



**Alkyon**



Enabling Delta Life



**Deltas**



Delft Hydraulics

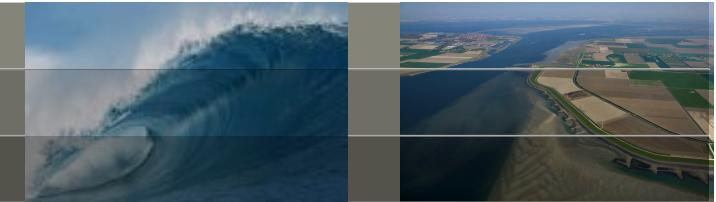
## Spectral wave modelling in tidal inlet seas: Results from the SBW project

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Netherlands; <sup>4</sup>Witteveen+Bos, Netherlands; <sup>5</sup>Svasek Hydraulics, Netherlands;

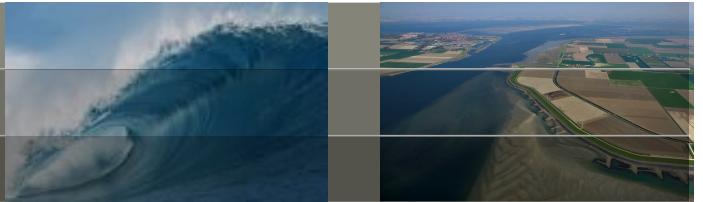
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# Flood protection in the Netherlands



The Netherlands without dikes



Dike rings and safety levels



# Project motivation

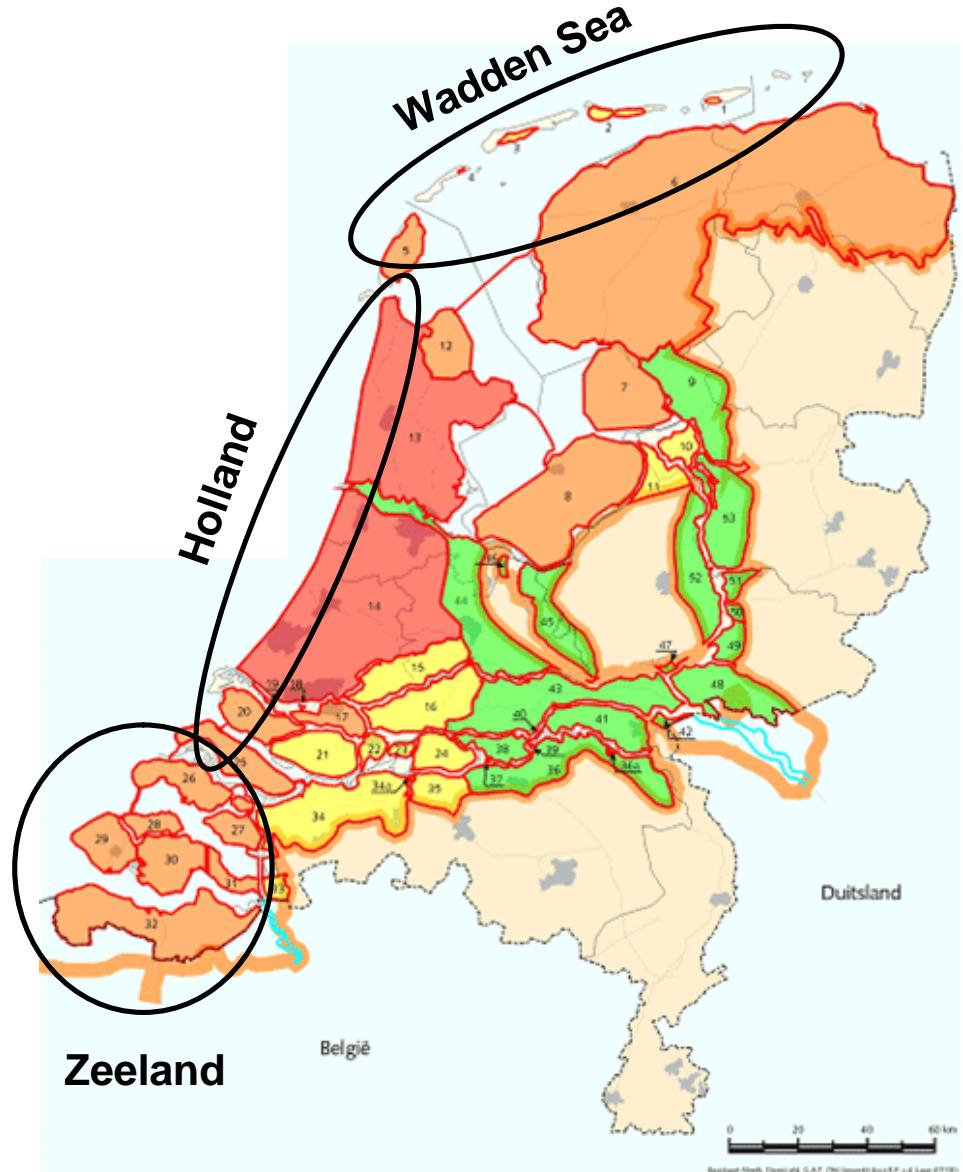


Safety level of Dutch Sea defenses  
checked every 5-6 years

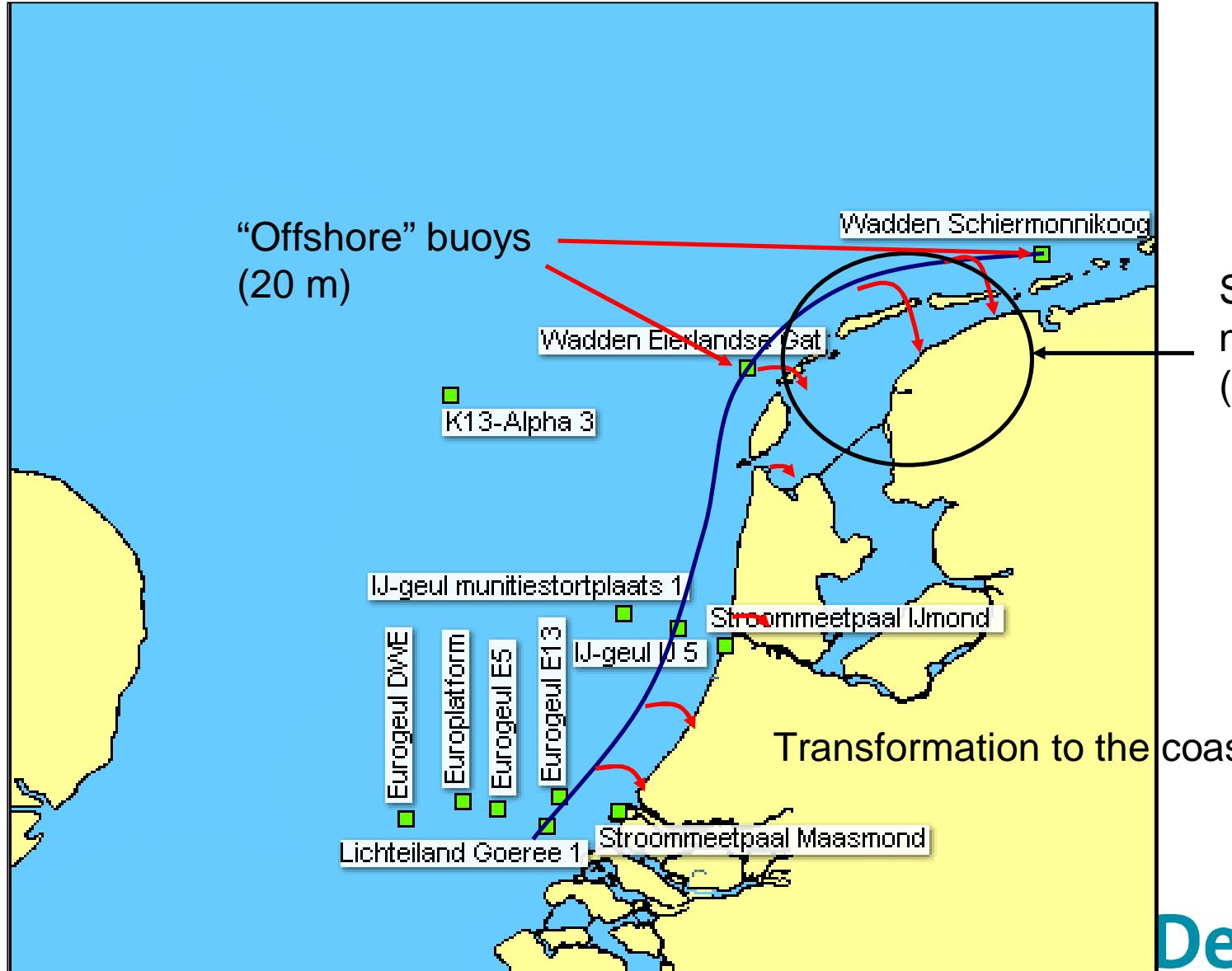
Need Hydraulic Boundary Conditions  
(HBCs) at toe of dike

For Holland and Zeeland coasts  
**SWAN** is used for wave  
transformation offshore/nearshore

In **Wadden Sea** historic/design data  
are used instead.



