

# A-type and B-type internal solitary waves in the northern South China Sea

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# OUTLOOK:

## 1. Motivation

- Introduction into the problem
- The area
- Some preliminary results
- Observational evidence of A and B internal waves

## 2. Analysis of some historical data

## 3. MITgcm modelling of A and B internal waves

- Model set-up
- Comparison with observational data

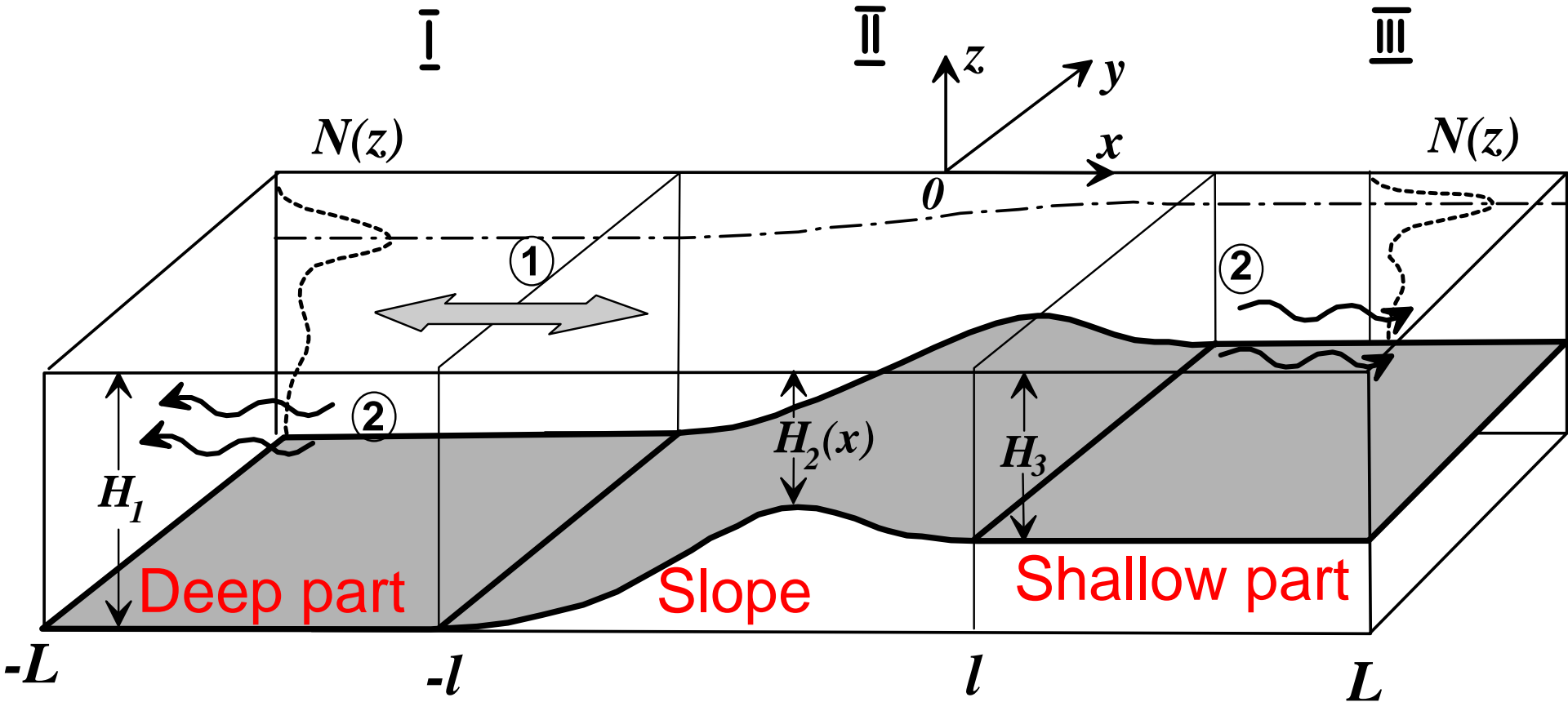
## 4. Analysis and interpretation of the model results

- Generation mechanism
- Multi-harmonic solution
- Evolutionary mechanism

## 5. Conclusions

# 1. Motivation

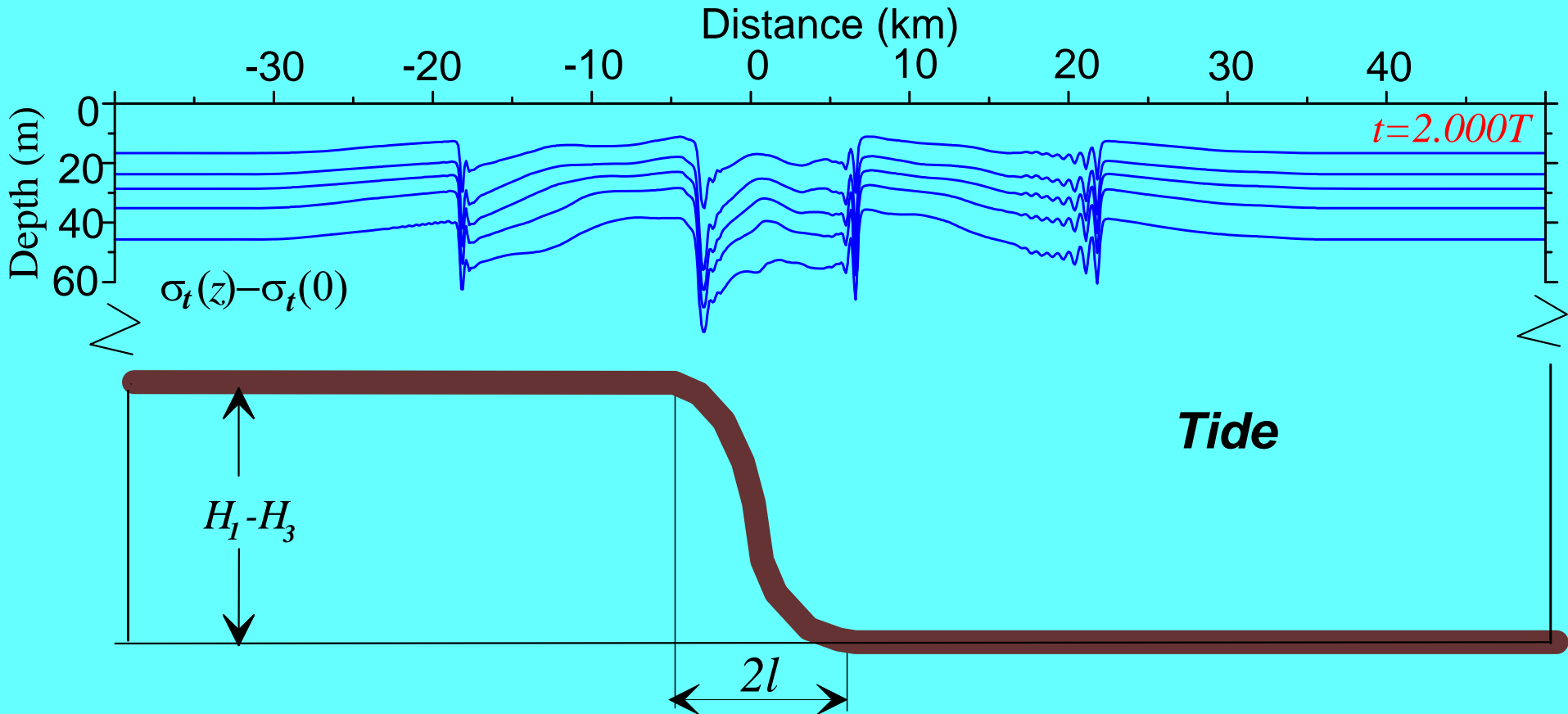
## Generation Mechanism



- 1 Tidal wave
- 2 Internal waves

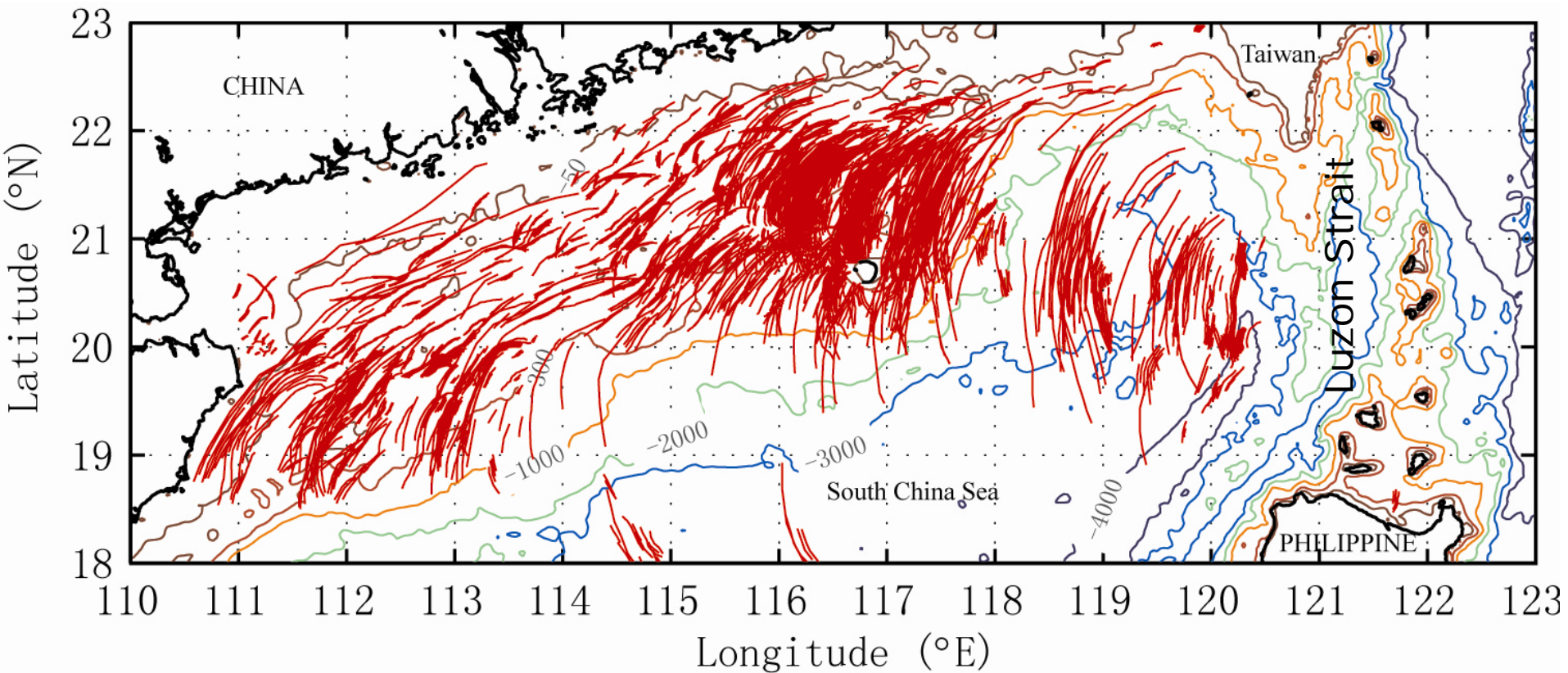
# 1. Motivation

## Generation of nonlinear internal waves



# 1. Motivation

## The area



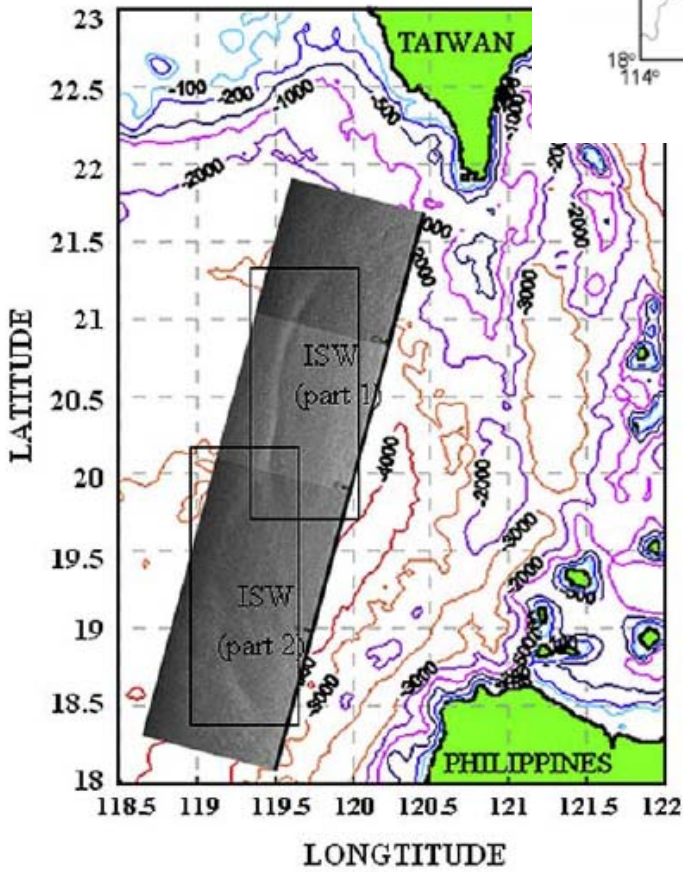
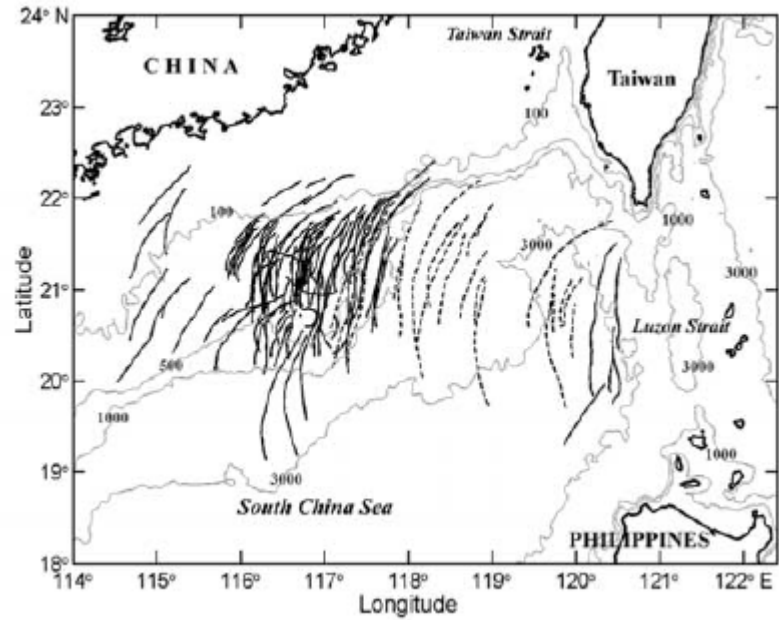
# 1. Motivation

Statistical analysis of SAR images from 1995-2001 (Zheng et al., 2007)

Single internal wave packet (width 2.5 km)

