

BET - BOREHOLE EROSION TEST

Procedure, Equipment, Data Reduction and Some Test Results

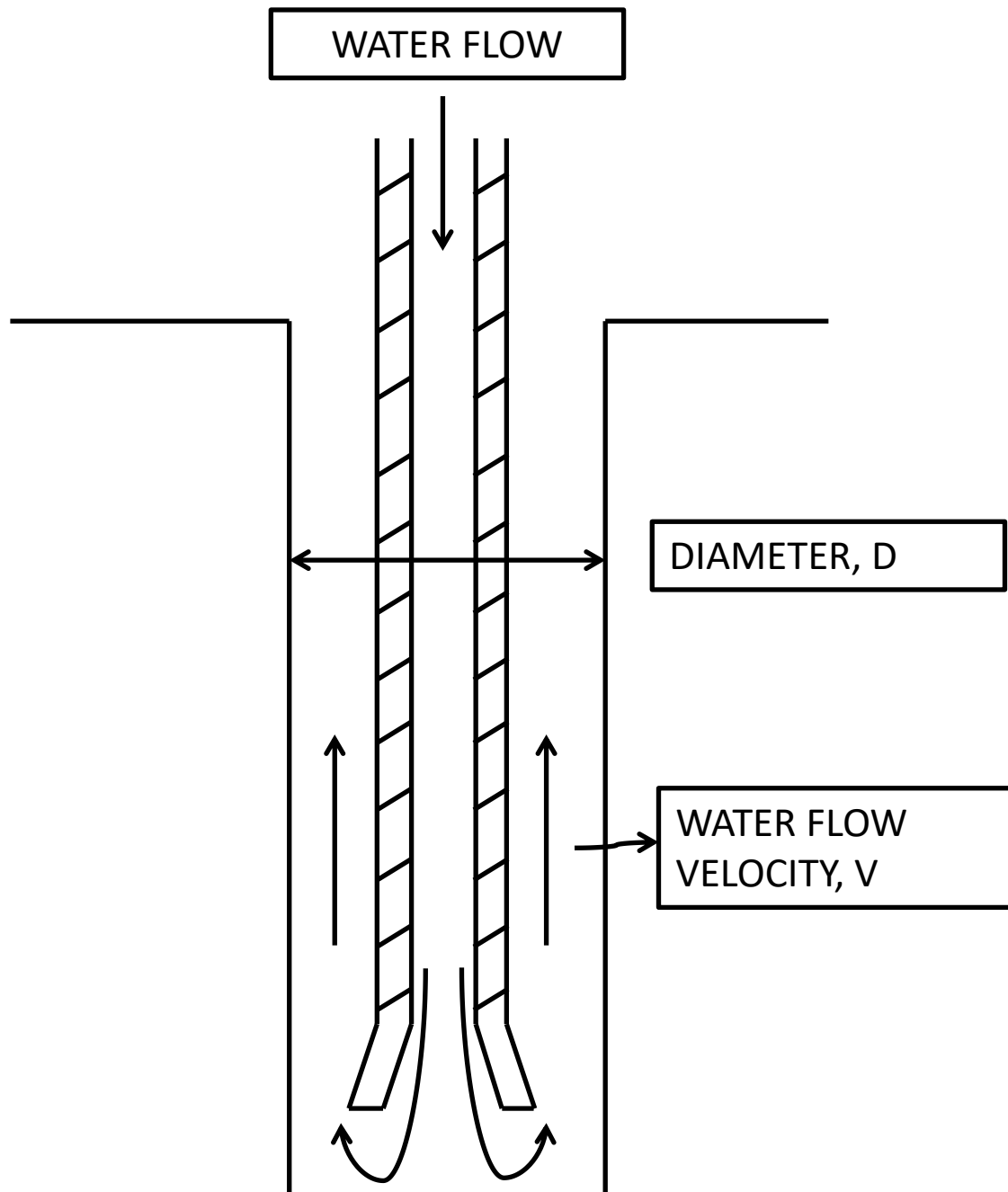
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President of ISSMGE (2009-2013)
President of ASCE (2020-2021)**



BOREHOLE EROSION TEST

- Invented in 2014
- Briaud J.-L., Chedid M., Chen H.C., Shidlovskaya A., 2017, “The Borehole Erosion Test”, Journal of Geotechnical and Geoenvironmental Engineering, Vol 143, Issue 8, ASCE.
- Shidlovskaya A., Bahmani, Briaud J.-L., Chen H.-C., 2023, “Improvements in Test Procedure And Data Reduction For The Borehole Erosion Test”, Geotechnical Testing Journal Vol. 46, No. 2 (March/April 2023): 295–315, ASTM.







