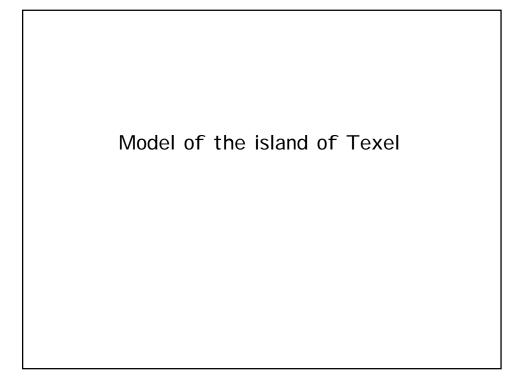


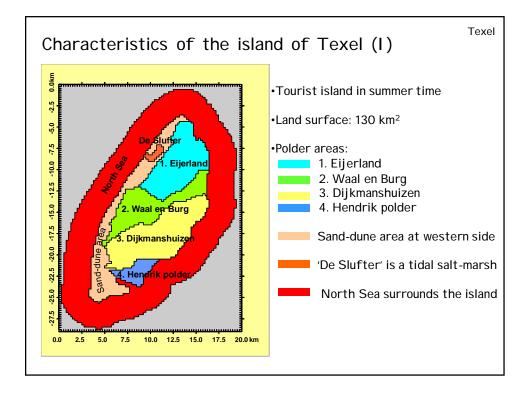


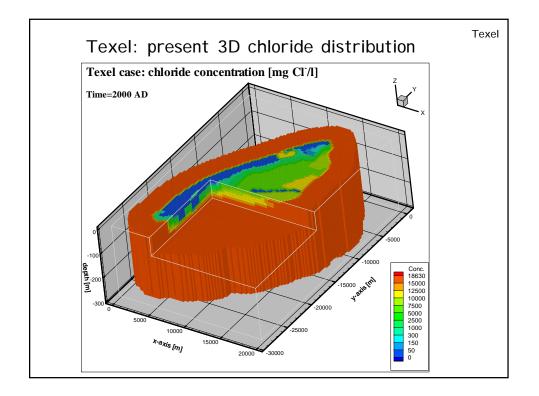
				3D modellin			
Characteristics 3D Cases (I): geometry & subsoil							
Case	Kop van Noord-Holland	Texel	Wieringer- meerpolder	Rijnland			
total land surface [km ²]	2150	130	200	1100			
L _x *L _y modelled area [km]	65*51	20*29	23*27	52*60			
depth system [m -N.A.P]	290	302	385	190			
aquifer hydr.cond. [m/d]	5-70	5-30	15-40	12-70			
aquitard hydr.cond. [m/d]	0.12-0.001	0.01-1	0.012-0.056	2.5E-4-0.8			
porosity	0.35	0.3	0.25	0.25			
anisotropy [k _z /k _x]	0.4	0.4	0.25	0.1			
long. dispersivity α_{L} [m]**	2	2	2	1			
# head&conc. observations	not applicable*	111	95	1632			
characteristics	not applicable*	Δφ =0.24 m	∆¢ =0.34 m	Δφ =0.60 m			
head calibration		σ=0.77 m	σ=0.21 m	σ=0.77 m			

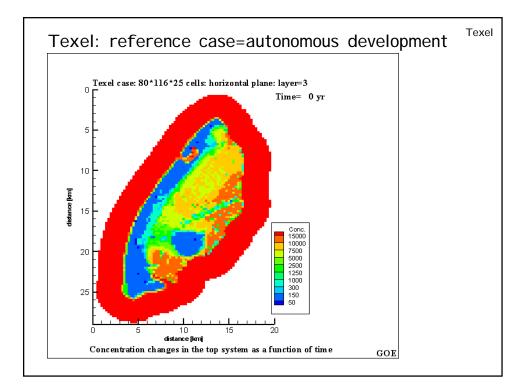
 * calibration with seepage & salt load in polders $^{\ast\ast}molecular$ diffusion=10-9 m²/s; trans. disp.=1/10 long. disp.

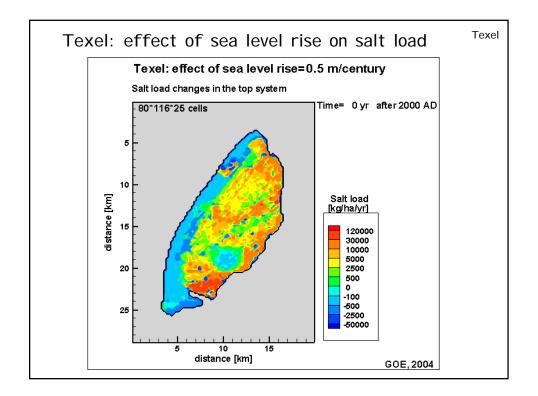
Case	Kop van Noord-Holland	Texel	Wieringer- meerpolder	Rijnland (=391 EM RAM)
horizontal cell size [m]	1250*1250	250*250	200*200	250*250
vertical cell size [m]	10	1.5 to 20	2 to 70	5 to 10
total # active cells	~40.000	~126.000	~312.000	~1.200.000
# cells	41*52*29	80*116*23	116*136*22	209*241*24
# particles per cell	27	8	8	1
total time [yr]	1000	500	50	500
convergence head crite flow time step $\Delta t=1$ yea				