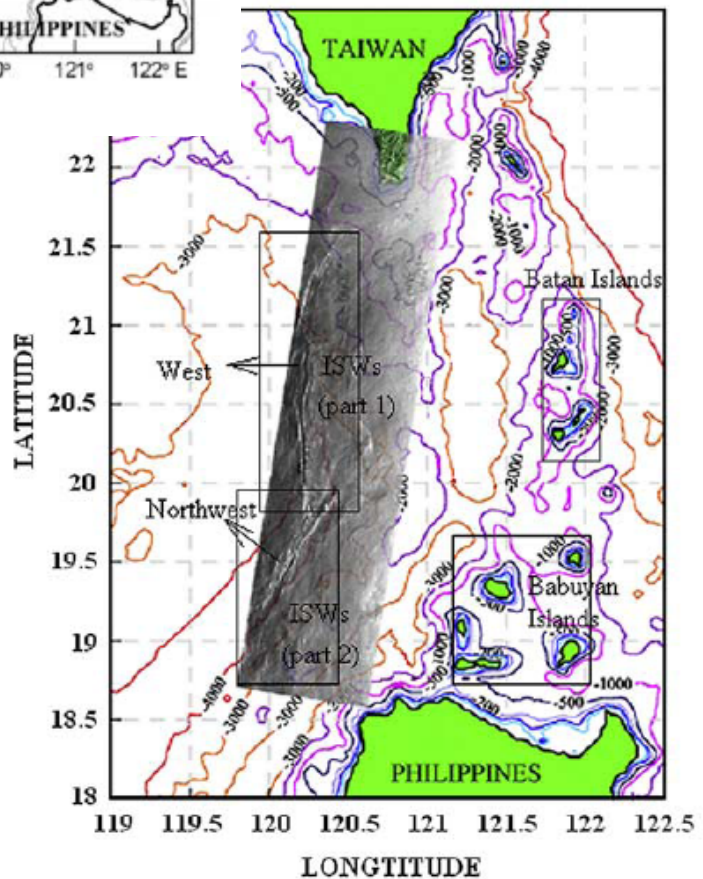
Zhao et al. (2004) compiled a spatial distribution by overlapping their signatures

Multiple internal wave Packets with (width 0.8 km)



Two types of solitary Waves have been identified between 118° and the west of the Luzon Strait

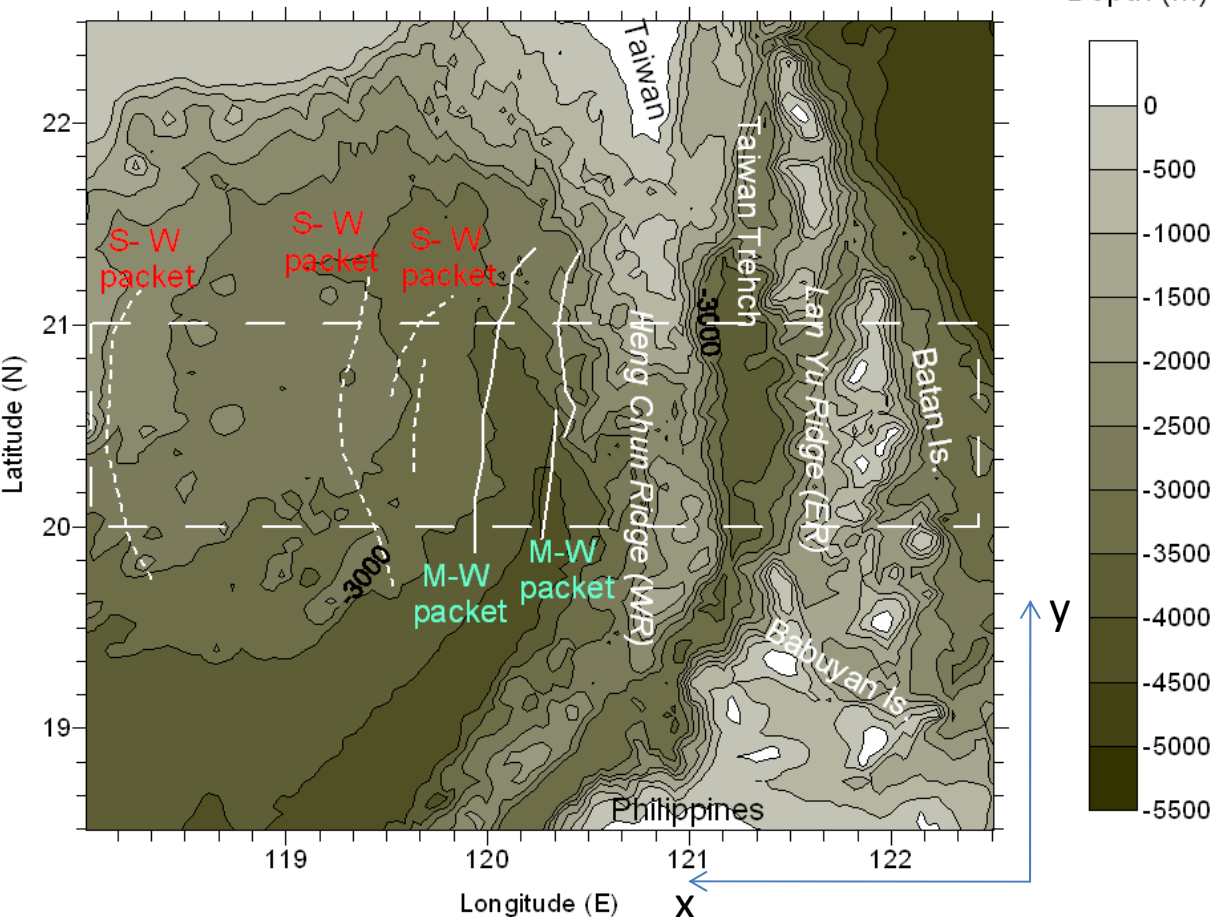
## Two types of ISWs



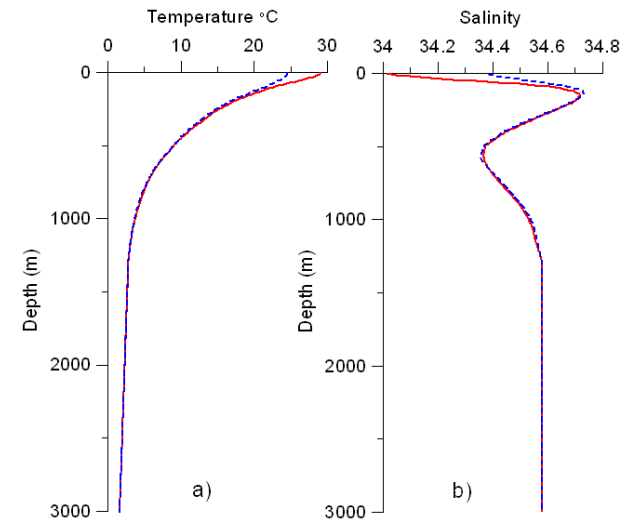
# 1. Motivation

## Preliminary Study

Bottom topography of the Luzon Strait with schematic presentation of multiple wave packets and solitary waves. White rectangle is the model domain  $L_x \times L_y = 670 \times 134 \text{ km}^2$



Averaged temperature and salinity



MITgcm is used

Grid in horizontal directions

$\Delta x = 250 \text{ m}$ ;  $\Delta y = 1000 \text{ m}$

Grid in vertical direction:

$\Delta z = 10 \text{ m}$  in upper 500 m

$\Delta z = 50 \text{ m}$  in the rest of water

Vlasenko, V., Stashchuk, N., Guo, C., Chen, X., 2010. Multimodal structure of baroclinic tides in the South China Sea. *Nonlinear Processes in Geophysics* 17, 529-543.

# Preliminary Study

The tidal dynamics is governed by a superposition of eight principal tidal harmonics: M2, S2, K1, O1, N2, K2, P1, Q1 (Egbert and Erofeeva, 2002). Zu et al. (2008) have shown That the model output for eight harmonics is similar to output with only two of them M2 and K1.

Forcing:

$$F_x = UH_0 / H(x, y) \sigma \cos(\sigma t); \quad F_y = UH_0 / H(x, y) f \sin(\sigma t).$$

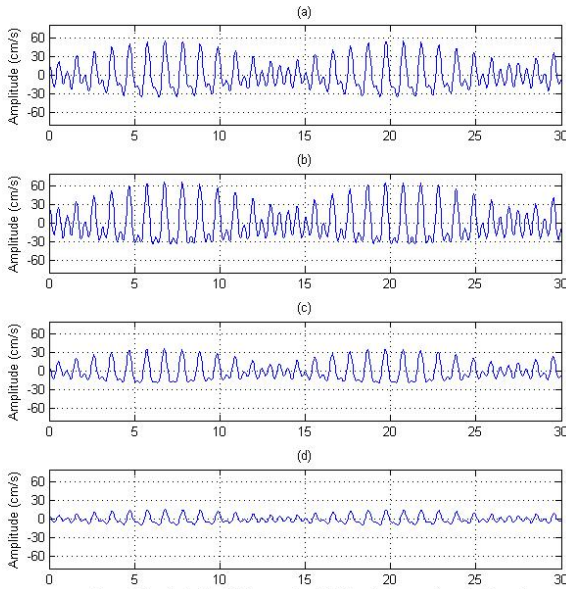
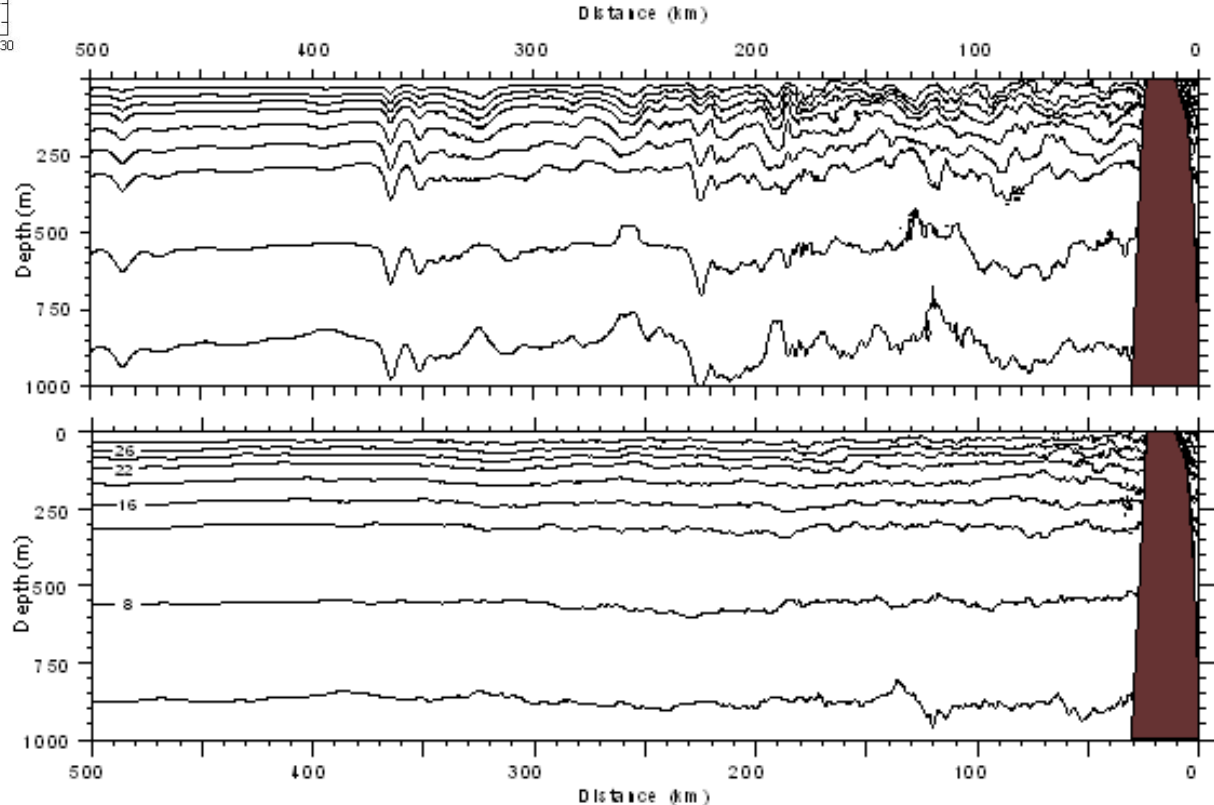


Figure 2 Zonal velocities (u) in a month at 4 different sites as shown in Figure 1:

