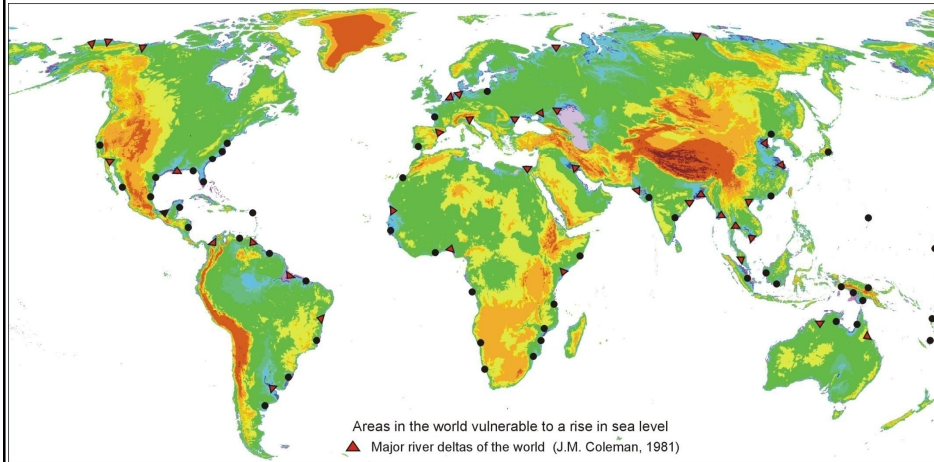


Effect sea level rise

Effects of sea level rise on groundwater resources in deltaic areas

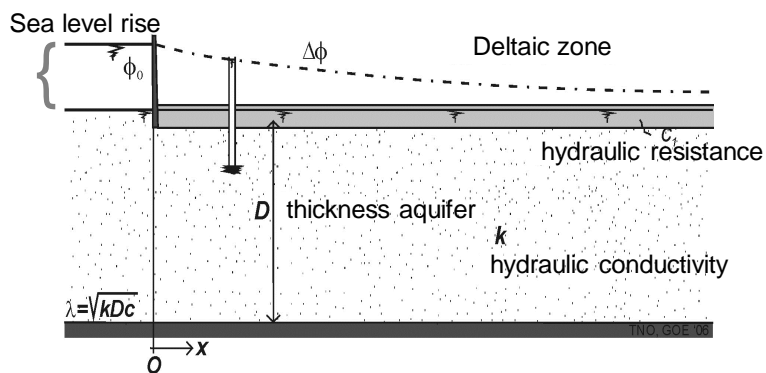
1. Increase of salt water intrusion
2. Increase of upconing under groundwater extraction wells
3. Increase of piezometric head
4. Increase of seepage and salt load to the surface water system
5. Risk of instable Holocene aquitards
6. [Decrease of fresh groundwater reservoirs due to decrease in natural groundwater recharge]

Effects of sea level rise on groundwater resources in deltaic areas



Digital Elevation Model (DEM)

Effect of sea level rise: Analytical approach for zone of influence in deltaic areas



$$\Delta\phi(x) = \phi_0 e^{-x/\lambda}$$

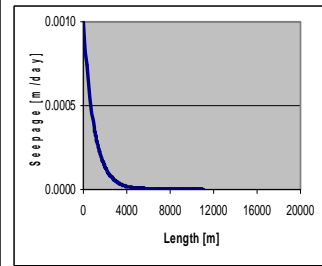
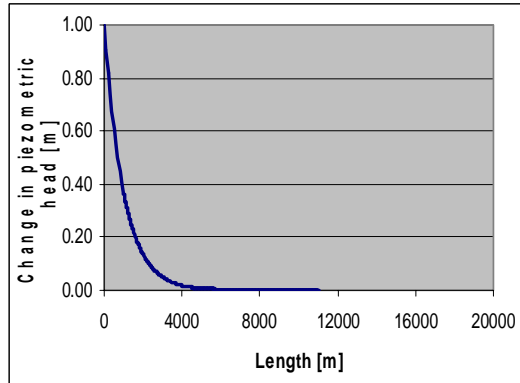
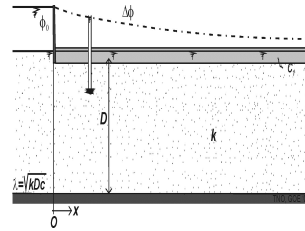
$$\lambda = \sqrt{kDc}$$

- Zone of influence is equal to \sqrt{kDc}
- At $x=3\lambda$, only 5% of sea level rise is detectable

Effect of sea level rise:

Case 1 with Dutch subsoil parameters

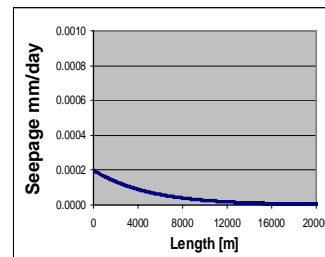
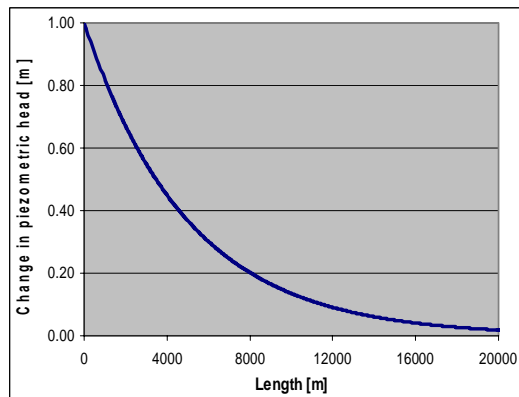
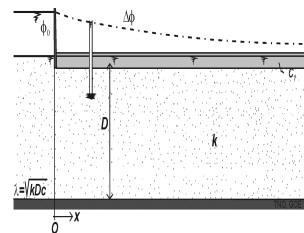
kD = 1000 m²/day
c = 1000 day
λ = 1000 m



Effect of sea level rise:

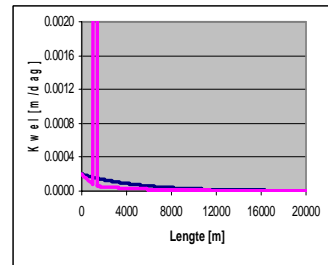
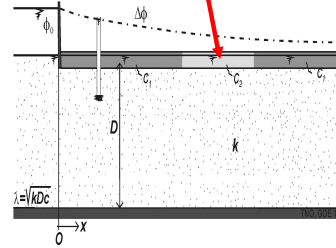
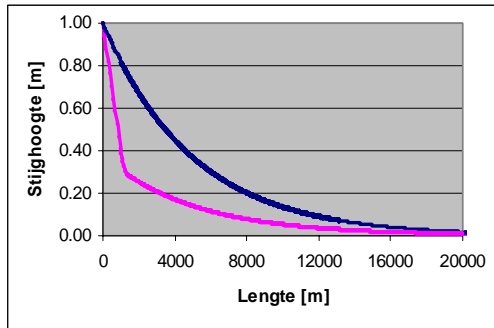
Case 2 with Dutch subsoil parameters

kD = 5000 m²/day
c = 5000 day
λ = 5000 m



Case 3 with Dutch subsoil parameters

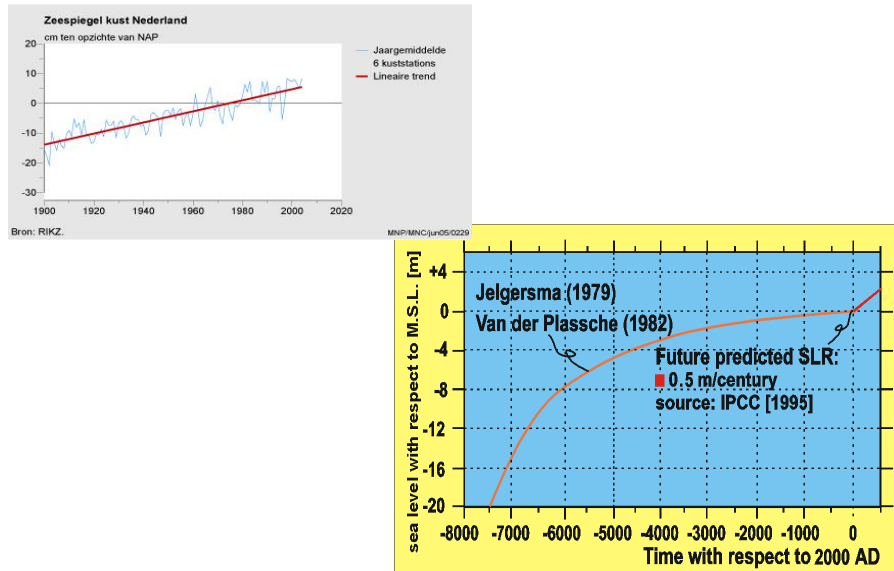
$kD = 5000 \text{ m}^2/\text{dag}$
 $c_1 = 5000 \text{ dag}, \quad c_2 = 50 \text{ dag}$



Climate change is HOT!



Past and future sea level rise in the Netherlands

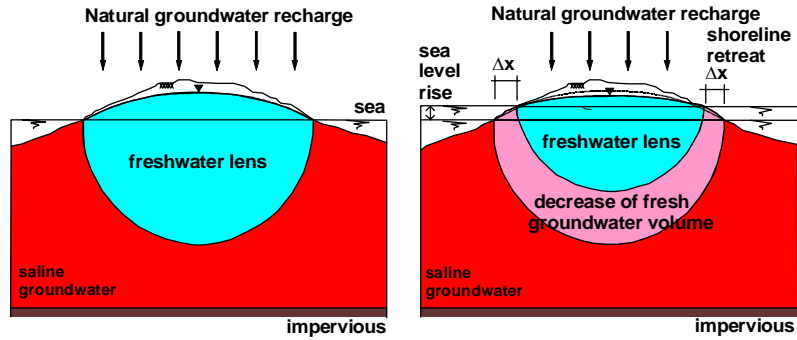


Implementing new KNMI 06 climate scenarios

2100		G	G+	W	W+	C	C+
Worldwide temperature rise in 2050		+1°C	+1°C	+2°C	+2°C	+3°C	+3°C
Worldwide temperature rise in 2100		+2°C	+2°C	+4°C	+4°C	+6°C	+6°C
Change in airstream pattern Western Europa		no	yes	no	yes	no	yes
Winter	Average temperature	+1,8°C	+2,3°C	+3,6°C	+4,6°C	+5,4°C	+6,9°C
	Coldest winter day each year	+2,1°C	+2,9°C	+4,2°C	+5,8°C	+6,3°C	+7,8°C
	Average precipitation	7%	14%	14%	28%	21%	42%
Summer	Average temperature	+1,7°C	+2,8°C	+3,4°C	+5,6°C	+5,1°C	+8,4°C
	Hottest summer day each year	+2,1°C	+3,8°C	+4,2°C	+7,6°C	+6,3°C	+11,4°C
	Average precipitation	6%	-19%	12%	-38%	18%	-57%
Sea level rise	Absolute rise (cm)	35-60	35-60	40-85	40-85	45-110	45-110

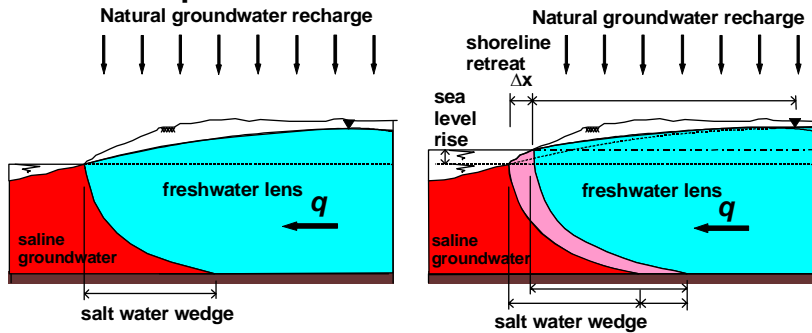
Effect of a relative sea level rise (1):

Deep aquifer

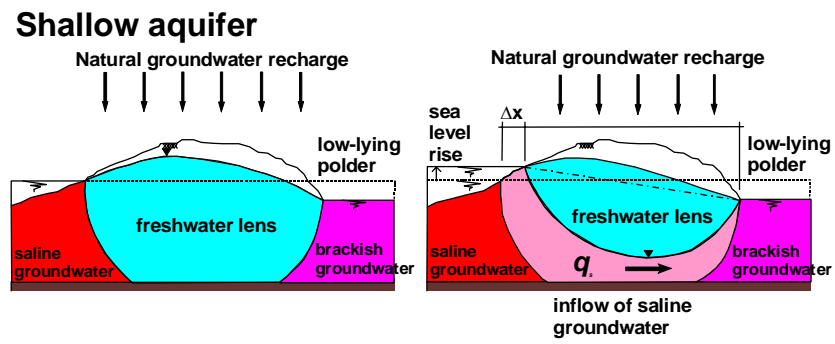


Effect of a relative sea level rise (2):

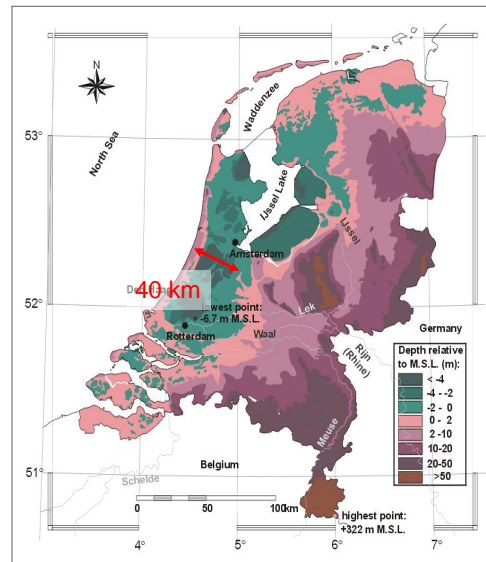
Shallow aquifer

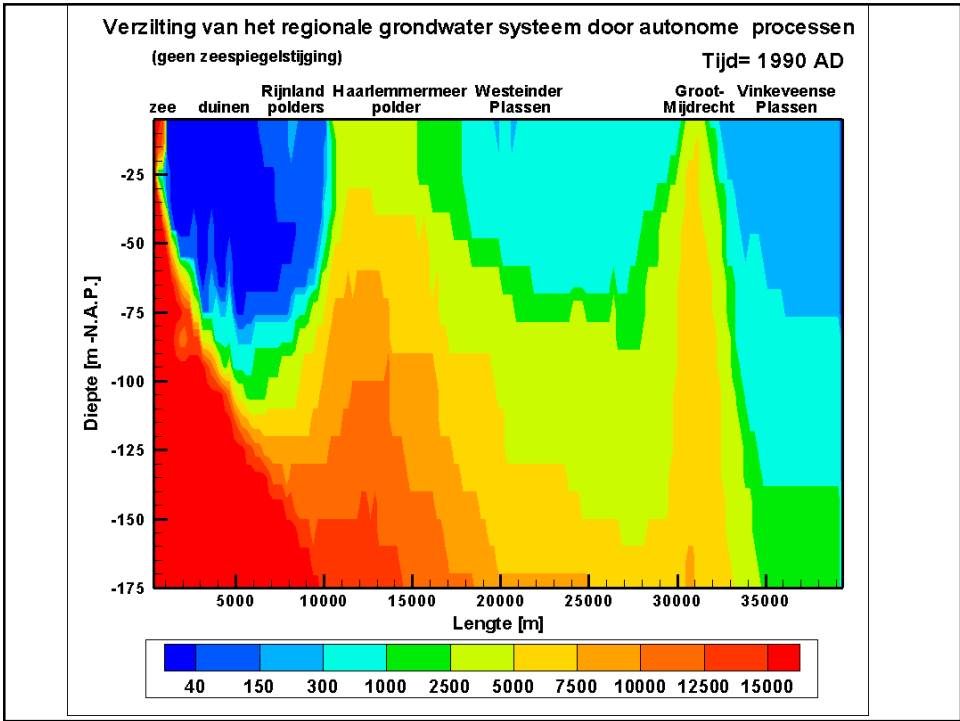
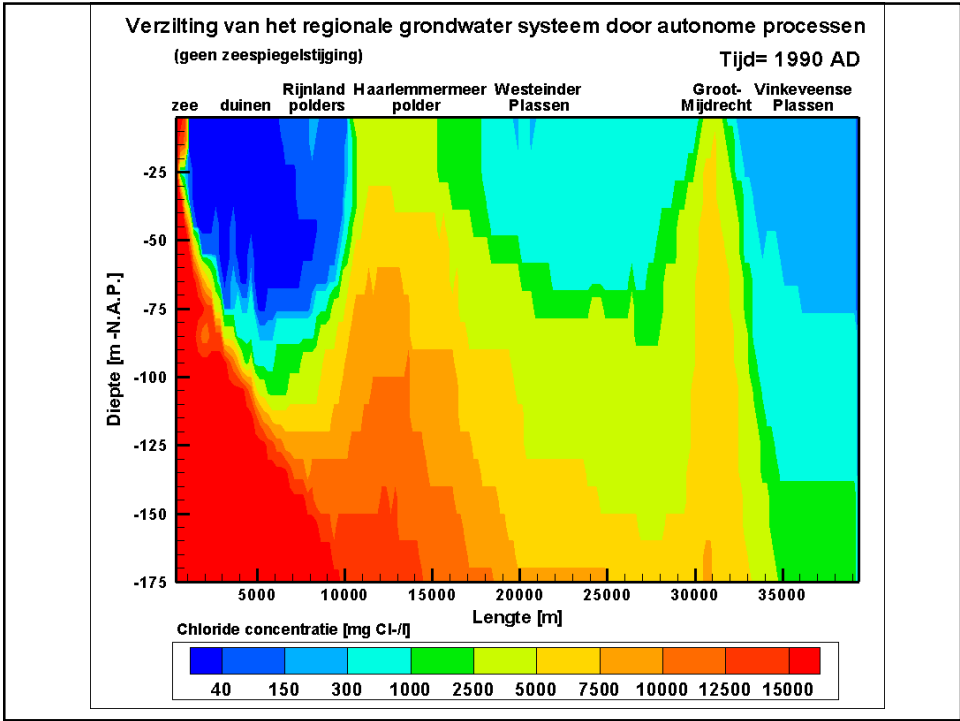


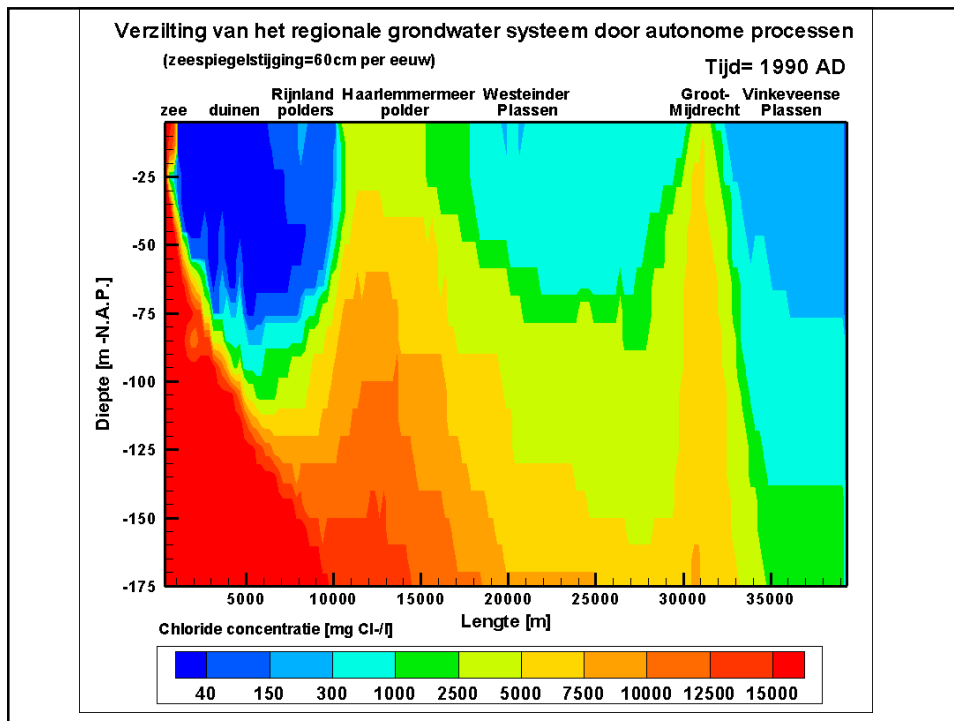
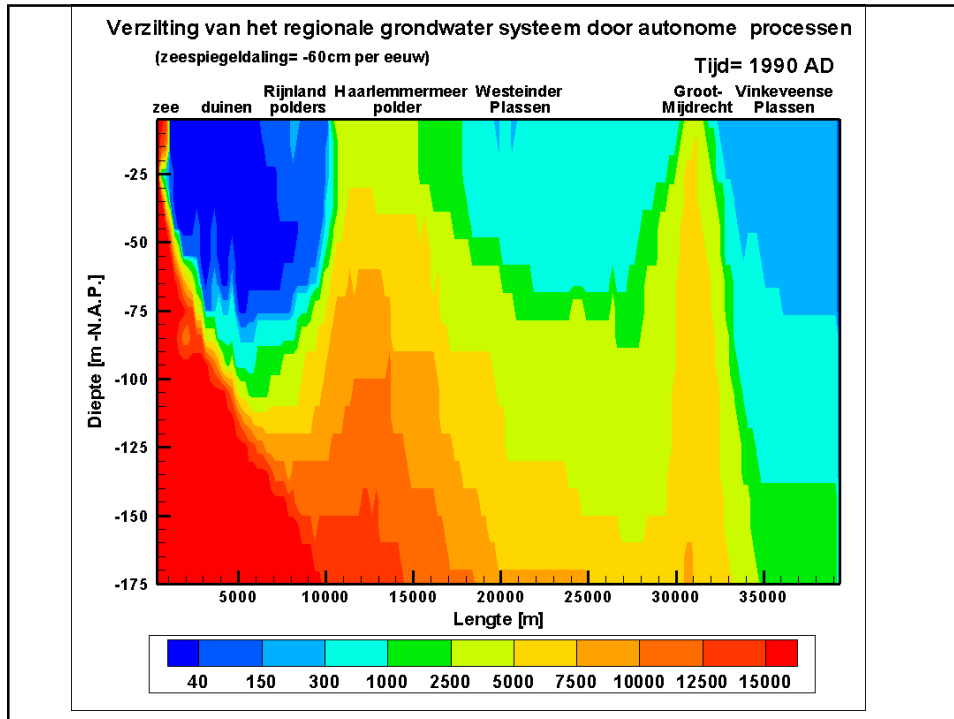
Effect of a relative sea level rise (3):

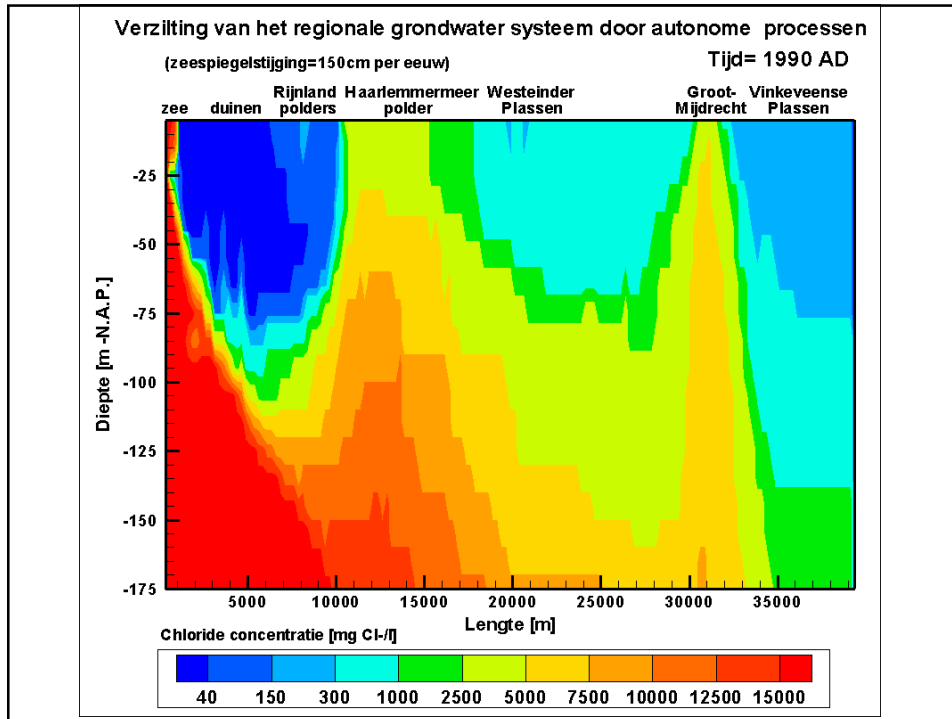


2D Profile and effect sea level rise



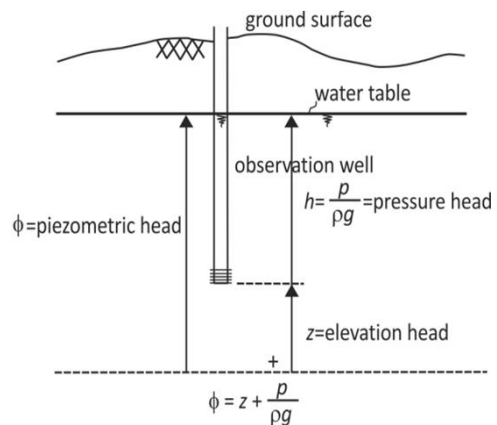






Point water head
and
Freshwater head ϕ_f

Piezometric head ϕ



$$\phi = \frac{p}{\rho g} + z$$

$$p = \rho g (\phi - z)$$

Freshwater head ϕ_f

$$\phi_f = \frac{p}{\rho_f g} + z$$

1. Groundwater with different densities can be compared
2. Fictive parameter
3. Hydrologists like to use heads instead of pressures
4. Pressure sometimes better
5. Confusing (heads not perpendicular to streamlines)

Freshwater head ϕ_f

$$h_f = \frac{\rho}{\rho_f} h$$

$$\phi_f = h_f + z$$

$$\phi_f = \frac{\rho}{\rho_f} h + z$$

e.g.:

$$\rho_s = 1025 \text{ kg/m}^3$$

$$h = 10 \text{ m}$$

$$\phi_f = 10.25 \text{ m}$$

Special case: hydrostatic pressure: $q_z = 0$

$$q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right) \quad \text{no vertical flow}$$

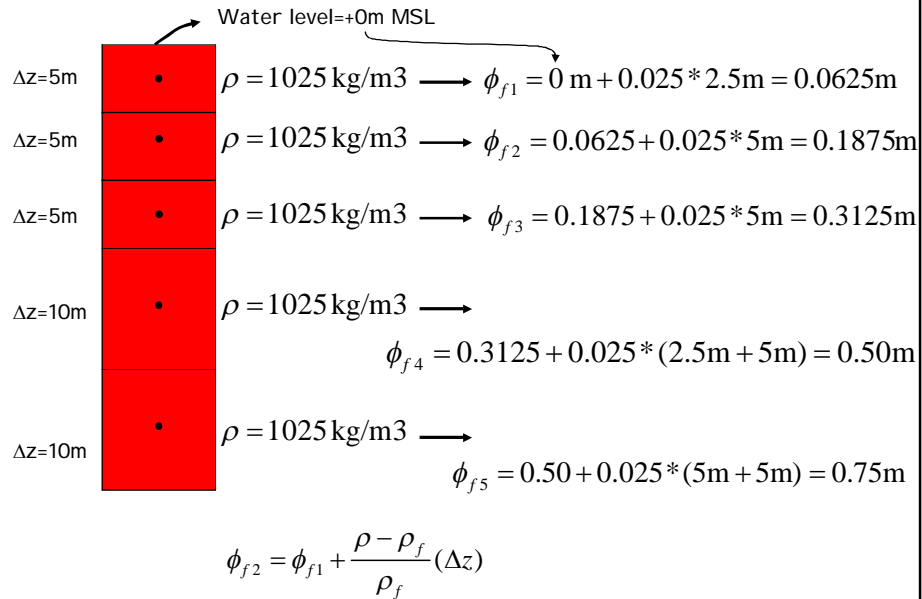
$$0 = \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$\frac{\partial \phi_f}{\partial z} = -\frac{\rho - \rho_f}{\rho_f} \partial z$$

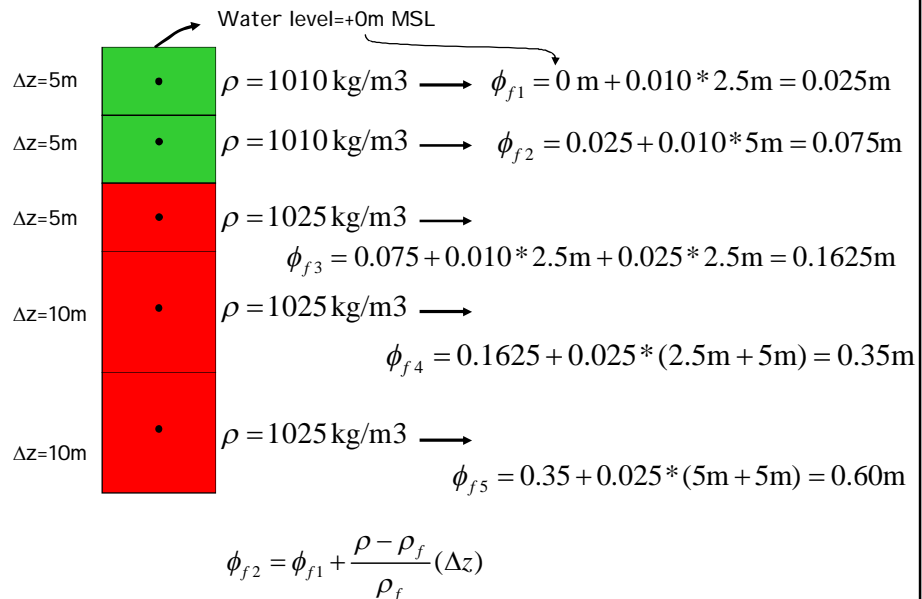
$$\phi_{f2} = \phi_{f1} - \frac{\rho - \rho_f}{\rho_f} (z_2 - z_1)$$

$$\downarrow + \quad \phi_{f2} = \phi_{f1} + \frac{\rho - \rho_f}{\rho_f} (\Delta z)$$

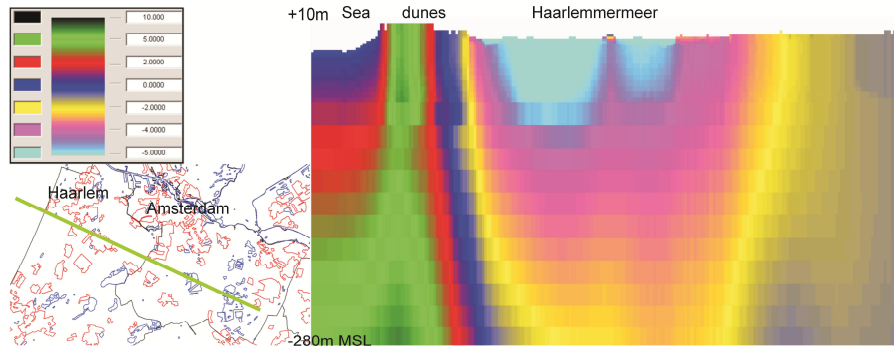
Hydrostatic boundary condition at the sea



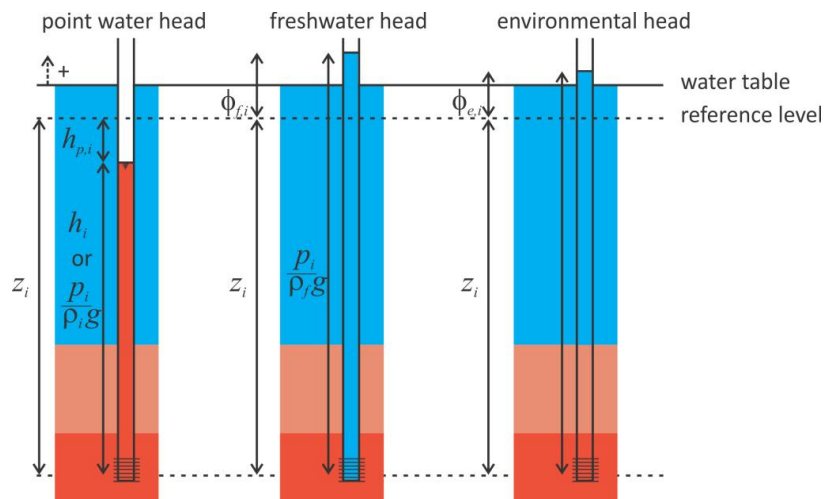
Hydrostatic boundary condition at the sea



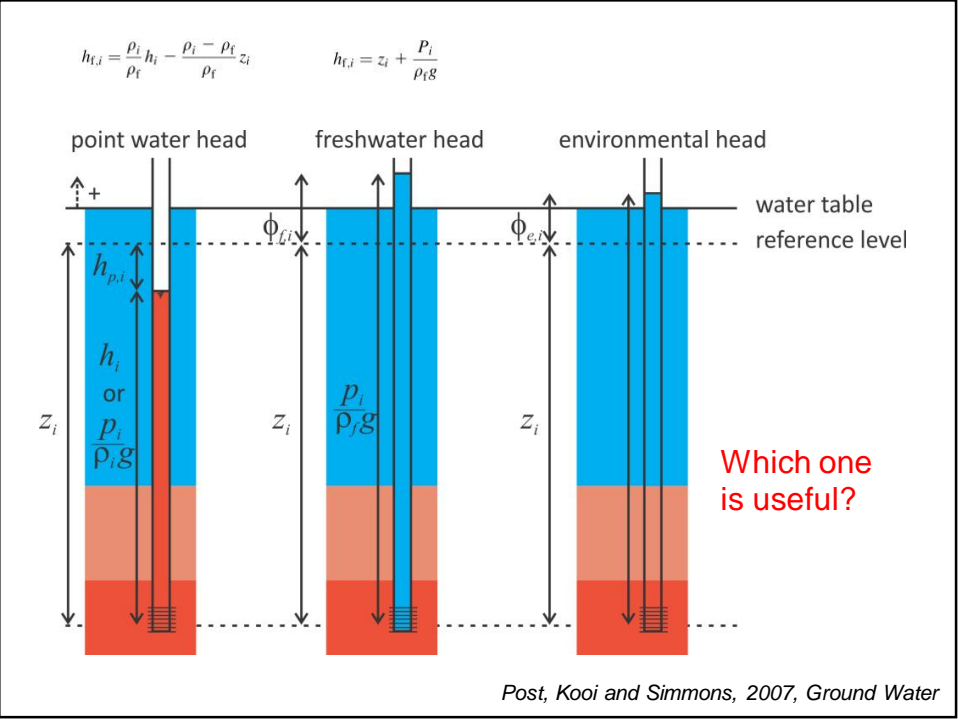
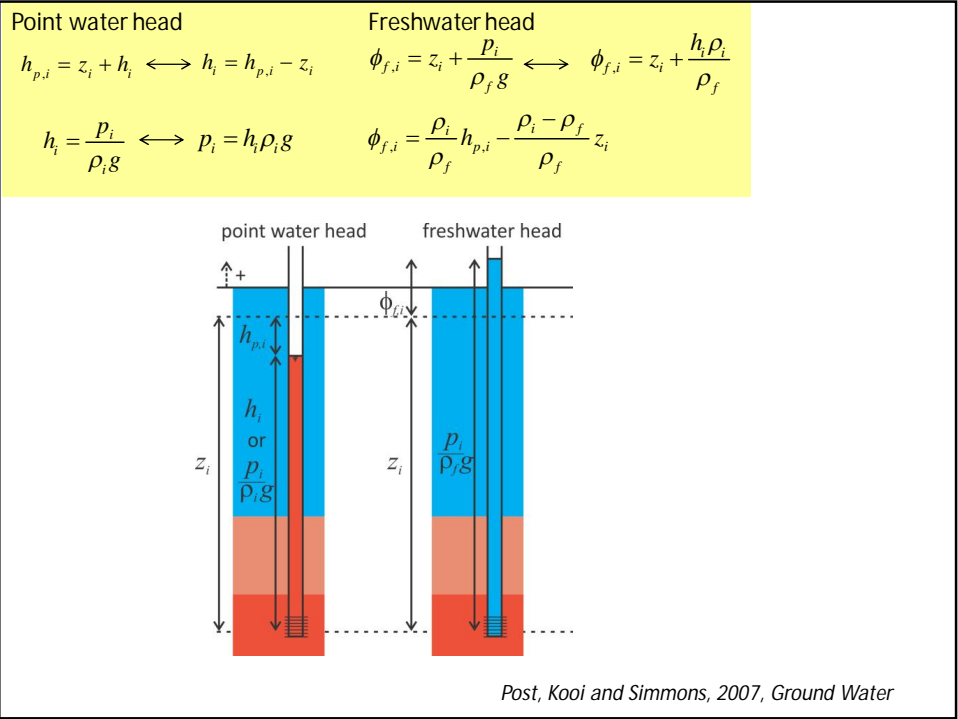
Example 2D profile NHI model freshwater head ϕ_f

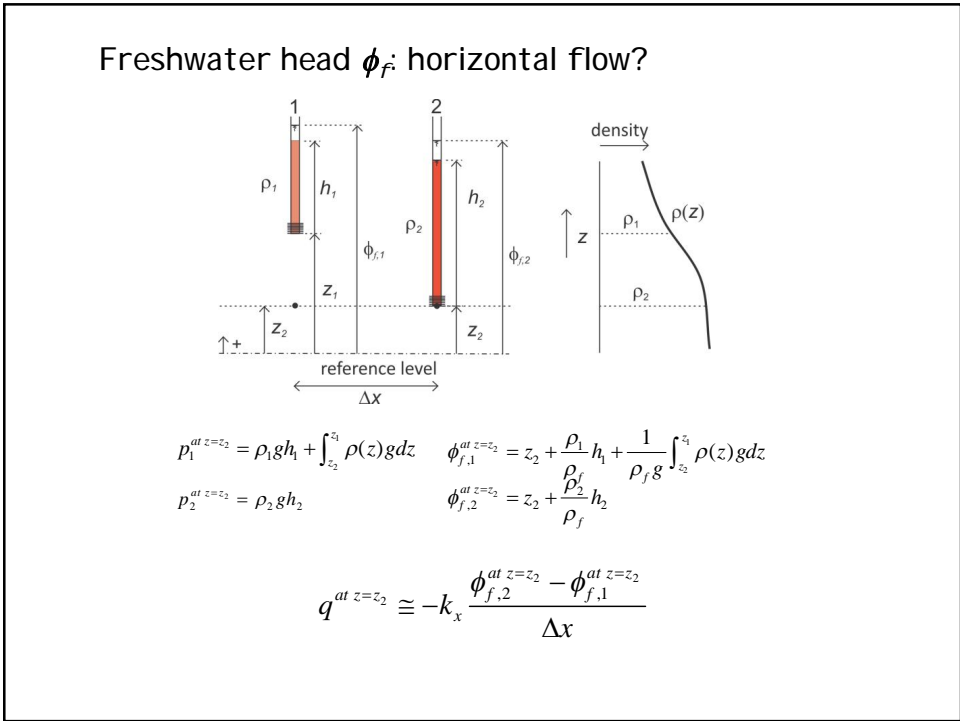
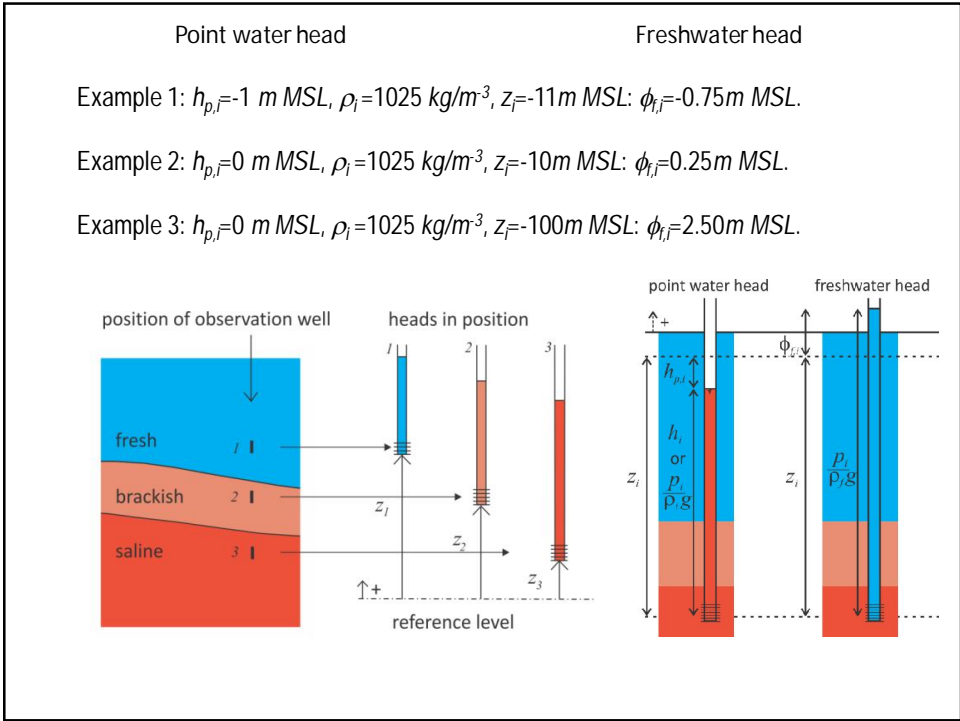


Which one is useful?

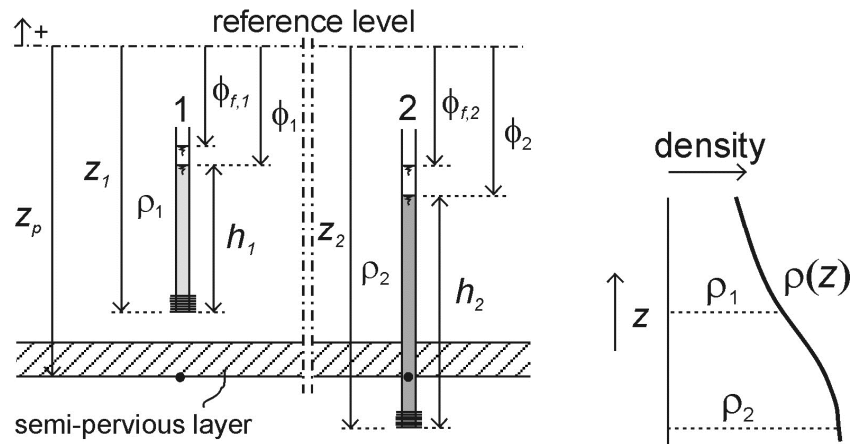


Post, Kooi and Simmons, 2007, Ground Water

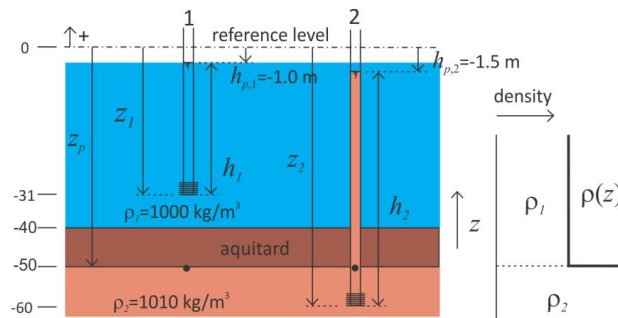




Freshwater head ϕ_f : vertical flow?