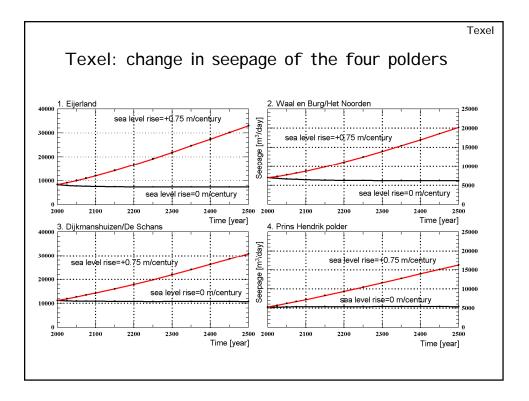


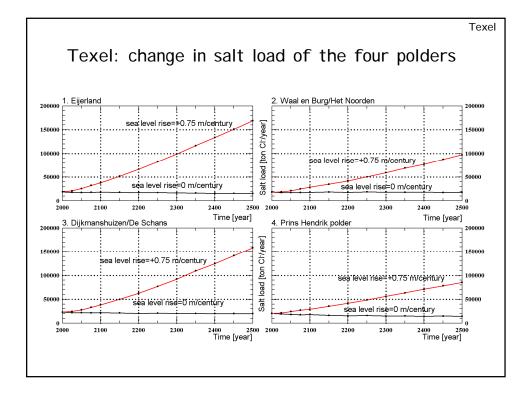


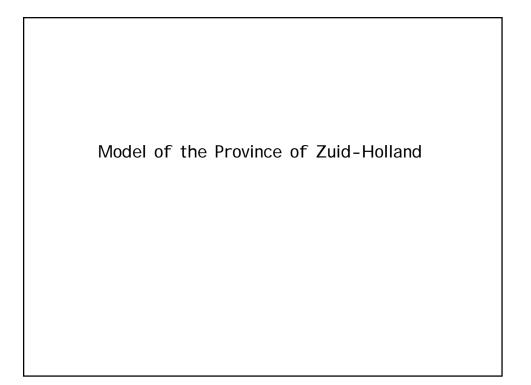


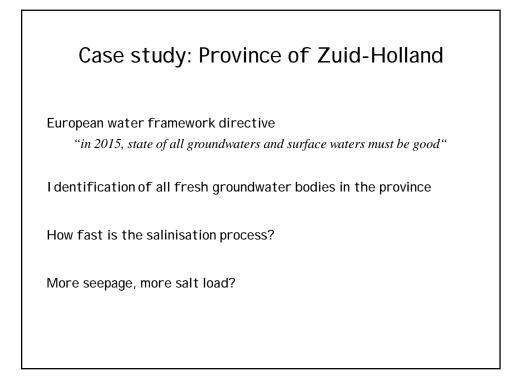


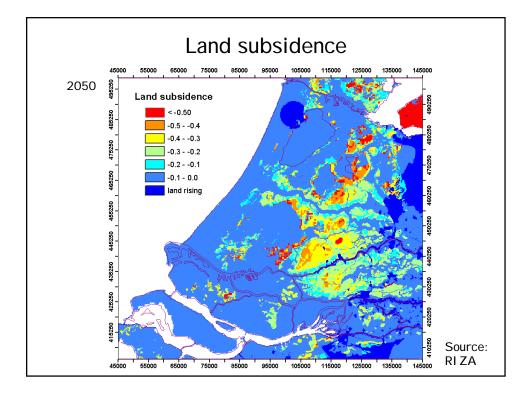


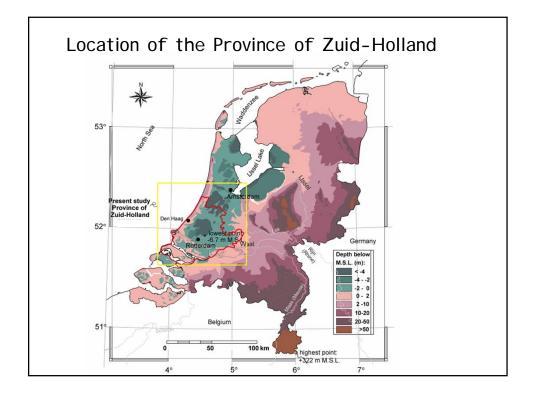


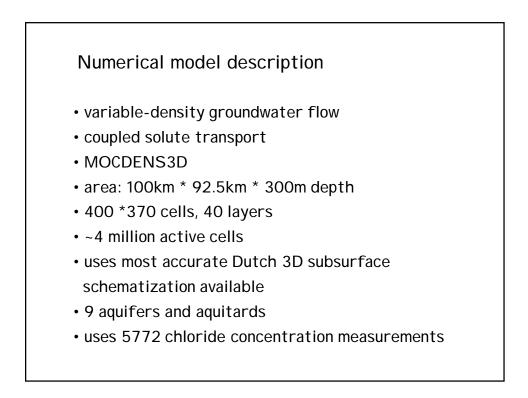


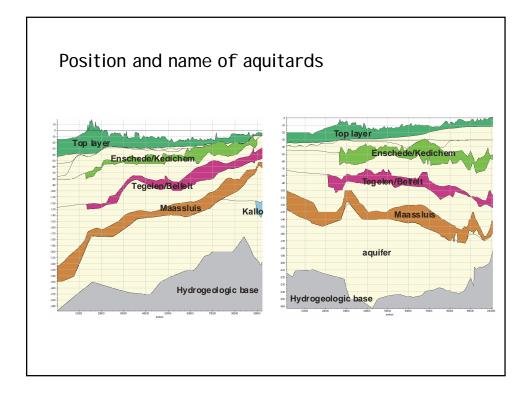


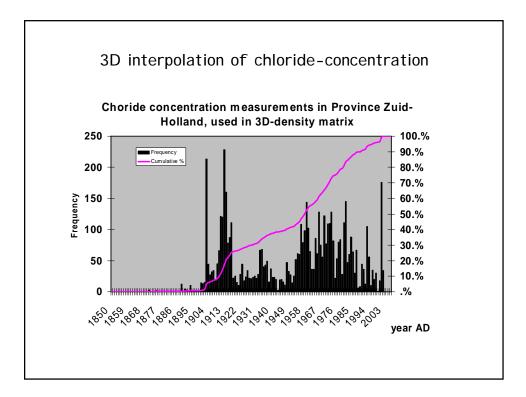


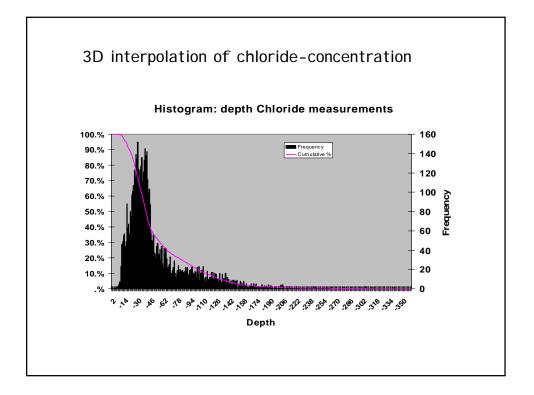


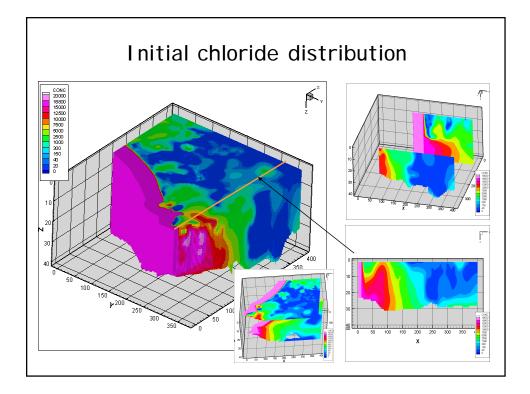


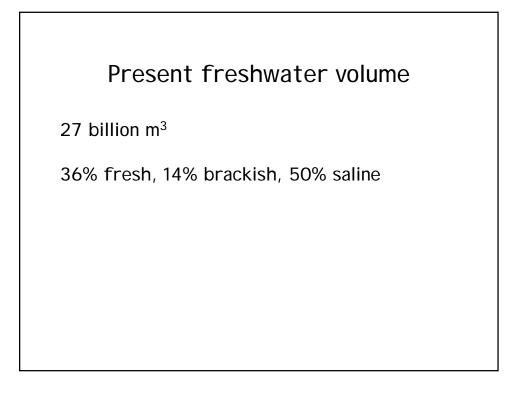


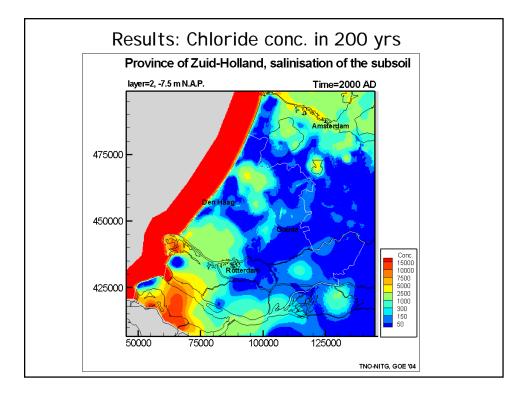


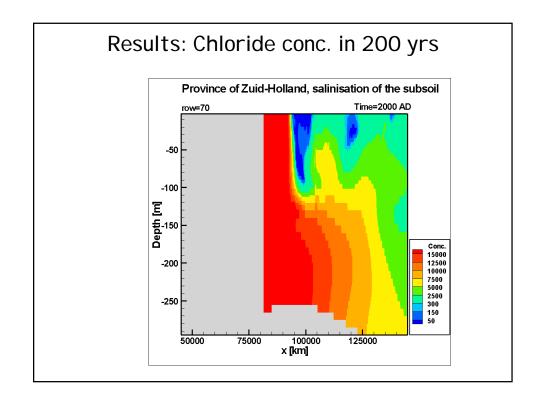


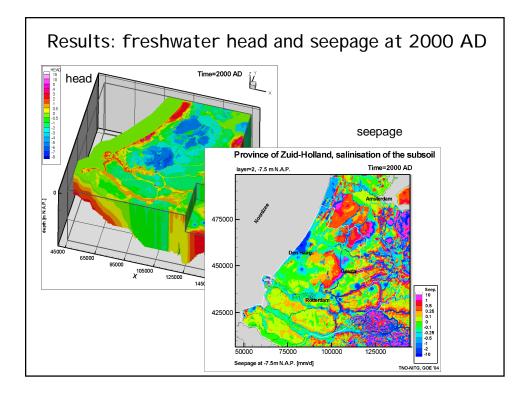


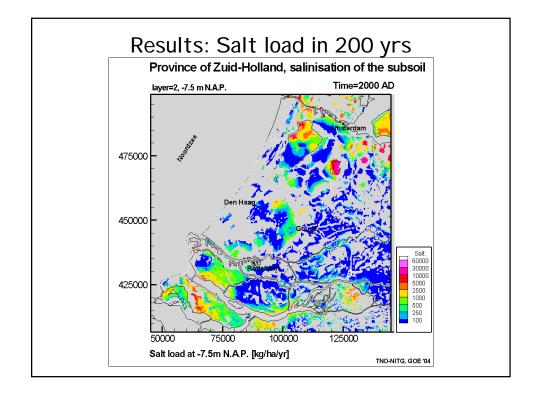


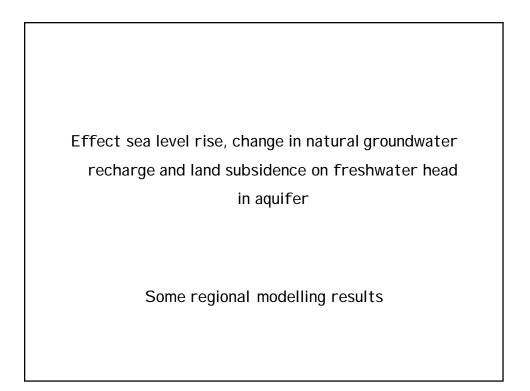