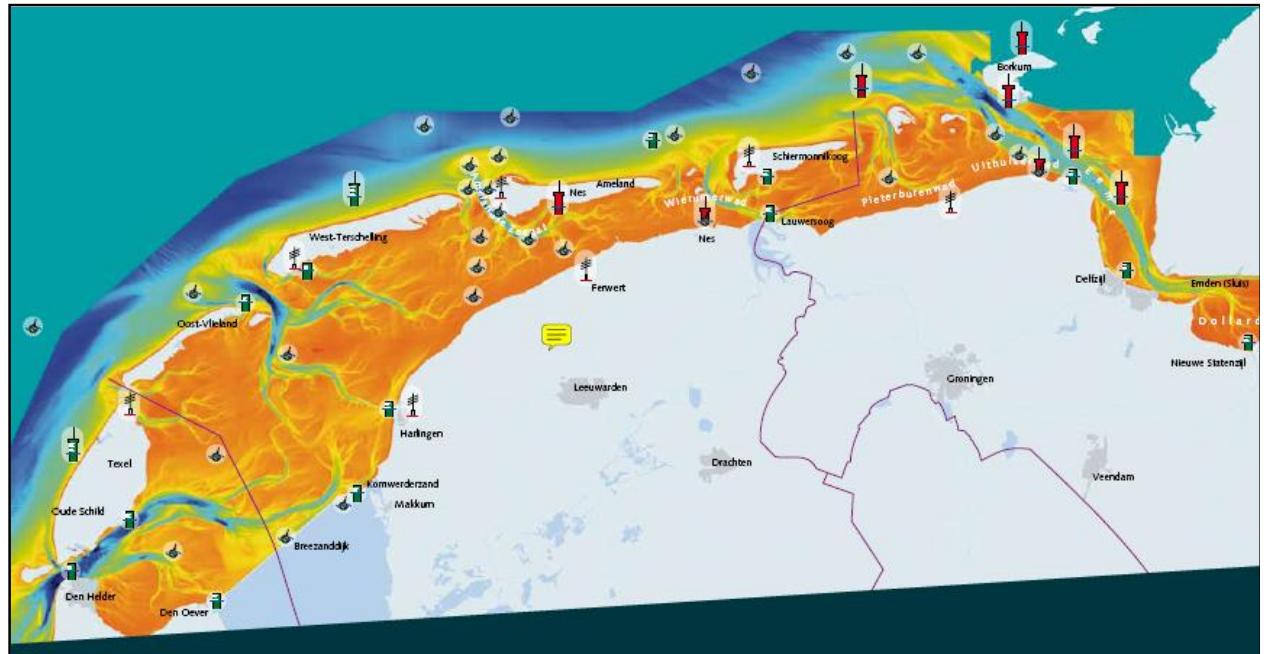
# Wave transformation from offshore to the coast



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# The problem with SWAN in Wadden Sea

- SWAN results are insufficient compared to observations in **Norderneyer Seegat**, especially wrt penetration of North Sea waves (Kaiser & Niemeyer 2001).
- No relevant verification wave data in Dutch part of the Wadden Sea.



Objective SBW-Waddenzee: a **consistent, calibrated wave model + tools** as part of the HBC chain to produce reliable HBC for the Wadden Sea in 2011 (and for other coastal areas and lakes) using Dutch and foreign **field data**.

# Measurement campaign



Bathymetry and buoy locations in tidal inlet of Ameland

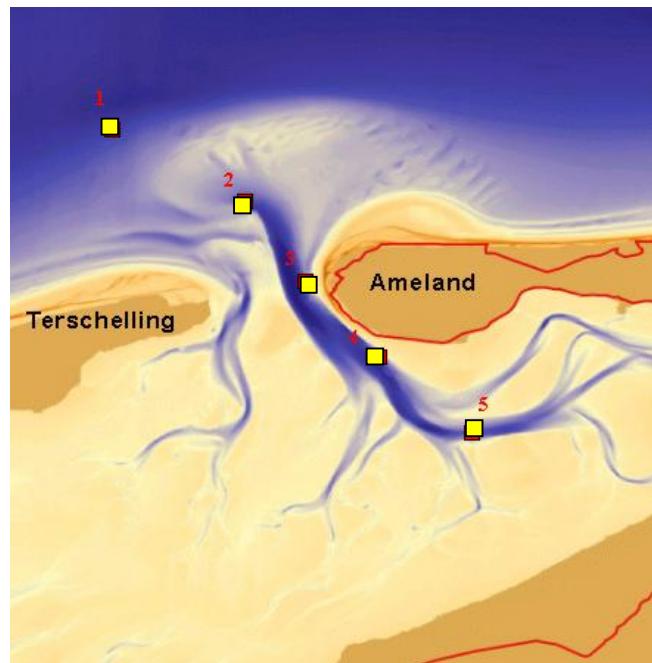
Wave riders:

■ directional

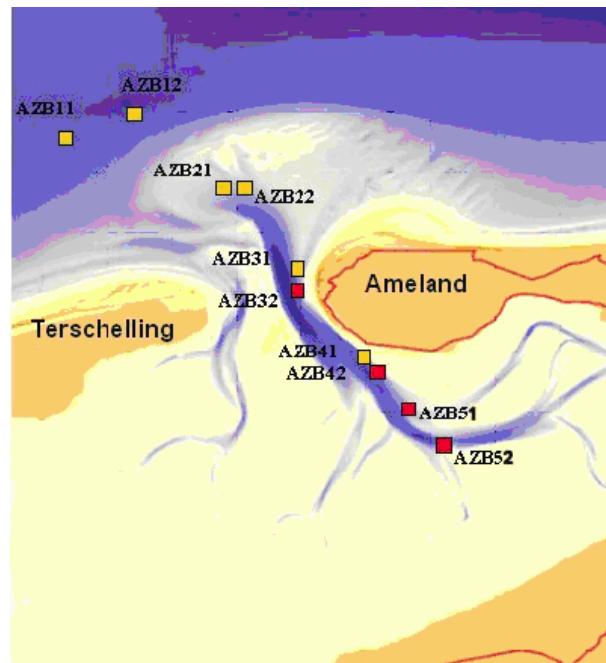
■ non-directional



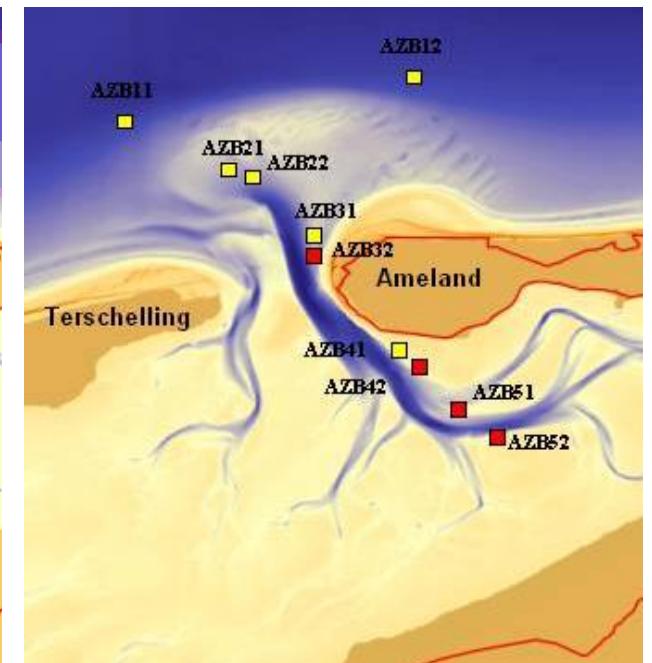
2003/2004



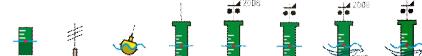
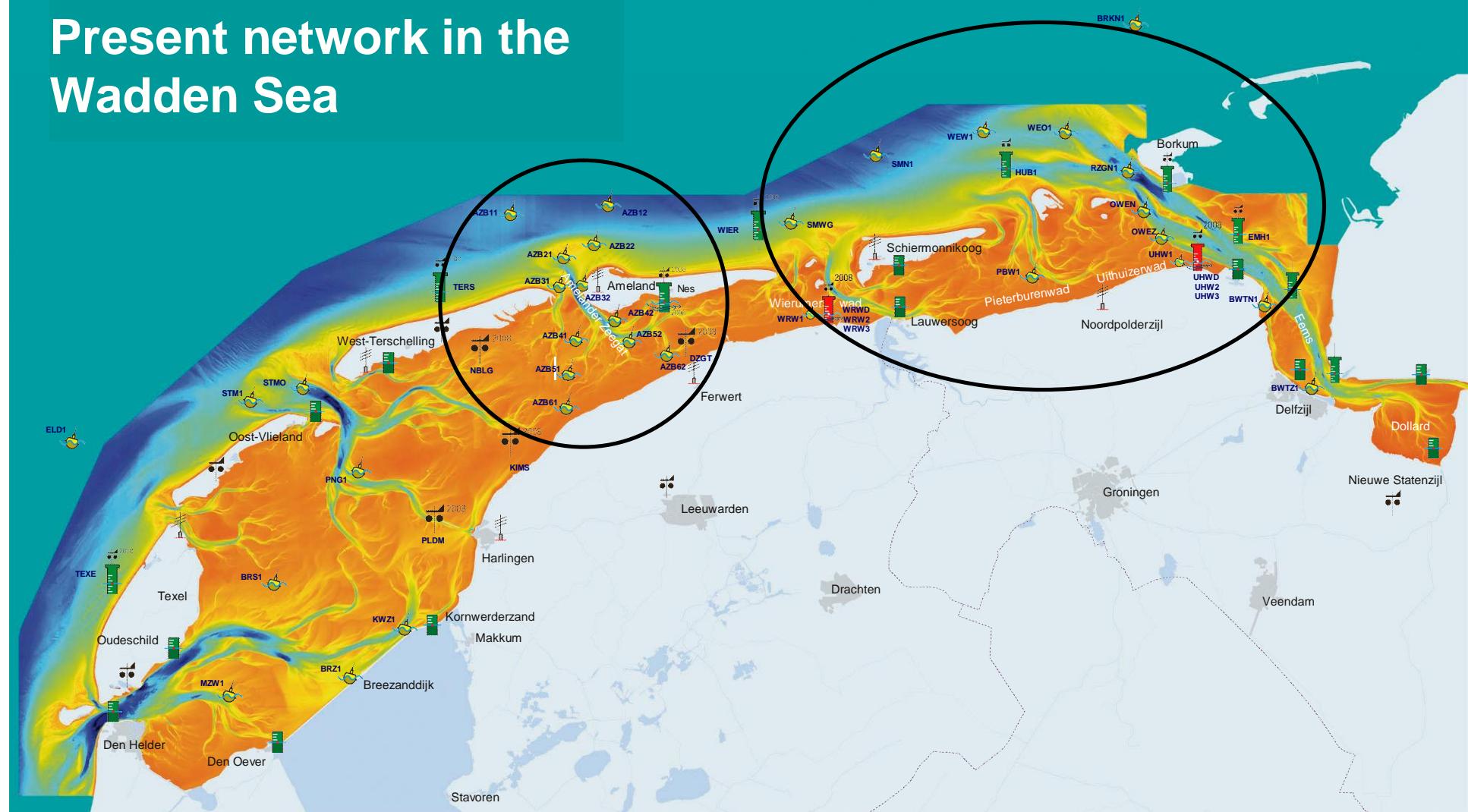
2004/2005