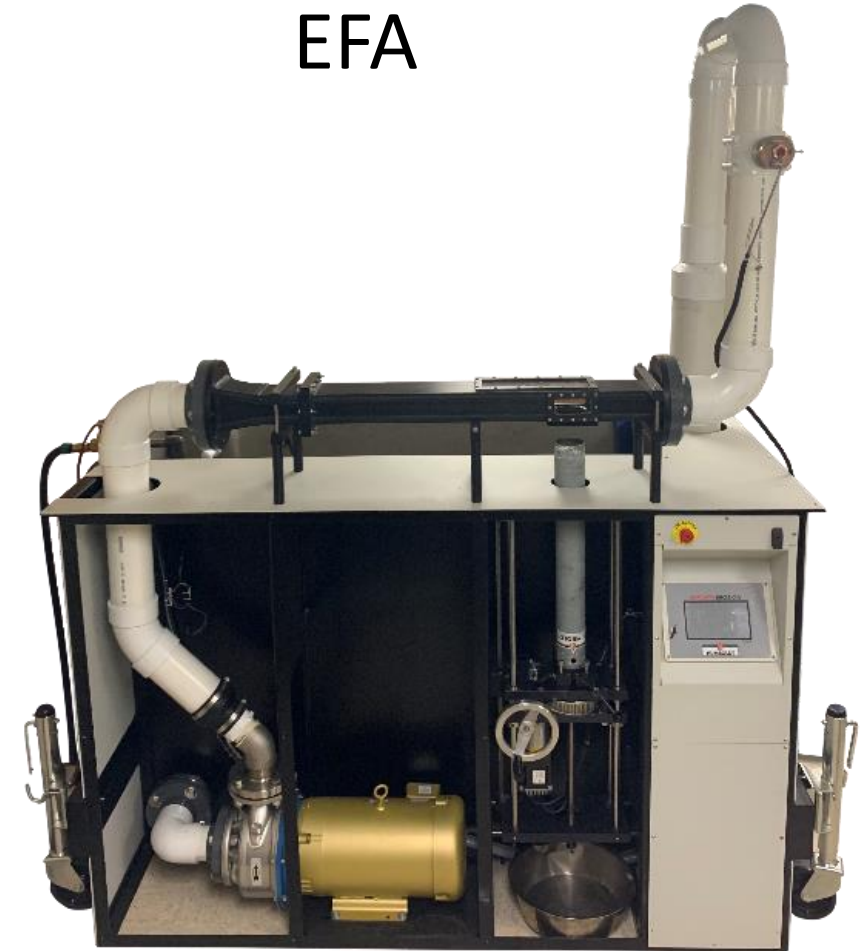
BET



PET



EFA



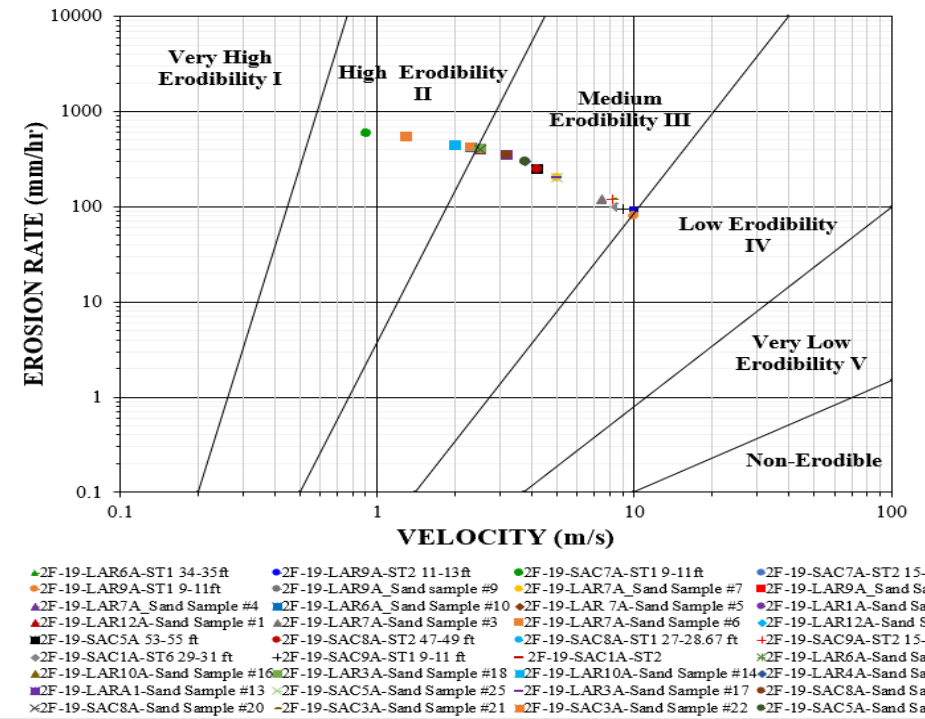
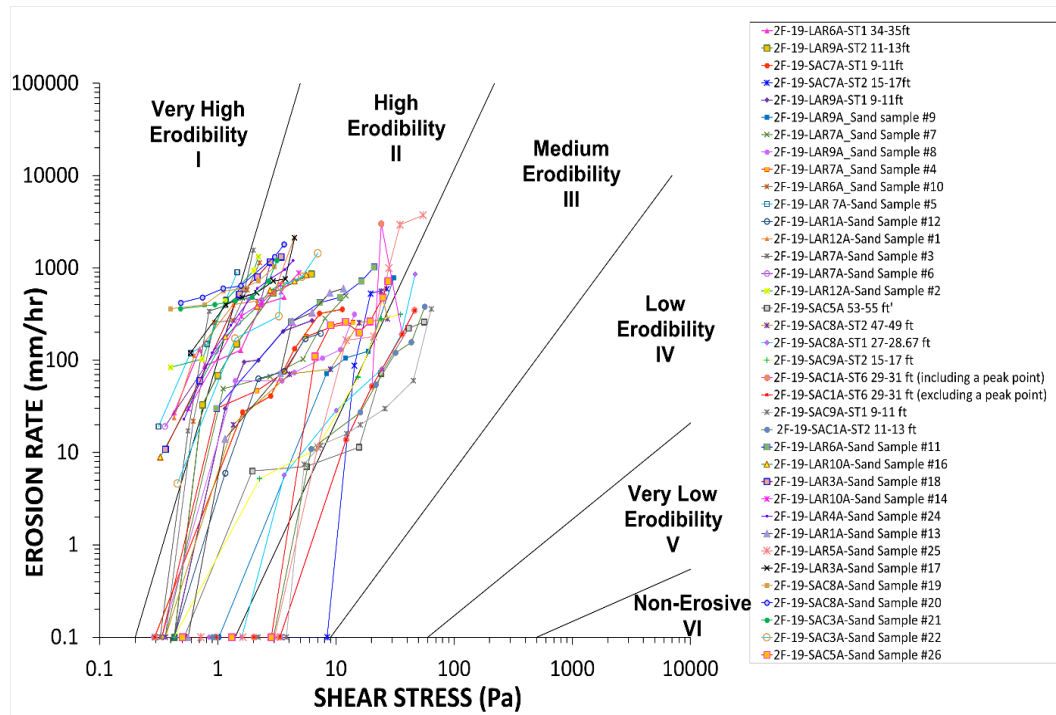
TESTING PROCEDURE

1. Drill a borehole ($OD_{rod} < 0.75 \times OD_{drill\ bit}$)
2. Remove the drilling equipment
3. Insert a mechanical caliper to the bottom of the hole.
4. Pull the caliper up the hole recording the borehole diameter (repeat this process) – **BOREHOLE DIAMETER PROFILE BEFORE FLOW**
5. Insert the drilling rods (no bit) and start the flow at a chosen velocity
6. Maintain the flow for 10 minutes at least and record the flow as a function of time.
7. Remove the drilling rods
8. Insert the caliper and repeat step 4. **BOREHOLE DIAMETER PROFILE AFTER FLOW**
9. Repeat steps 5 to 8 at different velocities as desired
10. Reduce the data

EFA



PET



Getting the BET shear stress

The hydraulic shear stress at the water soil interface (Munson, 2005):

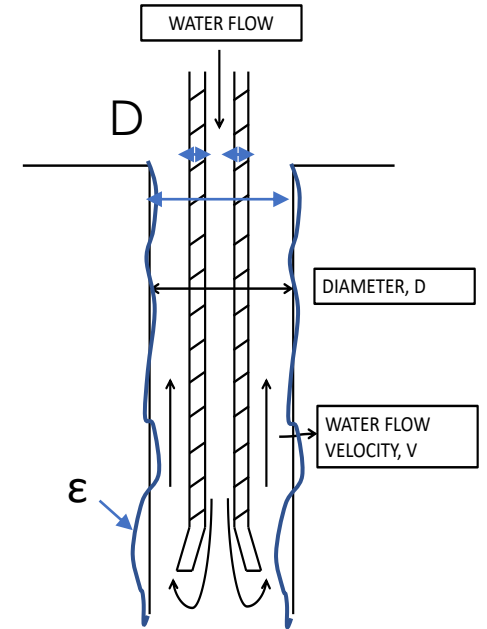
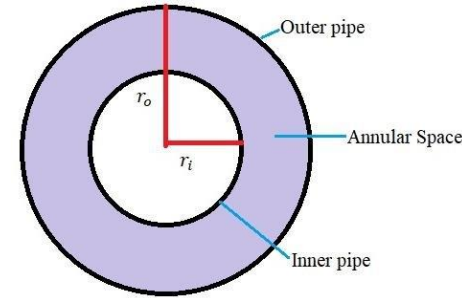
$$\tau = \frac{1}{8} f \rho V^2$$

f = friction factor, depends on ϵ/D_h and Reynolds number Re
 ρ = density of water
 V = mean flow velocity (m/s)

Step a. Obtain Reynolds number Re :

$$Re = \frac{VD_h}{\nu}$$

ν = kinematic viscosity of a fluid, $10^{-6} \text{ m}^2/\text{s}$ at 20°C
 D_h = hydraulic diameter of the annulus space between the rods and the borehole wall



Step b. Calculate hydraulic diameter D_h of the annulus space:

$$D_h = \frac{4 \text{ cross sectional area of flow}}{\text{wetted perimeter}} = D_o - D_i$$

D_o = outer diameter (borehole)
 D_i = inner diameter (rods)