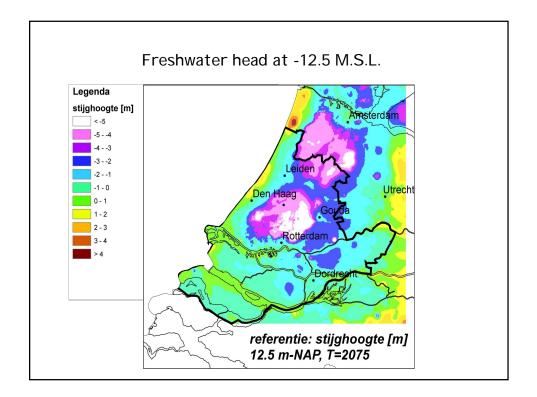


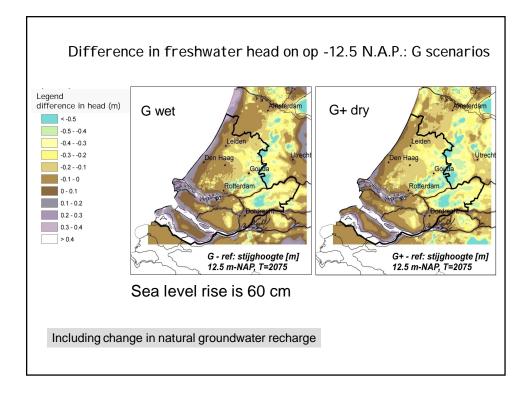


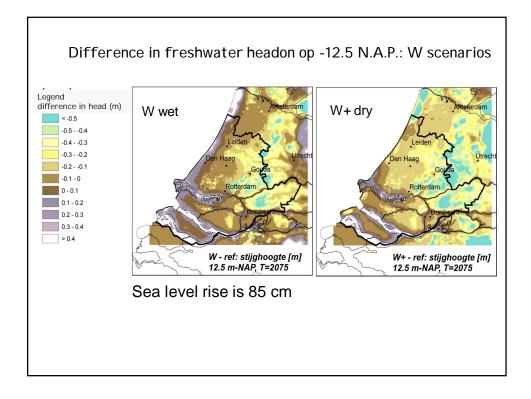


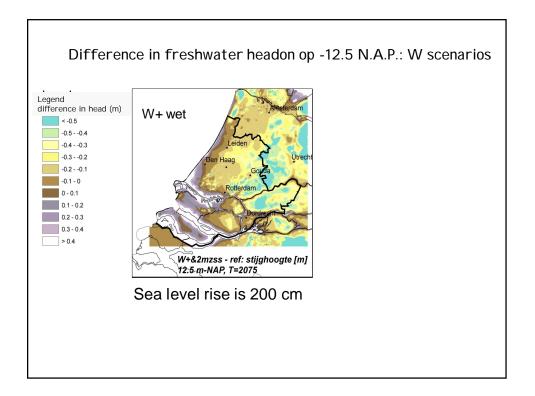


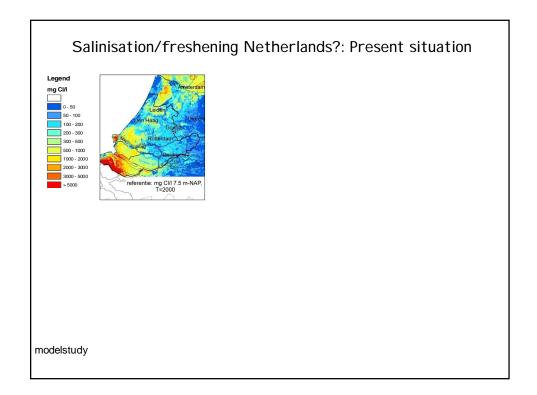


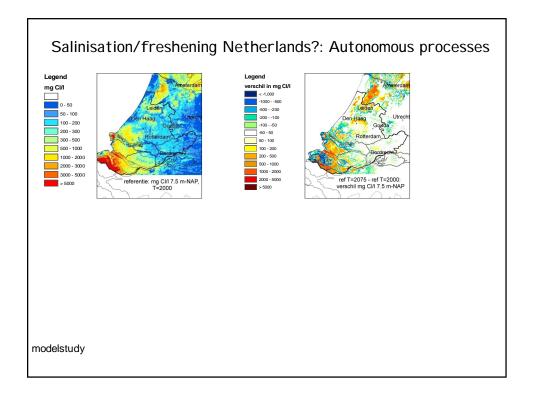


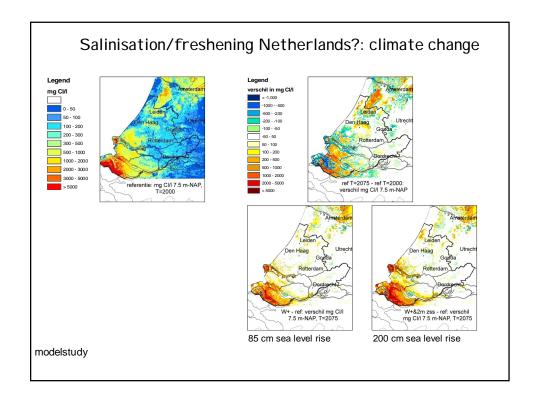


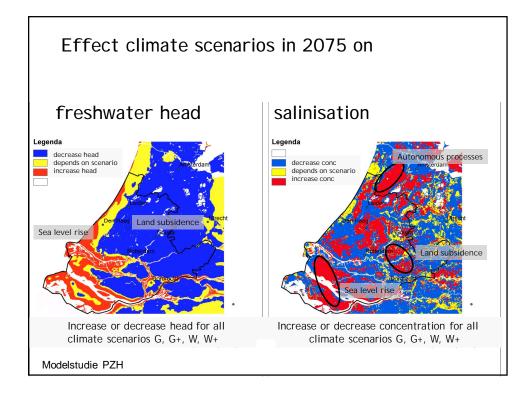


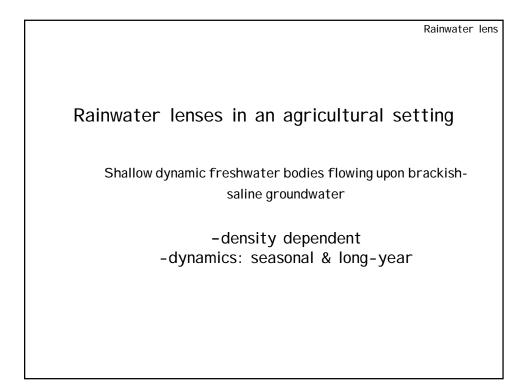


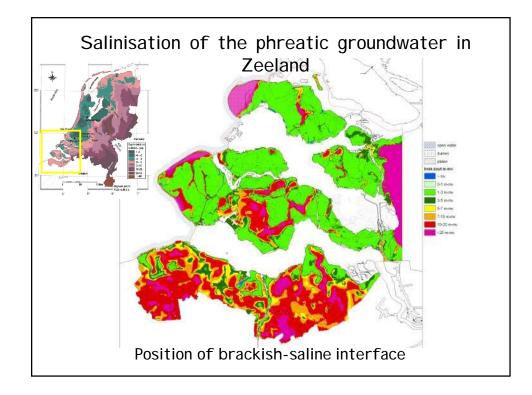


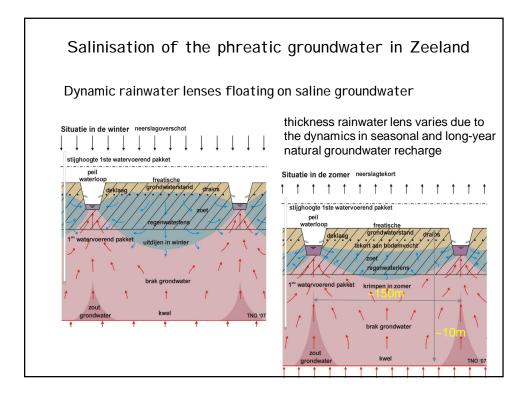


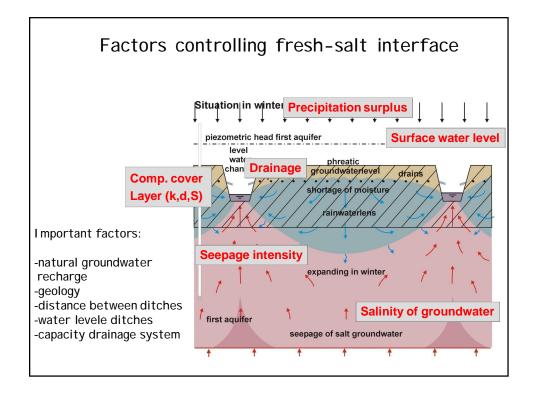


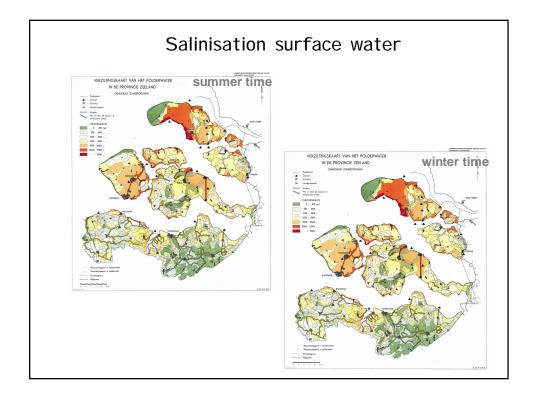


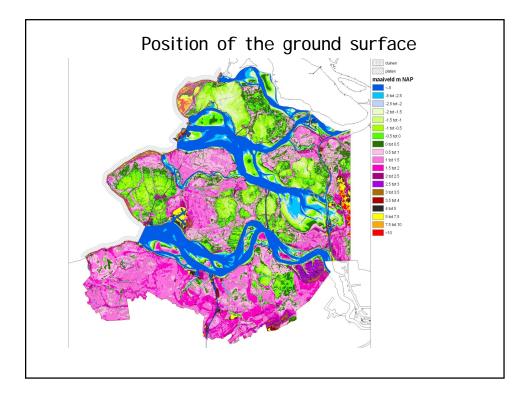


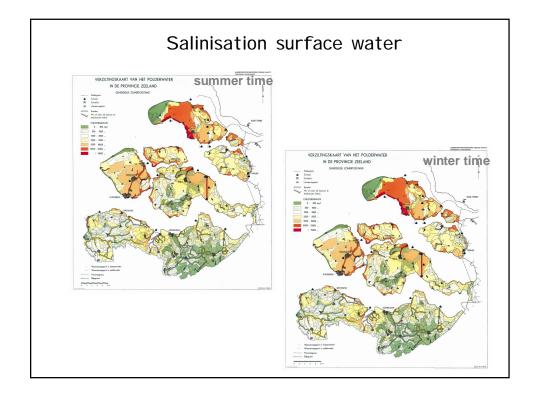


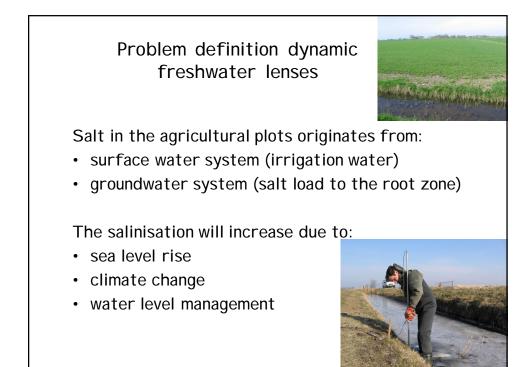












How to tackle the problem?