2005/2006



# Present network in the Wadden Sea



peilmeetstation

stromingsmeting

windmeting

meetpaal met zendverbinding

waterstandsmeting

2008 windmeting voorzien voor 2008

meetpaal met zendverbinding  
(gerealiseerd binnen het SBW-project)

waterstands- en golftelling

golfmeting

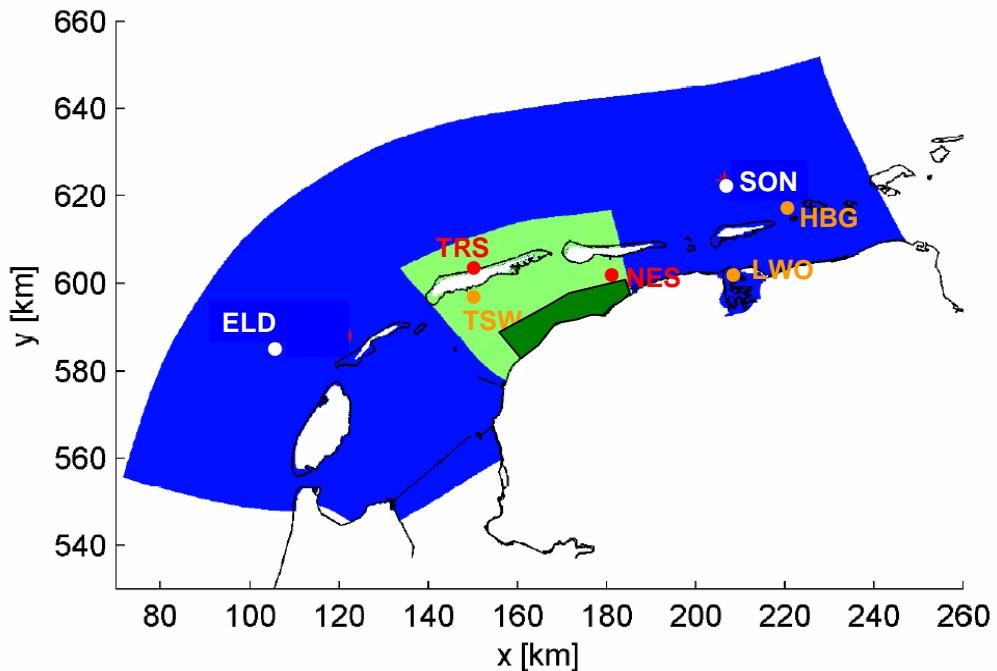
ontvangstlocatie

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# Observations at Uithuizerwad



# Wave modelling with SWAN (input and grids)



## Curvilinear grids :

- Overall ([GridCL](#))
- Ameland Zeegat ([AZG3A](#))
- Frisian coast ([AK4A](#))

## Measurement stations :

- Directional wave gauges at ELD, SON
- (Non-)Directional wave gauges in AZG
- Tidal gauges at **NES, TRS**
- Wind stations at **TSW, LWO, HBG**

## Models for wind and current fields :

- Wind field from HIRLAM
- Wind field from downscaling technique
- Water level / current field from WAQUA

## Bathymetry (based on soundings):

- Inlet of Ameland: yearly
- Elsewhere: 5-yearly

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# Modelling approach: SWAN, source terms, numerics



Action balance equation:

$$\nabla_x \bullet \left[ (\vec{c}_g + \vec{U}) N \right] + \frac{\partial c_\sigma N}{\partial \sigma} + \frac{\partial c_\theta N}{\partial \theta} = \frac{S_{tot}}{\sigma}$$

Wind input and whitecapping  
(vd Westhuysen et al., 2007):

$$S_{wc} = -C_{ds} \left[ \frac{B(k)}{B_r} \right]^{p/2} \left[ \tanh(kd) \right]^{\frac{2-p}{4}} g^{\frac{1}{2}} k^{\frac{1}{2}} E(\sigma, \theta)$$

Bottom friction (Hasselmann, 1973):

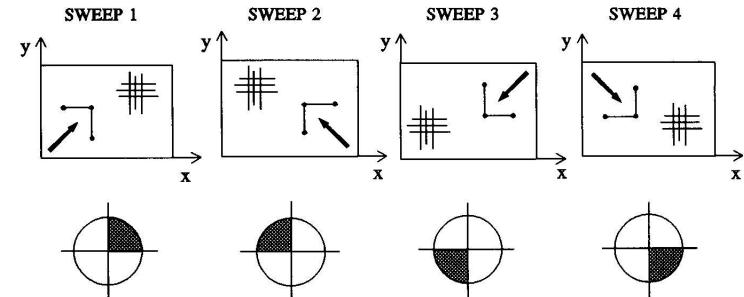
$$S_{bot} = -C_{JON} \frac{\sigma^2}{g^2 \sinh^2(kd)} E(\sigma, \theta)$$

Depth-induced breaking  
(Battjes & Janssen, 1978):

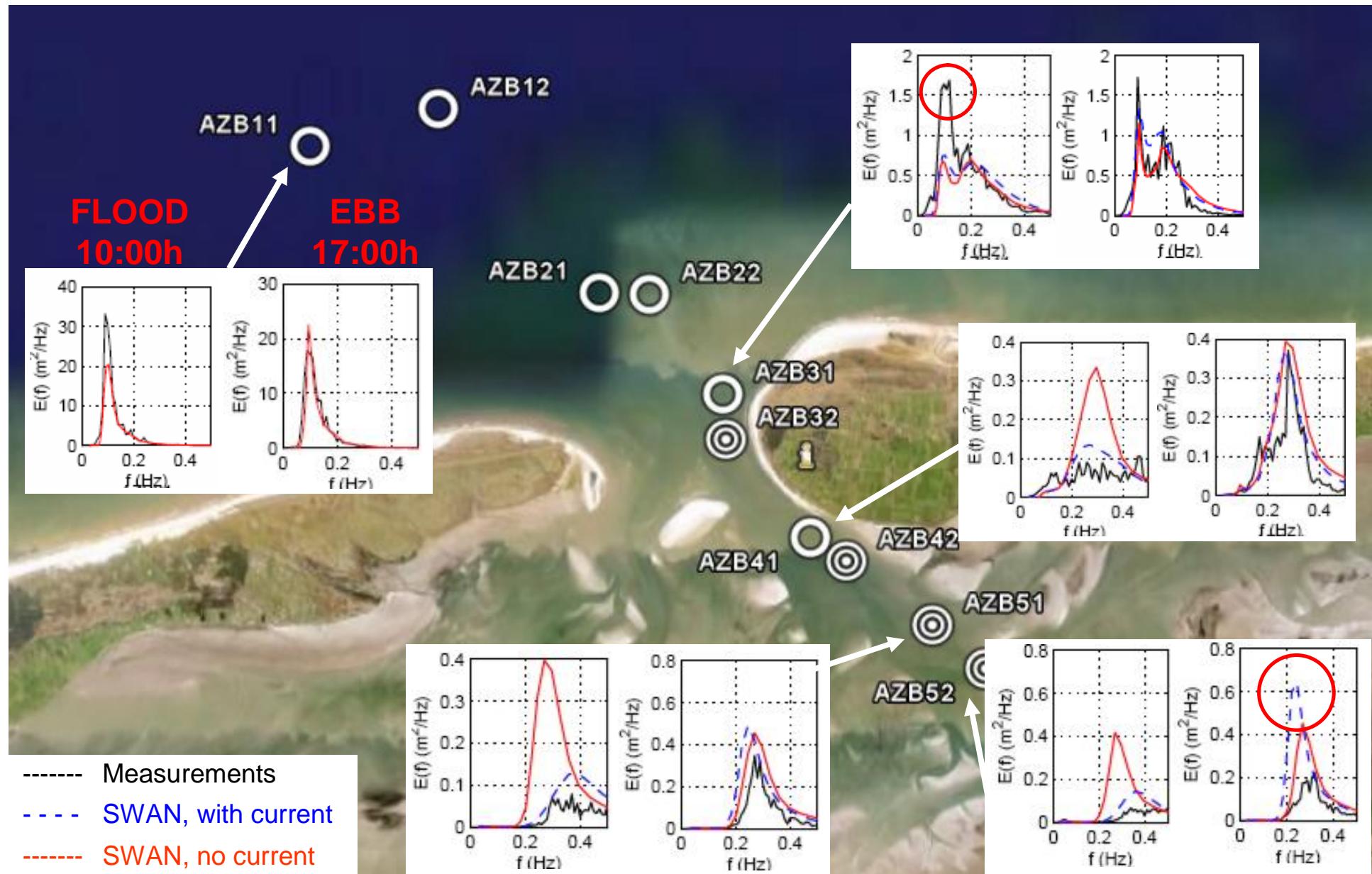
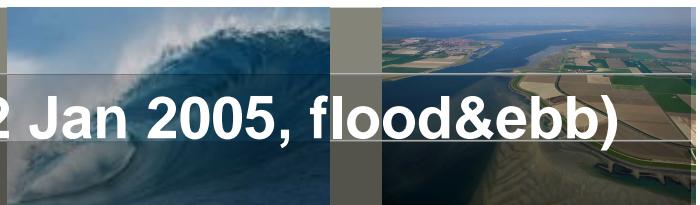
$$S_{brk} = D_{tot} \frac{E(\sigma, \theta)}{E_{tot}} , \quad D_{tot} = -\frac{1}{4} \alpha_{BJ} Q_b \bar{f} H_m^2$$