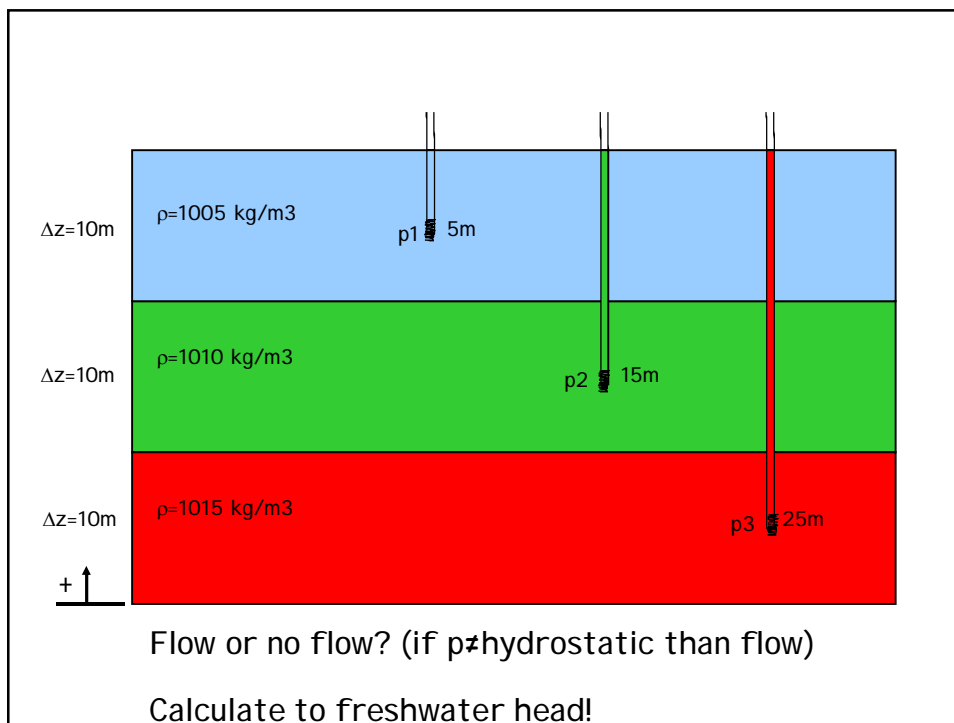
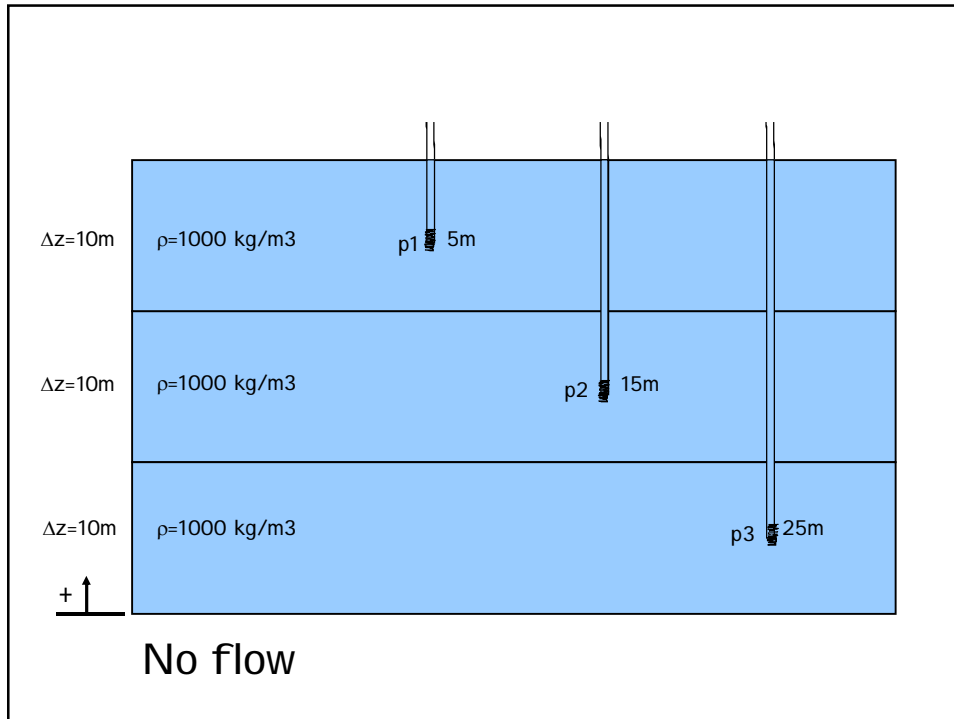


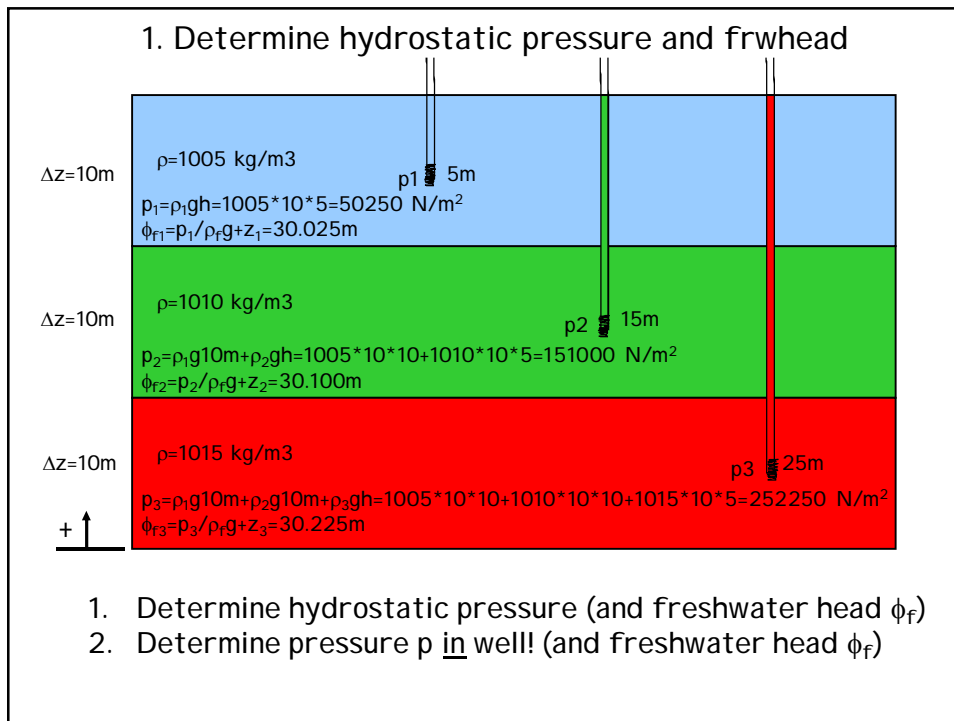
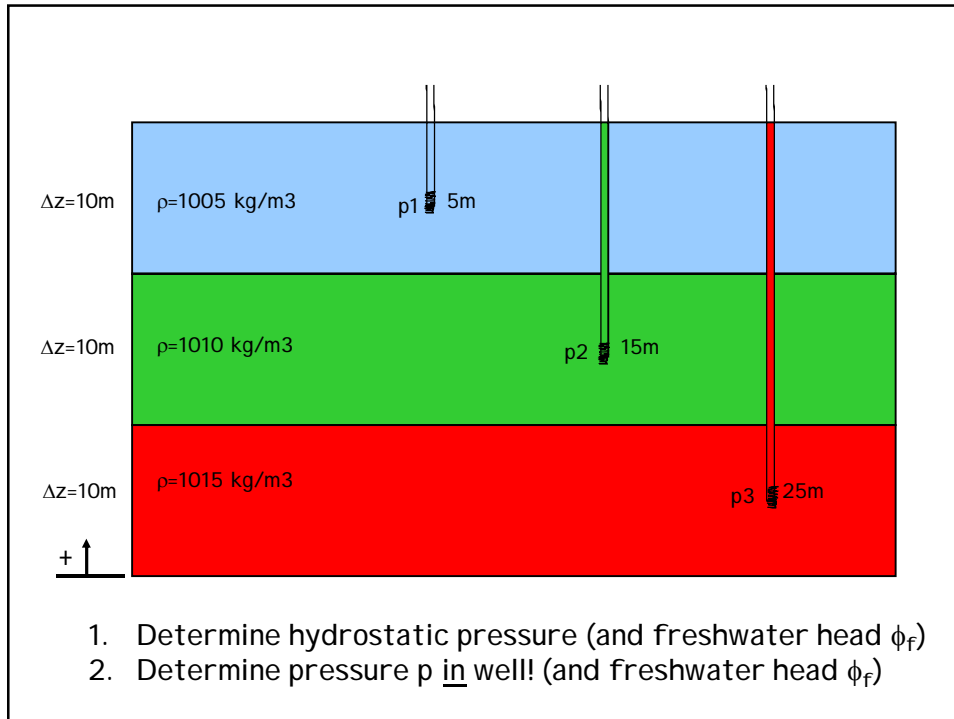
Freshwater head ϕ_f



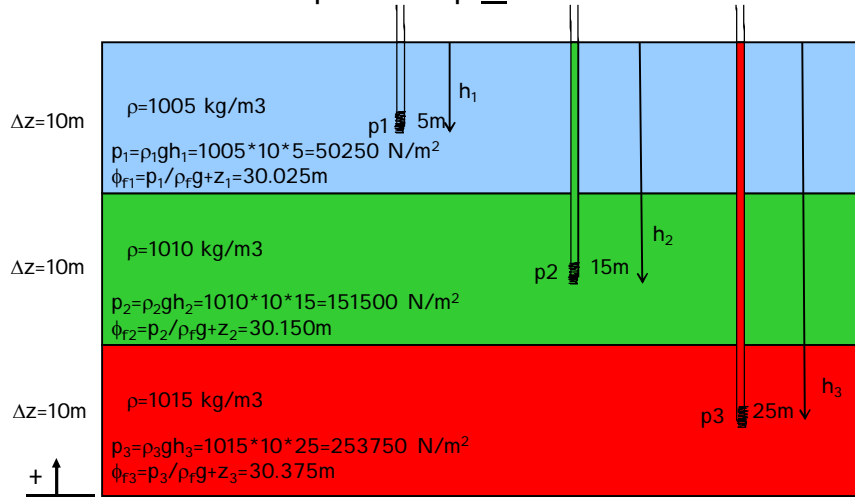
$$\phi_{f,1}^{z=-50} = -50 + \frac{1000}{1000}30 + \frac{1}{1000g} \int_{-50}^{-31} 1000g dz = -50 + 30 + 19 = -1.0$$

$$\phi_{f,2}^{z=-50} = -50 + \frac{1010}{1000}58.5 - \frac{1}{1000g} \int_{-60}^{-50} 1010g dz = -50 + 59.085 - 1.01(-50 + 60) = -1.015$$



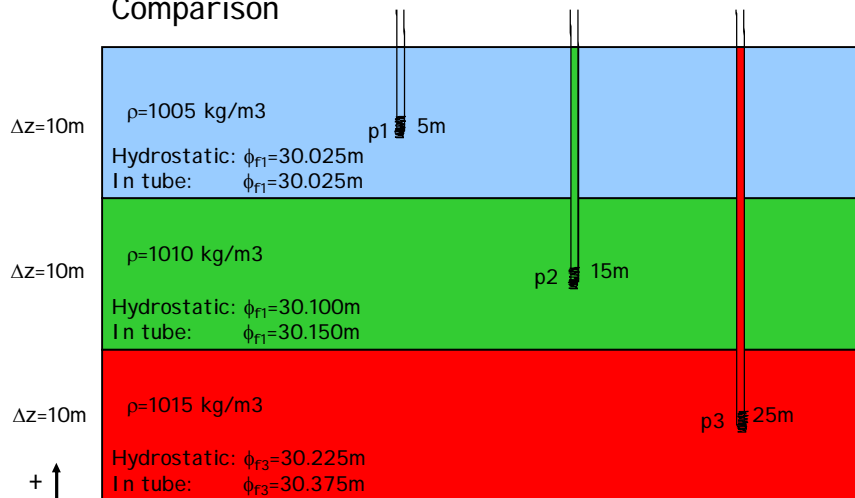


2. Determine pressure p in well and frwhead



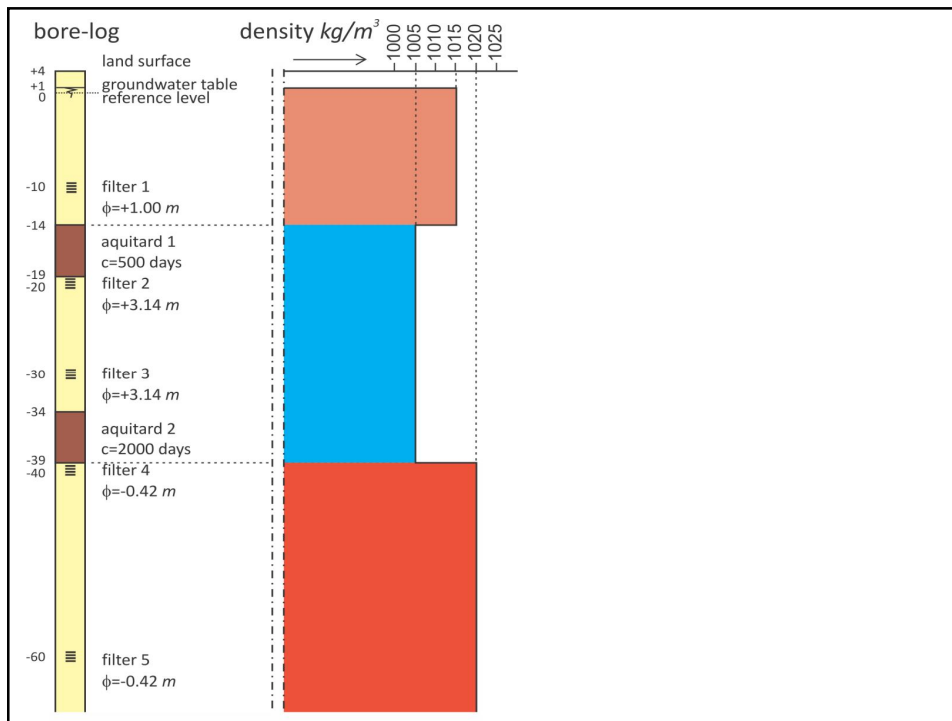
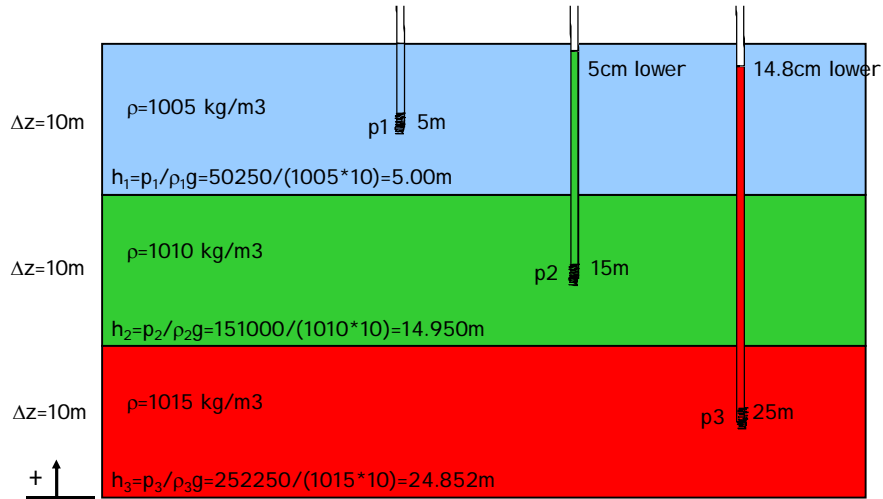
1. Determine hydrostatic pressure (and freshwater head ϕ_f)
2. Determine pressure p in well! (and freshwater head ϕ_f)

Comparison



Conclusion: freshwater head not equal, so vertical upward flow!

What would be the water level in the tube if hydrostatic?

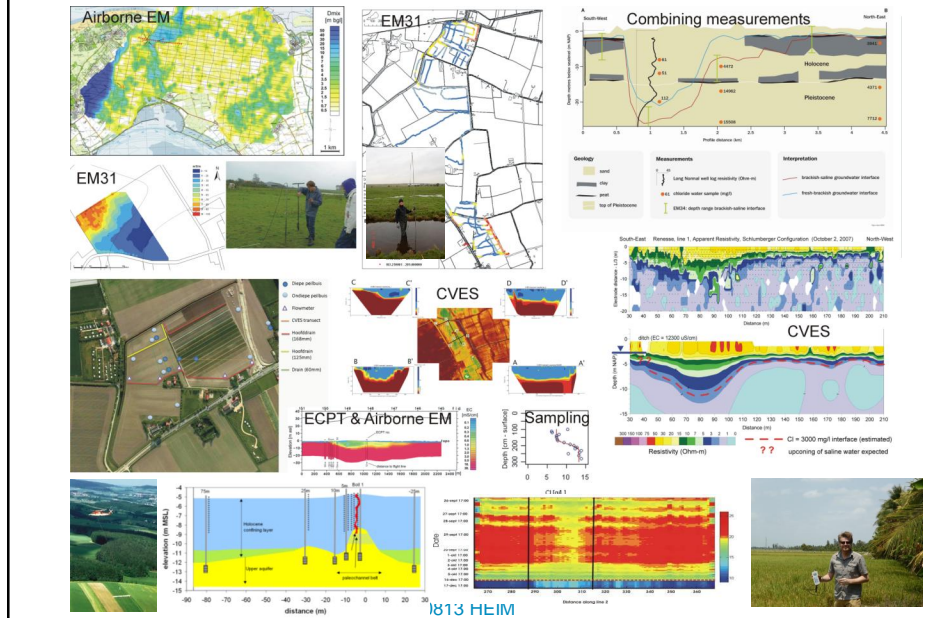


Take home message

1. In coastal area (with fresh-brackish-saline groundwater), always measure head and Electrical Conductivity (EC)
2. Convert EC to density
3. Determine freshwater head with lecture notes and ppt
4. Determine flow

Monitoring

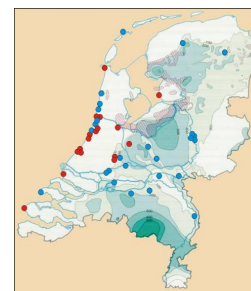
Different (fresh-salt) monitoring techniques



Monitoring salt in groundwater

- Why monitoring?
 - Mapping salt concentrations in the groundwater
 - Detection of trends (upconing near pumping stations)
 - System and process knowledge
 - Input for a groundwater model

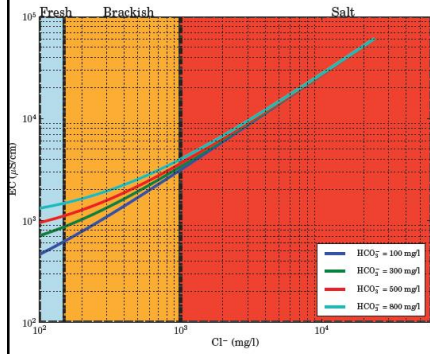
- Methods:
 1. Direct: water sample available
 2. Indirect: conductance of the subsoil



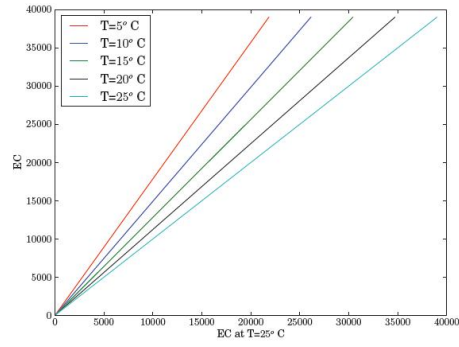
- Pumping stations with salinisation
- Pumping stations closed due to salinisation

Source: V. Post, 2007

EC and Chloride



EC-Cl at different HCO_3^- concentrations.

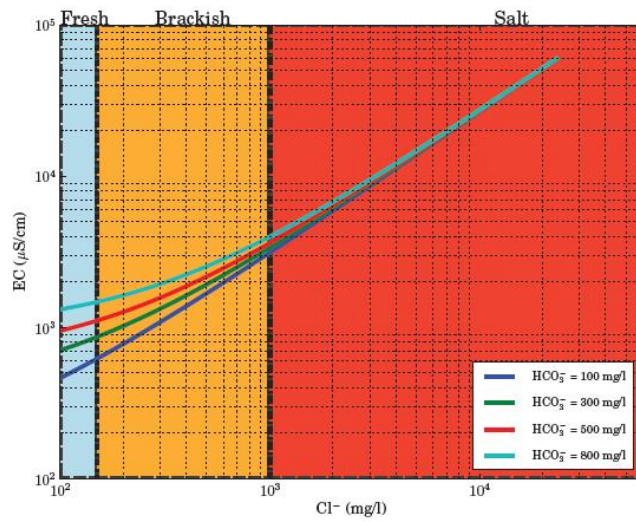


(b) EC and temperature standardized EC.

P. Pauw, 2009

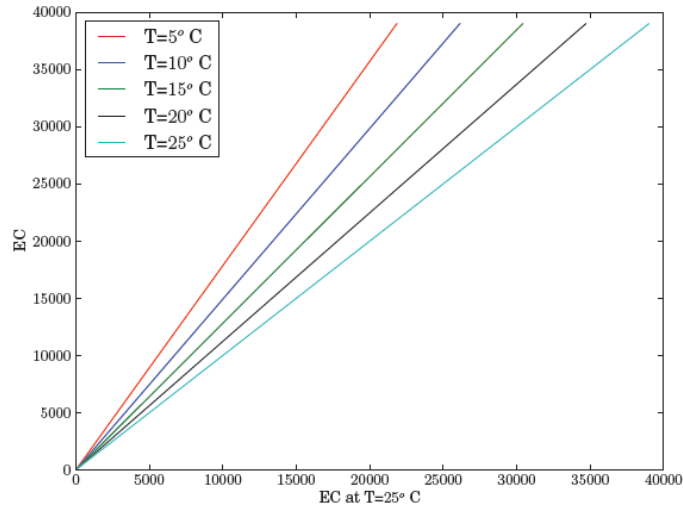
20120622 SWIM22

EC and Chloride



20120622 EC-Cl at different HCO_3^- concentrations.

EC and Chloride



²¹ (b) EC and temperature standardized EC.

Airborne measurements

Measuring system	Physical parameter	Geology/terrain information
radar	EM traveltime	Terrain elevation
Infrared photography	Infrared radiation	Surface temperature
Time domain EM Frequency domain EM	Electr. resistivity from induced EM fields	Lithology Water salinity
Magnetic gradiometer	Magnetic field (variations)	Lithology (magnetite) Artefacts Steel/Iron objects
Spectral gamma	Radiation (gamma)	Soil type Surface lithology Recent disturbance

Source: Koos Groen

Surface measurements

Measuring system	Physical parameter	Geology/terrain information
Ground penetrating radar	EM traveltime, dielectric constant,	Lithology Soil moisture
ERT	Electr. resistivity	Lithology Water salinity
Time domain EM Frequency domain EM	Electr. resistivity	Lithology Water salinity
Magnetometer (total field, gradiometer)	Magnetic field (variations) magnetic susceptibility	Lithology (magnetite) Artefacts Steel/Iron objects (UXO)
Spectral gamma	Radiation (gamma)	Soil type Surface lithology Recent disturbance

Source: Koos Groen

Cone Penetration Tests

Measuring system	Physical parameter	Geology/terrain information
mechanical CPT	Cone resistance Friction resistance	Lithology Geotechnical parameters
Electrical conductivity	Electrical formation conductivity	Water salinity
Continuous water pressure	Water pressure	Lithology Piezometric head
Water pressure dissipation in clay layers	Water pressure in time	Permeability clays
BAT sampling in CPT casing		Water chemistry
ROST, MIP		Contamination of hydrocarbons (high concentration)
Camera sonde	Visual view	Lithology, contamination, gas

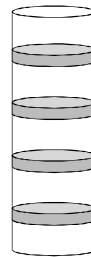
Source: Koos Groen

Monitoring salt in groundwater: Direct methods

Method	Advantage	Disadvantage
1. Observation well	<ul style="list-style-type: none"> •High accuracy •Detection trends 	<ul style="list-style-type: none"> •Costly •Point measurement
2. Well screens in observation well	<ul style="list-style-type: none"> •High accuracy •Detection trends •High vertical resolution 	<ul style="list-style-type: none"> •Costly
3. Sediment sample (extraction milliliters of water)	<ul style="list-style-type: none"> •High accuracy •High vertical resolution 	<ul style="list-style-type: none"> •Very costly and time consuming



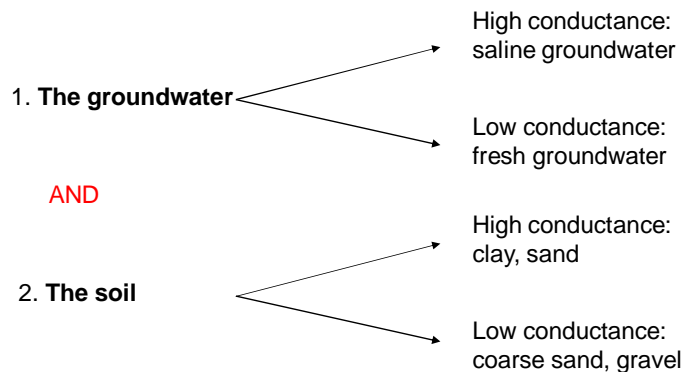
Direct methods 1 and 2



Source: V. Post, 2007

Monitoring salt in groundwater: Indirect methods

Indirect methods measure the **conductance** of:



Hence information about the lithology (sand, clay etc) is needed!

Source: V. Post, 2007

Monitoring salt in groundwater: Indirect methods

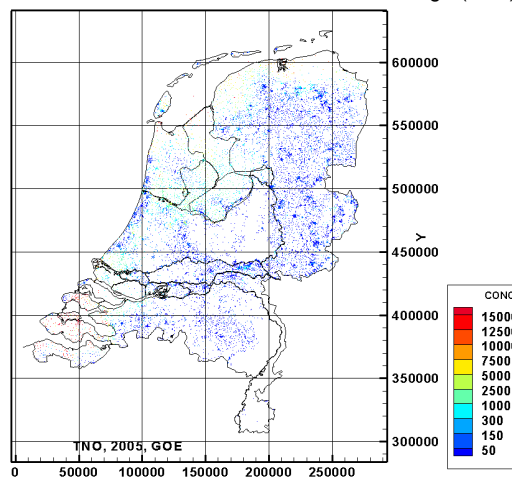
Method	Advantages	Disadvantages
1. Electrical conductance measurements	<ul style="list-style-type: none"> •High resolution (3D) •Depth ~200 m 	<ul style="list-style-type: none"> •Time consuming
2. Electromagnetic measurements	<ul style="list-style-type: none"> •Fast 	<ul style="list-style-type: none"> •Limited vertical resolution •Sensitive for underground conductors (pipes)
3. Satellites	<ul style="list-style-type: none"> •Suitable for large areas 	<ul style="list-style-type: none"> •Small vertical resolution •Low accuracy

Source: V. Post, 2007

Method used at Deltares

Number of measurements bottom Holocene top layer :
direct methods and Vertical Electric Soundings (VES)

- Combination of:
- Direct measurements
 - Electrical conductance measurements
 - Surface (VES)
 - Borehole



Source: Oude Essink et al (2005)

Electrical conductance measurements

1. Measuring:

- **Inside a borehole**
- From surface level
- From the air



Source: TNO

Source: V. Post, 2007

Electrical conductance measurements

1. Measuring:

- Inside a borehole
- **From surface level (depth ~ 200 m)**
- From the air



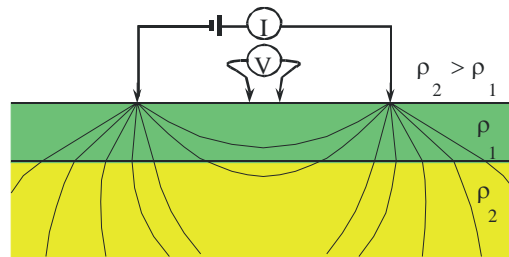
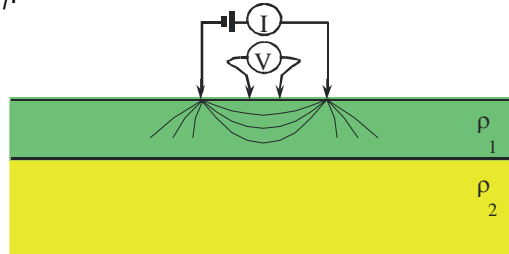
Source: V. Post, 2007



Source: Vitens

Principle geo-elektrical measurement

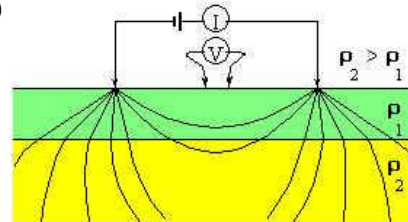
I: currentelektrode, V: potentialelektrodes, Ra: appearant elektrical resistivity
 $R_a = \text{constant} \cdot V/I$



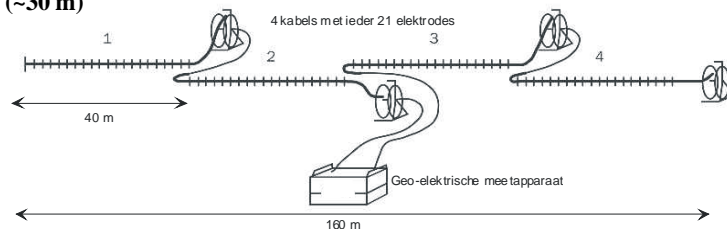
20120622 SWIM22

Types geo-elektrical measurements

- I Vertical Electrical Sounding (VES)
- 4 elektrodes at surface
- 1D elektrical resistivity profile
- Labor intense
- Accurate, great depths
- Deep hydrogeology



- II Continue Vertical Elektrical Sounding (CVES)
- >80 elektrodes at surface
- 2D elektrical resistivity subsurface
- Limited depth (~30 m)



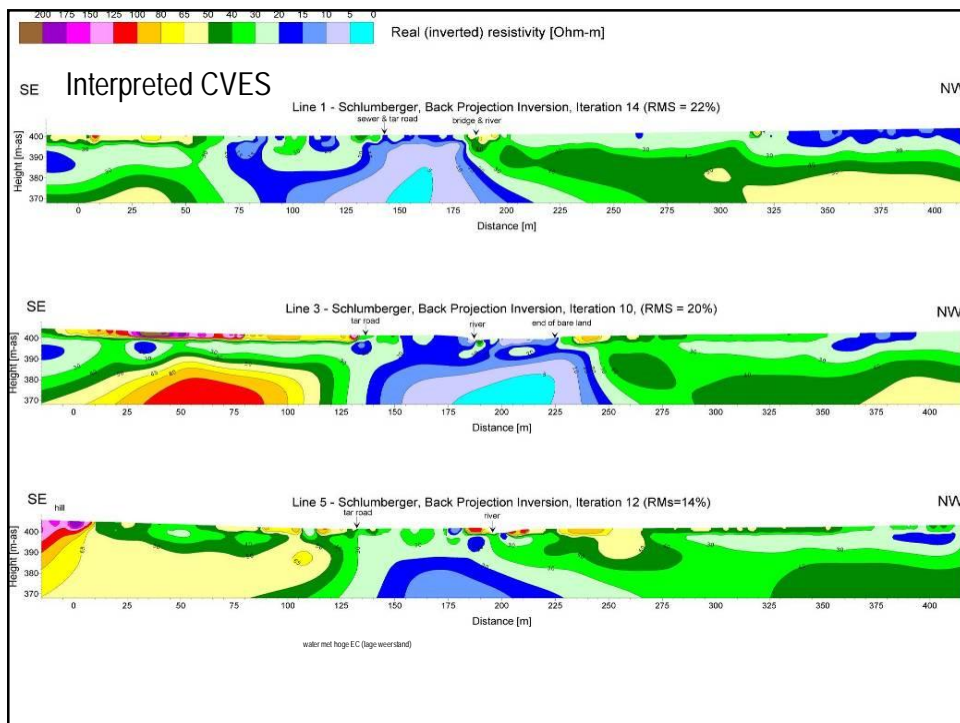
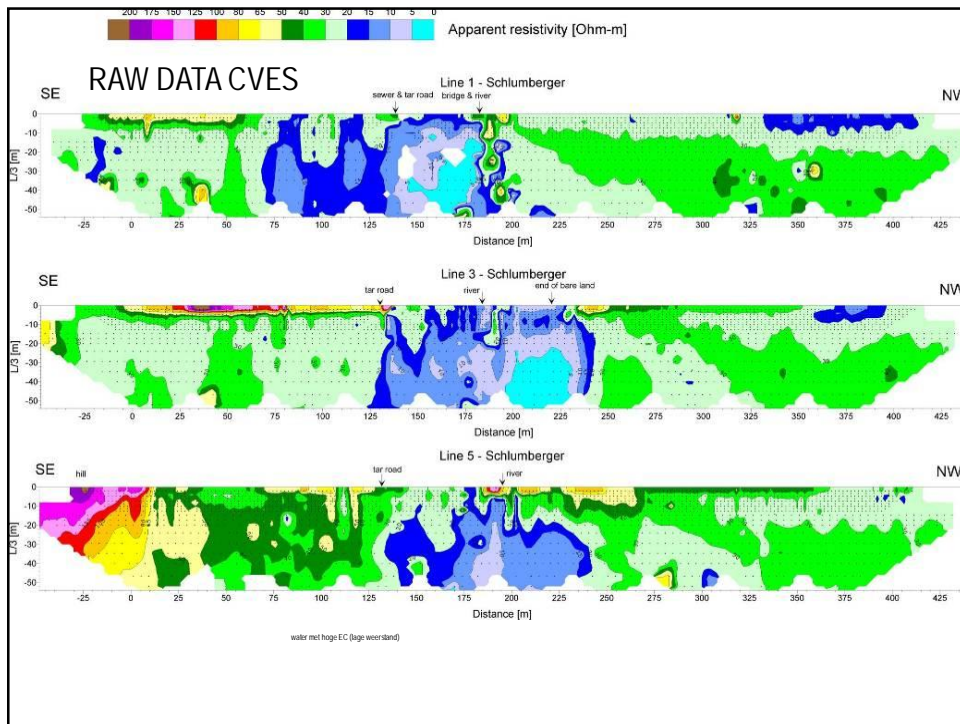
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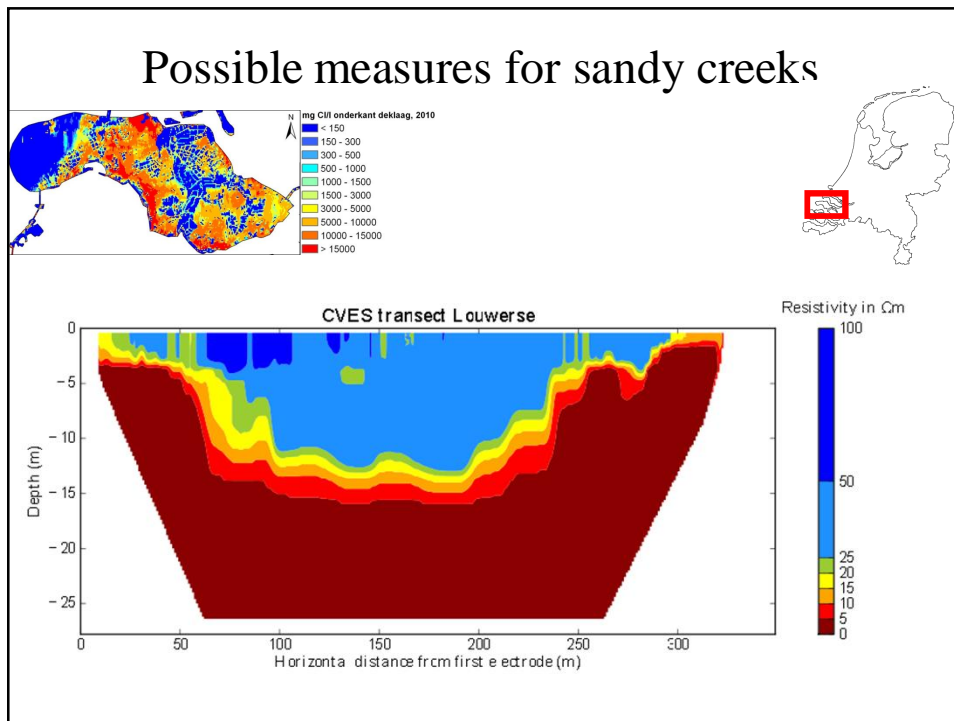
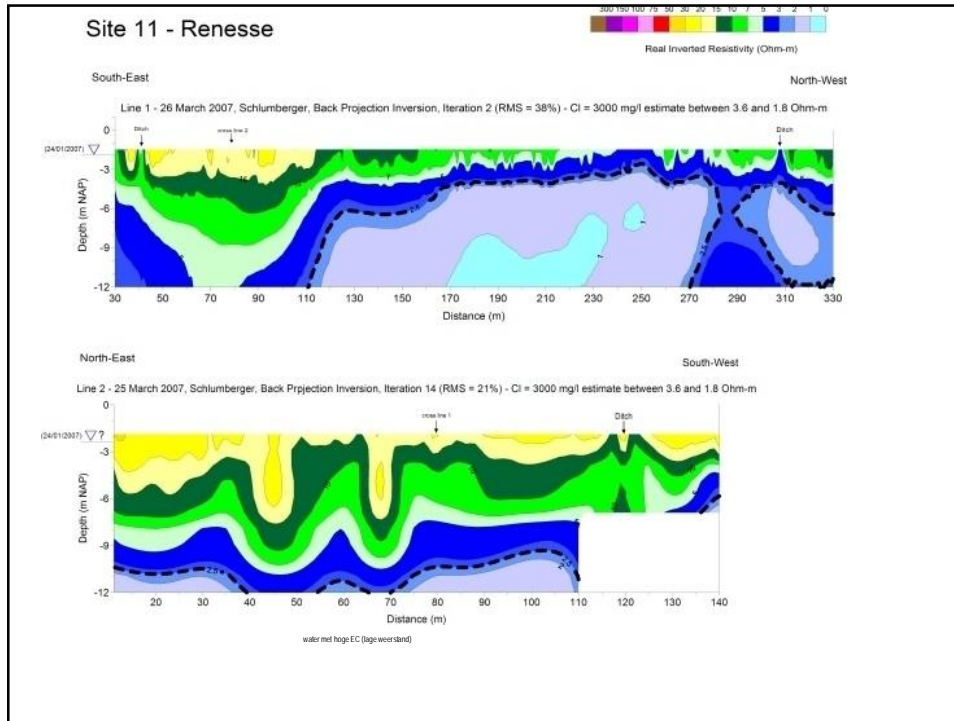
VES measurement end 1950s/begin 1960s



CVES
measurements 2010s







Monitoring salt in groundwater: Indirect methods

- Electrical conductance measurements

$$\rho_s = F \cdot \rho_w$$

ρ_s = resistance subsoil & groundwater
 ρ_w = resistance groundwater
 F = formation factor

Lithology	F
Gravel with sand	7
Coarse sand	5
Sand with silt	2 - 3
Clay	1-3*
peat	1*

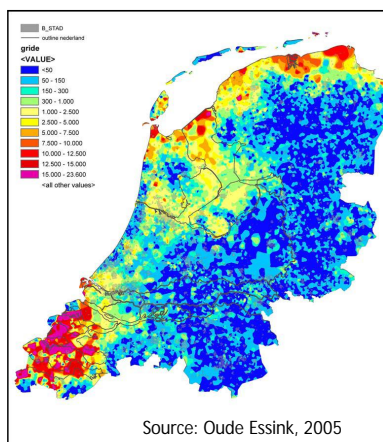
F varies with the resistance of the groundwater

If the lithology is known AND the measurement is in an aquifer
 → ρ_w can be calculated

VES measurements are used in combination with borehole logging

Source: Oude Essink, 2005

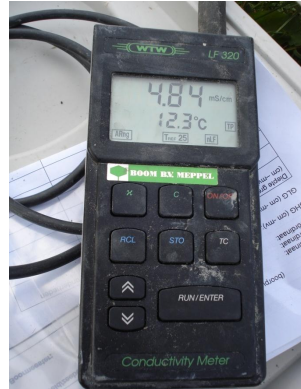
Result: chloride concentration bottom Holocene toplayer



Source: Oude Essink, 2005

- Software Geological Survey of the Netherlands (TNO) is used to determine the salt concentration of the groundwater in the measurements
- Inter- and extrapolation is used to make a continuous field
- 2D Result is a combination of:
 1. Direct measurements (3500)
 2. Electrical conductance in boreholes (2000)
 3. Vertical Electric Sounding (VES) measurements (10.000)

T-EC probe



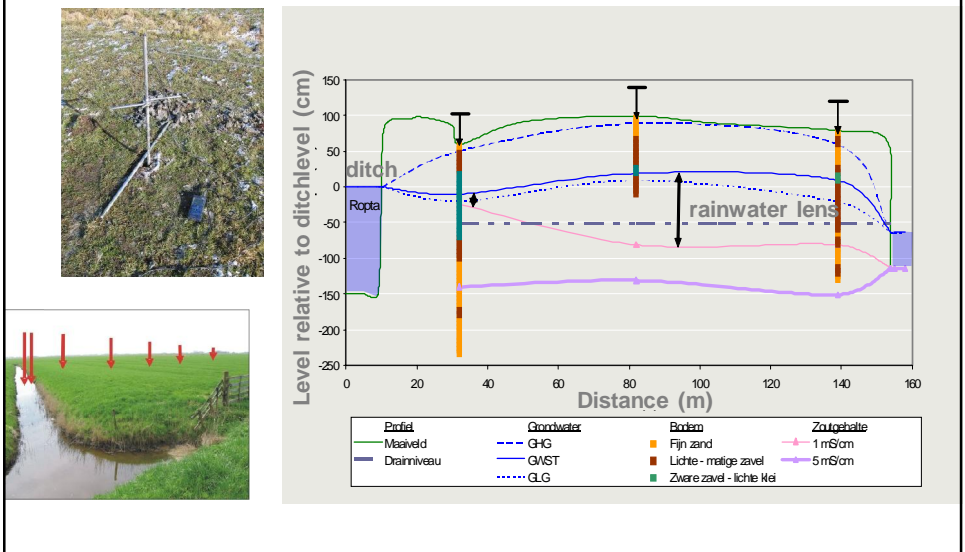
T EC fieldwork

Altitude measurements

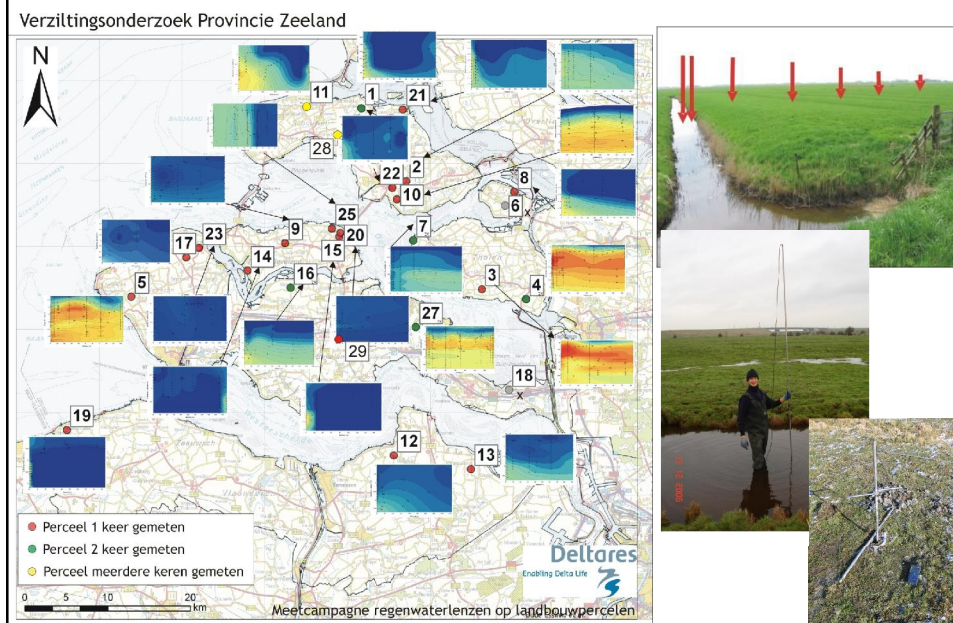




Use field measurements to understand the process



TEC-probe Monitoring campaign 2005-2009

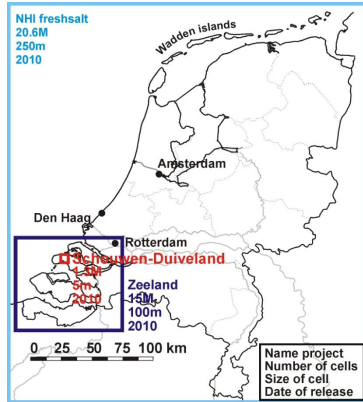


CliWat www.cliwat.eu

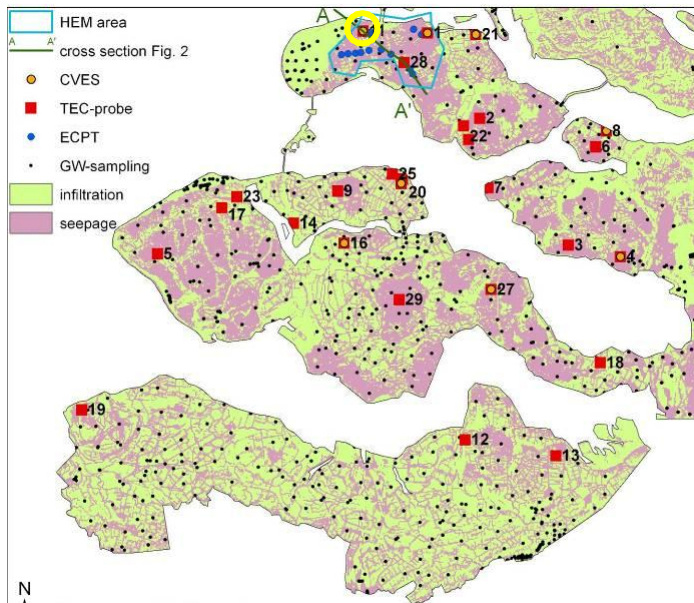
- Transnational project in the North Sea Region
- Main objectives:
 - to evaluate the physical and chemical impacts of climate change on groundwater and surface water systems
 - to provide data for adaptive and sustainable water management and infrastructure.
- Different innovative monitoring techniques (Helicopter EM, CVES, CPT, TEC-probe) are used to map the salinization status of the coastal groundwater system.