Field measurements at parcels

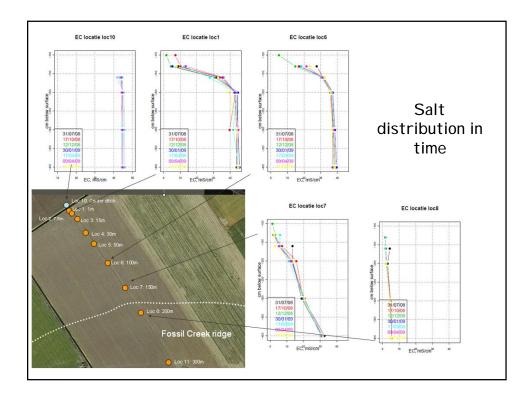
- fresh-brackish-salt interface at local scale using T-EC-probe and later CVES and ERT
- groundwater level and quality
- surface water level and quality

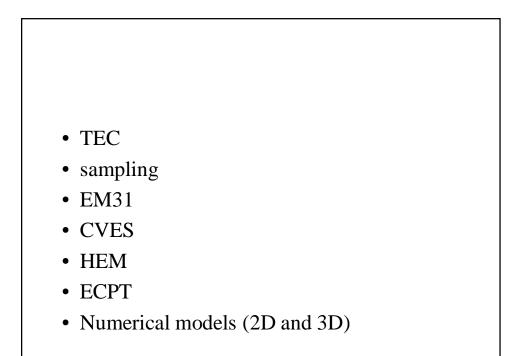
Modelling

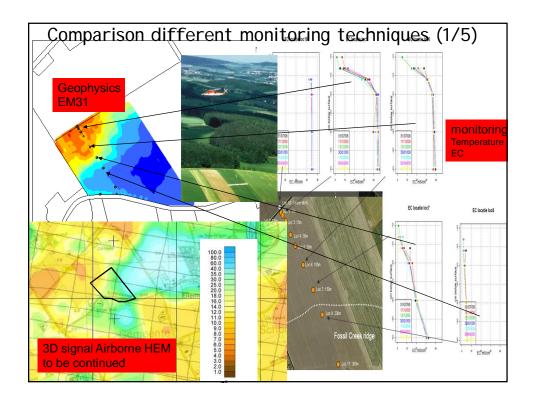
- density dependent groundwater flow
- two different scales:
 - regional scale: transect perpendicular at coast
 - Iocal scale: parcel between two ditches