Quadruplets (DIA,  
Hasselmann. et al. 1985)

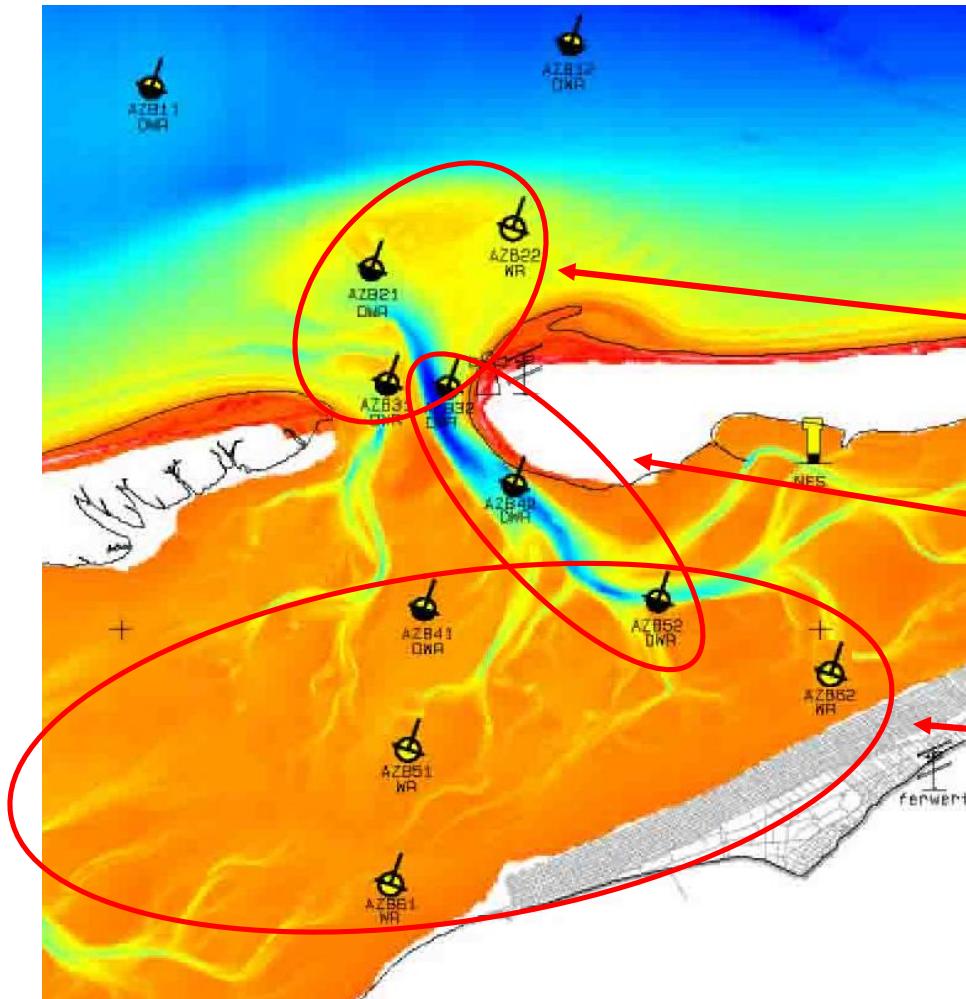
Triad interactions (LTA,  
Eldeberky 1996)



# Performance default model (Ameland, 2 Jan 2005, flood&ebb)



# Wave modelling challenges in the Wadden Sea



Configuration since Nov. 2006.  
Focus of hindcasts on specific aspects:

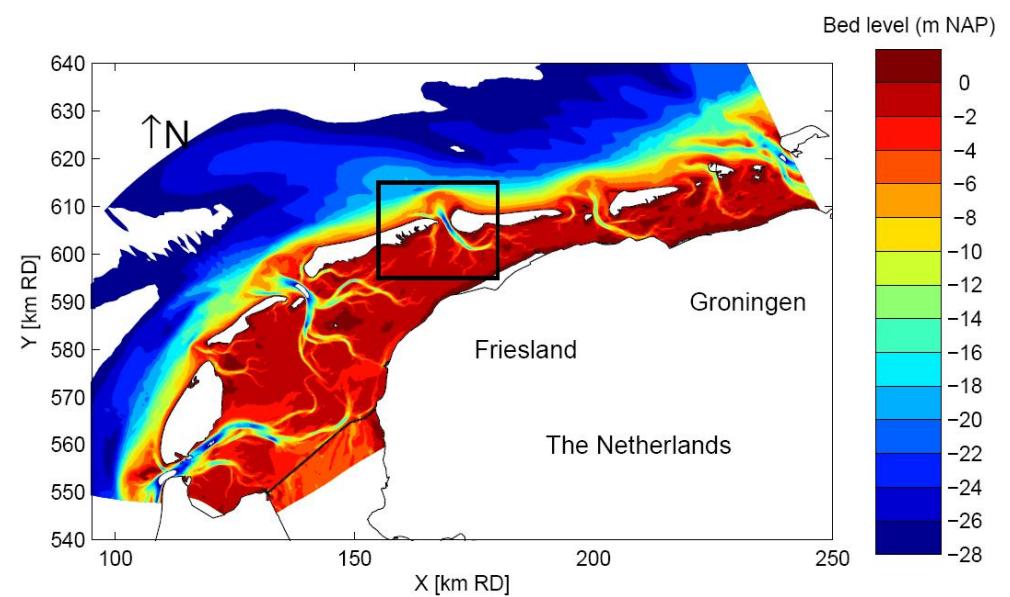
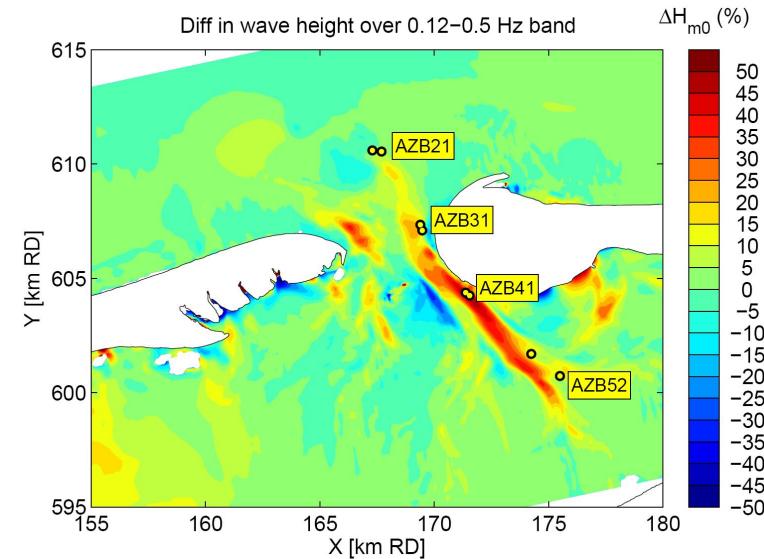
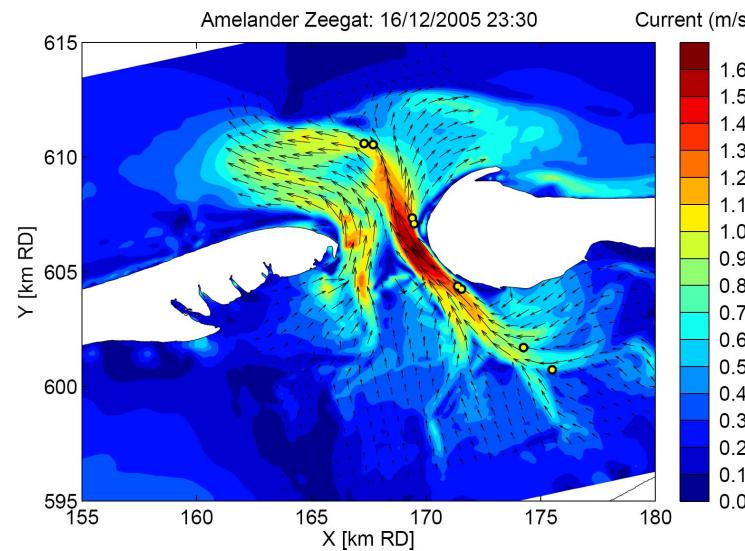
Penetration of **low-frequency energy** from North Sea