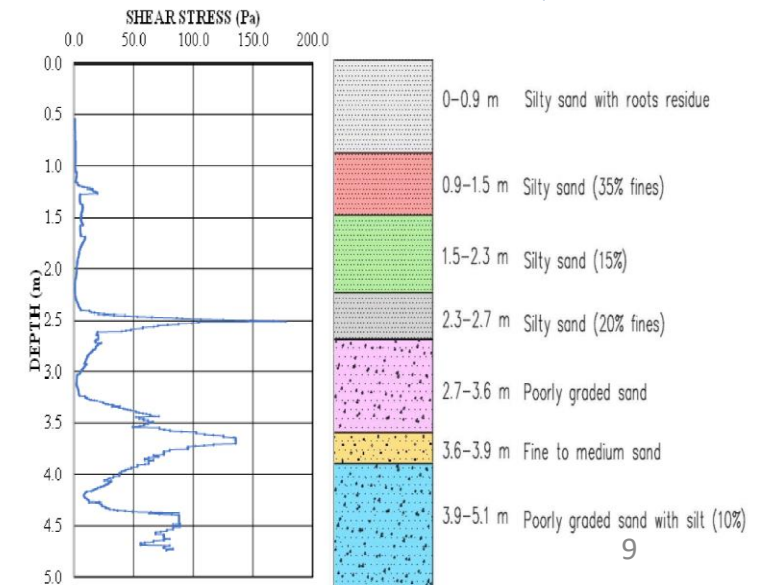
Step c. Obtain friction factor for the circular pipe (Moody chart):

$$\frac{1}{\sqrt{f}} = -1.8 \log \left[\left(\frac{\epsilon/D_h}{3.7} \right)^{1.11} + \frac{6.9}{Re} \right]$$

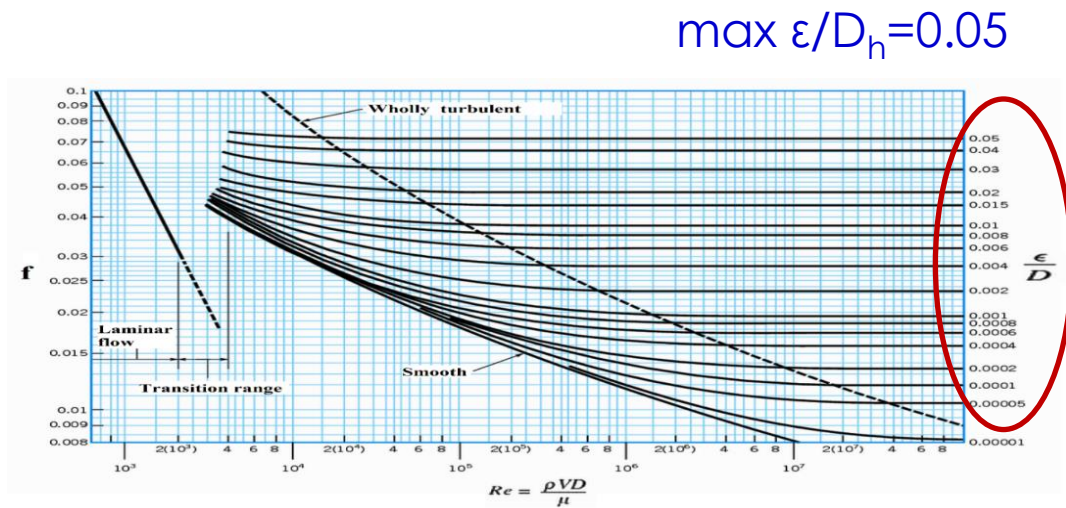
(Haaland, 1983) ϵ = roughness depth
 ϵ/D_h = relative roughness

Step d. Correct friction factor

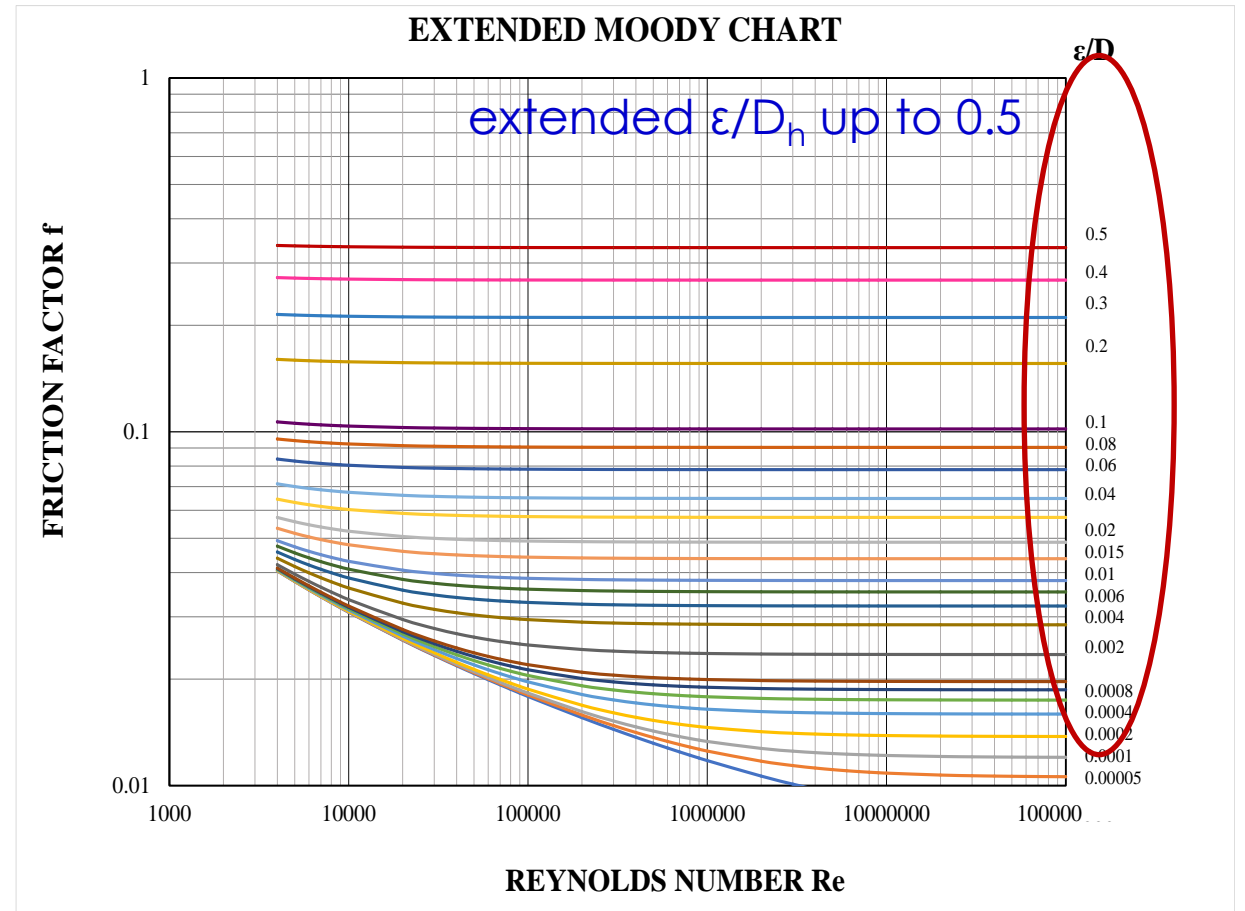
$$f_{annulus} = 1.5 f_{pipe} \text{ (Munson, 2009)}$$



Extend Moody chart to very rough surfaces (for relative roughness $\epsilon/D > 0.05$).



Moody chart (1944) for rough pipes



Extended Moody chart (Moody 1944; modified by Briaud and Shidlovskaya 2019) for very rough soil surfaces

Detailed data reduction procedure for the BET.