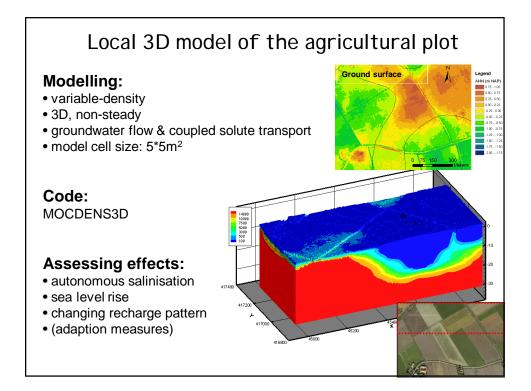


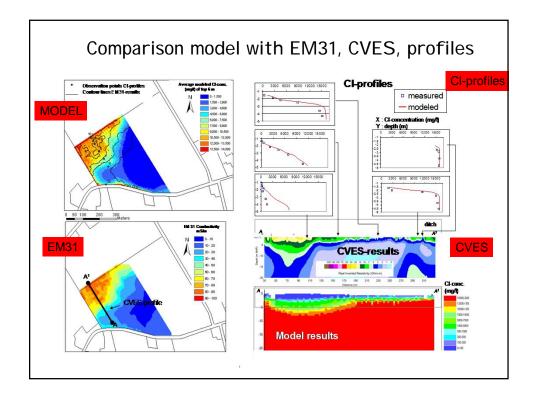


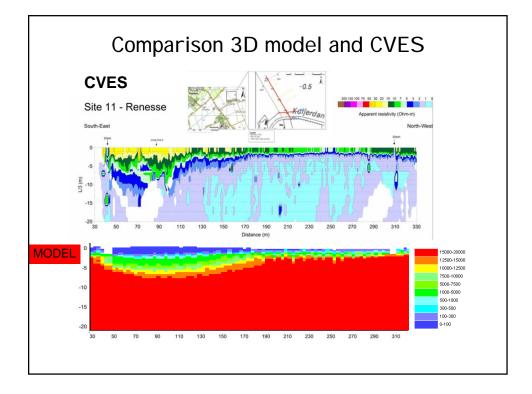


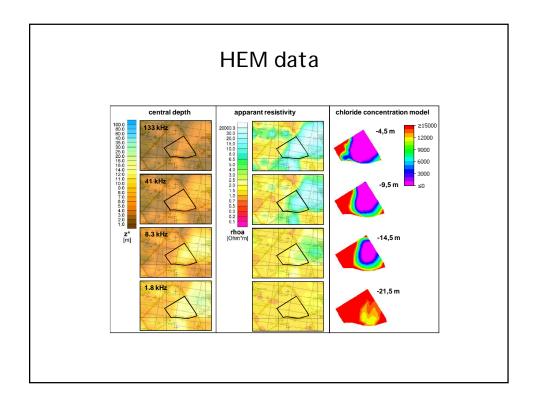


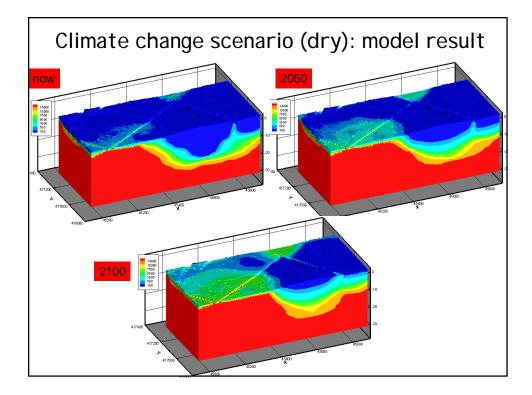


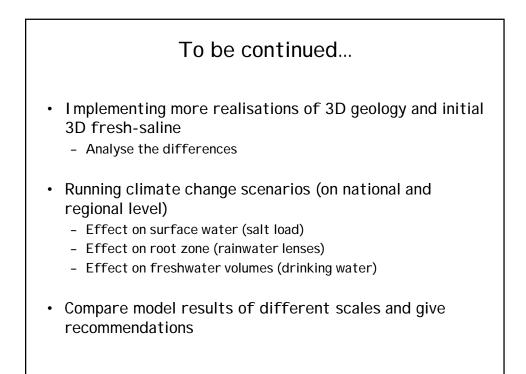


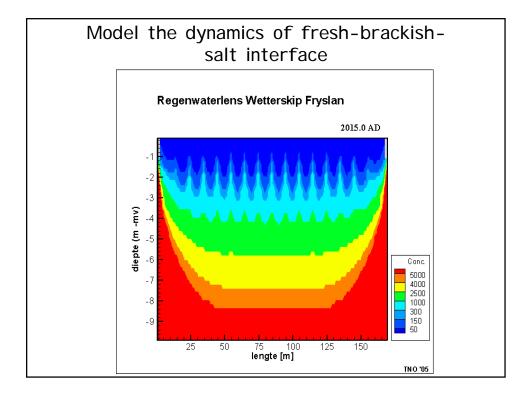


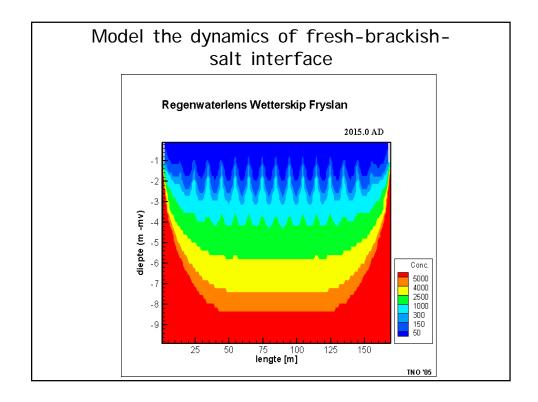


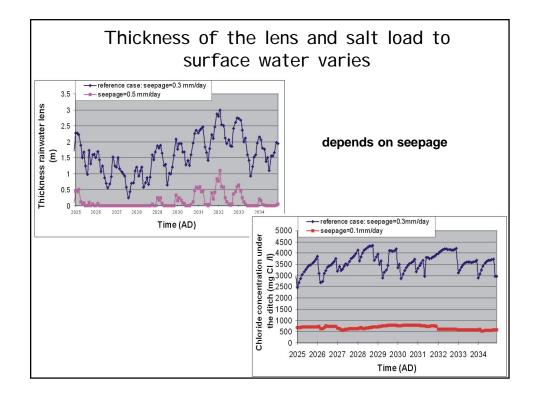




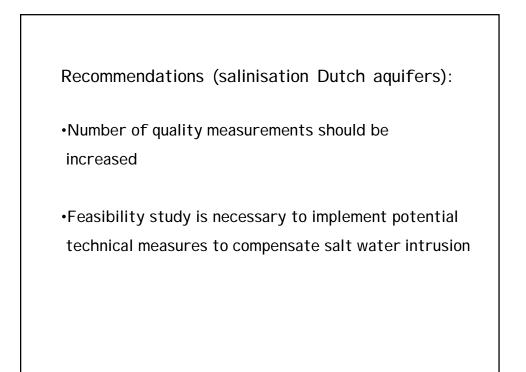


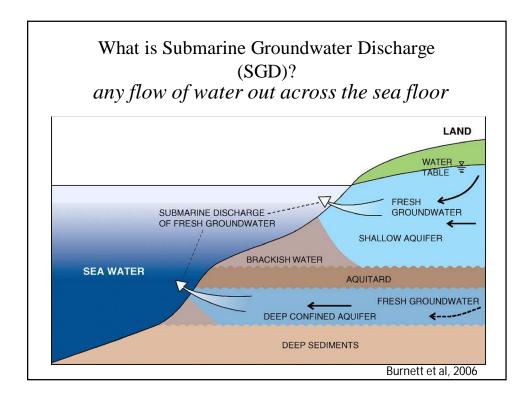


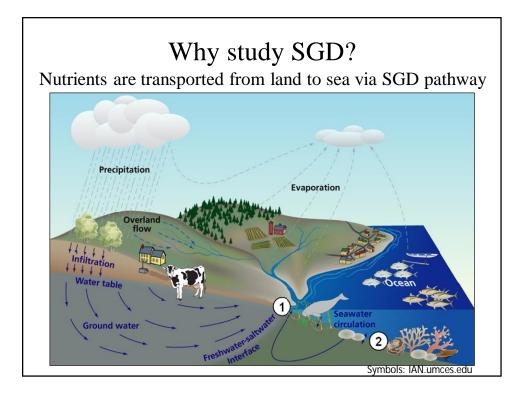


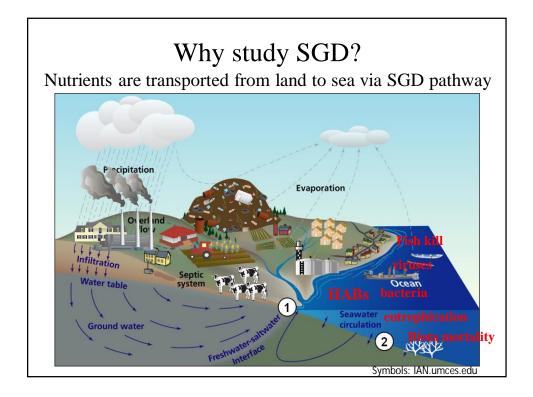


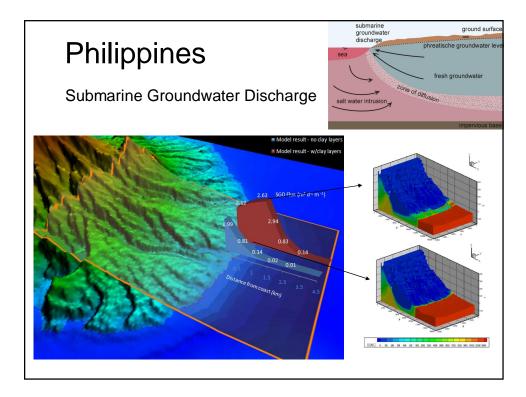


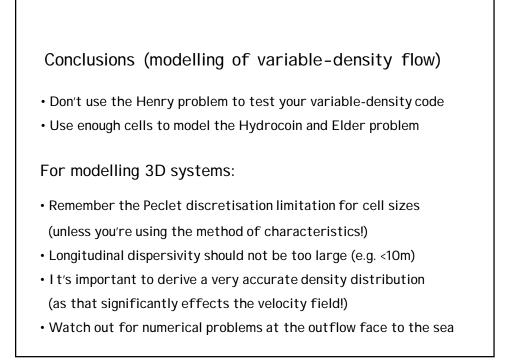






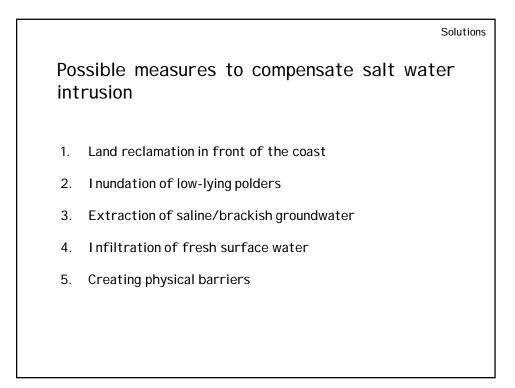


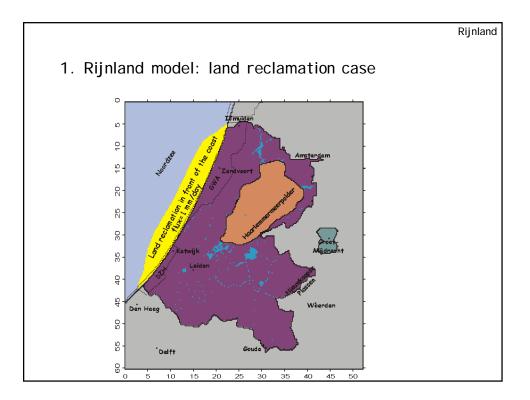


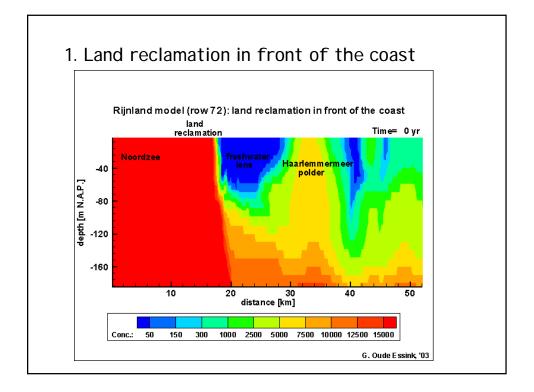


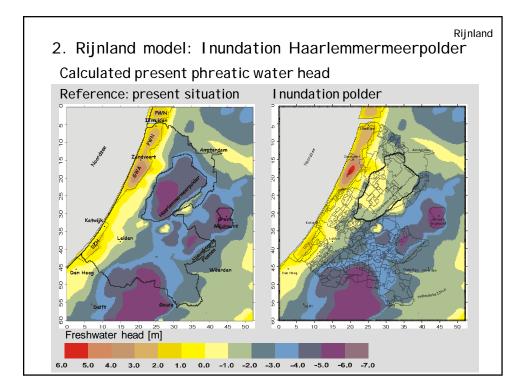
Challenges for the future

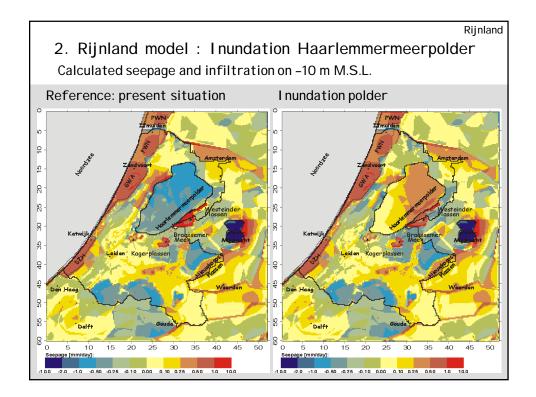
- I mprove the 3D density matrix, e.g. by more types of measurements
- I mplement effect of climate change and sea level rise on coastal aquifers
- Optimalisation of (ground)water management in coastal aquifers by using 3D variable-density flow models
- I mprove calibration of 3D models by using transient data of solute concentrations
- Incorporate reactive multicomponent solute transport