Effect of **wave-opposing and wave-following currents**

**Wave growth** in depth-limited areas

Improved modelling of **water levels and currents**

# Wave-current interaction: Influence of opposing current



# Enhanced dissipation on counter current



**Default whitecapping (saturation-based):**

$$S_{wc}(\sigma, \theta) = -C_{ds} \left[ \frac{B(k)}{B_r} \right]^{p/2} g^{\frac{1}{2}} k^{\frac{1}{2}} E(\sigma, \theta)$$

(V/d Westhuysen 2007,  
based on Alves & Banner 2003)

**Bore-based enhanced dissipation (Ris and Holthuijsen 1996):**

$$S_{diss,cur}(\sigma, \theta) = -C'_{ds} Q_b \left( \frac{s_{\max}}{\tilde{s}} \right)^2 \tilde{\sigma} \frac{k}{\tilde{k}} E(\sigma, \theta) , \quad \frac{1-Q_b}{\ln Q_b} = -8 \frac{E_{tot}}{H_m^2} \quad \text{and} \quad H_m = \frac{2\pi s_{\max}}{\tilde{k}}$$

**Saturation-based enhanced dissipation:**

$$S_{diss,cur}(\sigma, \theta) = -C''_{ds} \max \left[ \frac{c_\sigma(\sigma, \theta)}{\sigma}, 0 \right] \left[ \frac{B(k)}{B_r} \right]^{p/2} E(\sigma, \theta) , \quad \frac{\Delta s(\sigma, \theta)}{s(\sigma, \theta)} = \frac{\partial s}{\partial t} \Big/ s = \frac{c_\sigma(\sigma, \theta)}{\sigma}$$



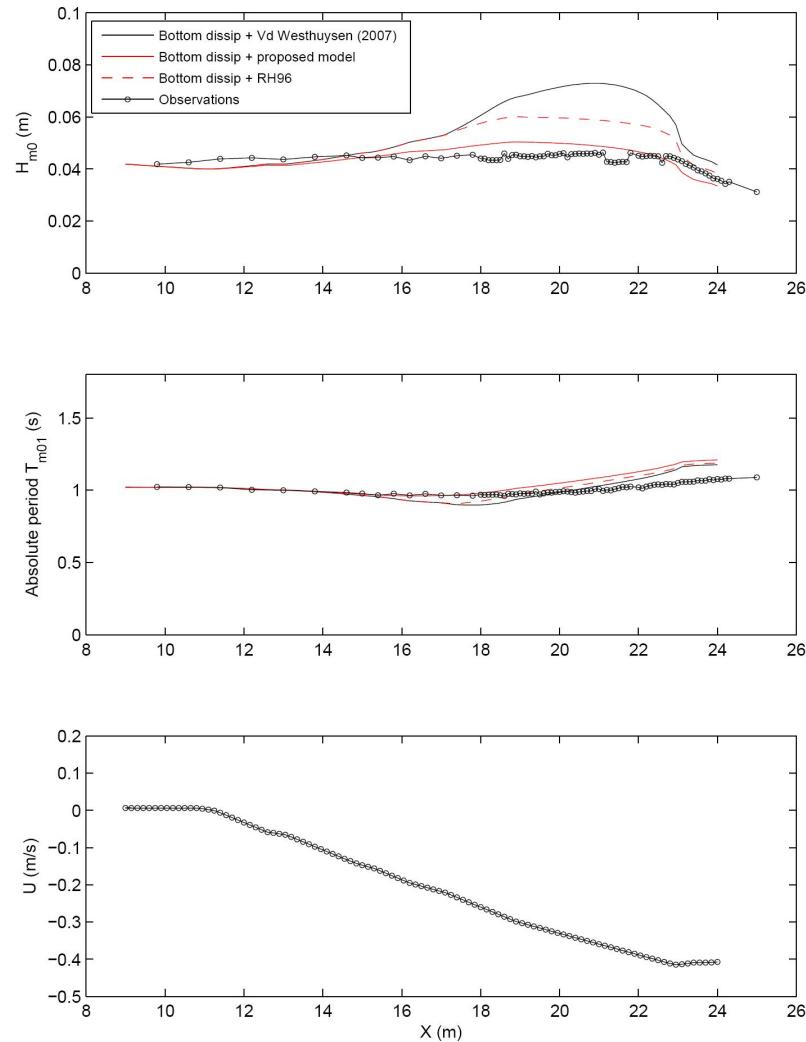
$$S_{diss} = S_{wc} + S_{diss,cur}$$

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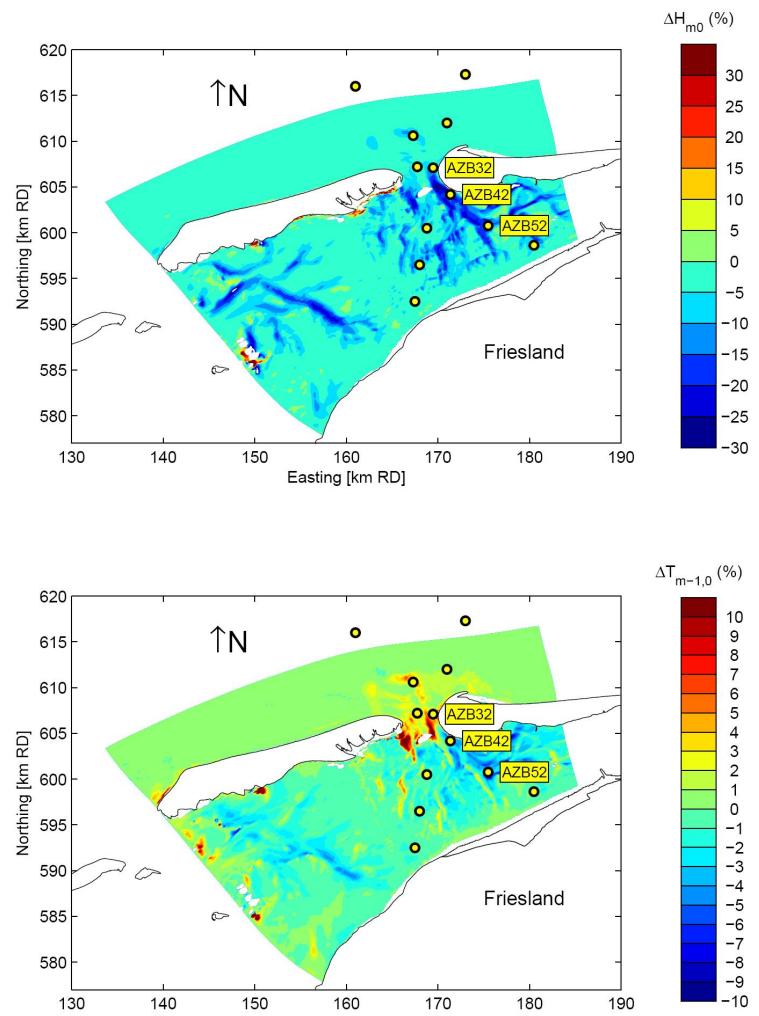
# Wave-current interaction: Results