Description local area



Monitoring network in our Pilot Area Zeeland



Up to local approach

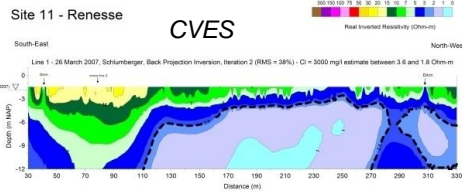
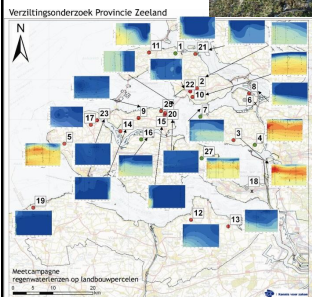
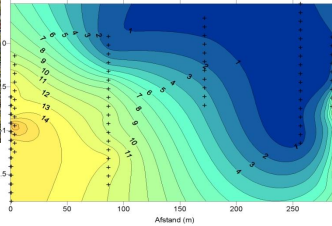
Example: Assessing effect of climate change on salt water intrusion

Monitoring:

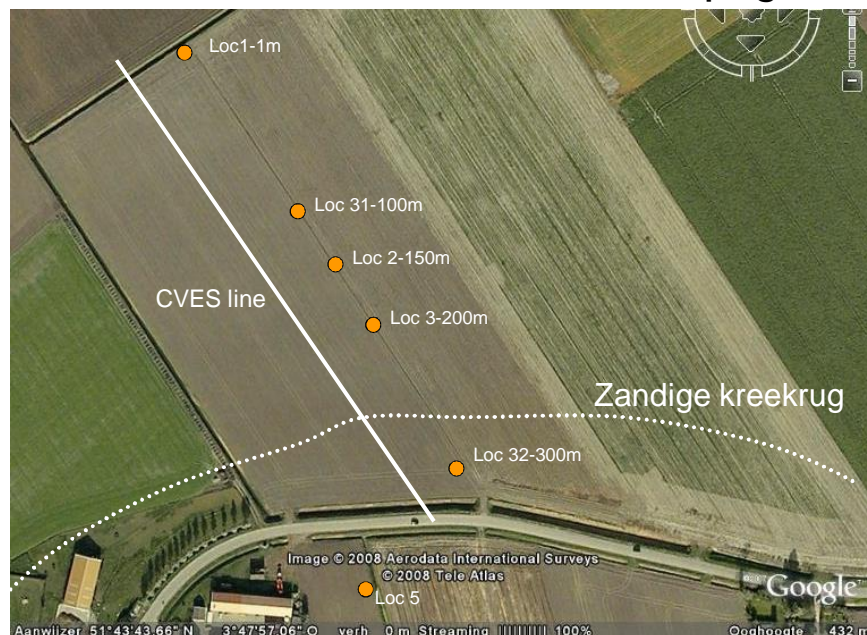
- piezometric head and solute concentration
- TEC probes, CVES
- online

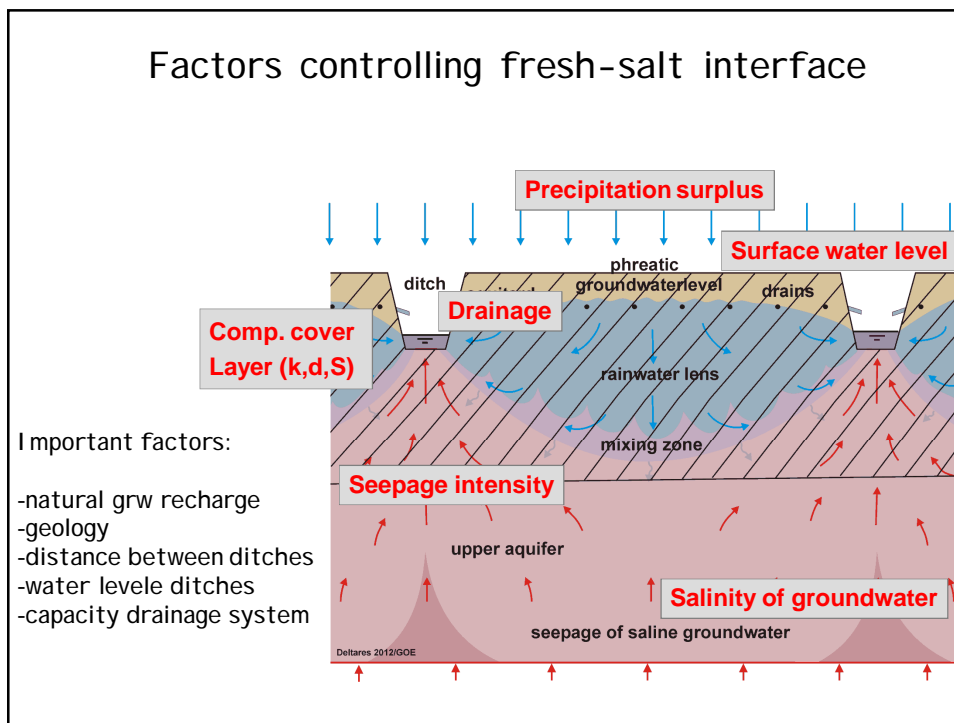
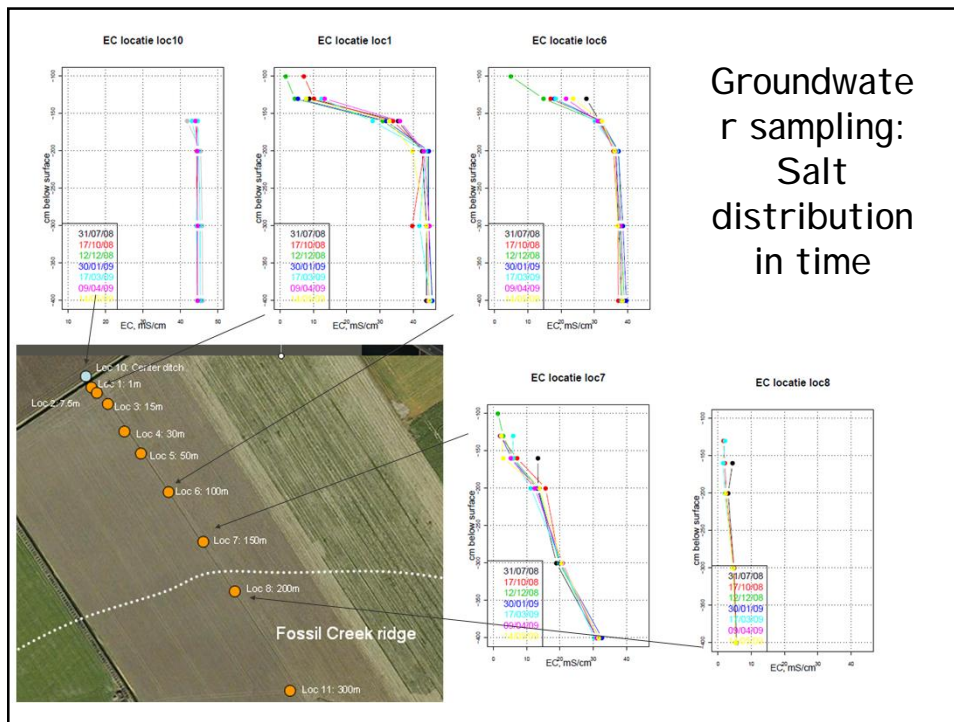
Source: Oude Essink, 2009

TEC probe

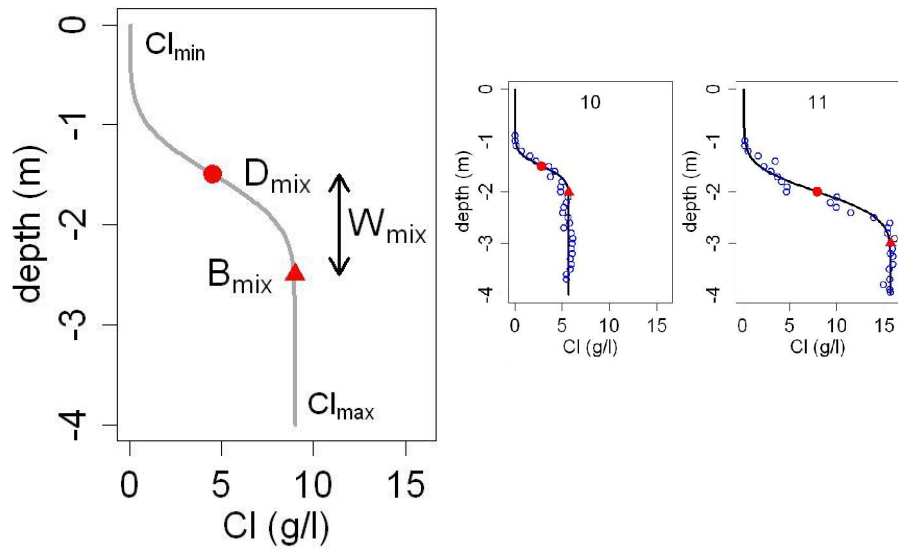


Site 11: from infiltration to seepage

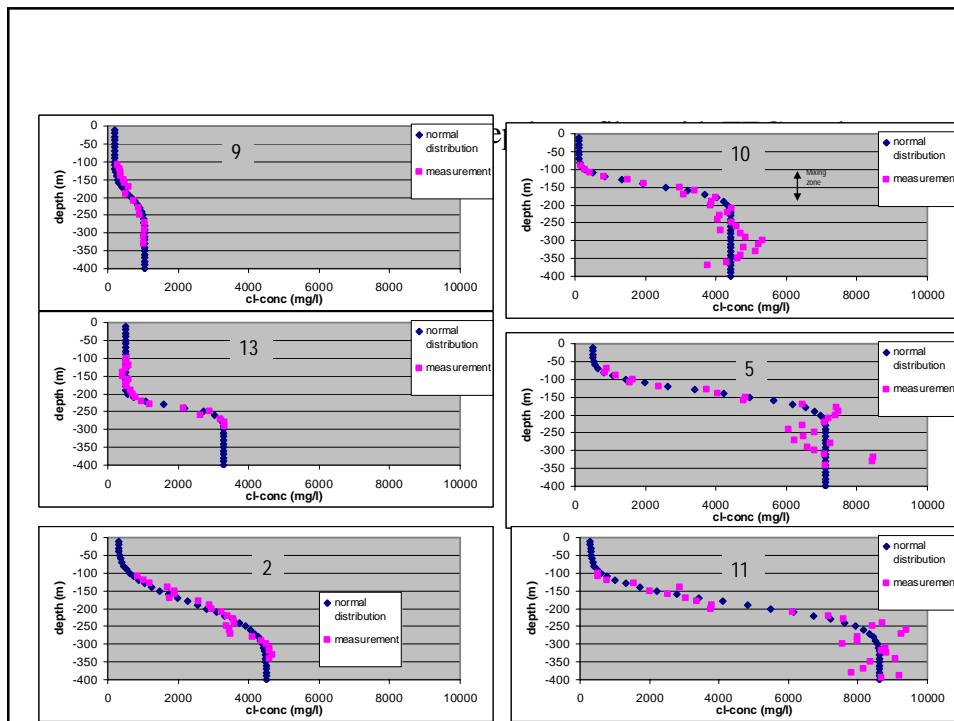


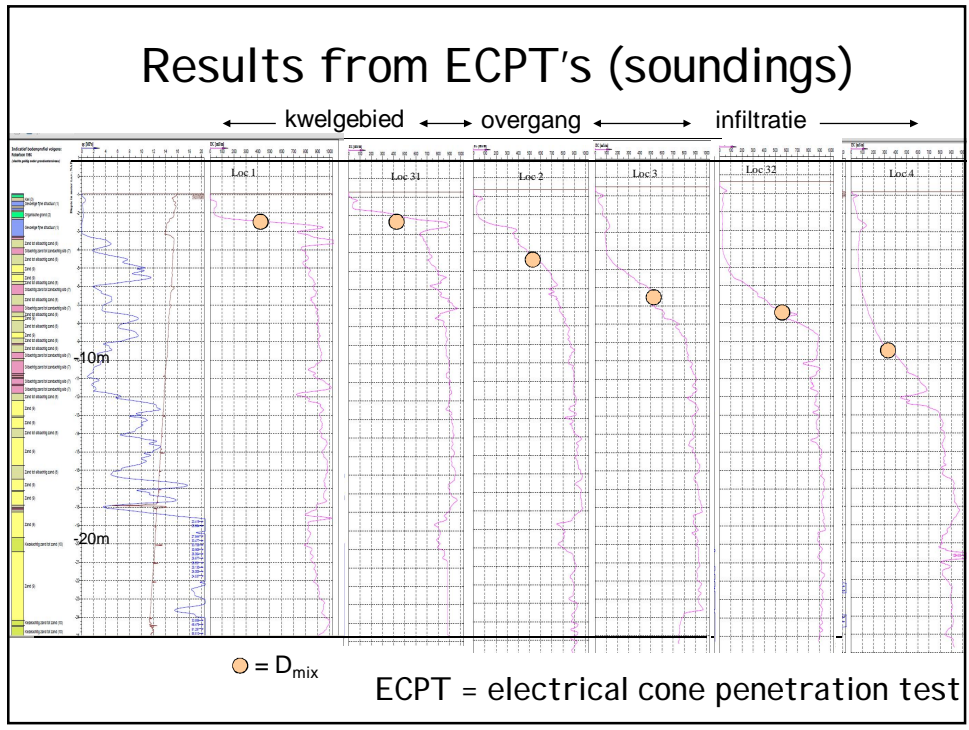
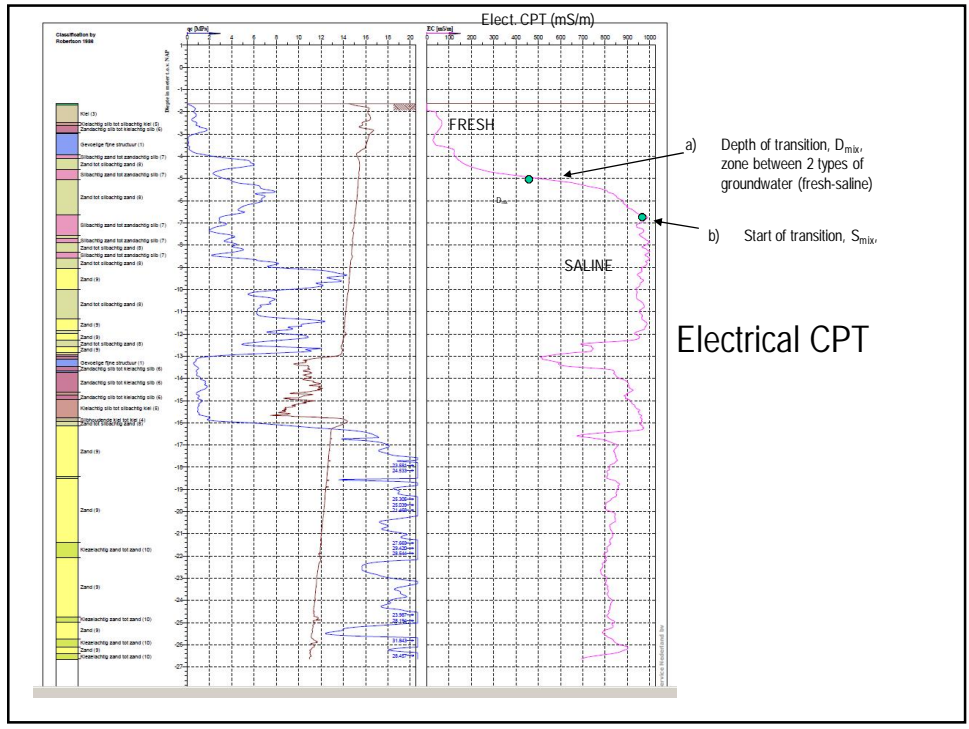


Lens characteristics



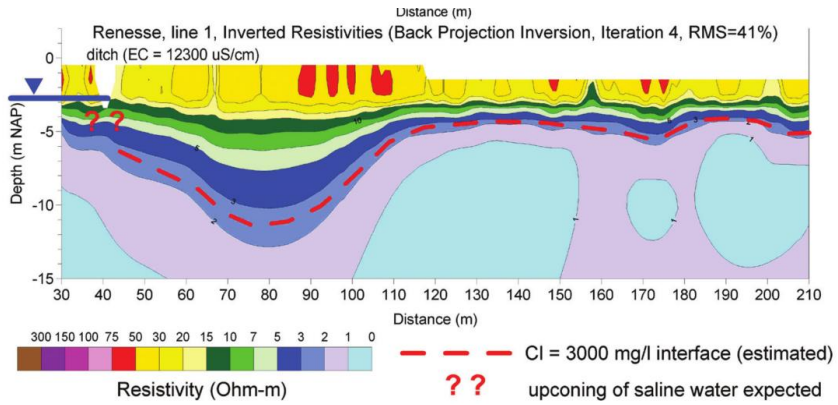
Louw, P.G.B., de Eeman, S., Siemon, B., Voortman, B.R., Gunnink, J., Baaren, E.S., van and G.H.P. Oude Essink, Shallow rainwater lenses in deltaic areas with saline seepage, *Hydrol. Earth Syst. Sci. Discuss.*, 8, 7657-7707, 2011.



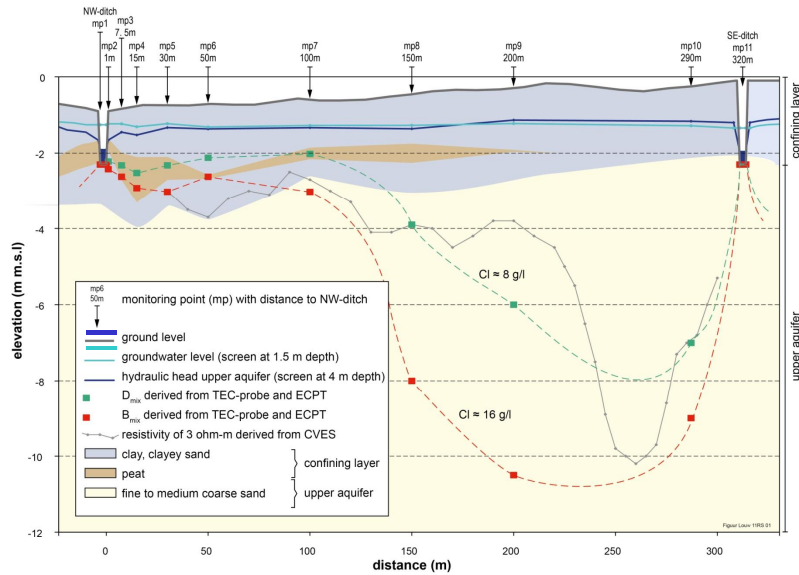


CVES

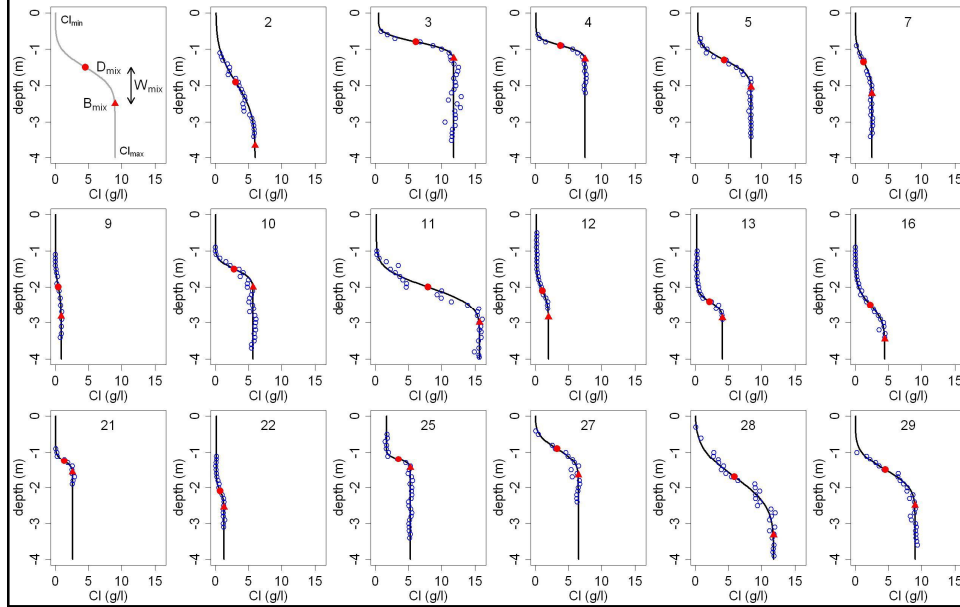
CVES: continuous vertical electrical sounding



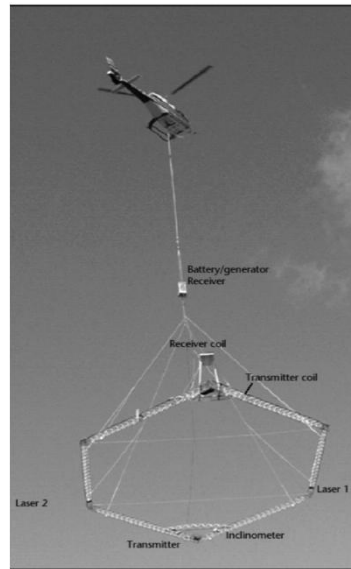
Seepage / infiltration determines thickness rainwaterlens



TEC-probe results

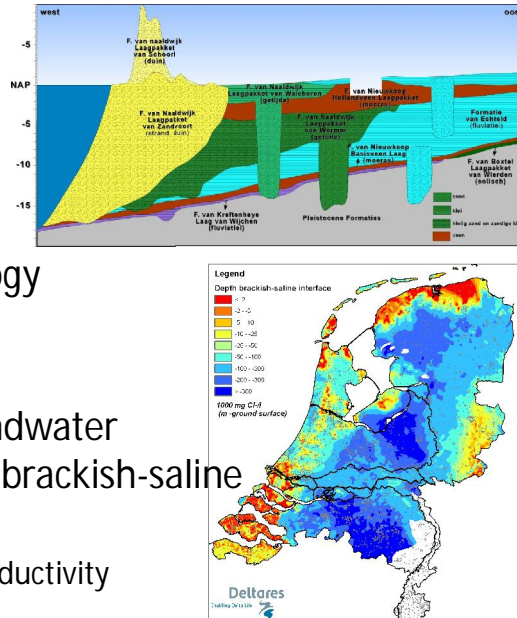
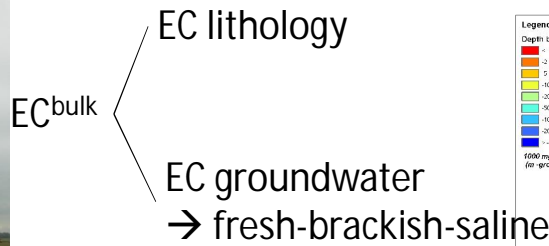


Electrical conductance measurements



10 juni 2013

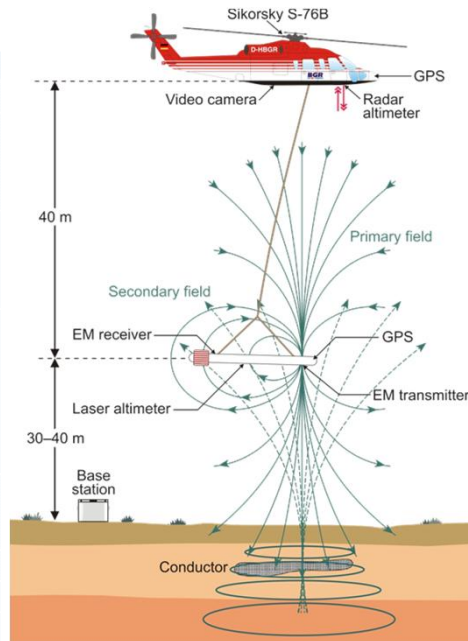
From bulk to groundwater resistivity



EC = Electrical Conductivity = conductivity

BGR helicopter-borne geophysical system

Airborne geophysical survey system	
Helicopter:	Sikorsky S-76B
Helicopter equipment:	GPS-Navigation GPS-Tracking Radar and barometric altimeters Video camera
Standard equipment:	Electromagnetic system Magnetometer Laser altimeter Gamma-ray spectrometer
Optional equipment:	Laser scanner Pulse radar Stepped frequency - Radar Gravimeter Differential GPS Photogrammetric camera Infrared camera
Base station equipment:	Magnetic total field sensor Air pressure sensor Differential GPS
Survey speed:	130 – 160 km/h
Sampling distance:	~ 4 and 40 m
Line separation	50 – 2000 m

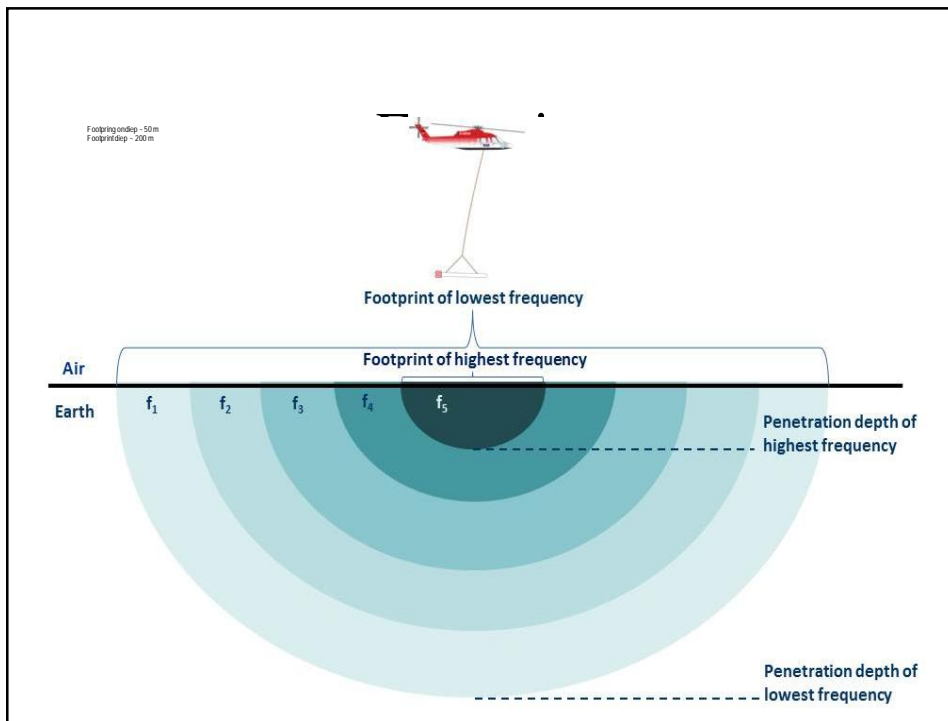
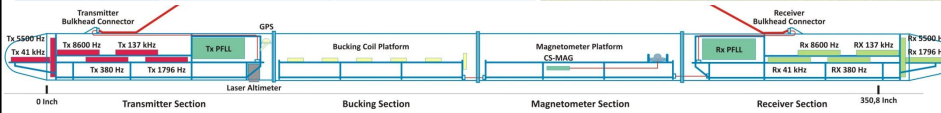


Meeting in Utrecht Feb. 25th 2014

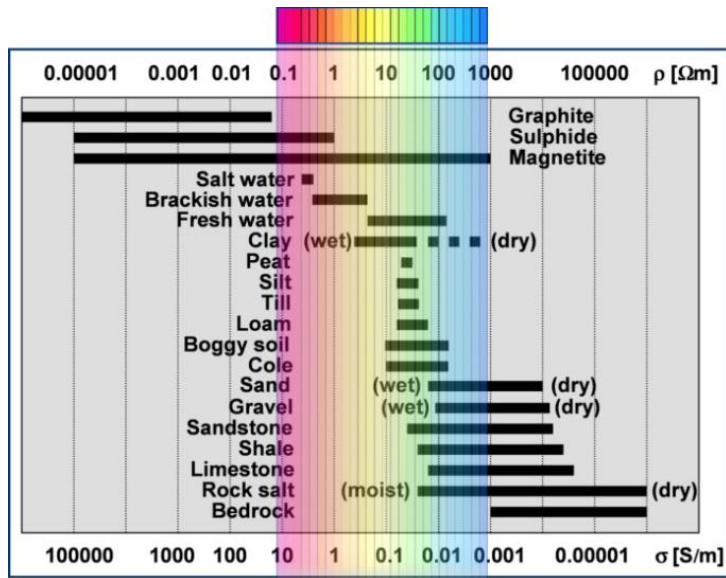
BGR helicopter-borne geophysical system

Recent six-frequency HEM system

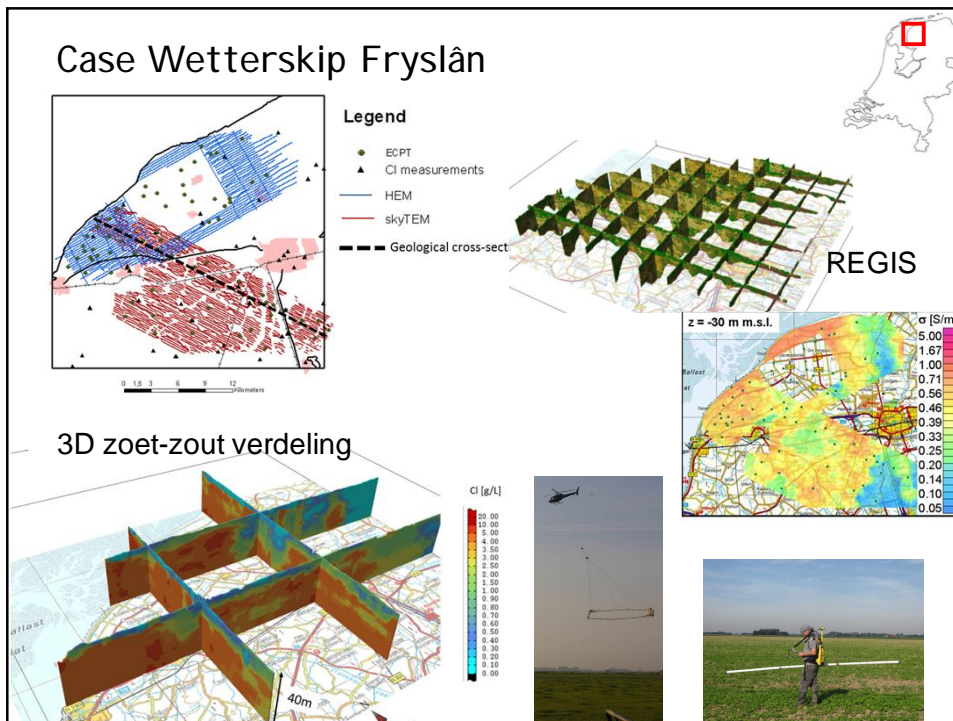
Type:	RESOLVE – Digital system Modified BKS36a DSP and BKS60 DSP systems	
Length:	~ 10 m	
Weight:	~ 400 kg incl. cable (80 kg)	
Manufacturer:	Fugro Airborne Systems, Canada	
Frequency [Hz]	Coil separation[m]	Geometry
387	7.94	horizontal coplanar
1820	7.93	horizontal coplanar
5500	9.06	vertical coaxial
8225	7.93	horizontal coplanar
41550	7.91	horizontal coplanar
133200	7.92	horizontal coplanar



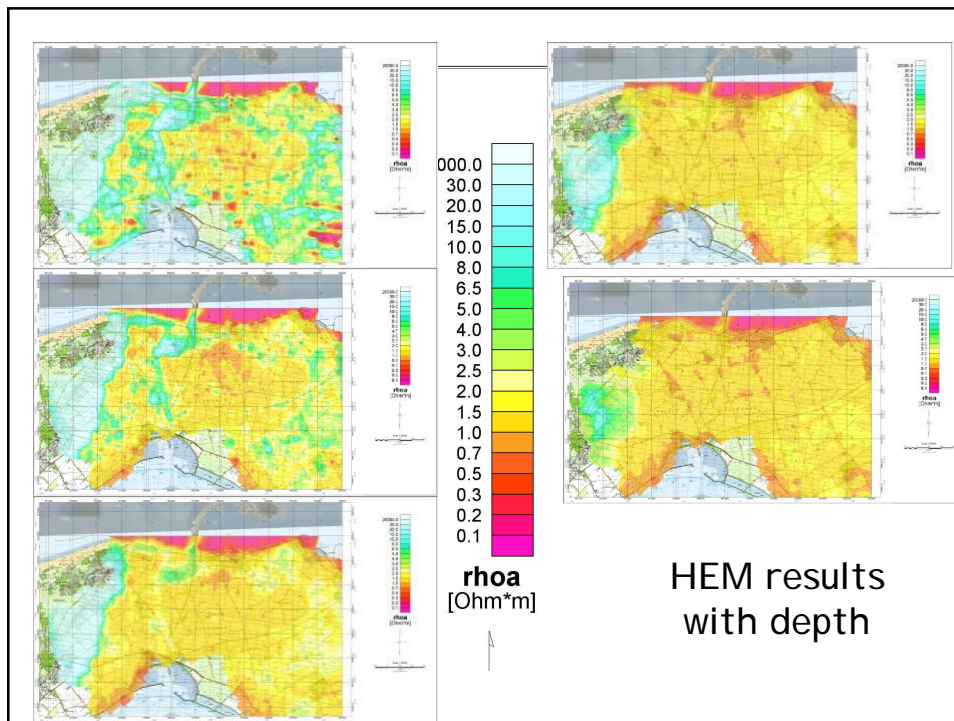
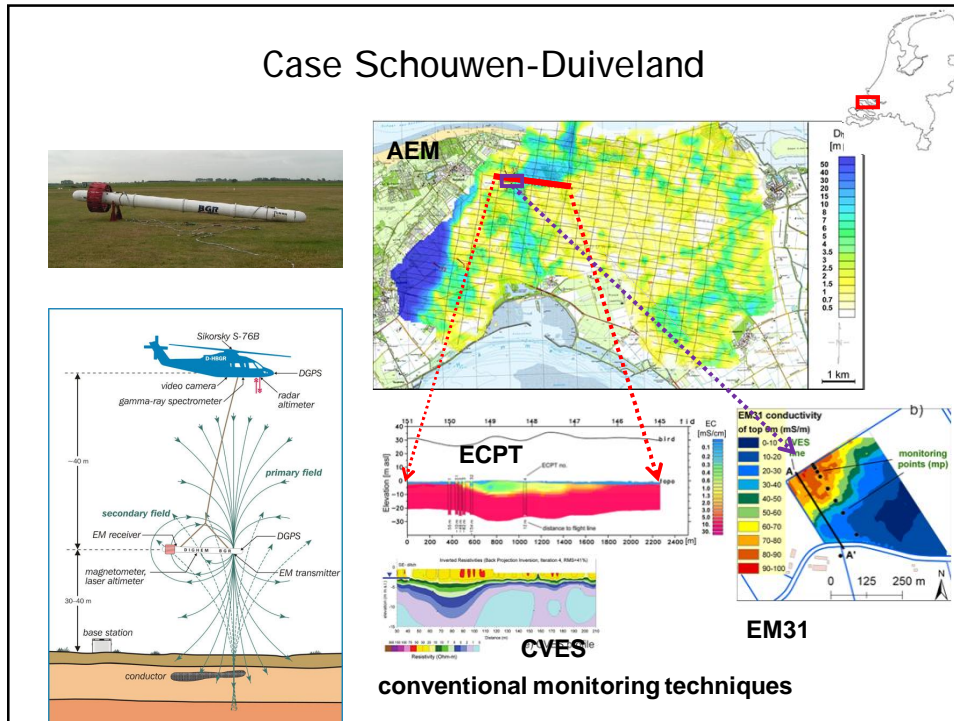
Typical resistivities / conductivities



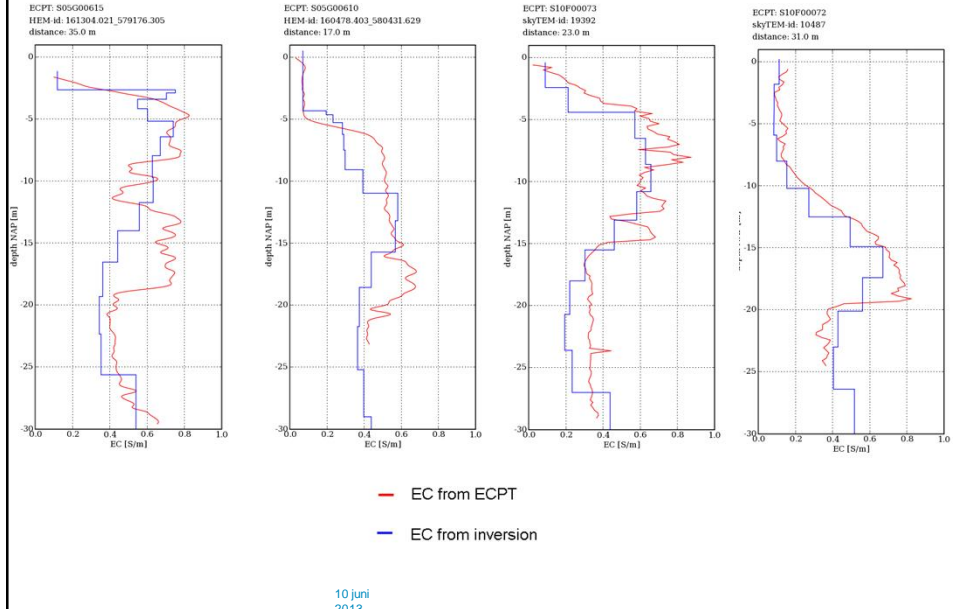
Case Wetterskip Fryslân



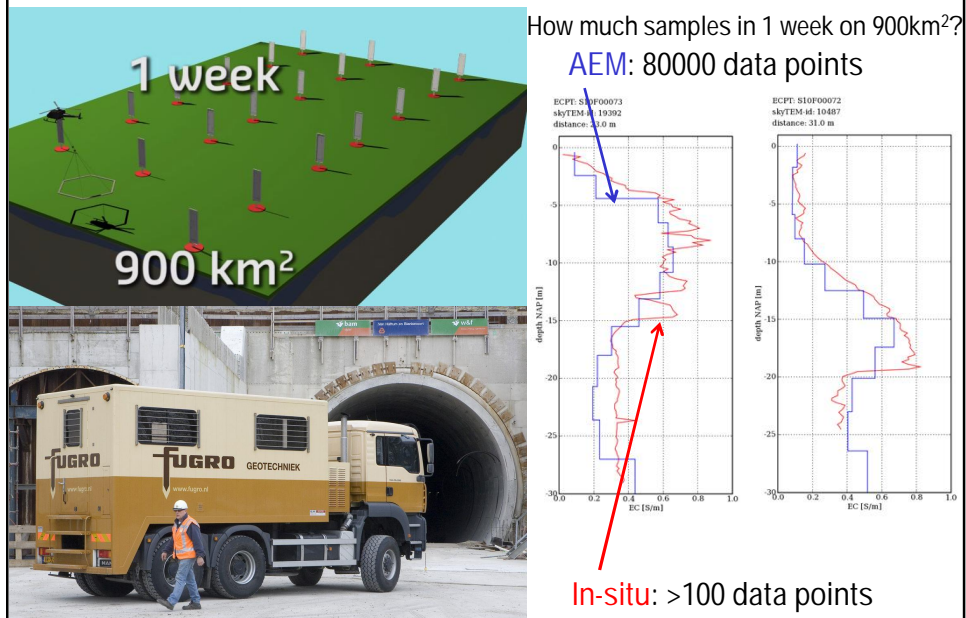
Case Schouwen-Duiveland



Compare Airborne EM with ECPT Case Wetterskip Fryslân

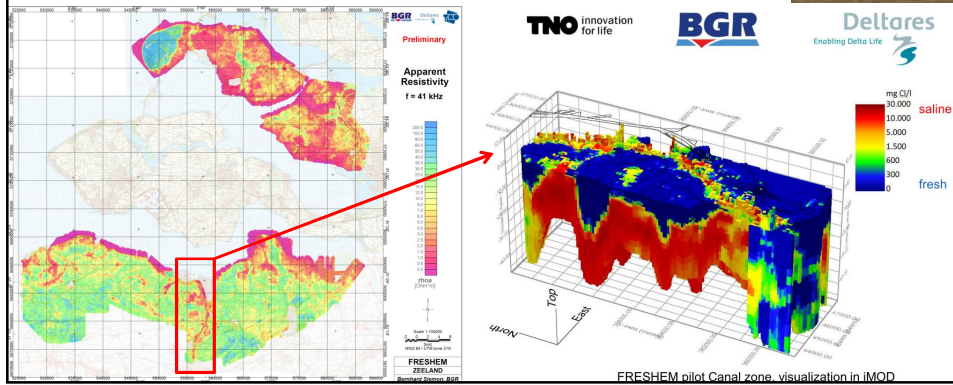


3D characterising fresh-saline groundwater

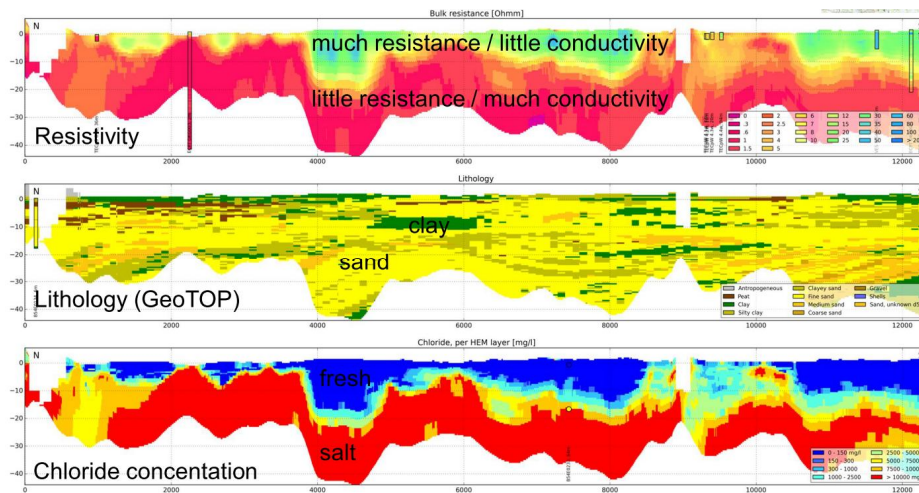


3D Characterisation of the subsoil

Airborne EM surveys:
 much cheaper, faster, 3D,
 and as equal accurate as
 conventional geophysical methods

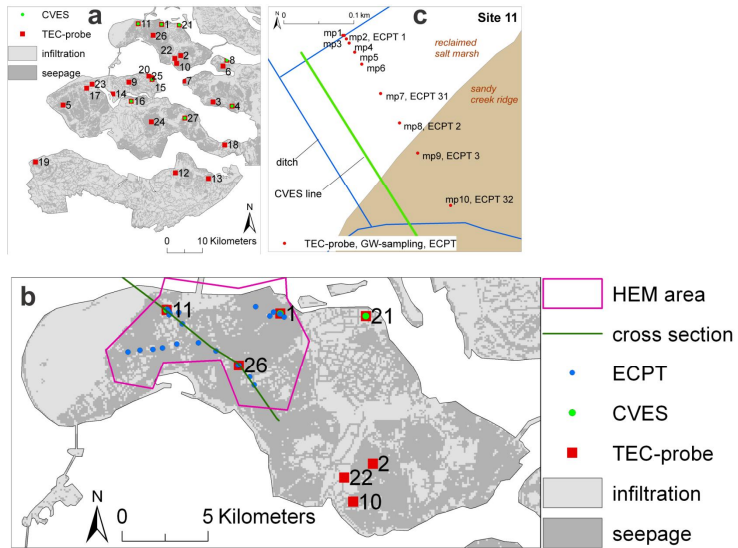


Example NL, Zeeland, project FRESHEM



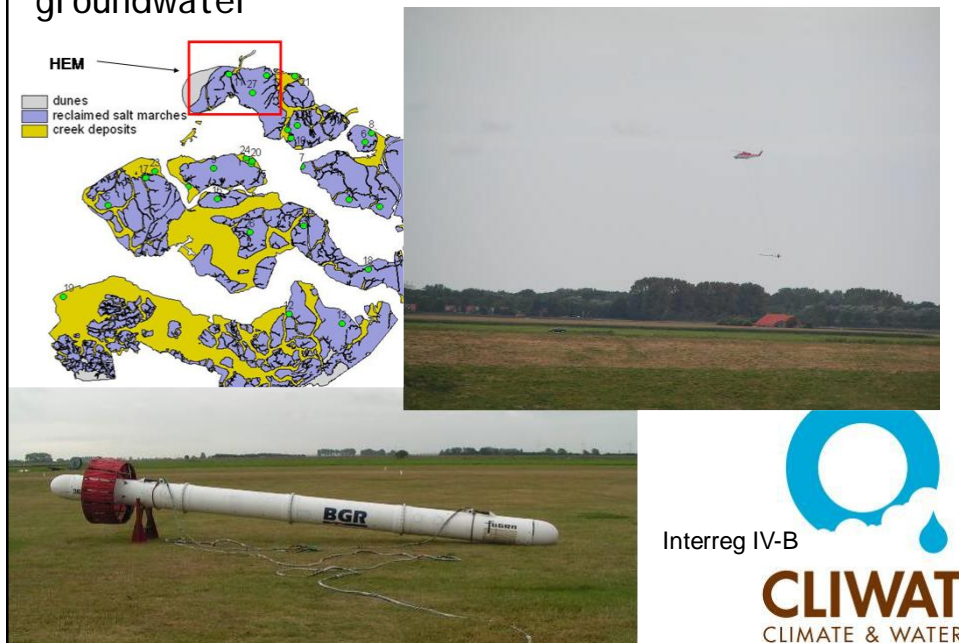
20160524 Ara Sul

Combining monitoring techniques

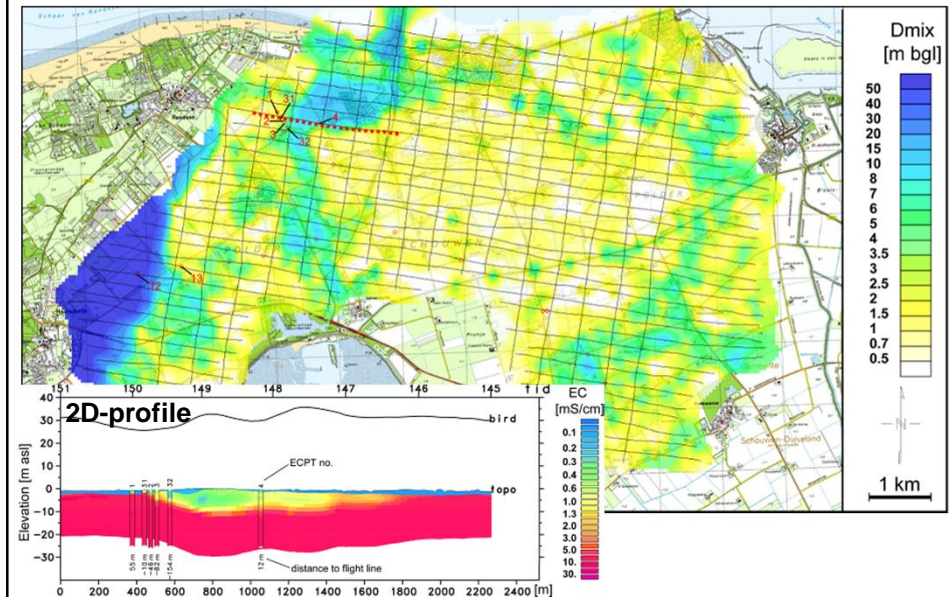


10 juni 2013

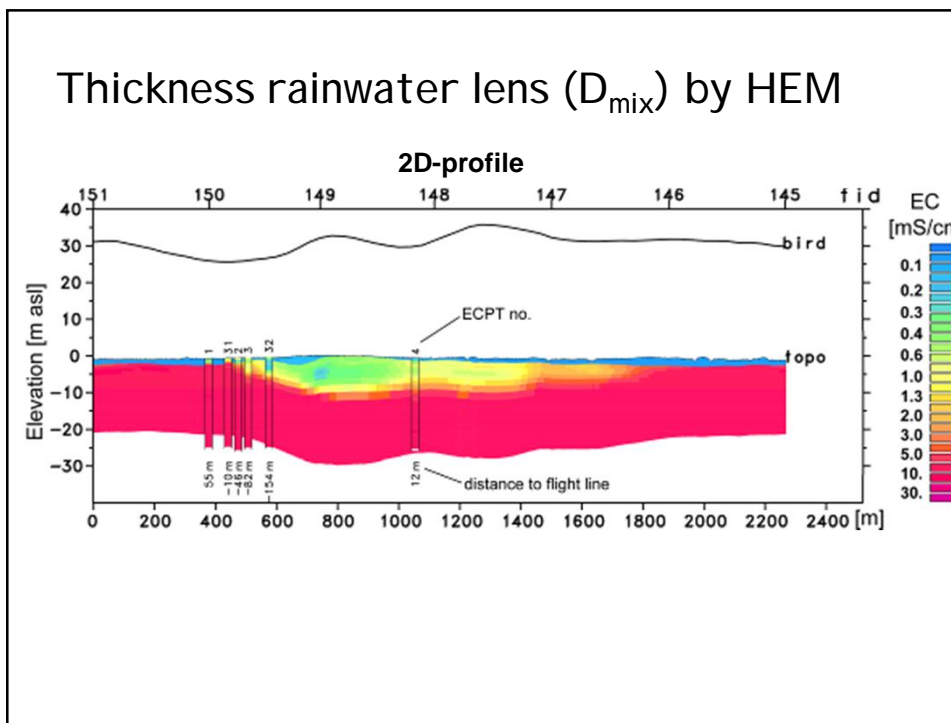
Helicopter-EM data for mapping fresh-saline groundwater