1. Input the field data which includes the site location, the site elevation, the borehole number, the depths at which the caliper reading are taken, the corresponding borehole diameter (caliper reading), the flow rate as a function of time, the time duration of the flow, and the outside radius of the rods.
2. Calculate the average radius versus depth profile for the borehole before any flow takes place. This requires making an average at any depth of the caliper diameter measurements recorded right after drilling the borehole. The radius is used because the erosion rate is the increase in radius divided by the elapsed time of flow. Indeed, several caliper diameter profiles are often recorded in the same borehole.
3. Calculate the average radius versus depth profile for the borehole after the first 10 minutes of flow. This requires making an average at any depth of the caliper diameter measurements recorded right after the 10 minutes of flow. Indeed, several caliper diameter profiles are often recorded in the same borehole.
4. Calculate the difference in radius between the profiles of step 1 and step 2 and record it as the radial erosion increment as a function of depth.
5. Calculate the erosion rate at any depth by dividing the radial erosion increment by the duration of the flow (~10 minutes). This gives the erosion rate profile for the first flow velocity.
6. Repeat steps 2 to 5 for the other chosen flow rates.
7. During the first flow rate application, the flow rate varies somewhat, and an average value must be calculated. Calculate the average flow rate for the duration of the flow (~10 minutes).
8. Repeat step 7 for all flow rates applied during the BET.
9. For each one of the flow rates, calculate the associated velocity by dividing the flow rate by the area available for the water to flow. This area varies with depth and is taken as the area of the annulus between the outside diameter of the rods and the diameter of the borehole at that depth. The diameter of the borehole at a given depth during the 10 minutes of flow is taken as the average of the annulus area before the flow start and after the flow stops. This step gives the velocity profile for the first average flow rate.

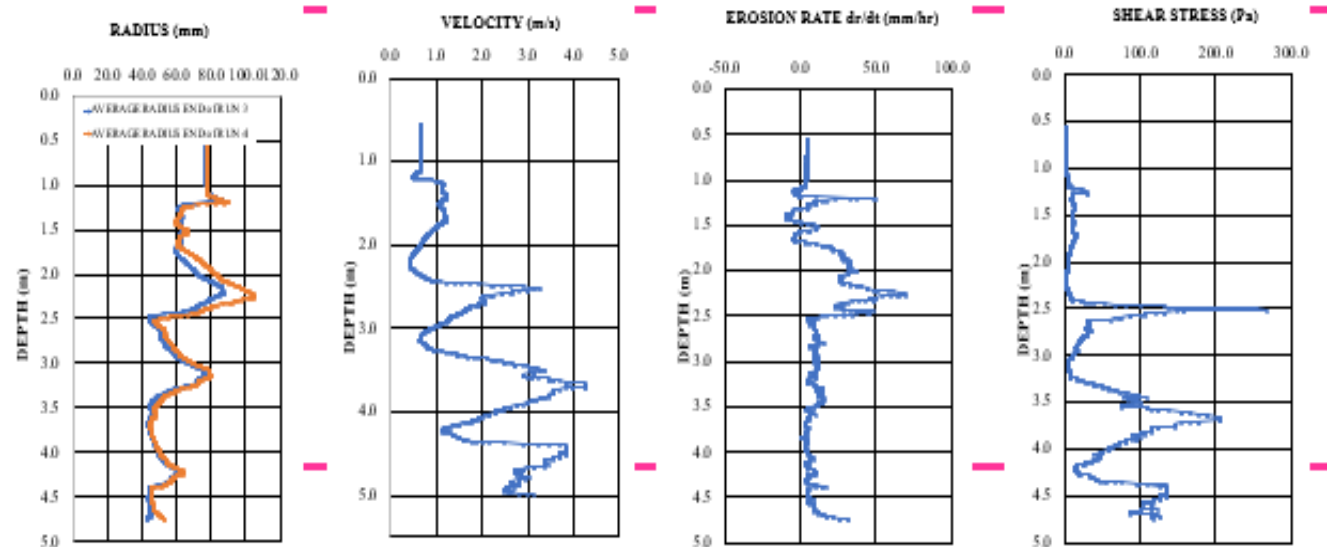
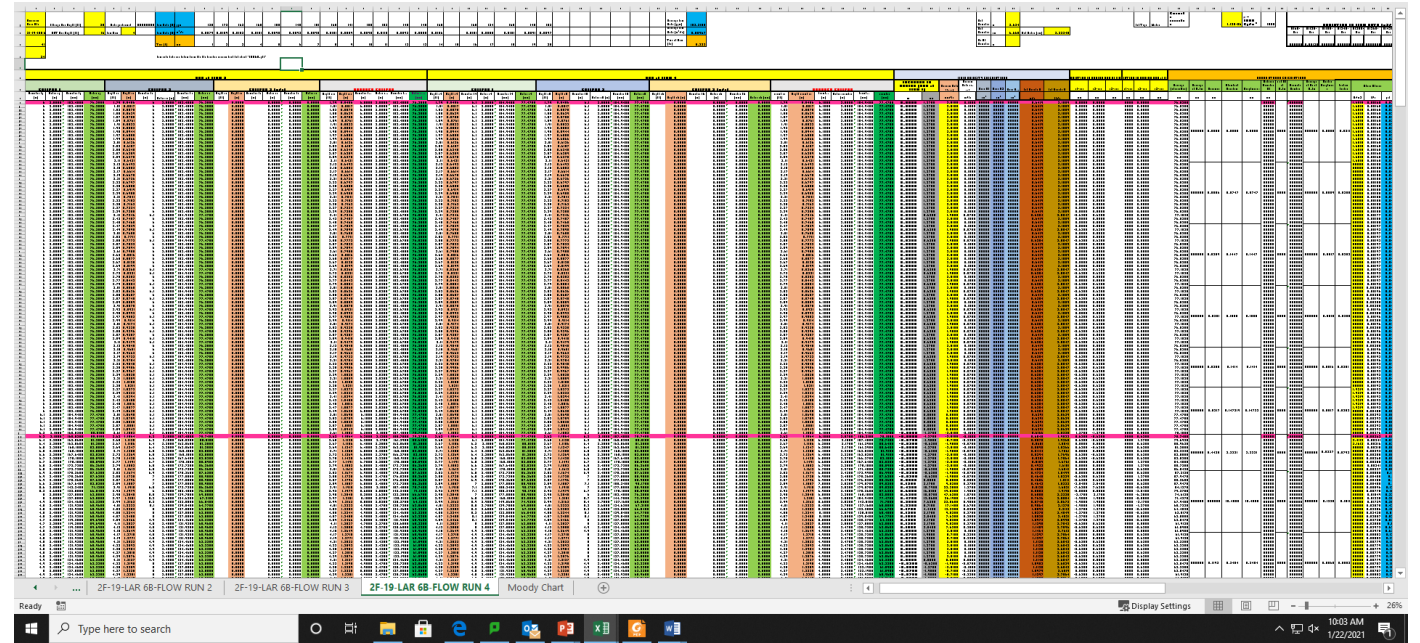
$$v = \frac{4Q}{\pi(R_{\text{borehole}}^2 - R_{\text{rod}}^2)}$$

10. Repeat step 9 for all other flow rates.
11. Calculate the shear stress associated with the velocity as described in the following steps.
12. The equation to go from the velocity to the shear stress is $\tau = \frac{1}{2}f\rho v^2$ (Munson, 2009) where τ is the hydraulic shear stress at the water soil interface, f is the friction factor, ρ is the density of water (1000 kg/m^3), and v is the mean flow velocity (m/s). The friction factor f depends on the interface relative roughness ϵ/D , and the Reynolds Number Re . The roughness ϵ is the mean depth of the asperities along the borehole wall. Note that the roughness of the outside wall of the pipe is much smoother and so would the associated shear stress but since the quantity of interest is the shear stress on the soil surface, the roughness of the soil surface is the one used here. The parameter D_0 is the hydraulic diameter associated with the annulus between the outside diameter of the rods and the diameter of the borehole. The Reynolds Number Re is $Re = \frac{VD_0}{\nu}$ where V is the velocity, D_0 is the hydraulic diameter of the annulus space between the rods and the wall of the borehole and ν is the kinematic viscosity of water ($10^{-6} \text{ m}^2/\text{s}$ at 20°C). The parameter D_0 for an annulus is given by $D_0 = D_o - D_i$ where D_o is the outside diameter and D_i the inside diameter. At any depth, the outside diameter D_o is taken as the average of 2 times the borehole radius before the flow and 2 times the borehole radius after the flow. The inside diameter D_i is equal to 2 times the outside radius of the rods.