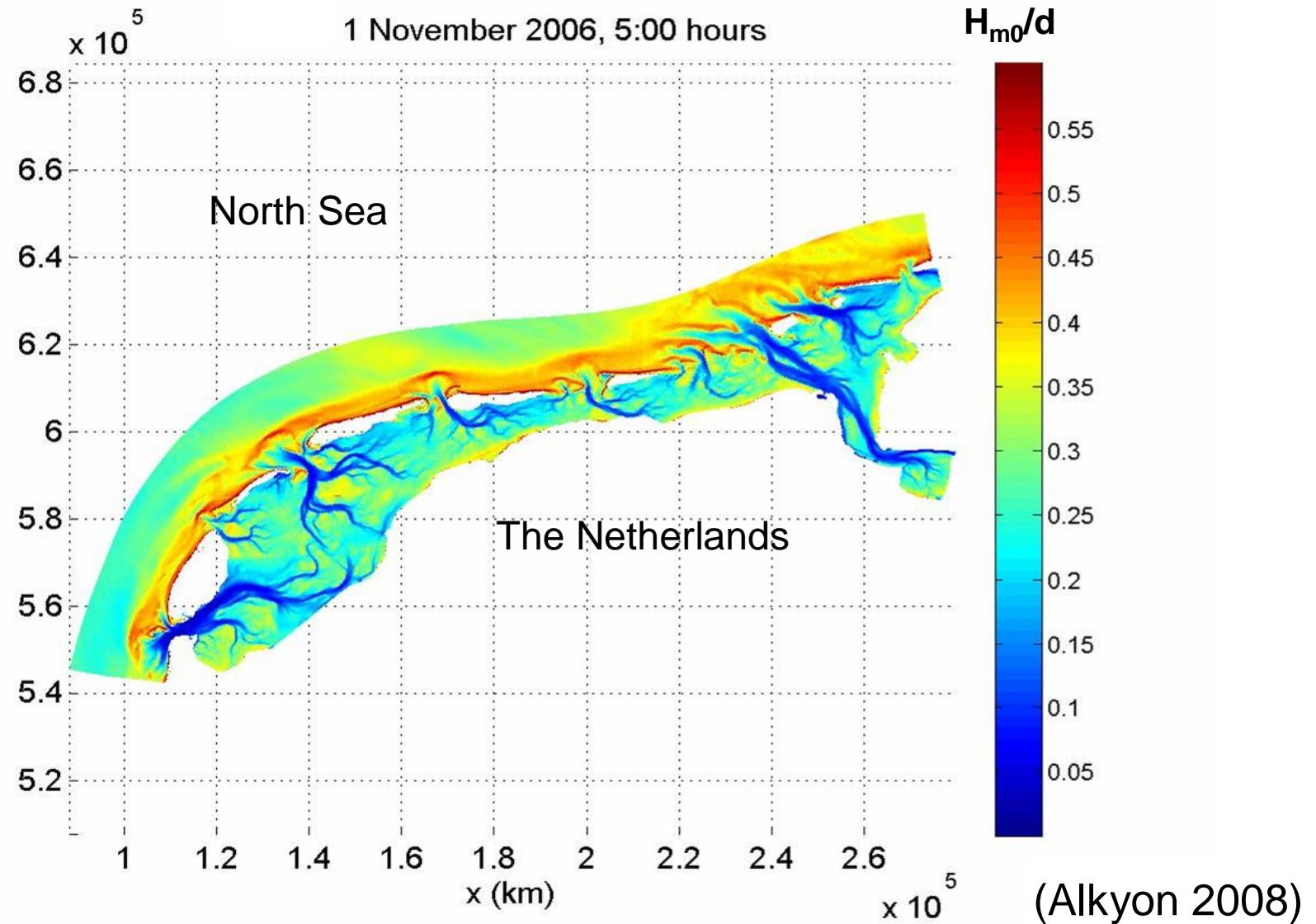
Suastika (2004) flume, partial blocking



AZG 18/03/2007 at 14:40 (ebb)  
Diff. proposed & default models



# Wave growth in finite-depth areas: Depth limitation



# Depth breaking based on shallow water nonlinearity



From Thornton & Guza (1983):

$$D_{tot} = -\frac{B^3}{4} \frac{f_{m01}}{d} \int_0^\infty H^3 p_b(H) dH$$

$$p_b(H) = W(H) p(H)$$

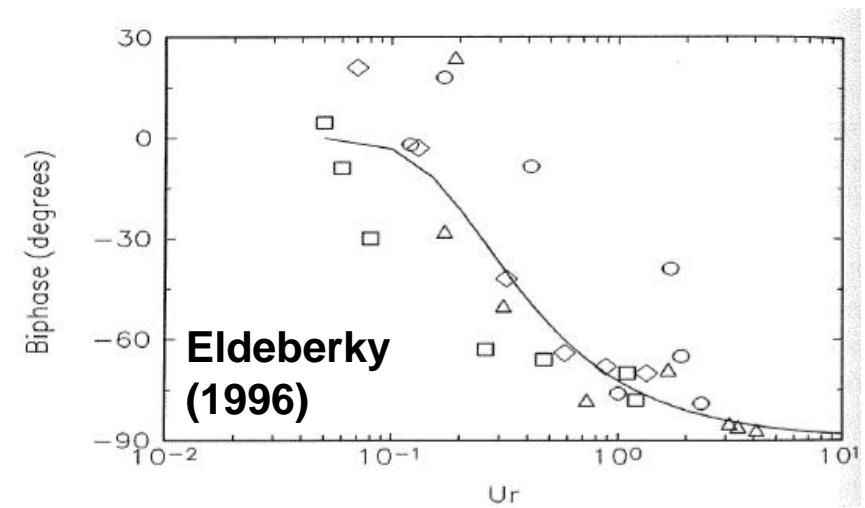
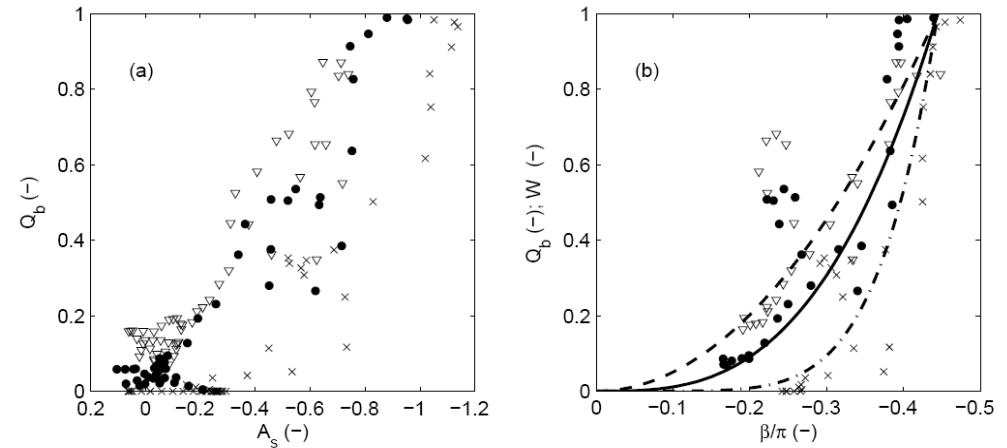
Introduce a biphase-dependent weighting function on the pdf:

$$W(H) = \left( \frac{\beta}{\beta_{ref}} \right)^n , \quad \beta_{ref} = -\frac{4\pi}{9}$$

$$n = 4 - \frac{4}{\pi} \arctan \left[ \nu \left( S_{loc} - \tilde{S}_{loc} \right) \right]$$

$$D_{tot} = \frac{3\sqrt{\pi}}{16} \frac{B^3 f_{m01}}{d} \left( \frac{\beta}{\beta_{ref}} \right)^n H_{rms}^3$$