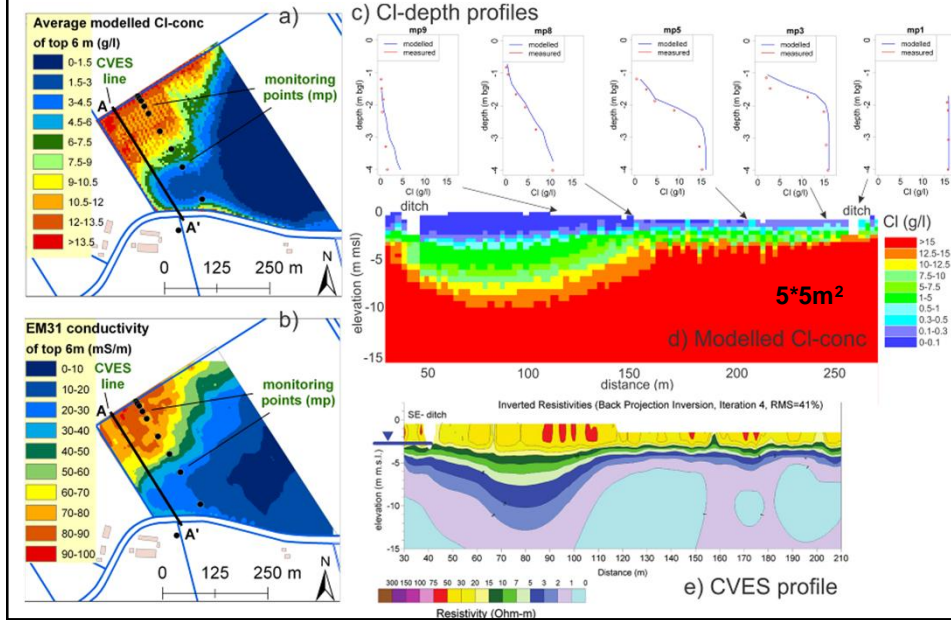
Thickness rainwater lens (D_{mix}) by HEM



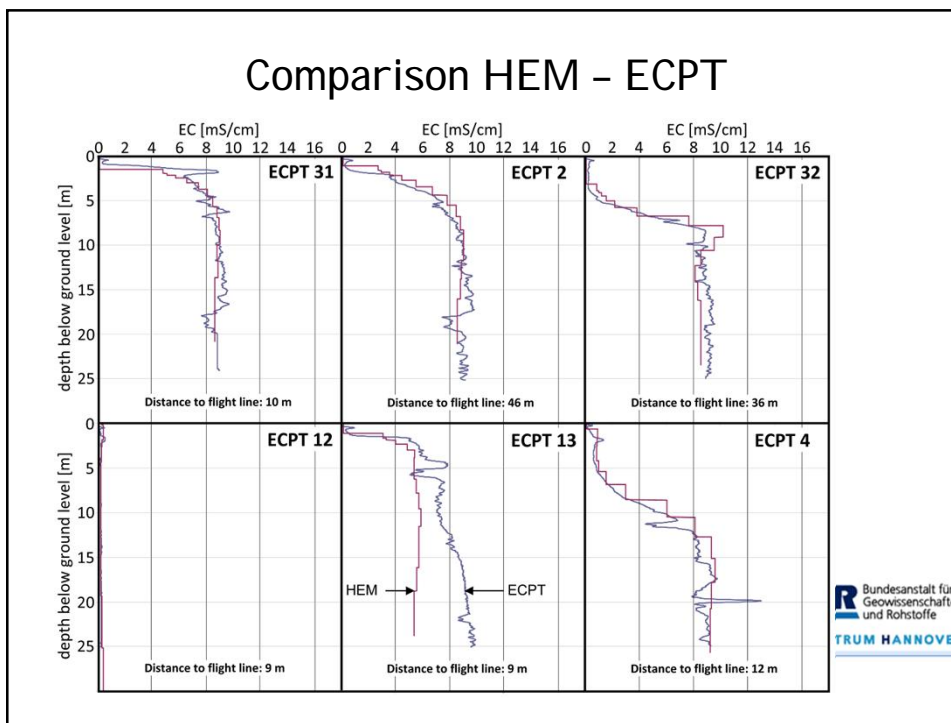
Thickness rainwater lens (D_{mix}) by HEM



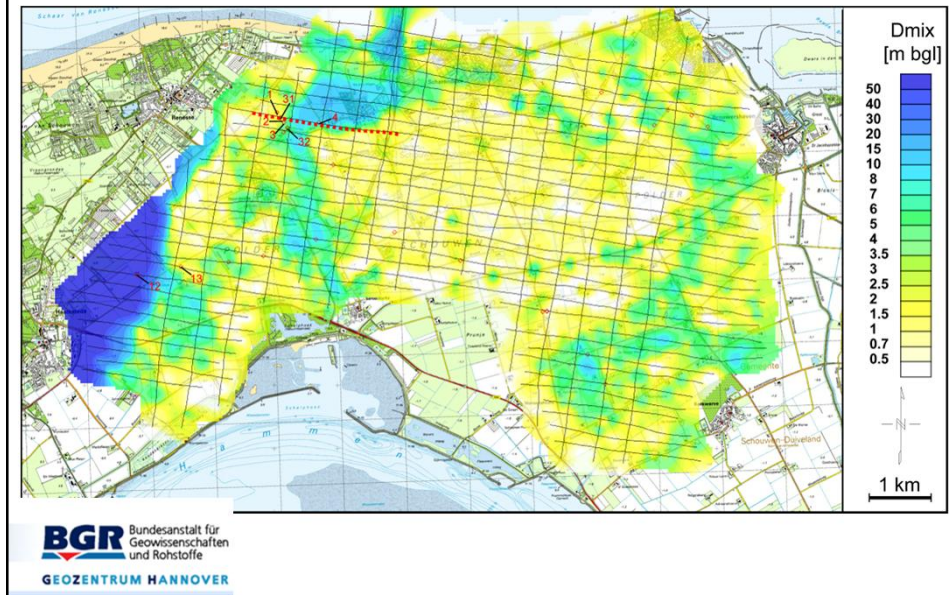
Comparison monitoring data with model results



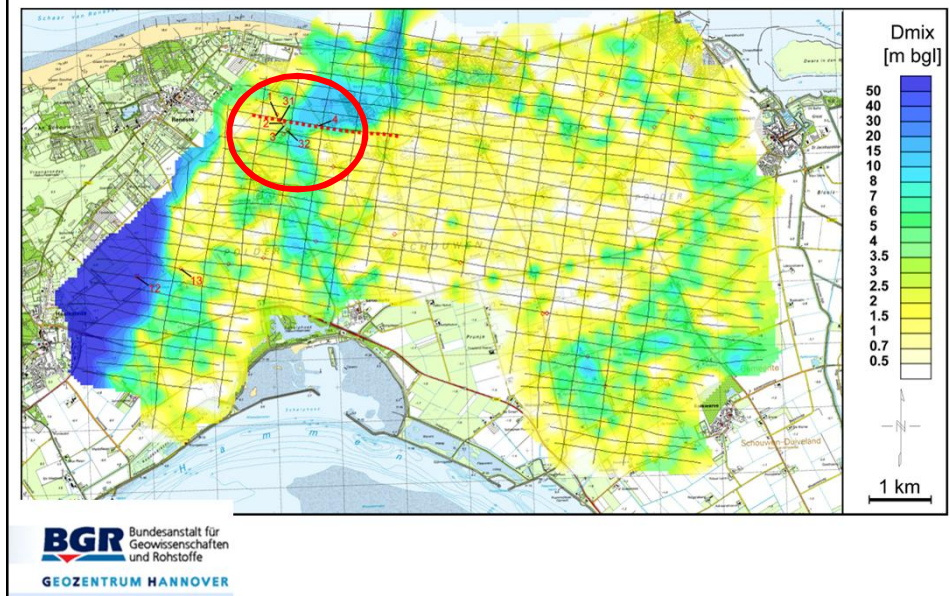
Comparison HEM – ECPT



Rainwater lens thickness (D_{mix} = average position mixing zone)
mapped with HEM



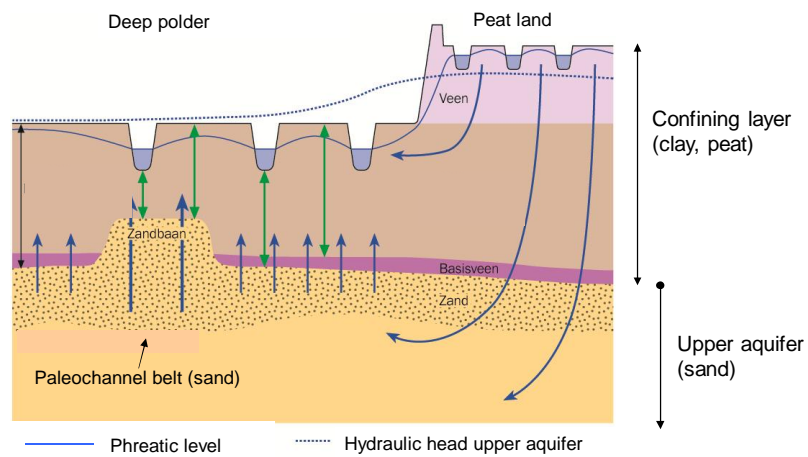
Rainwater lens thickness (D_{mix} = average position mixing zone)
mapped with HEM

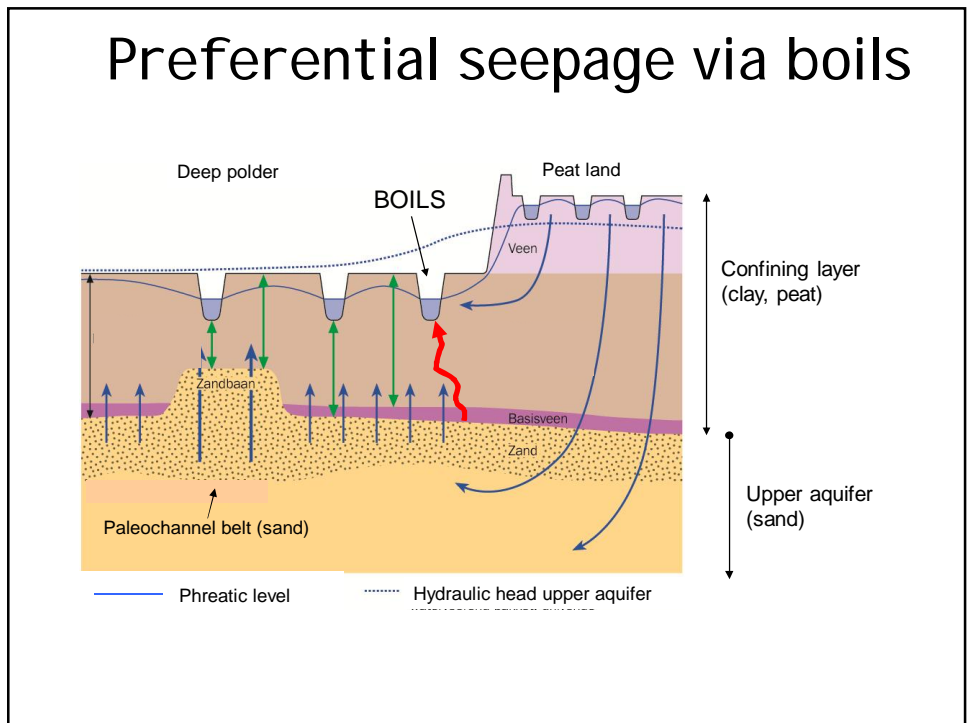
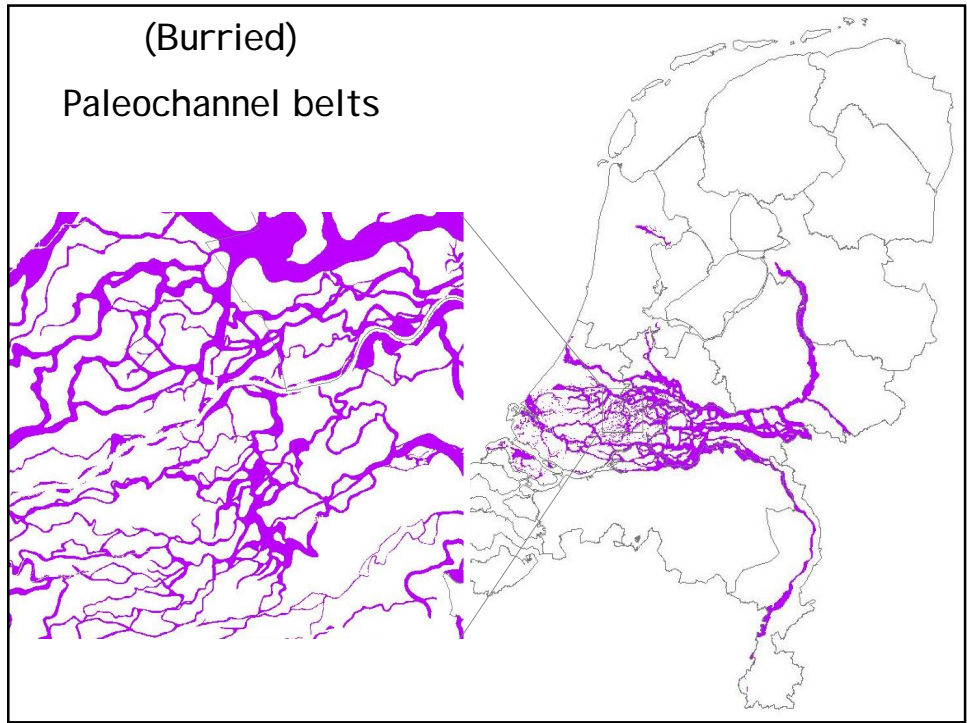


Salty boils

Louw, P.G.B., de, Oude Essink, G.H.P., Stuyfzand, P.J., Zee, van der, S.E.A.T.M., 2010, Upward groundwater flow in boils as the dominant mechanism of salinization in deep polders, The Netherlands, J. Hydrol. 394, 494-506.

Upward groundwater seepage in a deep polder and paleochannel belts as preferential flow paths





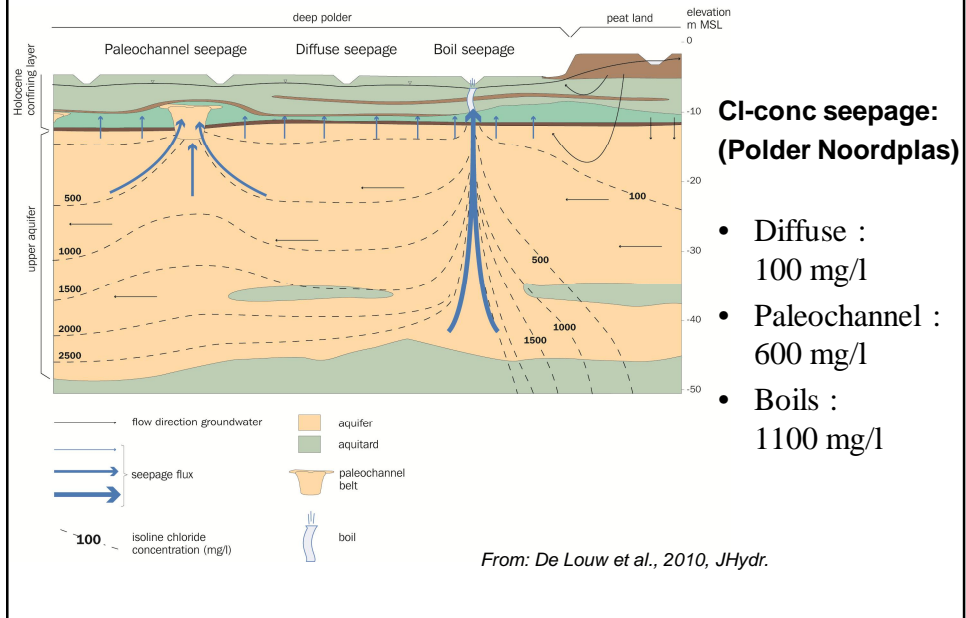
Preferential saline seepage via boils



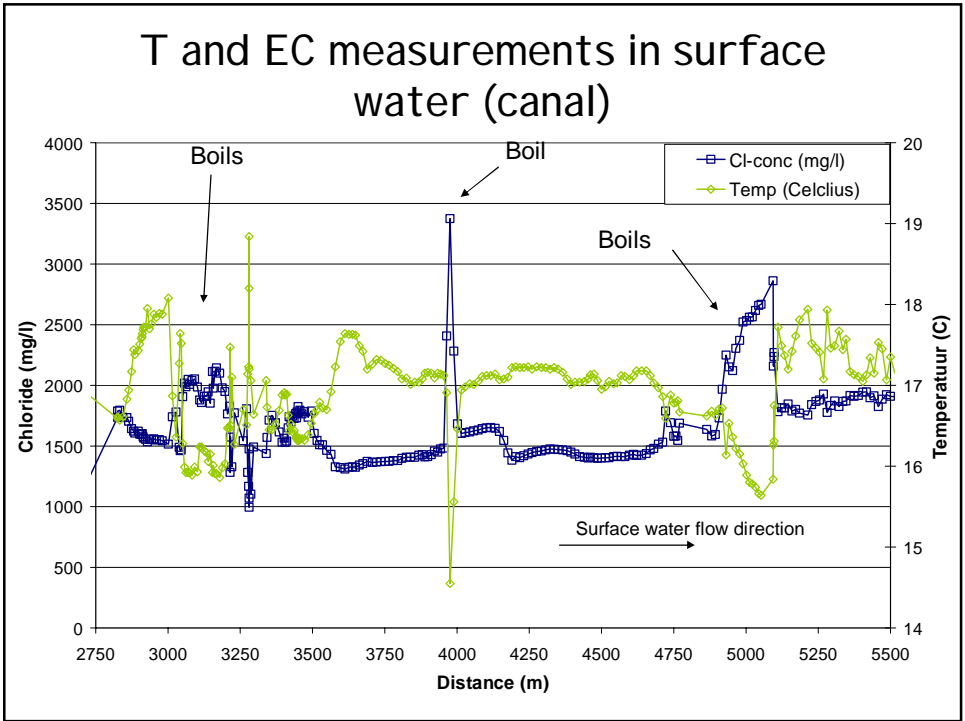
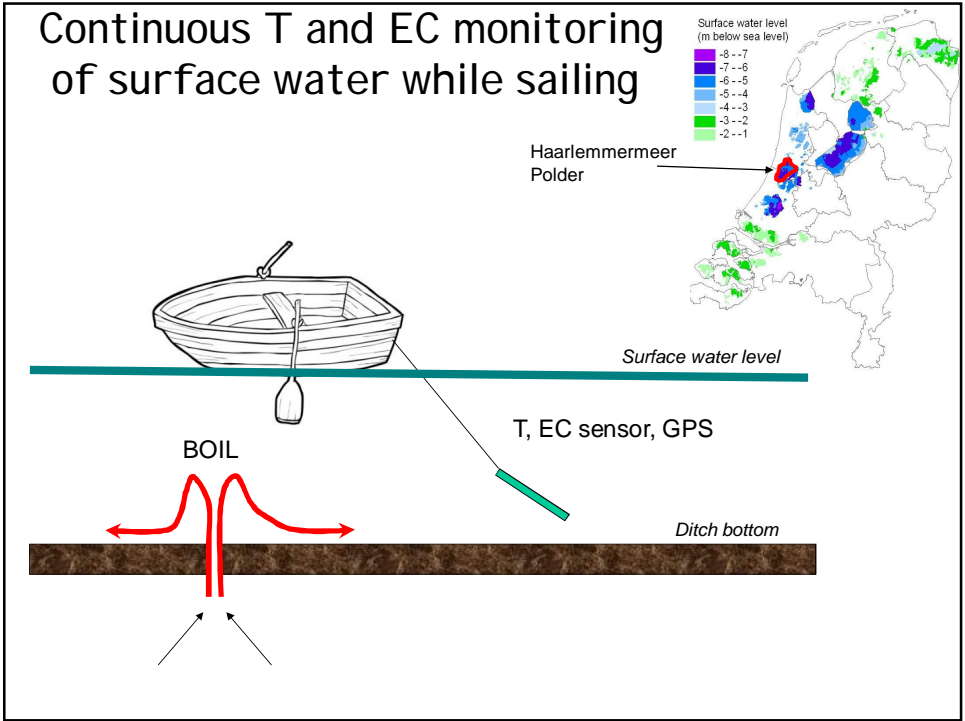
Preferential saline seepage via boils

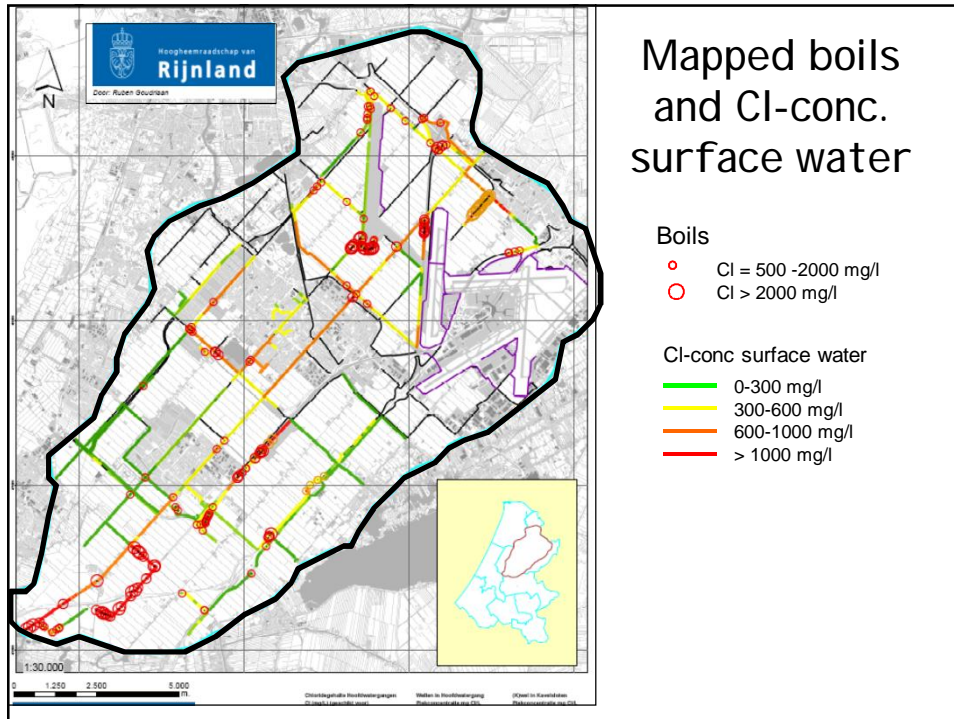


Three types of upward groundwater seepage









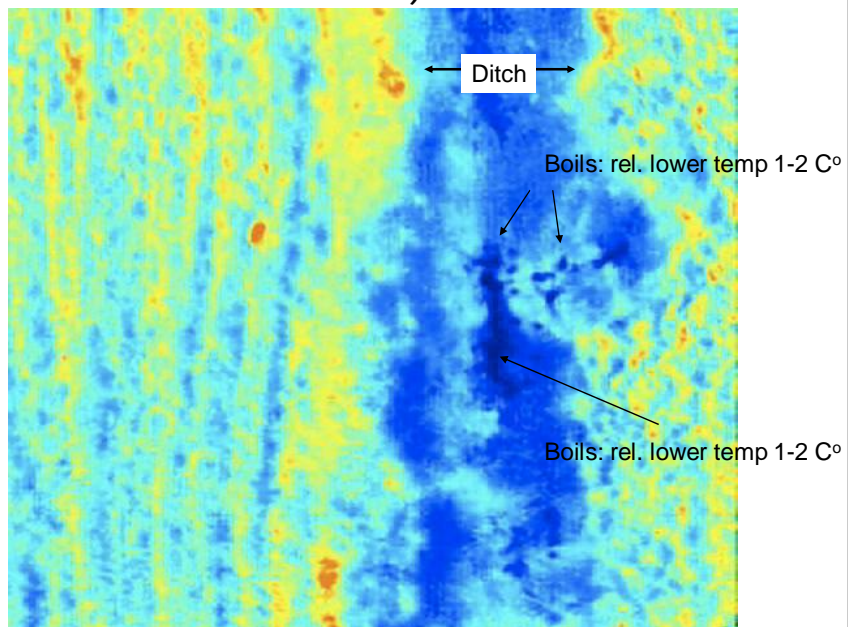
LARS technology (TNO Industry): Thermal Infra-red

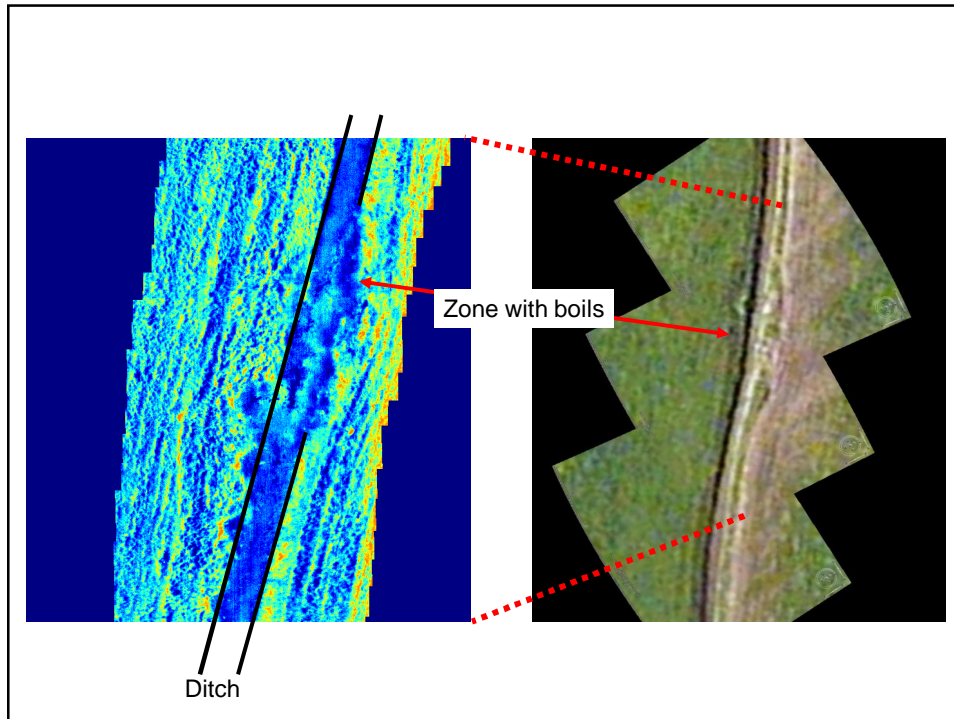
- Altitude: 0-150 m
- Temp-detection using Thermal Infra Red sensors (only surface !)

The diagram shows a cross-section of a boiling pot on a surface. A red arrow labeled 'BOIL' points upwards from the pot, indicating heat. A black arrow labeled 'V' points upwards from the surface, representing the thermal infrared radiation being detected by the drone's sensor.



Thermal infra-red results (blue is cold, red is warm)

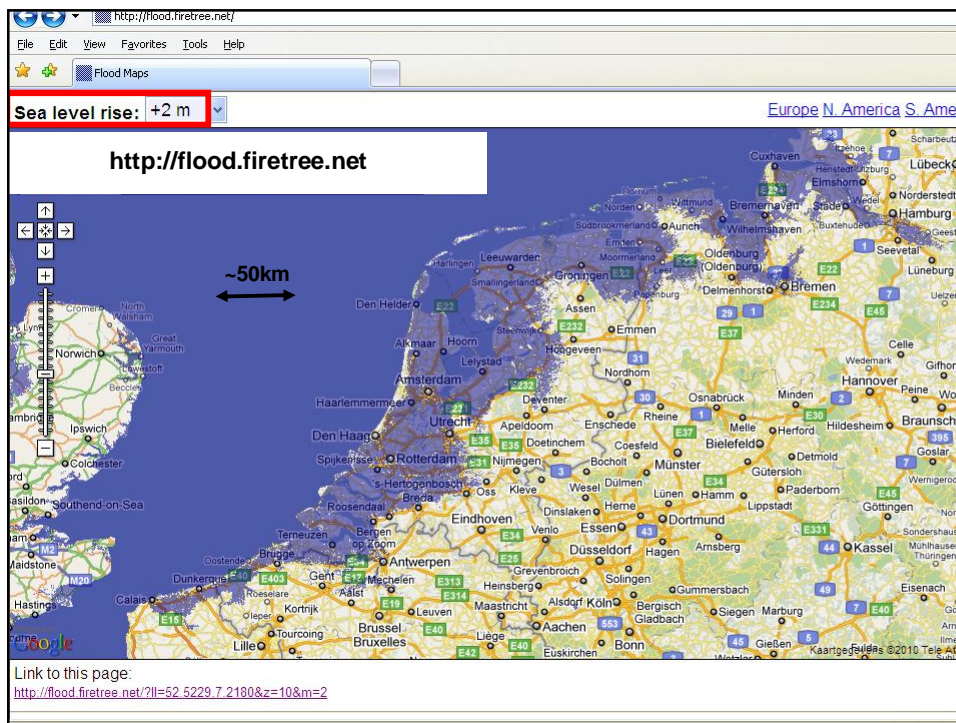




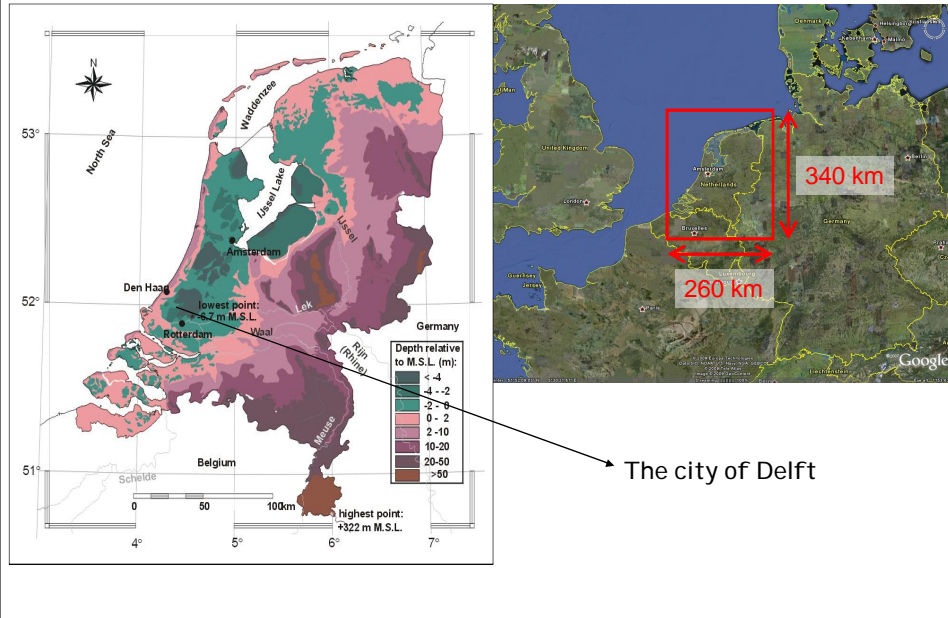
To get an idea about the possible future effects of sea level rise and climate change in your delta ...

evaluate of the past water management in the Dutch delta

Salt water intrusion in the Netherlands



The 'low-lying' lands: Netherlands



Case study: The Netherlands

The Dutch coastal zone is already threatened by sea level rise and land subsidence for many centuries

Intensive water management system

Coping with salt water intrusion problems since 1950's



The 'low-lying' lands: Netherlands

The facts:

- a deltaic area with 3 rivers: Meuse, Scheldt & Rhine
- 25% of land surface is lying below mean sea level
- 65 % would be flooded regularly if there were no dunes and dikes
- 8 million people would be endangered



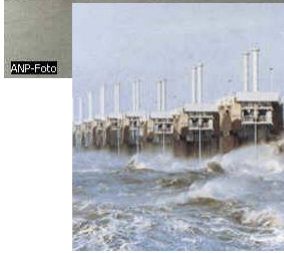
The Great Flooding in february 1953

Combination of high tide and heavy storm:

- 1853 casualties
- 2000 km² flooded

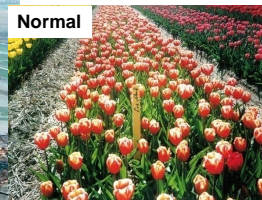


Infrastructure to protect our low-lying land from flooding



River flooding in 1995

Combination of heavy rains upstream the catchment
& short retention time



Dike collapse 2003

Combination of peat dike instability and very dry summer

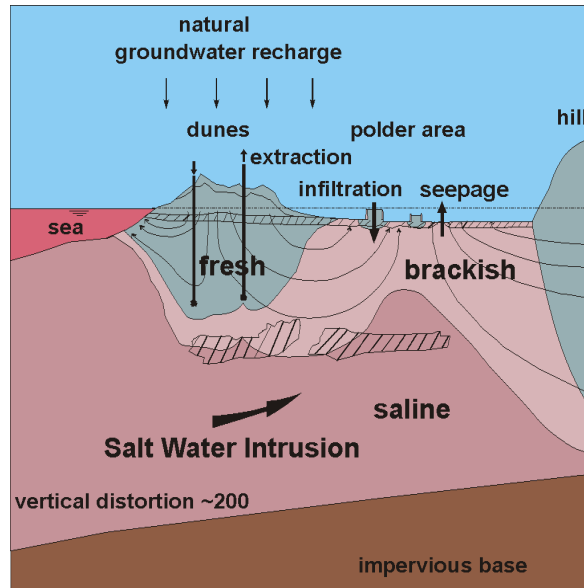


Estimated water management costs 'to keep our feet dry'

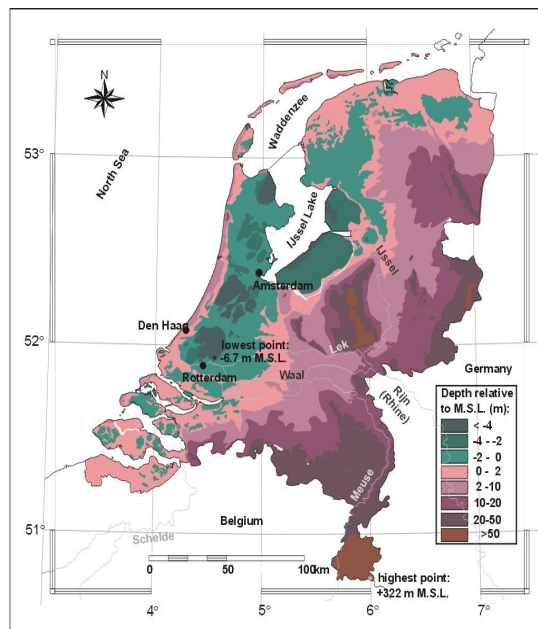
Costs up till 2050 in billion euros:

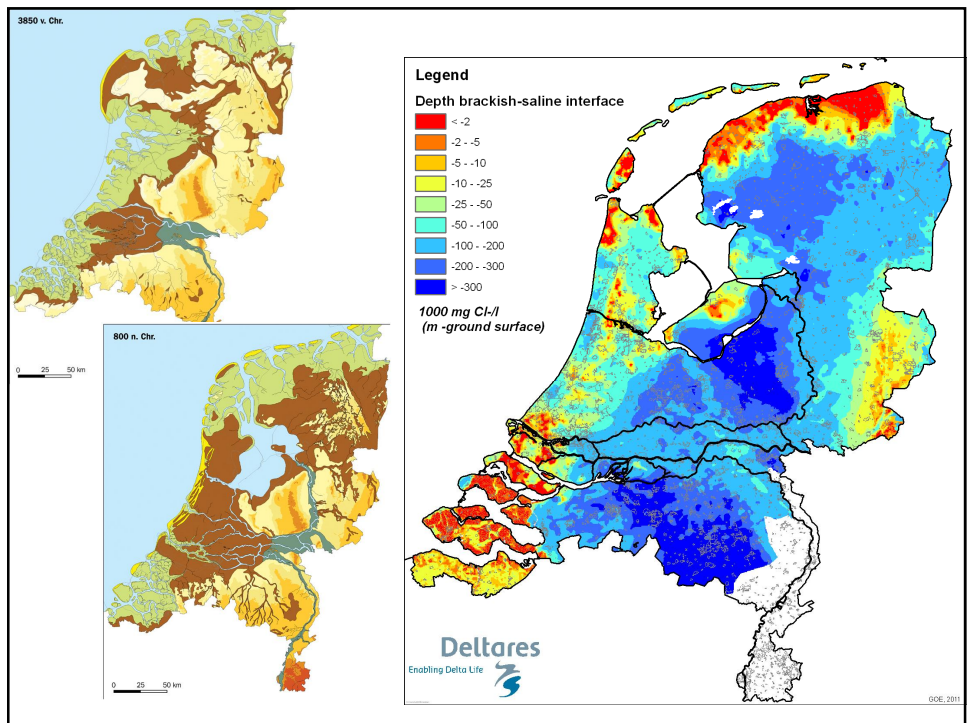
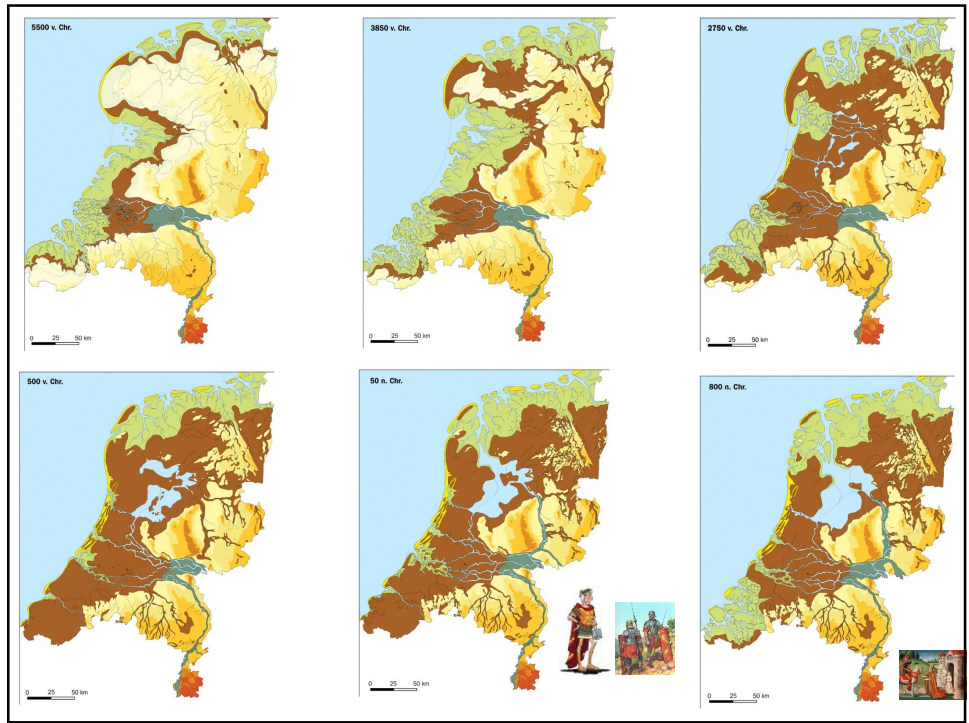
ivers: upper part	5.7
ivers: lower part	5.6
low-lands	1.7
coastal zone	8.0
infrastructure	3.5
purchase of ground	2.0
	-----+
	26.5 billion euros

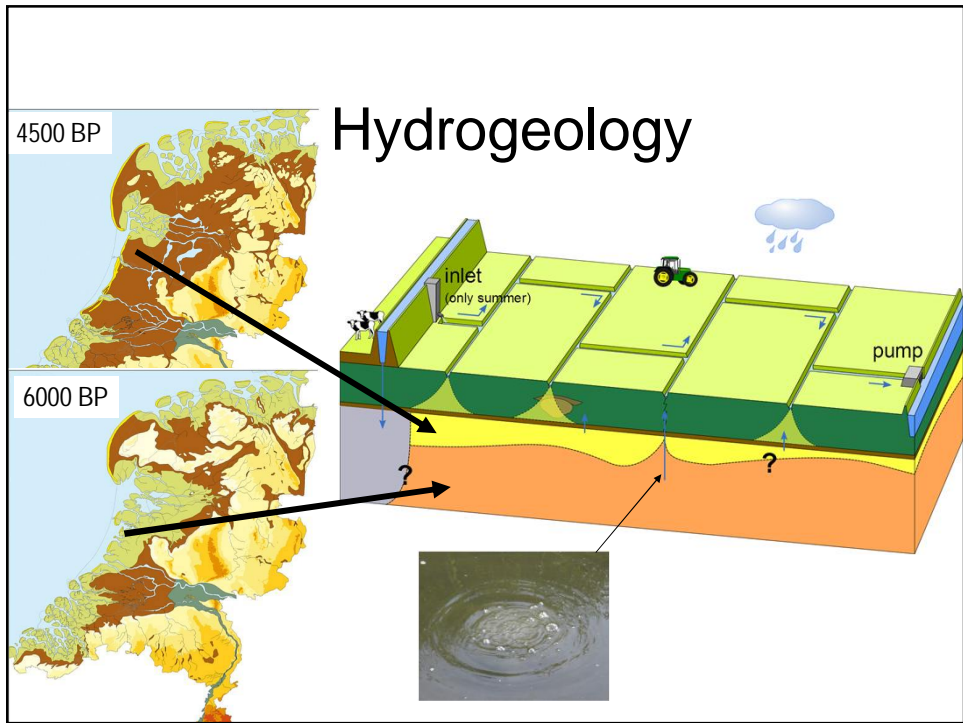
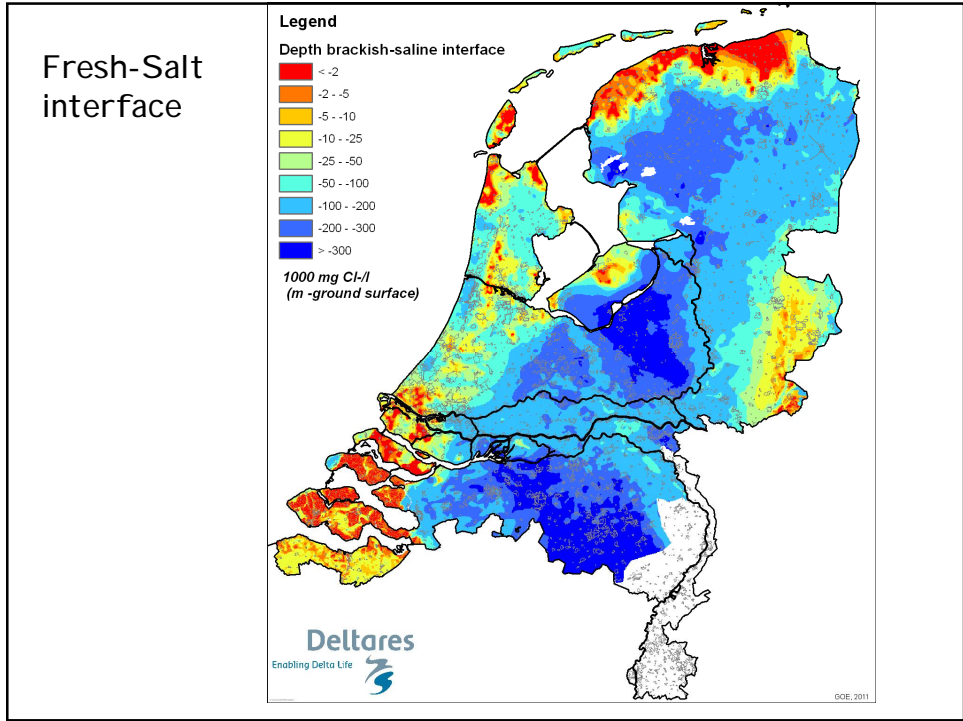
Salt water intrusion in the Netherlands



Present ground surface in the Netherlands







Salinisation of the Dutch subsurface

Physical transport processes:

- advective: e.g. trans- and regressions
- dispersive: mixing with marine deposits
- diffusive: e.g. IJsselmeer lake
- chemical: solution, precipitation, ion-exchange