Zonal velocities in a month at different sites

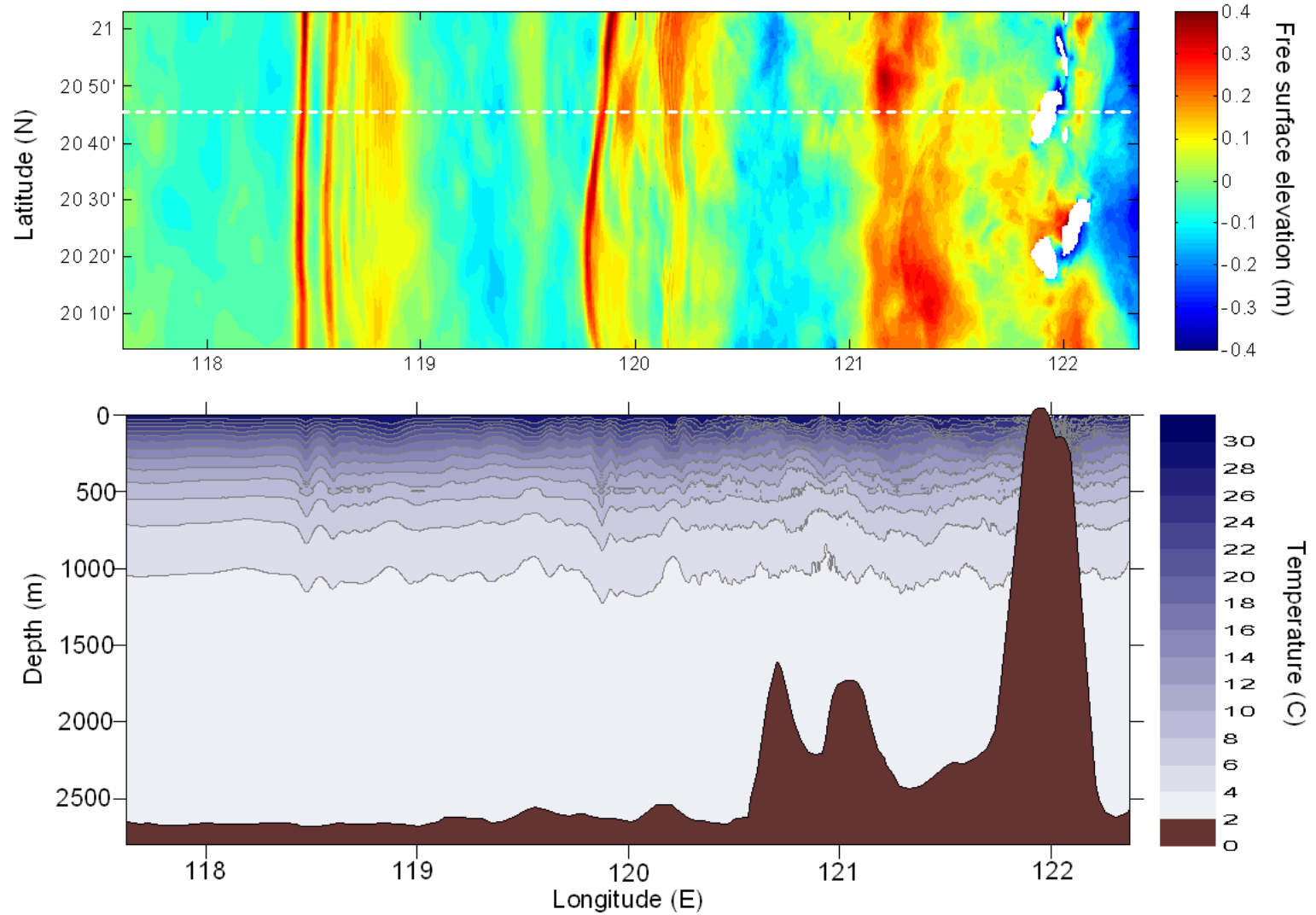
**M<sub>2</sub>**

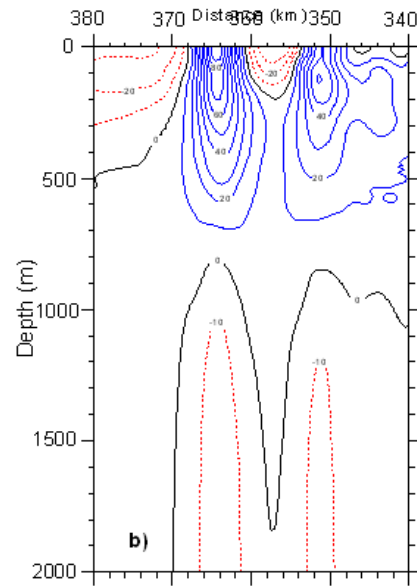
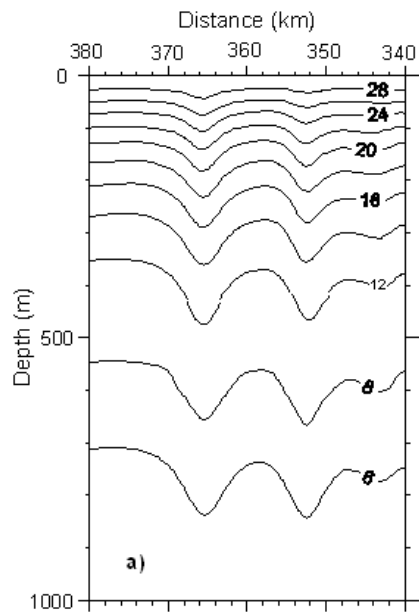
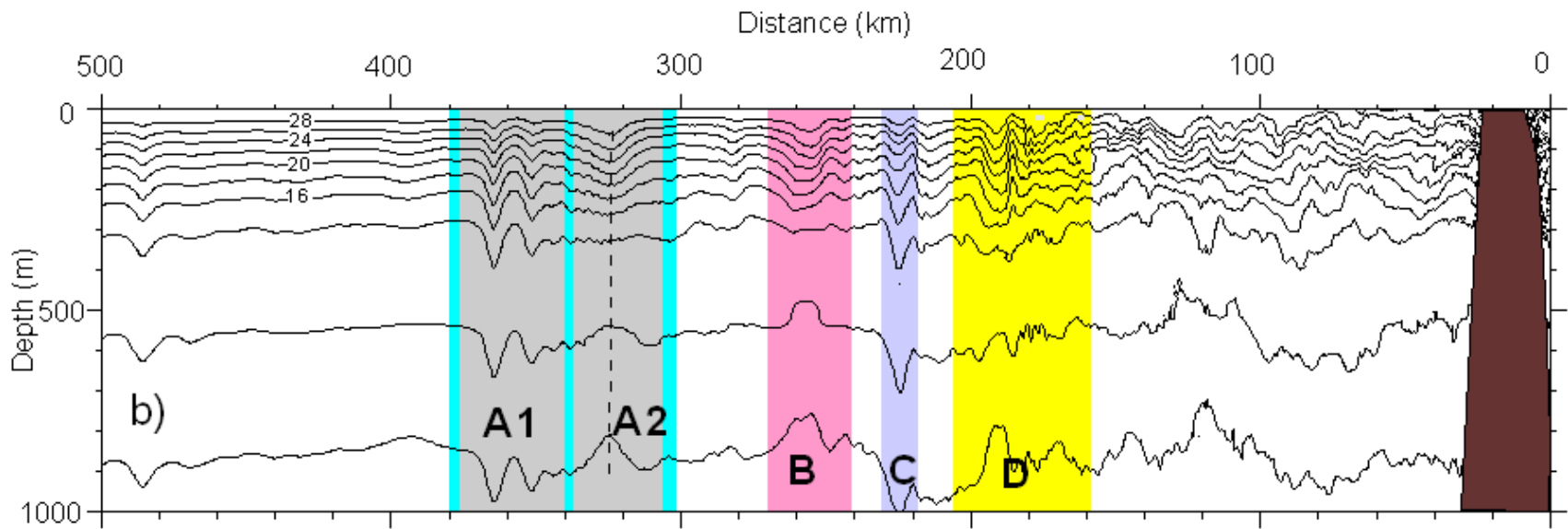
**K<sub>1</sub>**



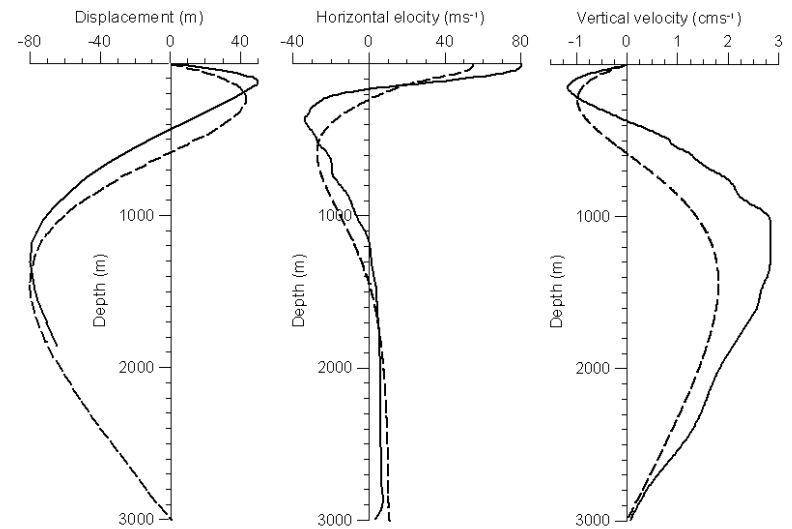


# 3D modelling of baroclinic tides using nonhydrostatic MITgcm





A1



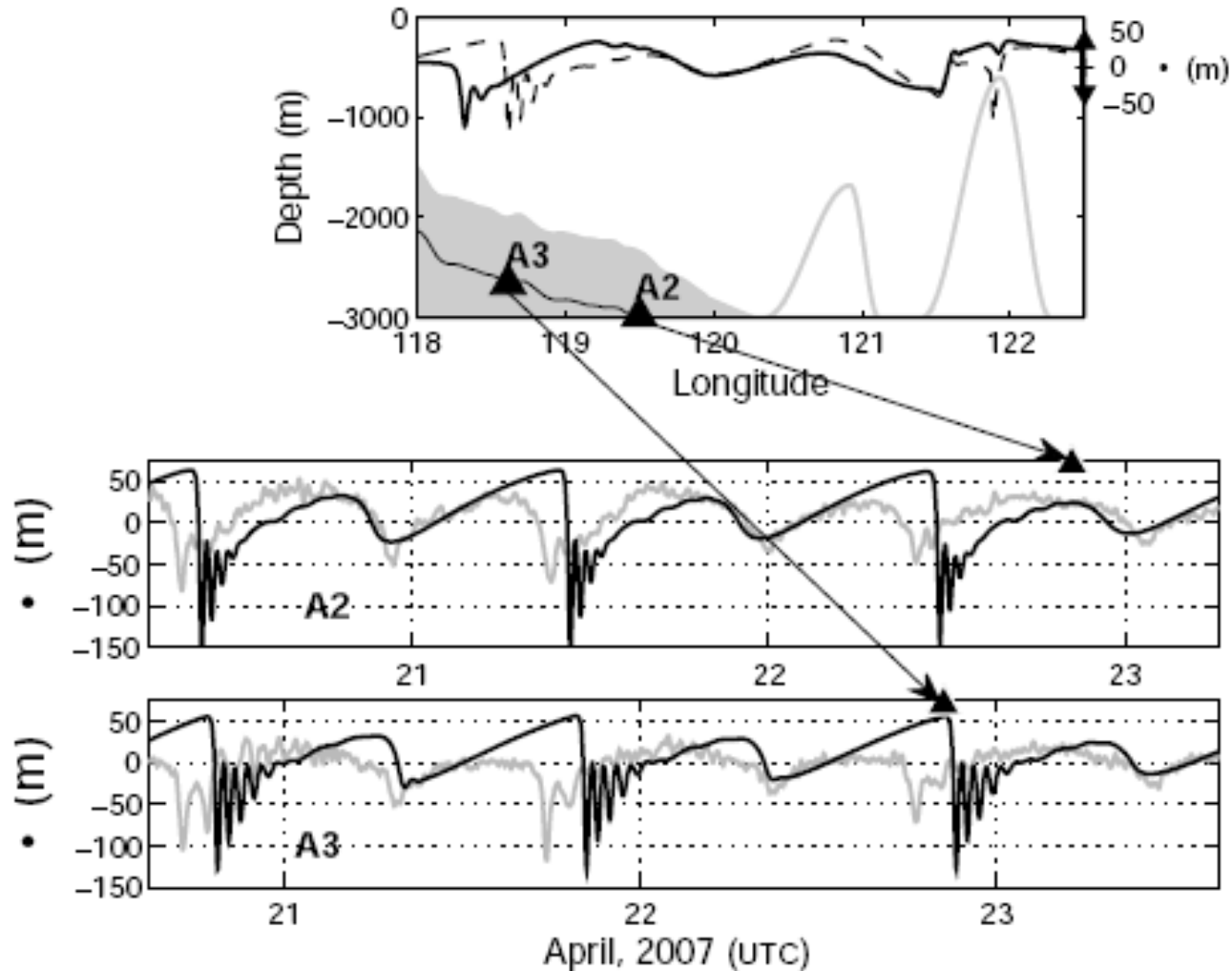
Vertical profile of a second-mode solitary Waves in its centre (fragment A2)

— numerical model; - - - BVP

A pair of first-mode solitary waves (rectangle A1)

# 1. Motivation

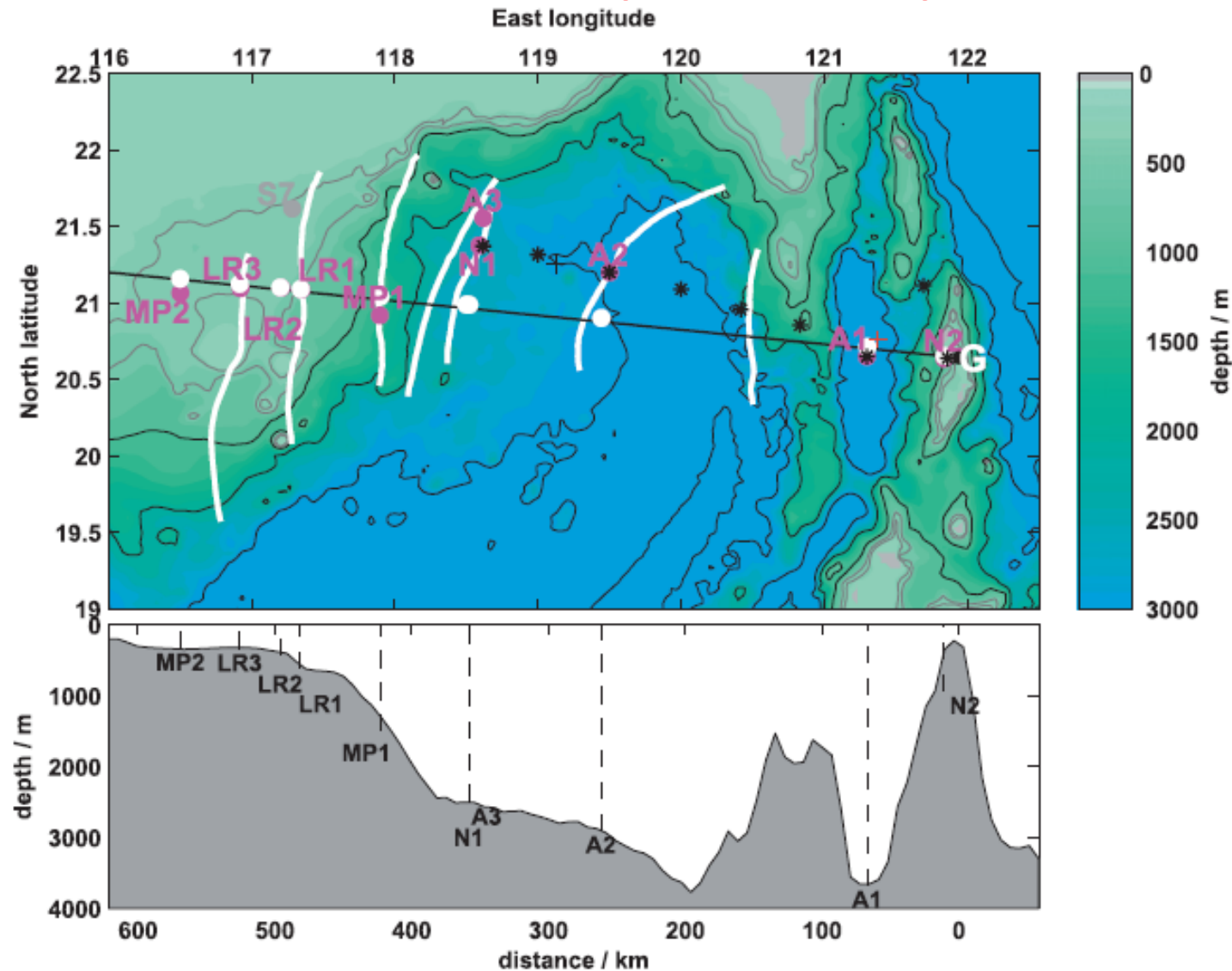
## Observational evidence of A-type and B-type internal waves



Farmer, D., Li, Q., Park, J.-H., 2009. Internal wave observations in the South China Sea: the role of rotation and non-linearity. *Atmos.-Ocean* 47(4), 267-280.