**Boers (1996):**

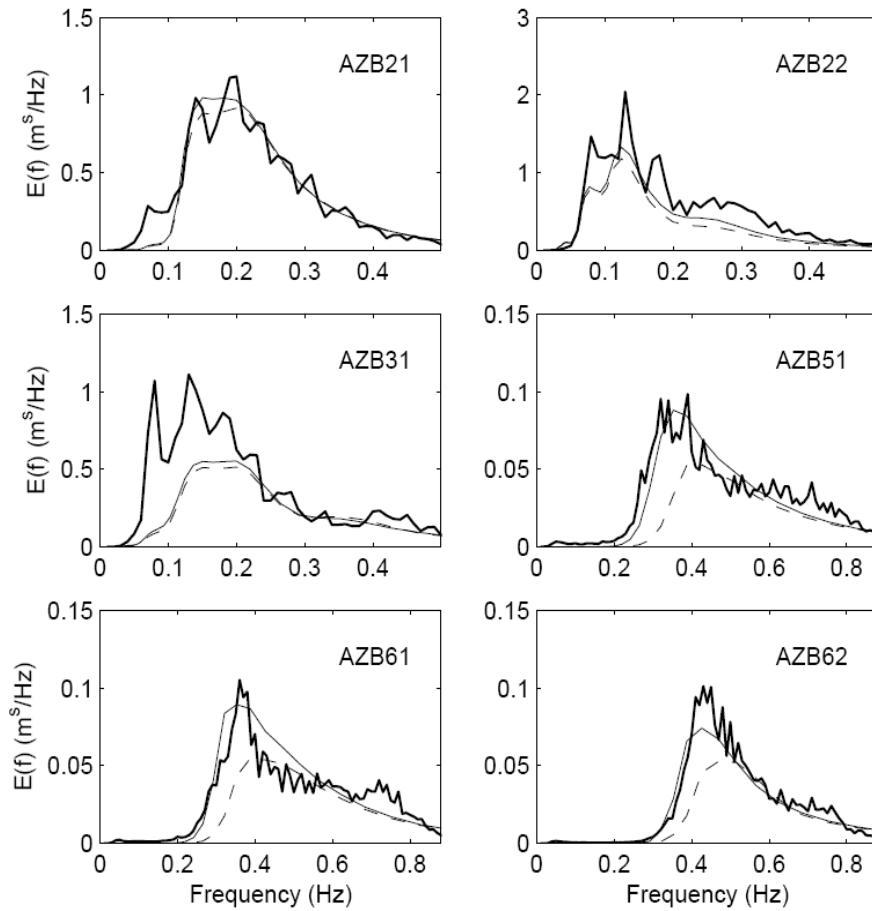


Deltas

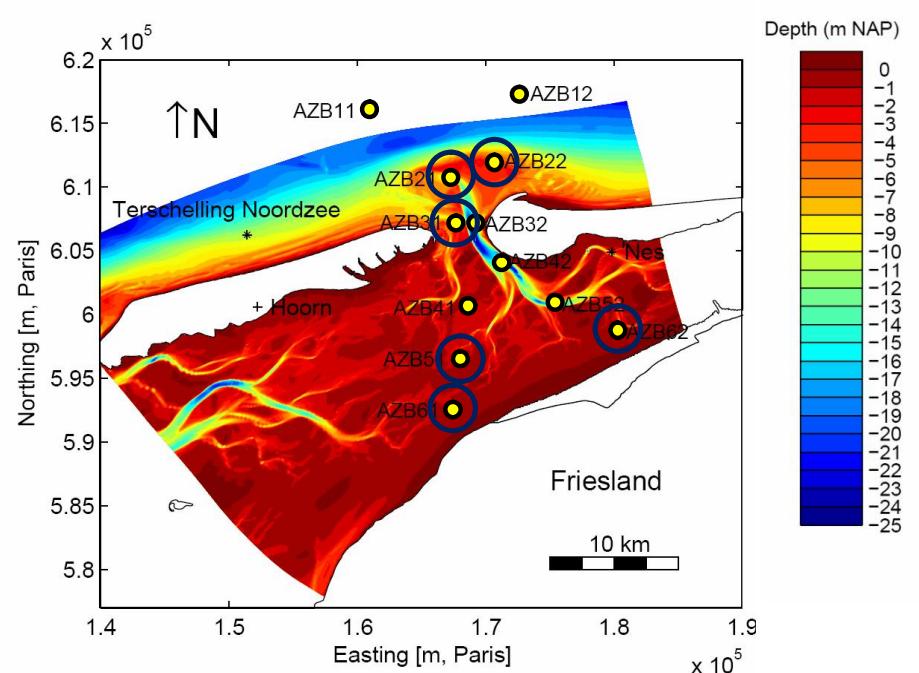
# Wave growth in finite-depth areas: Results



Amelander Zeegat (18/01/07, 12:20)



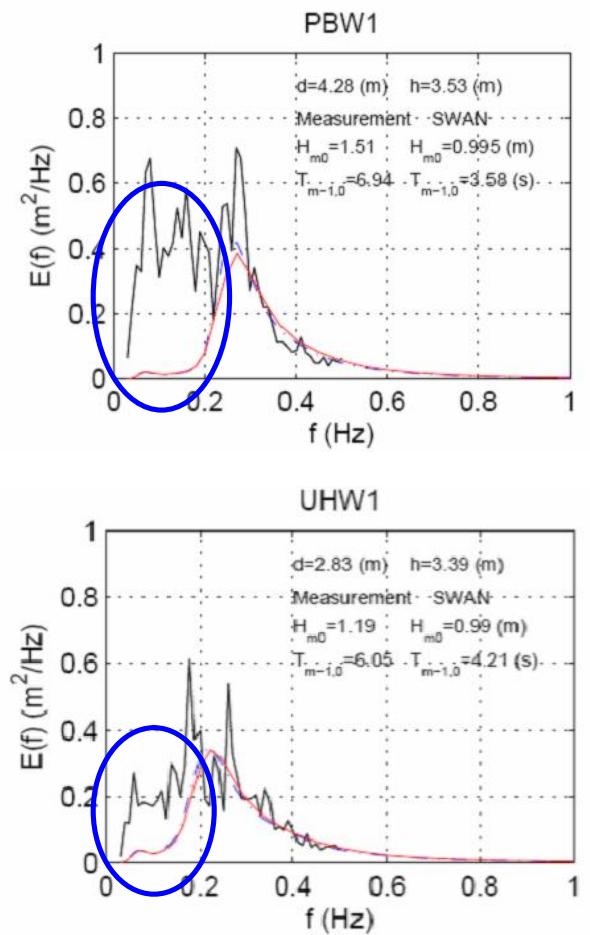
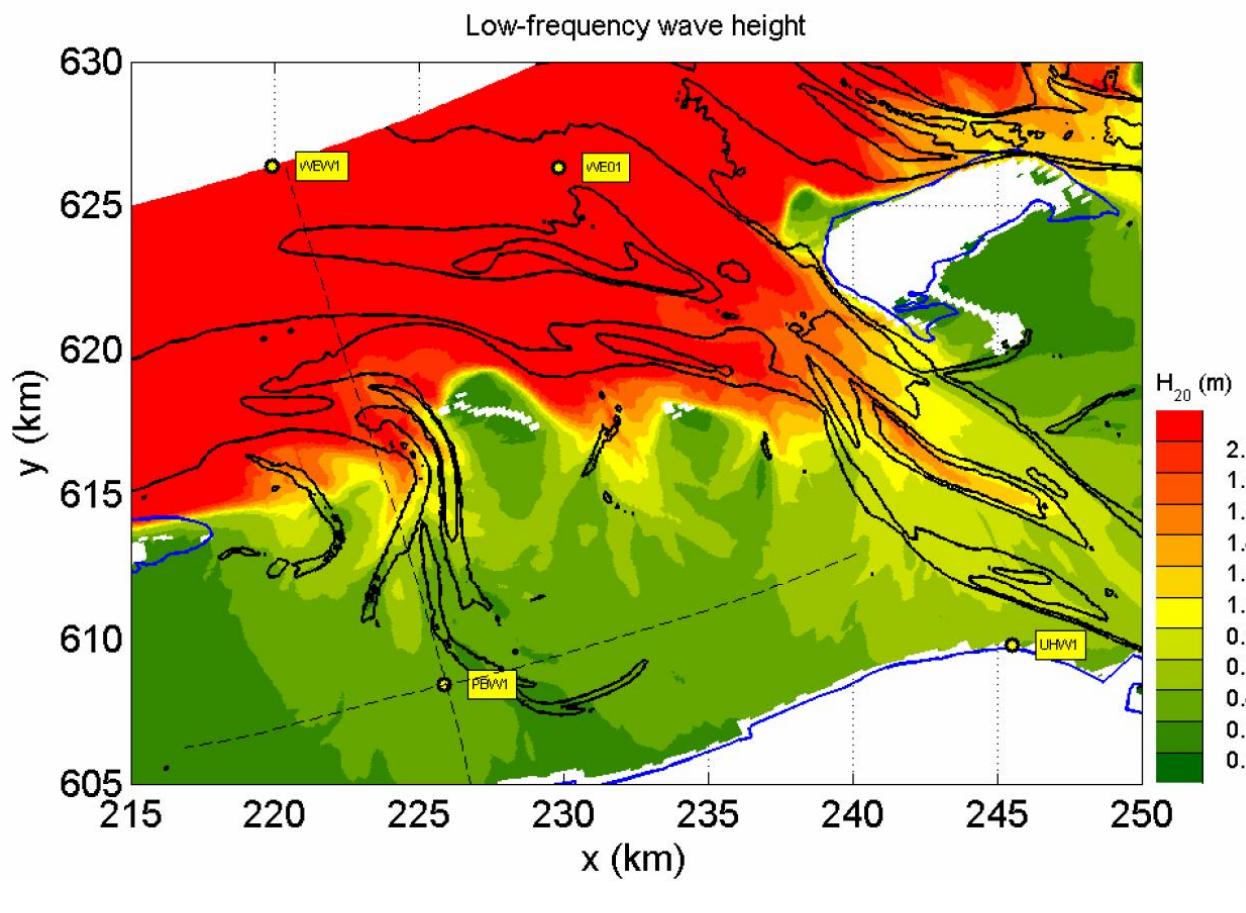
B&J 1978 (dashed); proposed (solid)



Van der Westhuysen (2010, JGR)

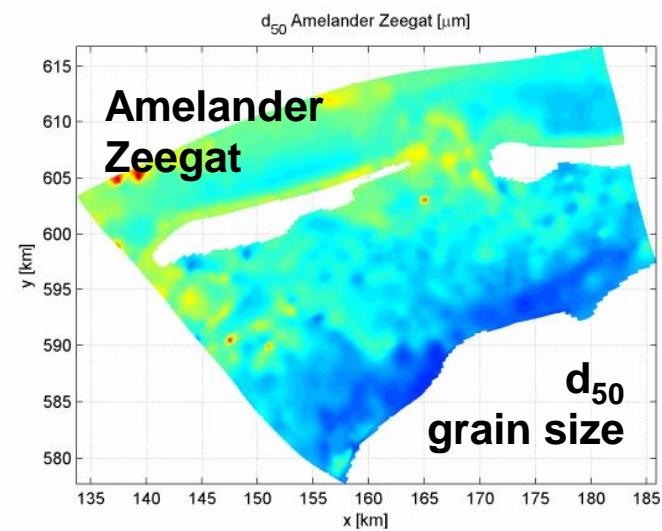
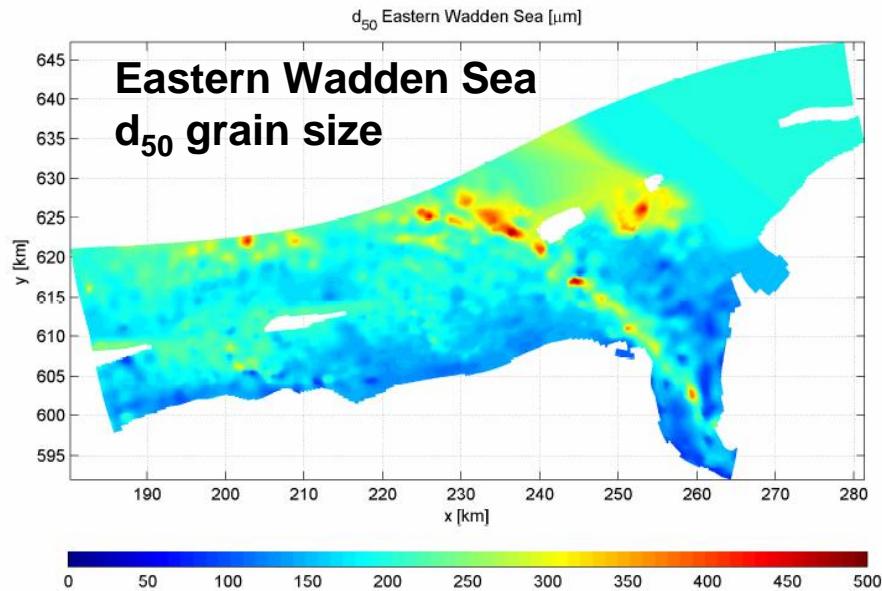
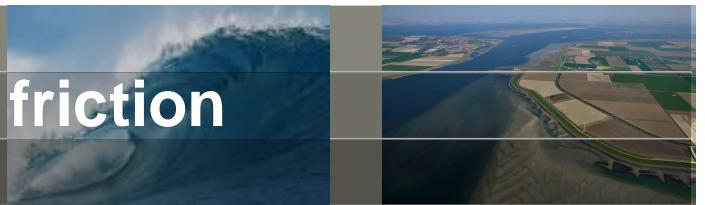
Deltas