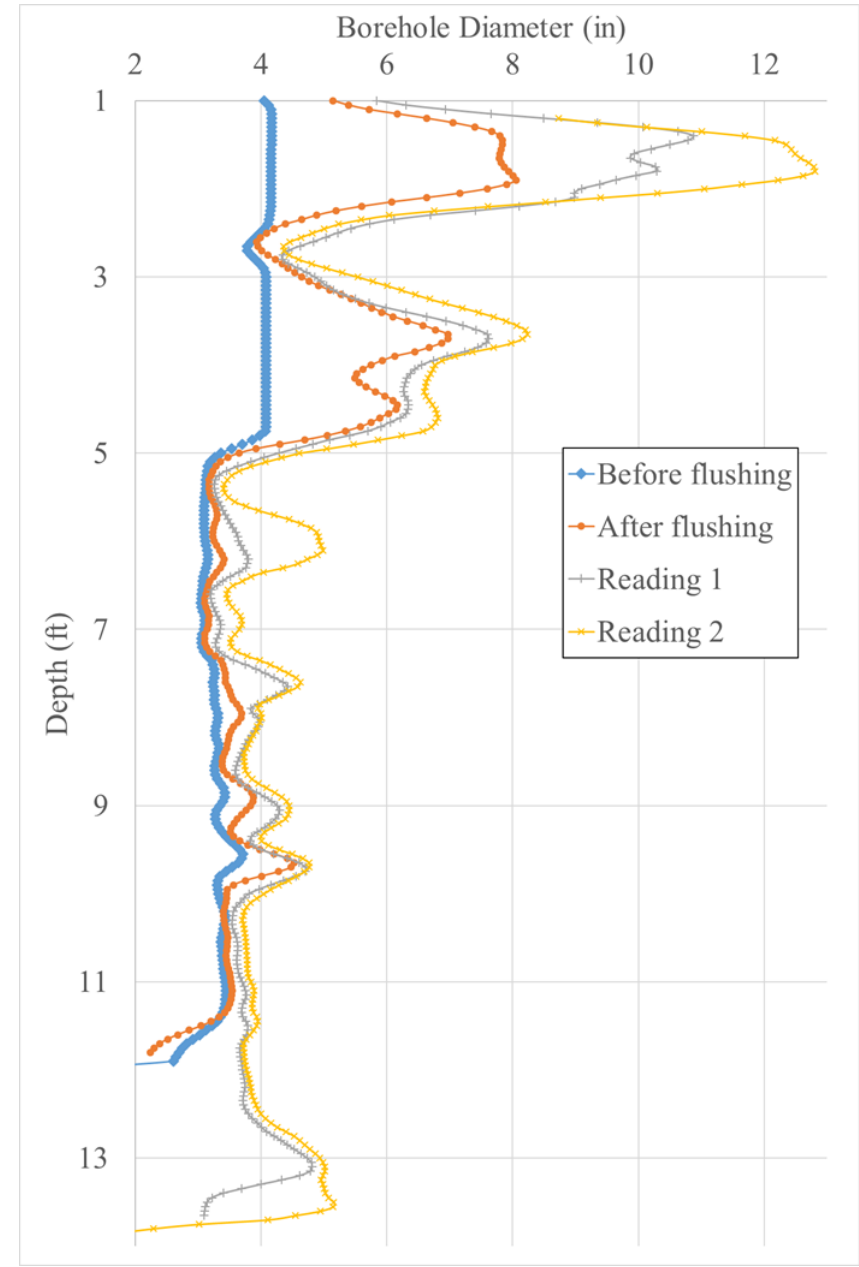
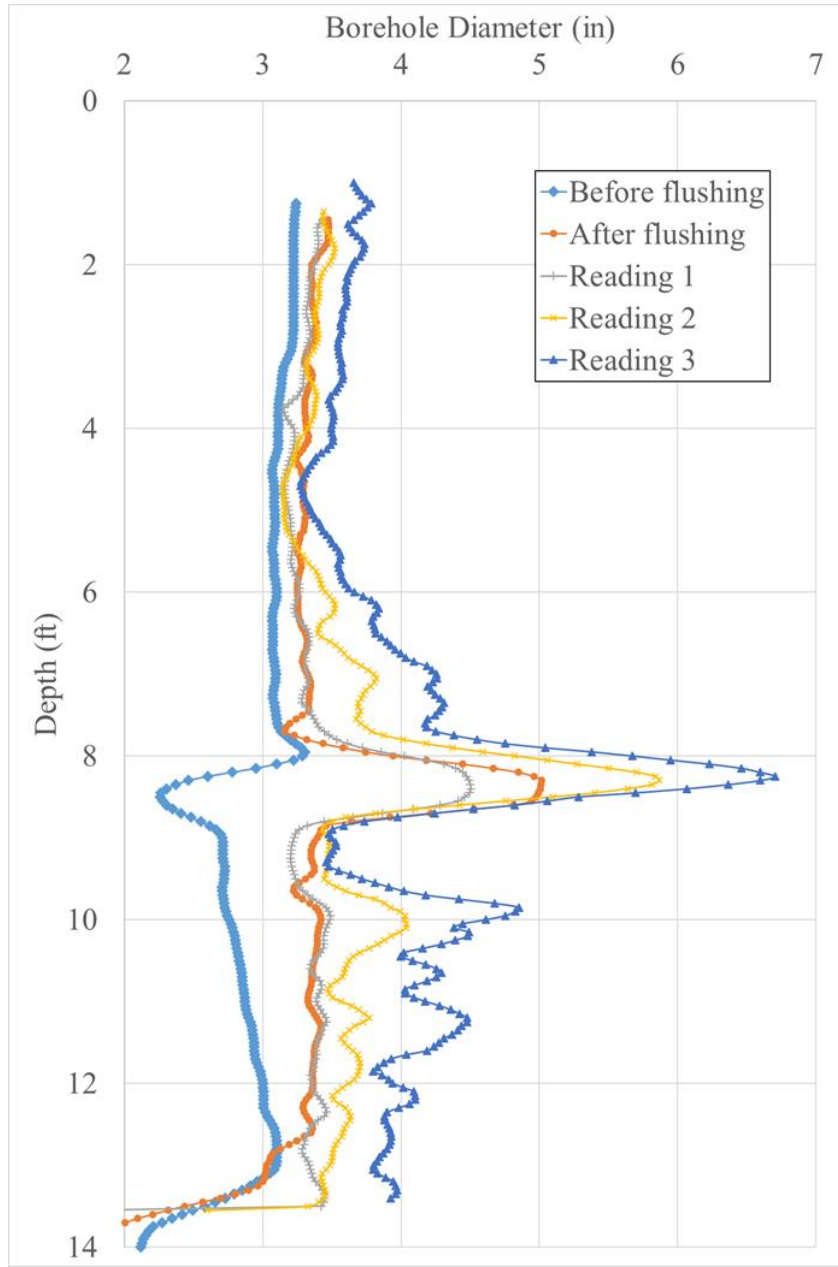
13. Moody (1944) developed a chart which gives the friction factor as a function of the relative roughness and the Reynolds Number (Fig. 4.1 and 4.2). This chart is for circular pipes and leads to the following equation proposed by Haaland (1983).