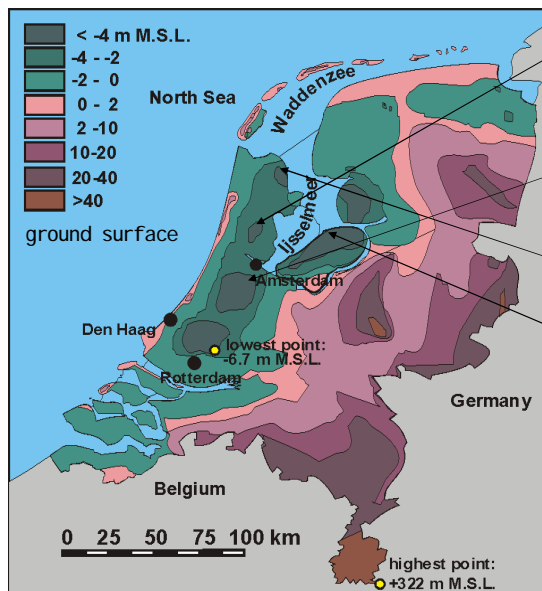
Anthropogenic causes:

- land subsidence
- polder level lowering
- groundwater extractions

Future developments (climate change):

- sea level rise
- changes in recharge

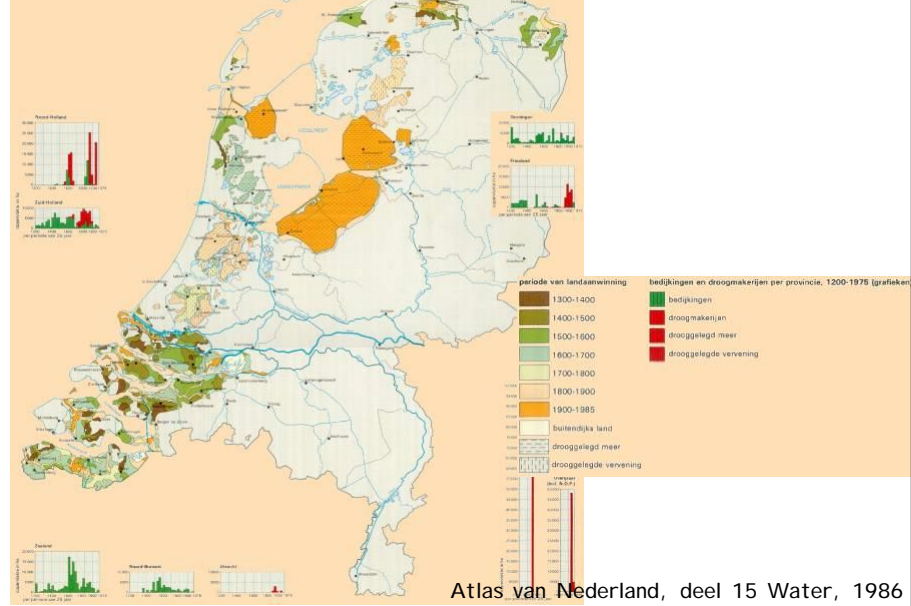
Abrupt land subsidence



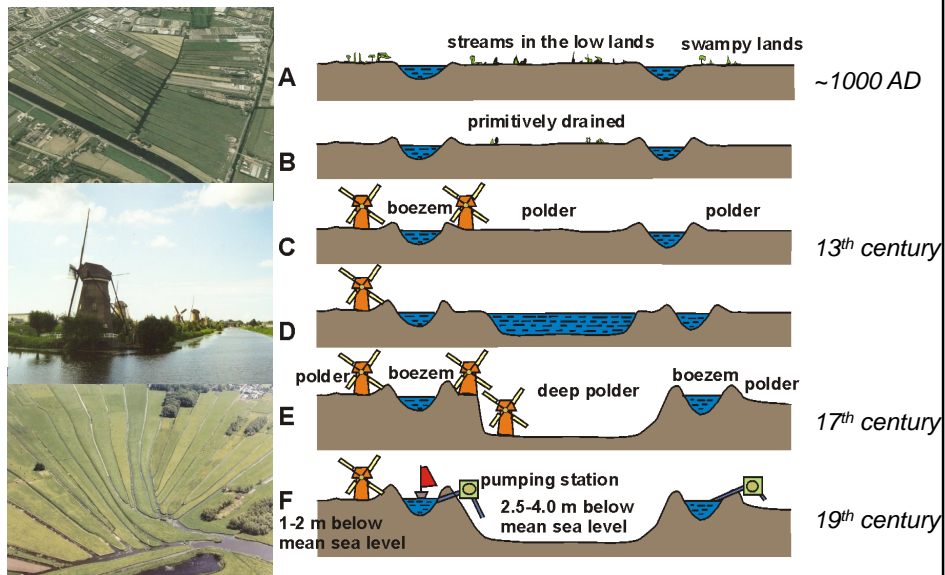
position polders:

- Beemster 1608-1612
- Wormer 1625-1626
- Schermer 1633-1635
- Purmer 1618-1622
- Haarlemmermeer polder 1850-1852
- Wieringermeer polder ~1930
- Flevo polders 1950-60s

Land reclamation since 1300



Development of the Dutch 'Polder' Landscape

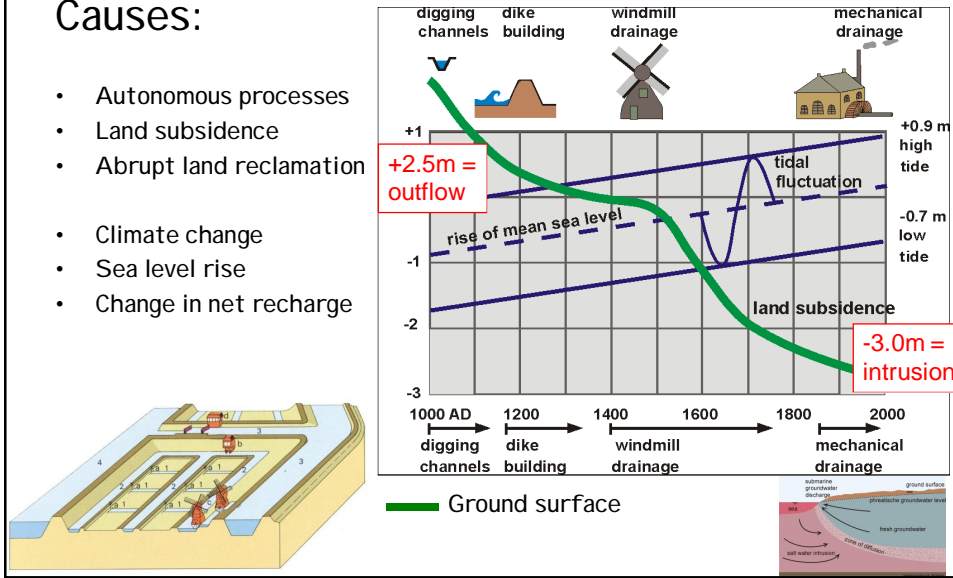


From fresh water outflow to salt water inflow

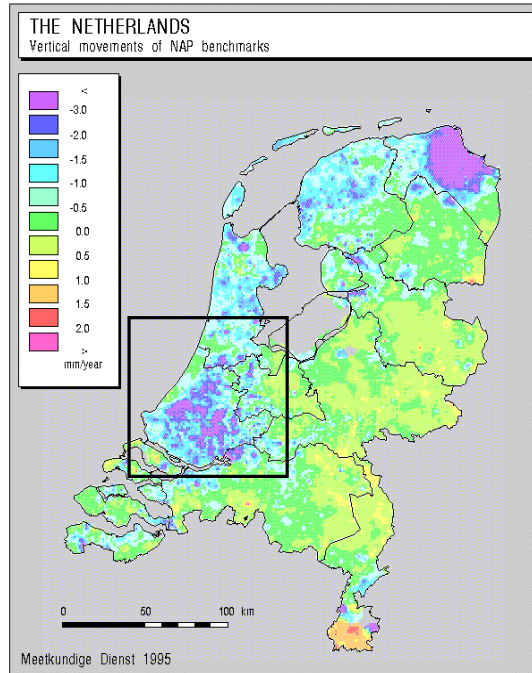
Causes:

- Autonomous processes
- Land subsidence
- Abrupt land reclamation
- Climate change
- Sea level rise
- Change in net recharge

Historical subsidence of the ground surface in Holland



Land subsidence related to M.S.L.



Land subsidence



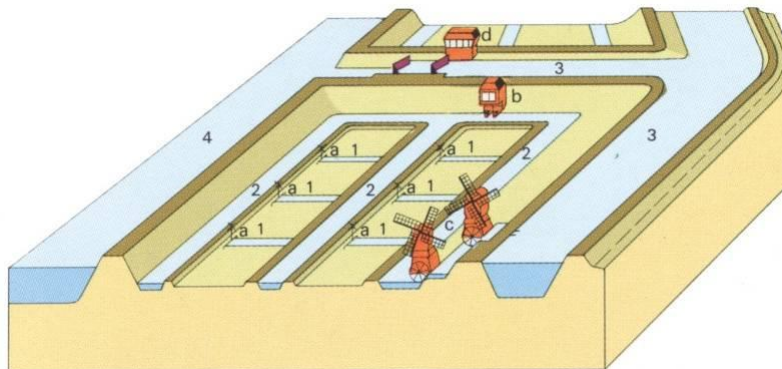
up to 1 m per century



The polder system

A land below the sea with an excess of water needs..

a sophisticated drainage system



The polder system

Many agricultural plots with different water levels throughout the season



The polder system



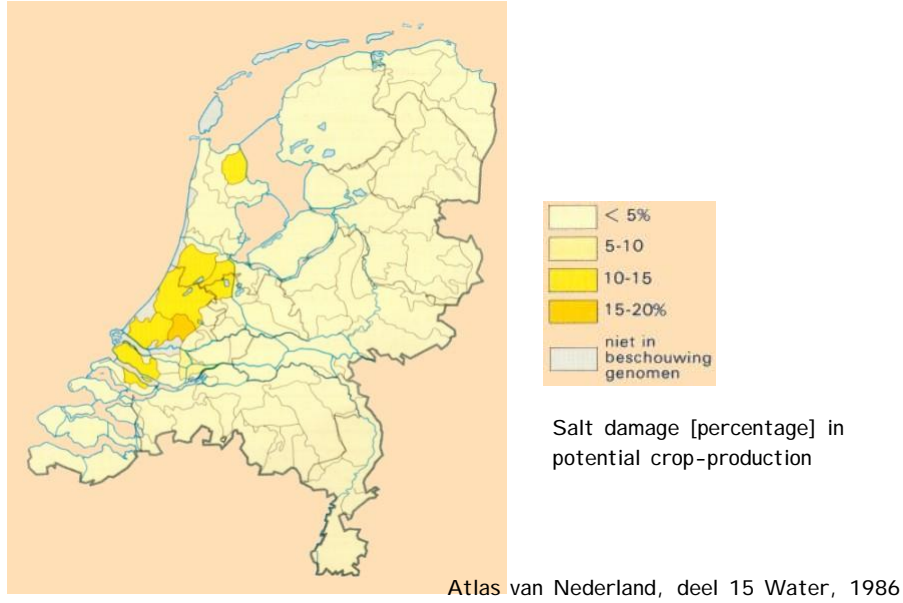
The polder system



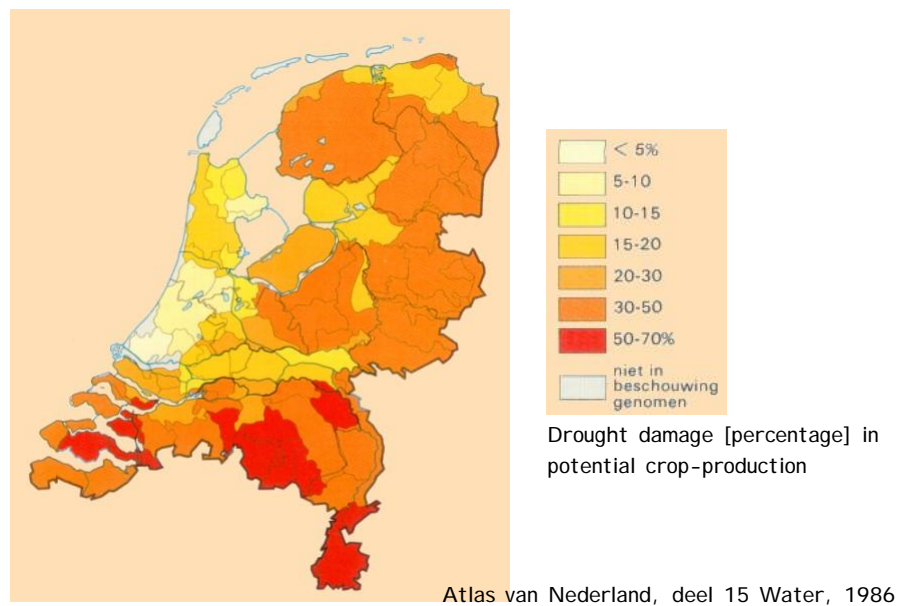
Bulb farms at the landside of the sand dunes



Salt damage in 1976 (very dry year)



Drought damage in 1976 (very dry year)



'Wetting' damage

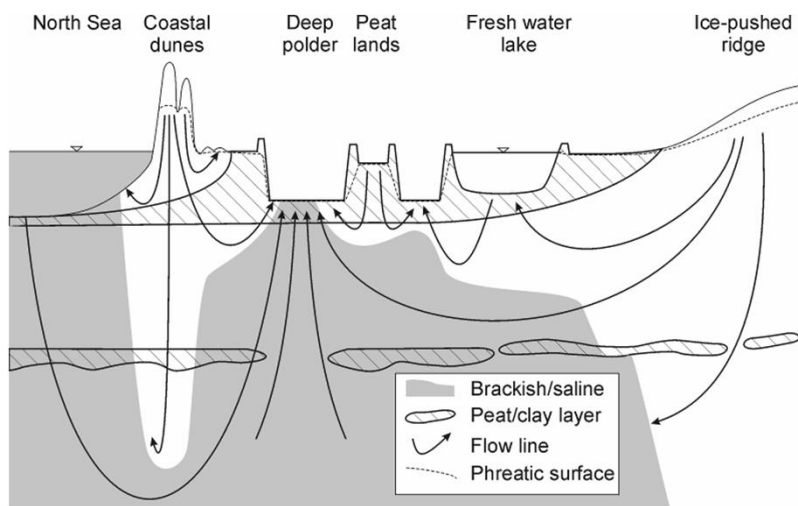


Normal situation



Crop damage due to a reduction in groundwater extraction in the dune area

Now focus on groundwater...



Threats to water management due to climate change:

Short term threats:

- flooding
- dike collapse
- drought

asks for operational water management

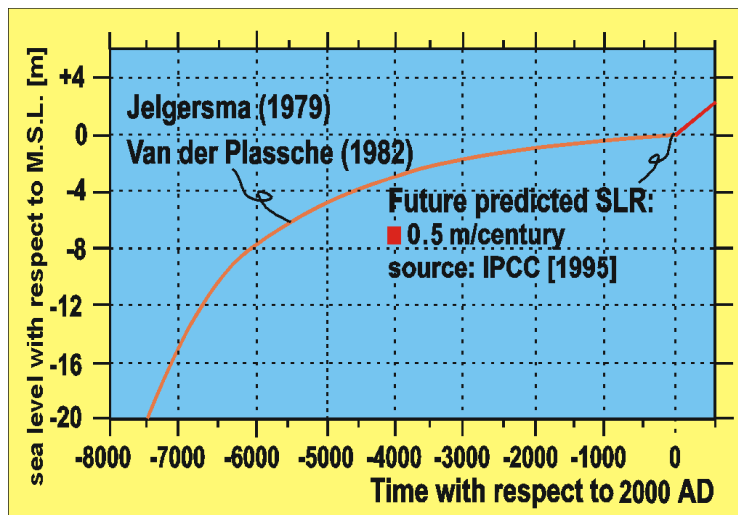
Long term threats:

- salt water intrusion
- land subsidence
- smaller fresh groundwater resources

asks for strategic water management

Dutch setting

Past and future sea level rise in the Netherlands



Numerical variable density models at Deltares

Characteristics:

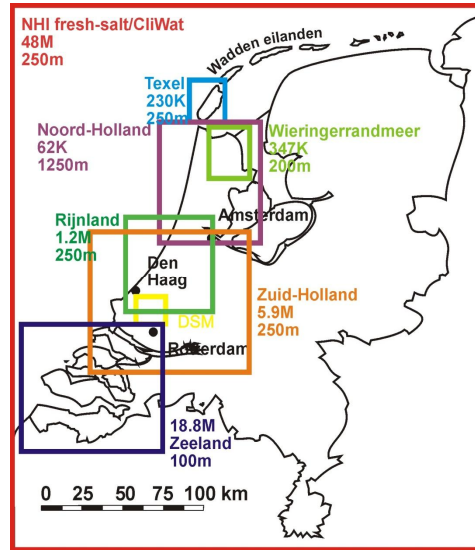
- variable-density groundwater
- fresh, brackish and saline
- 3D, non-steady
- coupled solute transport

Code (MODFLOW family):

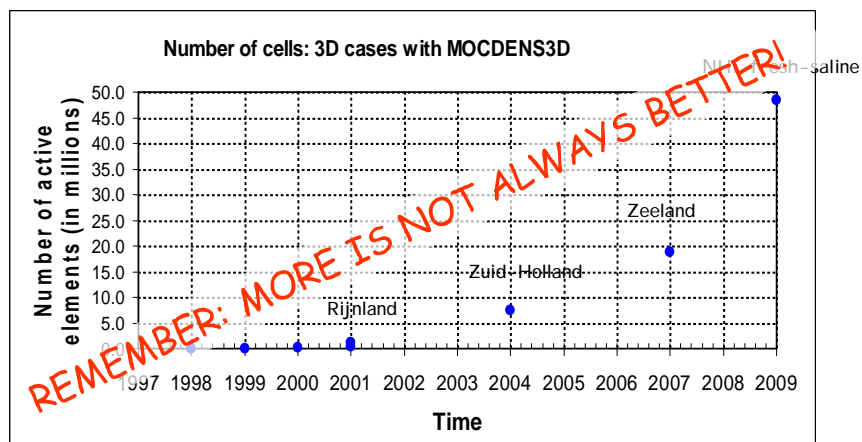
MOCDENS3D
SEAWAT

Assessing effects:

- autonomous salinisation
- sea level rise
- changing recharge pattern
- land subsidence
- changing extraction rates
- adaption measures

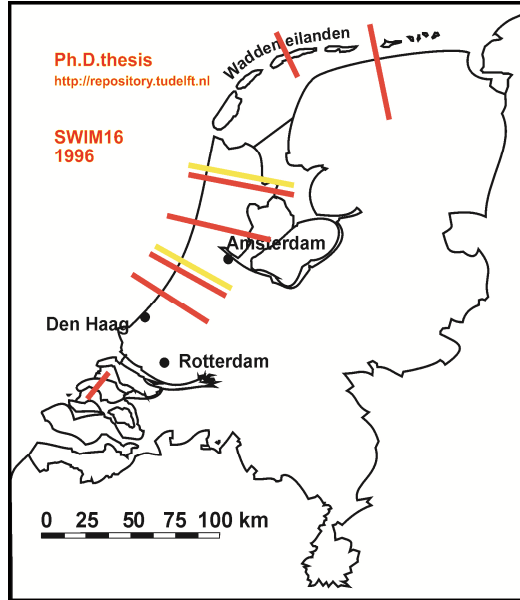


'DO NOT DO THIS AT HOME!' (DATA PROBLEM)



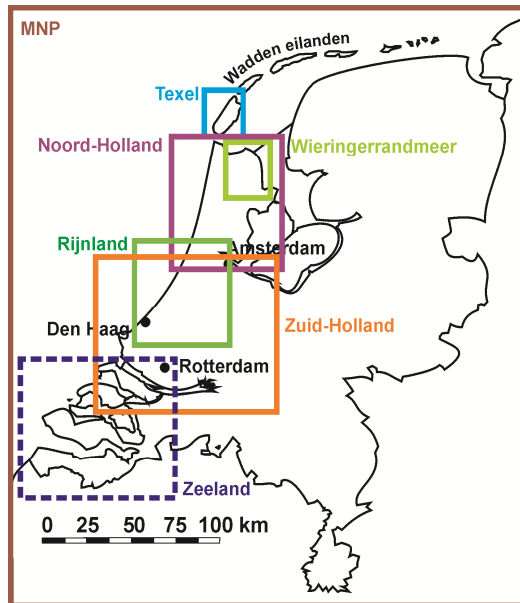
Modelling effect sea level rise on salt water intrusion

2D models



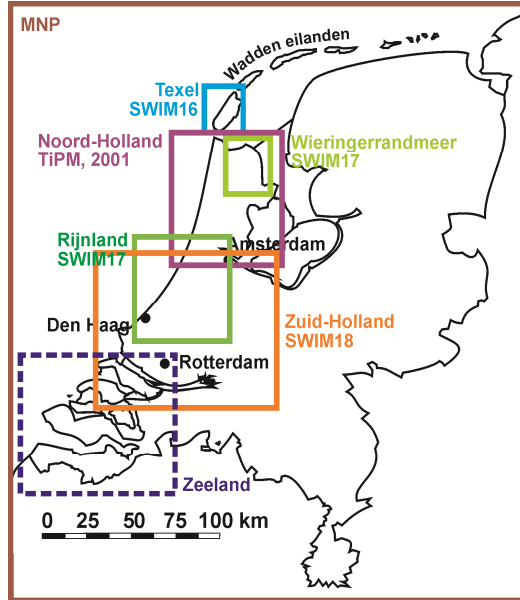
Modelling effect sea level rise on salt water intrusion

3D models



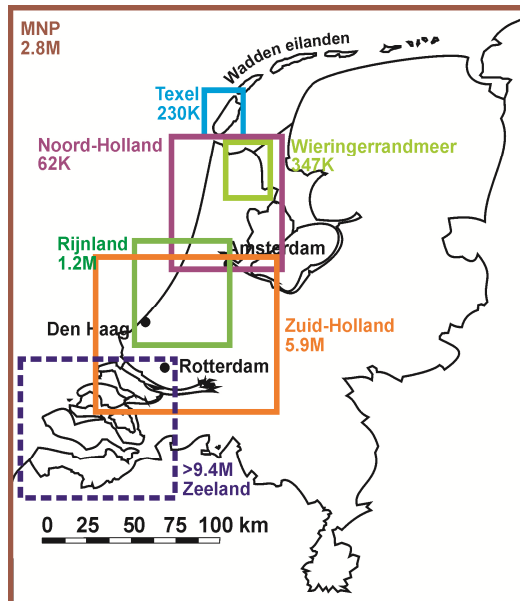
Modelling effect sea level rise on salt water intrusion

3D models
SWIM



Modelling effect sea level rise on salt water intrusion

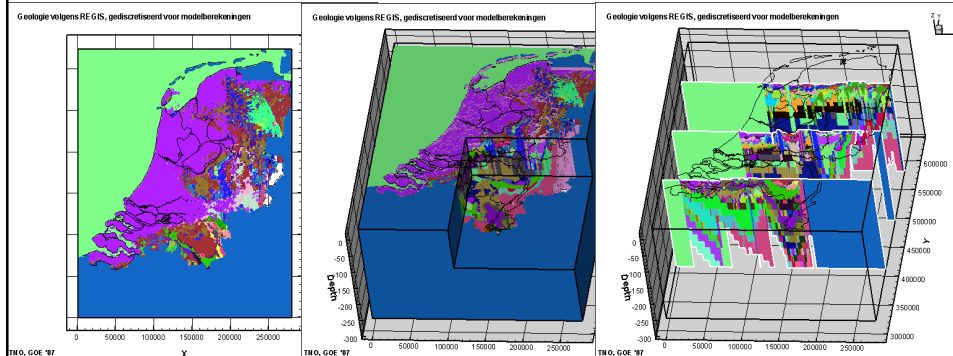
3D models
number cells



Recent model study for the whole Netherlands on the effect of sea level rise of water management (1)

Using the national subsoil parametrisation

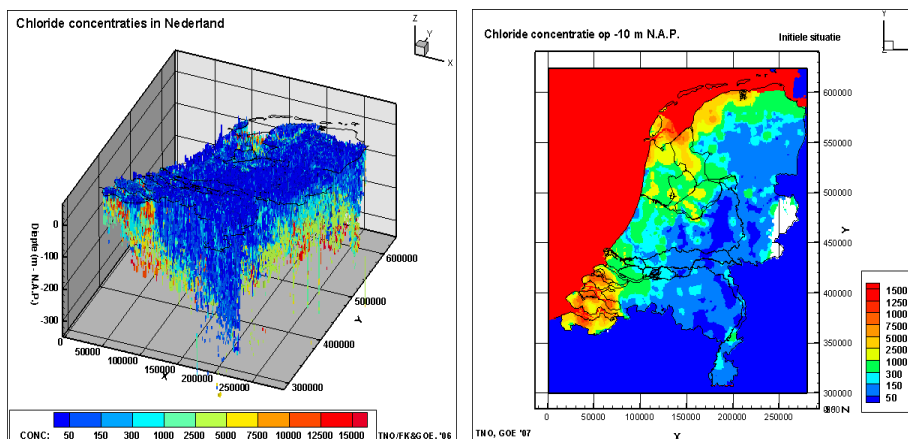
- REGIS V2
- Top geological system from +10m up to -280m M.S.L.
- 31 modellayers with thicknesses: 2*5m; 10*2m; 8*5m en 11*20m
- cellsize 1000x1000m (coarse)



Recent model study for the whole Netherlands on the effect of sea level rise of water management (2)

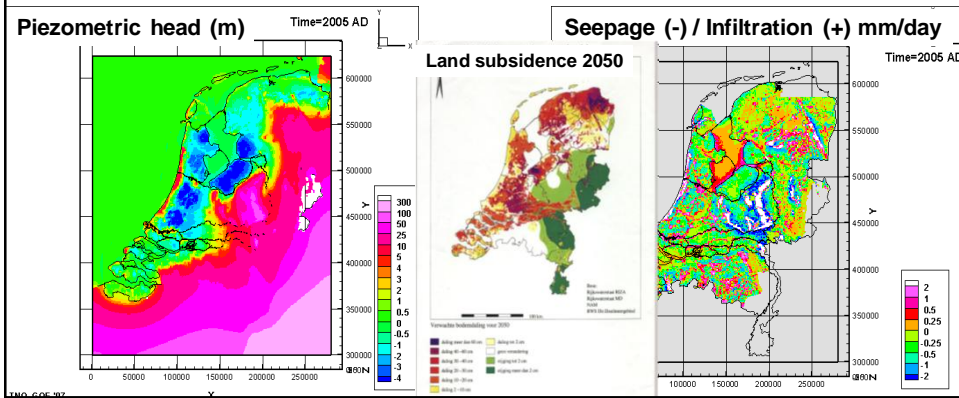
Using the national 3D salt concentration in groundwater

Zoet-Zout REGIS: ~65000 measuring points (analyses, VES, Borehole)

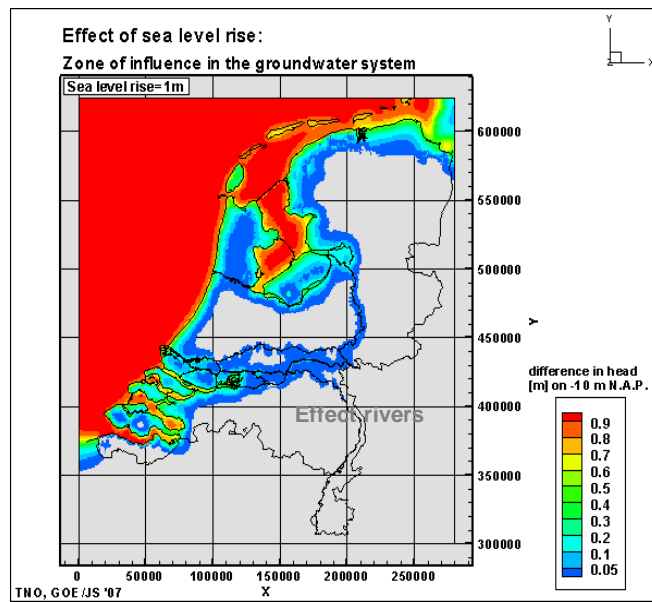


Recent model study for the whole Netherlands on the effect of sea level rise of water management (3)

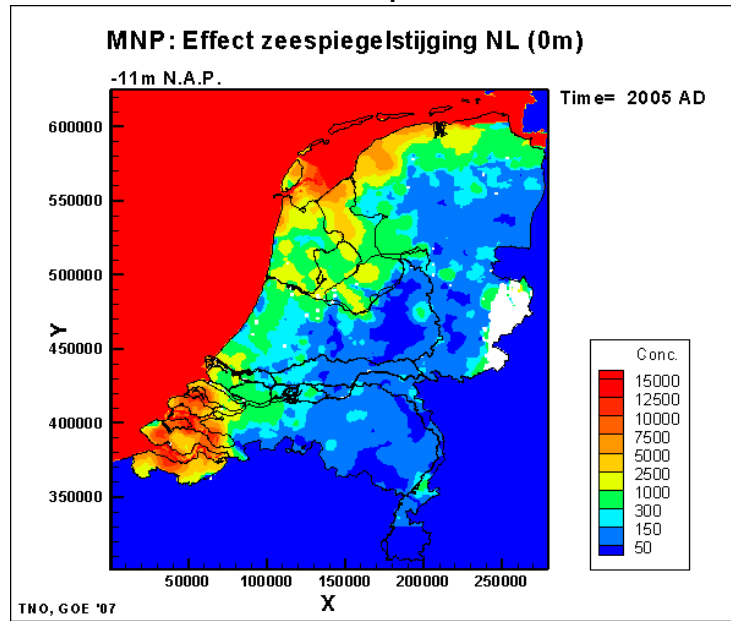
- Variable-density 3D groundwater flow model and coupled solute transport
 - 10 scenario's, including extreme sea level rise
 - including land subsidence estimates



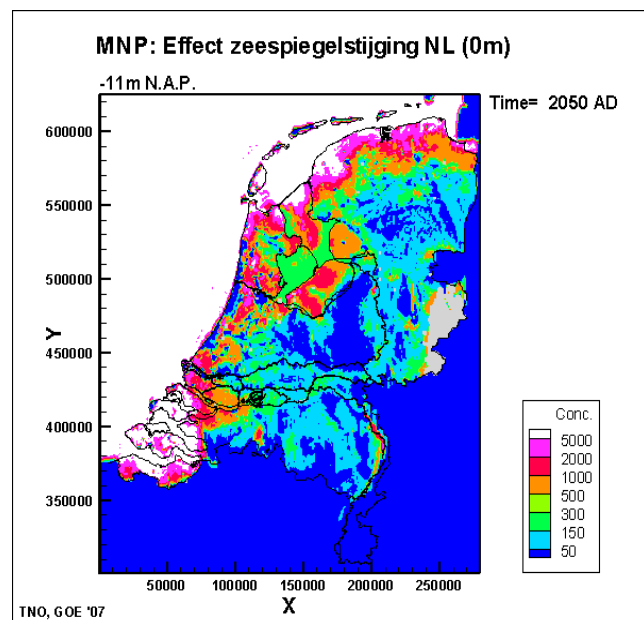
Results: zone of influence 1m sea level rise



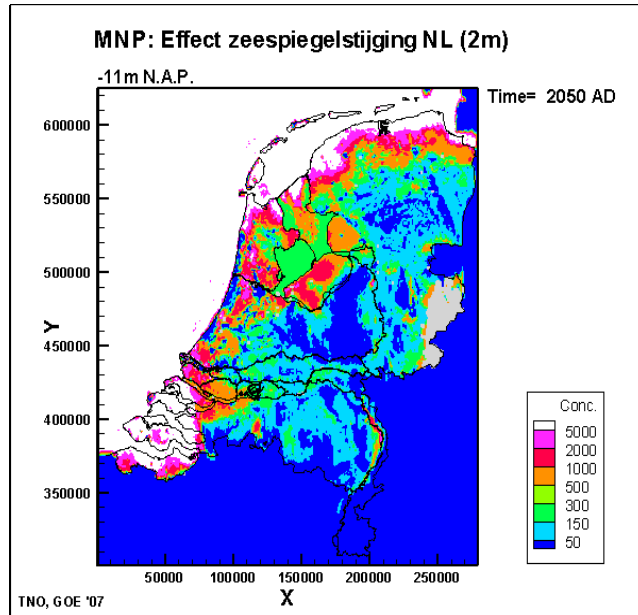
Salinisation over the period 2000-2050



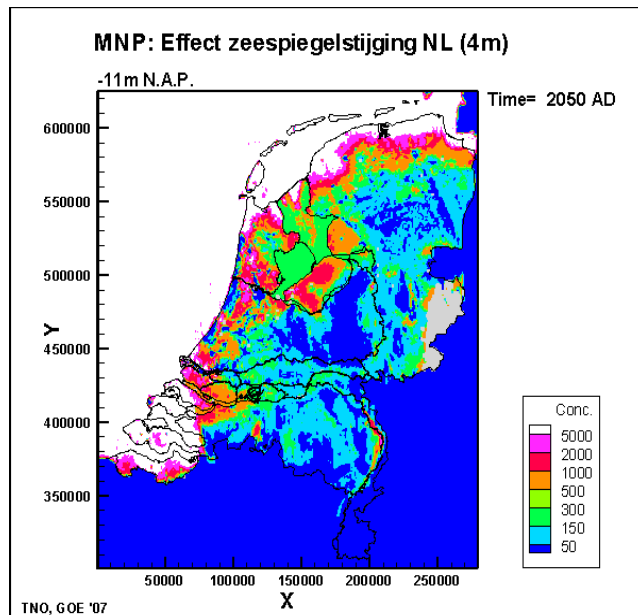
Salinisation subsoil at 0m sea level rise in 2050



Salinisation subsoil at 2m sea level rise in 2050

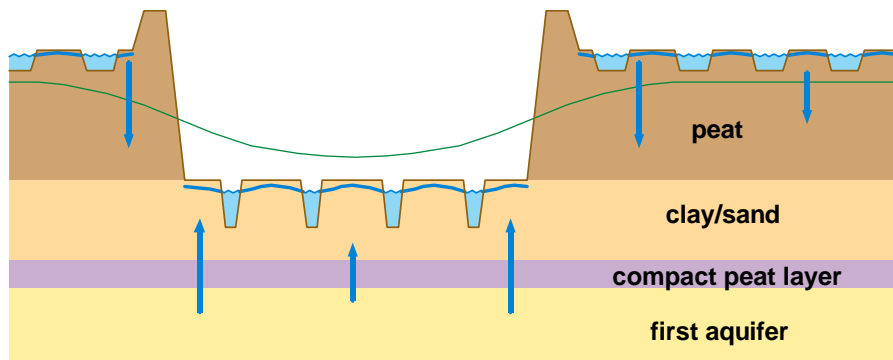


Salinisation subsoil at 4m sea level rise in 2050

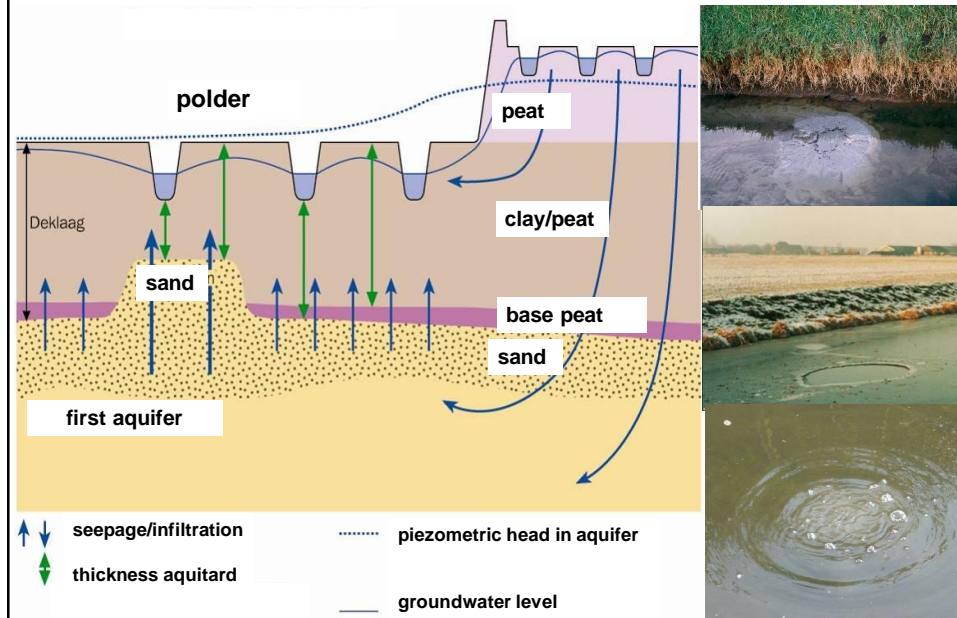


Salty wells

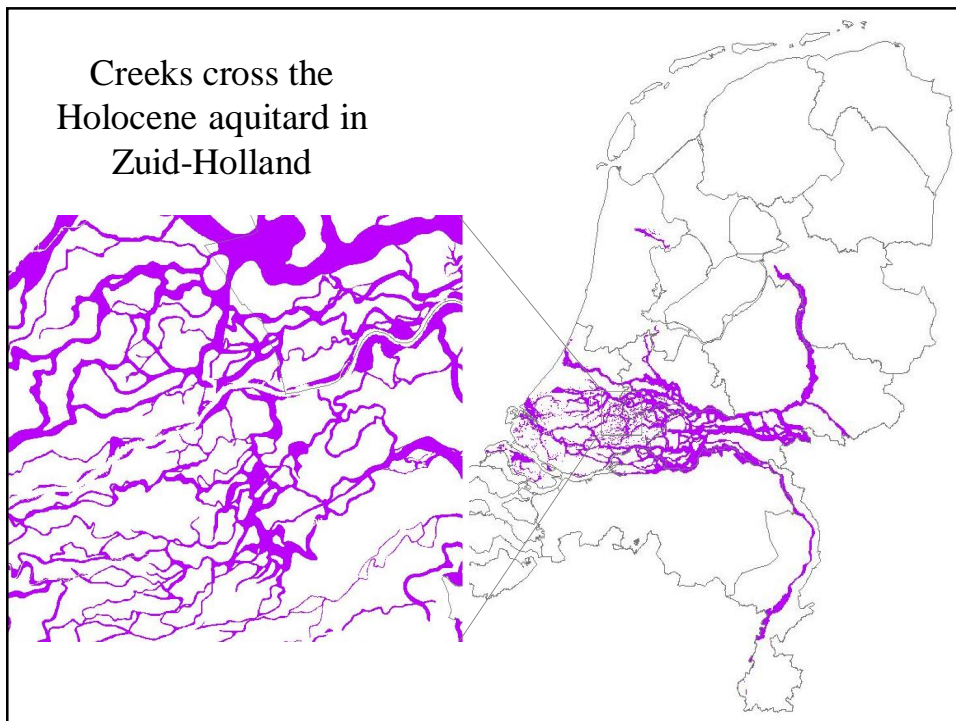
Seepage and infiltration situation around deep polders

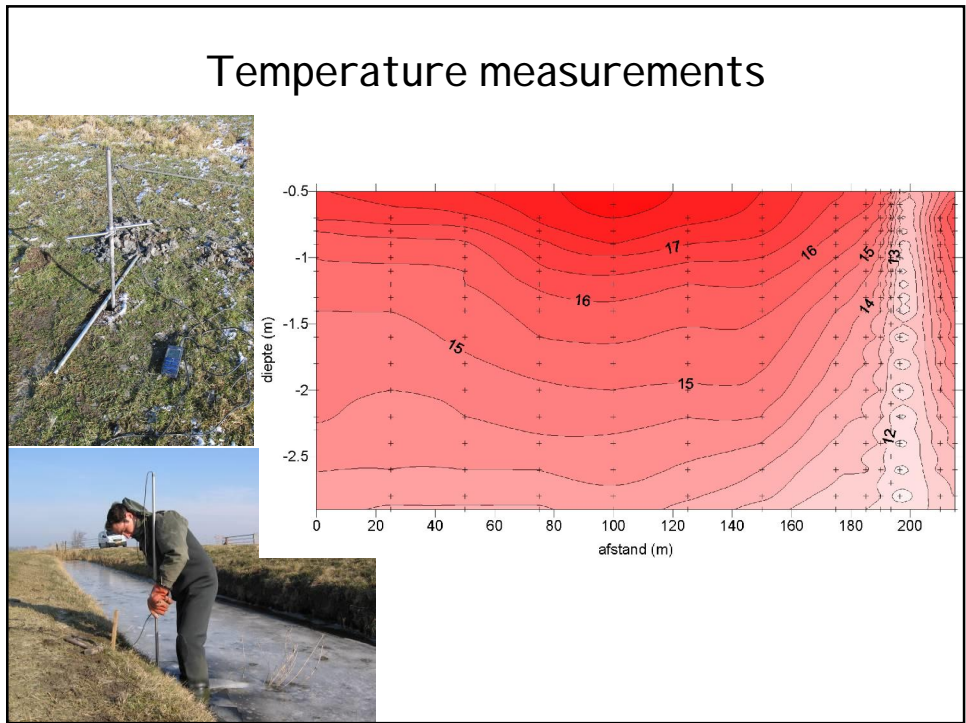


Risk of instable Holocene aquitards (1)

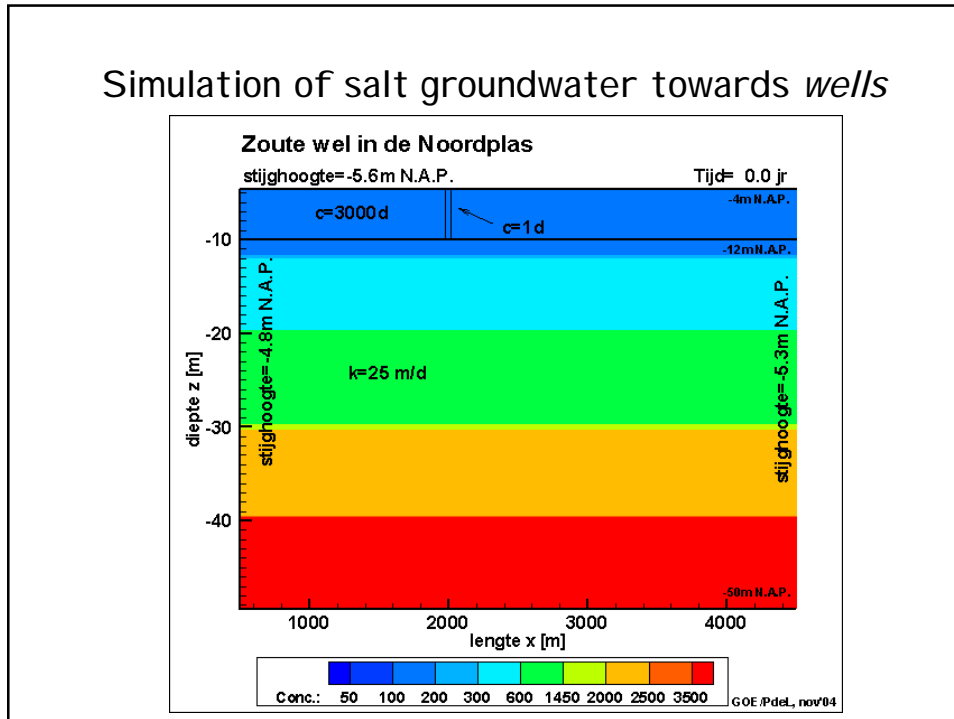


Creeks cross the Holocene aquitard in Zuid-Holland

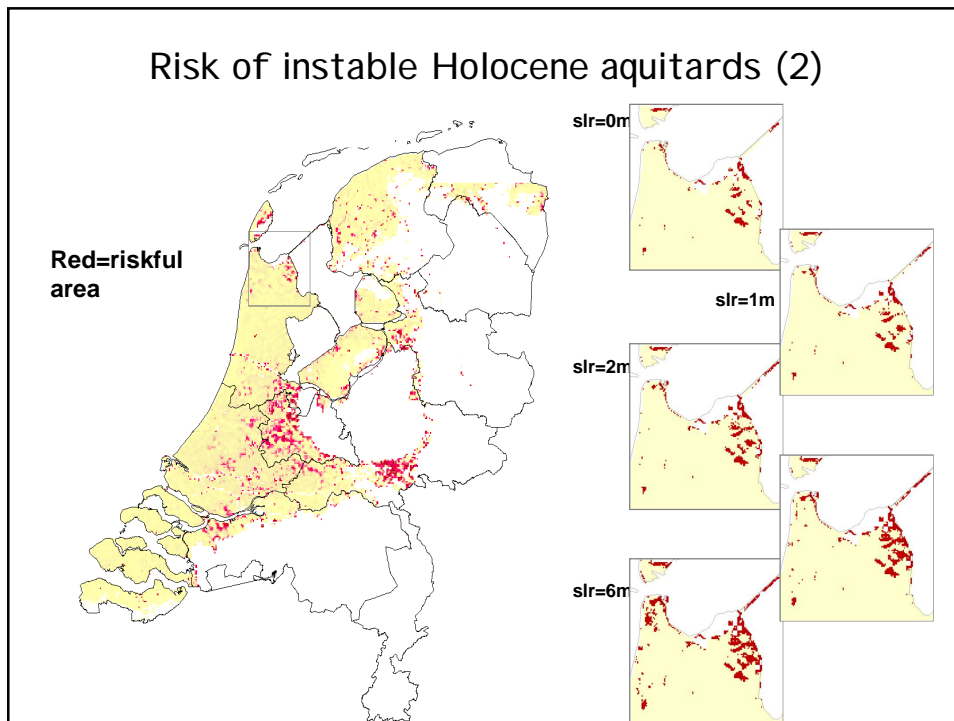




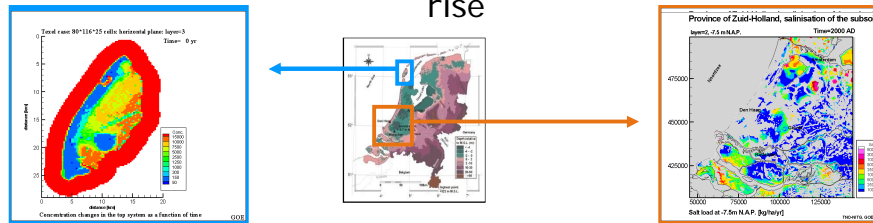
Simulation of salt groundwater towards wells