# Swell penetration into the Wadden Sea interior

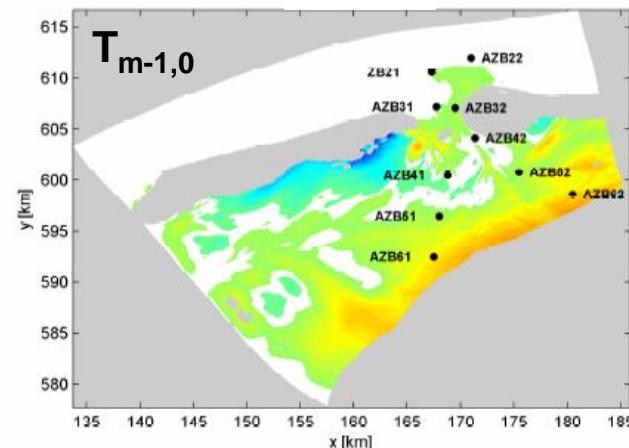
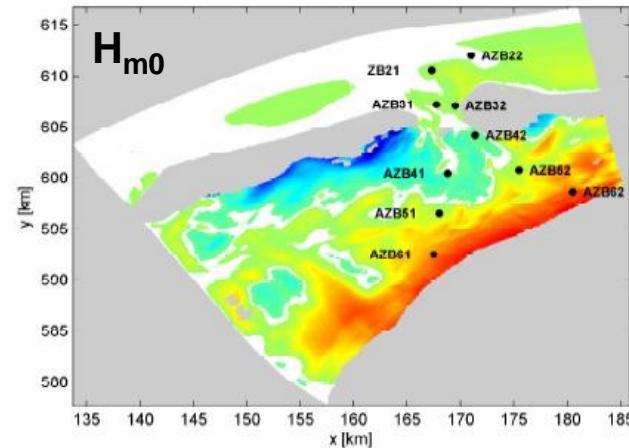


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# Swell penetration: Reduced bottom friction

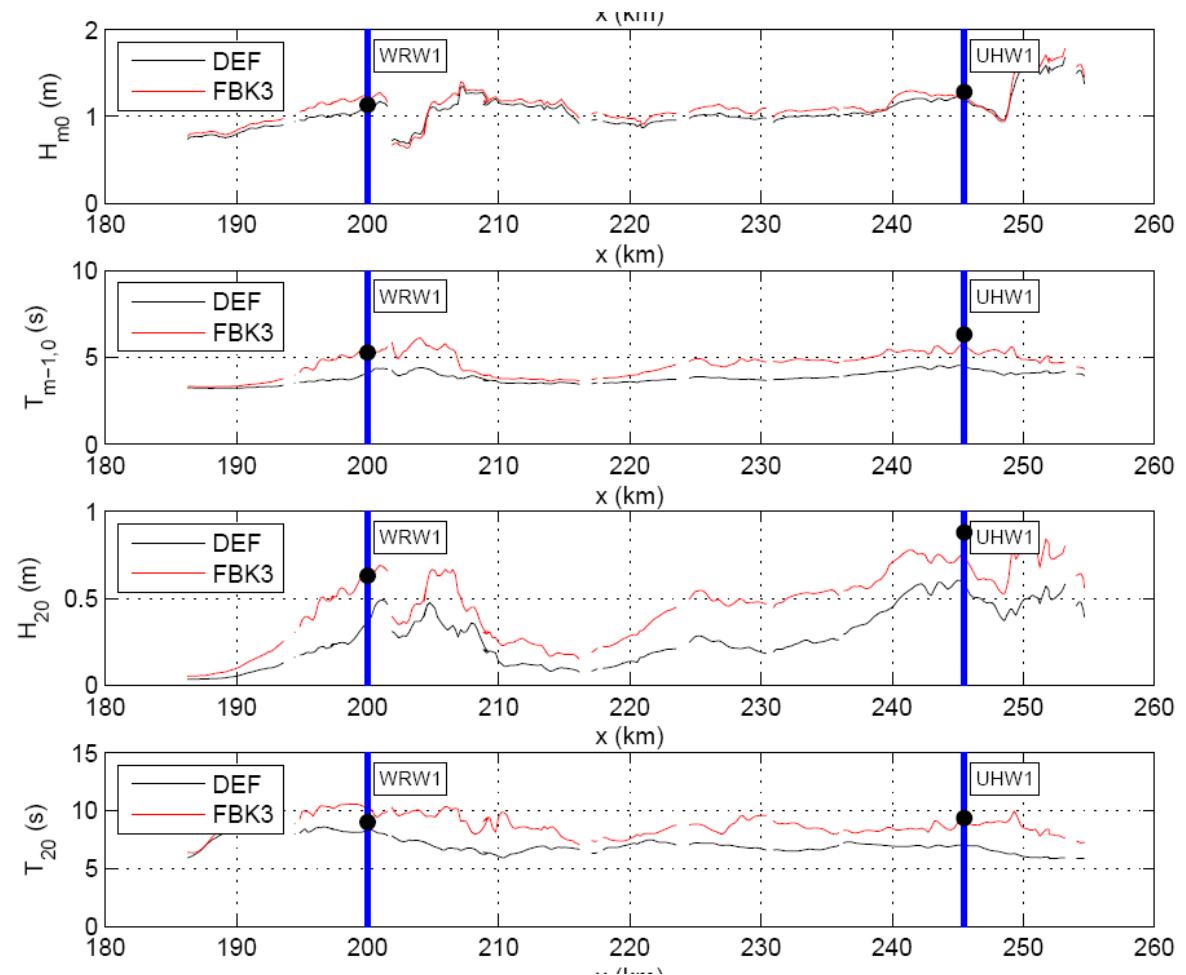
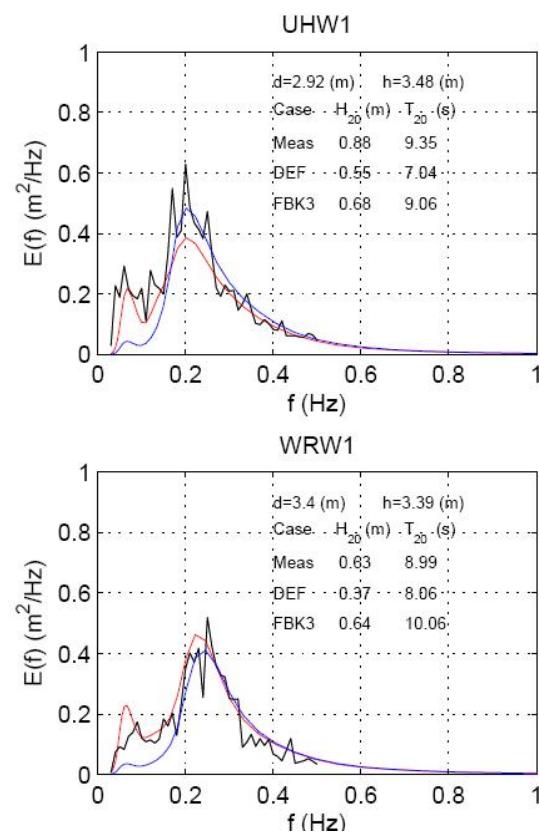


Madsen (1988) vs. JONSWAP (18/03/07 19:20)



# Swell penetration: Bottom friction and limit on refraction

- Largest improvement in  $H_{20}$  and  $T_{20}$  and integral parameters.
- $H_{m0}$  and  $T_{m-1,0}$  predicted within 10% accuracy



## Overall Conclusions



1. Three modelling challenges in the Wadden Sea identified: (a) waves on opposing current, (b) depth-limited wave growth over the flats and (c) swell penetration.
2. New expression developed for dissipation on counter current. Improvement for counter current; no deterioration for no-current and following current situations.
3. Depth-induced breaking related to shallow water nonlinearity. Proposed model corrects underestimation over horizontal beds (finite-depth growth conditions), and maintains good results over sloping beds.
4. Bottom friction and propagation play important part in penetration of swell waves. Spatial information of bottom characteristics provides valuable insights.