$$\frac{1}{\sqrt{f}} = -1.8 \log \left[\left(\frac{\epsilon/D}{3.7} \right)^{1.11} + \frac{6.9}{Re} \right]$$

14. Applying this equation to pipes with an annulus cross section requires a modification of the value of f as follows (Munson, 2009): $f_{\text{annulus}} = 1.5 f_{\text{pipe}}$
15. The roughness ϵ is generated as a profile by considering a rolling depth equal to 0.1 m of the eroded radius profile and calculating for each one of those 0.1 m depth the mean depth of the asperities.
16. Now all the elements are set to calculate the shear stress from the velocity as follows. At any depth, obtain the velocity from step 9, then the fluid density, then the roughness, then the hydraulic diameter of the annulus, then Reynolds Number, then the friction factor, and then the hydraulic shear stress.
17. Prepare a profile of shear stress versus depth.
18. Use the profiles of erosion rate vs depth, velocity vs depth, and shear stress vs depth to generate for each stratigraphic layer the erosion functions of erosion rate vs velocity and erosion rate vs. shear stress.

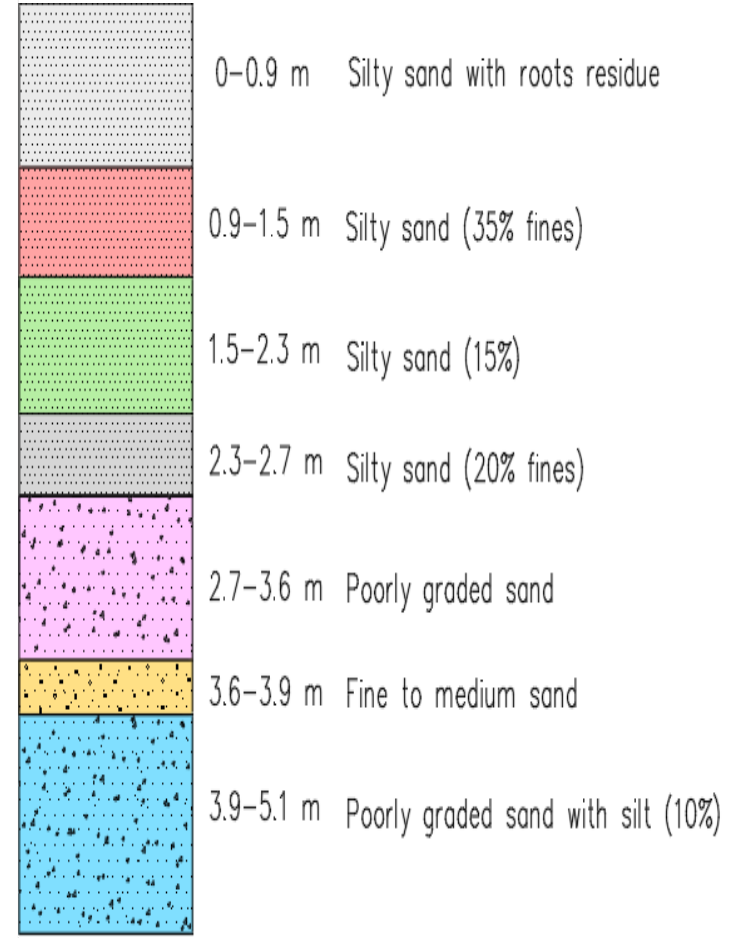
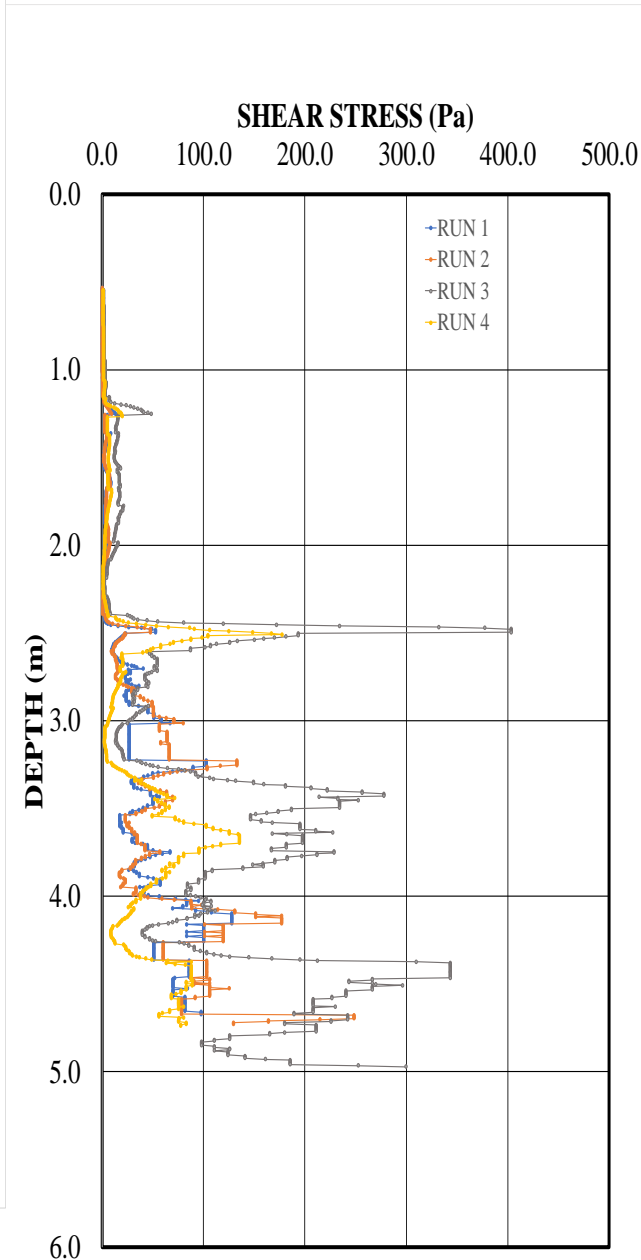
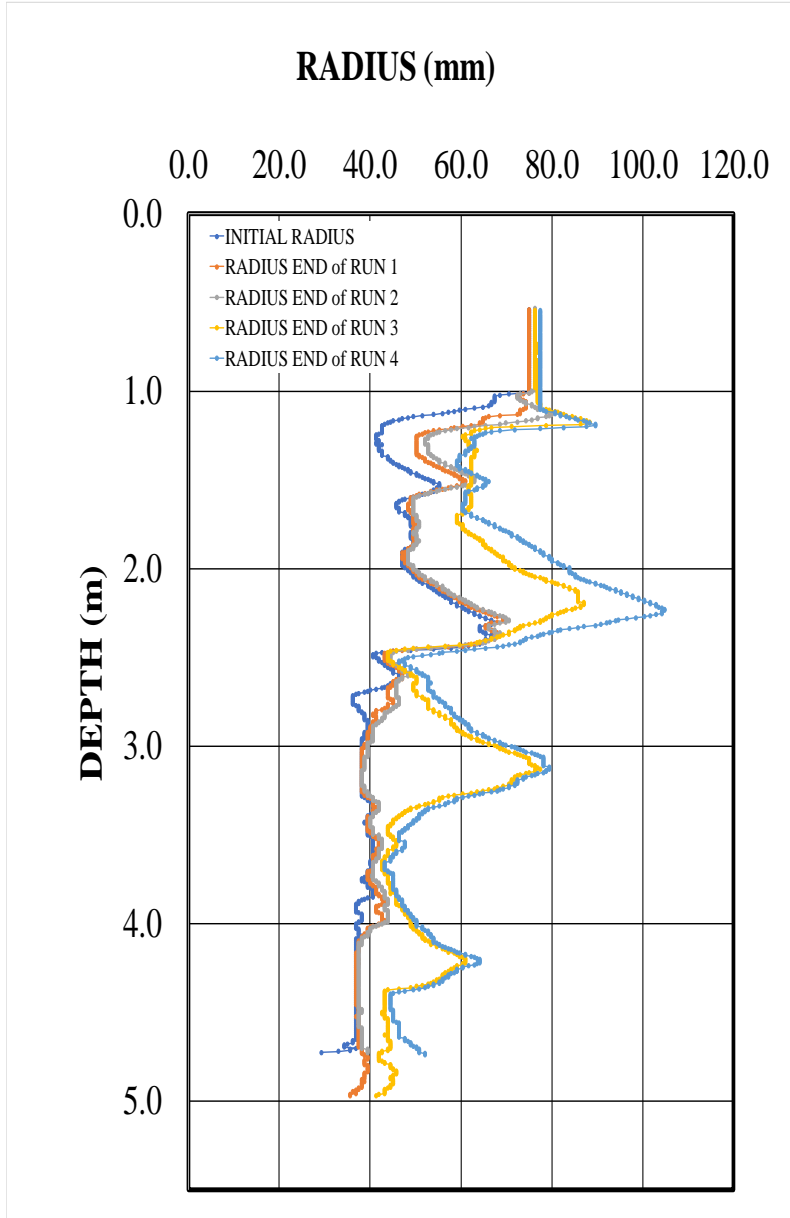