Risk of instable Holocene aquitards (2)



Quantification hydrogeological impacts of sea level rise

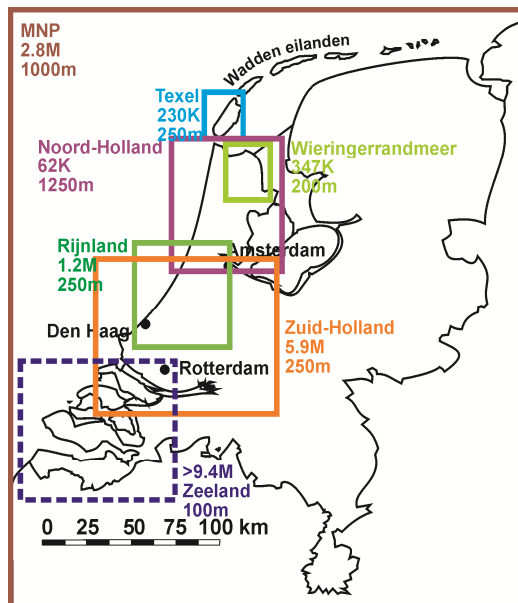


Situation at 2100 AD with sea level rise of 0.5m/century,
Including land subsidence at Zuid-Holland (max 1.0m/century)

	<u>Texel</u>	<u>Zuid-Holland</u>
Increase seepage (%)	+22	+4
Increase salt load (%)	+46	+34
Hinge area: from infiltration to seepage (% land surface)	+3	+5

Modelling effect sea level rise on salt water intrusion

3D models
number cells
grid size



Characteristics 3D Cases (I): geometry & subsoil

Case	Kop van Noord-Holland	Texel	Wieringer-meerpolder	Rijnland
total land surface [km ²]	2150	130	200	1100
L _x *L _y modelled area [km]	65*51	20*29	23*27	52*60
depth system [m -N.A.P]	290	302	385	190
aquifer hydr.cond. [m/d]	5-70	5-30	15-40	12-70
aquitard hydr.cond. [m/d]	0.12-0.001	0.01-1	0.012-0.056	2.5E-4-0.8
porosity	0.35	0.3	0.25	0.25
anisotropy [k _z /k _x]	0.4	0.4	0.25	0.1
long. dispersivity α _L [m]**	2	2	2	1
# head&conc. observations	not applicable*	111	95	1632
characteristics head calibration	not applicable*	Δφ =0.24 m σ=0.77 m	Δφ =0.34 m σ=0.21 m	Δφ =0.60 m σ=0.77 m

* calibration with seepage & salt load in polders

**molecular diffusion=10⁻⁹ m²/s; trans. disp.=1/10 long. disp.

Characteristics 3D Cases (II): model parameters

Case	Kop van Noord-Holland	Texel	Wieringer-meerpolder	Rijnland (=391 EM RAM)
horizontal cell size [m]	1250*1250	250*250	200*200	250*250
vertical cell size [m]	10	1.5 to 20	2 to 70	5 to 10
total # active cells	~40.000	~126.000	~312.000	~1.200.000
# cells	41*52*29	80*116*23	116*136*22	209*241*24
# particles per cell	27	8	8	8
total time [yr]	1000	500	50	500

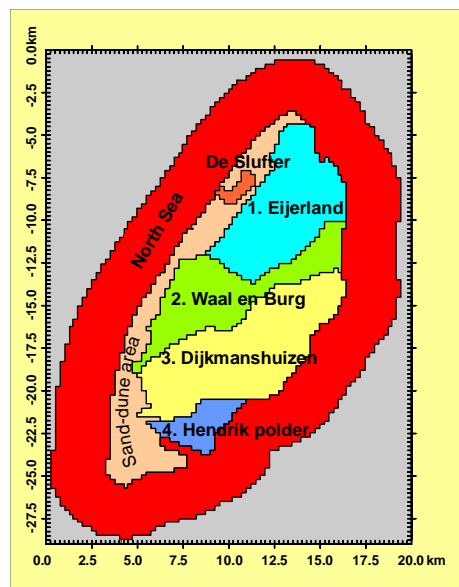
convergence head criterion= 10⁻⁵/10⁻⁴ m

flow time step Δt=1 year

Model of the island of Texel

Characteristics of the island of Texel (I)

Texel



- Tourist island in summer time

- Land surface: 130 km²

- Polder areas:

- 1. Eijerland
- 2. Waal en Burg
- 3. Dijkmanshuizen
- 4. Hendrik polder

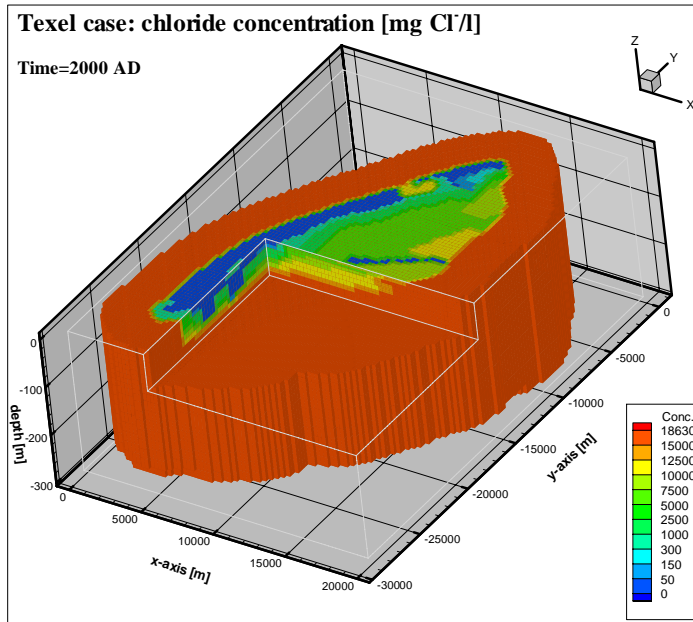
- Sand-dune area at western side

- 'De Slufter' is a tidal salt-marsh

- North Sea surrounds the island

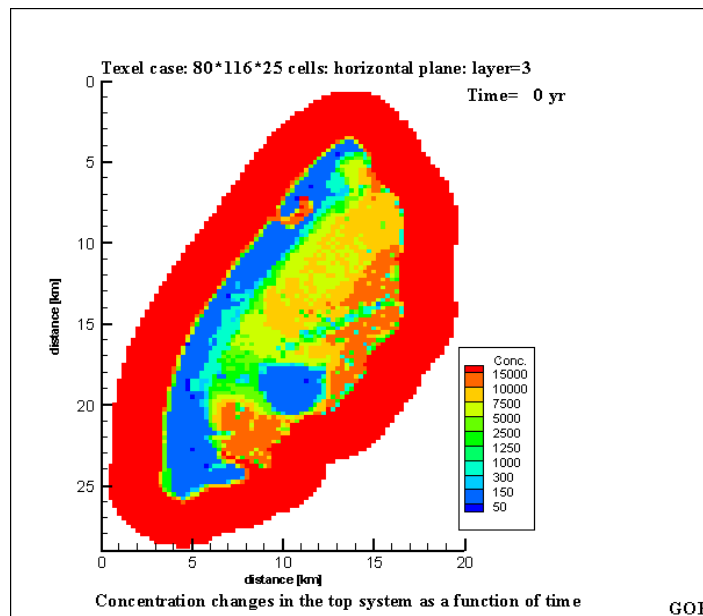
Texel: present 3D chloride distribution

Texel



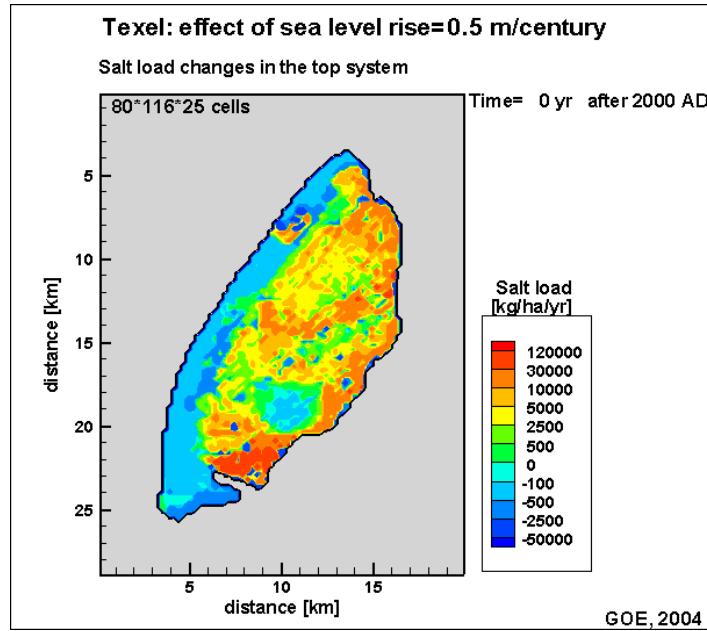
Texel: reference case=autonomous development

Texel



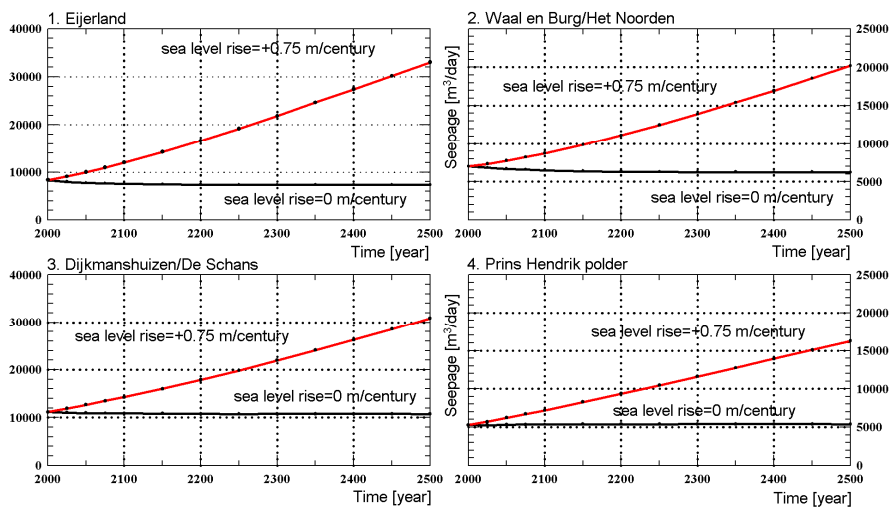
Texel: effect of sea level rise on salt load

Texel

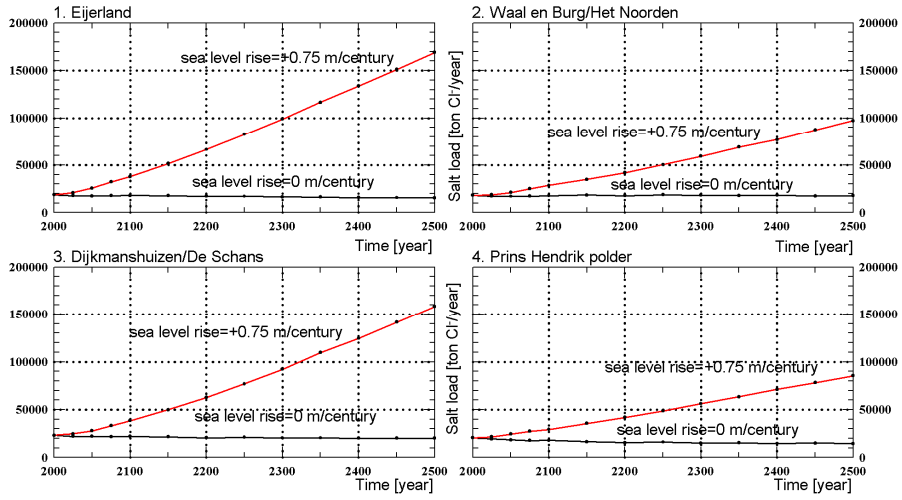


Texel: change in seepage of the four polders

Texel



Texel: change in salt load of the four polders



Model of the Province of Zuid-Holland

Case study: Province of Zuid-Holland

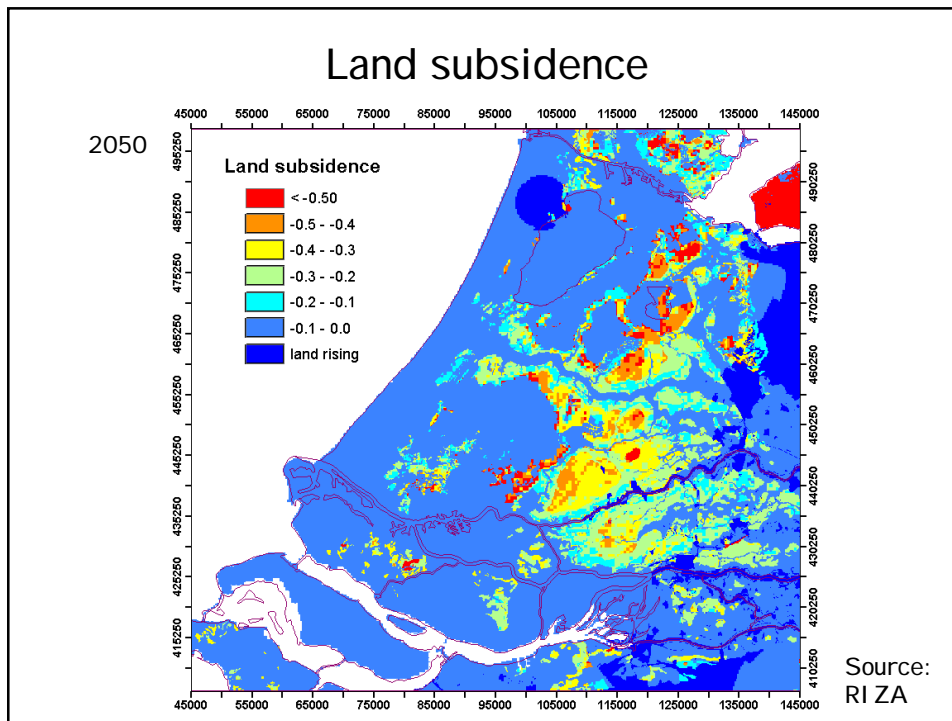
European water framework directive

“in 2015, state of all groundwaters and surface waters must be good“

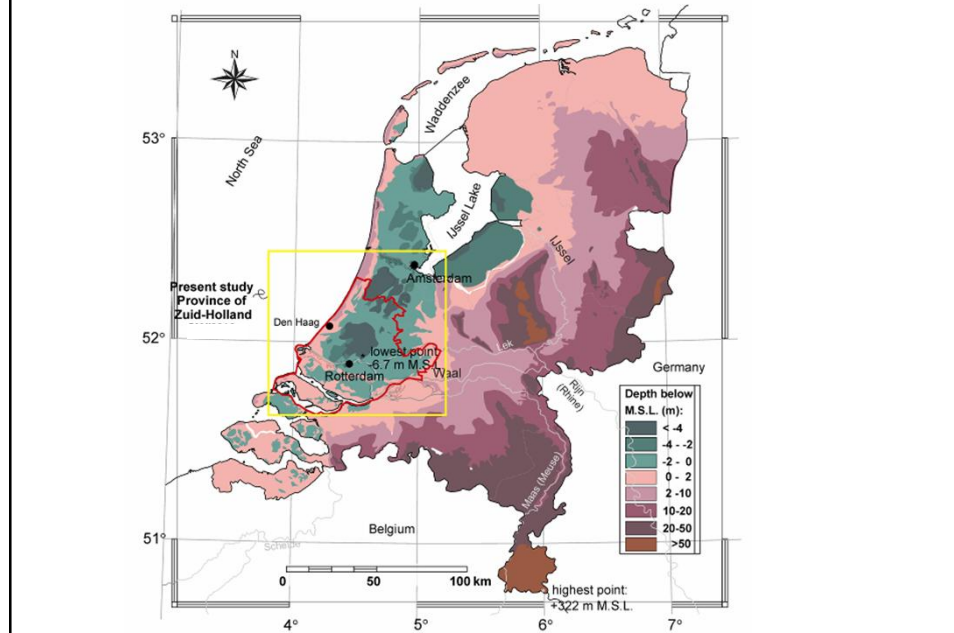
Identification of all fresh groundwater bodies in the province

How fast is the salinisation process?

More seepage, more salt load?



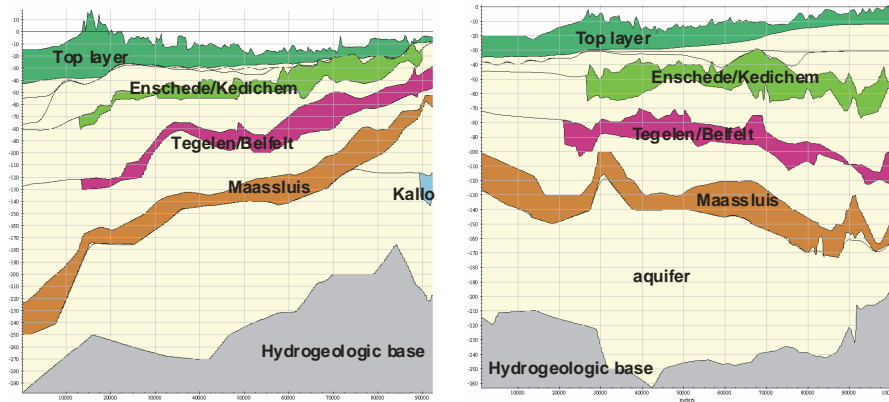
Location of the Province of Zuid-Holland



Numerical model description

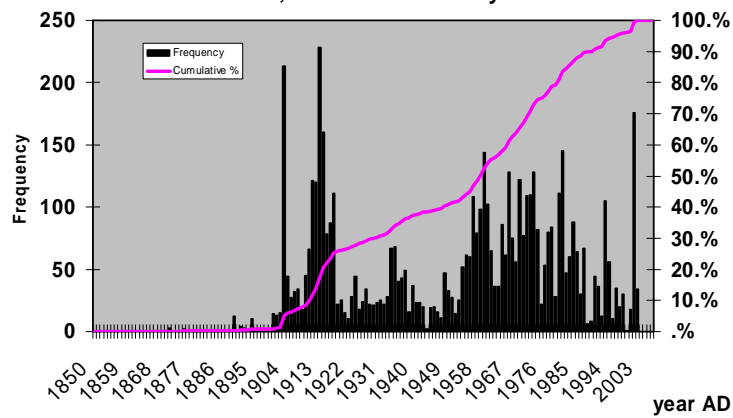
- variable-density groundwater flow
- coupled solute transport
- MOCDENS3D
- area: 100km * 92.5km * 300m depth
- 400 * 370 cells, 40 layers
- ~4 million active cells
- uses most accurate Dutch 3D subsurface schematization available
- 9 aquifers and aquitards
- uses 5772 chloride concentration measurements

Position and name of aquitards



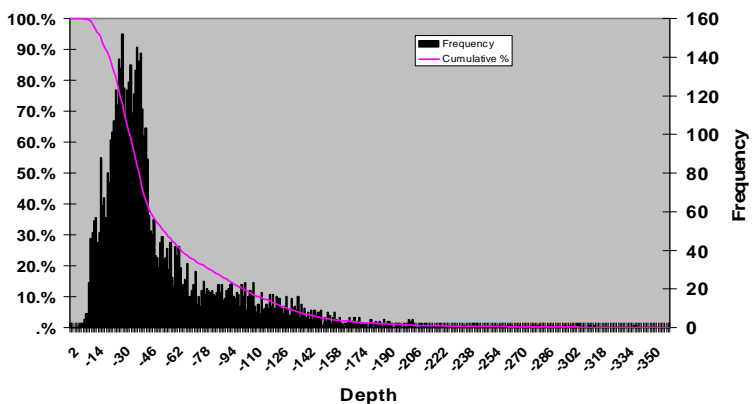
3D interpolation of chloride-concentration

Chloride concentration measurements in Province Zuid-Holland, used in 3D-density matrix

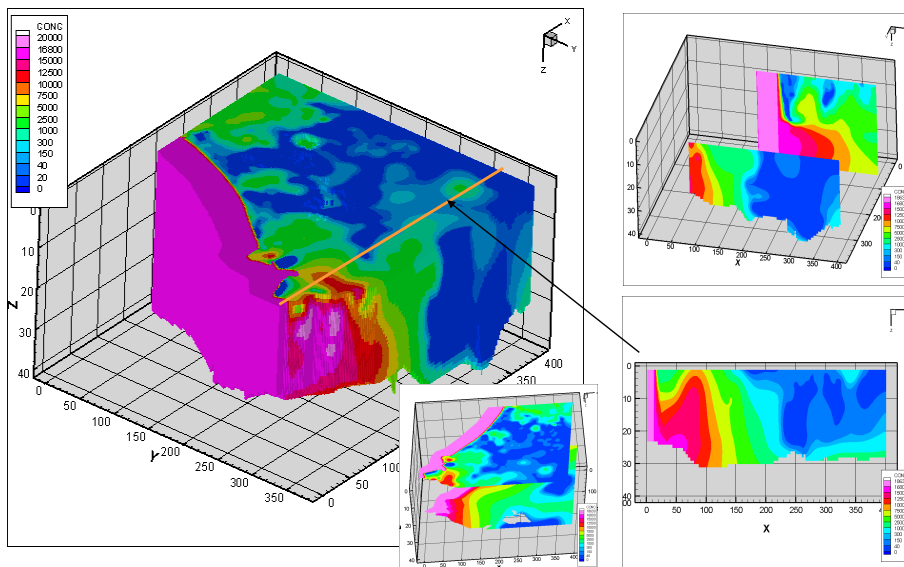


3D interpolation of chloride-concentration

Histogram: depth Chloride measurements



Initial chloride distribution

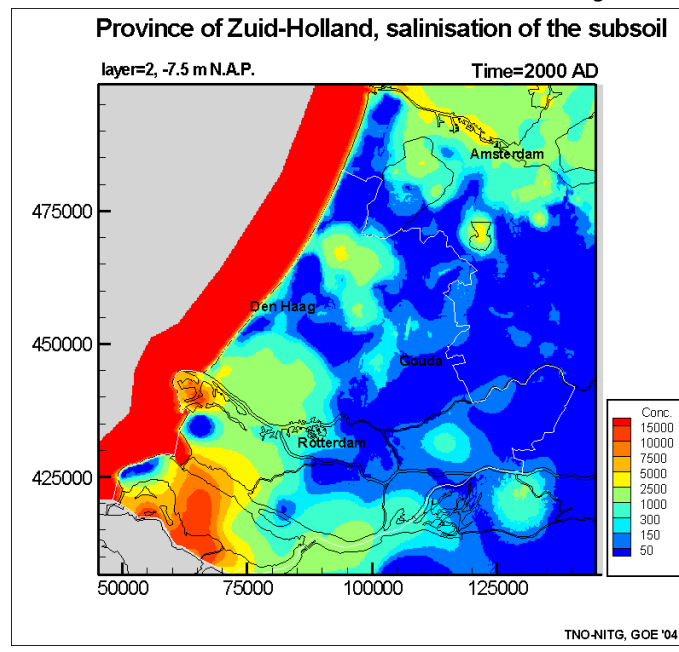


Present freshwater volume

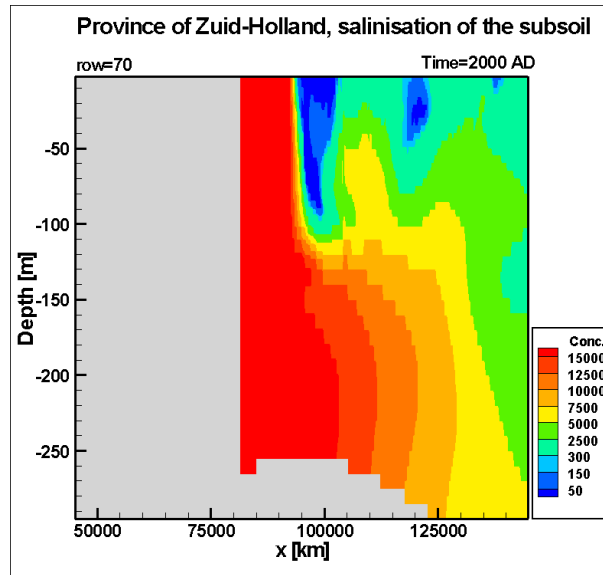
27 billion m³

36% fresh, 14% brackish, 50% saline

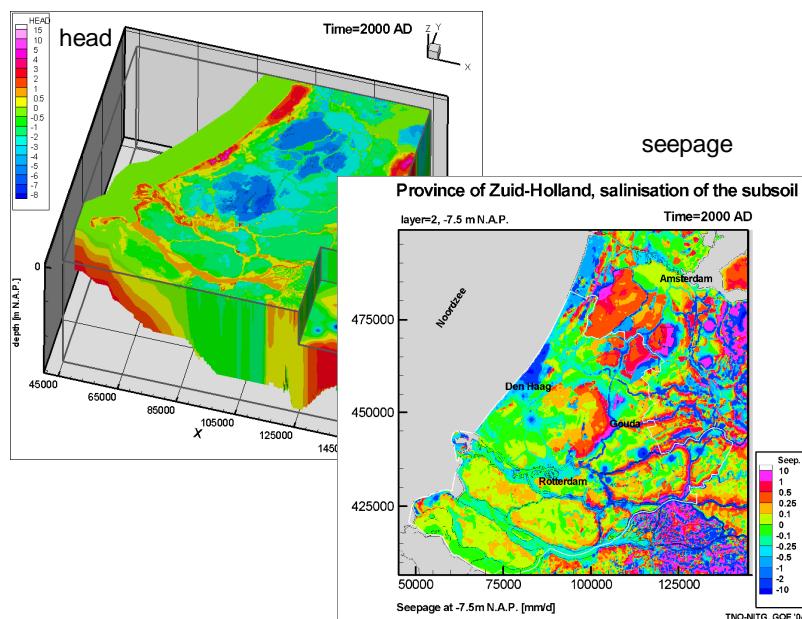
Results: Chloride conc. in 200 yrs



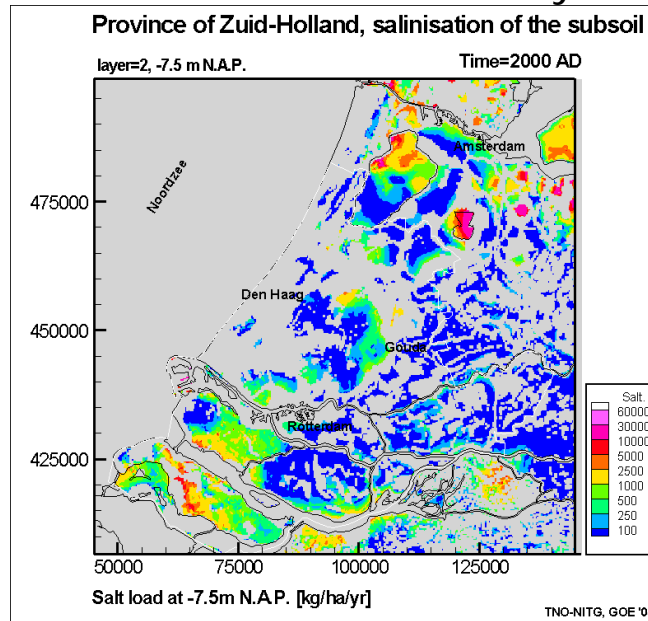
Results: Chloride conc. in 200 yrs



Results: freshwater head and seepage at 2000 AD



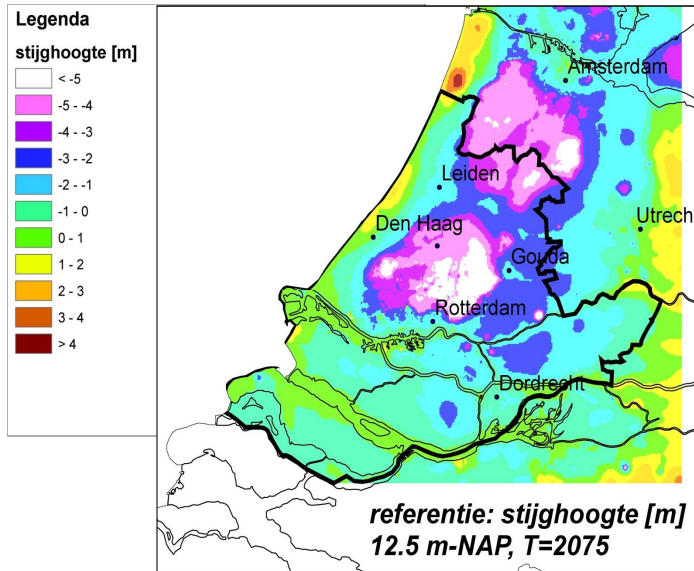
Results: Salt load in 200 yrs



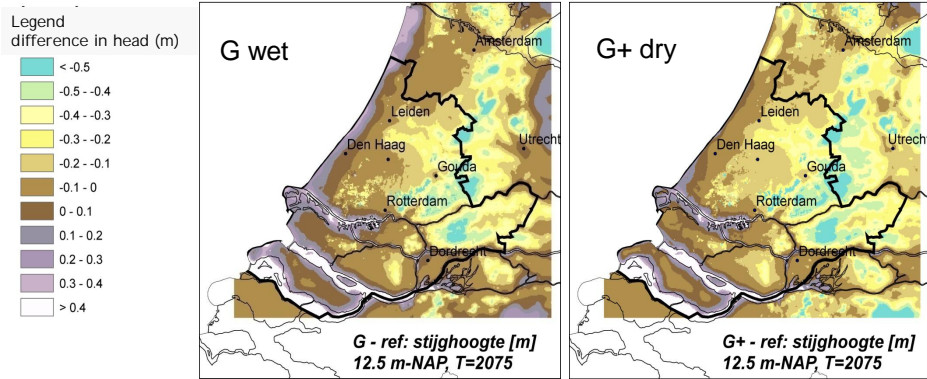
Effect sea level rise, change in natural groundwater recharge and land subsidence on freshwater head in aquifer

Some regional modelling results

Freshwater head at -12.5 M.S.L.



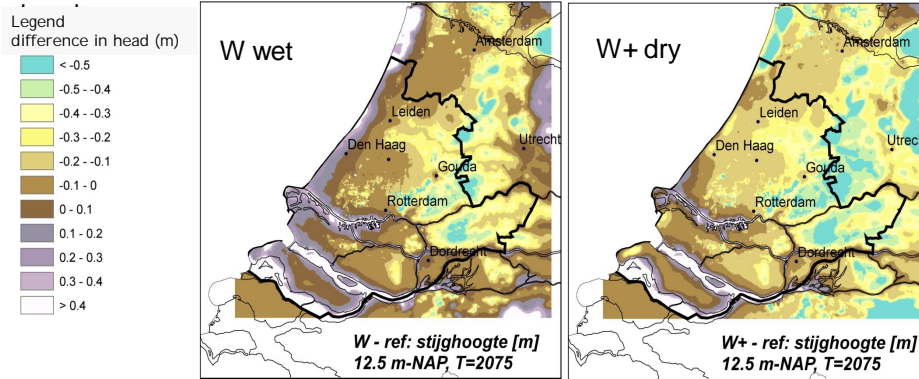
Difference in freshwater head on op -12.5 N.A.P.: G scenarios



Sea level rise is 60 cm

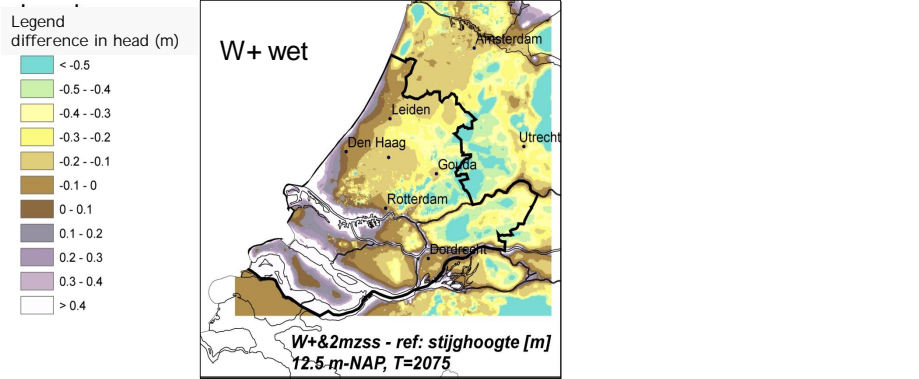
Including change in natural groundwater recharge

Difference in freshwater head on op -12.5 N.A.P.: W scenarios



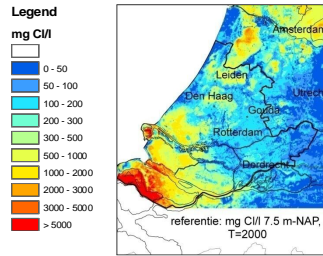
Sea level rise is 85 cm

Difference in freshwater head on op -12.5 N.A.P.: W scenarios



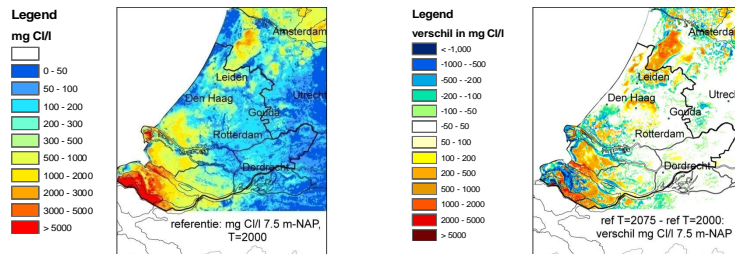
Sea level rise is 200 cm

Salinisation/freshening Netherlands?: Present situation



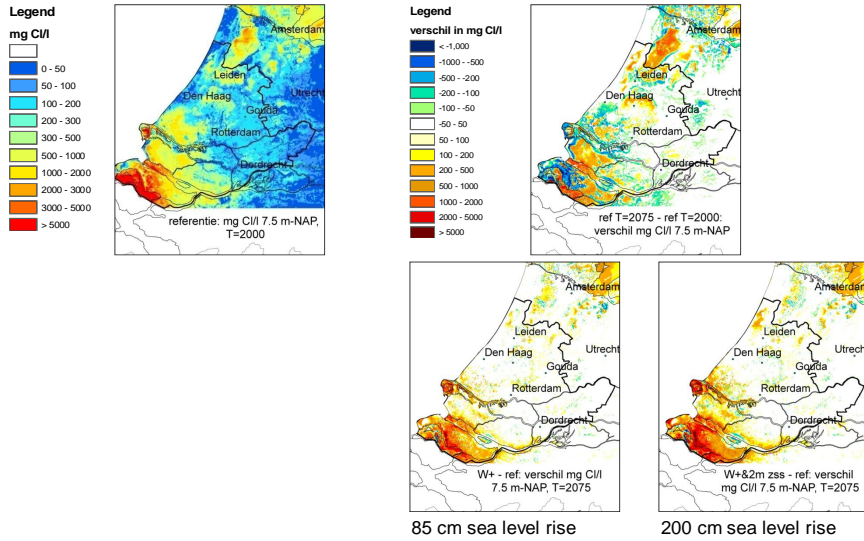
modelstudy

Salinisation/freshening Netherlands?: Autonomous processes



modelstudy

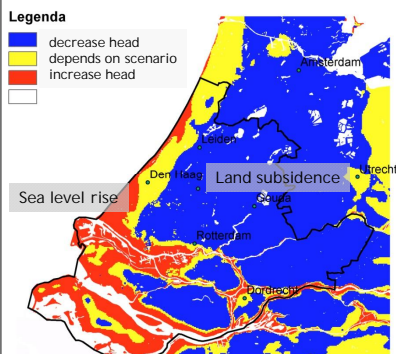
Salinisation/freshening Netherlands?: climate change



modelstudy

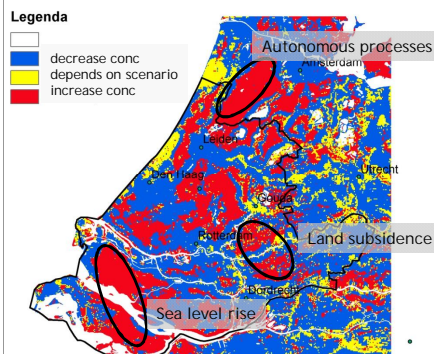
Effect climate scenarios in 2075 on

freshwater head



Increase or decrease head for all climate scenarios G, G+, W, W+

salinisation



Increase or decrease concentration for all climate scenarios G, G+, W, W+

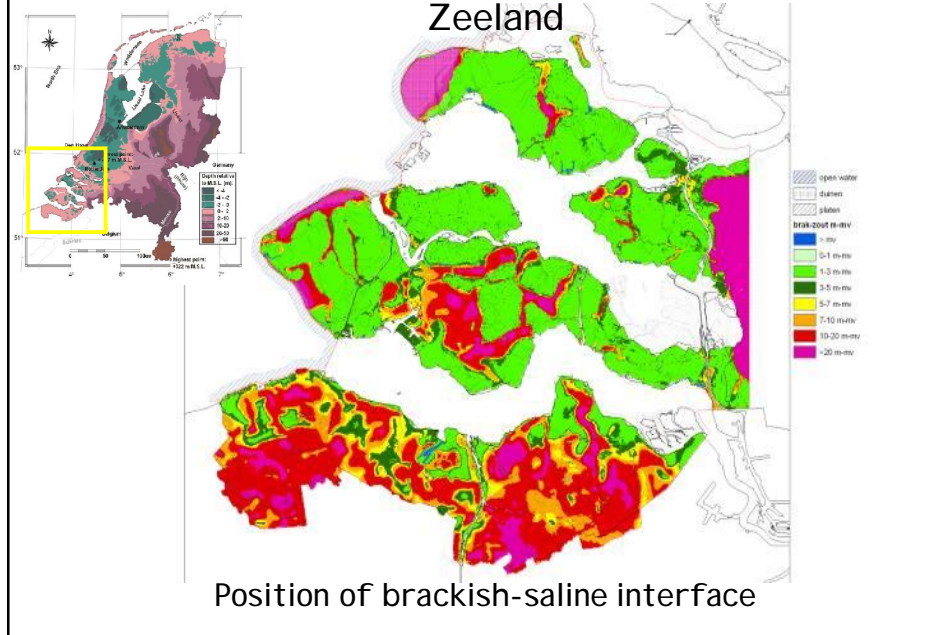
Modelstudie PZH

Rainwater lenses in an agricultural setting

Shallow dynamic freshwater bodies flowing upon brackish-saline groundwater

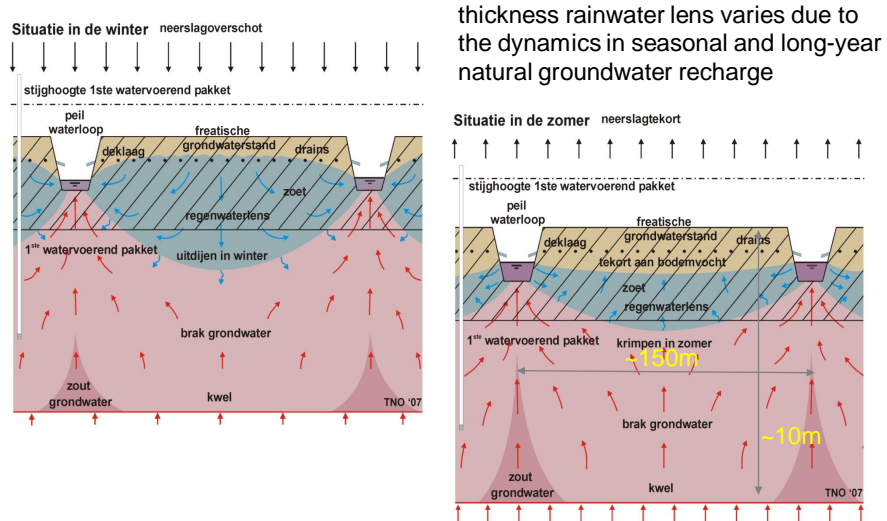
- density dependent
- dynamics: seasonal & long-year

Salinisation of the phreatic groundwater in Zeeland

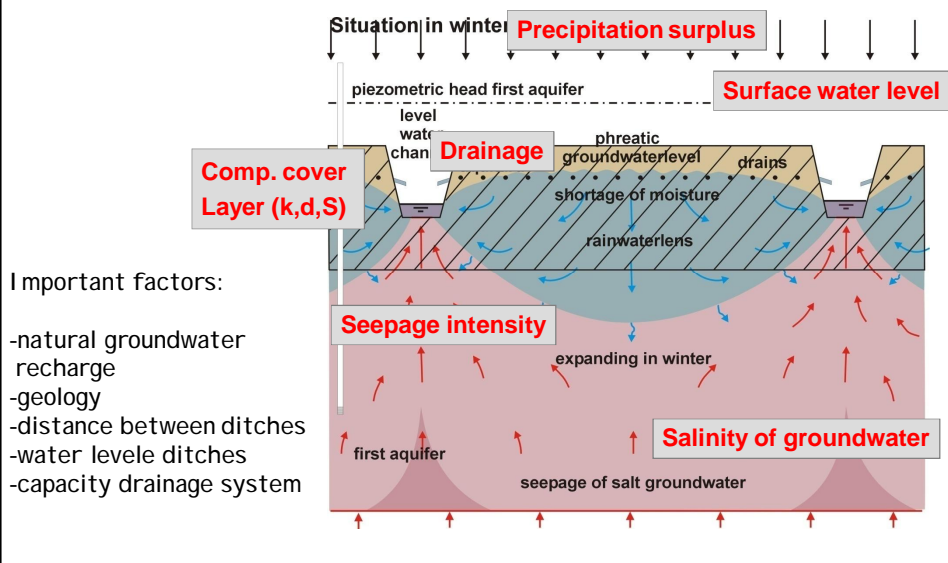


Salinisation of the phreatic groundwater in Zeeland

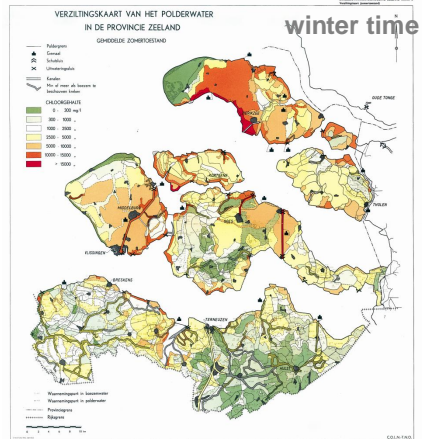
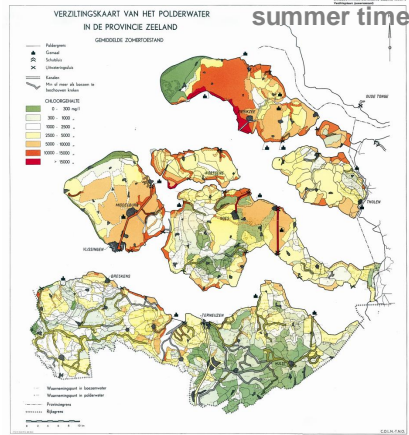
Dynamic rainwater lenses floating on saline groundwater



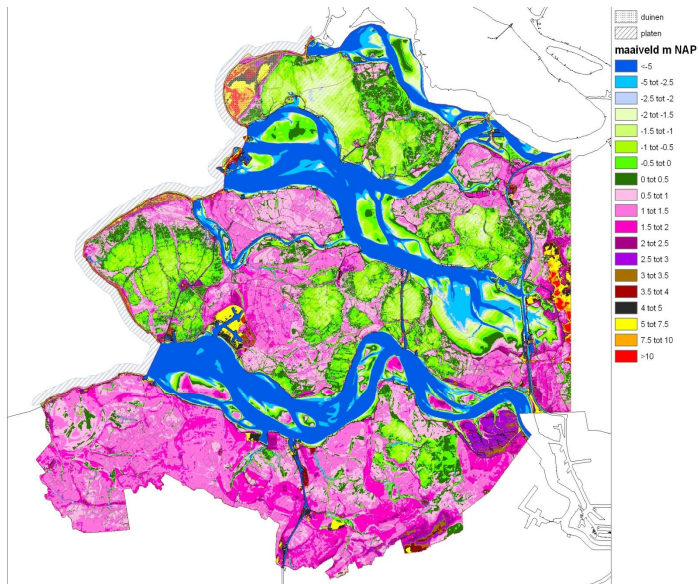
Factors controlling fresh-salt interface



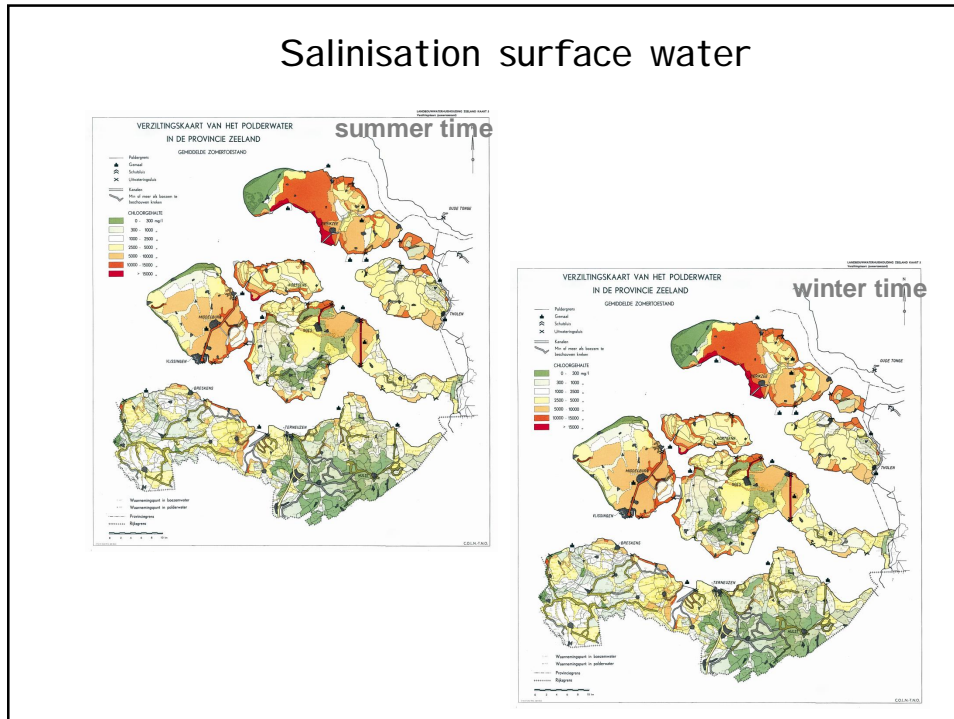
Salinisation surface water



Position of the ground surface



Salinisation surface water



Problem definition dynamic freshwater lenses



Salt in the agricultural plots originates from:

- surface water system (irrigation water)
- groundwater system (salt load to the root zone)

The salinisation will increase due to:

- sea level rise
- climate change
- water level management



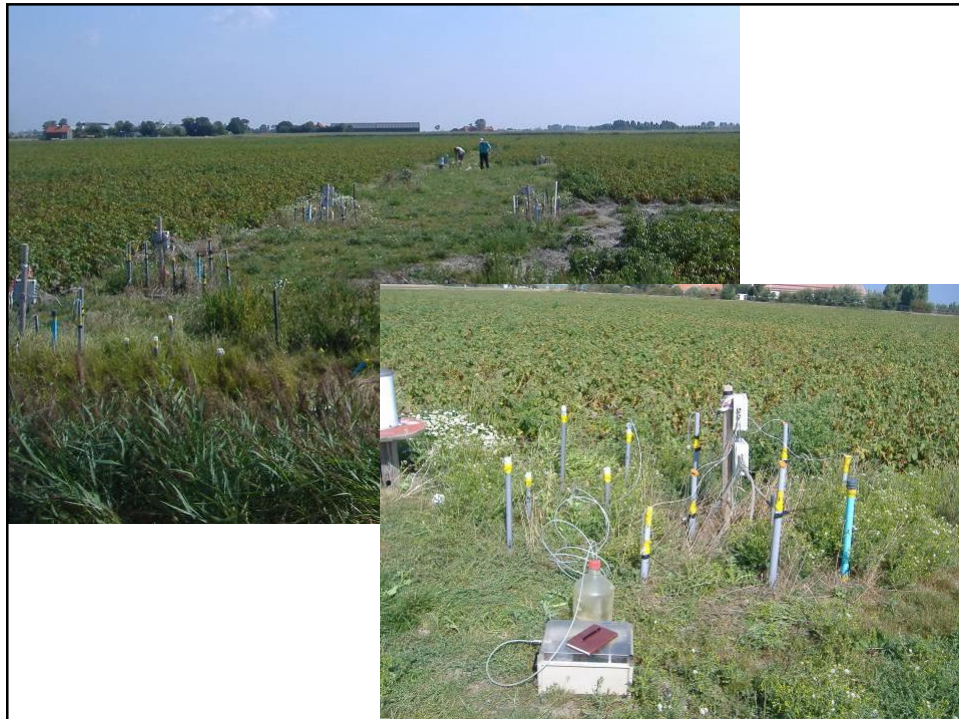
How to tackle the problem?