# 1. Motivation

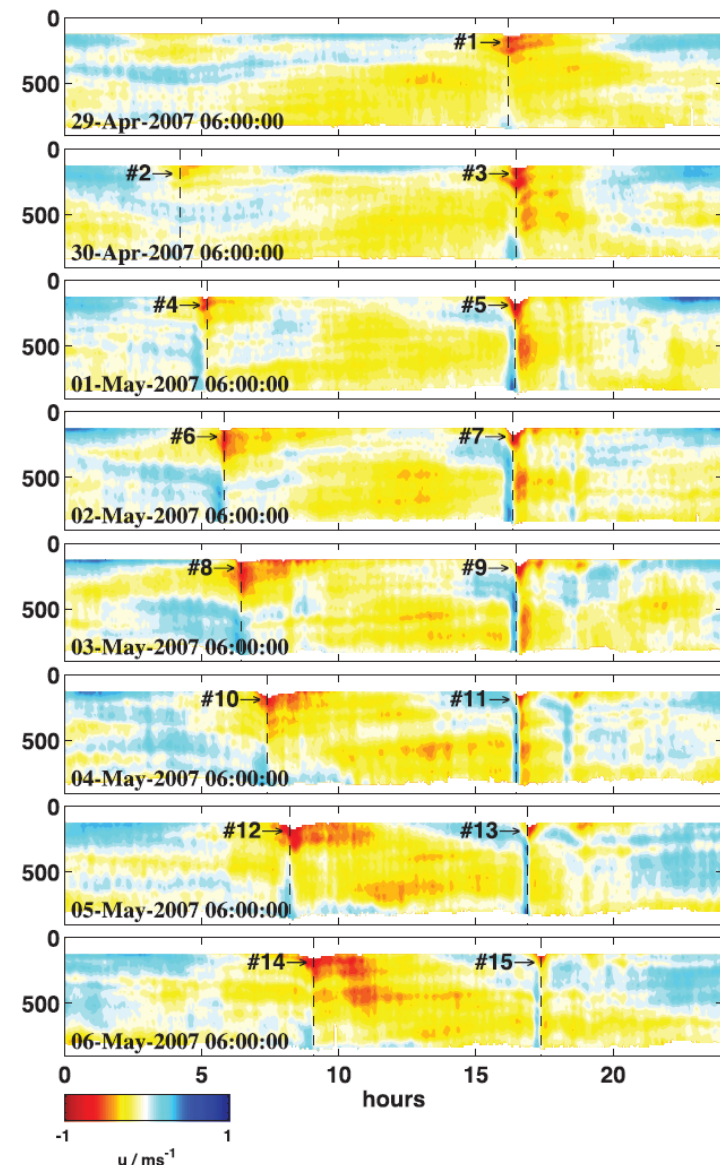
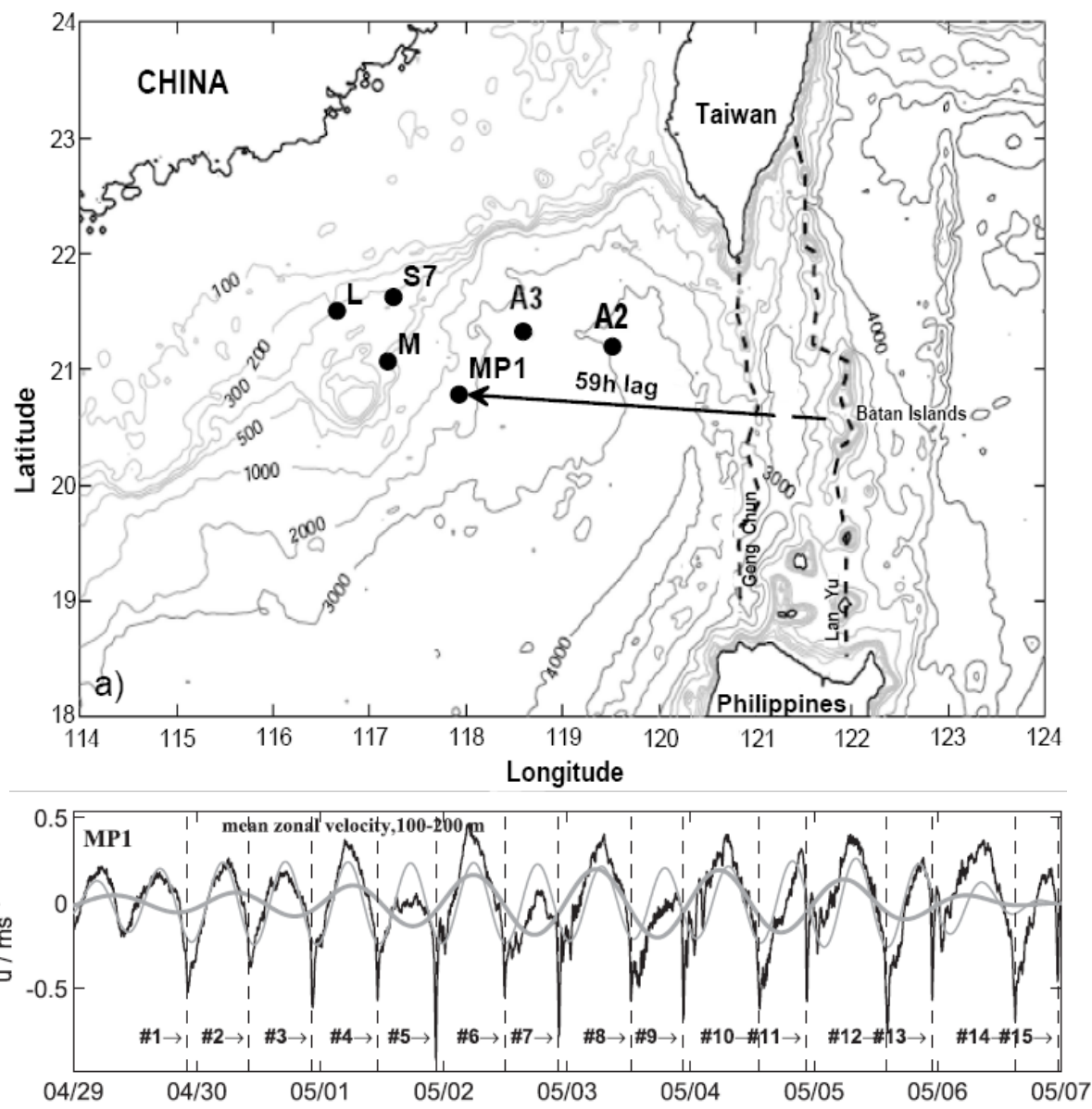
## Observational evidence of A-type and B-type internal waves



Alford, M., Lien, R., Simmons, H., Klymak, J., Ramp, S., Yang, Y., Tang, D., Chang, M., 2010. Speed and evolution of nonlinear internal waves transiting the South China Sea. JPO, 40,1338-

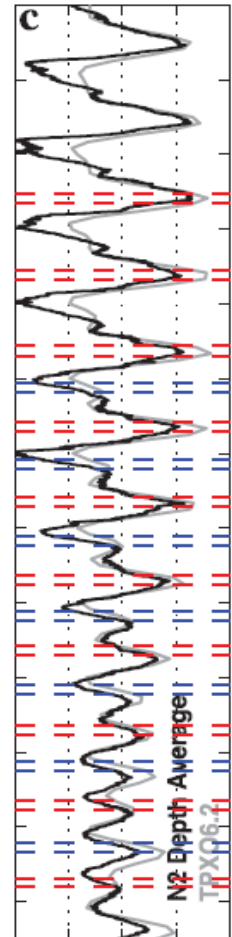
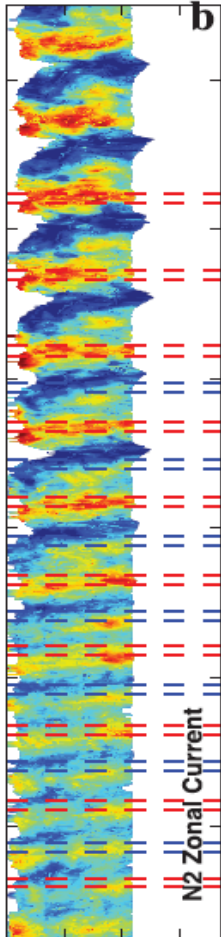
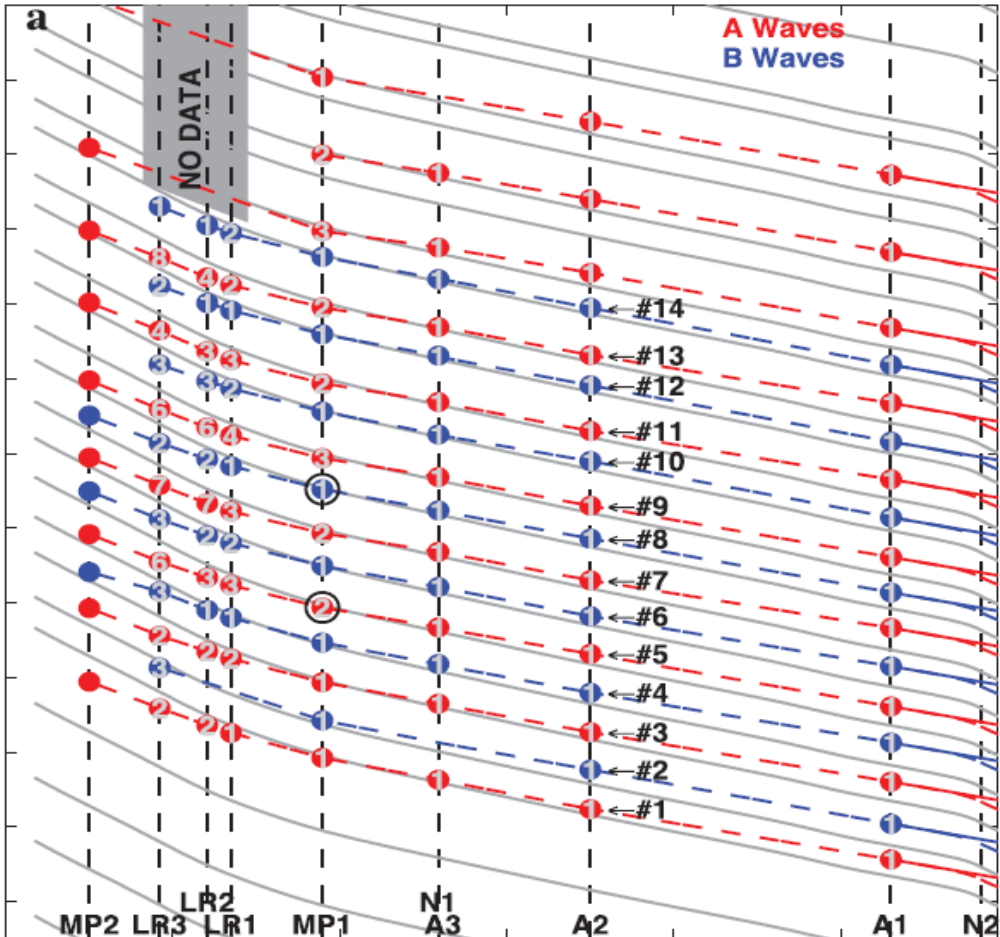
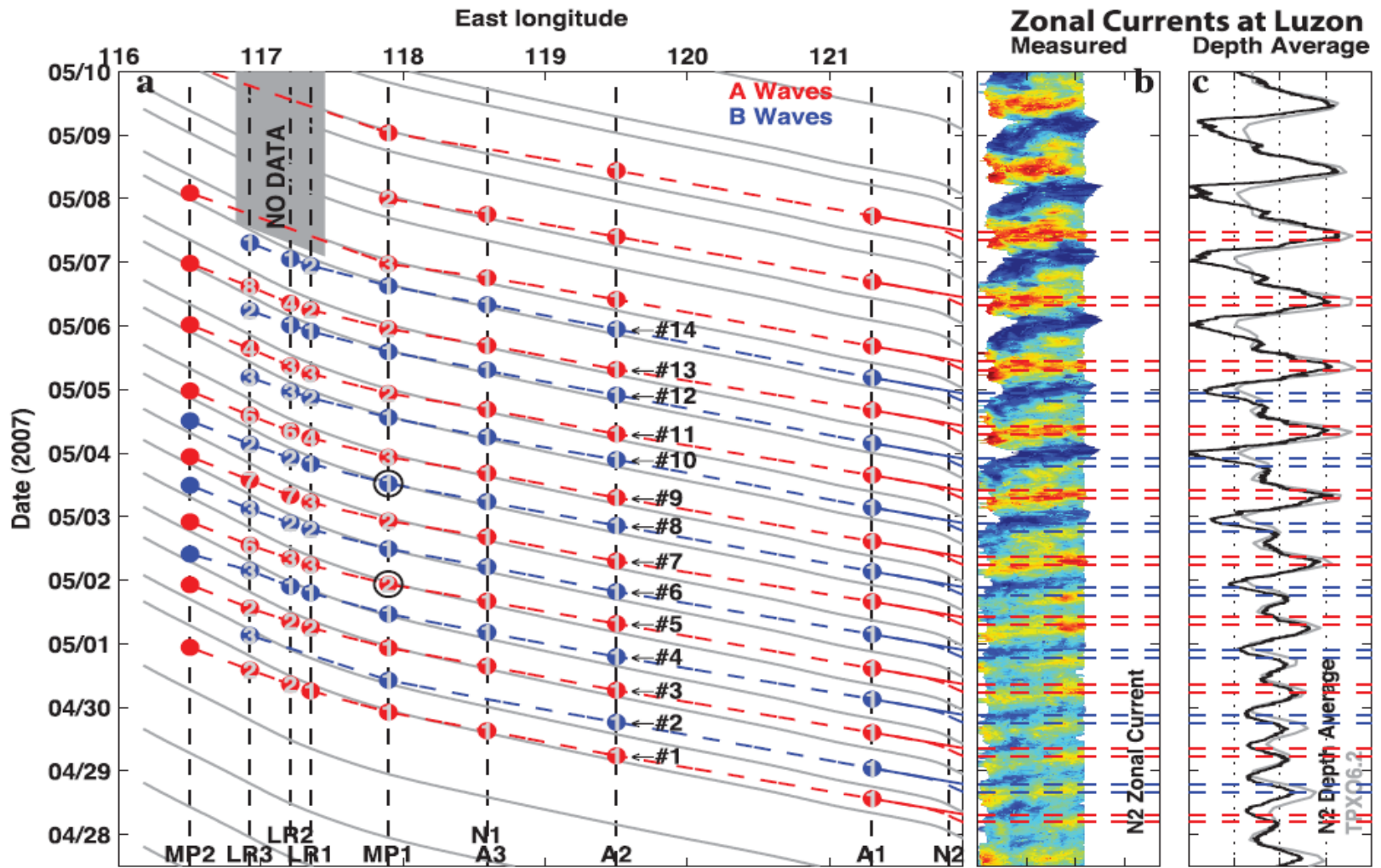
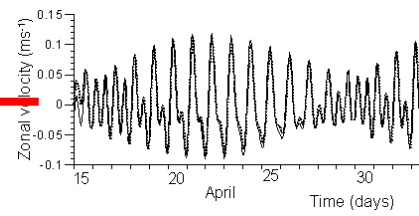
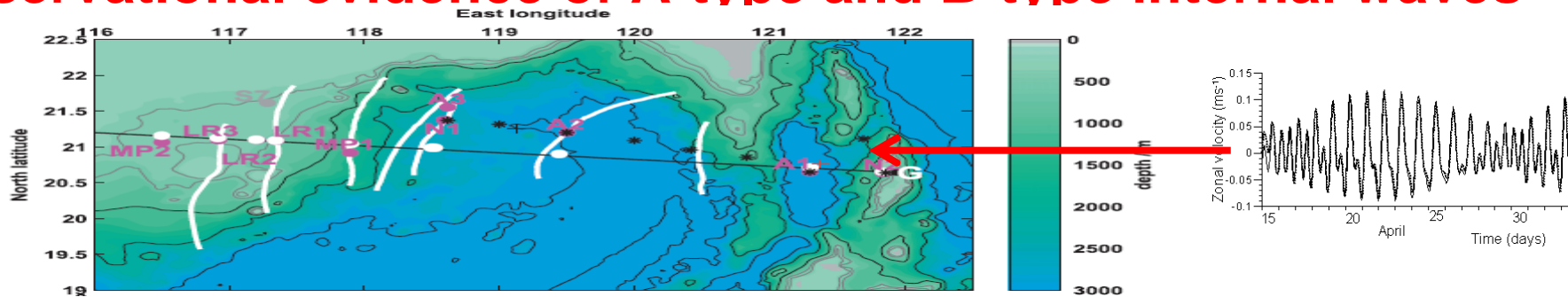
# Observational evidence of A-type and B-type internal waves