BOREHOLE EROSION TEST - BET



EXAMPLE OF BET RESULTS

Run 1 $v = 1.71$ m/s Run 2 $v = 1.81$ m/s, Run 3 $v = 2.82$ m/s, Run 4 $v = 1.65$ m/s



Evaluating the BET precision

The BET precision: procedure

Variation in radius r:

- ❑ Consider two caliper reading profiles (radius r_1 and r_2 as a function of depth) recorded in the field within the same borehole at the end of a flow run.
- ❑ Calculate the average caliper reading profile as $r_{av} = 0.5(r_1 + r_2)$ as a function of depth.
- ❑ Calculate the differences Δr_1 and Δr_2 at any given depth between the radius given by each caliper reading (r_1 and r_2) and the average radius r_{av} calculated in step 2.
- ❑ Calculate the sum of the absolute values of the differences Δr_1 and Δr_2 over the borehole depth.

- ❑ The variation V_r is estimated as:
$$V_r = \frac{\sum |\Delta r_1| + \sum |\Delta r_2|}{\sum (r_1 + r_2)}$$

Variation in flow rate Q(t):

- ❑ The difference between a flow value $Q(t)$ and the average flow value Q_{av} is calculated for many time values, say every minute.

$$\Delta Q(t) = Q(t) - Q_{av}$$

- ❑ The variation is quantified by the ratio of the sum of the absolute values of $\Delta Q(t)$ over the sum of the flow values for all time values.

$$V_Q = \frac{\sum |\Delta Q(t)|}{\sum Q(t)}$$

The BET precision

Results:

- ❑ The out of roundness of the borehole - 0% to 11.91% with average 1.89%. $(\Delta r/r)_{av} = 1.89\%$.
- ❑ The flow variation during the “constant flow” - 2.12% to 34.78% with average 10.31%. $(\Delta Q/Q)_{av} = 10.31\%$

BET advantages and limitations.

Advantages

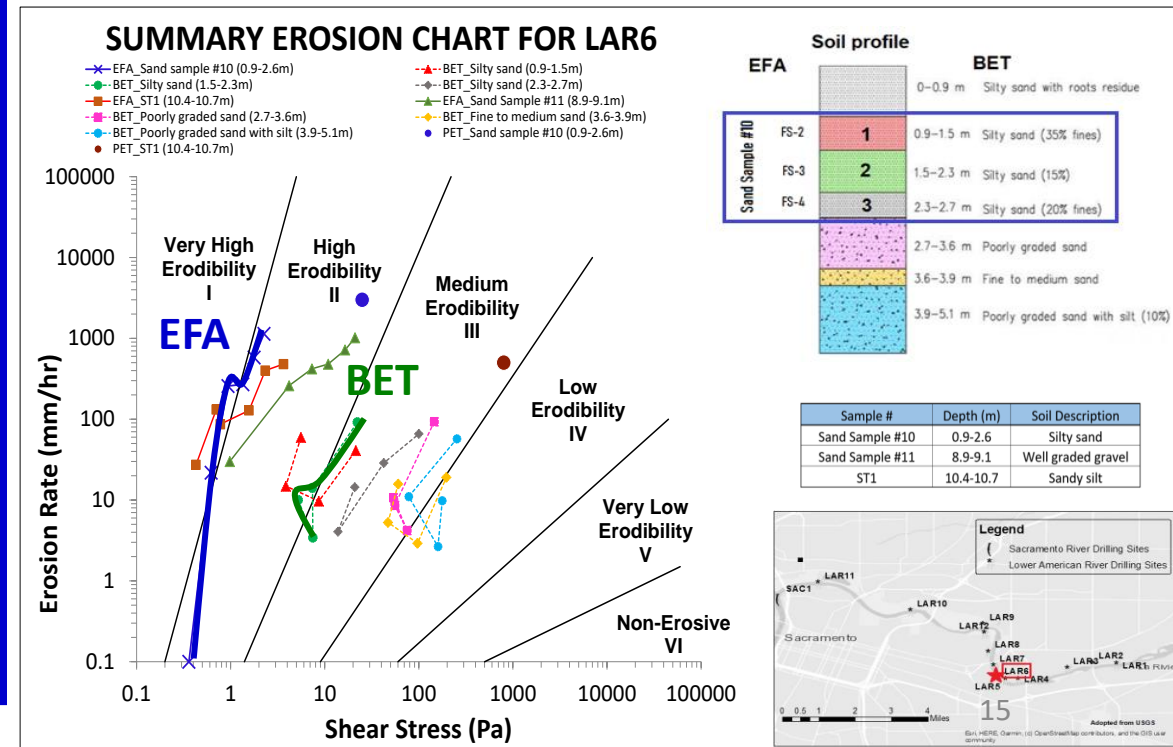
- ❑ Continuous profile of erodibility
- ❑ Commonly available equipment
- ❑ Calibration of laboratory data
- ❑ Calibration of numerical simulation
- ❑ Economically advantageous:
\$5,000-\$6,000 per 10m borehole