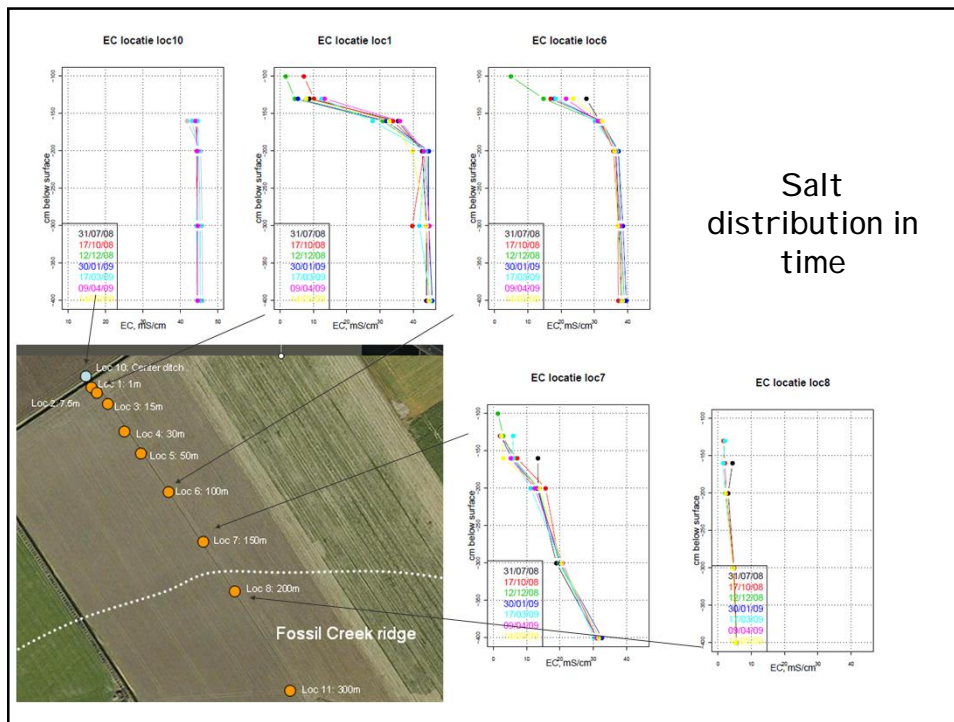
Field measurements at parcels

- fresh-brackish-salt interface at local scale using T-EC-probe and later CVES and ERT
- groundwater level and quality
- surface water level and quality

Modelling

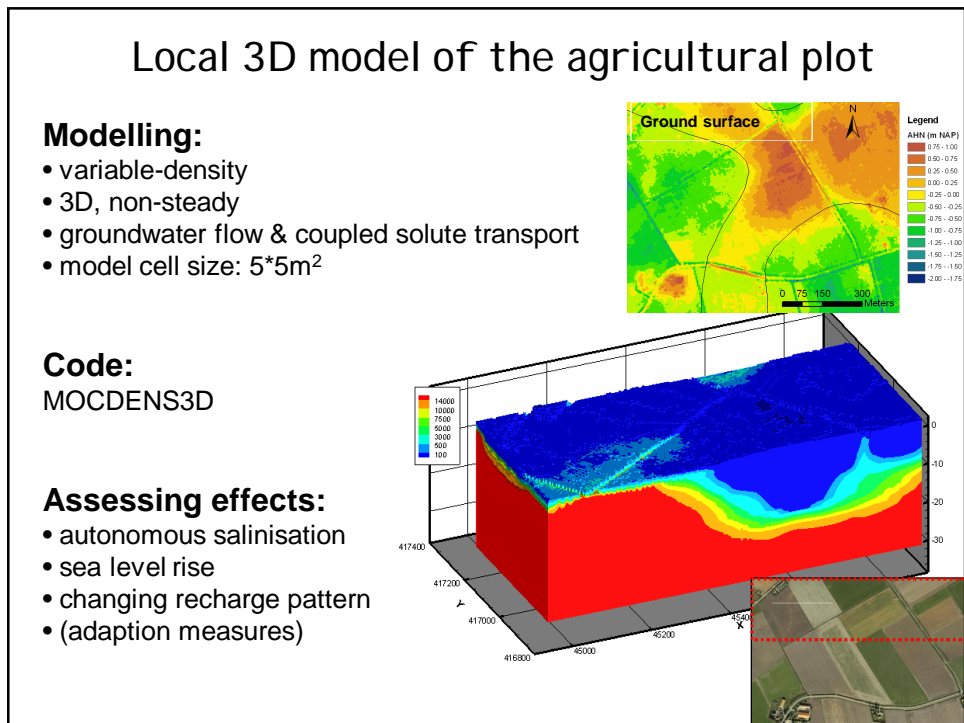
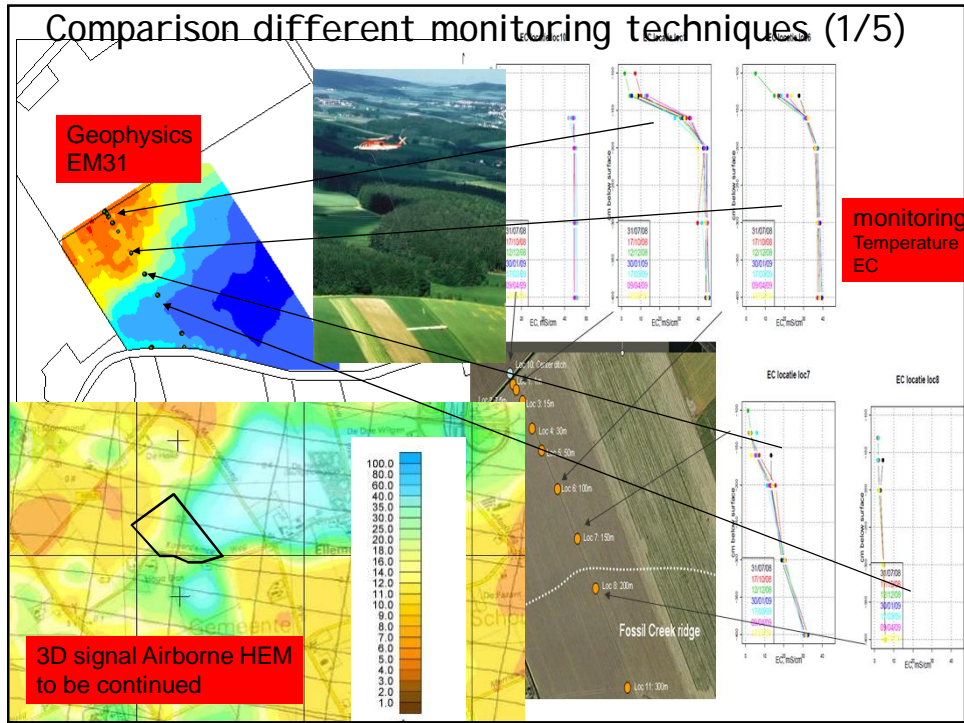
- density dependent groundwater flow
- two different scales:
 - regional scale: transect perpendicular at coast
 - local scale: parcel between two ditches



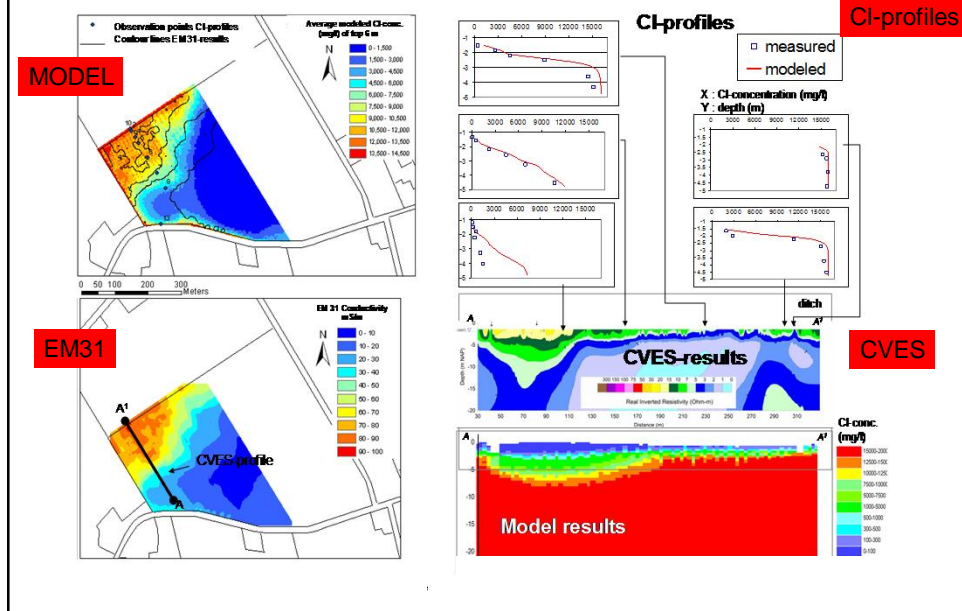


Salt distribution in time

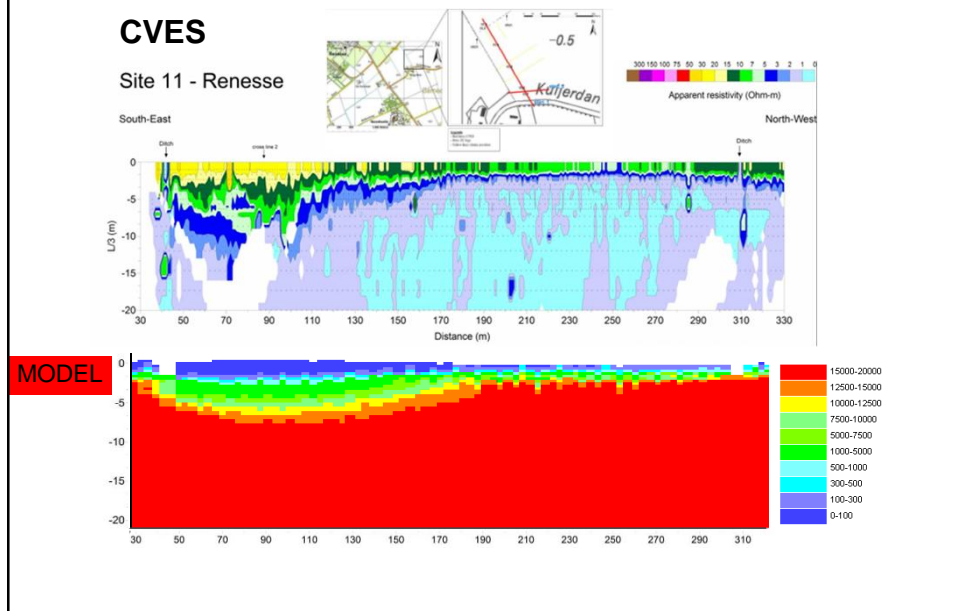
- TEC
- sampling
- EM31
- CVES
- HEM
- ECPT
- Numerical models (2D and 3D)



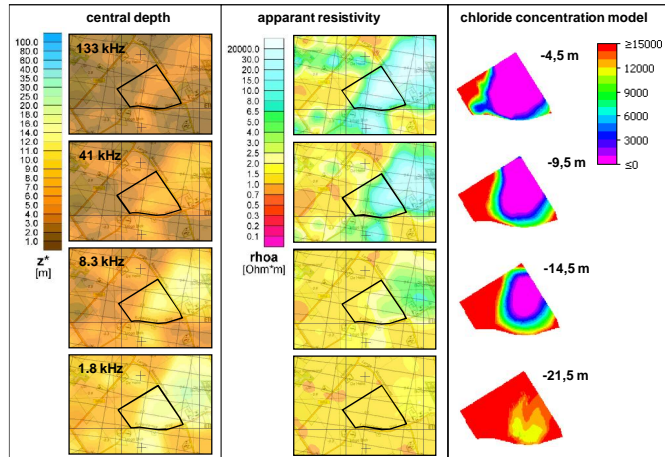
Comparison model with EM31, CVES, profiles



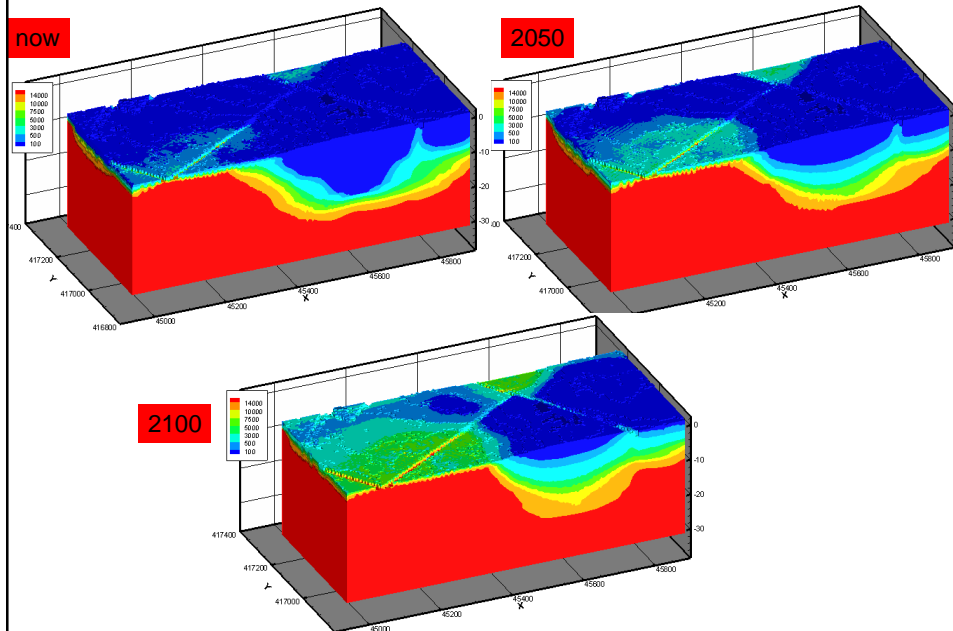
Comparison 3D model and CVES



HEM data



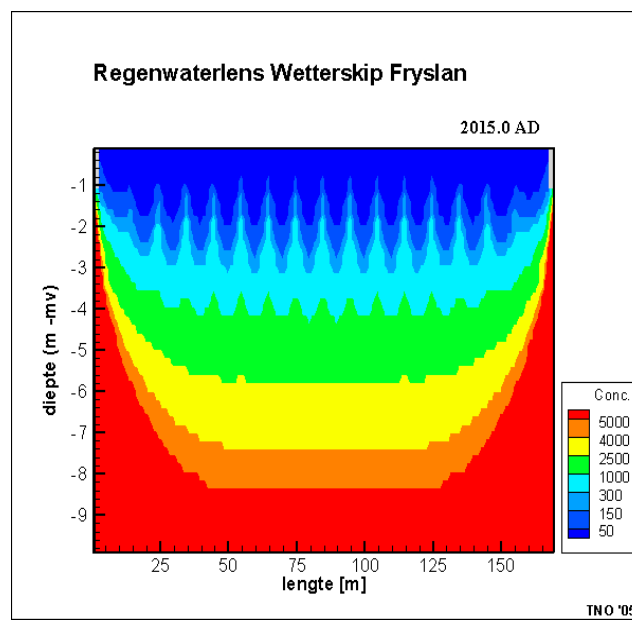
Climate change scenario (dry): model result



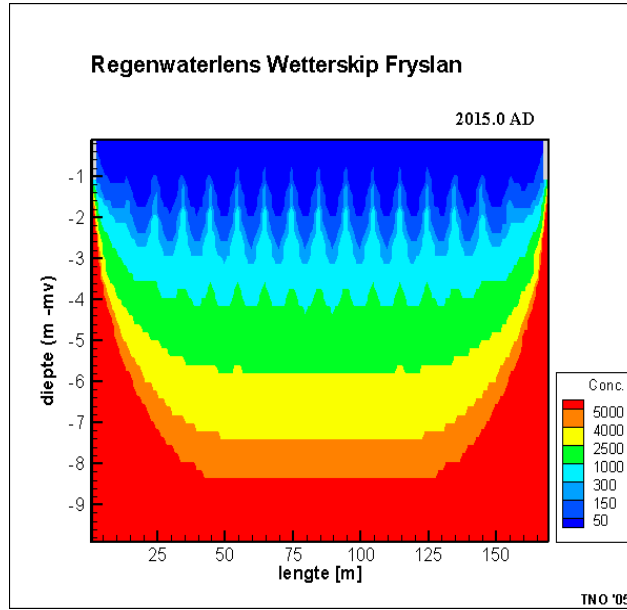
To be continued...

- Implementing more realisations of 3D geology and initial 3D fresh-saline
 - Analyse the differences
- Running climate change scenarios (on national and regional level)
 - Effect on surface water (salt load)
 - Effect on root zone (rainwater lenses)
 - Effect on freshwater volumes (drinking water)
- Compare model results of different scales and give recommendations

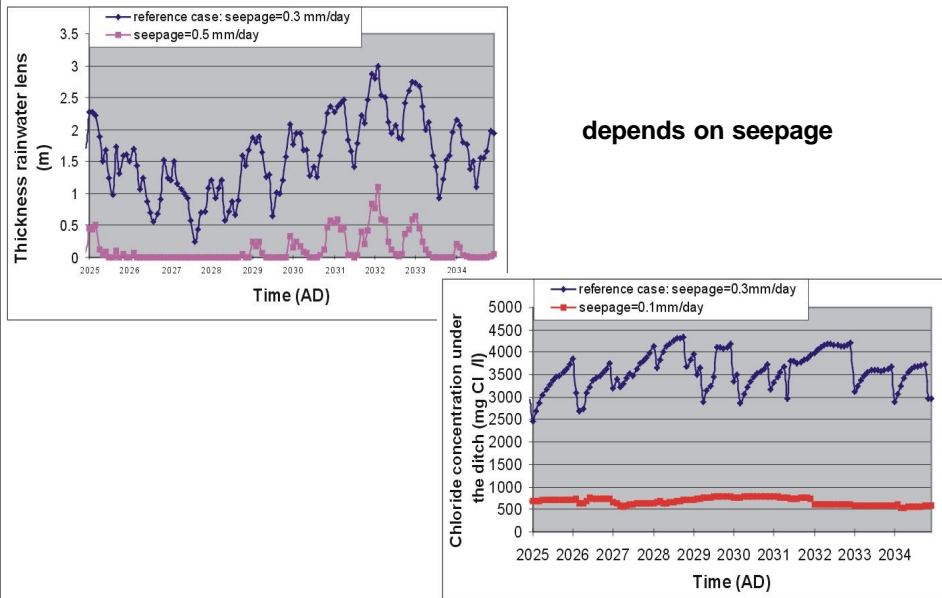
Model the dynamics of fresh-brackish-salt interface



Model the dynamics of fresh-brackish-salt interface



Thickness of the lens and salt load to surface water varies



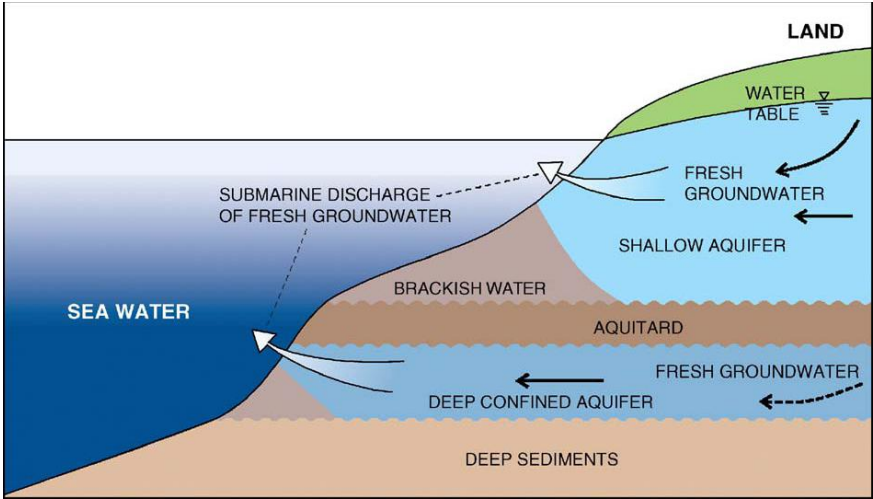
Conclusions (salinisation Dutch aquifers):

- Salinisation in the Netherlands is a non-stationary process
- Three physical processes threaten the Dutch aquifers:
 - autonomous development
 - land subsidence
 - sea level rise
- Increase in seepage and salt load can be severe during the coming 50/100 years
- Modelling techniques are available to assess possible effects

Recommendations (salinisation Dutch aquifers):

- Number of quality measurements should be increased
- Feasibility study is necessary to implement potential technical measures to compensate salt water intrusion

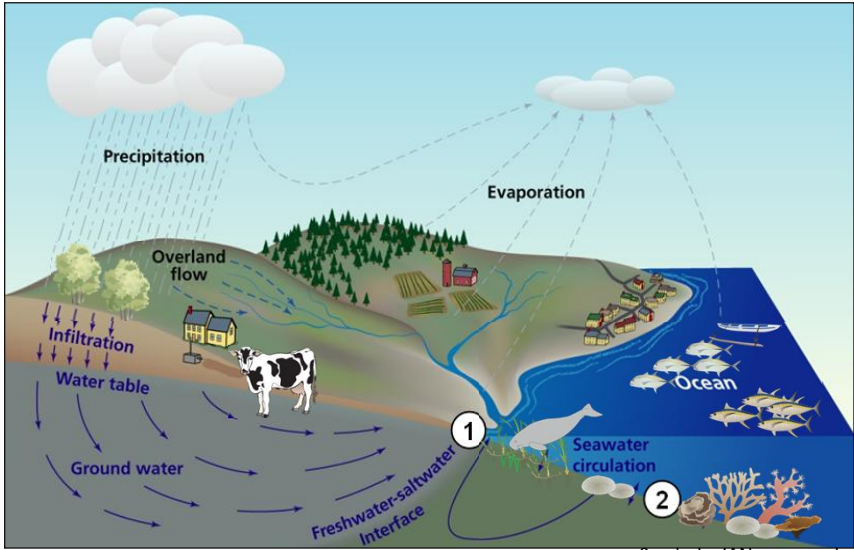
What is Submarine Groundwater Discharge (SGD)?
any flow of water out across the sea floor



Burnett et al, 2006

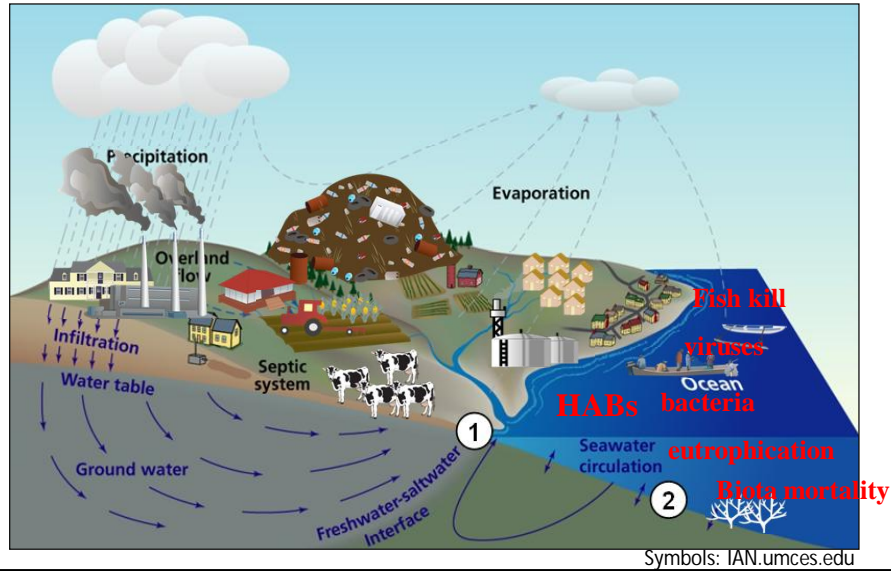
Why study SGD?

Nutrients are transported from land to sea via SGD pathway



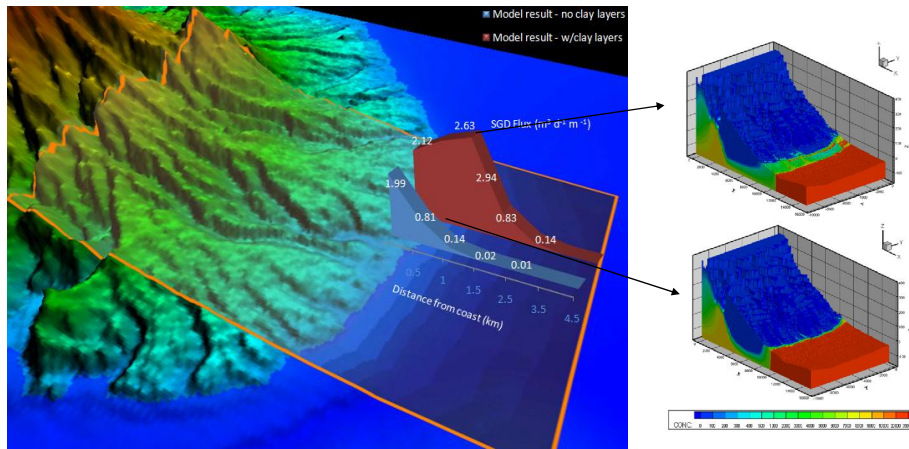
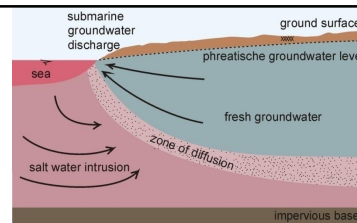
Why study SGD?

Nutrients are transported from land to sea via SGD pathway



Philippines

Submarine Groundwater Discharge



Conclusions (modelling of variable-density flow)

- Don't use the Henry problem to test your variable-density code
- Use enough cells to model the Hydrocoin and Elder problem

For modelling 3D systems:

- Remember the Peclet discretisation limitation for cell sizes (unless you're using the method of characteristics!)
- Longitudinal dispersivity should not be too large (e.g. <10m)
- It's important to derive a very accurate density distribution (as that significantly effects the velocity field!)
- Watch out for numerical problems at the outflow face to the sea

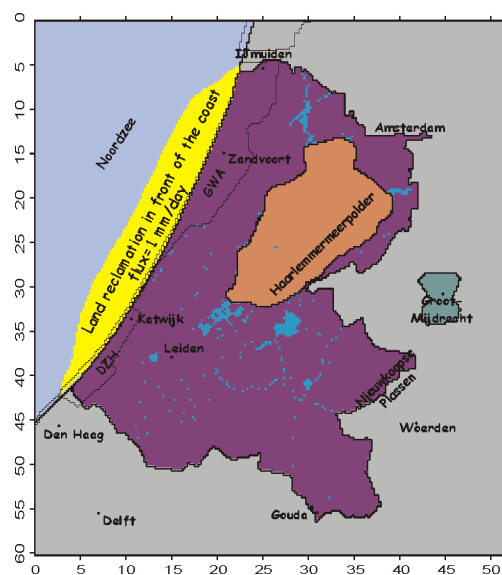
Challenges for the future

- Improve the 3D density matrix, e.g. by more types of measurements
- Implement effect of climate change and sea level rise on coastal aquifers
- Optimisation of (ground)water management in coastal aquifers by using 3D variable-density flow models
- Improve calibration of 3D models by using transient data of solute concentrations
- Incorporate reactive multicomponent solute transport

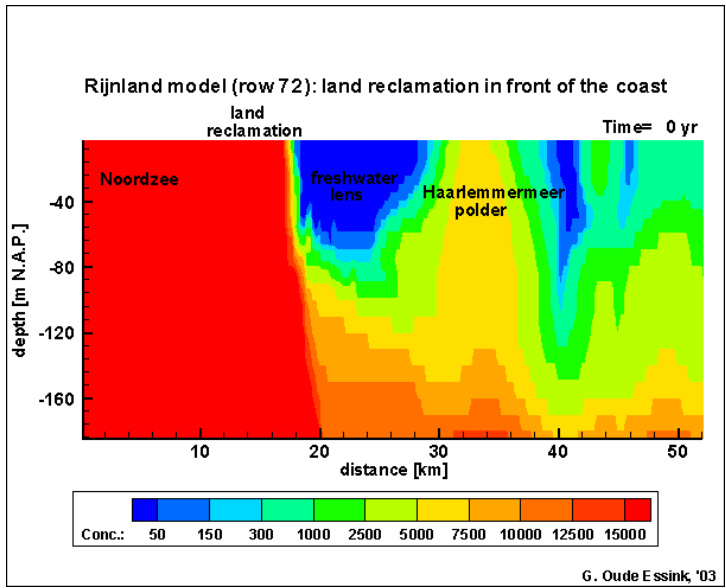
Possible measures to compensate salt water intrusion

1. Land reclamation in front of the coast
2. Inundation of low-lying polders
3. Extraction of saline/brackish groundwater
4. Infiltration of fresh surface water
5. Creating physical barriers

1. Rijnland model: land reclamation case



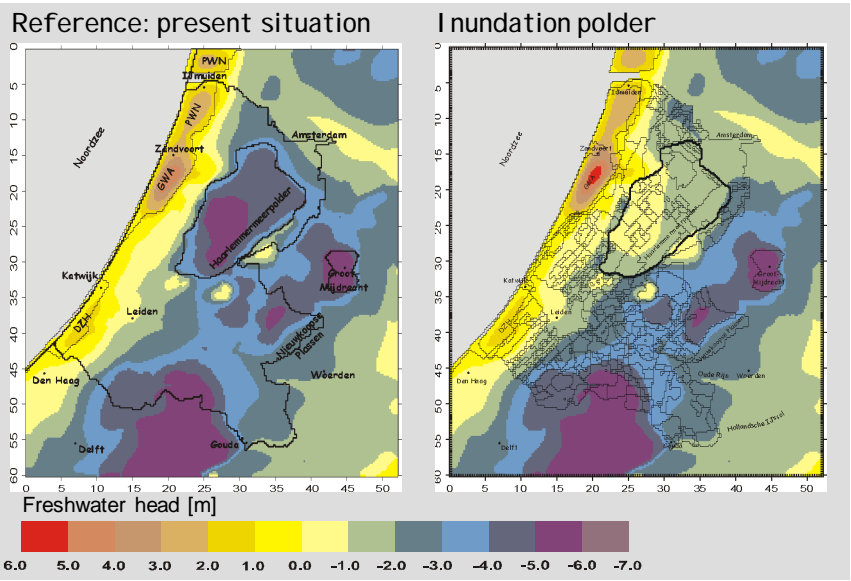
1. Land reclamation in front of the coast



2. Rijnland model: Inundation Haarlemmermeerpolder

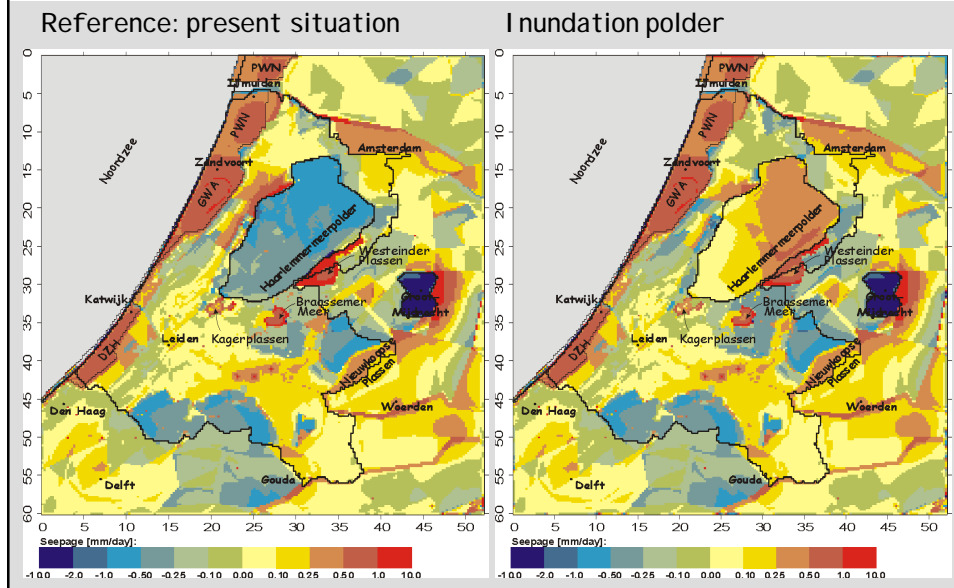
Rijnland

Calculated present phreatic water head



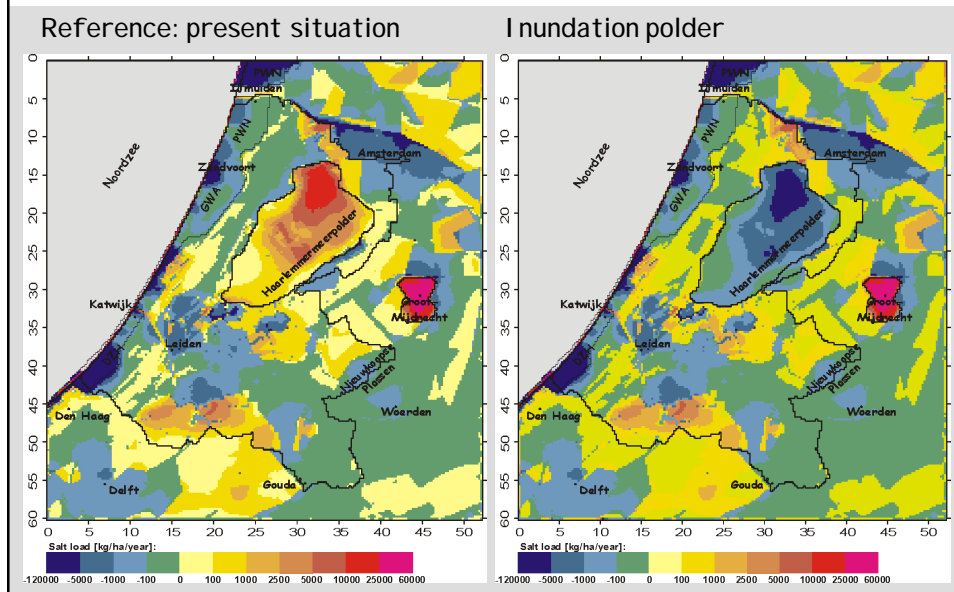
2. Rijnland model : I nundation Haarlemmermeerpolder

Calculated seepage and infiltration on -10 m M.S.L.

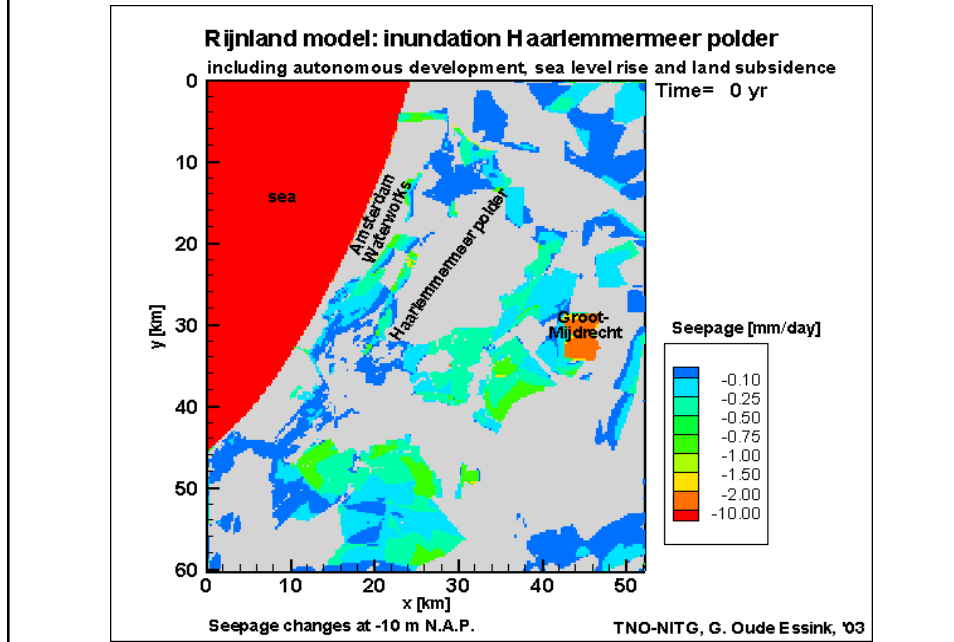


2. Rijnland model: I nundation Haarlemmermeerpolder

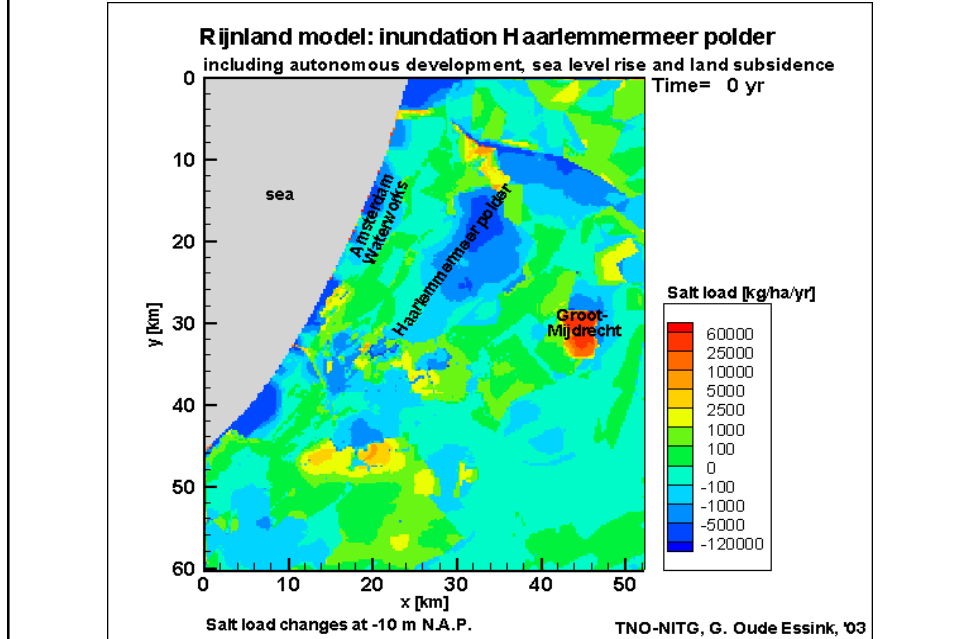
Calculated salt load on -10 m M.S.L.