ADCP data at point MP1

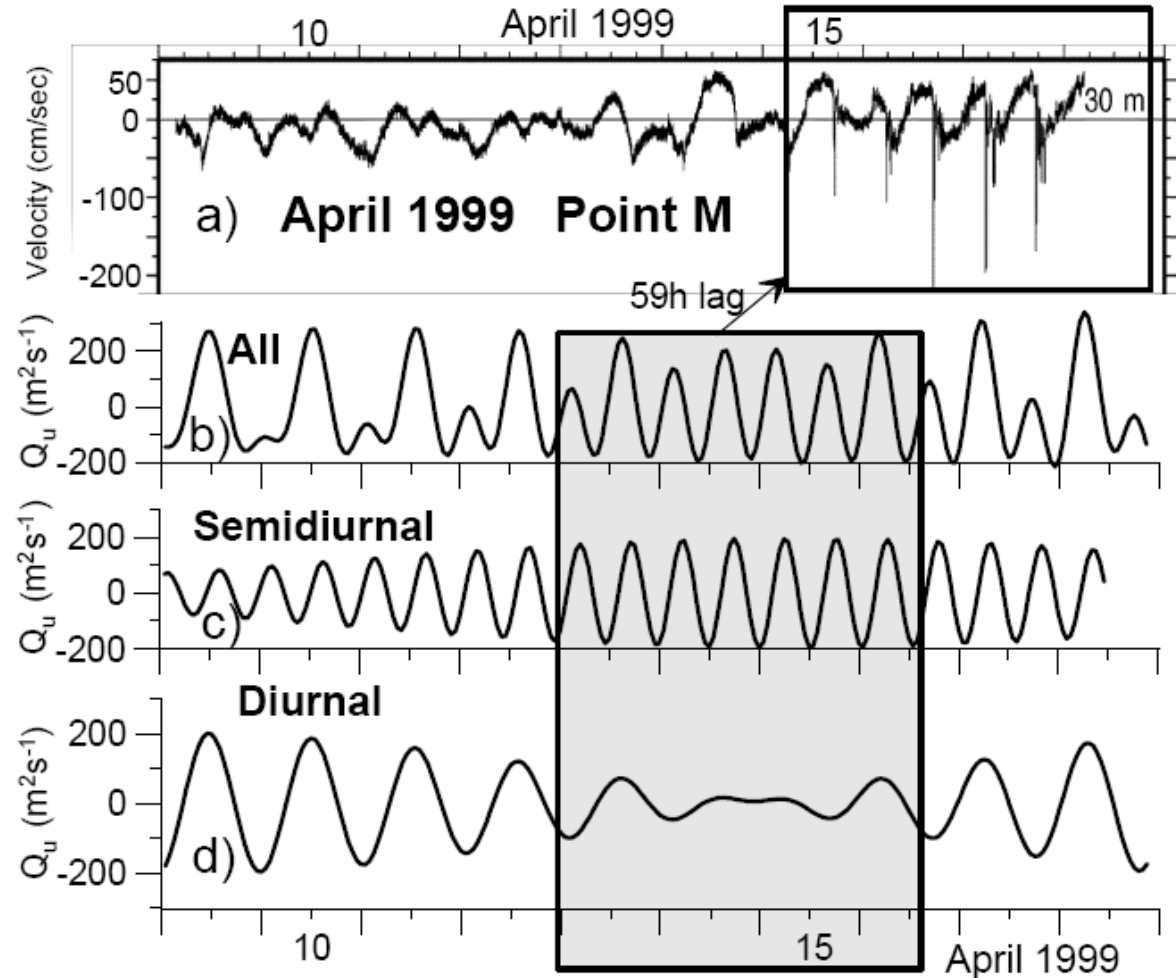
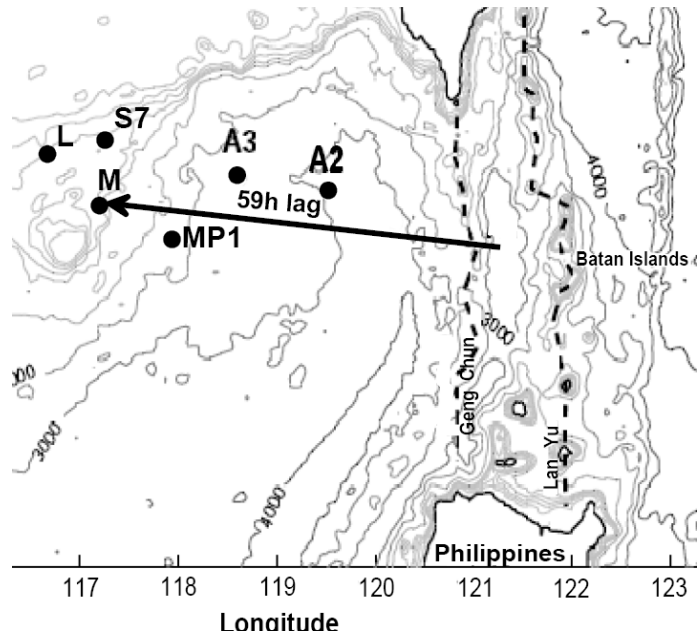


Ramp et al., IEEE J. Ocean. Engineering, 2004.  
Alford et al., Journal of Physical Oceanography, 2010.

# Observational evidence of A-type and B-type internal waves

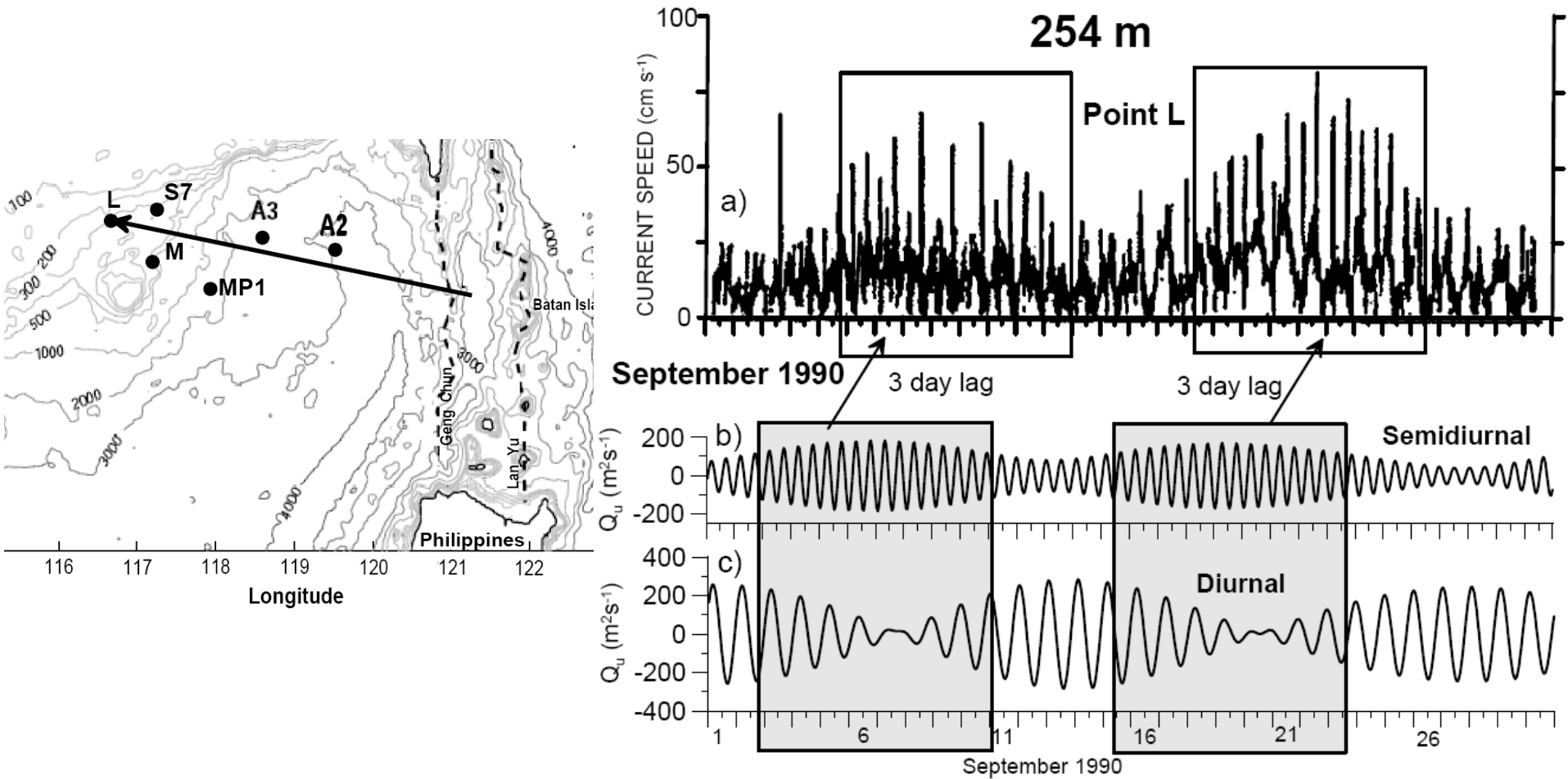


## 2. Analysis of some historical data: point M



Yang, Y.-J., Tang, T. Y., Chang, M. H., Liu, A. K., Hsu, M.-K., Ramp, S.R., 2004. Solitons northeast of Tung-Sha Island during the ASIAEX pilot studies. IEEE J. Ocean. Engineering 29(4), 1182-1315.

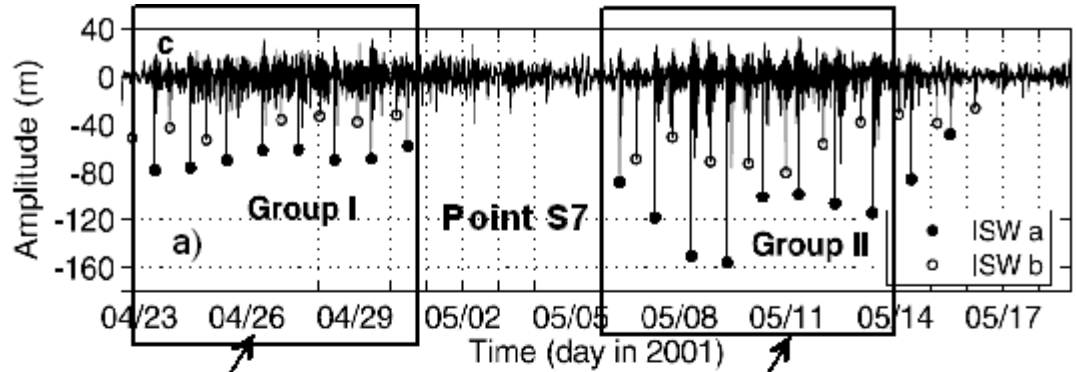
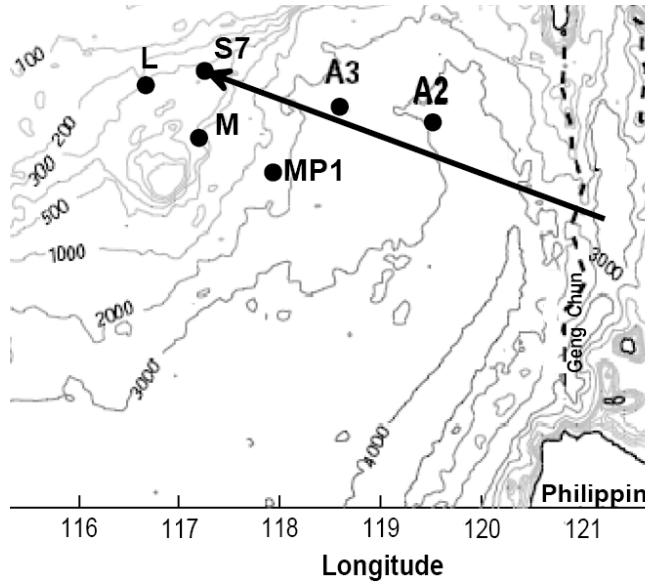
# Analysis of some historical data: Point L



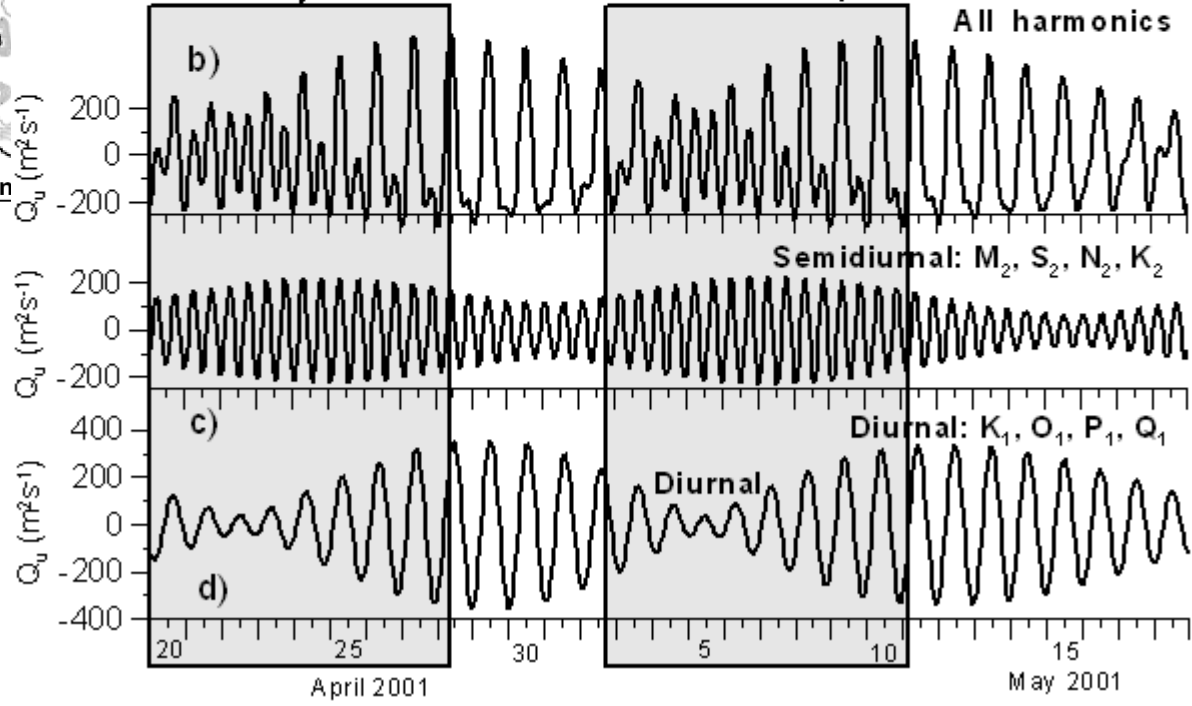
Ebbersmeyer, C.C., Coomes, C.A., Hamilton, R.C., Kurrus, K.A., Sullivan, T.C., Salem B.L., Romea, R.D., Bauer, R.J., 1991. New observations of internal waves (solitons) in the South China Sea using an acoustic Doppler current profiler. In: Proceedings of Marine Technology Society Conference, New Orleans, May 1991, 165-175.



# Analysis of some historical data: Point S7

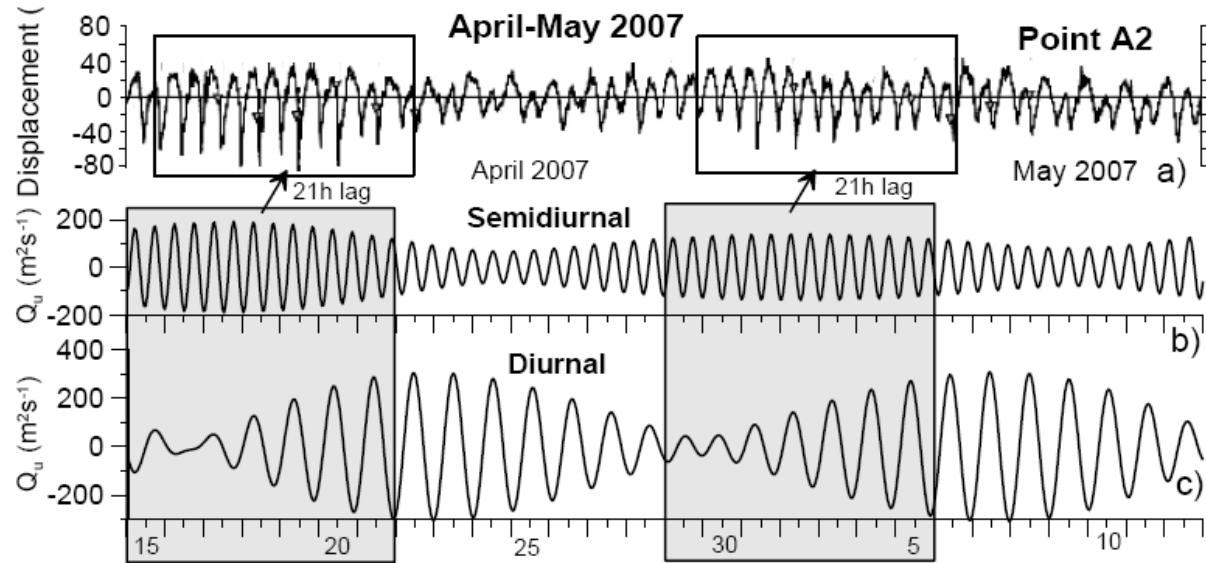
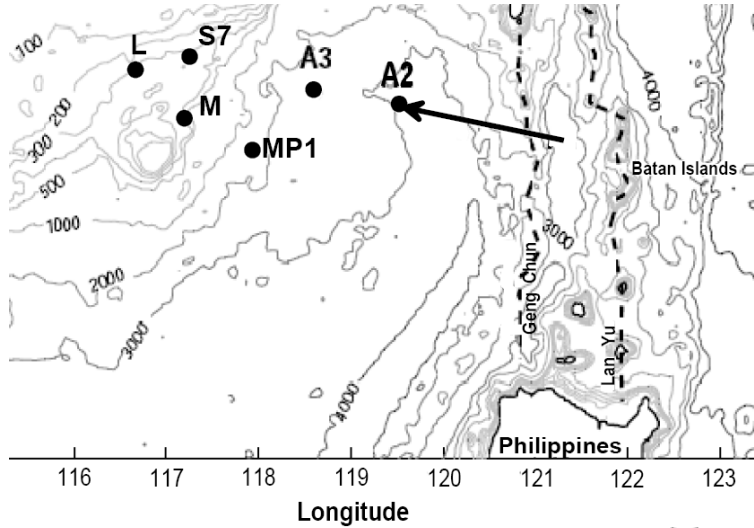


**April-May 2001**



Zhao, Z., Alford, M. H., 2006. Source and propagation of internal solitary waves in the northeastern South China Sea. *Journal of Geophysical Research* 111, C11012, doi:10.1029/2006JC003644.