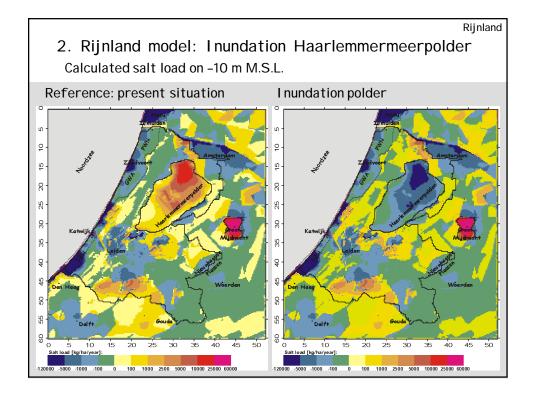


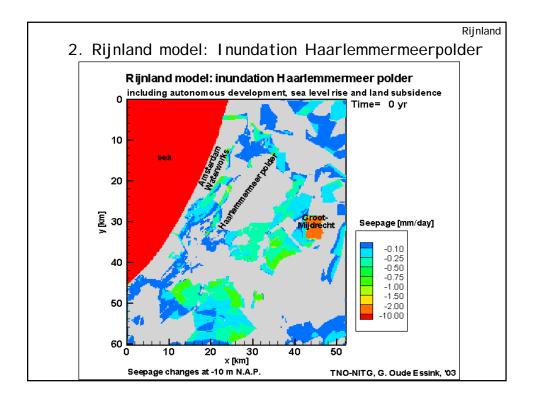


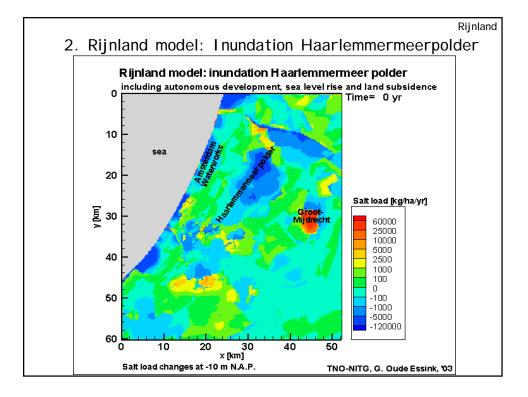


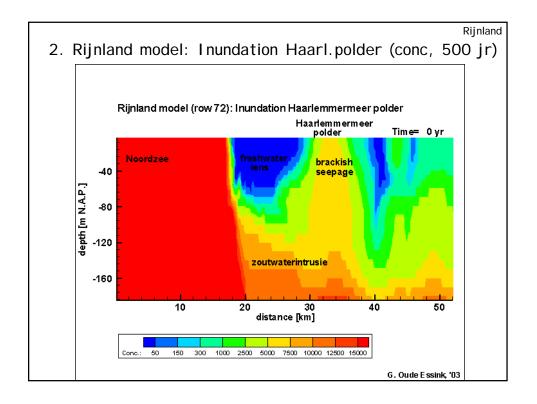


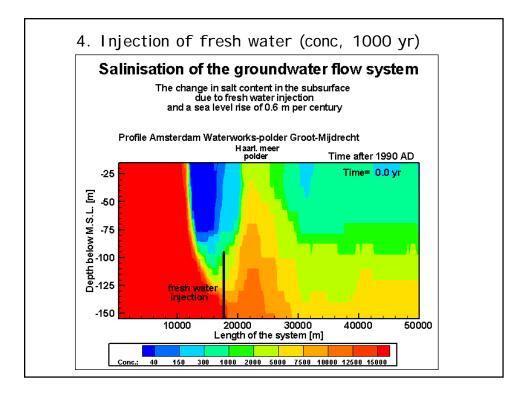


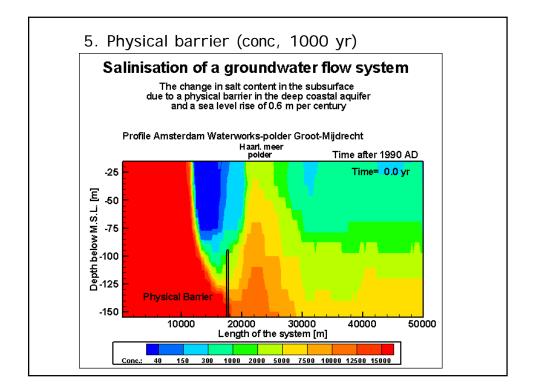


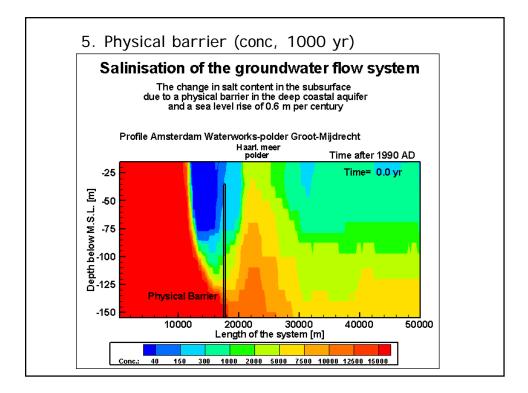




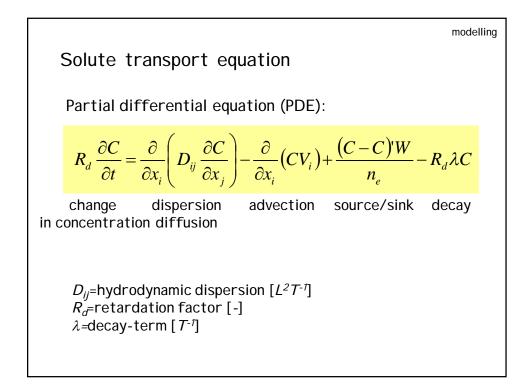


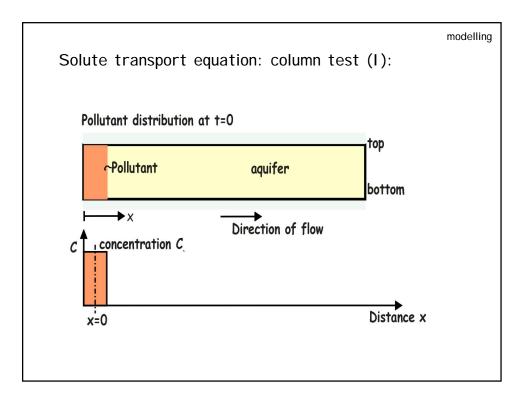


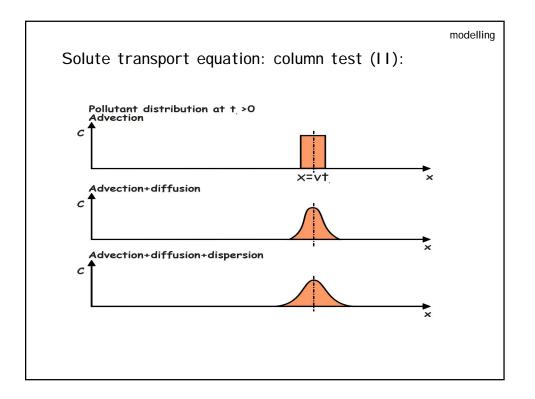


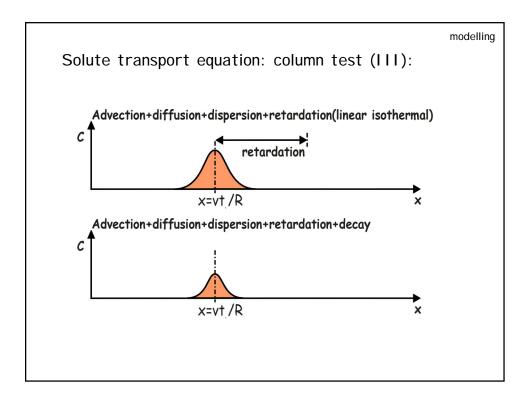


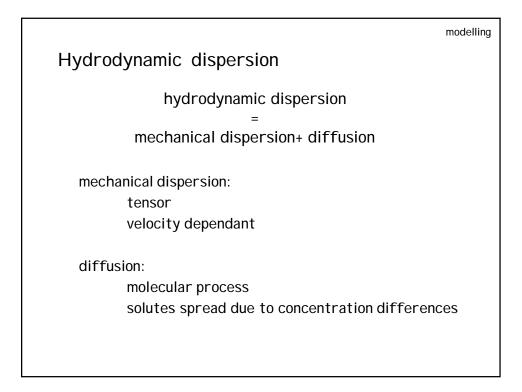
solute transport models Combine the groundwater flow equation and the advection-dispersion equation by means of an equation of state

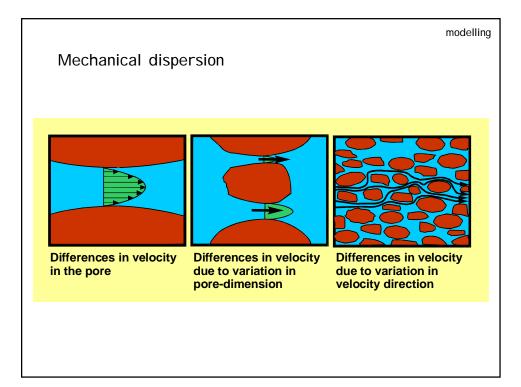


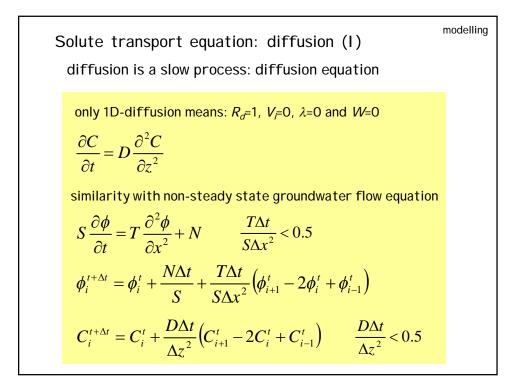


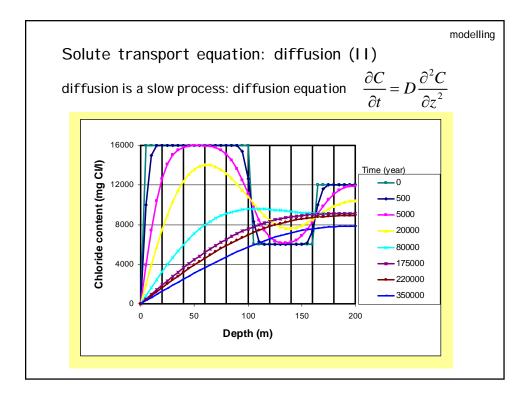


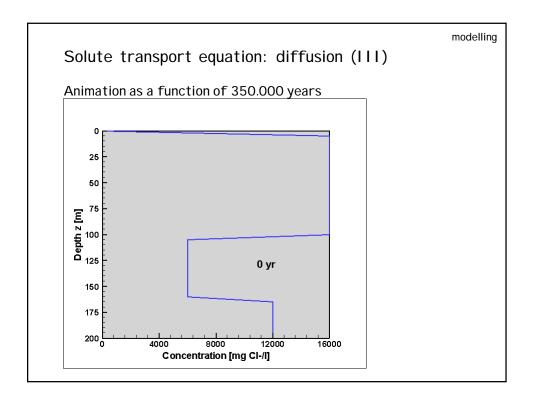








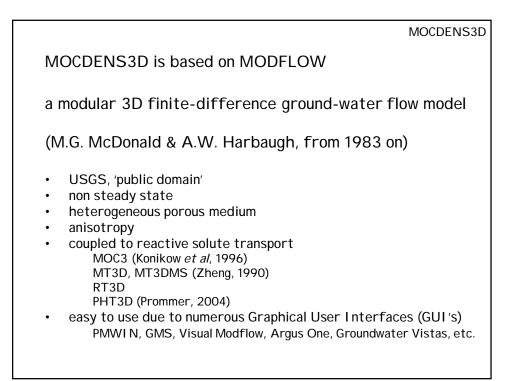


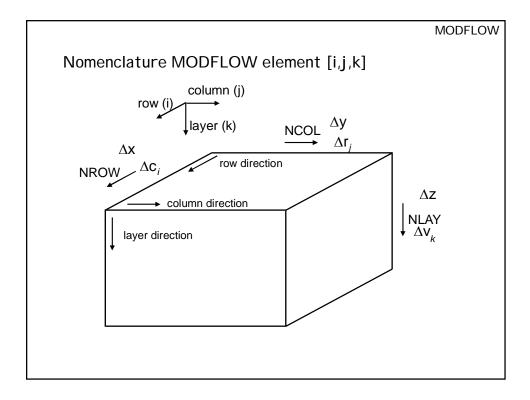


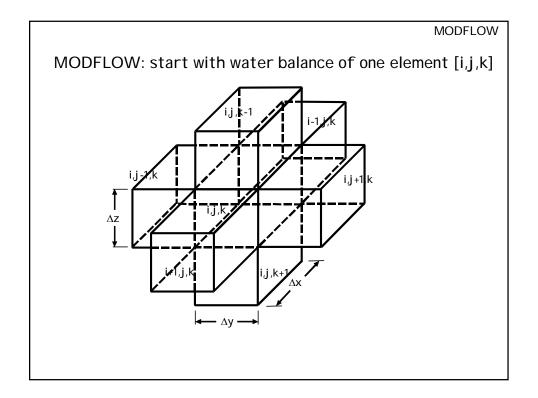
MOCDENS3D
Groundwater flow equation (MODFLOW, 1988)
Darcy

$$q_x = -\frac{\kappa_x \rho_f g}{\mu} \frac{\partial \phi_f}{\partial x}; \quad q_y = -\frac{\kappa_y \rho_f g}{\mu} \frac{\partial \phi_f}{\partial y}; \quad q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

Continuity
 $-\left[\frac{\partial \rho q_x}{\partial x} + \frac{\partial \rho q_y}{\partial y} + \frac{\partial \rho q_z}{\partial z} \right] = \frac{\partial n \rho}{\partial t} + W$
buoyancy
Freshwater head
 $\phi_f = \frac{p}{\rho_f g} + z$
Advection-dispersion equation (MOC3D, 1996)
 $\frac{\partial C}{\partial t} = \frac{1}{nR_f} \frac{\partial}{\partial x_i} \left[nD_{ij} \frac{\partial C}{\partial x_j} \right] - \frac{V_i}{R_f} \frac{\partial C}{\partial x_i} + \frac{\sum [W(C'-C)]}{nR_f} - \lambda C$
Equation of state: relation density & concentration
 $\rho_{i,j,k} = \rho_f (1 + \beta C_{i,j,k})$