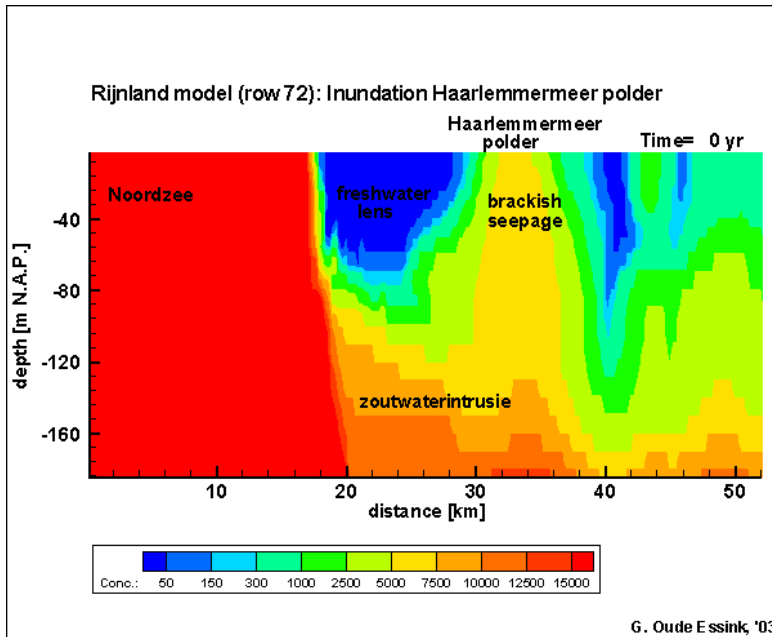
2. Rijnland model: Inundation Haarlemmermeerpolder



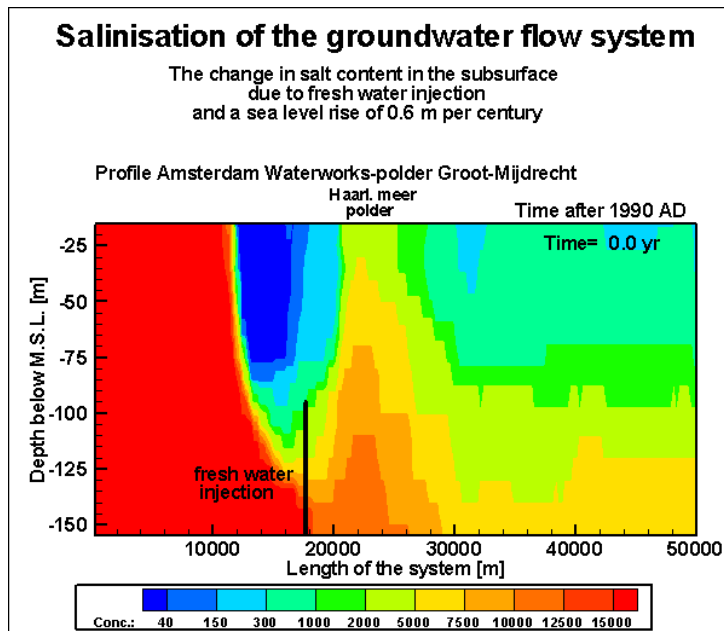
2. Rijnland model: Inundation Haarlemmermeerpolder



2. Rijnland model: Inundation Haarl.polder (conc, 500 jr)



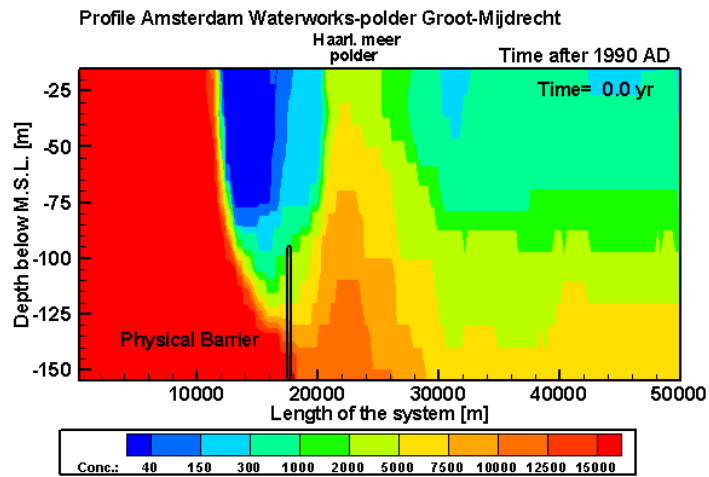
4. Injection of fresh water (conc, 1000 yr)



5. Physical barrier (conc, 1000 yr)

Salinisation of a groundwater flow system

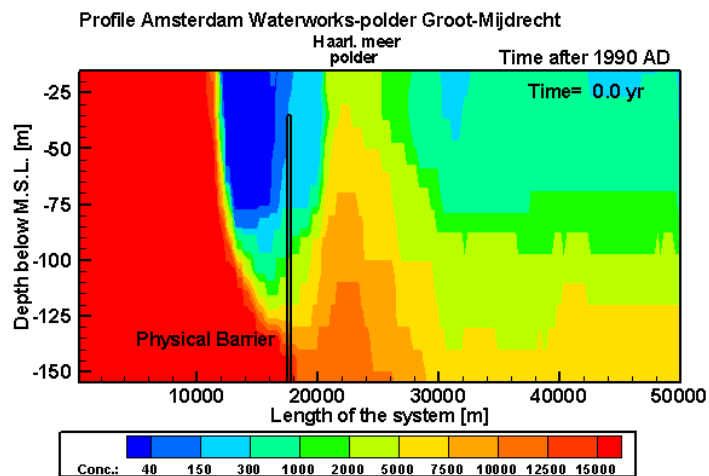
The change in salt content in the subsurface due to a physical barrier in the deep coastal aquifer and a sea level rise of 0.6 m per century

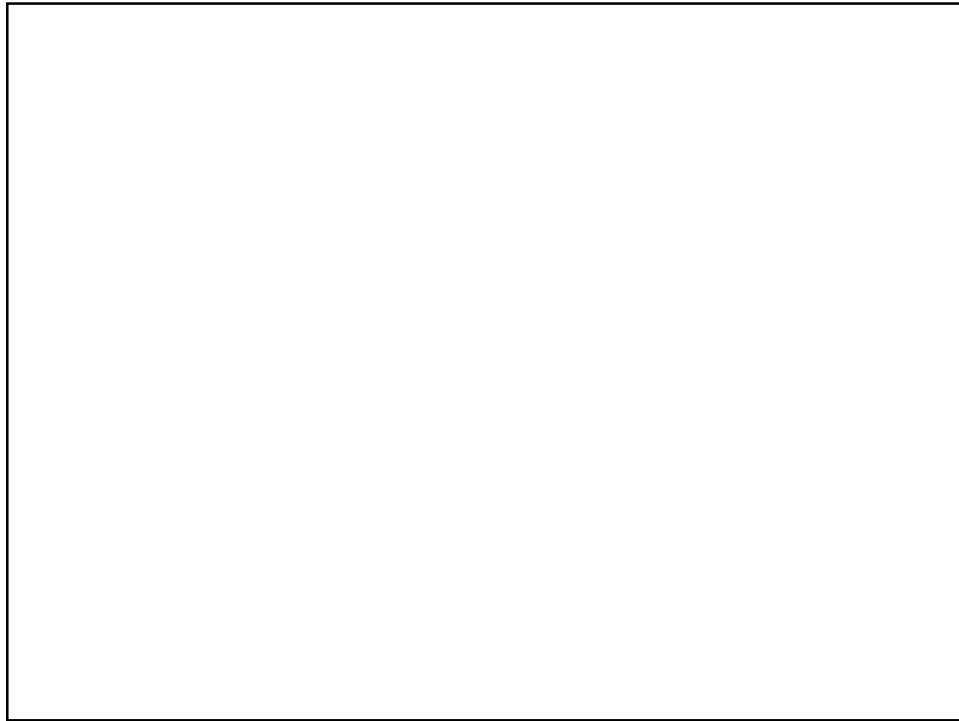


5. Physical barrier (conc, 1000 yr)

Salinisation of the groundwater flow system

The change in salt content in the subsurface due to a physical barrier in the deep coastal aquifer and a sea level rise of 0.6 m per century





modelling

Solute transport models

Combine
the groundwater flow equation
and
the advection-dispersion equation
by means of
an equation of state

Solute transport equation

Partial differential equation (PDE):

$$R_d \frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (C V_i) + \frac{(C - C^*) W}{n_e} - R_d \lambda C$$

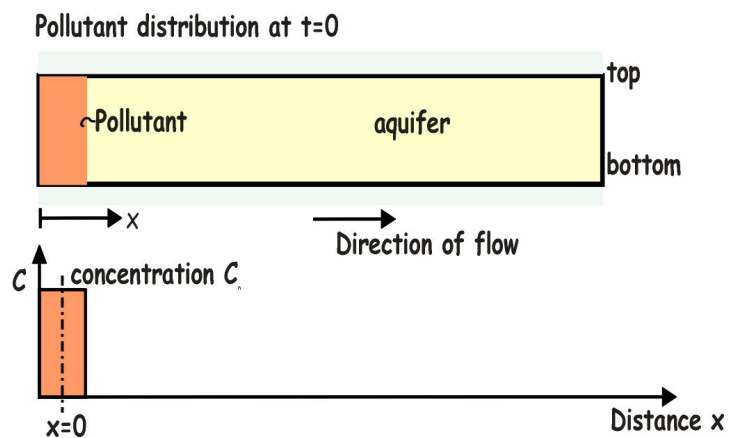
change in concentration dispersion advection source/sink decay

D_{ij} = hydrodynamic dispersion [$L^2 T^{-1}$]

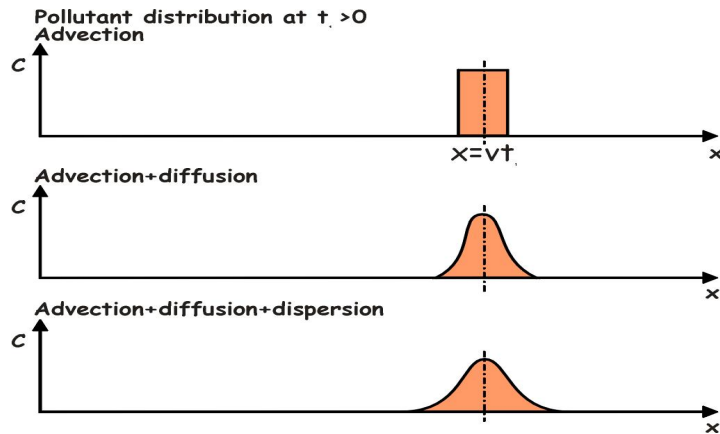
R_d = retardation factor [-]

λ = decay-term [T^{-1}]

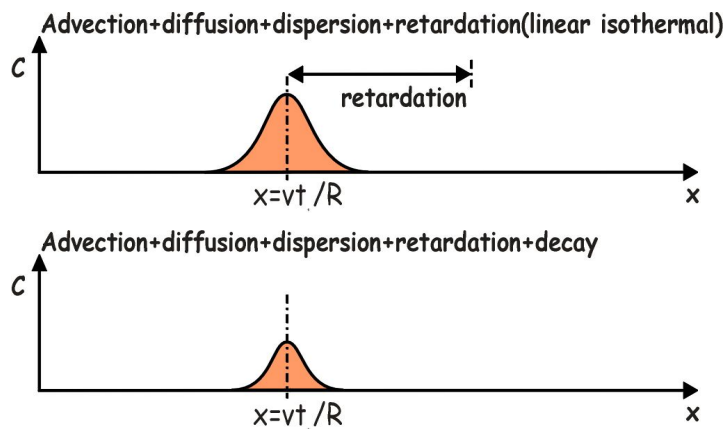
Solute transport equation: column test (I):



Solute transport equation: column test (II):



Solute transport equation: column test (III):



Hydrodynamic dispersion

$$\text{hydrodynamic dispersion} = \text{mechanical dispersion} + \text{diffusion}$$

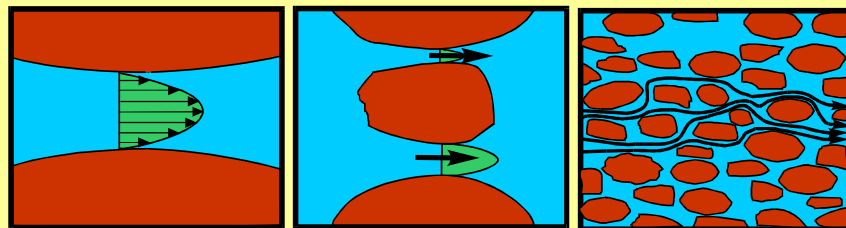
mechanical dispersion:

tensor
velocity dependant

diffusion:

molecular process
solute spread due to concentration differences

Mechanical dispersion



Differences in velocity in the pore

Differences in velocity due to variation in pore-dimension

Differences in velocity due to variation in velocity direction

Solute transport equation: diffusion (I)

diffusion is a slow process: diffusion equation

only 1D-diffusion means: $R_f=1$, $V_f=0$, $\lambda=0$ and $W=0$

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$$

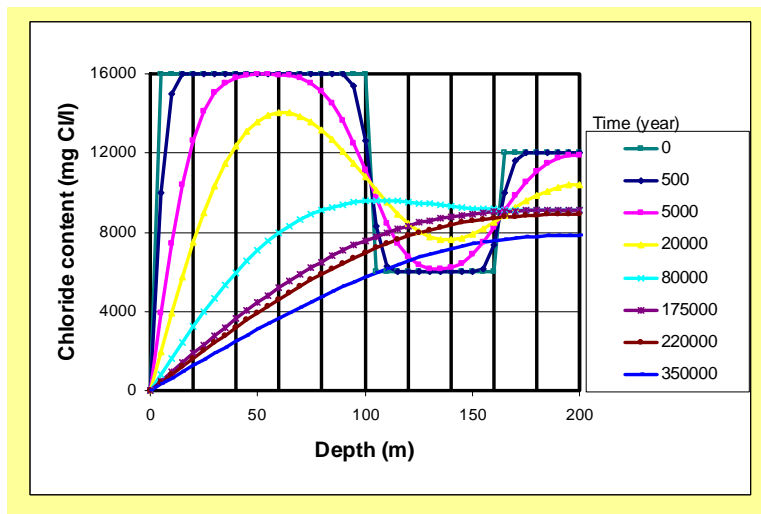
similarity with non-steady state groundwater flow equation

$$S \frac{\partial \phi}{\partial t} = T \frac{\partial^2 \phi}{\partial x^2} + N \quad \frac{T\Delta t}{S\Delta x^2} < 0.5$$

$$\phi_i^{t+\Delta t} = \phi_i^t + \frac{N\Delta t}{S} + \frac{T\Delta t}{S\Delta x^2} (\phi_{i+1}^t - 2\phi_i^t + \phi_{i-1}^t)$$

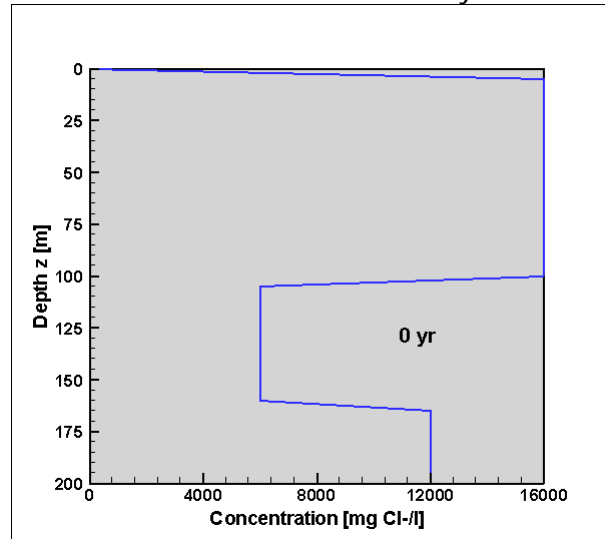
$$C_i^{t+\Delta t} = C_i^t + \frac{D\Delta t}{\Delta z^2} (C_{i+1}^t - 2C_i^t + C_{i-1}^t) \quad \frac{D\Delta t}{\Delta z^2} < 0.5$$

Solute transport equation: diffusion (II)

diffusion is a slow process: diffusion equation $\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$ 

Solute transport equation: diffusion (III)

Animation as a function of 350.000 years



Groundwater flow equation (MODFLOW, 1988)

Darcy

$$q_x = -\frac{\kappa_x \rho_f g}{\mu} \frac{\partial \phi_f}{\partial x}; \quad q_y = -\frac{\kappa_y \rho_f g}{\mu} \frac{\partial \phi_f}{\partial y}; \quad q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

Continuity

$$-\left[\frac{\partial \rho q_x}{\partial x} + \frac{\partial \rho q_y}{\partial y} + \frac{\partial \rho q_z}{\partial z} \right] = \frac{\partial n \rho}{\partial t} + W$$

Freshwater head

$$\phi_f = \frac{p}{\rho_f g} + z$$

↑
buoyancy
term

Advection-dispersion equation (MOC3D, 1996)

$$\frac{\partial C}{\partial t} = \frac{1}{nR_f} \frac{\partial}{\partial x_i} \left(nD_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{V_i}{R_f} \frac{\partial C}{\partial x_i} + \frac{\Sigma[W(C' - C)]}{nR_f} - \lambda C$$

Equation of state: relation density & concentration

$$\rho_{i,j,k} = \rho_f (1 + \beta C_{i,j,k})$$

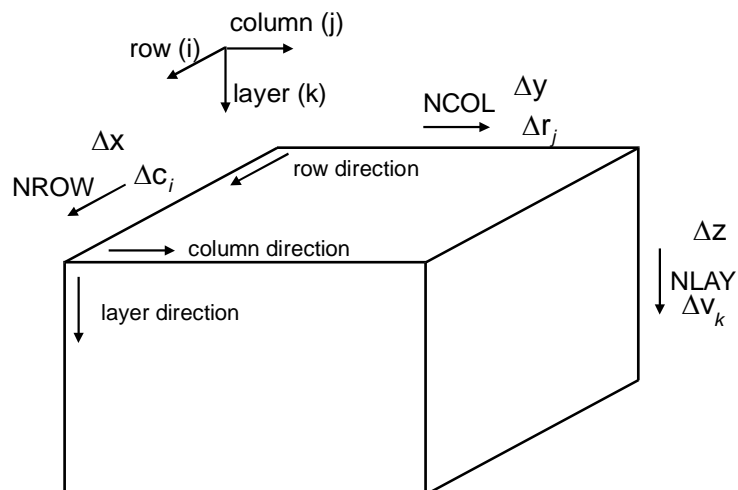
MOCDENS3D is based on MODFLOW

a modular 3D finite-difference ground-water flow model

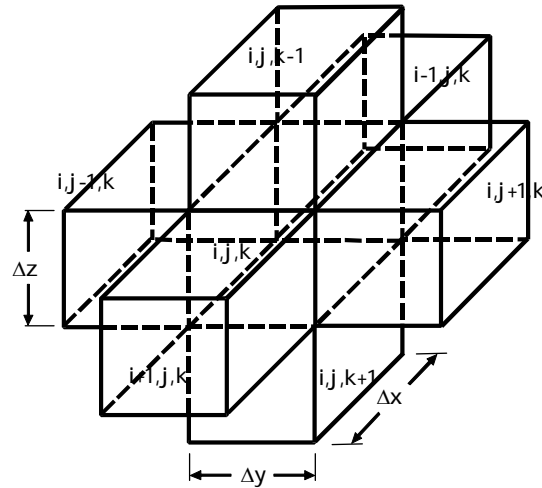
(M.G. McDonald & A.W. Harbaugh, from 1983 on)

- USGS, 'public domain'
- non steady state
- heterogeneous porous medium
- anisotropy
- coupled to reactive solute transport
 - MOC3 (Konikow *et al*, 1996)
 - MT3D, MT3DMS (Zheng, 1990)
 - RT3D
 - PHT3D (Prommer, 2004)
- easy to use due to numerous Graphical User Interfaces (GUI 's)
 - PMWIN, GMS, Visual Modflow, Argus One, Groundwater Vistas, etc.

Nomenclature MODFLOW element [i,j,k]



MODFLOW: start with water balance of one element [i,j,k]



Continuity equation (I)

In - Out = Storage

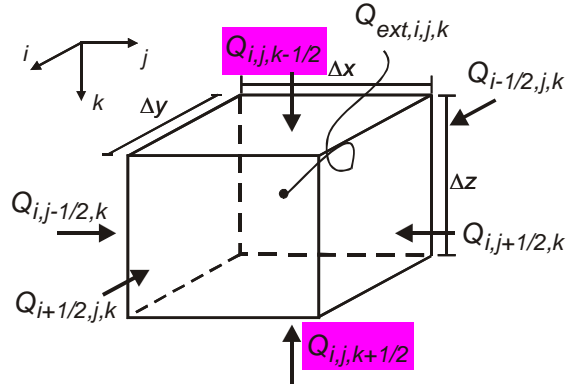
$$\frac{\partial}{\partial x} \left(k_{xx} \frac{\partial \phi}{\partial x} \right) + \frac{\partial}{\partial y} \left(k_{yy} \frac{\partial \phi}{\partial y} \right) + \frac{\partial}{\partial z} \left(k_{zz} \frac{\partial \phi}{\partial z} \right) - W = S_s \frac{\partial \phi}{\partial t}$$

$$\sum Q_i = S_s \frac{\Delta \phi}{\Delta t} \Delta V$$

Continuity equation (II)

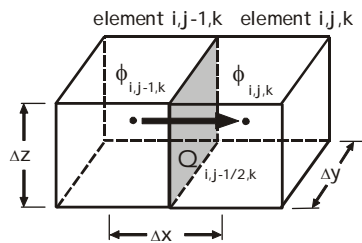
$$\sum Q_i = S_s \frac{\Delta \phi}{\Delta t} \Delta V$$

In = positive



$$\begin{aligned} & Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k} \\ &= SS_{i,j,k} \frac{\phi_{i,j,k}^t - \phi_{i,j,k}^{t+\Delta t}}{\Delta t} \Delta V \end{aligned}$$

Flow equation (Darcy's Law)



$$Q = \text{surface} * q = \text{surface} * k \frac{\partial \phi}{\partial x}$$

$$Q_{i,j-1/2,k} = k_{i,j-1/2,k} \Delta y \Delta z \frac{\phi_{i,j-1,k} - \phi_{i,j,k}}{\Delta x}$$

$$Q_{i,j-1/2,k} = CR_{i,j-1/2,k} (\phi_{i,j-1,k} - \phi_{i,j,k})$$

$$\text{where } CR_{i,j-1/2,k} = \frac{k_{i,j-1/2,k} \Delta y \Delta z}{\Delta x} \text{ is the conductance [L}^2\text{/T]}$$

Density dependent vertical flow equation

$$q_z = -\frac{\kappa_z \rho_f g}{\mu} \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$q_z = -k_z \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$Q_z = \text{surface} * q_z$$

$$= \text{surface} * k_z \left(\frac{\partial \phi_f}{\partial z} + \frac{\rho - \rho_f}{\rho_f} \right)$$

$$Q_{i,j,k-1/2} = k_{i,j,k-1/2} \Delta x \Delta y \left(\frac{\phi_{f,i,j,k-1} - \phi_{f,i,j,k}}{\Delta z} + BUOY_{i,j,k-1/2} \right)$$

$$Q_{i,j,k-1/2} = CV_{i,j,k-1/2} (\phi_{f,i,j,k-1} - \phi_{f,i,j,k} + BUOY_{i,j,k-1/2} \Delta z)$$

$$\text{where } BUOY_{i,j,k-1/2} = \left(\frac{(\rho_{i,j,k-1/2} + \rho_{i,j,k})}{2} - \rho_f \right) = \text{buoyancy term [-]}$$

$$\text{where } CV_{i,j,k-1/2} = \frac{k_{i,j,k-1/2} \Delta x \Delta y}{\Delta z} = \text{conductance [L}^2/\text{T]}$$

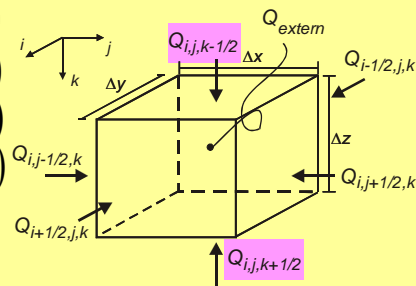
Density dependent groundwater flow equation

$$Q_{i,j-1/2,k} = CR_{i,j-1/2,k} (\phi_{f,i,j-1,k} - \phi_{f,i,j,k})$$

$$Q_{i,j+1/2,k} = CR_{i,j+1/2,k} (\phi_{f,i,j+1,k} - \phi_{f,i,j,k})$$

$$Q_{i-1/2,j,k} = CC_{i-1/2,j,k} (\phi_{f,i-1,j,k} - \phi_{f,i,j,k})$$

$$Q_{i+1/2,j,k} = CC_{i+1/2,j,k} (\phi_{f,i+1,j,k} - \phi_{f,i,j,k})$$



$$Q_{i,j,k-1/2} = CV_{i,j,k-1/2} (\phi_{f,i,j,k-1} - \phi_{f,i,j,k} + BUOY_{i,j,k-1/2} \Delta v_{k-1/2})$$

$$Q_{i,j,k+1/2} = CV_{i,j,k+1/2} (\phi_{f,i,j,k+1} - \phi_{f,i,j,k} - BUOY_{i,j,k+1/2} \Delta v_{k+1/2})$$

$$Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k}$$

$$= SS_{i,j,k} \frac{\phi_{f,i,j,k}^t - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t} \Delta V$$

The term $Q_{ext,i,j,k}$

Takes into account all external sources

Rewriting the term:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

The variable density groundwater flow equation

$$Q_{i,j-1/2,k} + Q_{i,j+1/2,k} + Q_{i-1/2,j,k} + Q_{i+1/2,j,k} + Q_{i,j,k-1/2} + Q_{i,j,k+1/2} + Q_{ext,i,j,k} \\ = SS_{i,j,k} \frac{\phi_{f,i,j,k}^t - \phi_{f,i,j,k}^{t+\Delta t}}{\Delta t} \Delta V$$

and:

$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{f,i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

gives:

$$CV_{i,j,k-1/2} \phi_{f,i,j,k-1}^{t+\Delta t} + CC_{i-1/2,j,k} \phi_{f,i-1,j,k}^{t+\Delta t} + CR_{i,j-1/2,k} \phi_{f,i,j-1,k}^{t+\Delta t} \\ + (-CV_{i,j,k-1/2} - CC_{i-1/2,j,k} - CR_{i,j-1/2,k} - CR_{i,j+1/2,k} - CC_{i+1/2,j,k} - CV_{i,j,k+1/2} + HCOF_{i,j,k}) \phi_{f,i,j,k}^{t+\Delta t} \\ + CR_{i,j+1/2,k} \phi_{f,i,j+1,k}^{t+\Delta t} + CC_{i+1/2,j,k} \phi_{f,i+1,j,k}^{t+\Delta t} + CV_{i,j,k+1/2} \phi_{f,i,j,k+1}^{t+\Delta t} = RHS_{i,j,k}$$

with:

$$HCOF_{i,j,k} = P_{i,j,k} - SC1_{i,j,k} / (\Delta t)$$

$$RHS_{i,j,k} = -Q'_{i,j,k} - SC1_{i,j,k} \phi'_{f,i,j,k} / (\Delta t)$$

$$-CV_{i,j,k-1/2} BUOY_{i,j,k-1/2} \Delta v_{k-1/2} + CV_{i,j,k+1/2} BUOY_{i,j,k+1/2} \Delta v_{k+1/2}$$

$$SC1_{i,j,k} = SS_{i,j,k} \Delta V$$

Equation of state

$$BUOY_{i,j,k-1/2} = \left(\frac{(\rho_{i,j,k-1/2} + \rho_{i,j,k})/2 - \rho_f}{\rho_f} \right)$$

$$\rho_{i,j,k} = \rho_f \left(1 + \frac{\rho_s - \rho_f}{\rho_f} \frac{C_{i,j,k}}{C_s} \right)$$

or

$$\rho_{i,j,k} = \rho_f (1 + \beta C_{i,j,k})$$

Method of Characteristics (MOC)

Solve the advection-dispersion equation (ADE)
with the Method of Characteristics

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (C V_i) + \frac{(C - C)W}{n_e}$$

Lagrangian approach:

Splitting up the advection part and the dispersion/source part:

- advection by means of a particle tracking technique
- dispersion/source by means of the finite difference method

Advantage of the MOC approach by splitting up the advection-dispersion equation

It is difficult to solve the whole advection-dispersion equation in one step, because the so-called Peclet-number is high in most groundwater flow/solute transport problems.

The Peclet number stands for the ratio between advection and dispersion

Procedure of MOC: advective transport by particle tracking

- Place a number of particles in each element
- Determine the effective velocity of each particle by (bi)linear interpolation of the velocity field which is derived from MODFLOW
- Move particles during one solute time step Δt_{solute}
- Average values of all particles in an element to one node value
- Calculate the change in concentration in all nodes due to advective transport
- Add this result to dispersive/source changes of solute transport

Steps in MOC-procedure

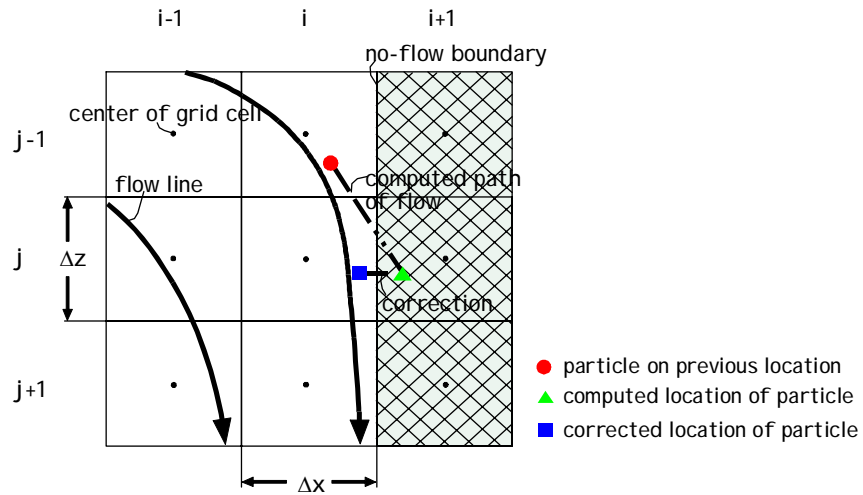
1. Determine concentration gradients at old timestep $k-1$
2. Move particles to model advective transport
3. Concentration of particles to concentration in element node
4. Determine concentration gradients on new timestep k^*
5. Determine concentration in element node after advective, dispersive/source transport on timestep k

Konikow and Bredehoeft, 1978

Causes of errors in MOC-procedure

1. Concentration gradients
2. Average from particles to node element, and visa versa
3. Concentration of sources/sinks to entire element
4. Empty elements
5. No-flow boundary: reflection in boundary

Reflection in boundary



Stability criteria (III) 3. Courant criterium

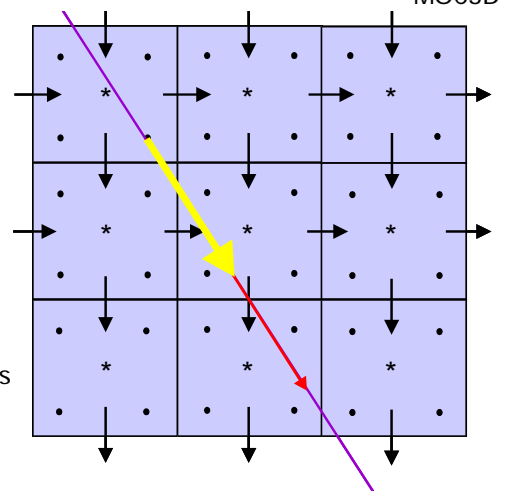
- * Node element
- Particle
- Velocity direction
- Movement particles

$$0 < \xi \leq 1$$

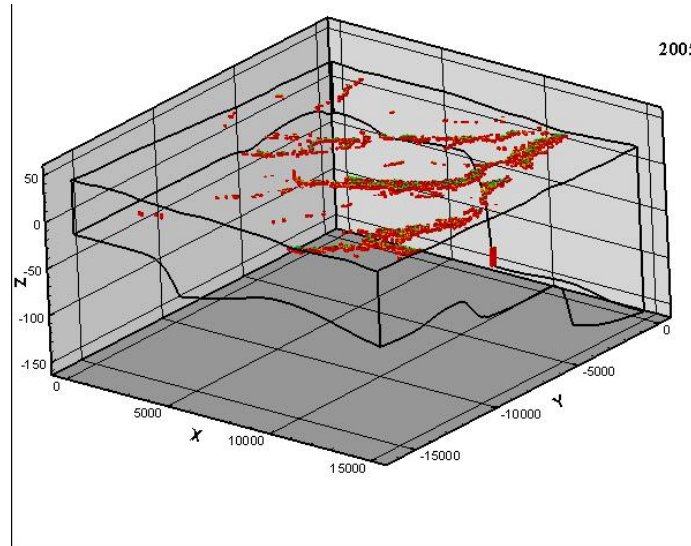
$$\Delta t_s \leq \frac{\xi \Delta x}{V_{x,\max}}$$

$$\Delta t_s \leq \frac{\xi \Delta y}{V_{y,\max}}$$

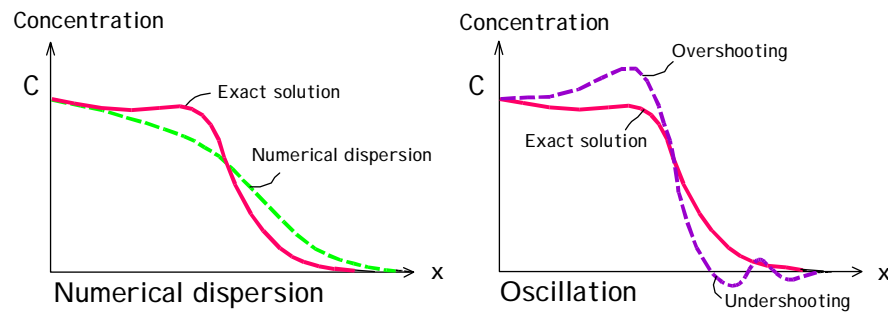
$$\Delta t_s \leq \frac{\xi \Delta z}{V_{z,\max}}$$



Courant criterion: places where timestep is smaller than 40 days



Numerical dispersion and oscillation



$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2} \quad C_i^{t+\Delta t} = C_i^t + \frac{D\Delta t}{\Delta z^2} (C_{i+1}^t - 2C_i^t + C_{i-1}^t) \quad \frac{D\Delta t}{\Delta z^2} < 0.5$$

Numerical dispersion problem (I)

To solve the advection-dispersion equation, standard finite difference and element techniques should consider the following spatial discretisation criterion:

$$\text{Peclet number } Pe \leq 2 \text{ to } 4$$

$$\text{where: } Pe = \frac{V\Delta x}{D_h}$$

V = effective velocity [L/T]

Δx = dimension grid cell [L]

D_h = hydrodynamic dispersion [L²/T]

Numerical dispersion problem (II)

For advection dominant groundwater flow, the Peclet number can be rewritten as:

$$\Delta x \leq 2\alpha_L \text{ to } 4\alpha_L$$

where α_L = longitudinal dispersivity [L]

What does that mean?

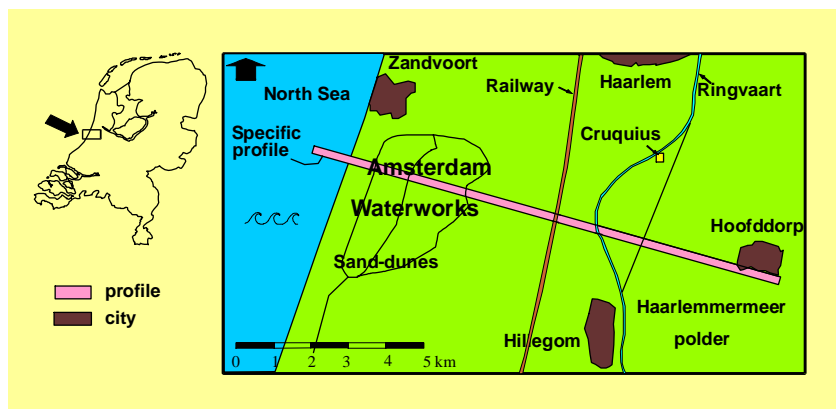
If α_L is small, then Δx should be small too!!

Numerical dispersion problem (III)

Now follows an transient salt water intrusion case to demonstrate why in many coastal aquifers the longitudinal dispersivity α_L [L] should be small

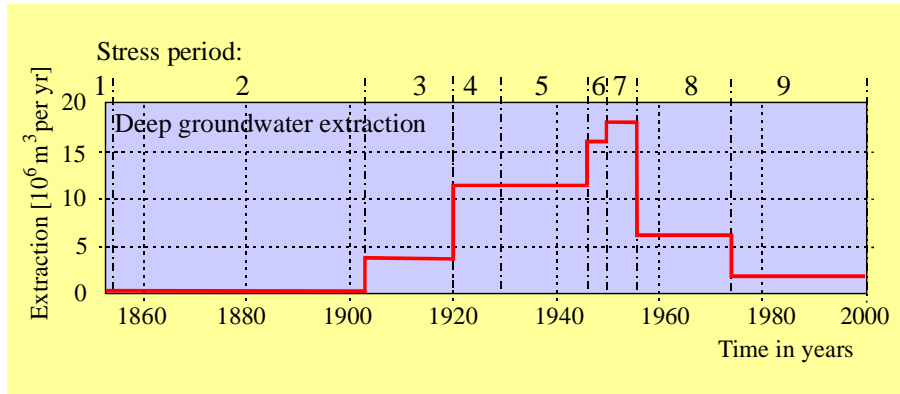
Effect of α_L on the salinisation of the aquifer (I)

Position profile through Amsterdam Waterworks, Rijnland polders and Haarlemmeer polder



Effect of α_L on the salinisation of the aquifer (II)

Grondwater extractions out of the middle aquifer in the sand-dune area of Amsterdam Waterworks

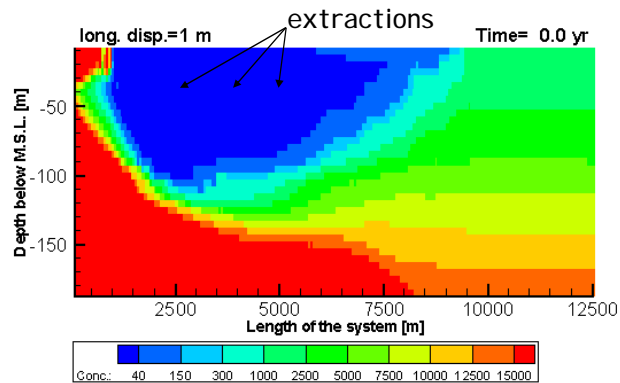


Effect of α_L on the salinisation of the aquifer (III)

$\alpha_L = 1 \text{ m}$

Initial situation: 154 years ago

Profile Amsterdam Waterworks-Haarlemmermeerpolder

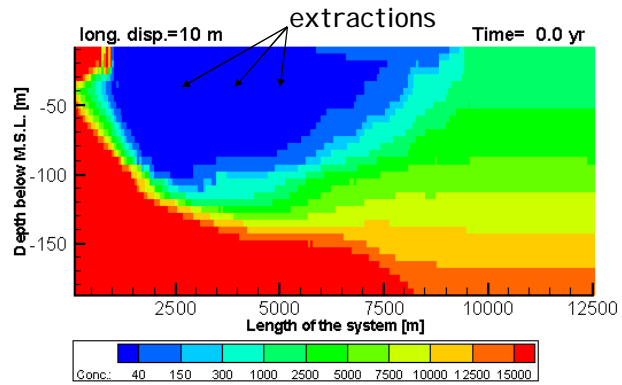


Effect of α_L on the salinisation of the aquifer (IV)

$\alpha_L = 10$ m

Initial situation: 154 years ago

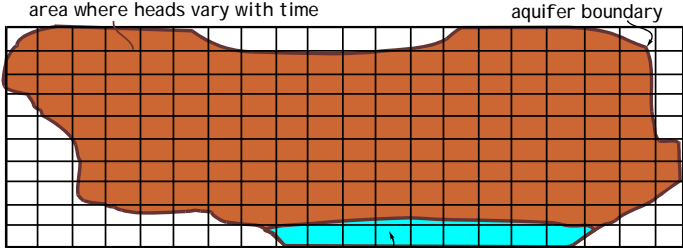
Profile Amsterdam Waterworks-Haarlemmemeerpolder



MODFLOW

Boundary conditions in MODFLOW (I)

Example of a system with three types of boundary conditions



Numeric model

0	1	1	1	1	1	0	0	0	0	0	0	0	1	1	1	1	1	0	0	
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	0	0	0	0	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	0	0	0	

Boundary conditions in MODFLOW (II)

- For a constant head condition: IBOUND<0
- For a no flow condition: IBOUND=0
- For a variable head: IBOUND>0

Packages in MODFLOW

1. Well package
2. River package
3. Recharge package
4. Drain package
5. Evaporation package
6. General head package

1. Well package

$$Q_{well} = Q_{i,j,k}$$

Example: an extraction of 10 m³ per day should be inserted
in an element as:

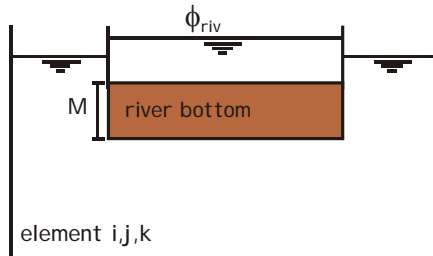
$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

$$Q_{ext,i,j,k} = -10 \quad (\text{in} = \text{positive})$$

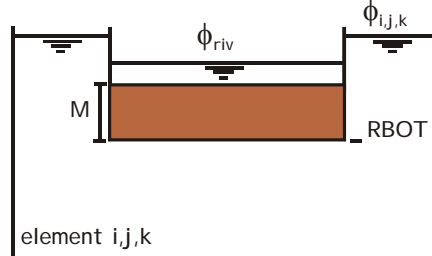
$$Q'_{i,j,k} = -10$$

2. River package (I)

river loses water



river gains water



$$Q_{riv} = KLW \left(\frac{\phi_{riv} - \phi_{i,j,k}}{M} \right)$$

$$Q_{riv} = \frac{KLW}{M} (\phi_{riv} - \phi_{i,j,k}) \Leftrightarrow Q_{riv} = C_{riv} (\phi_{riv} - \phi_{i,j,k})$$

2. River package (II)

$$Q_{riv} = C_{riv} (\phi_{riv} - \phi_{i,j,k})$$

Example: the river conductance C_{riv} is 20 m²/day and the river level=3 m, than this package should be inserted in an element as:

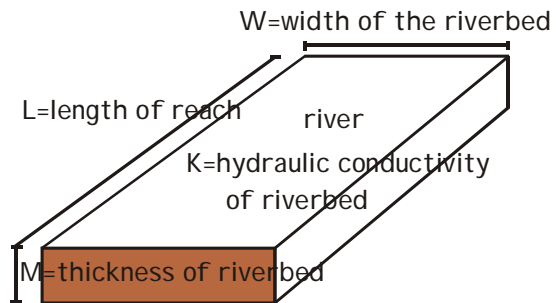
$$Q_{ext,i,j,k} = P_{i,j,k} \phi_{i,j,k}^{t+\Delta t} + Q'_{i,j,k}$$

$$Q_{ext,i,j,k} = 20(3 - \phi_{i,j,k})$$

$$Q'_{i,j,k} = 60 \quad \text{and} \quad P_{i,j,k} = -20$$

2. River package (III)

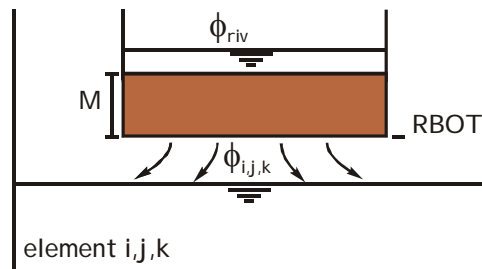
Determine the conductance of the river in one element:



where $C_{riv} = \frac{KLW}{M}$ is the
conductance [L^2/T] of the river

2. River package (IV)

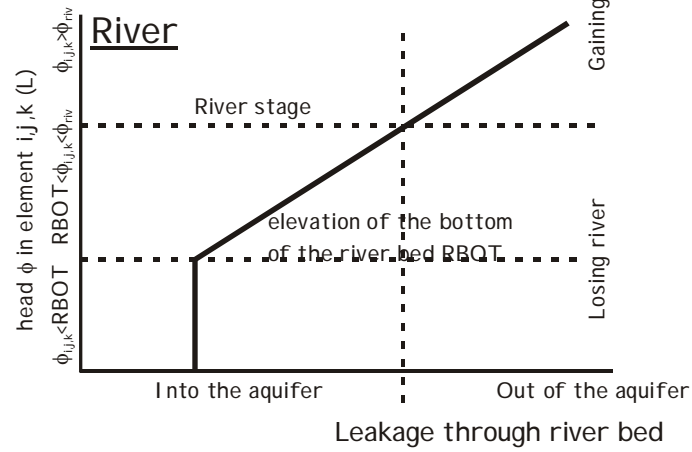
Leakage to the groundwater system



Special case:

if $\phi_{i,j,k} < RBOT$, then $Q_{riv} = C_{riv}(\phi_{riv} - RBOT)$

2. River package (V)



3. Recharge package

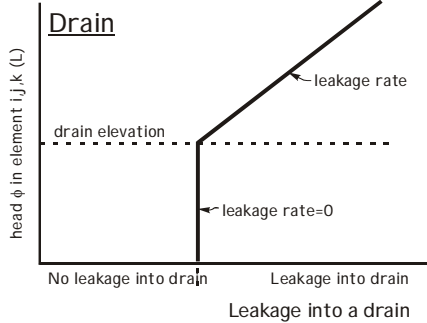
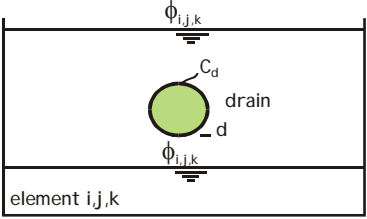
$$Q_{rec} = I\Delta x\Delta y$$

4. Drain package

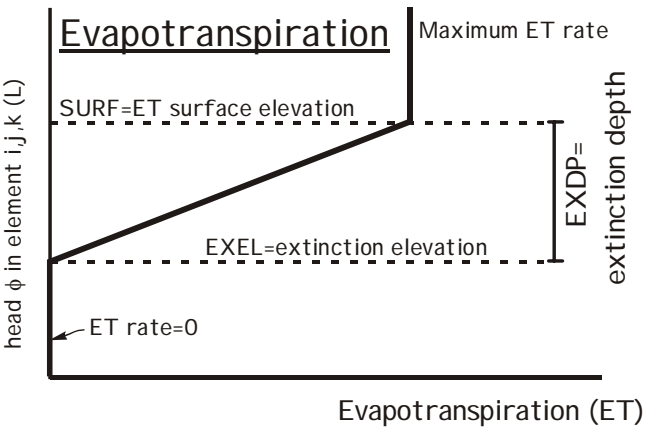
$$Q_{dm} = C_{dm} (\phi_{i,j,k} - d)$$

Special case:

if $\phi_{i,j,k} < d$ than $Q_{dm} = 0$

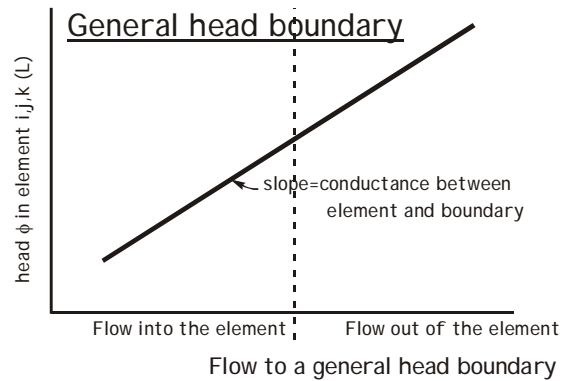
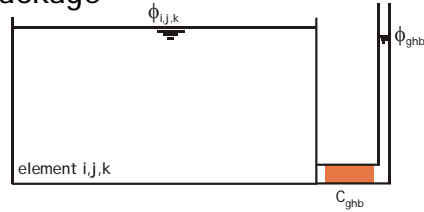


5. Evapotranspiration package



6. General head boundary package

$$Q_{ghb} = C_{ghb} (\phi_{ghb} - \phi_{i,j,k})$$

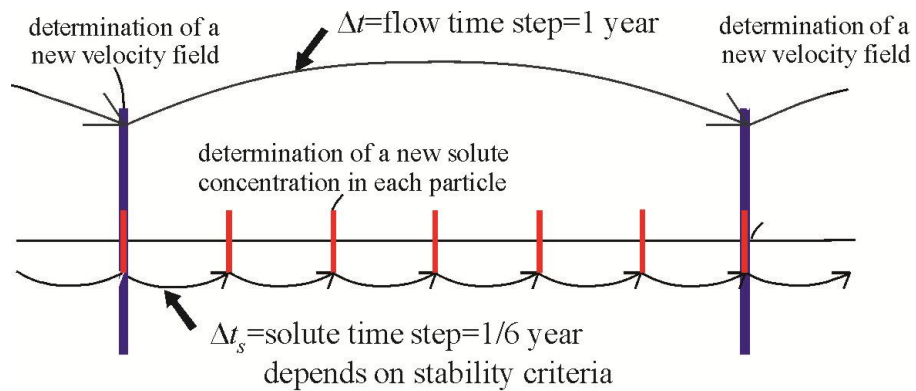


- 1 (name).bas-file
- 2 (name).bcf-file
- 3 (name).moc-file
- 4 (name).wel-file
- 5 (name).riv-file
- 6 (name).drn-file
- 7 (name).ghb-file
- 8 (name).sip-file
- 9 densin.dat-file
- 10 (name).nam-files

Time indication MODFLOW

ITMUNI=1: seconde
ITMUNI=2: minute
ITMUNI=3: hour
ITMUNI=4: day
ITMUNI=5: year

Flow time step and solute time step



- * velocity field remains constant during 1 year
- * solute concentration changes during each solute time step