# Analysis of some historical data: Point A2

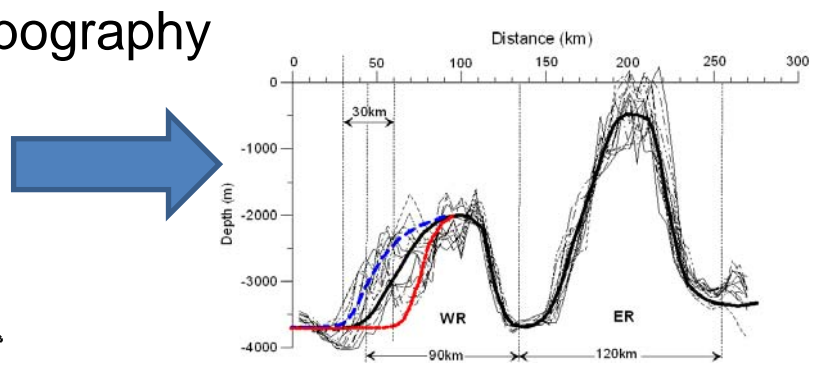
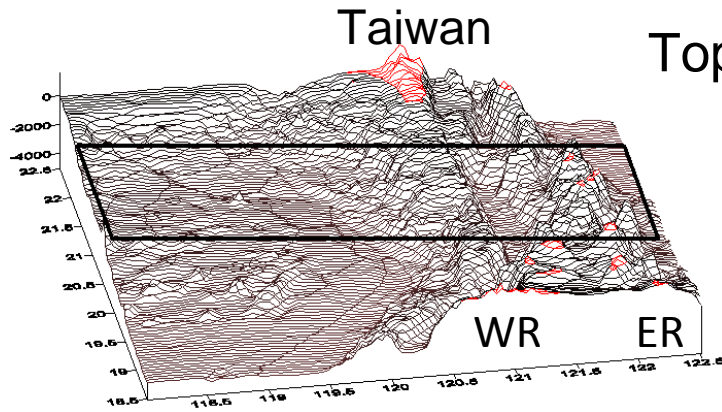


Farmer, D., Li, Q., Park, J.-H., 2009. Internal wave observations in the South China Sea: the role of rotation and non-linearity. *Atmos.-Ocean* 47(4), 267-280.

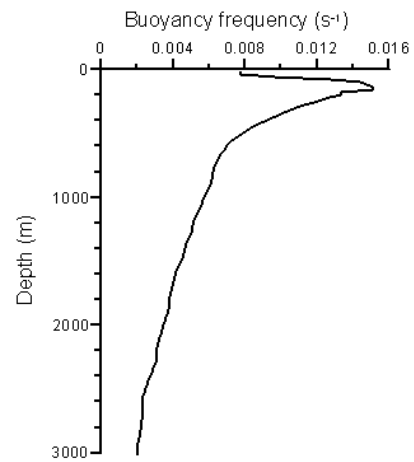
### **3. MITgcm modelling of A and B internal waves**

- **Model set-up**
- **Comparison with observational data**

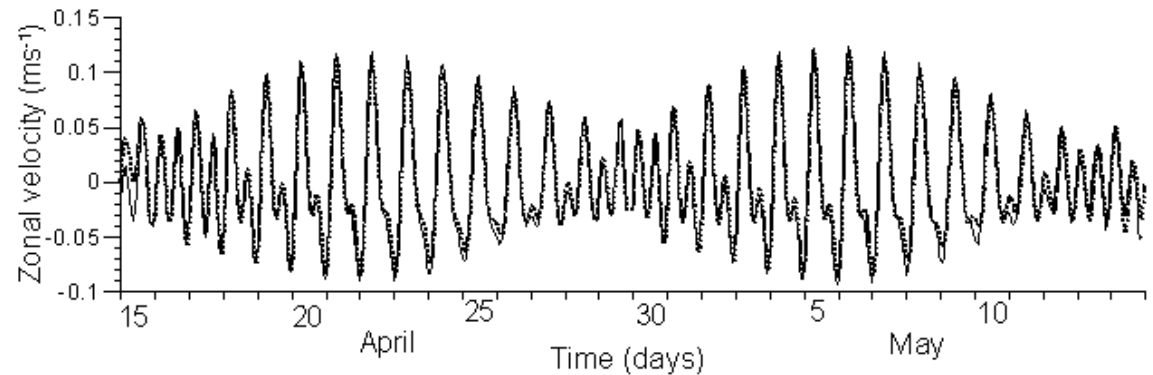
# 3. MITgcm modelling of A and B waves: Model set-up



## Stratification

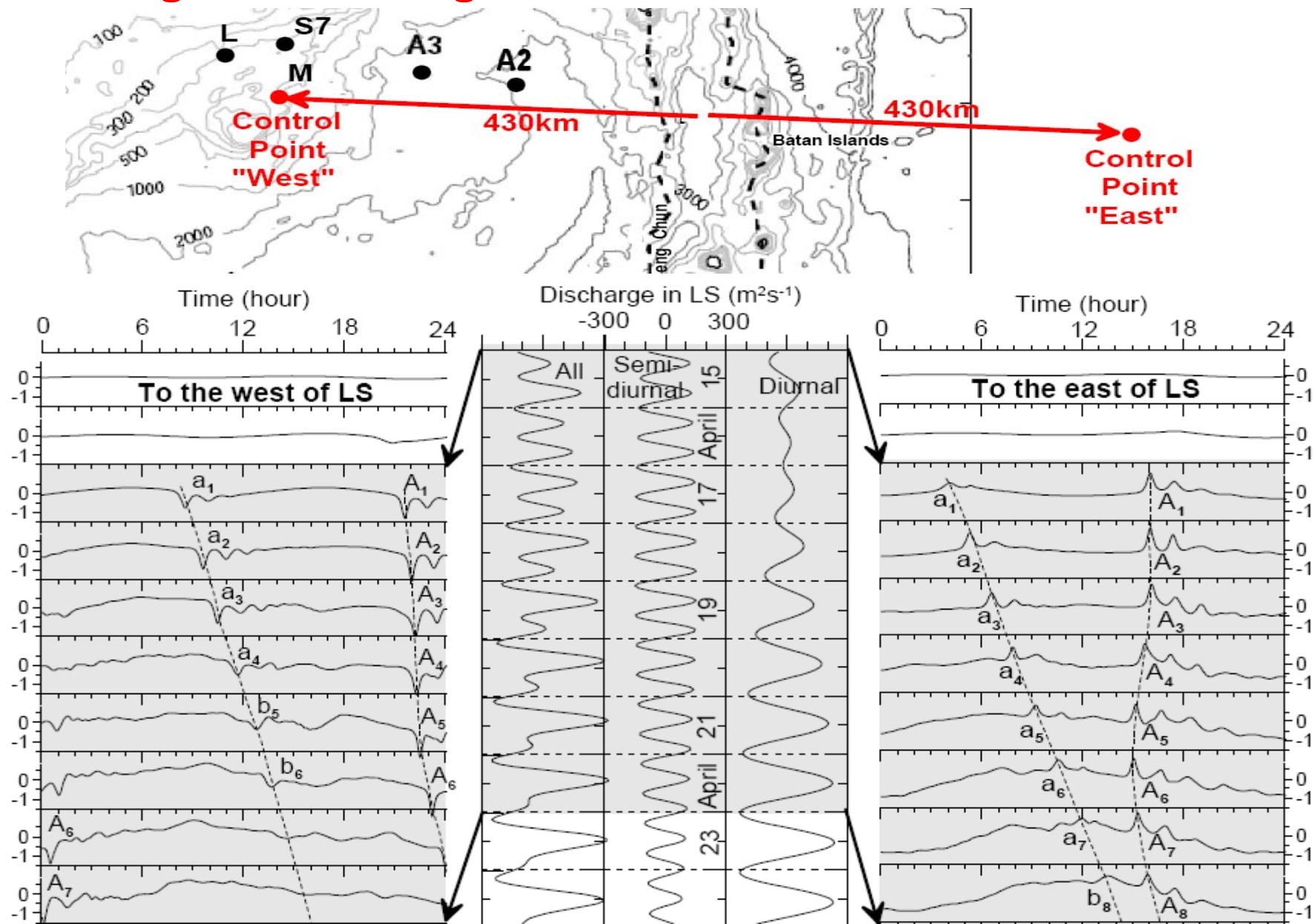


## Forcing



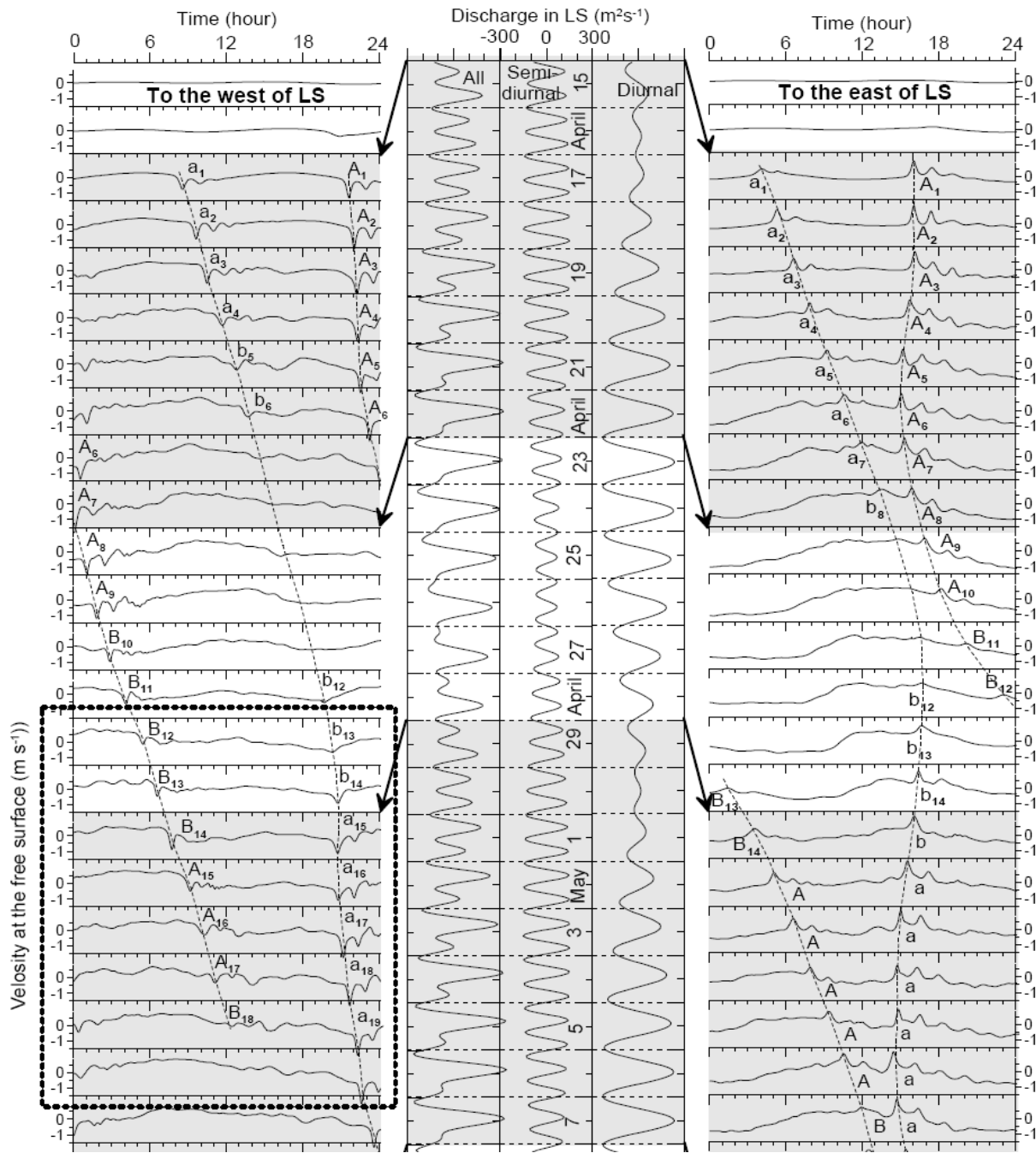
Resolution: Grid in horizontal direction:  $\Delta x=250$  m;  
Grid in vertical direction:  $\Delta z=10$  m in upper 500 m;  $\Delta z=20$  m for the next 20 layers;  
 $\Delta z=150$ m in the bottom layers.

### 3. MITgcm modelling of A and B waves: Results

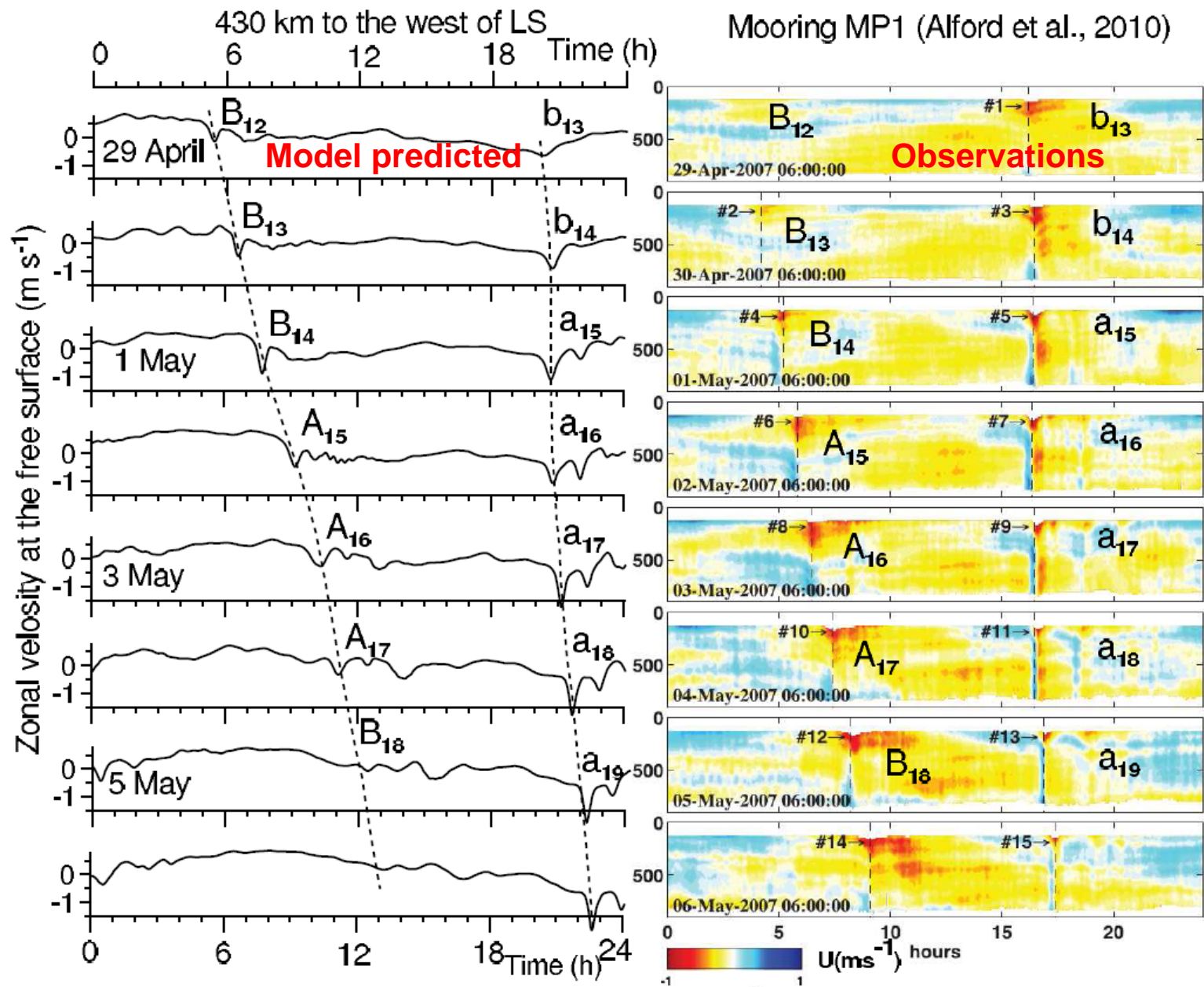


Time series of horizontal velocity on the surface  $u(x_a, 0, t)$  at two control points, "West" and "East".