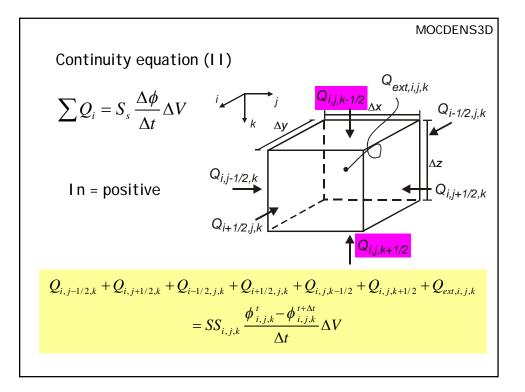


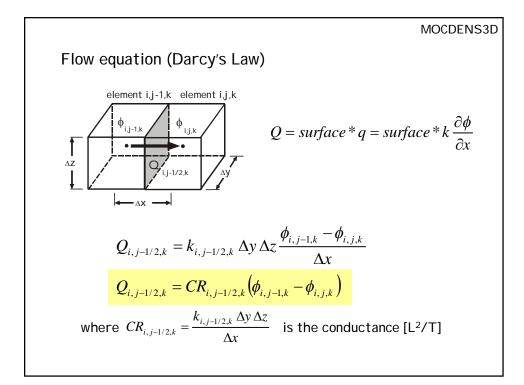


Continuity equation (1)
In - Out = Storage

$$\frac{\partial}{\partial x} \left(k_{xx} \frac{\partial \phi}{\partial x} \right) + \frac{\partial}{\partial y} \left(k_{yy} \frac{\partial \phi}{\partial y} \right) + \frac{\partial}{\partial z} \left(k_{zz} \frac{\partial \phi}{\partial z} \right) - W = S_s \frac{\partial \phi}{\partial t}$$

$$\sum Q_i = S_s \frac{\Delta \phi}{\Delta t} \Delta V$$





$$Density dependent groundwater flow equation
Q_{i,j-1/2,k} = CR_{i,j-1/2,k}(\phi_{f,i,j-1,k} - \phi_{f,i,j,k})
Q_{i,j+1/2,k} = CR_{i,j+1/2,k}(\phi_{f,i,j+1,k} - \phi_{f,i,j,k})
Q_{i-1/2,j,k} = CC_{i-1/2,j,k}(\phi_{f,i-1,j,k} - \phi_{f,i,j,k})
Q_{i+1/2,j,k} = CC_{i+1/2,j,k}(\phi_{f,i+1,j,k} - \phi_{f,i,j,k})
Q_{i+1/2,j,k} = CC_{i+1/2,j,k}(\phi_{f,i+1,j,k} - \phi_{f,i,j,k})
Q_{i,j,k+1/2} = CV_{i,j,k-1/2}(\phi_{f,i,j,k-1} - \phi_{f,i,j,k} + BUOY_{i,j,k-1/2}\Delta v_{k-1/2})
Q_{i,j,k+1/2} = CV_{i,j,k+1/2}(\phi_{f,i,j,k+1} - \phi_{f,i,j,k} + BUOY_{i,j,k+1/2}\Delta v_{k+1/2})
Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k} + SS_{i,j,k} \frac{\phi_{f,i,j,k}^{t} - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t}\Delta V$$

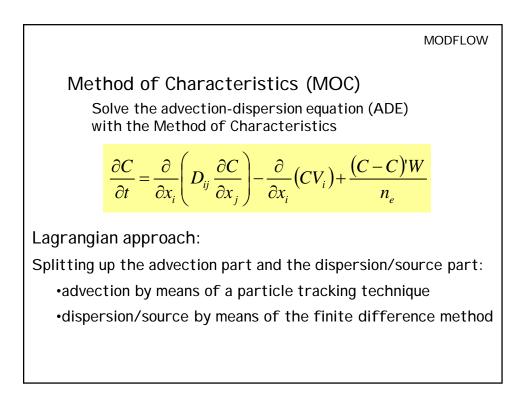
The term $Q_{ext,i,j,k}$ Takes into account all external sources Rewriting the term: $Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$

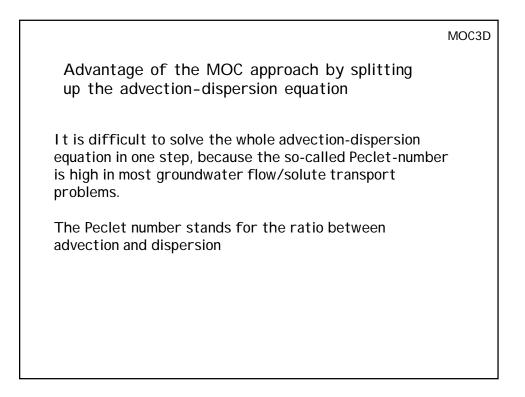
$$\begin{aligned} & \text{DOCDENS3D} \\ \text{Thé variable density groundwater flow equation} \\ & \mathcal{Q}_{i,j-1/2,k} + \mathcal{Q}_{i,j+1/2,k} + \mathcal{Q}_{i-1/2,j,k} + \mathcal{Q}_{i+1/2,j,k} + \mathcal{Q}_{i,j,k-1/2} + \mathcal{Q}_{i,j,k+1/2} + \mathcal{Q}_{ext,i,j,k} \\ & = SS_{i,j,k} \frac{\phi_{f,i,j,k}^{t} - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t} \Delta V \\ & \text{and:} \\ & \mathcal{Q}_{ext,i,j,k} = P_{i,j,k} \phi_{f,i,j,k}^{t+\Delta t} + \mathcal{Q}_{i,j,k}^{t} \\ & \text{gives:} \\ & + (-CV_{i,j,k-1/2} - CC_{i-1/2,j,k} - CR_{i,j-1/2,k} - CR_{i,j+1/2,k} - CV_{i,j,k+1/2} + HCOF_{i,j,k}) \phi_{f,i,j,k}^{t+\Delta t} \\ & + CR_{i,j+1/2,k} \phi_{f,i,j+1,k}^{t+\Delta t} + CC_{i+1/2,j,k} \phi_{f,i+1,j,k}^{t+\Delta t} + CV_{i,j,k+1/2} \phi_{f,i,j,k+1}^{t+\Delta t} = RHS_{i,j,k} \end{aligned}$$
with:
$$& \text{HCOF}_{i,j,k} = P_{i,j,k} - SC1_{i,j,k} / (\Delta t) \\ & \text{RHS}_{i,j,k} = -Q_{i,j,k}^{t} - SC1_{i,j,k} / (\Delta t) \\ & -CV_{i,j,k-1/2} BUOY_{i,j,k-1/2} \Delta V_{k-1/2} + CV_{i,j,k+1/2} BUOY_{i,j,k+1/2} \Delta V_{k+1/2} \\ & SC1_{i,j,k} = SS_{i,j,k} \Delta V \end{aligned}$$

Equation of state

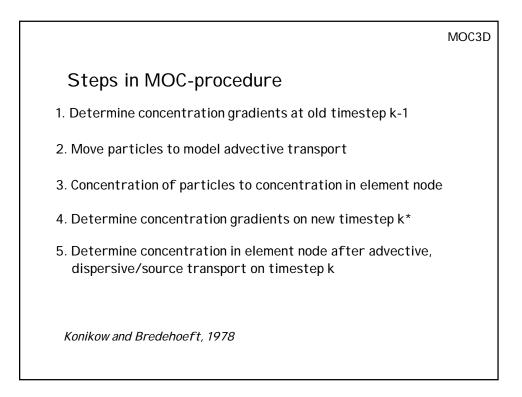
$$BUOY_{i,j,k-1/2} = \left(\frac{(\rho_{i,j,k-1/2} + \rho_{i,j,k})/2 - \rho_f}{\rho_f}\right)$$

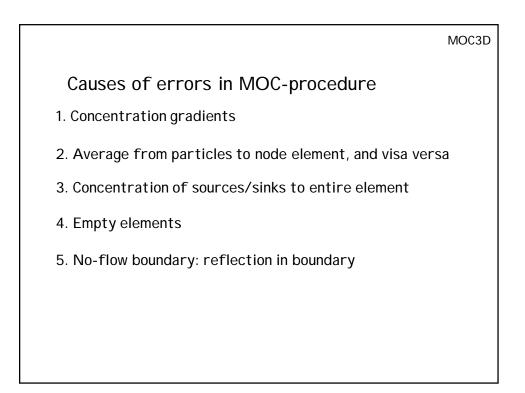
$$\rho_{i,j,k} = \rho_f \left(1 + \frac{\rho_s - \rho_f}{\rho_f} \frac{C_{i,j,k}}{C_s}\right)$$
or
$$\rho_{i,j,k} = \rho_f \left(1 + \beta C_{i,j,k}\right)$$

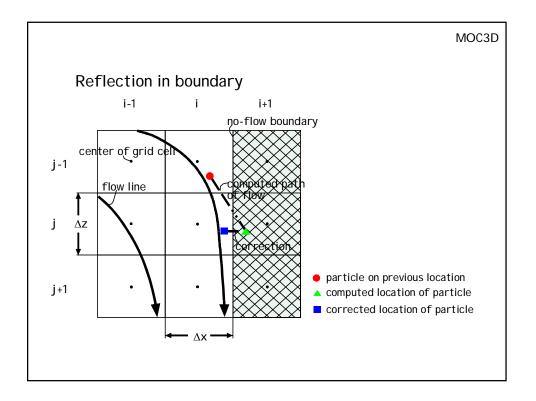


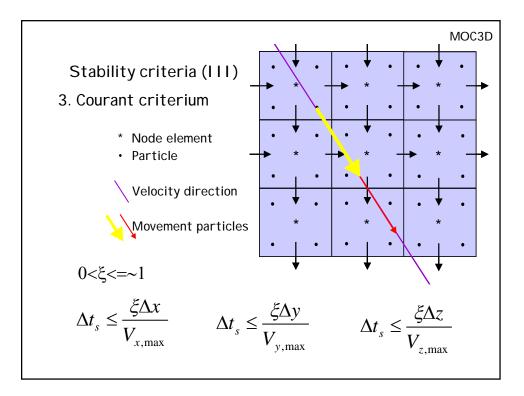


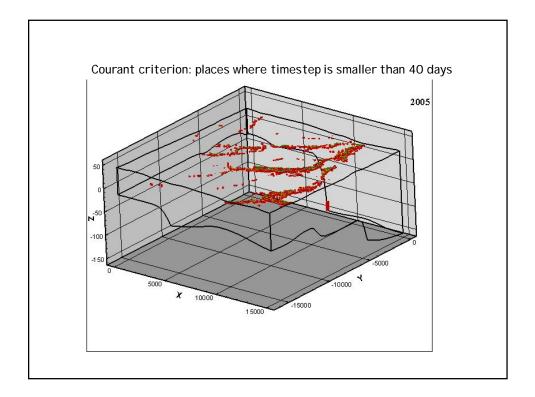
MOC3D
Procedure of MOC: advective transport by particle tracking
•Place a number of particles in each element
•Determine the effective velocity of each particle by (bi)linear interpolation of the velocity field which is derived from MODFLOW
•Move particles during one solute time step Δt_{solute}
•Average values of all particles in an element to one node value
•Calculate the change in concentration in all nodes due to advective transport
•Add this result to dispersive/source changes of solute transport