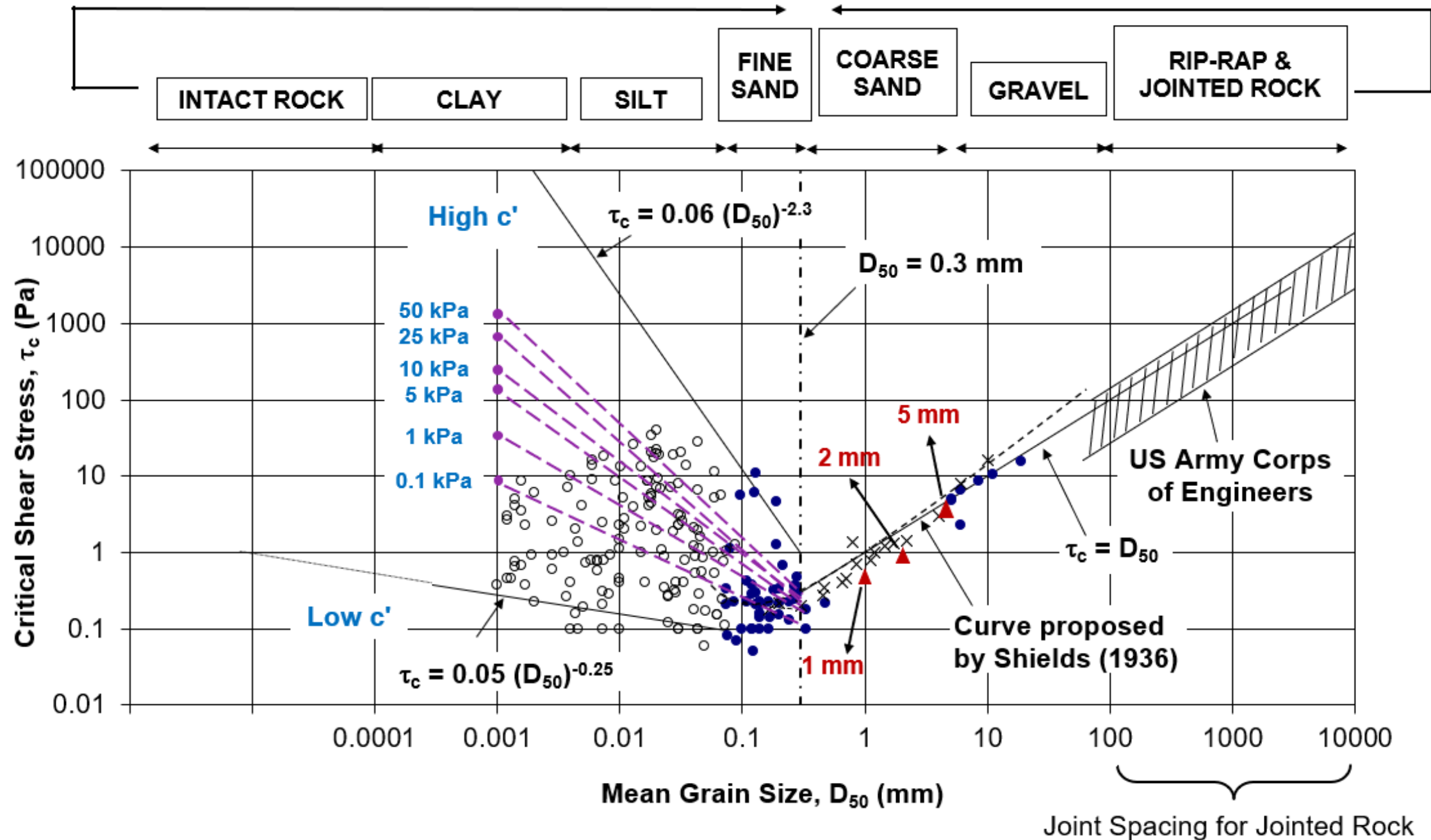
Recommendations:

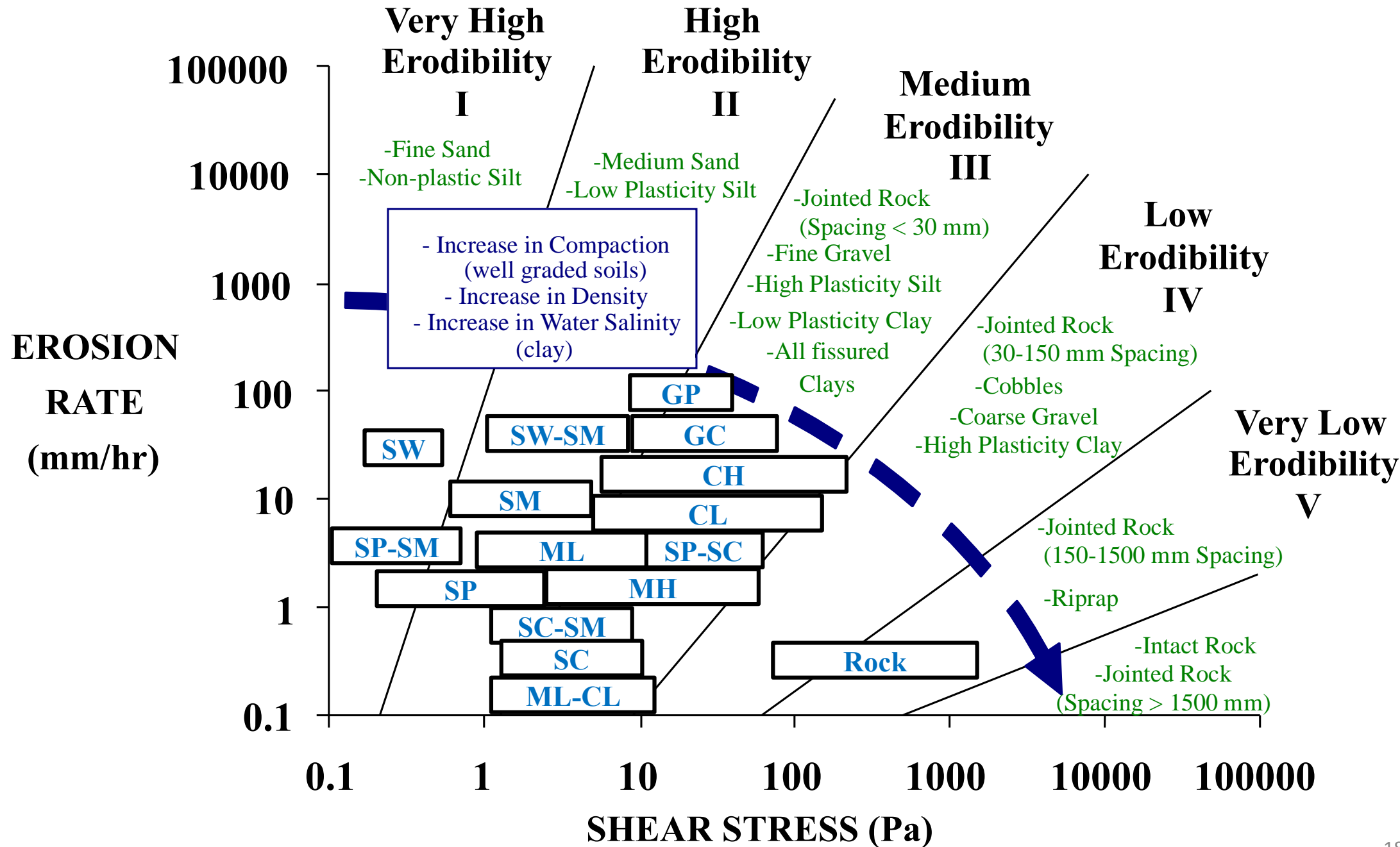
- ❑ Use BET in parallel with a few EFA tests
- ❑ Use BET to identify erodible layers
- ❑ Collect samples after inspection of profile

Limitations

- ❑ Precision less than laboratory
- ❑ Less erosion than EFA
 $\tau_c(BET) = 5.6 \tau_c(EFA)$
- ❑ Instability of the walls
- ❑ Water permeating walls







SOME PUBLICATIONS WHICH MAY BE OF INTEREST

- SHAFII I., MEDINA-CETINA Z., SHIDLOVSKAYA* A., BRIAUD J.-L., 2022, “Relationship between Soil Erodibility and Soil Properties” Journal of Geotechnical and Geoenvironmental Engineering, Vol. 149, Issue 1, ASCE.
- SHIDLOVSKAYA A., BRIAUD J.-L., 2023, “Erosion Mitigation Using Grass, Riprap, Lime, and Enzymes, Journal of Geotechnical and Geoenvironmental Engineering, Vol. 149, Issue 4, ASCE.