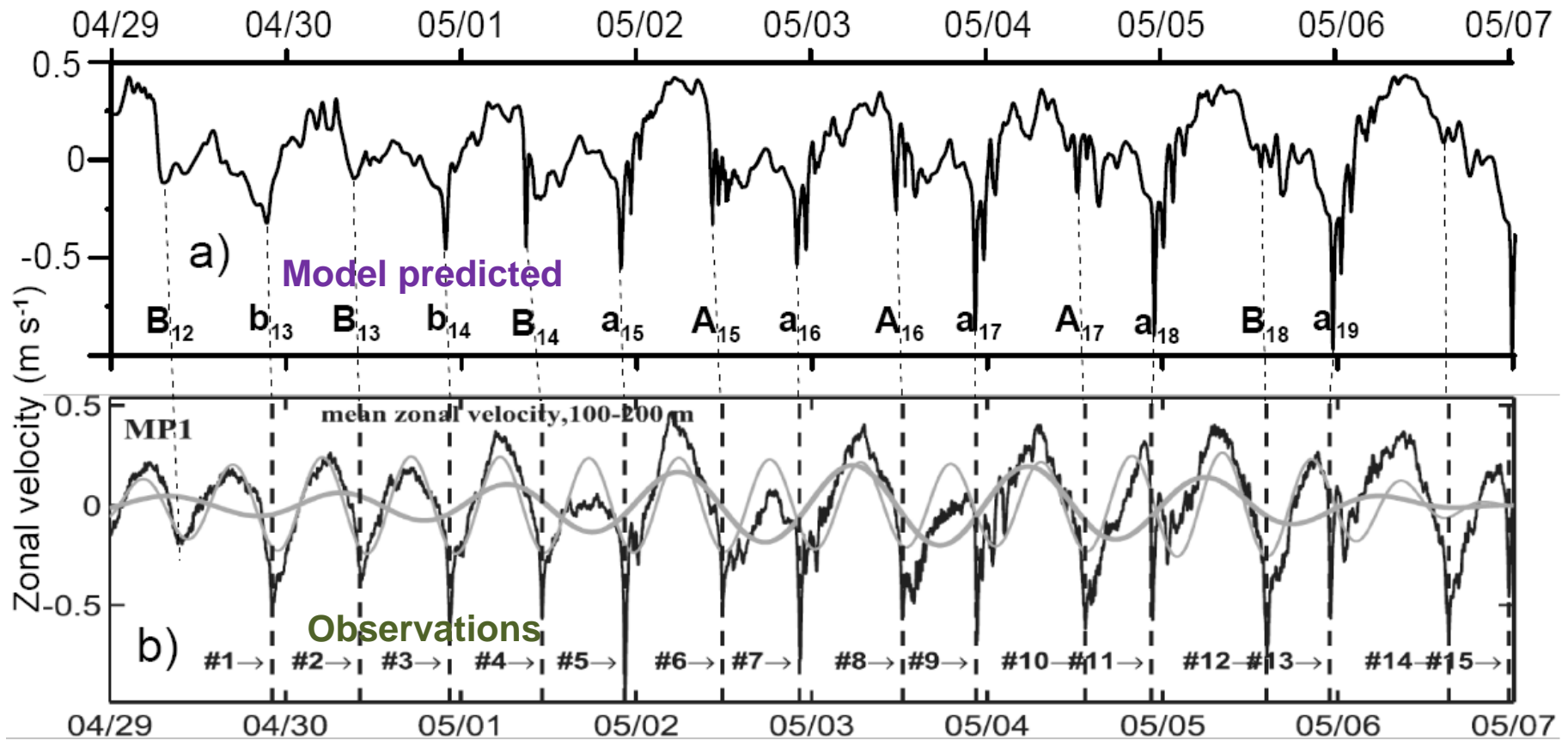
# 3. Long-term MITgcm modelling of A and B waves: Results



### 3. Comparison of the model output with observational data



### 3. Comparison of the model output with observational data





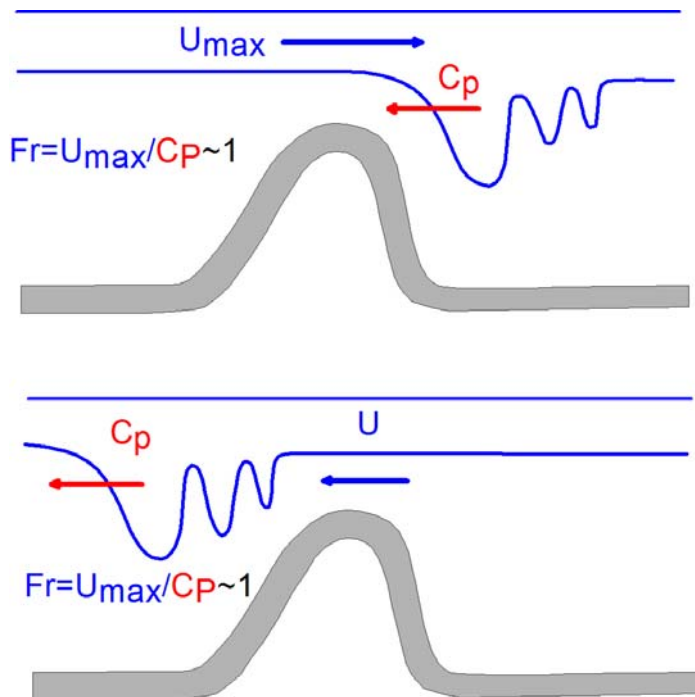
## **4. Analysis and interpretation of the model results**

- **Generation mechanism**
- **Multi-harmonic solution**
- **Evolutionary mechanism**

## 4a. Generation mechanisms

**“Release”** mechanism:  $Fr \sim 1$

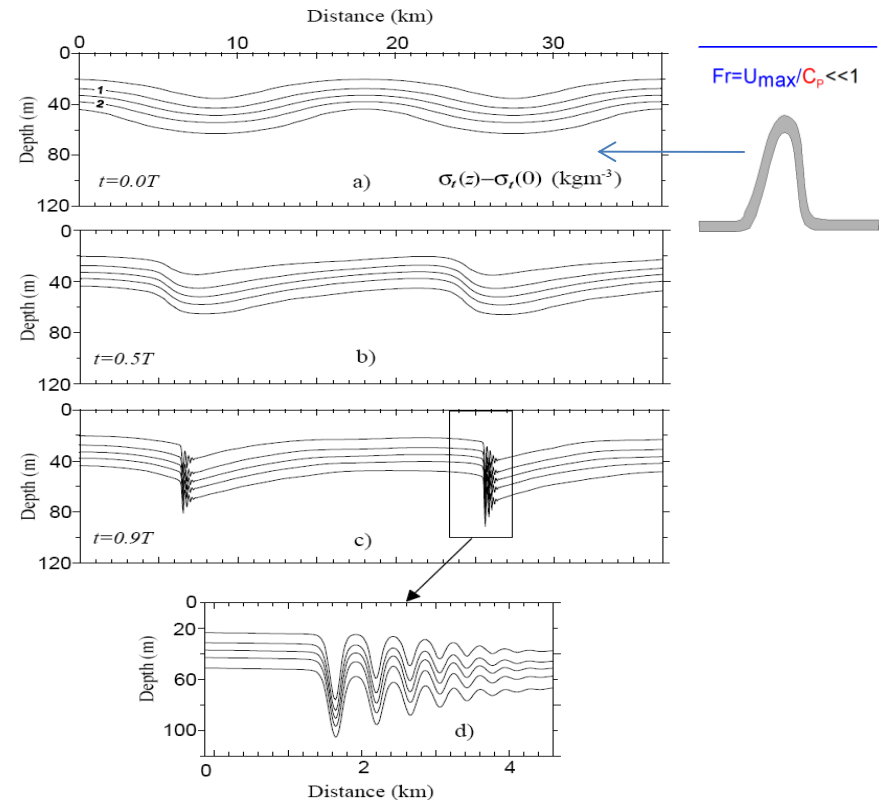
Lee waves are generated downstream the ridge and radiated when flow slackens



$$\frac{dF}{dt} = \frac{\partial F}{\partial t} + U \frac{\partial F}{\partial x}$$

**“Evolutionary”** mechanism:  $Fr \ll 1$

Steepening and disintegration of long internal tidal waves into packets of ISWs



# Linear theory prediction for ONE particular frequency $\sigma$

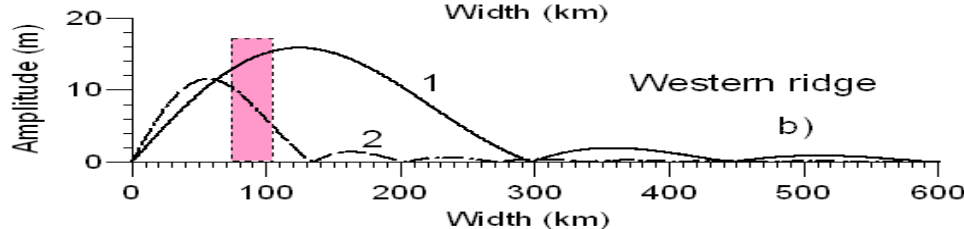
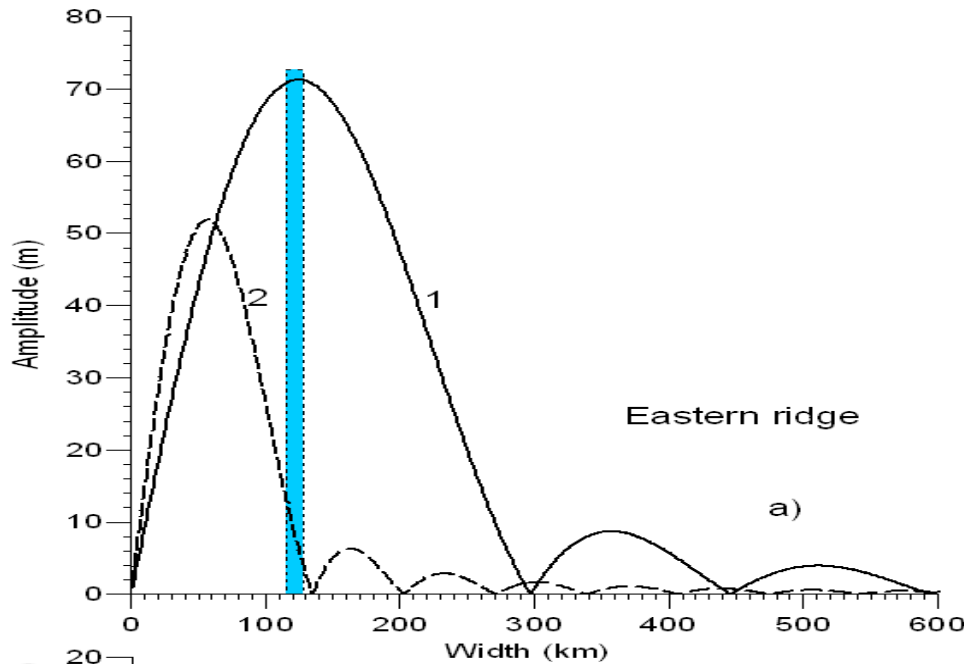
Analytical solution for idealised ridge  
(Vlasenko et al. 2005)

$$\Psi_{xx} - \frac{\sigma^2 - f^2}{N^2(z) - \sigma^2} \Psi_{zz} = 0,$$

$$\Psi = \Psi_m, \quad z = 0,$$

$$\Psi = 0, \quad z = -H(x),$$

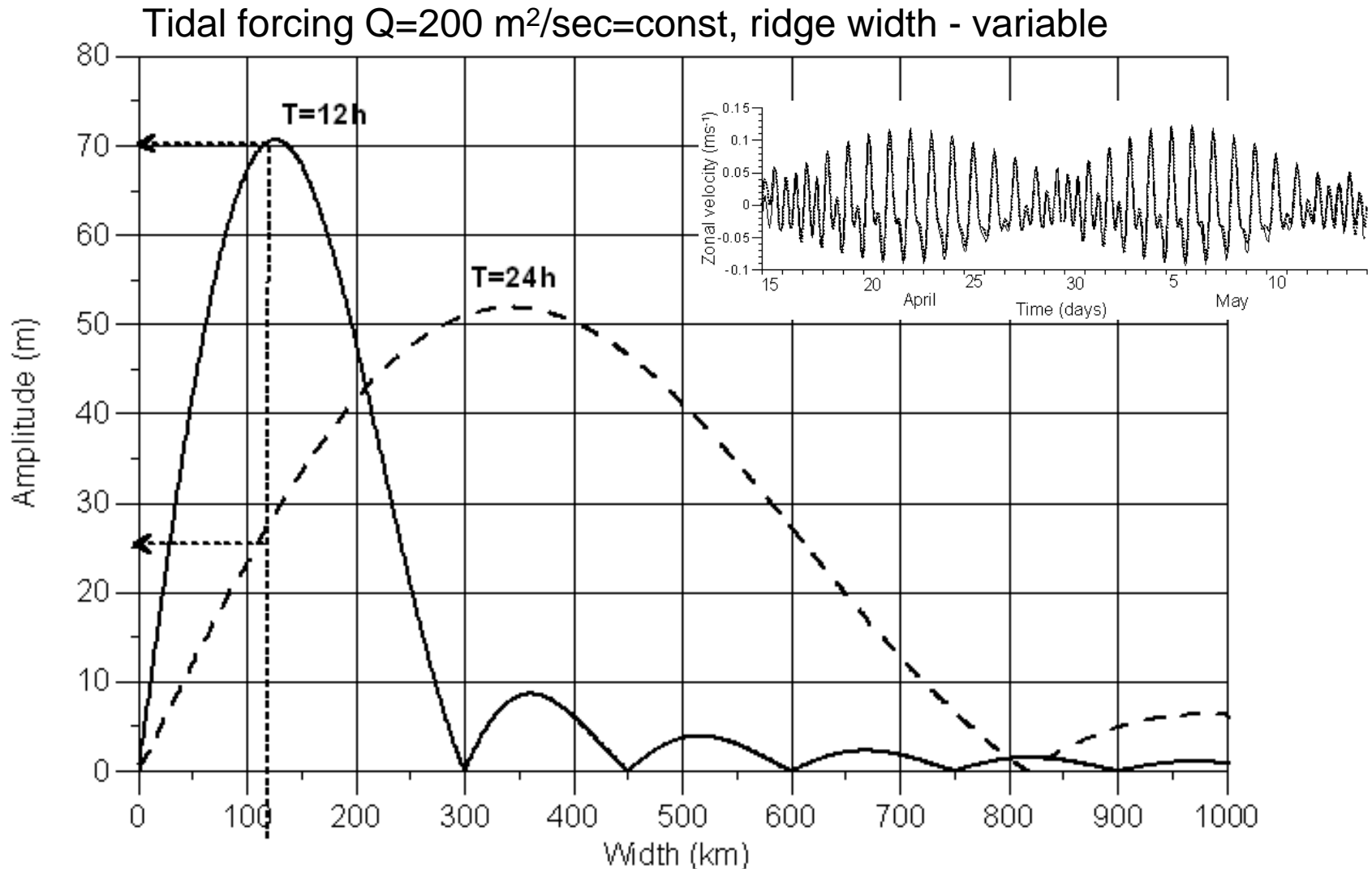
$$\Psi(x, z, t) = \Psi_m(1 + z/H) \exp(-i\sigma t) + \sum_{j=1}^{\infty} a_j g_j(z) \exp[i(k_j x - \sigma t + \varphi_j)].$$