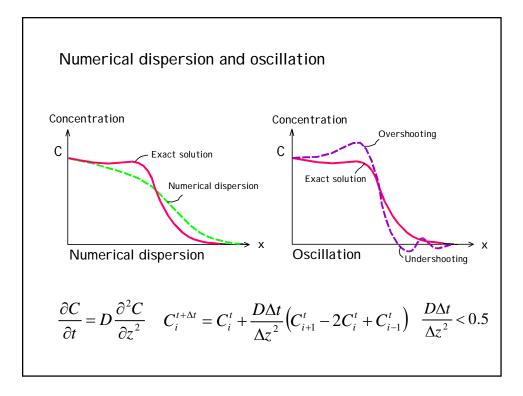


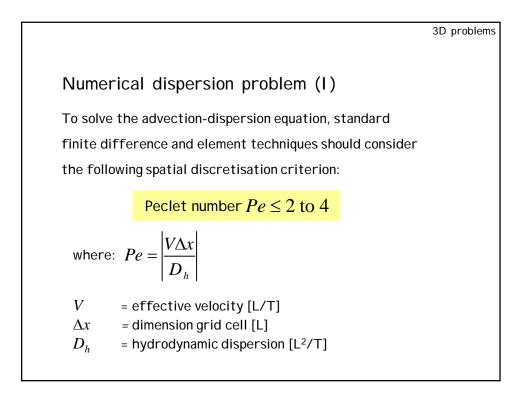


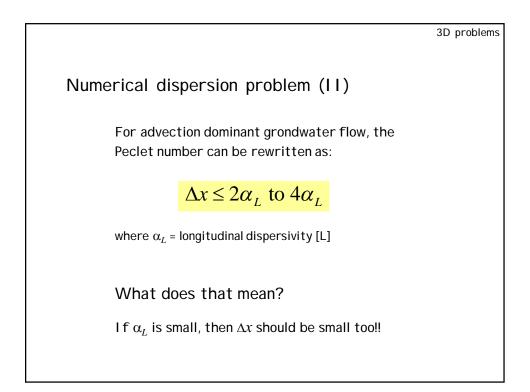








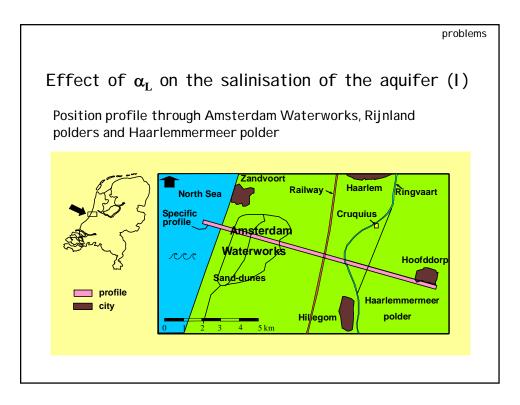


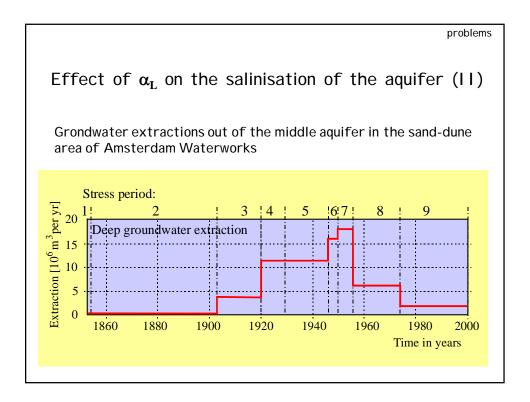


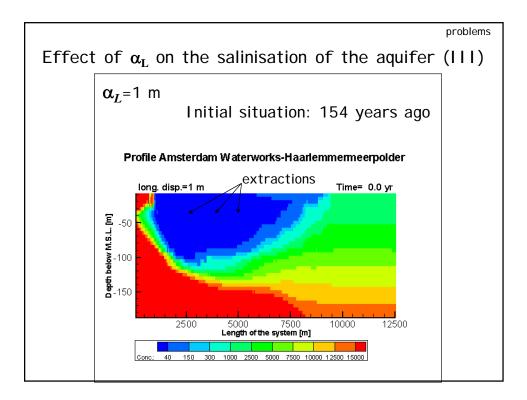
3D problems

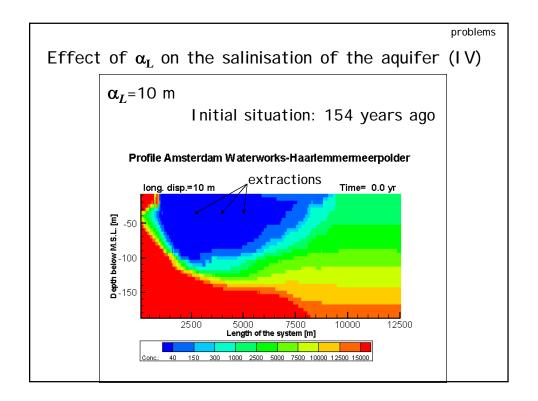
Numerical dispersion problem (III)

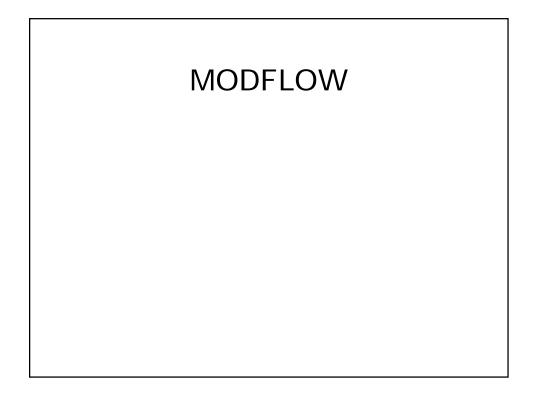
Now follows an transient salt water intrusion case to demonstrate why in many coastal aquifers the longitudinal dispersivity α_L [L] should be small

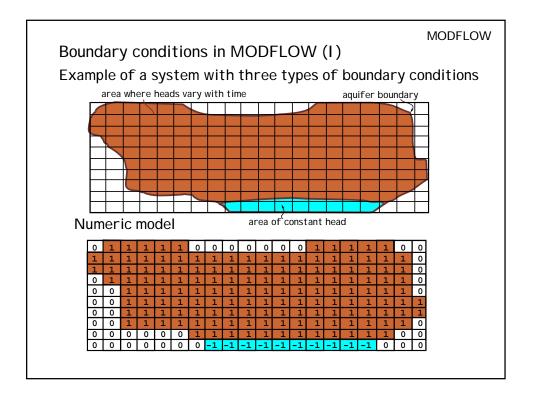


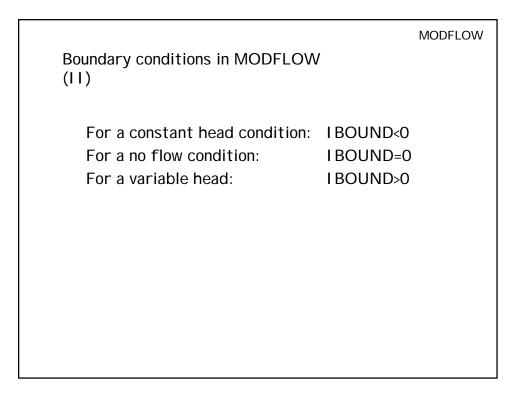


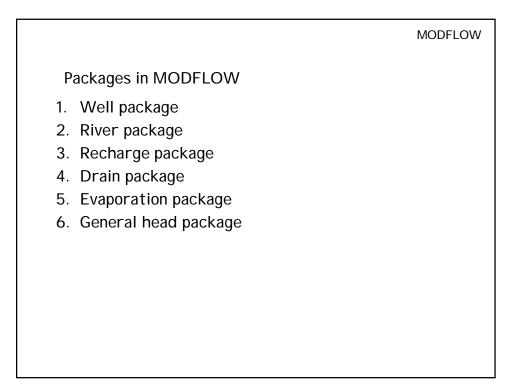




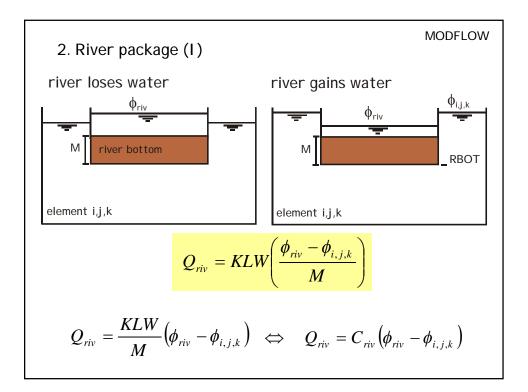








1. Well package $Q_{well} = Q_{i,j,k}$ Example: an extraction of 10 m³ per day should be inserted in an element as: $Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$ $Q_{ext,i,j,k} = -10 \quad (in = positive)$ $Q'_{i,j,k} = -10$



2. River package (11) $Q_{riv} = C_{riv} (\phi_{riv} - \phi_{i,j,k})$ Example: the river conductance C_{riv} is 20 m²/day and the rivel level=3 m, than this package should be inserted in an element as: $Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$ $Q_{ext,i,j,k} = 20(3 - \phi_{i,j,k})$ $Q'_{i,j,k} = 60 \text{ and } P_{i,j,k} = -20$