Resonant generation of modes

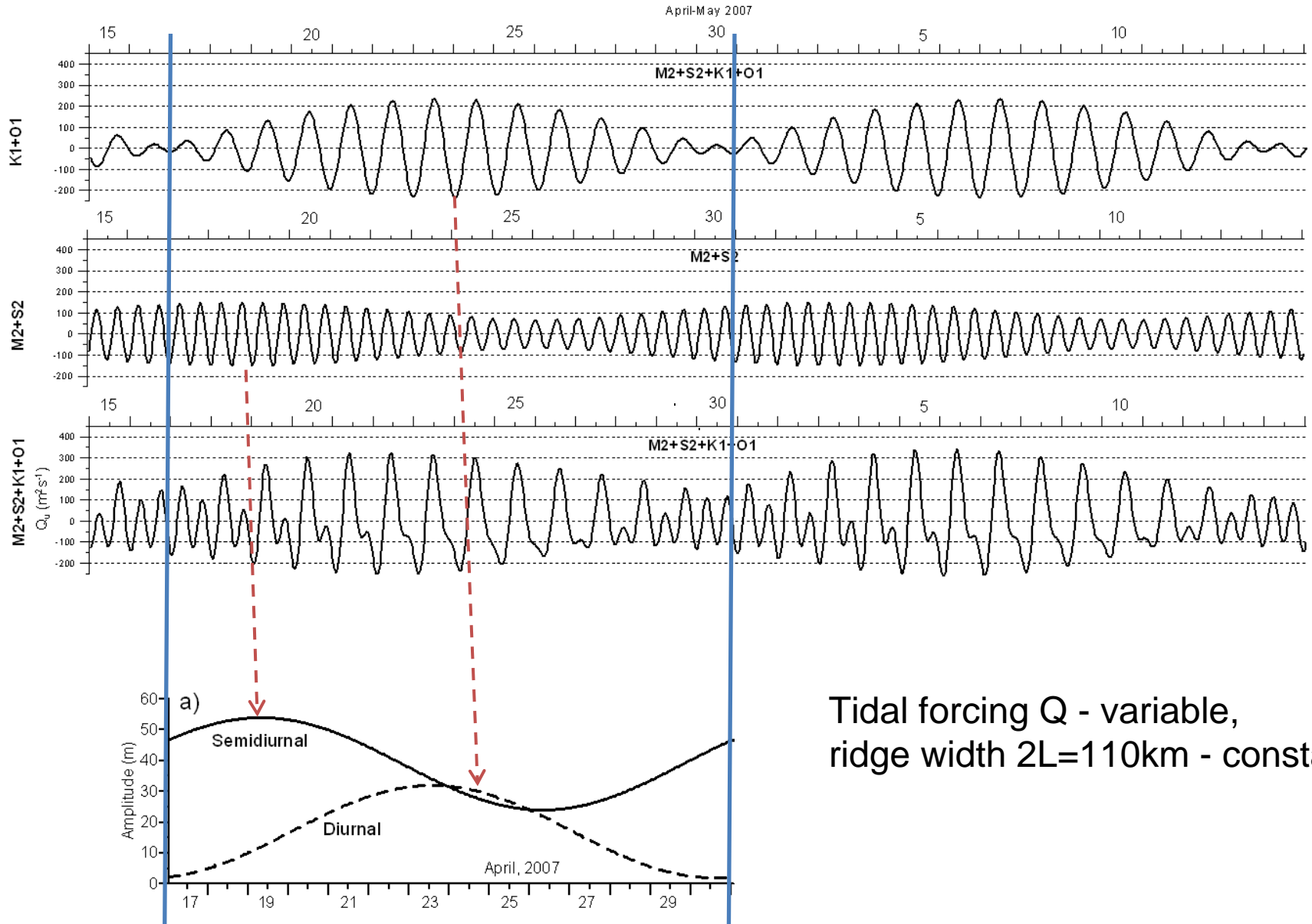
Second-mode amplitude for two ridges

# Linear theory prediction for TWO tidal harmonics: semidiurnal and diurnal



Linear theory prediction for the generation of the first-mode baroclinic tide in the South China Sea by the semidiurnal and diurnal barotropic tide ( $Q=200\text{m}^2/\text{sec}$  in the Luzon Strait)

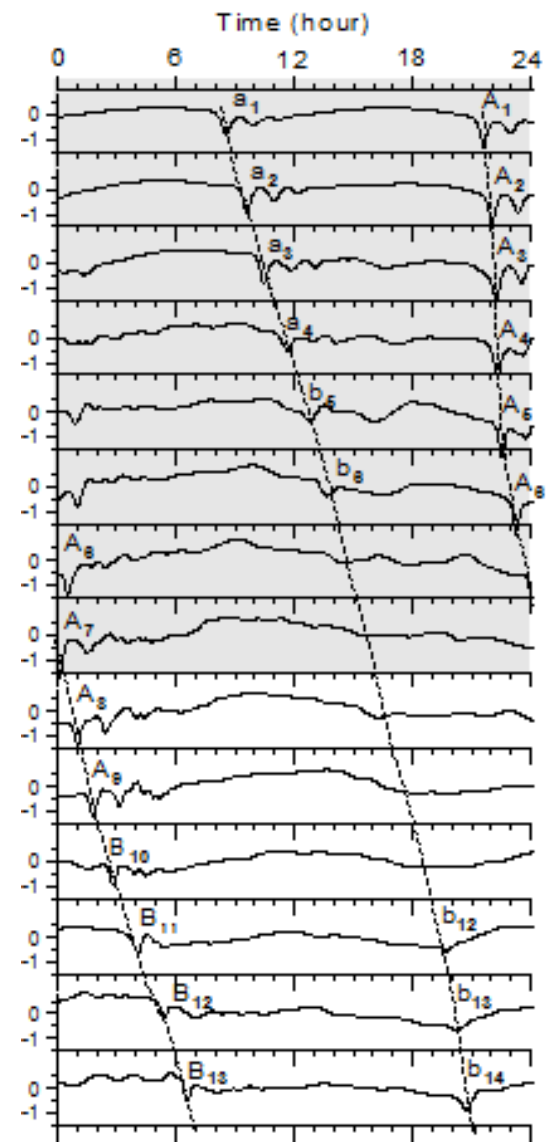
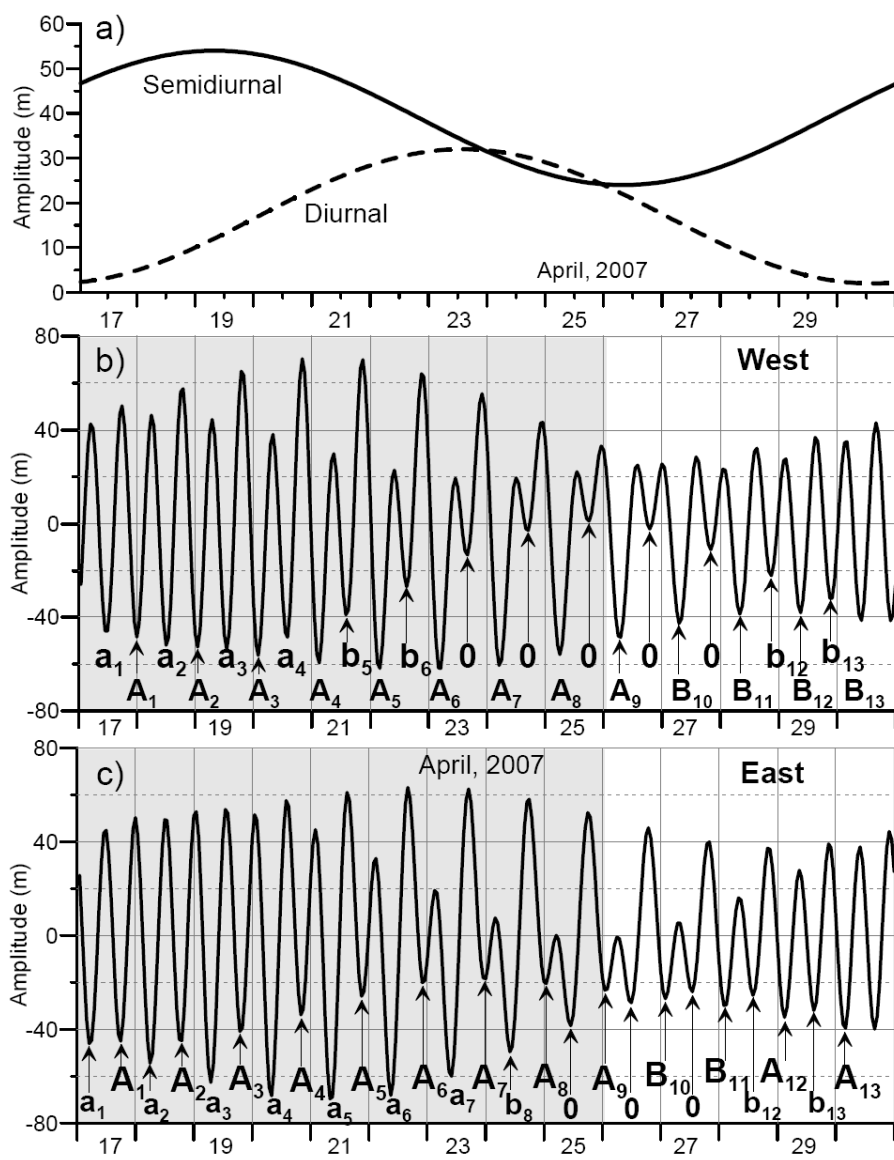
# Linear theory prediction for TWO tidal harmonics: semidiurnal and diurnal



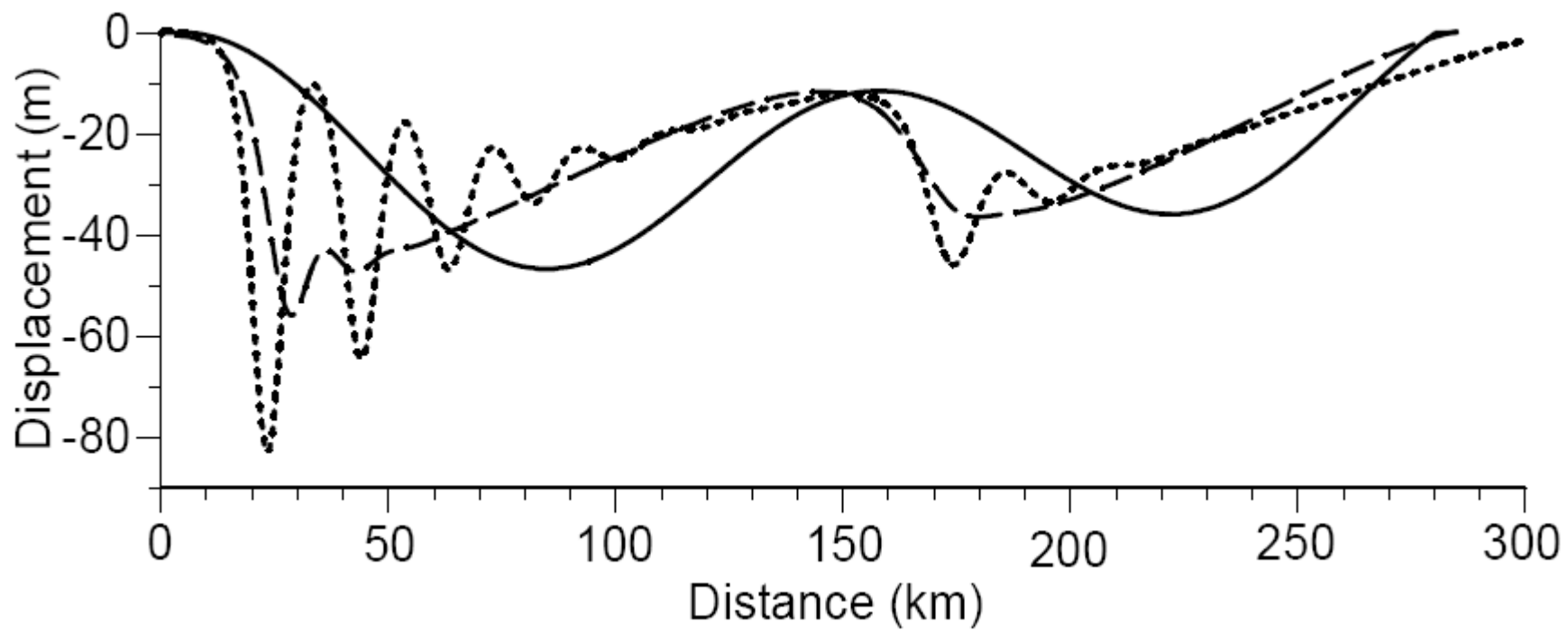
Tidal forcing  $Q$  - variable,  
ridge width  $2L=110\text{km}$  - constant.

# Superposition of TWO tidal harmonics: semidiurnal and diurnal

$$\zeta(x, z, t) = a_1^s g_1(z) \exp(k_1^s x - \sigma^s t + \varphi_1^s) + a_1^d g_1(z) \exp(k_1^d x - \sigma^d t + \varphi_1^d)$$



# Evolutionary mechanism: steepening and disintegration into ISWs



$$N < \frac{1}{2} \left[ \sqrt{1 + \frac{6a\epsilon(1 - 2\alpha)}{\nu^2\delta}} + 1 \right],$$

## 5. Conclusions

1. The amplitudes of ISWs is controlled by the intensity of semidiurnal tidal harmonics. Much stronger diurnal constituents do not reveal any substantial influence on the appearance of ISWs. This effect can be treated in terms of rotational dispersion.
2. The role of the diurnal tidal harmonics is in modulation of the generated internal waves. Diurnal periodicity is introduced into the ISW signal known as A and B waves. Appearance of A or B type waves is not directly linked to strong or weak tidal current peaks in the LS.
3. The MITgcm modelling shows that the number of ISWs in A and B wave packets varies with neap-spring periodicity with a gradual transition of A waves into B waves, and vice versa. The arrival time of A and B waves at observational point varies both for A and B packets depending on the forcing conditions in the LS.
4. The effect of A-B-A-B wave transition can be treated in terms of a multi-harmonic evolutionary mechanism. Generated in the LS semidiurnal and diurnal internal tidal harmonics freely radiate from the ridge. Being superimposed, these two progressive waves produce an intermittent baroclinic signal with large and small wave troughs alternating in space and time. In the course of nonlinear evolution these large and small wave troughs steepen and ultimately disintegrate into A and B wave packets.



